# Acoustic and Auditory Phonetics

KEITH JOHNSON





BLACKWELL PUBLISHING 350 Main Street, Malden, MA 02148-5020, USA 9600 Garsington Road, Oxford OX4 2DQ, UK 550 Swanston Street, Carlton, Victoria 3053, Australia

The right of Keith Johnson to be identified as the Author of this Work has been asserted in accordance with the UK Copyright, Designs, and Patents Act 1988.

All rights reserved. No part of this publication may be reproduced, stored in a retrieval system, or transmitted, in any form or by any means, electronic, mechanical, photocopying, recording or otherwise, except as permitted by the UK Copyright, Designs, and Patents Act 1988, without the prior permission of the publisher.

First edition published 1997 Second edition published 2003 by Blackwell Publishing Ltd

6 2006

Library of Congress Cataloging-in-Publication Data

Johnson, Keith, 1958– Acoustic and auditory phonetics / Keith Johnson.—2nd ed. p. cm. Includes bibliographical references and index. ISBN 1-4051-0122-9 (hb : alk. paper) — ISBN 1-4051-0123-7 (pb : alk. paper) 1. Phonetics, Acoustic. 2. Hearing. I. Title. P221.5 .J64 2003 414—dc21 2002026253

ISBN-13: 978-1-4051-0122-6 (hb : alk. paper) - ISBN-13: 978-1-4051-0123-3 (pb : alk. paper)

A catalogue record for this title is available from the British Library.

Set in 10/12.5pt Palatino by Graphicraft Ltd, Hong Kong Printed and bound in Singapore by C.O.S. Printers Pte Ltd

The publisher's policy is to use permanent paper from mills that operate a sustainable forestry policy, and which has been manufactured from pulp processed using acid-free and elementary chlorine-free practices. Furthermore, the publisher ensures that the text paper and cover board used have met acceptable environmental accreditation standards.

For further information on Blackwell Publishing, visit our website: www.blackwellpublishing.com

# Contents

viii

1

3

3

4

6

6

8

12 14

17

19 19

20

21

24

28 28

31

33

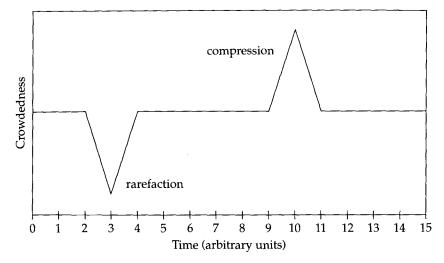
37

40 42

45

Acknowledgments											
In	trodu	action									
1	Bas	Basic Acoustics and Acoustic Filters									
	1.1	The sensation of sound									
	1.2	The propagation of sound									
	1.3	Types of sounds									
		1.3.1 Simple periodic waves									
	1.3.2 Complex periodic waves										
	1.3.3 Aperiodic waves										
	1.4 Acoustic filters										
	Exercises										
2	Digital Signal Processing										
	-	Continuous versus discrete signals									
		Analog-to-digital conversion									
		2.2.1 Sampling									
		2.2.2 Quantization									
	2.3	Signal analysis methods									
		2.3.1 Auto-correlation pitch tracking									
		2.3.2 RMS amplitude									
		2.3.3 Fast Fourier transform (FFT)									
		2.3.4 Digital filters									
		2.3.5 Linear predictive coding (LPC)									
		2.3.6 Spectra and spectrograms									

Exercises



**Figure 1.2** A pressure waveform of the wave motion shown in figure 1.1. Time is again shown on the horizontal axis. The vertical axis shows the distance between people.

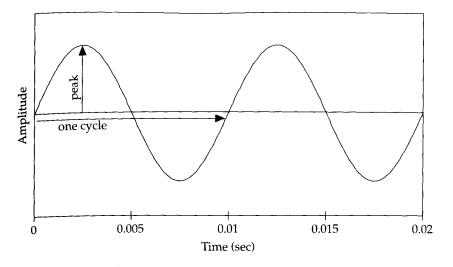
(the signal-to-noise ratio) may be difficult to detect if the movement is small. The rate of sound dissipation in air is different from the dissipation of a movement in a line, because sound radiates in three dimensions from the sound source (in a sphere). This means that the number of air molecules being moved by the sound wave greatly increases as the wave radiates from the sound source. Thus the amount of energy available to move the molecules (energy per unit surface area on the sphere) decreases as the wave expands out from the sound source, consequently the amount of particle movement decreases as a function of the distance from the sound source (by a power of 3). That is why singers in heavy metal bands put the microphone right up to their lips. They would be drowned out by the general din otherwise. It is also why you should position the microphone close to the speaker's mouth when you record a sample of speech (although it is important to keep the microphone to the side of the speaker's lips, to avoid the blowing noises in [p]'s, etc.).

## 1.3 Types of sounds

There are two types of sounds: periodic and aperiodic. Periodic sounds have a pattern that repeats at regular intervals. They come in two types: simple and complex.

#### 1.3.1 Simple periodic waves

Simple periodic waves are also called sine waves: they result from simple harmonic motion, such as the swing of a pendulum. The only time we humans get close to producing simple periodic waves in speech is when we're very young. Children's vocal cord vibration comes close to being sinusoidal, and usually women's vocal cord



**Figure 1.3** A 100 Hz sine wave with the duration of one cycle (the period) and the peak amplitude labeled.

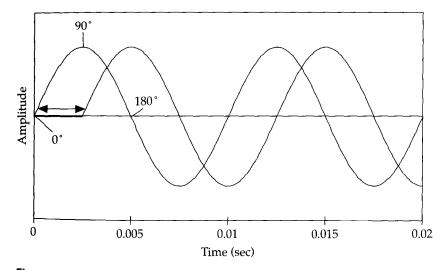


Figure 1.4 Two sine waves with identical frequency and amplitude, but 90° out of phase.

vibration is more sinusoidal than men's. Despite the fact that simple periodic waves rarely occur in speech, they are important, because more complex sounds can be described as combinations of sine waves. In order to define a sine wave, one needs to know just three properties. These are illustrated in figures 1.3–1.4.

The first is frequency: the number of times the sinusoidal pattern repeats per unit time (on the horizontal axis). Each repetition of the pattern is called a cycle, and the duration of a cycle is its period. Frequency can be expressed as cycles per second, which, by convention, is called hertz (and abbreviated Hz). So to get the frequency of a sine wave in Hz (cycles per second), you divide one second by the period (the duration of one cycle). That is, frequency in Hz equals 1/T, where T

8

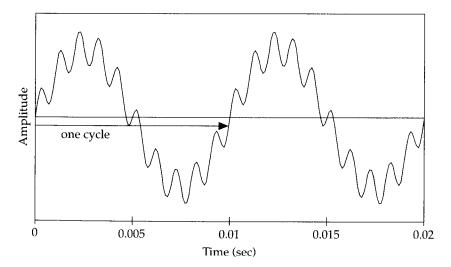
is the period in seconds. For example, the sine wave in figure 1.3 completes one cycle in 0.01 seconds. The number of cycles this wave could complete in one second is 100 (that is, one second divided by the amount of time each cycle takes in seconds, or 1/0.01 = 100). So, this waveform has a frequency of 100 cycles per second (100 Hz).

The second property of a simple periodic wave is its amplitude: the peak deviation of a pressure fluctuation from normal, atmospheric pressure. In a sound pressure waveform the amplitude of the wave is represented on the vertical axis.

The third property of sine waves is their phase: the timing of the waveform relative to some reference point. You can draw a sine wave by taking amplitude values from a set of right triangles that fit inside a circle (see exercise 4 at the end of this chapter). One time around the circle equals one sine wave on the paper. Thus we can identify locations in a sine wave by degrees of rotation around a circle. This is illustrated in figure 1.4. Both sine waves shown in this figure start at 0° in the sinusoidal cycle. In both, the peak amplitude occurs at 90°, the downward-going (negative-going) zero-crossing at 180°, the negative peak at 270°, and the cycle ends at 360°. But these two sine waves with exactly the same amplitude and frequency may still differ in terms of their relative timing, or phase. In this case they are 90° out of phase.

# 1.3.2 Complex periodic waves

Complex periodic waves are like simple periodic waves in that they involve a repeating waveform pattern and thus have cycles. However, complex periodic waves are composed of at least two sine waves. Consider the wave shown in figure 1.5, for example. Like the simple sine waves shown in figures 1.3 and 1.4, this waveform completes one cycle in 0.01 seconds (i.e. 10 milliseconds). However,



**Figure 1.5** A complex periodic wave composed of a 100 Hz sine wave and a 1,000 Hz sine wave. One cycle of the fundamental frequency ( $F_0$ ) is labeled.

it has an additional component that completes ten cycles in this same amount of time. Notice the "ripples" in the waveform. You can count ten small positive peaks in one cycle of the waveform, one for each cycle of the additional frequency component in the complex wave. I produced this example by adding a 100 Hz sine wave and a (lower-amplitude) 1,000 Hz sine wave. So the 1,000 Hz wave combined with the 100 Hz wave produces a complex periodic wave. The rate at which the complex pattern repeats is called the fundamental frequency (abbreviated  $F_0$ ).

# Fundamental frequency and the GCD

The wave shown in figure 1.5 has a fundamental frequency of 100 Hz and also a 100 Hz component sine wave. It turns out that the fundamental frequency of a complex wave is the greatest common denominator (GCD) of the frequencies of the component sine waves. For example, the fundamental frequency ( $F_0$ ) of a complex wave with 400 Hz and 500 Hz components is 100 Hz. You can see this for yourself if you draw the complex periodic wave that results from adding a 400 Hz sine wave and a 500 Hz sine wave. We will use the sine wave in figure 1.3 as the starting point for this graph. The procedure is as follows:

### 1 Take some graph paper.

**Calculate** the period of a 400 Hz sine wave. Because frequency is equal to one divided by the period (in math that's f = 1/T), we know that the period is equal to one divided by the frequency (T = 1/f). So the period of a 400 Hz sine wave is 0.0025 seconds. In milliseconds (1/1,000ths of a second) that's 2.5 ms (0.0025 times 1,000).

**3** Calculate the period of a 500 Hz sine wave.

Now we are going to derive two tables of numbers that constitute instructions for drawing 400 Hz and 500 Hz sine waves. To do this, add some new labels to the time axis on figure 1.3, once for the 400 Hz sine wave and once for the 500 Hz sine wave. The 400 Hz time axis will have 2.5 ms in place of 0.01 sec, because the 400 Hz sine wave completes one cycle in 2.5 ms. In place of 0.005 sec the 400 Hz time axis will have 1.25 ms. The peak of the 400 Hz sine wave occurs at 0.625 ms, and the valley at 1.875 ms. This gives us a table of times and amplitude values for the 400 Hz wave (where we assume that the amplitude of the peak is 1 and the amplitude of the valley is -1, and the amplitude value given for time 3.125 is the peak in the second cycle):

T	n	5	in in		Ş.	0			0.	62	25		1.	25		1.	87	75		2	5		3.1	25	
61	-	ηŗ	Ű.	1.2	73	n	6		1				n				1			ń			1		
	1015	•1	غ		đ.	v			1.				U			- Th	Ŀ			Ų			T.		

The interval between successive points in the waveform (with 90° between each point) is 0.625 ms. In the 500 Hz sine wave the interval between comparable points is 0.5 ms. 5 Now on your graph paper mark out 20 ms with 1 ms intervals. Also mark an amplitude scale from 1 to -1, allowing about an inch.

- 6 Draw the 400 Hz and 500 Hz sine waves by marking dots on the graph paper for the intersections indicated in the tables. For instance, the first dot in the 400 Hz sine wave will be at time 0 ms and amplitude 0, the second at time 0.625 ms and amplitude 1, and so on. Note that you may want to extend the table above to 20 ms (I stopped at 3.125 to keep the times right for the 400 Hz wave). When you have marked all the dots for the 400 Hz wave, connect the dots with a freehand sine wave. Then draw the 500 Hz sine wave in the same way, using the same time and amplitude axes. You should have a figure with overlapping sine waves something like figure 1.6.
- 7 Now add the two waves together. At each 0.5 ms point, take the sum of the amplitudes in the two sine waves to get the amplitude value of the new complex periodic wave, and then draw the smooth waveform by eye.

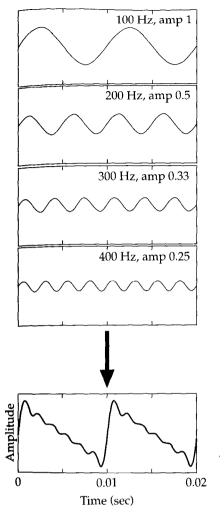
Take a look at the complex periodic wave that results from adding a 400 Hz sine wave and a 500 Hz sine wave. Does it have a fundamental frequency of 100 Hz? If it does, you should see two complete cycles in your 20 ms long complex wave; the waveform pattern from 10 ms to 20 ms should be an exact copy of the pattern that you see in the 0 ms to 10 ms interval.

Figure 1.6 shows another complex wave (and four of the sine waves that were added together to produce it). This wave shape approximates a sawtooth pattern. Unlike the previous example, it is not possible to identify the component sine waves by looking at the complex wave pattern. Notice how all four of the component sine waves have positive peaks early in the complex wave's cycle and negative peaks toward the end of the cycle. These peaks add together to produce a sharp peak early in the cycle and a sharp valley at the end of the cycle, and tend to cancel each other over the rest of the cycle. We can't see individual peaks corresponding to the cycles of the component waves. Nonetheless, the complex wave *was* produced by adding together simple components.

Now let's look at how to represent the frequency components that make up a complex periodic wave. What we're looking for is a way to show the component sine waves of the complex wave when they are not easily visible in the waveform itself. One way to do this is to list the frequencies and amplitudes of the component sine waves like this:

frequency (Hz)	100	200	300	400	500
amplitude	1	0.5	0.33	0.25	0.2

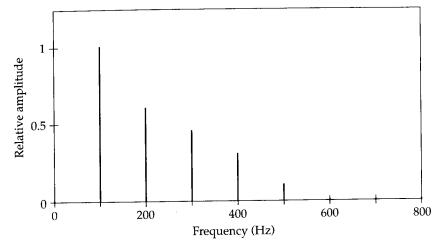
Figure 1.7 shows a graph of these values with frequency on the horizontal axis and amplitude on the vertical axis. The graphical display of component frequencies is the method of choice for showing the simple periodic components of a complex periodic wave, because complex waves are often composed of so many frequency



**Figure 1.6** A complex periodic wave that approximates the "sawtooth" wave shape, and the four lowest sine waves of the set that were combined to produce the complex wave.

**components** that a table is impractical. An amplitude versus frequency plot of the simple sine wave components of a complex wave is called a **power spectrum**.

Here's why it is so important that complex periodic waves can be constructed by adding together sine waves. It is possible to produce an infinite variety of complex wave shapes by combining sine waves that have different frequencies, amplitudes, and phases. A related property of sound waves is that any complex acoustic wave can be analyzed in terms of the sine wave components that could have been used to produce that wave. That is, any complex waveform can be decomposed into a set of sine waves having particular frequencies, amplitudes, and phase relations. This property of sound waves is called Fourier's theorem, after the seventeenth-century mathematician who discovered it.



**Figure 1.7** The frequencies and amplitudes of the simple periodic components of the complex wave shown in figure 1.6 presented in graphic format.

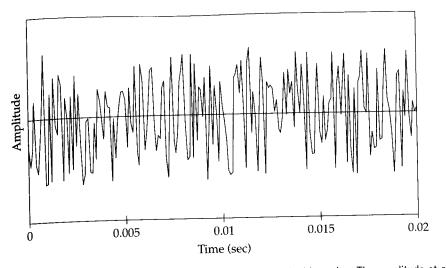
In Fourier analysis we take a complex periodic wave having an arbitrary number of components and derive the frequencies, amplitudes, and phases of those components. The result of Fourier analysis is a power spectrum similar to the one shown in figure 1.7. (We ignore the phases of the component waves, because these have only a minor impact on the perception of sound.)

### 1.3.3 Aperiodic waves

Aperiodic sounds, unlike simple or complex periodic sounds, do not have a regularly repeating pattern; they have either a random waveform or a pattern that doesn't repeat. Sound characterized by random pressure fluctuation is called "white noise." It sounds something like radio static or wind blowing through trees. Even though white noise is not periodic, it is possible to perform a Fourier analysis on it; however, unlike Fourier analyses of periodic signals composed of only a few sine waves, the spectrum of white noise is not characterized by sharp peaks, but, rather, has equal amplitude for all possible frequency components (the spectrum is flat). Like sine waves, white noise is an abstraction, although many naturally occurring sounds are similar to white noise. For instance, the sound of the wind or fricative speech sounds like [s] or [f].

Figures 1.8 and 1.9 show the acoustic waveform and the power spectrum, respectively, of a sample of white noise. Note that the waveform shown in figure 1.8 is irregular, with no discernible repeating pattern. Note too that the spectrum shown in figure 1.9 is flat across the top. As we noted earlier, a Fourier analysis of a short chunk (called an "analysis window") of a waveform leads to inaccuracies in the resultant spectrum. That's why this spectrum has some peaks and valleys even though, according to theory, white noise should have a flat spectrum.

The other main type of aperiodic sounds are **transients**. These are various types of clanks and bursts which produce a sudden pressure fluctuation that is not



**Figure 1.8** A 20 ms section of an acoustic waveform of white noise. The amplitude at any given point in time is random.

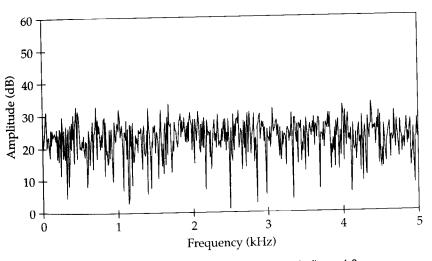


Figure 1.9 The power spectrum of the white noise shown in figure 1.8.

sustained or repeated over time. Door slams, balloon pops, and electrical clicks are all transient sounds. Like aperiodic noise, transient sounds can be analyzed into their spectral components using Fourier analysis. Figure 1.10 shows an idealized transient signal. At only one point in time is there any energy in the signal; at all other times pressure is equal to zero. This type of idealized sound is called an "impulse." Naturally occurring transients approximate the shape of an impulse, but usually with a bit more complicated fluctuation. Figure 1.11 shows the power spectrum of the impulse shown in figure 1.10. As with white noise, the spectrum is flat. This is more obvious in figure 1.11 than in figure 1.9 because the "impulseness" of the impulse waveform depends on only one point in time, while the "white noiseness"

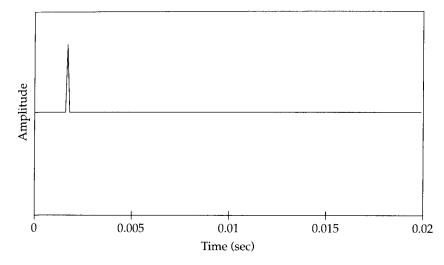


Figure 1.10 Acoustic waveform of a transient sound (an impulse).

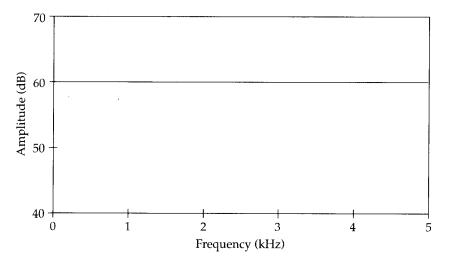


Figure 1.11 Power spectrum of the transient signal shown in figure 1.10.

of the white noise waveform depends on every point in time. Thus, because the Fourier analysis is only approximately valid for a short sample of a waveform, the white noise spectrum is not as completely specified as is the impulse spectrum.

#### 1.4 Acoustic filters

We are all familiar with how filters work. For example, you use a paper filter to keep the coffee grounds out of your coffee, or a tea ball to keep the tea leaves out of your tea. These everyday examples illustrate some important properties of acoustic filters. For instance, the practical difference between a coffee filter and a

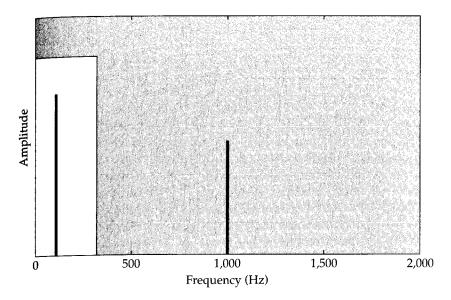


Figure 1.12 Illustration of the spectrum of a low-pass filter.

tea ball is that the tea ball will allow larger bits into the drink, while the coffee filter captures smaller particles than does the tea ball. So the difference between these filters can be described in terms of the size of particles they let pass.

Rather than passing or blocking particles of different sizes like a coffee filter, an acoustic filter passes or blocks components of sound of different frequencies. For example, a **low-pass** acoustic filter blocks the high-frequency components of a wave, and passes the low-frequency components. Earlier I illustrated the difference between simple and complex periodic waves by adding a 1,000 Hz sine wave to a 100 Hz sine wave to produce a complex wave. With a low-pass filter that, for instance, filtered out all frequency components above 300 Hz, we could remove the 1,000 Hz wave from the complex wave. Just as a coffee filter allows small particles to pass through and blocks large particles, so a low-pass acoustic filter allows low-frequency components through, but blocks high-frequency components.

You can visualize the action of a low-pass filter in a spectral display of the filter's response function. For instance, figure 1.12 shows a low-pass filter that has a cutoff frequency of 300 Hz. The part of the spectrum shaded white is called the **pass band**, because sound energy in this frequency range is passed by the filter, while the part of the spectrum shaded gray is called the **reject band**, because sound energy in this region is blocked by the filter. Thus, in a complex wave with components at 100 and 1,000 Hz, the 100 Hz component is passed, and the 1,000 Hz component is blocked. Similarly, a **high-pass** acoustic filter blocks the low-frequency components of a wave, and passes the high-frequency components. A spectral display of the response function of a high-pass filter shows that low-frequency components are blocked by the filter, and highfrequency components are passed.