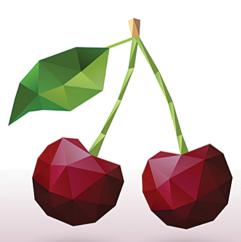
Elayn Martín-Gay

Basic College Mathematics



Sixth Edition



Basic College Mathematics This page intentionally left blank

Basic College Mathematics

Sixth Edition

Elayn Martín-Gay

University of New Orleans



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1 17



This book is dedicated to students everywhere and we should all be students. After all, is there anyone among us who truly knows too much? Take that hint and continue to learn something new every day of your life.

> Best wishes from a fellow student: Elayn Martin-Gay

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Preface

Basic College Mathematics, Sixth Edition, was written to provide students with a solid foundation in the basics of college mathematics, including the topics of whole numbers, fractions, decimals, ratio and proportion, percent, and measurement as well as introductions to geometry, statistics and probability, and algebra topics. To help students accomplish this solid foundation, my goals for this text are:

- Most importantly, to write an organized, student-friendly text that is keyed to objectives and contains many worked-out examples.
- To introduce operations on whole numbers in the first chapter and repeat these operations in each subsequent chapter while different sets of numbers are introduced, thus providing students with a solid foundation of the basics of college mathematics.
- To include a later chapter of introduction to algebra, thus laying the groundwork for the next algebra course your students will take.
- To show students the relevancy of mathematics in everyday life and in the workplace by emphasizing and integrating the following throughout this text: reallife and real-data applications, data interpretation, conceptual understanding, problem solving, writing, cooperative learning, number sense, estimation, critical thinking and geometric concepts.

The many factors that contributed to the success of the previous editions have been retained. In preparing the Sixth Edition, I considered comments and suggestions of colleagues, students, and many users of the prior edition throughout the country.

What's New in the Sixth Edition?

- **The Martin-Gay Program** has been revised and enhanced with a new design in the text and MyLab Math to actively encourage students to use the text, video program, and Video Organizer as an integrated learning system.
- New Getting Ready for the Test can be found before each Chapter Test. These exercises can increase student success by helping students prepare for their Chapter Test. The purpose of these exercises is to check students' conceptual understanding of the topics in the chapter as well as common student errors. It is suggested that students complete and check these exercises before taking a practice Chapter Test. All Getting Ready for the Test exercises are either Multiple Choice or Matching, and all answers can be found in the answer section of this text.

Video Solutions of all exercises can be found in MyLab Math. These video solutions contain brief explanations and reminders of material in the chapter. Where applicable, incorrect choices contain explanations.

Getting Ready for the Test exercise numbers marked in blue indicate that the exercise is available in Learning Catalytics. LC

- New Learning Catalytics is an interactive student response tool that uses students' smartphones, tablets, or laptops to engage them in more sophisticated tasks and thinking. Generate class discussion, guide your lecture, and promote peer-to-peer learning with real-time analytics. Accessible through MyLab Math, instructors can use Learning Catalytics to:
 - Pose a variety of open-ended questions that help your students develop critical thinking skills.
 - Monitor responses to find out where students are struggling.
 - Use real-time data to adjust your instructional strategy and try other ways of engaging your students during class.
 - Manage student interactions by automatically grouping students for discussion, teamwork, and peer-to-peer learning.

Preface

- Pearson-created questions for developmental math topics are available to allow you to take advantage of this exciting technology. Additionally, "Getting Ready for the Test" exercises (marked in blue) are available in Learning Catalytics. Search the question library for "MGBCM" and the chapter number, for example, MGBCM7 would be the questions from Chapter 7.
- **Revised and updated Key Concept Activity Lab Workbook** includes Extension Exercises, Exploration Activities, Conceptual Exercises, and Group Activities. These activities are a great way to engage students in conceptual projects and exploration as well as group work. This workbook is available in MyLab Math, or can be packaged with a text or MyLab code.
- **Exercise Sets** have been carefully examined and revised. Special focus was placed on making sure that even- and odd-numbered exercises are carefully paired and that real-life applications are updated.
- The Martin-Gay MyLab Math course has been updated and revised to provide more exercise coverage, including assignable Video Check questions and an expanded video program. There are Lecture Videos for every section, which students can also access at the specific objective level; Student Success Tips videos; and an increased number of video clips at the exercise level to help students while doing homework in MyLab Math. Suggested homework assignments have been premade for assignment at the instructor's discretion.

Key Continuing Resources and Pedagogical Features

- Vocabulary, Readiness & Video Check Questions continue to be available in the text and for assignment in MyLab Math. The Readiness exercises center on a student's understanding of a concept that is necessary in order to continue to the exercise set. The Video Check questions are included in every section for every learning objective. These exercises are a great way to assess whether students have viewed and understood the key concepts presented in the videos. Answers to all Video Check questions are available in an answer section at the back of the text.
- Interactive Lecture Series in MyLab Math, featuring author Elayn Martin-Gay, provides students with active learning at their own pace. The videos offer the following resources and more:

A complete lecture for each section of the text highlights key examples and exercises from the text. Pop-ups reinforce key terms, definitions, and concepts.

An interface with menu navigation features allows students to quickly find and focus on the examples and exercises they need to review.

Interactive Concept Check exercises measure students' understanding of key concepts and common trouble spots.

Student Success Tips Videos are 3-5 minute videos designed to be daily reminders to students to continue practicing and maintaining good organizational and study habits. They include student success tips for general college success, tips specific to success in math courses, and content-specific tips to avoid common mathematical mistakes.

• The Interactive Lecture Series also includes the following resources for test prep:

New Getting Ready for the Test Videos

The Chapter Test Prep Videos help students during their most teachable moment—when they are preparing for a test. This innovation provides stepby-step solutions for the exercises found in each Chapter Test. For the Sixth Edition, the Chapter Test Prep Videos are also available on YouTubeTM. The videos are captioned in English and Spanish.

The Practice Final Exam Videos help students prepare for an end-of-course final. Students can watch full video solutions to each exercise in the Practice Final Exam at the end of this text.

- The Video Organizer helps students take notes and work practice exercises while watching the Interactive Lecture Series videos in their MyLab Math course. All content in the Video Organizer is presented in the same order as it is presented in the videos, making it easy for students to create a course notebook and build good study habits.
 - Covers all of the video examples in order.
 - Provides prompts with ample space for students to write down key definitions and properties.
 - Includes Play and Pause button icons to prompt students to follow along with the author for some exercises while they try others on their own.

The Video Organizer is available in a loose-leaf, notebook-ready format. It is also available for download in MyLab Math.

Key Pedagogical Features

The following key features have been retained and/or updated for the Sixth Edition of the text:

- **Problem-Solving Process** This is formally introduced in Chapter 1 with a four-step process that is integrated throughout the text. The four steps are **Understand, Translate, Solve, and Interpret.** The repeated use of these steps in a variety of examples shows their wide applicability. Reinforcing the steps can increase students' comfort level and confidence in tackling problems.
- Exercise Sets Revised and Updated The exercise sets have been carefully examined and extensively revised. Special focus was placed on making sure that even- and odd-numbered exercises are paired and that real-life applications were updated.
- **Examples** Detailed, step-by-step examples were added, deleted, replaced, or updated as needed. Many examples reflect real life. Additional instructional support is provided in the annotated examples.
- **Practice Exercises** Throughout the text, each worked-out example has a parallel Practice exercise. These invite students to be actively involved in the learning process. Students should try each Practice exercise after finishing the corresponding example. Learning by doing will help students grasp ideas before moving on to other concepts. Answers to the Practice exercises are provided at the bottom of each page.
- **Helpful Hints** Helpful Hints contain practical advice on applying mathematical concepts. Strategically placed where students are most likely to need immediate reinforcement, Helpful Hints help students avoid common trouble areas and mistakes.
- **Concept Checks** This feature allows students to gauge their grasp of an idea as it is being presented in the text. Concept Checks stress conceptual understanding at the point-of-use and help suppress misconceived notions before they start. Answers appear at the bottom of the page. Exercises related to Concept Checks are included in the exercise sets.
- **Mixed Practice Exercises** In the section exercise sets, these exercises require students to determine the problem type and strategy needed to solve it just as they would need to do on a test.
- **Integrated Reviews** This unique, mid-chapter exercise set helps students assimilate new skills and concepts that they have learned separately over several sections. These reviews provide yet another opportunity for students to work with "mixed" exercises as they master the topics.
- Vocabulary Check This feature provides an opportunity for students to become more familiar with the use of mathematical terms as they strengthen their verbal skills. These appear at the end of each chapter before the Chapter Highlights. Vocabulary, Readiness & Video exercises provide practice at the section level.

Preface

- **Chapter Highlights** Found at the end of every chapter, these contain key definitions and concepts with examples to help students understand and retain what they have learned and help them organize their notes and study for tests.
- **Chapter Review** The end of every chapter contains a comprehensive review of topics introduced in the chapter. The Chapter Review offers exercises keyed to every section in the chapter, as well as Mixed Review exercises that are not keyed to sections.
- Chapter Test and Chapter Test Prep Videos The Chapter Test is structured to include those problems that involve common student errors. The Chapter Test Prep Videos gives students instant access to a step-by-step video solution of each exercise in the Chapter Test.
- **Cumulative Review** This review follows every chapter in the text (except Chapter 1). Each odd-numbered exercise contained in the Cumulative Review is an earlier worked example in the text that is referenced in the back of the book along with the answer.
- Writing Exercises \ These exercises occur in almost every exercise set and require students to provide a written response to explain concepts or justify their thinking.
- **Applications** Real-world and real-data applications have been thoroughly updated, and many new applications are included. These exercises occur in almost every exercise set and show the relevance of mathematics and help students gradually and continuously develop their problem-solving skills.
- **Review Exercises** These exercises occur in each exercise set (except in Chapter 1) and are keyed to earlier sections. They review concepts learned earlier in the text that will be needed in the next section or chapter.
- **Exercise Set Resource Icons** Located at the opening of each exercise set, these icons remind students of the resources available for extra practice and support:



See Student Resources descriptions on page xvii for details on the individual resources available.

Exercise lcons These icons facilitate the assignment of specialized exercises and let students know what resources can support them.

- Video icon: exercise worked in the Interactive Lecture Series found in MyLab Math.
- \triangle Triangle icon: identifies exercises involving geometric concepts.
- Pencil icon: indicates a written response is needed.
- Calculator icon: optional exercises intended to be solved using a scientific or graphing calculator.

Group Activities Found at the end of each chapter, these activities are for individual or group completion, and are usually hands-on or data-based activities that extend the concepts found in the chapter, allowing students to make decisions and interpretations and to think and write about algebra.

Optional: Calculator Exploration Boxes and Calculator Exercises The optional Calculator Explorations provide keystrokes and exercises at appropriate places to give students an opportunity to become familiar with these tools. Section exercises that are best completed by using a calculator are identified by for ease of assignment.

Student and Instructor Resources

STUDENT RESOURCES

Video Organizer

Designed to help students take notes and work practice exercises while watching the Interactive Lecture Series videos.

- Covers all of the video examples in order.
- Provides prompts with ample space for students to write down key definitions and rules.
- Includes "Play" and "Pause" button icons to prompt students to follow along with the author for some exercises while they try others on their own.
- Includes Student Success Tips Outline and Questions

Available in loose-leaf, notebook-ready format and in MyLab Math.

Key Concept Activity Lab Workbook

Includes Extension Exercises, Exploration Activities, Conceptual Exercises, and Group Activities. This workbook is available in MyLab Math, or can be packaged in printed form with a text or MyLab Math code.

Student Solutions Manual

Provides completely worked-out solutions to the odd-numbered section exercises; all exercises in the Integrated Reviews, Chapter Reviews, Chapter Tests, and Cumulative Reviews.

Annotated Instructor's Edition Contains all the content found in the student edition, plus the following:	Instructor's Resource Manual with Tests and Mini-Lectures This resource includes:
 Answers to even and odd exercises on the same text page Teaching Tips throughout the text placed at key points 	 Mini-lectures for each text section Additional practice worksheets for each section Several forms of tests per chapter—free response and multiple choice Answers to all items
	Instructor's Solutions Manual TestGen [®]
	(These resources are available for download from MyLab Math or from the Instructor's Resource Center on pear- son.com.)
Instructor-to-Instructor Videos —available in the Instructor Resources section of the MyLab Math course.	Online Resources MyLab Math (access code required)
	MathXL [®] (access code required)

INSTRUCTOR RESOURCES

Resources for Success

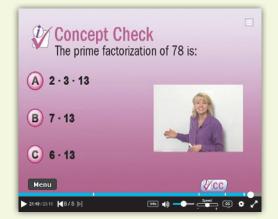


Get the Most Out of MyLab Math for Basic College Mathematics, Sixth Edition by Elayn Martin-Gay

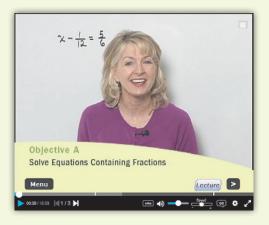
Elayn Martin-Gay believes that every student can succeed, and each MyLab course that accompanies her texts is infused with her student-centric approach. The seamless integration of Elayn's award-winning content with the #1 choice in digital learning for developmental math gives students a completely consistent experience from print to MyLab.

A Comprehensive and Dynamic Video Program

The **Martin-Gay video program** is 100% presented by Elayn Martin-Gay to ensure consistency with the text. The video program includes full section lectures and shorter objective level videos, and an intuitive navigation menu and pop-ups that reinforce key definitions.



All videos can be assigned as a **media** assignment in the Assignment Manager, to ensure that students are getting the most out of their MyLab resources. Additionally, **Video Check questions** ensure that students have viewed and understood the key concepts from the section lecture videos.



Within the section lecture videos, Interactive Concept Checks measure a student's understanding of key concepts and common trouble spots. Concept Checks ask students to try a question on their own within the video, after which Elayn Martin-Gay explains why they were correct or incorrect.

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All parts showing	Clear All	Final Check

Additional hallmark Martin-Gay video types include Student Success Tip videos and Chapter Test Prep videos. **Student Success Tip videos** are in short segments designed to be daily reminders to stay organized and to study. **Chapter Test Prep videos**, a Martin-Gay innovation, help students during their most teachable moment–when they are preparing for a test–with step-bystep solutions for the exercises in the Chapter Test.

New Tools Improve Preparedness and Personalize Learning

New! Getting Ready for the Test video solutions cover every Getting Ready for the Test exercise. These come at the end of each chapter to give students an opportunity to assess if they understand the big picture concepts of the chapter, and help them focus on avoiding common errors.

New! Skill Builder exercises offer just-in-time additional adaptive practice. The adaptive engine tracks student performance and delivers questions to each individual that adapt to his or her level of understanding. This new feature allows instructors to assign fewer questions for homework, allowing students to complete as many or as few questions needed.

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New Ways to Engage Students

New! Learning Catalytics

Martin-Gay-specific questions are pre-built and available through MyLab Math. Learning Catalytics is an interactive student response tool that uses students' smartphones, tablets, or laptops to engage them in more sophisticated tasks and thinking. **Getting Ready for the Test** exercises marked in blue in the text are pre-built in Learning Catalytics to use in class. These questions can be found in Learning Catalytics by searching for "MGBCM".

New! Vocab and Readiness questions in MyLab Math have been expanded to 100% coverage, and are now available with a new **Drag and Drop functionality!** Drag and Drop exercises allow students to manually select elements of the question, such as expressions, words, graphs, or images, and place them into a designated target area.

Easier Start-Up for Instructors

Enhanced Sample Assignments make course set-up easier by giving instructors a starting point for each section. Each assignment has been carefully curated for this specific text, and includes a thoughtful mix of question types.

pearson.com/mylab/math

Preface

Acknowledgments

There are many people who helped me develop this text, and I will attempt to thank some of them here. Cindy Trimble was *invaluable* for contributing to the overall accuracy of the text. Gina Linko and Patty Bergin provided guidance throughout the production process and Suellen Robinson provided many suggestions for updating applications during the writing of this Sixth Edition.

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Elayn Martín-Gay

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About the Author

Elayn Martin-Gay has taught mathematics at the University of New Orleans for more than 25 years. Her numerous teaching awards include the local University Alumni Association's Award for Excellence in Teaching, and Outstanding Developmental Educator at University of New Orleans, presented by the Louisiana Association of Developmental Educators.

Prior to writing textbooks, Elayn Martin-Gay developed an acclaimed series of lecture videos to support developmental mathematics students in their quest for success. These highly successful videos originally served as the foundation material for her texts. Today, the videos are specific to each book in the Martin-Gay series. The author has also created Chapter Test Prep Videos to help students during their most "teachable moment"—as they prepare for a test—along with Instructor-to-Instructor videos that provide teaching tips, hints, and suggestions for each developmental mathematics course, including basic mathematics, prealgebra, beginning algebra, and intermediate algebra.

Elayn is the author of 12 published textbooks as well as multimedia, interactive mathematics, all specializing in developmental mathematics courses. She has also published series in Algebra 1, Algebra 2, and Geometry. She has participated as an author across the broadest range of educational materials: textbooks, videos, tutorial software, and courseware. This provides an opportunity of various combinations for an integrated teaching and learning package offering great consistency for the student.

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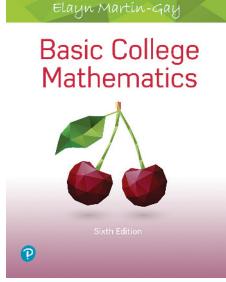
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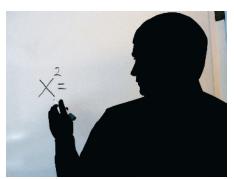
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The Whole Numbers

A Selection of Resources for Success in This Mathematics Course



Textbook



Instructor

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MyLab Math and MathXL



Video Organizer



Interactive Lecture Series

or more information about the resources illustrated above, read Section 1.1.

Whole numbers are the basic building blocks of mathematics. The whole numbers answer the question "How many?"

This chapter covers basic operations on whole numbers. Knowledge of these operations provides a good foundation on which to build further mathematical skills.

Sections

- **1.1** Study Skill Tips for Success in Mathematics
- **1.2** Place Value, Names for Numbers, and Reading Tables
- **1.3** Adding Whole Numbers and Perimeter
- 1.4 Subtracting Whole Numbers
- **1.5** Rounding and Estimating
- 1.6 Multiplying Whole Numbers and Area
- **1.7** Dividing Whole Numbers

Integrated Review— Operations on Whole Numbers

- **1.8** An Introduction to Problem Solving
- 1.9 Exponents, Square Roots, and Order of Operations

Check Your Progress

Vocabulary Check Chapter Highlights Chapter Review Getting Ready for the Test Chapter Test

1.1 Study Skill Tips for Success in Mathematics

Objectives

- A Get Ready for This Course.
- B Understand Some General Tips for Success.
- C Know How to Use This Text. D
- D Know How to Use Text Resources.
- E Get Help as Soon as You Need It.
- F Learn How to Prepare for and Take an Exam.
- G Develop Good Time Management.

Helpful

MyLab Math and MathXL

When assignments are turned in online, keep a hard copy of your complete written work. You will need to refer to your written work to be able to ask questions and to study for tests later.

Before reading this section, ask yourself a few questions.

- 1. Were you satisfied—really satisfied—with your performance in your last math course? In other words, do you feel that your outcome represented your best effort?
- 2. When you took your last math course, were your notes and materials from that course organized and easy to find, or were they disorganized and hard to find—if you saved them at all?

If the answer is "no" to these questions, then it is time to make a change. To begin, continue reading this section.

Objective 🗛 Let's Get Ready for This Course 💟

1. Start With a Positive Attitude. 🙂

Now that you have decided to take this course, remember that a *positive attitude* will make all the difference in the world. Your belief that you can succeed is just as important as your commitment to this course. Make sure you are ready for this course by having the time and positive attitude that it takes to succeed.

2. Understand How Your Course Material Is Presented—Lecture by Instructor, Online With Computer, or Both?

Make sure that you are familiar with the way that this course is being taught. Is it a traditional course, in which you have a printed textbook and meet with an instructor? Is it taught totally online, and your textbook is electronic and you e-mail your instructor? Or is your course structured somewhere in between these two methods? (Not all of the tips that follow will apply to all forms of instruction.)

3. Schedule Your Class So That It Does Not Interfere With Other Commitments.

Make sure that you have scheduled your math course for a time that will give you the best chance for success. For example, if you are also working, you may want to check with your employer to make sure that your work hours will not conflict with your course schedule.

Objective **B** Here are a Few General Tips for Success 🕑

Below are some general tips that will increase your chance for success in a mathematics class. Many of these tips will also help you in other courses you may be taking.

1. Most Important! Organize Your Class Materials. Unless Told Otherwise, Use a 3-Ring Binder Solely for Your Mathematics Class.

In the next couple pages, many ideas will be presented to help you organize your class materials—notes, any handouts, completed homework, previous tests, etc. In general, you MUST have these materials organized. All of them will be valuable references throughout your course and when studying for upcoming tests and the final exam. One way to make sure you can locate these materials when you need them is to use a three-ring binder. This binder should be used solely for your mathematics class and should be brought to each and every class or lab. This way, any material can be immediately inserted in a section of this binder and will be there when you need it.

2. Choose to attend all class periods.

If possible, sit near the front of the classroom. This way, you will see and hear the presentation better. It may also be easier for you to participate in classroom activities.

3. Complete Your Homework. This Means: Attempt All of It, Check All of It, Correct Any Mistakes, and Ask for Help if Needed.

You've probably heard the phrase "practice makes perfect" in relation to music and sports. It also applies to mathematics. You will find that the more time you spend solving mathematics exercises, the easier the process becomes. Be sure to schedule enough time to complete your assignments before the due date assigned by your instructor.

Review the steps you took while working a problem. Learn to check your answers in the original exercises. You may also compare your answers with the "Answers to Selected Exercises" section in the back of the book. If you have made a mistake, try to figure out what went wrong. Then correct your mistake. If you can't find what went wrong, **don't** erase your work or throw it away. Show your work to your instructor, a tutor in a math lab, or a classmate. It is easier for someone to find where you had trouble if he or she looks at your original work.

It's all right to ask for help. In fact, it's a good idea to ask for help whenever there is something that you don't understand. Make sure you know when your instructor has office hours and how to find his or her office. Find out whether math tutoring services are available on your campus. Check on the hours, location, and requirements of the tutoring service.

4. Learn from your mistakes and be patient with yourself.

Everyone, even your instructor, makes mistakes. (That definitely includes me— Elayn Martin-Gay.) Use your errors to learn and to become a better math student. The key is finding and understanding your errors.

Was your mistake a careless one, or did you make it because you can't read your own math writing? If so, try to work more slowly or write more neatly and make a conscious effort to carefully check your work.

Did you make a mistake because you don't understand a concept? Take the time to review the concept or ask questions to better understand it.

Did you skip too many steps? Skipping steps or trying to do too many steps mentally may lead to preventable mistakes.

5. Turn in assignments on time.

This way, you can be sure that you will not lose points for being late. Show every step of a problem and be neat and organized. Also be sure that you understand which problems are assigned for homework. If allowed, you can always double-check the assignment with another student in your class.

Objective C Knowing and Using Your Text or e-Text 🕑

Flip through the pages of this text or view the e-text pages on a computer screen. Start noticing examples, exercise sets, end-of-chapter material, and so on. Learn the way this text is organized by finding an example in your text of each type of resource listed below. Finding and using these resources throughout your course will increase your chance of success.

- *Practice Exercises.* Each example in every section has a parallel Practice exercise. Work each Practice exercise after you've finished the corresponding example. Answers are at the bottom of the page. This "learn-by-doing" approach will help you grasp ideas before you move on to other concepts.
- Objectives. Every section of this text is divided into objectives, such as A or B. They are listed at the beginning of the section and noted in that section. The main section of exercises in each exercise set is also referenced by an objective, such as A or B, and also an example(s). There is also often a section of exercises entitled "Mixed Practice," which is referenced by two or more objectives or sections. These are mixed exercises written to prepare you for your next exam. Use all of this referencing if you have trouble completing an assignment from the exercise set.

Helpful Hint

MyLab Math and MathXL If you are doing your homework online, you can work and re-work those exercises that you struggle with until you master them. Try working through all the assigned exercises twice before the due date.



MyLab Math and MathXL If you are completing your homework online, it's important to work each exercise on paper before submitting the answer. That way, you can check your work and follow your steps to find and correct any mistakes.

Helpful Hint

MyLab Math and MathXL Be aware of assignments and due dates set by your instructor. Don't wait until the last minute to submit work online.

- *Icons (Symbols).* Make sure that you understand the meaning of the icons that are beside many exercises. tells you that the corresponding exercise may be viewed on the video Lecture Series that corresponds to that section. ▲ tells you that this exercise is a writing exercise in which you should answer in complete sentences. △ tells you that the exercise involves geometry.
- *Integrated Reviews.* Found in the middle of each chapter, these reviews offer you a chance to practice—in one place—the many concepts that you have learned separately over several sections.
- *End-of-Chapter Opportunities.* There are many opportunities at the end of each chapter to help you understand the concepts of the chapter.

Vocabulary Checks contain key vocabulary terms introduced in the chapter.

Chapter Highlights contain chapter summaries and examples.

Chapter Reviews contain review problems. The first part is organized section by section and the second part contains a set of mixed exercises.

Getting Ready for the Tests are multiple choice or matching exercises designed to check your knowledge of chapter concepts, before you attempt the chapter test. Video solutions are available for all these exercises.

Chapter Tests are sample tests to help you prepare for an exam. The Chapter Test Prep Videos found in MyLab Math and YouTube provide the video solution to each question on each Chapter Test.

Cumulative Reviews start at Chapter 2 and are reviews consisting of material from the beginning of the book to the end of that particular chapter.

• *Student Resources in Your Textbook.* You will find a **Student Resources** section at the back of this textbook. It contains the following to help you study and prepare for tests:

Study Skill Builders contain study skills advice. To increase your chance for success in the course, read these study tips, and answer the questions.

Bigger Picture – Study Guide Outline provides you with a study guide outline of the course, with examples.

Practice Final provides you with a Practice Final Exam to help you prepare for a final.

• **Resources to Check Your Work.** The **Answers to Selected Exercises** section provides answers to all odd-numbered section exercises and to all integrated review, chapter review, getting ready for the test, chapter test, and cumulative review exercises. Use the **Solutions to Selected Exercises** to see the worked-out solution to every other odd-numbered exercise in the section exercises and chapter tests.

Objective D Knowing and Using Video and Notebook Organizer Resources

Video Resources

Below is a list of video resources that are all made by me—the author of your text, Elayn Martin-Gay. By making these videos, I can be sure that the methods presented are consistent with those in the text. All video resources may be found in MyLab Math and some also on YouTube.

- *Interactive Video Lecture Series.* Exercises marked with a are fully worked out by the author. The lecture series provides approximately 20 minutes of instruction per section and is organized by Objective.
- *Getting Ready for the Test Videos.* These videos provide solutions to all of the Getting Ready for the Test exercises.



In MyLab Math, you have access to the following video resources:

- Lecture Videos for each section
- Getting Ready for the Test Videos
- Chapter Test Prep Videos
- Final Exam Videos

Use these videos provided by the author to prepare for class, review, and study for tests.

- *Chapter Test Prep Videos.* These videos provide solutions to all of the Chapter Test exercises worked out by the author. They can be found in MyLab Math and YouTube. This supplement is very helpful before a test or exam.
- *Tips for Success in Mathematics.* These video segments are about 3 minutes long and are daily reminders to help you continue practicing and maintaining good organizational and study habits.
- *Final Exam Videos.* These video segments provide solutions to each question.

Video Organizer

This organizer is in three-ring notebook ready form. It is to be inserted in a three-ring binder and completed. This organizer is numbered according to the sections in your text to which it refers.

It is closely tied to the Interactive (Video) Lecture Series. Each section should be completed while watching the lecture video on the same section. Once completed, you will have a set of notes to accompany the (Video) Lecture Series section by section.

Objective 🗉 Getting Help 🜔

If you have trouble completing assignments or understanding the mathematics, get help as soon as you need it! This tip is presented as an objective on its own because it is so important. In mathematics, usually the material presented in one section builds on your understanding of the previous section. This means that if you don't understand the concepts covered during a class period, there is a good chance that you will not understand the concepts covered during the next class period. If this happens to you, get help as soon as you can.

Where can you get help? Try your instructor, a tutoring center, or a math lab, or you may want to form a study group with fellow classmates. If you do decide to see your instructor or go to a tutoring center, make sure that you have a neat notebook and are ready with your questions.

Objective F Preparing for and Taking an Exam 🕑

Make sure that you allow yourself plenty of time to prepare for a test. If you think that you are a little "math anxious," it may be that you are not preparing for a test in a way that will ensure success. The way that you prepare for a test in mathematics is important. To prepare for a test:

- 1. Review your previous homework assignments.
- **2.** Review any notes from class and section-level quizzes you have taken. (If this is a final exam, also review chapter tests you have taken.)
- **3.** Review concepts and definitions by reading the Chapter Highlights at the end of each chapter.
- **4.** Practice working out exercises by completing the Chapter Review found at the end of each chapter. (If this is a final exam, go through a Cumulative Review. There is one found at the end of each chapter except Chapter 1. Choose the review found at the end of the latest chapter that you have covered in your course.) *Don't stop here!*
- **5.** Take the Chapter Getting Ready for the Test. All answers to these exercises are available to you as well as video solutions.
- **6.** Take a sample test with no notes, etc, available for help. It is important that you place yourself in conditions similar to test conditions to find out how you

Helpful Hint and MathXL

- Use the **Help Me Solve This** button to get stepby-step help for the exercise you are working. You will need to work an additional exercise of the same type before you can get credit for having worked it correctly.
- Use the **Video** button to view a video clip of the author working a similar exercise.

Helpful

MyLab Math and MathXL Review your written work for previous assignments. Then, go back and re-work previous assignments. Open a previous assignment, and click Similar Exercise to generate new exercises. Re-work the exercises until you fully understand them and can work them without help features. will perform. There is a Chapter Test available at the end of each chapter, or you can work selected problems from the Chapter Review. Your instructor may also provide you with a review sheet. Then check your sample test. If your sample test is the Chapter Test in the text, don't forget that the video solutions are in MyLab Math and YouTube.

7. On the day of the test, allow yourself plenty of time to arrive at where you will be taking your exam.

When taking your test:

- 1. Read the directions on the test carefully.
- **2.** Read each problem carefully as you take the test. Make sure that you answer the question asked.
- **3.** Watch your time and pace yourself so that you can attempt each problem on your test.
- 4. If you have time, check your work and answers.
- **5.** Do not turn your test in early. If you have extra time, spend it double-checking your work.

Objective G Managing Your Time 💟

As a college student, you know the demands that classes, homework, work, and family place on your time. Some days you probably wonder how you'll ever get everything done. One key to managing your time is developing a schedule. Here are some hints for making a schedule:

- 1. Make a list of all of your weekly commitments for the term. Include classes, work, regular meetings, extracurricular activities, etc. You may also find it help-ful to list such things as laundry, regular workouts, grocery shopping, etc.
- 2. Next, estimate the time needed for each item on the list. Also make a note of how often you will need to do each item. Don't forget to include time estimates for the reading, studying, and homework you do outside of your classes. You may want to ask your instructor for help estimating the time needed.
- **3.** In the exercise set that follows, you are asked to block out a typical week on the schedule grid given. Start with items with fixed time slots like classes and work.
- **4.** Next, include the items on your list with flexible time slots. Think carefully about how best to schedule items such as study time.
- 5. Don't fill up every time slot on the schedule. Remember that you need to allow time for eating, sleeping, and relaxing! You should also allow a little extra time in case some items take longer than planned.
- 6. If you find that your weekly schedule is too full for you to handle, you may need to make some changes in your workload, classload, or other areas of your life. You may want to talk to your advisor, manager or supervisor at work, or someone in your college's academic counseling center for help with such decisions.



1.1 Exercise Set MyLab Math

- **1.** What is your instructor's name?
- **3.** What is the best way to contact your instructor?
- **5.** Will your instructor allow you to use a calculator in this class?
- **7.** Is there a tutoring service available on campus? If so, what are its hours? What services are available?
- **9.** List some steps that you can take if you begin having trouble understanding the material or completing an assignment. If you are completing your homework in MyLab Math and MathXL, list the resources you can use for help.
- **11.** What does the i icon in this text mean?
- **13.** What does the \bigcirc icon in this text mean?
- **15.** When might be the best time to work a Practice exercise?
- **17.** What answers are contained in this text and where are they?
- **19.** What and where are Integrated Reviews?
- **21.** How far in advance of the assigned due date is it suggested that homework be submitted online? Why?
- **23.** Chapter Reviews are found at the end of each chapter. Find the Chapter 1 Review and explain how you might use it and how it might be helpful.
- **25.** What is the Video Organizer? Explain the contents and how it might be used.

- **2.** What are your instructor's office location and office hours?
- **4.** Do you have the name and contact information of at least one other student in class?
- **6.** Why is it important that you write step-by-step solutions to homework exercises and keep a hard copy of all work submitted?
- **8.** Have you attempted this course before? If so, write down ways that you might improve your chances of success during this attempt.
- **10.** How many hours of studying does your instructor advise for each hour of instruction?
- **12.** What does the \triangle icon in this text mean?
- **14.** Search the minor columns in your text. What are Practice exercises?
- **16.** Where are the answers to Practice exercises?
- **18.** What are Tips for Success in Mathematics and where are they located?
- **20.** How many times is it suggested that you work through the homework exercises in MyLab Math or MathXL before the submission deadline?
- **22.** Chapter Highlights are found at the end of each chapter. Find the Chapter 1 Highlights and explain how you might use it and how it might be helpful.
- **24.** Chapter Tests are found at the end of each chapter. Find the Chapter 1 Test and explain how you might use it and how it might be helpful when preparing for an exam on Chapter 1. Include how the Chapter Test Prep Videos may help. If you are working in MyLab Math and MathXL, how can you use previous homework assignments to study?
- **26.** Read or reread objective **G** and fill out the schedule grid on the next page.

	Monday	Tuesday	Wednesday	Thursday	Friday	Saturday	Sunday
4:00 a.m.							
5:00 a.m.							
6:00 a.m.							
7:00 a.m.							
8:00 a.m.							
9:00 a.m.							
10:00 a.m.							
11:00 a.m.							
12:00 p.m.							
1:00 p.m.							
2:00 p.m.							
3:00 p.m.							
4:00 p.m.							
5:00 p.m.							
6:00 p.m.							
7:00 p.m.							
8:00 p.m.							
9:00 p.m.							
10:00 p.m.							
11:00 p.m.							
Midnight							
1:00 a.m.							
2:00 a.m.							
3:00 a.m.							

1.2 Place Value, Names for Numbers, and Reading Tables

Objectives

- A Find the Place Value of a Digit in a Whole Number.
- B Write a Whole Number in Words and in Standard Form.
- C Write a Whole Number in Expanded Form.
- D Read Tables. 🜔

The **digits** 0, 1, 2, 3, 4, 5, 6, 7, 8, and 9 can be used to write numbers. For example, the **whole numbers** are

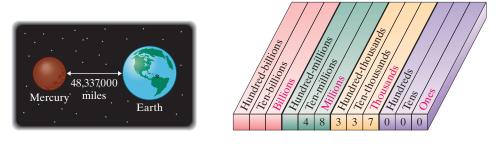
0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, ...

and the **natural numbers** are 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, ...

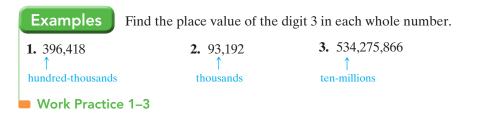
The three dots (\ldots) after each 11 means that these lists continue indefinitely. That is, there is no largest whole number. The smallest whole number is 0. Also, there is no largest natural number. The smallest natural number is 1.

Objective A Finding the Place Value of a Digit in a Whole Number 🜔

The position of each digit in a number determines its **place value**. For example, the distance (in miles) between the planet Mercury and the planet Earth can be represented by the whole number 48,337,000. Next is a place-value chart for this whole number.



The two 3s in 48,337,000 represent different amounts because of their different placements. The place value of the 3 on the left is hundred-thousands. The place value of the 3 on the right is ten-thousands.



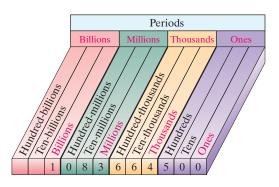
Practice 1–3

Find the place value of the digit 8 in each whole number.

- 1. 38,760,005
- **2.** 67,890
- **3.** 481,922

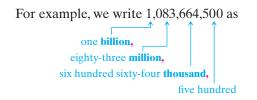
Objective B Writing a Whole Number in Words and in Standard Form ()

A whole number such as 1,083,664,500 is written in **standard form.** Notice that commas separate the digits into groups of three, starting from the right. Each group of three digits is called a **period.** The names of the first four periods are shown in red.



Writing a Whole Number in Words

To write a whole number in words, write the number in each period followed by the name of the period. (The ones period is usually not written.) This same procedure can be used to read a whole number.



Helpful Notice the commas after the name of each period.

Answers1. millions2. hundreds3. ten-thousands

Helpful Hint

The name of the ones period is not used when reading and writing whole numbers. For example,

9.265

is read as

"nine thousand, two hundred sixty-five."

- Examples Write each number in words. 4. 85 eighty-five
- 5. 126 one hundred twenty-six
- twenty-seven thousand, thirty-four **6.** 27,034

Work Practice 4–6

Helpful The word "and" is not used when reading and writing whole numbers. It is used when reading and writing mixed numbers and some decimal values, as shown later in this text.

Example 7	Write 106,052,447 in words.
Solution:	106,052,447 is written as
on	e hundred six million , fifty-two thousand , four hundred forty-s

Work Practice 7

Concept Check True or false? When writing a check for \$2600, the word name we write for the dollar amount of the check is "two thousand sixty." Explain your answer.

Writing a Whole Number in Standard Form

To write a whole number in standard form, write the number in each period, followed by a comma.

Examples

- Write each number in standard form.
- 9. eight hundred five 805 **8.** sixty-one 61
- 10. nine thousand, three hundred eighty-six
 - 9,386 or 9386
- 11. two million, five hundred sixty-four thousand, three hundred fifty



Work Practice 8–11

Practice 8–11

- 8. twenty-nine
- seventy-one
- **11.** six million, five hundred seven

Answers

4. sixty-seven 5. three hundred ninety-five 6. twelve thousand, eight hundred four **7.** three hundred twenty-one million, six hundred seventy thousand, two hundred 8. 29 9. 710 **10.** 26,071 **11.** 6,000,507

Concept Check Answer false

Write each number in standard form.

- 9. seven hundred ten
- 10. twenty-six thousand,



Practice 4–6

4. 67

5. 395

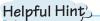
6. 12,804

Practice 7

Write each number in words.

Write 321,670,200 in words.

10



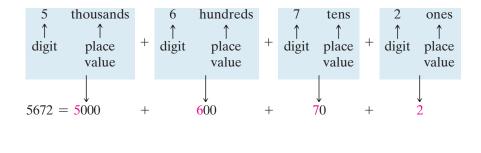
A comma may or may not be inserted in a four-digit number. For example, both

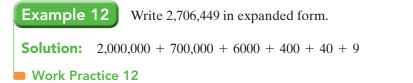
9,386 and 9386

are acceptable ways of writing nine thousand, three hundred eighty-six.

Objective C Writing a Whole Number in Expanded Form

The place value of a digit can be used to write a number in expanded form. The **expanded form** of a number shows each digit of the number with its place value. For example, 5672 is written in expanded form as





We can visualize whole numbers by points on a line. The line below is called a **number line.** This number line has equally spaced marks for each whole number. The arrow to the right simply means that the whole numbers continue indefinitely. In other words, there is no largest whole number.

	Nu	ımbe	er Li	ne			
 1	2	3	4	5	6	7	•

We will study number lines further in Section 1.5.

Objective D Reading Tables 🜔

Now that we know about place value and names for whole numbers, we introduce one way that whole numbers may be presented. **Tables** are often used to organize and display facts that involve numbers. The table on the next page shows the ten countries with the most Nobel Prize winners since the inception of the Nobel Prize in 1901, and the categories of the prizes. The numbers for the Economics prize reflect the winners since 1969, when this category was established. (The numbers may seem large because the annual Nobel Prize is often awarded to more than one individual.) **Practice 12** Write 1,047,608 in expanded form.

Most Nobel Prize Winners by Countries of Birth, 1901–2016								
	Country	Chemistry	Economics	Literature	Peace	Physics	Physiology & Medicine	Total
	United States	52	43	9	19	66	70	259
	United Kingdom	24	8	7	11	23	26	99
	Germany	24	1	7	5	23	17	77
	France	9	4	11	10	9	12	55
-	Sweden	4	2	7	5	4	7	29
	Russia (USSR)	3	2	5	2	11	2	25
	Japan	6	0	2	1	11	4	24
*	Canada	4	3	2	1	4	4	18
	Netherlands	4	2	0	1	9	2	18
	Italy	1	1	5	0	5	5	17
Source: Nob	pelprize.org		·	·	·	·	·	

Practice 13

Use the Nobel Prize Winner table to answer the following questions:

- a. How many Nobel Prize winners in Literature were born in France?
- **b.** Which countries shown have more than 60 Nobel Prize winners?

Answers

13. a. 11 **b.** United States, United Kingdom, and Germany For example, by reading from left to right along the row marked "United States," we find that the United States is the birthplace of 52 Chemistry, 43 Economics, 9 Literature, 19 Peace, 66 Physics, and 70 Physiology and Medicine Nobel Prize winners.

Example 13 Use the Nobel Prize Winner table to answer each question.

- a. How many total Nobel Prize winners were born in Sweden?
- b. Which countries shown have fewer Nobel Prize winners than Russia?

Solution:

- a. Find "Sweden" in the left column. Then read from left to right until the "Total" column is reached. We find that 29 Nobel Prize winners were born in Sweden.
- **b.** There are 25 Russian-born Nobel Prize winners. Japan has 24, Canada has 18, Netherlands has 18, and Italy has 17, so they have fewer Nobel Prize winners.

Work Practice 13

Vocabulary, Readiness & Video Check

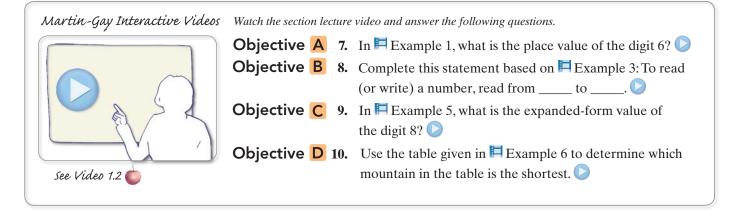
Use the choices below to fill in each blank.

standard form	period	whole	
expanded form	place value	words	

1. The numbers 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, ... are called _____ numbers.

2. The number 1,286 is written in ____

- 3. The number "twenty-one" is written in _____.
- **4.** The number 900 + 60 + 5 is written in _____
- 5. In a whole number, each group of three digits is called a(n) ______.
- 6. The ______ of the digit 4 in the whole number 264 is ones.



1.2 Exercis	se Set MyLab Math 🌘		
Objective A Dete	rmine the place value of the dig	it 5 in each whole number. See E.	xamples 1 through 3.
1. 657	2. 905	3. 5423	4. 6527
5. 43,526,000	6. 79,050,000	7. 5,408,092	8. 51,682,700
Objective B Write	e each whole number in words.	See Examples 4 through 7.	
9. 354	10. 316	11. 8279	12. 5445
13. 26,990	14. 42,009	15. 2,388,000	16. 3,204,000
17. 24,350,185		18. 47,033,107	

Write each number in the sentence in words. See Examples 4 through 7.

- 19. As of March 2017, the population of Iceland was 322,653. (*Source:* livepopulation.com)
 20. The land area of Belize is 22,806 square kilometers. (*Source:* CIA World Factbook)
- **21.** The Burj Khalifa, in Dubai, United Arab Emirates, a hotel and office building, is the world's tallest building at a height of 2717 feet. (*Source:* Council on Tall Buildings and Urban Habitat)
- **22.** As of March 2017, there were 118,049 patients in the United States waiting for an organ transplant. (*Source:* Organ Procurement and Transplantation Network)

- **23.** In 2016, UPS received an average of 101,500,000 online tracking requests per day. (*Source:* UPS)
- **25.** The highest point in Colorado is Mount Elbert, at an elevation of 14,433 feet. (*Source:* U.S. Geological Survey)



27. In 2016, the Great Internet Mersenne Prime Search, a cooperative computing project, helped find a prime number that has 22,338,618 digits. (*Source:* Mersenne Research, Inc.)

- **24.** In fall 2015, there were 347,219 first-time freshmen enrolled in four-year colleges and universities in the United States. (*Source:* Cooperative Institutional Research Program, UCLA)
- **26.** The highest point in Oregon is Mount Hood, at an elevation of 11,239 feet. (*Source:* U.S. Geological Survey)



28. The Goodyear blimp *Eagle* holds 202,700 cubic feet of helium. (*Source:* The Goodyear Tire & Rubber Company)

Write each whole number in standard form. See Examples 8 through 11.

- **29.** Six thousand, five hundred eighty-seven
- ▶ 31. Fifty-nine thousand, eight hundred
 - **33.** Thirteen million, six hundred one thousand, eleven
 - **35.** Seven million, seventeen
 - **37.** Two hundred sixty thousand, nine hundred ninety-seven

- **30.** Four thousand, four hundred sixty-eight
- **32.** Seventy-three thousand, two
- **34.** Sixteen million, four hundred five thousand, sixteen
- **36.** Two million, twelve
- **38.** Six hundred forty thousand, eight hundred eighty-one

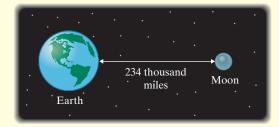
Write the whole number in each sentence in standard form. See Examples 8 through 11.

39. After an orbit correction in October 2013, the International Space Station orbited Earth at an average altitude of about four hundred eighteen kilometers. (*Source:* Heavens Above)



41. La Rinconada, Peru, is the highest town in the world. It is located sixteen thousand, seven hundred thirty-two feet above sea level. (*Source:* Russell Ash: *Top 10 of Everything*)

40. The average distance between the surfaces of Earth and the Moon is about two hundred thirty-four thousand miles.



42. The world's tallest freestanding tower is the Tokyo Sky Tree in Japan. Its height is two thousand eighty feet tall. (*Source:* Council on Tall Buildings and Urban Habitat)

- **43.** The Buena Vista film *Star Wars VII: The Force Awakens* holds the record for U.S./Canada opening day box office gross when it took in approximately one hundred nineteen million, one hundred nineteen thousand dollars on its opening day in 2015. (*Source:* Box Office Mojo)
- **45.** In 2017, the UPS delivery fleet consisted of more than one hundred eight thousand vehicles. (*Source:* UPS)
- **44.** The Warner Bros. film *Harry Potter and the Deathly Hallows Part 2* set the U.S./Canada record for secondhighest opening day box office gross when it took in approximately ninety-one million, seventy-one thousand dollars on its opening day in 2011. (*Source:* Box Office Mojo)
- **46.** Morten Andersen, who played football for New Orleans, Atlanta, N.Y. Giants, Kansas City, and Minnesota between 1982 and 2007, holds the record for the most points scored in a career. Over his 25-year career he scored two thousand, five hundred forty-four points. (*Source:* NFL.com)

Objective C Write each whole number in expanded form. See Example 12.

47. 406	48. 789	49. 3470	50. 6040
51. 80,774	52. 20,215	53. 66,049	54. 99,032
55. 39,680,000		56. 47,703,029	

Objectives B C D Mixed Practice *The table shows the six tallest mountains in New England and their elevations. Use this table to answer Exercises 57 through 62. See Example 13.*

Mountain (State)	Elevation (in feet)
Boott Spur (NH)	5492
Mt. Adams (NH)	5793
Mt. Clay (NH)	5532
Mt. Jefferson (NH)	5712
Mt. Sam Adams (NH)	5584
Mt. Washington (NH)	6288
Source: U.S. Geological Sur	vey

- 57. Write the elevation of Mt. Clay in standard form and then in words.
- **59.** Write the height of Boott Spur in expanded form.
- 61. Which mountain is the tallest in New England?



- **58.** Write the elevation of Mt. Washington in standard form and then in words.
- **60.** Write the height of Mt. Jefferson in expanded form.
- **62.** Which mountain is the second tallest in New England?

The table shows the top ten museums in the world in 2015. Use this table to answer Exercises 63 through 68. See Example 13.

Top 10 Museums Worldwide in 2015 Museum Location Visitors 8,700,000 Louvre Paris, France Beijing, China 7,290,000 National Museum of China National Museum of Natural History Washington, DC, United States 6,900,000 National Air and Space Museum Washington, DC, United States 6,900,000 British Museum London, England 6.821.000 The Metropolitan Museum of Art New York, NY, United States 6,300,000 6,002,000 Vatican Museums Vatican, Vatican City 5,948,000 Shanghai Science and Technology Museum Shanghai, China London, England 5,908,000 National Gallery Taipei, Taiwan 5,288,000 National Palace Museum (Taiwan) (Source: Themed Entertainment Association)

67. How many of 2015's top ten museums in the world were located in the United States?

- **63.** Which museum had fewer visitors, the National Gallery in London or the National Air and Space Museum in Washington, DC?
- **64.** Which museum had more visitors, the British Museum in London or the Shanghai Science and Technology Museum in Shanghai?
- **65.** How many people visited the Vatican Museums? Write the number of visitors in words.
- **66.** How many people visited the Louvre? Write the number of visitors in words.
- **68.** How many of 2015's top ten museums in the world were visited by fewer than 6,000,000 people?

Concept Extensions

- **69.** Write the largest four-digit number that can be made from the digits 1, 9, 8, and 6 if each digit must be used once. _____ ____
- **70.** Write the largest five-digit number that can be made using the digits 5, 3, and 7 if each digit must be used at least once. _____ ____ _____

Check to see whether each number written in standard form matches the number written in words. If not, correct the number in words. See the Concept Check in this section.



73. If a number is given in words, describe the process used to write this number in standard form.

72	
72.	60-9124/7233 1402 1000613331
	DATE
	PAY TO \$ 7030,00
	Seven Thousand Thirty and 100 - Dollars
	FIRST STATE BANK OF FARTHINGTON FARTHINGTON, U-6422
	МЕМО
	"621497260" 1000613331" 1402

- **74.** If a number is written in standard form, describe the process used to write this number in expanded form.
- **75.** In November 2016, the Chinese supercomputer Sunway TaihuLight was ranked as the world's fastest computer. Its speed was clocked at 93 petaflops, or more than 93 quadrillion arithmetic operations per second. Look up "quadrillion" (in the American system) and use the definition to write this number in standard form. (*Source:* top500.org)
- **76.** As of March 2017, the national debt of France was approximately \$5 trillion. Look up "trillion" (in the American system) and use the definition to write 5 trillion in standard form. (*Source:* CIA World Factbook)
- **77.** The Pro Football Hall of Fame was established on September 7, 1963, in this town. Use the information and the diagram to the right to find the name of the town.
 - Alliance is east of Massillon.
 - Dover is between Canton and New Philadelphia.
 - Massillon is not next to Alliance.
 - Canton is north of Dover.



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1.3 Adding Whole Numbers and Perimeter 🔘

Objective 🗛 Adding Whole Numbers 🕑

According to Gizmodo, the iPod nano (currently in its seventh generation) is still the best overall MP3 player.

Suppose that an electronics store received a shipment of two boxes of iPod nanos one day and an additional four boxes of iPod nanos the next day. The **total** shipment in the two days can be found by adding 2 and 4.

2 boxes of iPod nanos + 4 boxes of iPod nanos = 6 boxes of iPod nanos

The **sum** (or total) is 6 boxes of iPod nanos. Each of the numbers 2 and 4 is called an **addend**, and the process of finding the sum is called **addition**.

2	+	4	+	6
1		1		1
addend		addend		sum

To add whole numbers, we add the digits in the ones place, then the tens place, then the hundreds place, and so on. For example, let's add 2236 + 160.

2 3 9 6 sum of ones sum of tens sum of hundreds	2236 + 160	Line up numbers vertically so that the place values correspond. Then add digits in corresponding place values, starting with the ones place.
sum of tens	2396	
sum of thousands	sum of sum of	tens hundreds



Work Practice 1

When the sum of digits in corresponding place values is more than 9, **carrying** is necessary. For example, to add 365 + 89, add the ones-place digits first.

Carrying

 $\frac{+ 89}{4}$ 5 ones + 9 ones = 14 ones or 1 ten + 4 ones 4 Write the 4 ones in the ones place and carry the 1 ten to the tens place.

Next, add the tens-place digits.

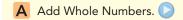
365

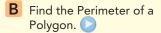
 $\frac{3 6 5}{5 4}$ $\frac{4 89}{5 4}$ 1 ten + 6 tens + 8 tens = 15 tens or 1 hundred + 5 tens Write the 5 tens in the tens place and carry the 1 hundred to the hundreds place.

Next, add the hundreds-place digits.

 $\frac{1}{3}\frac{1}{6}\frac{1}{5}$ $\frac{+89}{454}$ 1 hundred + 3 hundreds = 4 hundreds Write the 4 hundreds in the hundreds place.

Objectives





```
C Solve Problems by Adding
Whole Numbers.
```



Practice 1 Add: 7235 + 542 Practice 2 Add: 27,364 + 92,977

Example 2	Add:	34,285 + 149,761			
Solution:	$ \begin{array}{r} 111 \\ 34,28 \end{array} $	35			
+ 149,761					
184,046					
Work Practice 2					

Concept Check What is wrong with the following computation?

Before we continue adding whole numbers, let's review some properties of addition that you may have already discovered. The first property that we will review is the **addition property of 0**. This property reminds us that the sum of 0 and any number is that same number.

Addition Property of 0

The sum of 0 and any number is that number. For example,

7 + 0 = 70 + 7 = 7

Next, notice that we can add any two whole numbers in any order and the sum is the same. For example,

4 + 5 = 9 and 5 + 4 = 9

We call this special property of addition the commutative property of addition.

Commutative Property of Addition

Changing the order of two addends does not change their sum. For example,

2 + 3 = 5 and 3 + 2 = 5

Another property that can help us when adding numbers is the **associative property of addition.** This property states that when adding numbers, the grouping of the numbers can be changed without changing the sum. We use parentheses to group numbers. They indicate which numbers to add first. For example, let's use two different groupings to find the sum of 2 + 1 + 5.

$$\underbrace{(2+1)}_{\uparrow} + 5 = 3 + 5 = 8$$

Also,

2 + (1+5) = 2 + 6 = 8

Both groupings give a sum of 8.

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Concept Check Answer

Answer 2. 120,341

forgot to carry 1 hundred to the hundreds place

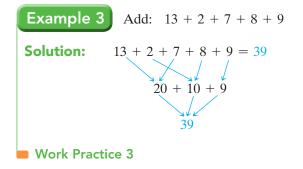
Associative Property of Addition

Changing the grouping of addends does not change their sum. For example,

$$3 + (5+7) = 3 + 12 = 15$$
 and $(3+5) + 7 = 8 + 7 = 15$

The commutative and associative properties tell us that we can add whole numbers using any order and grouping that we want.

When adding several numbers, it is often helpful to look for two or three numbers whose sum is 10, 20, and so on. Why? Adding multiples of 10 such as 10 and 20 is easier.



Feel free to use the process of Example 3 anytime when adding.

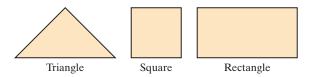
Example 4 Add: 1647 + 246 + 32 + 85 Solution: 1647 246 32 + 85 2010 Work Practice 4 Add: 11 + 7 + 8 + 9 + 13

Practice 3

Practice 4 Add: 19 + 5042 + 638 + 526

Objective **B** Finding the Perimeter of a Polygon 🕑

In geometry, addition is used to find the perimeter of a polygon. A **polygon** can be described as a flat figure formed by line segments connected at their ends. (For more review, see Appendix A.3.) Geometric figures such as triangles, squares, and rectangles are called polygons.

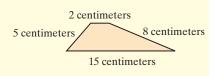


The **perimeter** of a polygon is the *distance around* the polygon. This means that the perimeter of a polygon is the sum of the lengths of its sides.

Answers 3. 48 4. 6225

Practice 5

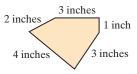
Find the perimeter of the polygon shown. (A centimeter is a unit of length in the metric system.)



Practice 6

A park is in the shape of a triangle. Each of the park's three sides is 647 feet. Find the perimeter of the park.

Example 5 Find the perimeter of the polygon shown.



Solution: To find the perimeter (distance around), we add the lengths of the sides.

2 in. + 3 in. + 1 in. + 3 in. + 4 in. = 13 in.

The perimeter is 13 inches.

Work Practice 5

To make the addition appear simpler, we will often not include units with the addends. If you do this, make sure units are included in the final answer.

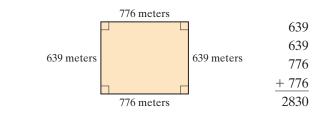
Example 6

6 Calculating the Perimeter of a Building

The world's largest commercial building under one roof is the flower auction building of the cooperative VBA in Aalsmeer, Netherlands. The floor plan is a rectangle that measures 776 meters by 639 meters. Find the perimeter of this building. (A meter is a unit of length in the metric system.) (*Source: The Handy Science Answer Book*, Visible Ink Press)



Solution: Recall that opposite sides of a rectangle have the same length. To find the perimeter of this building, we add the lengths of the sides. The sum of the lengths of its sides is



The perimeter of the building is 2830 meters.

Work Practice 6

Objective C Solving Problems by Adding 🜔

Often, real-life problems occur that can be solved by adding. The first step in solving any word problem is to *understand* the problem by reading it carefully.

Descriptions of problems solved through addition *may* include any of these key words or phrases:

Addition			
Key Words or Phrases	Symbols		
added to	5 added to 7	7 + 5	
plus	0 plus 78	0 + 78	
increased by	12 increased by 6	12 + 6	
more than	11 more than 25	25 + 11	
total	the total of 8 and 1	8 + 1	
sum	the sum of 4 and 133	4 + 133	

To solve a word problem that involves addition, we first use the facts given to write an addition statement. Then we write the corresponding solution of the reallife problem. It is sometimes helpful to write the statement in words (brief phrases) and then translate to numbers.

Example 7 Finding the Number of Trucks Sold in the United States

In 2015, a total of 9,879,465 trucks were sold in the United States. In 2016, total truck sales in the United States had increased by 712,397 vehicles. Find the total number of trucks sold in the United States in 2016. (Source: Alliance of Automobile Manufacturers)

Solution: The key phrase here is "had increased by," which suggests that we add. To find the number of trucks sold in 2016, we add the increase 712.397 to the number of trucks sold in 2015.

In Words

Number sold in 2015	5 →	9	9,879,465
+ increase	$e \longrightarrow$	+	712,397
Number sold in 2016	$\overline{5} \longrightarrow$	10),591,862

The number of passenger vehicles sold in the United States in 2016 was 10,591,862.

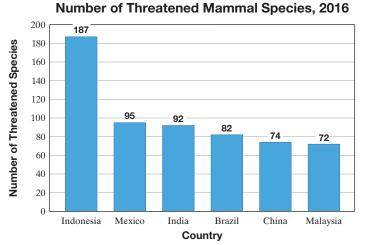
Translate to Numbers

Work Practice 7

Graphs can be used to visualize data. The graph shown next is called a bar graph. For this bar graph, the height of each bar is labeled above the bar. To check this height, follow the top of each bar to the vertical line to the left. For example, the first bar is labeled 187. Follow the top of that bar to the left until the vertical line is reached, between 180 and 200, but closer to 180, or 187.

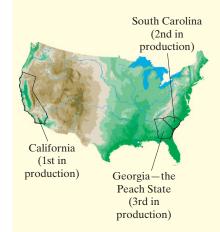
Example 8 Reading a Bar Graph

In the following graph, each bar represents a country and the height of each bar represents the number of threatened mammal species identified in that country.



Practice 7

Georgia produces 70 million pounds of freestone peaches per year. The second largest U.S. producer of peaches, South Carolina, produces 50 million pounds more freestone peaches than Georgia. How much does South Carolina produce? (*Source:* farms.com)



Practice 8

Use the graph in Example 8 to answer the following:

- **a.** Which country shown has the fewest threatened mammal species?
- **b.** Find the total number of threatened mammal species for Brazil, India, and Mexico.

Answers **7.** 120 million lb 8. a. Malaysia b. 269

(*Continued on next page*)

- a. Which country shown has the greatest number of threatened mammal species?
- **b.** Find the total number of threatened mammal species for Malaysia, China, and Indonesia.

Solution:

- **a.** The country with the greatest number of threatened mammal species corresponds to the tallest bar, which is Indonesia.
- **b.** The key word here is "total." To find the total number of threatened mammal species for Malaysia, China, and Indonesia, we add.

In Words		Transla	ate to Numbers
Malaysia	\longrightarrow		72
China	\longrightarrow		74
Indonesia	\longrightarrow		+ 187
		Total	333

The total number of threatened mammal species for Malaysia, China, and Indonesia is 333.

Work Practice 8

Calculator Explorations Adding Number	5	
To add numbers on a calculator, find the keys marked $[+]$ and $[=]$ or $[ENTER]$.	Use a calculator to add.	
For example, to add 5 and 7 on a calculator, press the keys	1. 89 + 45	2. 76 + 97
$5 + 7$ then \equiv or ENTER.	3. 285 + 55	4. 8773 + 652
The display will read 12.	5. 985	6. 465
Thus, $5 + 7 = 12$.	1210 562	9888 620
To add 687, 981, and 49 on a calculator, press the keys $687 + 981 + 49$ then = or ENTER.	+ 77	+1550
The display will read 1717 .		
Thus, $687 + 981 + 49 = 1717$. (Although entering 687, for example, requires pressing more than one key, here numbers are grouped together for easier reading.)		

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Some choices may be used more than once.

sum	order	addend	associative
perimeter	number	grouping	commutative

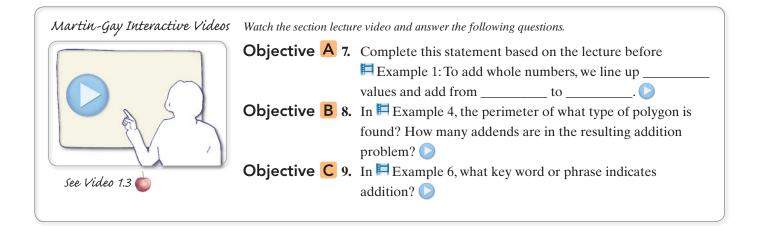
1. The sum of 0 and any number is the same _____.

2. The sum of any number and 0 is the same _____.

3. In 35 + 20 = 55, the number 55 is called the _____ and 35 and 20 are each called a(n) _____.

4. The distance around a polygon is called its _____

- 5. Since (3 + 1) + 20 = 3 + (1 + 20), we say that changing the _____ in addition does not change the sum. This property is called the _____ property of addition.
- 6. Since 7 + 10 = 10 + 7, we say that changing the _____ in addition does not change the sum. This property is called the _____ property of addition.



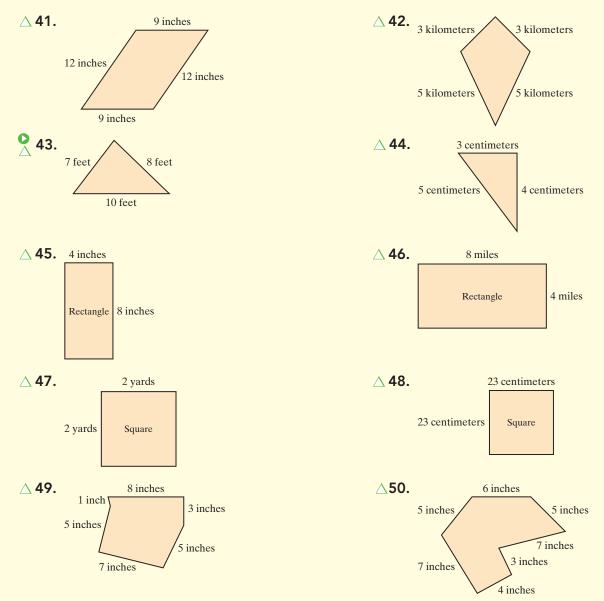
1.3 Exercise Set MyLab Math

Objective A Add. See Examples 1 through 4.

1. 14 + 22	2. 27 + 31	3. 62 $+230$	4. 37 + 542	5. 12 13 +24
6. 23 45 +30	7. 5267 + 132	8. 236 + 6243	9. 53 + 64	10. 41 + 74
11. 22 + 490	12. 35 + 470		13. 22,781 + 186,297	14. 17,427 + 821,059
▶ 15. 8 9 2 5 +1	16. 3 5 8 5 +7		17. 6 21 14 9 +12	18. 12 4 8 26 +10
19. 81 17 23 79 +12	20. 64 28 56 25 +32		21. 62 + 18 + 14	22. 23 + 49 + 18
23. 40 + 800 + 70	24. 90 + 900 +	20	25. 7542 + 49 + 682	26. 1624 + 32 + 976

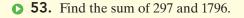
0 27.	24 + 9006 +	489 + 2407 2	8. 16 + 1056 + 748 + 7770	29. 627 628 +629	30. 427 383 +229
31.	6820 4271 +5626	32. 6789 4321 +5555	33. 507 593 + 10	34. 864 33 +356	35. 4200 2107 +2692
36.	5000 1400 +3021	37. 49 628 5 762 +29,462	38. 26 582 4 763 +62,511	39. 121,742 57,279 26,586 +426,782	40. 504,218 321,920 38,507 +594,687

Objective B *Find the perimeter of each figure. See Examples 5 and 6.*





Objectives A B C Mixed Practice–**Translating** Solve. See Examples 1 through 8.



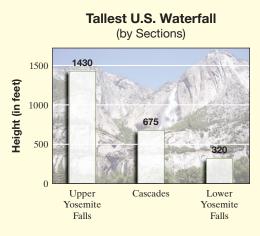
- **55.** Find the total of 76, 39, 8, 17, and 126.
- **57.** What is 452 increased by 92?
- **59.** What is 2686 plus 686 plus 80?
- **61.** The estimated population of Florida was 20,148 thousand in 2016. If it is projected to increase by 2286 thousand by 2025, what is Florida's projected population in 2025? (*Source:* University of Florida, Bureau of Economic and Business research)
- 63. The highest point in South Carolina is Sassafras Mountain at 3560 feet above sea level. The highest point in North Carolina is Mt. Mitchell, whose peak is 3124 feet increased by the height of Sassafras Mountain. Find the height of Mt. Mitchell. (*Source:* U.S. Geological Survey)
- \triangle **65.** Leo Callier is installing an invisible fence in his backyard. How many feet of wiring are needed to enclose the yard below?



- Solve. See Examples 1 through 8.
- **54.** Find the sum of 802 and 6487.
- **56.** Find the total of 89, 45, 2, 19, and 341.
- **58.** What is 712 increased by 38?
- **60.** What is 3565 plus 565 plus 70?
- **62.** The estimated population of California was 39,250 thousand in 2016. It is projected in increase by 4850 thousand by 2030. What is California's projected population in 2030? (*Source:* Public Policy Institute of California)
- **64.** The distance from Kansas City, Kansas, to Hays, Kansas, is 285 miles. Colby, Kansas, is 98 miles farther from Kansas City than Hays. Find the total distance from Kansas City to Colby.
- \triangle **66.** A homeowner is considering installing gutters around her home. Find the perimeter of her rectangular home.



67. The tallest waterfall in the United States is Yosemite Falls in Yosemite National Park in California. Yosemite Falls is made up of three sections, as shown in the graph. What is the total height of Yosemite Falls? (*Source:* U.S. Department of the Interior)



69. In 2016, Harley-Davidson sold 161,839 motorcycles domestically. In addition, 100,352 Harley-Davidson motorcycles were sold internationally. What was the total number of Harley-Davidson motorcycles sold in 2016? (*Source:* Harley-Davidson, Inc.)



71. During one month is 2016, the two top-selling vehicles in the United States were the Ford F-Series and the Chevrolet Silverado, both trucks. There were 65,542 F-Series trucks and 49,768 Silverados sold that month. What was the total number of these trucks sold in that month? (*Source:* www.goodcarbadcar.com)

68. Jordan White, a nurse at Mercy Hospital, is recording fluid intake on a patient's medical chart. During his shift, the patient had the following types and amounts of intake measured in cubic centimeters (cc). What amount should Jordan record as the total fluid intake for this patient?

Oral	Intravenous	Blood
240	500	500
100	200	
355		

70. Hank Aaron holds Major League Baseball's record for the most runs batted in over his career. He batted in 1305 runs from 1954 to 1965. He batted in another 992 runs from 1966 until he retired in 1976. How many total runs did Hank Aaron bat in during his career in professional baseball?

72. In 2016, the country of New Zealand had 22,867,835 more sheep than people. If the human population of New Zealand in 2016 was 4,573,567, what was the sheep population? (*Source:* www.stats.govt.nz)

73. The largest permanent Monopoly board is made of granite and located in San Jose, California. Find the perimeter of the square playing board.



74. The smallest commercially available jigsaw puzzle (with a minimum of 1000 pieces) is manufactured in Hong Kong, China. Find the exact perimeter of this rectangular-shaped puzzle in millimeters. (*Source: Guinness World Records*)



(about 10 in.)

182 millimeters (about 7 in.)

- **75.** In 2016, there were 2669 Gap Inc. (Gap, Banana Republic, Athleta, Old Navy, and Intermix North America) stores located in the United States and 606 located outside the United States. How many Gap Inc. stores were located worldwide? (*Source:* Gap Inc.)
- **76.** Wilma Rudolph, who won three gold medals in track and field events in the 1960 Summer Olympics, was born in 1940. Allyson Felix, who also won three gold medals in track and field events but in the 2012 Summer Olympics, was born 45 years later. In what year was Allyson Felix born?

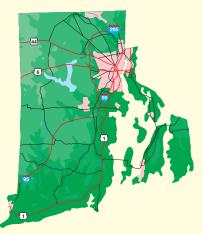
The table shows the number of CVS Pharmacies in ten states. Use this table to answer Exercises 77 through 82.

The Top Ten States for CVS Pharmacies in 2016		
State Number of Pharmacies		
Massachusetts	356	
California	867	
Florida	756	
Georgia	313	
Indiana	301	
New York	486	
North Carolina	313	
Ohio	309	
Pennsylvania	408	
Texas	659	
(Source: CVS Pharmacy Inc.)		

- **77.** Which state had the most CVS pharmacies?
- **78.** Which of the states listed in the table had the fewest CVS pharmacies?
- **79.** What was the total number of CVS pharmacies located in the three states with the most CVS pharmacies?
- **80.** How many CVS pharmacies were located in the ten states listed in the table?
- **81.** Which pair of neighboring states had more CVS pharmacies combined, Pennsylvania and New York or Florida and Georgia?
- **82.** There were 3048 CVS pharmacies located in the states not listed in the table. How many CVS pharmacies were there in the 50 states?

83. The state of Delaware has 2997 miles of urban highways and 3361 miles of rural highways. Find the total highway mileage in Delaware. (Source: U.S. Federal Highway Administration)

84. The state of Rhode Island has 5260 miles of urban highways and 1225 miles of rural highways. Find the total highway mileage in Rhode Island. (Source: U.S. Federal Highway Administration)



Concept Extensions

85. In your own words, explain the commutative property of addition.	86. In your own words, explain the associative property of addition.
87. Give any three whole numbers whose sum is 100.	88. Give any four whole numbers whose sum is 25.
89. Add: 56,468,980 + 1,236,785 + 986,768,000	90. Add: 78,962 + 129,968,350 + 36,462,880
Check each addition below. If it is incorrect, find the corre	ct answer. See the Concept Check in this section.

91. 566	92. 773	93. 14	94. 19
932	659	173	214
+ 871	+ 481	86	49
2369	1913	+257	+651
		520	923

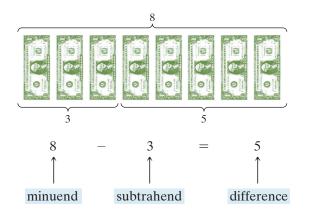
Objectives

- 🗛 Subtract Whole Numbers. D
- **B** Solve Problems by Subtracting Whole Numbers. D

Subtracting Whole Numbers 1.4

Objective A Subtracting Whole Numbers 🕗

If you have \$5 and someone gives you \$3, you have a total of \$8, since 5 + 3 = 8. Similarly, if you have \$8 and then someone borrows \$3, you have \$5 left. **Subtraction** is finding the **difference** of two numbers.



In this example, 8 is the **minuend**, and 3 is the **subtrahend**. The **difference** between these two numbers, 8 and 3, is 5.

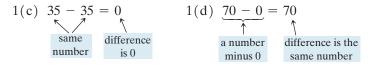
Notice that addition and subtraction are very closely related. In fact, subtraction is defined in terms of addition.

8 - 3 = 5 because 5 + 3 = 8

This means that subtraction can be *checked* by addition, and we say that addition and subtraction are reverse operations.

Example 1Subtract. Check each answer by adding.a. 12 - 9b. 22 - 7c. 35 - 35d. 70 - 0Solution:a. 12 - 9 = 3 because 3 + 9 = 12b. 22 - 7 = 15 because 15 + 7 = 22c. 35 - 35 = 0 because 0 + 35 = 35d. 70 - 0 = 70 because 70 + 0 = 70Work Practice 1

Look again at Examples 1(c) and 1(d).



These two examples illustrate the subtraction properties of 0.

Subtraction Properties of 0

The difference of any number and that same number is 0. For example,

11 - 11 = 0

The difference of any number and 0 is that same number. For example,

45 - 0 = 45

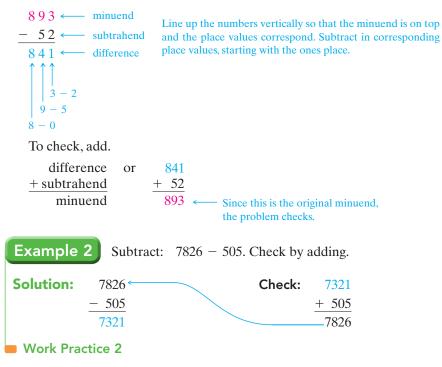
To subtract whole numbers we subtract the digits in the ones place, then the tens place, then the hundreds place, and so on. When subtraction involves numbers

Practice 1

Subtract. Check each answer by adding. **a.** 14 - 6

b. 20 - 8**c.** 93 - 93**d.** 42 - 0

Answers 1. a. 8 b. 12 c. 0 d. 42 of two or more digits, it is more convenient to subtract vertically. For example, to subtract 893 - 52,



Subtracting by Borrowing

When subtracting vertically, if a digit in the second number (subtrahend) is larger than the corresponding digit in the first number (minuend), **borrowing** is necessary. For example, consider

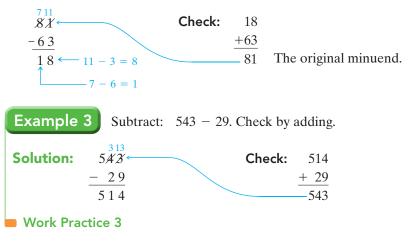


Since the 3 in the ones place of 63 is larger than the 1 in the ones place of 81, borrowing is necessary. We borrow 1 ten from the tens place and add it to the ones place.

Borrowing

 $\begin{array}{rcl} 8 & -1 & = & 7 & \rightarrow & 7 & 11 & \leftarrow 1 \text{ ten } + 1 \text{ one } = & 11 \text{ ones} \\ \text{tens} & \text{tens} & & \mathscr{B} & \mathscr{K} \\ & & -6 & 3 \end{array}$

Now we subtract the ones-place digits and then the tens-place digits.



Practice 3

697

- 49

-245

326

1234

822

a.

b.

c.

Subtract. Check by adding.

Practice 2

a. 9143 - 122

b. 978 - 851

Subtract. Check by adding.

Answers 2. a. 9021 b. 127 3. a. 648 b. 81 c. 412 Sometimes we may have to borrow from more than one place. For example, to subtract 7631 - 152, we first borrow from the tens place.

$$763\%^{211} - 152 = 9 \leftarrow 11 - 2 = 9$$

In the tens place, 5 is greater than 2, so we borrow again. This time we borrow from the hundreds place.



Example 4

Subtract: 900 - 174. Check by adding.

Solution: In the ones place, 4 is larger than 0, so we borrow from the tens place. But the tens place of 900 is 0, so to borrow from the tens place we must first borrow from the hundreds place.

Now borrow from the tens place.

$ \begin{array}{c} 8 & \cancel{10} \\ \cancel{9} & \cancel{9} & \cancel{9} \end{array} $	Check:	726
$\frac{-1}{7}$ $\frac{7}{2}$ $\frac{4}{6}$		+174 - 900

Work Practice 4

Objective **B** Solving Problems by Subtracting

Often, real-life problems occur that can be solved by subtracting. The first step in solving any word problem is to *understand* the problem by reading it carefully.

Descriptions of problems solved through subtraction *may* include any of these key words or phrases:

\checkmark			
Subtraction			
Key Words or Phrases	Examples	Symbols	
subtract	subtract 5 from 8	8 - 5	
difference	the difference of 10 and 2	10 - 2	
less	17 less 3	17 - 3	
less than	2 less than 20	20 - 2	
take away	14 take away 9	14 - 9	
decreased by	7 decreased by 5	7 - 5	
subtracted from	9 subtracted from 12	12 - 9	

Practice 4

Subtract. Check by adding.

a.	400	
	-164	
b.	1000)
	- 762	2

Helpful

Be careful when solving applications that suggest subtraction. Although order *does not* matter when adding, order *does* matter when subtracting. For example, 20 - 15 and 15 - 20do not simplify to the same number.

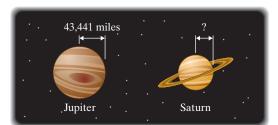
Answers 4. a. 236 b. 238

- **Concept Check** In each of the following problems, identify which number is the minuend and which number is the subtrahend.
- **a.** What is the result when 6 is subtracted from 40?
- **b.** What is the difference of 15 and 8?
- **c.** Find a number that is 15 fewer than 23.

To solve a word problem that involves subtraction, we first use the facts given to write a subtraction statement. Then we write the corresponding solution of the reallife problem. It is sometimes helpful to write the statement in words (brief phrases) and then translate to numbers.

Example 5 Finding the Radius of a Planet

The radius of Jupiter is 43,441 miles. The radius of Saturn is 7257 miles less than the radius of Jupiter. Find the radius of Saturn. (Source: National Space Science Data Center)



	Solution:	In Words	Translate to Numbers	
		radius of Jupiter \longrightarrow - 7257 \longrightarrow	,	
		radius of Saturn \longrightarrow	36,184	
-	The radius of Saturn is 36,184 miles.			

Work Practice 5

Example 6

6 Calculating Miles per Gallon

A subcompact car gets 42 miles per gallon of gas. A full-size car gets 17 miles per gallon of gas. Find the difference between the subcompact car miles per gallon and the full-size car miles per gallon.

Solution:	In Words	Translate to Numbers
	subcompact miles per gallon \longrightarrow	3 12 # 2
	$-$ full-size miles per gallon \longrightarrow	-17
	difference in miles per gallon	25

The difference in the subcompact car miles per gallon and the full-size car miles per gallon is 25 miles per gallon.

Work Practice 6

Practice 5

The radius of Uranus is 15,759 miles. The radius of Neptune is 458 miles less than the radius of Uranus. What is the radius of Neptune? (*Source:* National Space Science Data Center)

Helpful Hint Since subtrac-

tion and addition are reverse operations, don't forget that a subtraction problem can be checked by adding.

Practice 6

During a sale, the price of a new suit is decreased by \$47. If the original price was \$92, find the sale price of the suit.

Answers

5. 15,301 miles **6.** \$45

Concept Check Answers

a. minuend: 40; subtrahend: 6
b. minuend: 15; subtrahend: 8
c. minuend: 23; subtrahend: 15

Helpful Hint Once again, because subtraction and addition are reverse operations, don't forget that a subtraction problem can be checked by adding. É. **Calculator Explorations** Subtracting Numbers To subtract numbers on a calculator, find the keys marked Use a calculator to subtract. - and = or ENTER. 1. 865 - 95 **2.** 76 - 27 For example, to find 83 - 49 on a calculator, press the **4.** 366 - 87 **3.** 147 – 38 keys $\boxed{83}$ – $\boxed{49}$ then = or ENTER. **5.** 9625 - 647 **6.** 10,711 - 8925 The display will read 34. Thus, 83 - 49 = 34.

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank.

 0
 minuend
 difference

 number
 subtrahend

 1. The difference of any number and that same number is ______.

 2. The difference of any number and 0 is the same ______.

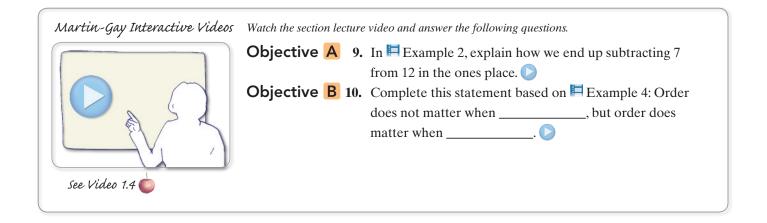
 3. In 37 - 19 = 18, the number 37 is the ______, and the number 19 is the ______.

 4. In 37 - 19 = 18, the number 18 is called the ______.

 Find each difference.

 5. 6 - 6
 6. 93 - 93

 7. 600 - 0
 8. 5 - 0



1.4 Exe	rcise Set My	Lab Math 🜔			
_		dding. See Examples 1	! and 2.		
1. 67 -23	2.	72 41	3. 389 -124		4. 572 <u>- 321</u>
5. 167 <u>- 32</u>	6.	286 - 45	7. 2677 – 4	23	8. 5766 – 324
9. 6998 – 1453	10.	4912 - 2610	● 11. 749 <u>- 149</u>		12. 257 <u>-257</u>
Subtract. Check b	y adding. See Examp	les 1 through 4.			
● 13. 62 <u>-37</u>	14. 55 <u>- 29</u>	15. 70 <u>-25</u>	16. 80 <u>- 37</u>	17. 938 <u>- 792</u>	18. 436 -275
19. 922 <u>- 634</u>	20. 674 <u>- 299</u>	21. 600 <u>- 432</u>	22. 300 <u>- 149</u>	23. 142 <u>- 36</u>	24. 773 - 29
25. 923 <u>- 476</u>	26. 813 <u>-227</u>	27. 6283 <u>- 560</u>	28. 5349 <u>- 720</u>	29. 533 <u>- 29</u>	30. 724 <u>- 16</u>
31. 200 <u>- 111</u>	32. 300 <u>-211</u>	33. 1983 <u>- 1904</u>	34. 1983 <u>- 1914</u>	35. 56,422 <u>-16,508</u>	36. 76,652 - 29,498
37. 50,000 - 17,	289	38. 40,000 - 23,58	82	39. 7020 - 197	79

40. 6050 - 1878 **41.** 51,111 - 19,898 **42.** 62,222 - 39,898

Objective B Solve. See Examples 5 and 6.	
43. Subtract 5 from 9.	44. Subtract 9 from 21.
• 45. Find the difference of 41 and 21.	46. Find the difference of 16 and 5.
47. Subtract 56 from 63.	48. Subtract 41 from 59.

49. Find 108 less 36.

- **51.** Find 12 subtracted from 100.
- 53. Professor Graham is reading a 503-page book. If she has just finished reading page 239, how many more pages must she read to finish the book?
- **55.** In 2012, the hole in the Earth's ozone layer over Antarctica was about 18 million square kilometers in size. By mid 2016, the hole peaked at about 23 million square kilometers. By how much did the hole grown from 2012 to 2016? (Source: NASA Ozone Watch)



50. Find 25 less 12.

- **52.** Find 86 subtracted from 90.
- **54.** When a couple began a trip, the odometer read 55,492. When the trip was over, the odometer read 59,320. How many miles did they drive on their trip?
- **56.** Bamboo can grow to 98 feet while Pacific giant kelp (a type of seaweed) can grow to 197 feet. How much taller is the kelp than the bamboo?

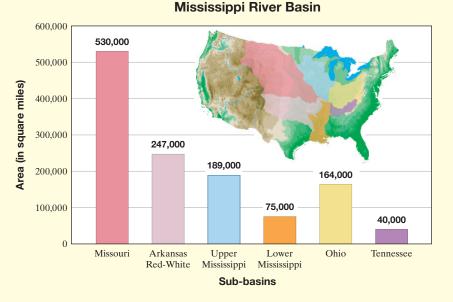




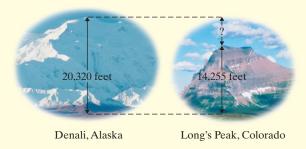
Kelp

A river basin is the geographic area drained by a river and its tributaries. The Mississippi River Basin is the third largest in the world and is divided into six sub-basins, whose areas are shown in the following bar graph. Use this graph for Exercises 57 through 60.

- 57. Find the total U.S. land area drained by the Upper Mississippi and Lower Mississippi sub-basins.
- **58.** Find the total U.S. land area drained by the Ohio and Tennessee sub-basins.
- **59.** How much more land is drained by the Missouri sub-basin than the Arkansas Red-White sub-basin?
- **60.** How much more land is drained by the Upper Mississippi sub-basin than the Lower Mississippi sub-basin?



61. The peak of Denali in Alaska is 20,320 feet above sea level. The peak of Long's Peak in Colorado is 14,255 feet above sea level. How much higher is the peak of Denali than Long's Peak? (*Source:* U.S. Geological Survey)



62. On January 12, 1916, the city of Indianapolis, Indiana, had the greatest temperature change in a day. It dropped 58 degrees. If the high temperature was 68° Fahrenheit, what was the low temperature?



- 63. The Oroville Dam, on the Feather River, is the tallest dam in the United States at 754 feet. The Hoover Dam, on the Colorado River, is 726 feet high. How much taller is the Oroville Dam than the Hoover Dam? (*Source:* U.S. Bureau of Reclamation)
 - **65.** The distance from Kansas City to Denver is 645 miles. Hays, Kansas, lies on the road between the two and is 287 miles from Kansas City. What is the distance between Hays and Denver?
 - **67.** A new 4D Blu-ray player with streaming and Wi-Fi costs \$295. A college student has \$914 in her savings account. How much will she have left in her savings account after she buys the Blu-ray player?
 - **69.** The population of Arizona is projected to grow from 6927 thousand in 2017 to 8536 thousand in 2030. What is Arizona's projected population increase over that time? (*Source:* Arizona Office of Economic Opportunity)



- **64.** A new iPhone 7 with 32 GB costs \$649. Jocelyn Robinson has \$845 in her savings account. How much will she have left in her savings account after she buys the iPhone? (*Source:* Apple, Inc.)
- **66.** Pat Salanki's blood cholesterol level is 243. The doctor tells him it should be decreased to 185. How much of a decrease is this?
- **68.** A stereo that regularly sells for \$547 is discounted by \$99 in a sale. What is the sale price?
- **70.** In 1996, the centennial of the Boston Marathon, the official number of participants was 38,708. In 2017, there were 6208 fewer participants. How many official participants were there for the 2017 Boston Marathon? (*Source:* Boston Athletic Association)



The decibel (dB) is a unit of measurement for sound. Every increase of 10 dB is a tenfold increase in sound intensity. The bar graph below shows the decibel levels for some common sounds. Use this graph for Exercises 71 through 74.

- **71.** What is the dB rating for live rock music?
- **72.** Which is the quietest of all the sounds shown in the graph?
- **73.** How much louder is the sound of snoring than normal conversation?
- **74.** What is the difference in sound intensity between live rock music and loud television?
- **75.** As of this writing, there have been 45 U.S. presidents. Of these 15, were freemasons. How many U.S. presidents were not freemasons?
- **Decibel Levels for Common Sounds** 120 100 100 88 Decibels (dB) 80 70 60 40 30 20 10 0 Leaves Normal Live Rock Loud Snoring Rustling Television Conversation Music
- **76.** In 2016, the population of Springfield, Illinois, was 117,006, and the population of Champaign, Illinois, was 83,424. How much larger was Springfield than Champaign? (*Source:* U.S. Census Bureau)

Sound Examples

77. Until recently, the world's largest permanent maze was located in Ruurlo, Netherlands. This maze of beech hedges covers 94,080 square feet. A new hedge maze using hibiscus bushes at the Dole Plantation in Wahiawa, Hawaii, covers 100,000 square feet. How much larger is the Dole Plantation maze than the Ruurlo maze? (*Source: The Guinness Book of Records*)



78. There were only 27 California condors in the entire world in 1987. To date, the number has increased to an estimated 276 living in the wild. How much of an increase is this? (*Source:* California Department of Fish and Wildlife)



The bar graph shows the top six U.S. airports according to number of passengers arriving and departing in 2016. Use this graph to answer Exercises 79 through 82.

- **79.** Which airport was the busiest?
- **80.** Which airports had 60 million passengers or fewer per year?
- **81.** How many more passengers per year did the Chicago O'Hare International Airport have than the Dallas/Ft. Worth International Airport?
- **82.** How many more passengers per year did the Hartsfield-Jackson Atlanta International Airport have than the Los Angeles International Airport?

Solve.

83. Two seniors, Jo Keen and Trudy Waterbury, were candidates for student government president. Who won the election if the votes were cast as follows? By how many votes did the winner win?

	Candidate	
Class	Jo Trudy	
Freshman	276	295
Sophomore	362	122
Junior	201	312
Senior	179	18



Source: Airports Council International

84. Two students submitted advertising budgets for a student government fund-raiser.

Student A	Student B
\$600	\$300
\$200	\$400
\$150	\$240
\$120	\$170
	\$600 \$200 \$150

If \$1200 is available for advertising, how much excess would each budget have?

Mixed Practice (Sections 1.3 and 1.4) Add or subtract as indicated.

85. 986 <u>+ 48</u>	86. 986 <u>- 48</u>	87. 76 - 67	88. 80 + 93 + 17 + 9 + 2
89. 9000 <u>- 482</u>	90. 10,000 <u>- 1786</u>	91. 10,962 4851 + 7063	92. 12,468 3211 + 1988

Concept Extensions

For each exercise, identify which number is the minuend and which number is the subtrahend. See the Concept Check in this section.

93.	48	94. 2863	
	<u>- 1</u>		

95. Subtract 7 from 70.

96. Find 86 decreased by 25.

Identify each answer as correct or incorrect. Use addition to check. If the answer is incorrect, then write the correct answer.

97. 741	98. 478	99. 1029	100. 7615
<u>- 56</u>	<u>- 89</u>	- 888	<u> </u>
675	389	141	7168

Fill in the missing digits in each problem.

101. 526_	102. 10,_4_
-2_85	- 85_4
28_4	710

103. Is there a commutative property of subtraction? In other words, does order matter when subtracting? Why or why not?

105. The local college library is having a Million Pages of Reading promotion. The freshmen have read a total of 289,462 pages; the sophomores have read a total of 369,477 pages; the juniors have read a total of 218,287 pages; and the seniors have read a total of 121,685 pages. Have they reached a goal of one million pages? If not, how many more pages need to be read?

1.5 Rounding and Estimating 🔘

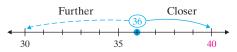
Objective 🗛 Rounding Whole Numbers 🜔

Rounding a whole number means approximating it. A rounded whole number is often easier to use, understand, and remember than the precise whole number. For example, instead of trying to remember the Missouri state population as 6,063,589, it is much easier to remember it rounded to the nearest million: 6,000,000, or 6 million people.(*Source: U.S. Census*)

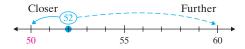
Recall from Section 1.2 that the line below is called a number line. To **graph** a whole number on this number line, we darken the point representing the location of the whole number. For example, the number 4 is graphed below.



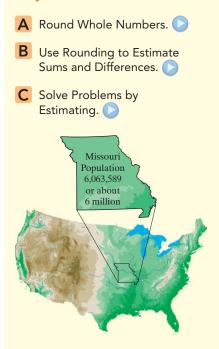
On a number line, the whole number 36 is closer to 40 than 30, so 36 rounded to the nearest ten is 40.



The whole number 52 is closer to 50 than 60, so 52 rounded to the nearest ten is 50.

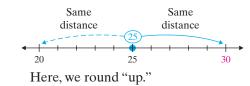


Objectives



^{104.} Explain why the phrase "Subtract 7 from 10" translates to "10 - 7."

In trying to round 25 to the nearest ten, we see that 25 is halfway between 20 and 30. It is not closer to either number. In such a case, we round to the larger ten, that is, to 30.

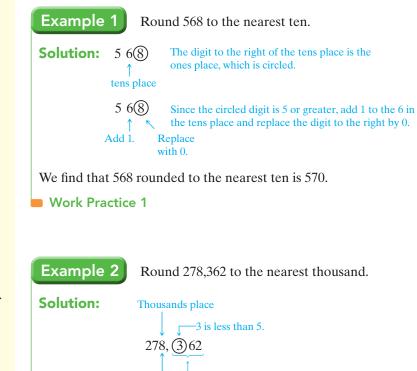


To round a whole number without using a number line, follow these steps:

Rounding Whole Numbers to a Given Place Value

Step 1: Locate the digit to the right of the given place value.

- **Step 2:** If this digit is 5 or greater, add 1 to the digit in the given place value and replace each digit to its right by 0.
- Step 3: If this digit is less than 5, replace it and each digit to its right by 0.



Do not add 1. Replace with zeros.

The number 278,362 rounded to the nearest thousand is 278,000.

Work Practice 2

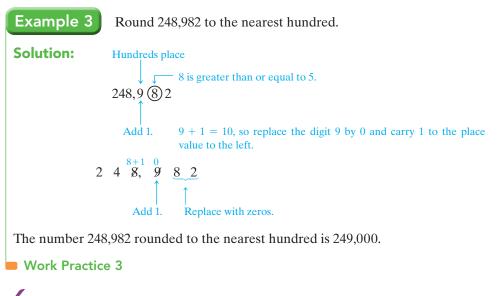
Practice 1
Round to the nearest ten.
a. 57
b. 641
c. 325

Practice 2

Round to the nearest thousand. **a.** 72,304 **b.** 9222 **c.** 671,800

Answers

1. a. 60 **b.** 640 **c.** 330 **2. a.** 72,000 **b.** 9000 **c.** 672,000



Concept Check Round each of the following numbers to the nearest *hundred*. Explain your reasoning.

a. 59 **b.** 29

Objective B Estimating Sums and Differences 🕗

By rounding addends, minuends, and subtrahends, we can estimate sums and differences. An estimated sum or difference is appropriate when the exact number is not necessary. Also, an estimated sum or difference can help us determine if we made a mistake in calculating an exact amount. To estimate the sum below, round each number to the nearest hundred and then add.

768	rounds to	800
1952	rounds to	2000
225	rounds to	200
+ 149	rounds to	+ 100
		3100

The estimated sum is 3100, which is close to the exact sum of 3094.

Example 4	Round each number to the nearest hundred to find sum.	an estimated Practice 4 Round each number to the
294		nearest ten to find an estimated
625		sum.
1071		49
+ 349		25
		32
Solution:		51
Exact:	Estimate:	+98
294 ro	ounds to 300	
625 ro	ounds to 600	
1071 ro	bunds to 1100	
<u>+ 349</u> ro	bunds to ± 300	Answers 3. a. 3500 b. 76,200 c. 979,000
	2300	4. 260
The estimated s	sum is 2300. (The exact sum is 2339.)	Concept Check Answers
Work Practice	re 4	a. 100 b. 0

Practice 3

Round to the nearest hundred. **a.** 3474 **b.** 76,243

c. 978,965

42

Practice 5

Round each number to the nearest thousand to find an estimated difference.

> 3785 - 2479

Example 5 Round each number to the nearest hundred to find an estimated difference.

	4725
_	2879

Solution:

Exact:		Estimate:
4725	rounds to	4700
-2879	rounds to	$\frac{-2900}{1800}$

The estimated difference is 1800. (The exact difference is 1846.)

Work Practice 5

Objective C Solving Problems by Estimating

Making estimates is often the quickest way to solve real-life problems when solutions do not need to be exact.

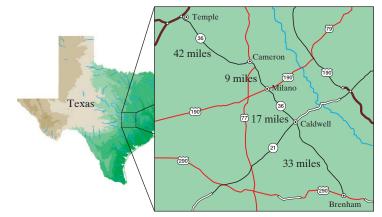
Practice 6

Tasha Kilbey is trying to estimate how far it is from Gove. Kansas, to Hays, Kansas. Round each given distance on the map to the nearest ten to estimate the total distance.



Example 6 **Estimating Distances**

A driver is trying to quickly estimate the distance from Temple, Texas, to Brenham, Texas. Round each distance given on the map to the nearest ten to estimate the total distance.



Solution:

Exact Distance:		Estimate:
42	rounds to	40
9	rounds to	10
17	rounds to	20
+33	rounds to	+30
		100

It is approximately 100 miles from Temple to Brenham. (The exact distance is 101 miles.)

Answers 5. 2000 6. 80 mi

Example 7

Estimating Data

In three months in 2016, the numbers of tons of mail that went through Hartsfield-Jackson Atlanta International Airport were 1993, 2538, and 3033. Round each number to the nearest hundred to estimate the tons of mail that passed through this airport.

Solution:

Exact Tons of Mail:		Estimate:
1993	rounds to	2000
2538	rounds to	2500
+3033	rounds to	+3000
		7500

The approximate tonnage of mail that moved through Atlanta's airport over this period was 7500 tons. (The exact tonnage was 7564 tons.)

Work Practice 7

Answer 7. 21,000 total cases

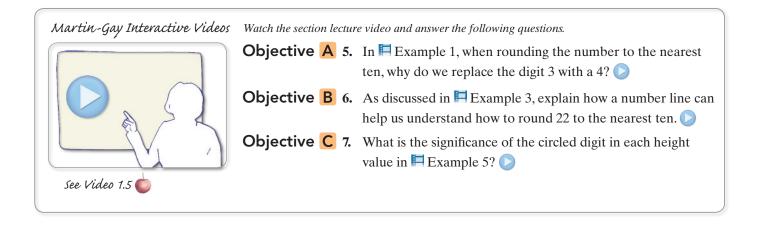
Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank.

60	rounding	exact
70	estimate	graph

- **1.** To ______ a number on a number line, darken the point representing the location of the number.
- 2. Another word for approximating a whole number is _____.
- 3. The number 65 rounded to the nearest ten is ______, but the number 61 rounded to the nearest ten is ______.

4. A(n) ______ number of products is 1265, but a(n) ______ is 1000.



Practice 7

In 2015, there were 2930 reported cases of mumps, 18,166 reported cases of pertussis (whooping cough), and 189 reported cases of measles. Round each number to the nearest thousand to estimate the total number of cases reported for these preventable diseases. (*Source:* Centers for Disease Control)

1.5 Exercise Set MyLab Math 🜔

Objective A *Round each whole number to the given place. See Examples 1 through 3.*

1. 423 to the nearest ten	2. 273 to the nearest ten	3. 635 to the nearest ten
4. 846 to the nearest ten	5. 2791 to the nearest hundred	6. 8494 to the nearest hundred
7. 495 to the nearest ten	8. 898 to the nearest ten	9. 21,094 to the nearest thousand
10. 82,198 to the nearest thousand	11. 33,762 to the nearest thousand	12. 42,682 to the nearest ten-thousand
13. 328,495 to the nearest hundred	14. 179,406 to the nearest hundred	15. 36,499 to the nearest thousand
16. 96,501 to the nearest thousand	17. 39,994 to the nearest ten	18. 99,995 to the nearest ten
19. 29,834,235 to the nearest ten-milli	on 20. 39,523,698 t	to the nearest million

Complete the table by estimating the given number to the given place value.

		Tens	Hundreds	Thousands
21.	5281			
22.	7619			
23.	9444			
24.	7777			
25.	14,876			
26.	85,049			

Round each number to the indicated place.

- **27.** The University of California, Los Angeles, had a total undergraduate enrollment of 27,214 students in fall 2016. Round this number to the nearest thousand. (*Source:* UCLA)
- **29.** Kareem Abdul-Jabbar holds the NBA record for points scored, a total of 38,387 over his NBA career. Round this number to the nearest thousand. (*Source:* National Basketball Association)
- **31.** In 2016, the most valuable brand in the world was Apple, Inc. The estimated brand value of Apple was \$154,118,000,000. Round this to the nearest ten billion. (*Source: Forbes*)

- **28.** In 2016, there were 15,667 Burger King restaurants worldwide. Round this number to the nearest thousand. (*Source:* Burger King Worldwide, Inc.)
- **30.** It takes 60,149 days for Neptune to make a complete orbit around the Sun. Round this number to the nearest hundred. (*Source:* National Space Science Data Center)
- **32.** According to the U.S. Population Clock, the population of the United States was 324,758,293 in March 2017. Round this population figure to the nearest million. (*Source:* U.S. Census population clock)

- **33.** The average salary for a professional baseball player in 2016 was \$4,155,907. Round this average salary to the nearest hundred thousand. (*Source: ESPN*)
- **35.** The United States currently has 219,600,000 smart phone users. Round this number to the nearest million. (*Source:* Pew Internet Research)
- **34.** The average salary for a professional football player in 2016 was \$2,110,000. Round this average salary to the nearest million. (*Source: ESPN*)
- **36.** U.S. farms produced 15,226,000,000 bushels of corn in 2016. Round the corn production figure to the nearest ten million. (*Source:* U.S. Department of Agriculture)





Objective B *Estimate the sum or difference by rounding each number to the nearest ten. See Examples 4 and 5.*

37. 39	38. 52	39. 449	40. 555
45	33	<u>-373</u>	-235
22	15		
+17	+29		

Estimate the sum or difference by rounding each number to the nearest hundred. See Examples 4 and 5.

41. 191	42. 4050	43. 1774	44. 1989	45. 3995	46. 799
188	3133	- 1492	-1870	2549	1655
+192	+1220			+4944	+ 271

Three of the given calculator answers below are incorrect. Find them by estimating each sum.

47. 463 + 219 602	48. 522 + 785 1307	
49. 229 + 443 + 606 1278	50. 542 + 789 + 198 2139	Helpful Hint Estimation is useful to check for incorrect answers when using a calculator. For example, pressing a key too hard may re- sult in a double digit, while pressing a key too
51. 7806 + 5150 12,956	52. 5233 + 4988 9011	softly may result in the digit not appearing in the display.

Objective C Solve each problem by estimating. See Examples 6 and 7.

- **53.** An appliance store advertises three refrigerators on sale at \$899, \$1499, and \$999. Round each cost to the nearest hundred to estimate the total cost.
- **55.** The distance from Kansas City to Boston is 1429 miles and from Kansas City to Chicago is 530 miles. Round each distance to the nearest hundred to estimate how much farther Boston is from Kansas City than Chicago is.
- 57. The peak of Denali, in Alaska, is 20,320 feet above sea level. The top of Mt. Rainier, in Washington, is 14,410 feet above sea level. Round each height to the nearest thousand to estimate the difference in elevation of these two peaks.(*Source:* U.S. Geological Survey)
 - **59.** In 2014, the United States Postal Service delivered 155,410,000,000 pieces of mail. In 2016, it delivered 154,239,000,000 pieces of mail. Round each number to the nearest billion to estimate how much the mail volume decreased from 2014 to 2016. (*Source:* United States Postal Service)



61. Head Start is a national program that provides developmental and social services for America's low-income preschool children ages three to five. Enrollment figures in Head Start programs showed a decrease from 1,128,030 in 2012 to 946,357 in 2016. Round each number of children to the nearest thousand to estimate this decrease. (*Source:* U.S. Department of Health and Human Services)

- **54.** Suppose you scored 89, 97, 100, 79, 75, and 82 on your biology tests. Round each score to the nearest ten to estimate your total score.
- **56.** The Gonzales family took a trip and traveled 588, 689, 277, 143, 59, and 802 miles on six consecutive days. Round each distance to the nearest hundred to estimate the distance they traveled.
- **58.** A student is pricing new car stereo systems. One system sells for \$1895 and another system sells for \$1524. Round each price to the nearest hundred dollars to estimate the difference in price of these systems.
- **60.** Round each distance given on the map to the nearest ten to estimate the total distance from North Platte, Nebraska, to Lincoln, Nebraska.



62. Enrollment figures at a local community college showed an increase from 49,713 credit hours in 2015 to 51,746 credit hours in 2016. Round each number to the nearest thousand to estimate the increase.

Mixed Practice (Sections 1.2 and 1.5) The following table shows the top five countries that spent the most in mobile Internet advertising in 2015 and the amount of money spent that year on advertising. Complete this table. The first *line is completed for you. (Source:* eMarketer)

	Country	Amount Spent on Mobile Internet Advertising in 2015 (in millions of dollars)	Amount Written in Standard Form	Standard Form Rounded to Nearest Hundred-Million	Standard Form Rounded to Nearest Billion
	United States	\$28,240	\$28,240,000,000	\$28,200,000,000	\$28,000,000,000
63.	China	\$12,140			
64.	Japan	\$3370			
65.	Germany	\$2110			
66.	United Kingdom	\$4670)

Concept Extensions

- **67.** Find one number that when rounded to the nearest hundred is 5700.
- **68.** Find one number that when rounded to the nearest ten is 5700.

Round each number to the nearest hundred. See the Concept Check in this section.

69. 999 **70.** 950

- **71.** 38 **72.** 48
- A number rounded to the nearest hundred is 8600. Use this for Exercise 73 and 74.
- **73.** Determine the smallest possible number. **74.** Determine the largest possible number.
- **75.** In your own words, explain how to round a number **76.** In your own words, explain how to round 9660 to the to the nearest thousand.
 - nearest thousand.
- \triangle **77.** Estimate the perimeter of the rectangle by first rounding the length of each side to the nearest ten.

54 meters	
Rectangle	17 meters

 \triangle **78.** Estimate the perimeter of the triangle by first rounding the length of each side to the nearest hundred.

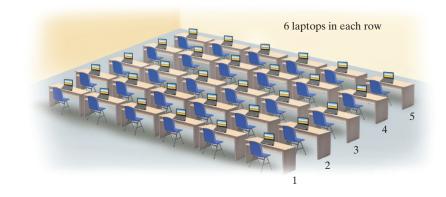


1.6 Multiplying Whole Numbers and Area 🔘

Objectives

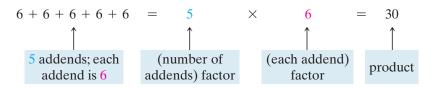
- A Use the Properties of Multiplication.
- B Multiply Whole Numbers.
- C Multiply by Whole Numbers Ending in Zero(s).
- D Find the Area of a Rectangle.
- E Solve Problems by Multiplying Whole Numbers.

Multiplication Shown as Repeated Addition Suppose that we wish to count the number of laptops provided in a computer class. The laptops are arranged in 5 rows, and each row has 6 laptops.



Adding 5 sixes gives the total number of laptops. We can write this as 6 + 6 + 6 + 6 = 30 laptops. When each addend is the same, we refer to this as **repeated addition.**

Multiplication is repeated addition but with different notation.



The \times is called a **multiplication sign.** The numbers 5 and 6 are called **factors.** The number 30 is called the **product.** The notation 5×6 is read as "five times six." The symbols \cdot and () can also be used to indicate multiplication.

$$5 \times 6 = 30$$
, $5 \cdot 6 = 30$, $(5)(6) = 30$, and $5(6) = 30$

Concept Check

- **a.** Rewrite 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 using multiplication.
- **b.** Rewrite 3×16 as repeated addition. Is there more than one way to do this? If so, show all ways.

Objective A Using the Properties of Multiplication 🕑

As with addition, we memorize products of one-digit whole numbers and then use certain properties of multiplication to multiply larger numbers. (If necessary, review the multiplication of one-digit numbers in Appendix A.2)

Notice that when any number is multiplied by 0, the result is always 0. This is called the **multiplication property of 0.**

Concept Check Answers

- **a.** $7 \times 5 = 35$

Multiplication Property of 0

The product of 0 and any number is 0. For example,

 $5 \cdot 0 = 0$ and $0 \cdot 8 = 0$

Also notice in Appendix A.2 that when any number is multiplied by 1, the result is always the original number. We call this result the **multiplication property of 1.**

Multiplication Property of 1

The product of 1 and any number is that same number. For example,

 $1 \cdot 9 = 9$ and $6 \cdot 1 = 6$

Example 1Multiply.a. 6×1 b. 0(18)c. $1 \cdot 45$ d. (75)(0)Solution:a. $6 \times 1 = 6$ b. 0(18) = 0c. $1 \cdot 45 = 45$ d. (75)(0) = 0

Practice 1
Multiply.
a. 3 × 0
b. 4(1)
c. (0)(34)
d. 1 ⋅ 76

Work Practice 1

Like addition, multiplication is commutative and associative. Notice that when multiplying two numbers, the order of these numbers can be changed without changing the product. For example,

 $3 \cdot 5 = 15$ and $5 \cdot 3 = 15$

This property is the commutative property of multiplication.

Commutative Property of Multiplication

Changing the order of two factors does not change their product. For example,

 $9 \cdot 2 = 18$ and $2 \cdot 9 = 18$

Another property that can help us when multiplying is the **associative property of multiplication.** This property states that when multiplying numbers, the grouping of the numbers can be changed without changing the product. For example,

$$\underbrace{(2\cdot 3)}_{} \cdot 4 = 6 \cdot 4 = 24$$

Also,

$$2 \cdot \underbrace{(3 \cdot 4)}_{} = 2 \cdot 12 = 24$$

Both groupings give a product of 24.

Answers 1. a. 0 b. 4 c. 0 d. 76

Associative Property of Multiplication

Changing the **grouping** of factors does not change their product. From the previous page, we know that for example,

 $(2\cdot 3)\cdot 4 = 2\cdot (3\cdot 4)$

With these properties, along with the **distributive property**, we can find the product of any whole numbers. The distributive property says that multiplication **distributes** over addition. For example, notice that 3(2 + 5) simplifies to the same number as $3 \cdot 2 + 3 \cdot 5$.

$$3(2+5) = 3(7) = 21$$

 $3 \cdot 2 + 3 \cdot 5 = 6 + 15 = 21$

Since 3(2 + 5) and $3 \cdot 2 + 3 \cdot 5$ both simplify to 21, then

 $3(2+5) = 3 \cdot 2 + 3 \cdot 5$

Notice in $3(2+5) = 3 \cdot 2 + 3 \cdot 5$ that each number inside the parentheses is multiplied by 3.

Distributive Property

Multiplication distributes over addition. For example,

 $2(3+4) = 2 \cdot 3 + 2 \cdot 4$

Example 2 Rewrite each using the distributive property.

a. 3(4+5)

b. 10(6+8) **c.** 2(7+3)

Solution: Using the distributive property, we have

- **a.** $3(4+5) = 3 \cdot 4 + 3 \cdot 5$
- **b.** $10(6+8) = 10 \cdot 6 + 10 \cdot 8$

c.
$$2(7+3) = 2 \cdot 7 + 2 \cdot 3$$

Work Practice 2

Objective **B** Multiplying Whole Numbers 🜔

Let's use the distributive property to multiply 7(48). To do so, we begin by writing the expanded form of 48 (see Section 1.2) and then applying the distributive property.

7(48) = 7(40 + 8)	Write 48 in expanded form.
$= 7 \cdot 40 + 7 \cdot 8$	Apply the distributive property.
= 280 + 56	Multiply.
= 336	Add.

Practice 2

Rewrite each using the distributive property.

a. 5(2+3)

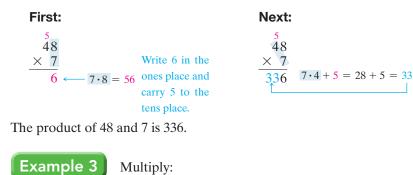
b. 9(8 + 7)

c. 3(6+1)

2. a. $5(2+3) = 5 \cdot 2 + 5 \cdot 3$

Answers

b. $9(8+7) = 9 \cdot 8 + 9 \cdot 7$ **c.** $3(6+1) = 3 \cdot 6 + 3 \cdot 1$ This is how we multiply whole numbers. When multiplying whole numbers, we will use the following notation.



b.

b.

246

 \times 5

23 246

 \times 5

1230

Pra	actice	3	
Mu	ltiply.		
a.	36	b.	
-	\times 4		\times

132

9

Work Practice 3

a.

a.

25

 \times 8

Solution:

25

 \times 8

200

To multiply larger whole numbers, use the following similar notation. Multiply 89 \times 52.

Step 1	Step 2	Step 3
1 89	4 89	89
\times 52	$\times 52$	\times 52
$178 \leftarrow Multiply 89 \times 2.$	178	178
	<u>4450</u> ← Multiply 89 × 50.	4450
		4628 ← Add.

The numbers 178 and 4450 are called **partial products.** The sum of the partial products, 4628, is the product of 89 and 52.

Example 4 Multiply: 236×86 Solution: 236 $\frac{\times 86}{1416} \leftarrow 6(236)$ $\frac{18880}{20,296} \leftarrow 80(236)$ 20,296 Add.	Practice 4 Multiply. a. 594 b. 306 <u>× 72</u> <u>× 81</u>
Example 5 Multiply: 631×125 Solution: 631 $\frac{\times 125}{3155} \leftarrow 5(631)$ $12620 \leftarrow 20(631)$	Practice 5 Multiply. a. 726 b. 288 ×142 × 4
$\frac{63100}{78,875} \leftarrow 100(631)$ Work Practice 5	Answers3. a. 144b. 11884. a. 42,768b. 24,7865. a. 103,092b. 1152

Concept Check Find and explain the error in the following multiplication problem.

 $\begin{array}{r}
102 \\
\times 33 \\
\overline{306} \\
306 \\
\overline{612}
\end{array}$

Objective C Multiplying by Whole Numbers Ending in Zero(s)

Interesting patterns occur when we multiply by a number that ends in zeros. To see these patterns, let's multiply a number, say 34, by 10, then 100, then 1000.

```
1 \text{ zero}
34 \cdot 10 = 340
2 \text{ zeros}
34 \cdot 100 = 3400
3 \text{ zeros}
34 \cdot 1000 = 34,000
3 \text{ zeros attached to 34.}
```

These patterns help us develop a shortcut for multiplying by whole numbers ending in zeros.

To multiply by 10, 100, 1000, and so on,

Form the product by attaching the number of zeros in that number to the other factor.

For example, $41 \cdot 100 = 4100$.

 Examples
 Multiply.

 6. $176 \cdot 1000 = 176,000$ Attach 3 zeros.

 7. $2041 \cdot 100 = 204,100$ Attach 2 zeros.

 Work Practice 6–7

We can use a similar format to multiply by any whole number ending in zeros. For example, since

 $15 \cdot 500 = 15 \cdot 5 \cdot 100$,

we find the product by multiplying 15 and 5, then attaching two zeros to the product.

$$\begin{array}{c} \stackrel{2}{15} \quad 15 \cdot 500 = 7500 \\ \times \begin{array}{c} 5 \\ 75 \end{array}$$

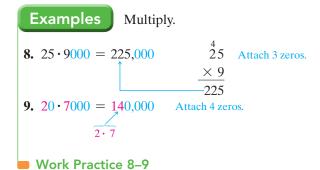
Practice 6–7 Multiply.

6. 75 ⋅ 1007. 808 ⋅ 1000

Answers

6. 7500 7. 808,000✓ Concept Check Answer

 $\begin{array}{r}
102 \\
\times 33 \\
\hline
306 \\
3060 \\
\overline{3366}
\end{array}$



 Practice 8–9

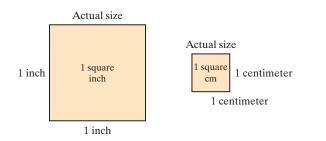
 Multiply.

 8. 35 ⋅ 3000

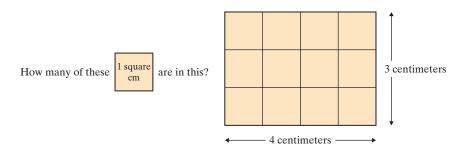
 9. 600 ⋅ 600

Objective D Finding the Area of a Rectangle

A special application of multiplication is finding the **area** of a region. Area measures the amount of surface of a region. For example, we measure a plot of land or the living space of a home by its area. The figures below show two examples of units of area measure. (A centimeter is a unit of length in the metric system.)



For example, to measure the area of a geometric figure such as the rectangle below, count the number of square units that cover the region.



This rectangular region contains 12 square units, each 1 square centimeter. Thus, the area is 12 square centimeters. This total number of squares can be found by counting or by multiplying $4 \cdot 3$ (length \cdot width).

Area of a rectangle = length · width = (4 centimeters)(3 centimeters) = 12 square centimeters

In this section, we find the areas of rectangles only. In later sections, we will find the areas of other geometric regions.

Helpful Hint

Notice that area is measured in **square** units while perimeter is measured in units.

Practice 10

The state of Wyoming is in the shape of a rectangle whose length is 360 miles and whose width is 280 miles. Find its area.

Example 10 Finding the Area of a State

The state of Colorado is in the shape of a rectangle whose length is 380 miles and whose width is 280 miles. Find its area.

Solution: The area of a rectangle is the product of its length and its width.

- Area = length \cdot width = (380 miles)(280 miles)
 - = 106,400 square miles



The area of Colorado is 106,400 square miles.

Work Practice 10

Objective E Solving Problems by Multiplying 💟



There are several words or phrases that indicate the operation of multiplication. Some of these are as follows:

Multiplication			
Key Words or Phrases Examples Symbol			
multiply	multiply 5 by 7	5.7	
product	the product of 3 and 2	3.2	
times	10 times 13	10.13	

Many key words or phrases describing real-life problems that suggest addition might be better solved by multiplication instead. For example, to find the total cost of 8 shirts, each selling for \$27, we can either add

27 + 27 + 27 + 27 + 27 + 27 + 27 + 27

or we can multiply 8(27).

Practice 11

A particular computer printer can print 16 pages per minute in color. How many pages can it print in 45 minutes?

Finding DVD Space Example 11

A digital video disc (DVD) can hold about 4800 megabytes (MB) of information. How many megabytes can 12 DVDs hold?

Solution: Twelve DVDs will hold 12×4800 megabytes.

In Words		Translate to Numbers
megabytes per disc	\rightarrow	4800
\times number of DVDs	\rightarrow	$\times 12$
		9600
		48000
total megabytes		57,600

Twelve DVDs will hold 57,600 megabytes.

Work Practice 11

Example 12 **Budgeting Money**

Suzanne Scarpulla and a friend plan to take their children to the New England Aquarium in Boston. The peak hour ticket price for each child is \$19 and for each adult \$27. If five children and two adults plan to go, how much money is needed for admission? (Source: New England Aquarium)

Solution: If the price of one child's ticket is \$19, the cost for 5 children is $5 \times 19 =$ \$95. The price of one adult ticket is \$27, so the cost for two adults is $2 \times 27 =$ \$54. The total cost is:

In Words

cost for 5 children 95 + cost for 2 adults + 54total cost 149

The total cost is \$149.

Work Practice 12

Translate to Numbers



Example 13

Estimating Word Count

The average page of a book contains 259 words. Estimate, rounding each number to the nearest hundred, the total number of words contained on 212 pages.

Solution: The exact number of words is 259×212 . Estimate this product by rounding each factor to the nearest hundred.

> 259 rounds to 300 $300 \times 200 = 60,000$ $\times 212$ $\times 200,$ rounds to $3 \cdot 2 = 6$

There are approximately 60,000 words contained on 212 pages.

Work Practice 13

Practice 12

Ken Shimura purchased DVDs and CDs through a club. Each DVD was priced at \$11, and each CD cost \$9. Ken bought eight DVDs and five CDs. Find the total cost of the order.

Practice 13

If an average page in a book contains 163 words, estimate, rounding each number to the nearest hundred, the total number of words contained on 391 pages.

Answers 12. \$133 13. 80,000 words

Calculator Explorations Multiplying Numbers

To multiply numbers on a calculator, find the keys marked \times and = or ENTER. For example, to find 31 · 66 on a

Use a calculator to multiply.

	1. 72×48	2. 81 × 92
calculator, press the keys 31×66 then $=$ or ENTER.	3. 163 • 94	4. 285 • 144
The display will read 2046 . Thus, $31 \cdot 66 = 2046$.	5. 983(277)	6. 1562(843)

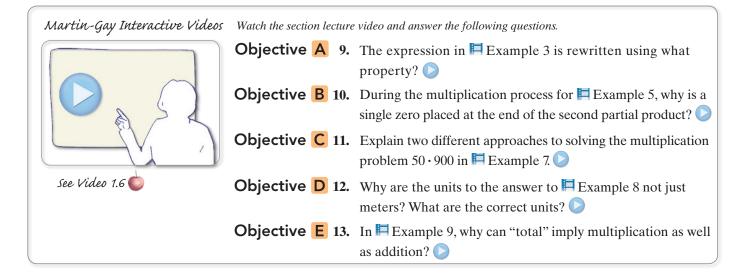
Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank.

area	grouping	commutative	1	product	length
factor	order	associative	0	distributive	number

1. The product of 0 and any number is _____.

- 2. The product of 1 and any number is the _____.
- 3. In $8 \cdot 12 = 96$, the 96 is called the _____ and 8 and 12 are each called a(n) _____.
- 4. Since $9 \cdot 10 = 10 \cdot 9$, we say that changing the _____ in multiplication does not change the product. This property is called the _____ property of multiplication.
- 5. Since $(3 \cdot 4) \cdot 6 = 3 \cdot (4 \cdot 6)$, we say that changing the ______ in multiplication does not change the product. This property is called the ______ property of multiplication.
- **6.** _____ measures the amount of surface of a region.
- 7. Area of a rectangle = $\dots \cdot$ width.
- 8. We know $9(10 + 8) = 9 \cdot 10 + 9 \cdot 8$ by the _____ property.



1.6 Exercise	e Set MyLab Math		
Objective A <i>Mult</i>	ply. See Example 1.		
○ 1. 1·24	2. 55 · 1	3. 0 • 19	4. 27 · 0
5. 8.0.9	6. 7 • 6 • 0	7. 87 · 1	8. 1 • 41

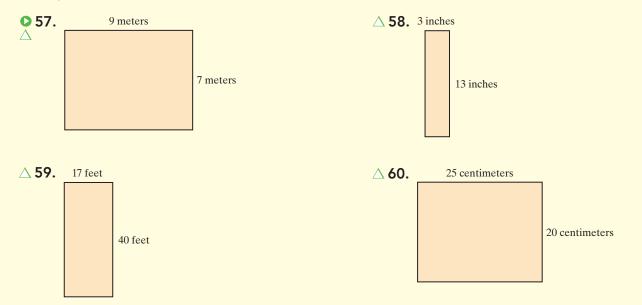
Use the distributive property	to rewrite each expression. See Example 2.
9. 6(3 + 8)	10. $5(8+2)$

12. 6(1+4) **13.** 20(14+6) **14.** 12(12+3)

11. 4(3 + 9)

Objective B Multiply. See Example 3.					
15. 64 <u>× 8</u>	$16. 79 \\ \times 3$		17. 613×6	18. 6	538 5
● 19. 277 × 6	20. 882 × 2		21. 1074 × 6	22. 902	21 × 3
Objectives A	B Mixed Practice	Multiply. See 1	Examples 1 through 5	i.	
23. 89 × 13	24. 91 25	$5. 421 \\ \times 58$	26. 526 <u>× 23</u>	27. 306 <u>× 81</u>	28. 708 <u>× 21</u>
29. (780)(20)	30. (720)(80)	31. (49	5)(13)(0) 32.	(593)(47)(0) 3	3. (640)(1)(10)
34. (240)(1)(20) 35. 1234 × 39	36. 135	7 × 79 37.	609 × 234 3	8. 807 × 127
● 39. 8649 × 274	40. 1234 41 <u>× 567</u>	$589 \\ \times 110$	42. 426 <u>×110</u>	43. 1941 × 2035	44. 1876 ×1407
Objective C Multiply. See Examples 6 through 9.					
● 45. 8 × 100	46. 6 × 100 47	. 11 × 1000	48. 26 × 1000	49. 7406 • 10	50. 9054 · 10
51. 6 • 4000	52. 3 · 9000 • 53	3. 50 • 900	54. 70 · 300	55. 41 • 80,000	56. 27 • 50,000

Objective D Mixed Practice (Section 1.3) Find the area and the perimeter of each rectangle. See Example 10.



Objective E Mixed Practice (Section 1.5) *Estimate the products by rounding each factor to the nearest* hundred. See Example 13.

	61. 576 × 354	62. 982 × 650	63. 604 × 451	64. 111 × 999
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Without actually calculating, mentally round, multiply, and choose the best estimate.

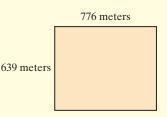
65. 38 × 42 =	66. 2872 × 12 =	67. 612 × 29 =	68. 706 × 409 =
a. 16	a. 2872	a. 180	a. 280
b. 160	b. 28,720	b. 1800	b. 2800
c. 1600	c. 287,200	c. 18,000	c. 28,000
d. 16,000	d. 2,872,000	d. 180,000	d. 280,000

Objectives D E Mixed Practice–Translating Solve. See Examples 10 through 13.

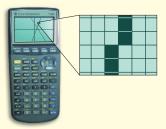
69.	Multiply 80 by 11.	70. Multiply 70 by 12.	71. Find the product of 6 and 700.
72.	Find the product of 9 and 900.	73. Find 2 times 2240.	74. Find 3 times 3310.
0 75.	One tablespoon of olive oil contain How many calories are in 3 tablesp oil? (<i>Source: Home and Garden Bu</i> U.S. Department of Agriculture)	oons of olive	One ounce of hulled sunflower seeds contains 14 grams of fat. How many grams of fat are in 8 ounces of hulled sunflower seeds? (<i>Source: Home</i> <i>and Garden Bulletin No. 72</i> , U.S. Department of Agriculture)
77.	The textbook for a course in biolog There are 35 students in the class. F cost of the biology books for the cla	ind the total	The seats in a lecture hall are arranged in 14 rows with 34 seats in each row. Find how many seats are in this room.
79.	Cabot Creamery is packing a pallet of cheddar cheese to send to a loca There are five layers of boxes on th each layer is four boxes wide by fiv a . How many boxes are in one laye b . How many boxes are on the pal c . What is the weight of the cheese	l restaurant. e pallet, and e boxes deep. er? let?	An apartment building has <i>three floors</i>. Each floor has five rows of apartments with four apartments in each row.a. How many apartments are on 1 floor?b. How many apartments are in the building?

- \triangle 81. A plot of land measures 80 feet by 110 feet. Find its \triangle 82. A house measures 45 feet by 60 feet. Find the floor area.
 - area of the house.

- \triangle 83. The largest hotel lobby can be found at the Hyatt Regency in San Francisco, CA. It is in the shape of a rectangle that measures 350 feet by 160 feet. Find its area.
- \triangle 84. Recall from an earlier section that the world's largest commercial building under one roof is the flower auction building of the cooperative VBA in Aalsmeer, Netherlands. The floor plan is a rectangle that measures 776 meters by 639 meters. Find the area of this building. (*Source: The Handy Science Answer Book*, Visible Ink Press)



85. A pixel is a rectangular dot on a graphing calculator screen. If a graphing calculator screen contains 62 pixels in a row and 94 pixels in a column, find the total number of pixels on a screen.



- **87.** A line of print on a computer contains 60 characters (letters, spaces, punctuation marks). Find how many characters there are in 35 lines.
- **89.** One ounce of Planters[®] Dry Roasted Peanuts has 170 calories. How many calories are in 8 ounces? (*Source:* Kraft Foods)
- **91.** The Thespian club at a local community college is ordering T-shirts. T-shirts size S, M, or L cost \$10 each and T-shirts size XL or XXL cost \$12 each. Use the table below to find the total cost. (The first row is filled in for you.)

	Number of		Cost per Size
T-Shirt Size	Shirts Ordered	Cost per Shirt	Ordered
S	4	\$10	\$40
М	6		
L	20		
XL	3		
XXL	3		

86. A certain compact disc (CD) can hold 700 megabytes (MB) of information. How many MB can 17 discs hold?



- **88.** An average cow eats 3 pounds of grain per day. Find how much grain a cow eats in a year. (Assume 365 days in 1 year.)
- **90.** One ounce of Planters[®] Dry Roasted Peanuts has 14 grams of fat. How many grams of fat are in 16 ounces? (*Source:* Kraft Foods)
- **92.** The student activities group at North Shore Community College is planning a trip to see the local minor league baseball team. Tickets cost \$5 for students, \$7 for nonstudents, and \$2 for children under 12. Use the following table to find the total cost.

	Number of	Cost per	Cost per
Person	Persons	Person	Category
Student	24	\$5	\$120
Nonstudent	4		
Children under 12	5		

93. Celestial Seasonings of Boulder, Colorado, is a tea company that specializes in herbal teas, accounting for over \$100,000,000 in herbal tea blend sales in the United States annually. Their plant in Boulder has bagging machines capable of bagging over 1000 bags of tea per minute. If the plant runs 24 hours a day, how many tea bags are produced in one day? (*Source:* Celestial Seasonings)
94. The number of "older" Americans (ages 65 and older) has increased sixteenfold since 1900. If there were 3 million "older" Americans in 1900, how many were there in 2016? (*Source:* U.S. Census Bureau)

Mixed Practice (Sections 1.3, 1.4, and 1.6) Perform each indicated operation.

95. 128	96. 126	97. 134
+ 7	<u> </u>	\times 16
98. 47 + 26 + 10 + 231 + 50	99. Find the sum of 19 and 4.	100. Find the product of 19 and 4.

101. Find the difference of 19 and 4. **102.** Find the total of 19 and 4.

Concept Extensions

Solve. See the first Concept Check in this section.

103. Rewrite 7 + 7 + 7 + 7 using multiplication.

104. Rewrite 11 + 11 + 11 + 11 + 11 + 11 using multiplication.

105. a. Rewrite $3 \cdot 5$ as repeated addition.	106. a. Rewrite 4 · 5 as repeated addition.
b. Explain why there is more than one way	b. Explain why there is more than one way to do this.
to do this.	

Find and explain the error in each multiplication problem. See the second Concept Check in this section.

107. 203	108. 31
\times 14	\times 50
812	155
203	
1015	

Fill in the missing digits in each problem.

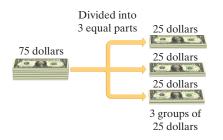
109. 4_	110. _7
$\times _3$	× 6_
126	171
3780	3420
3906	3591

- **111.** Explain how to multiply two 2-digit numbers using partial products.
 - **113.** A window washer in New York City is bidding for a contract to wash the windows of a 23-story building. To write a bid, the number of windows in the building is needed. If there are 7 windows in each row of windows on 2 sides of the building and 4 windows per row on the other 2 sides of the building, find the total number of windows.
- **112.** In your own words, explain the meaning of the area of a rectangle and how this area is measured.
 - **114.** During the 2015–2016 NBA regular season, Stephen Curry of the Golden State Warriors was named the Most Valuable Player. He scored 402 three-point field goals, 403 two-point field goals, and 363 free throws (worth one point each). How many points did Stephen Curry score during the 2015–2016 regular season? (*Source:* National Basketball Association)

1.7

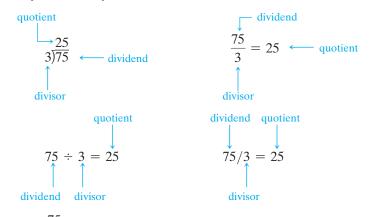
Dividing Whole Numbers 🔘

Suppose three people pooled their money and bought a raffle ticket at a local fundraiser. Their ticket was the winner, and they won a \$75 cash prize. They then divided the prize into three equal parts so that each person received \$25.



Objective 🗛 Dividing Whole Numbers 🕑

The process of separating a quantity into equal parts is called **division**. The division above can be symbolized by several notations.

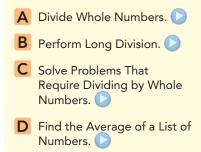


(In the notation $\frac{75}{3}$, the bar separating 75 and 3 is called a **fraction bar**.) Just as subtraction is the reverse of addition, division is the reverse of multiplication. This means that division can be checked by multiplication.

3)75 because
$$25 \cdot 3 = 75$$

Quotient \cdot Divisor $=$ Dividend

Objectives



Since multiplication and division are related in this way, you can use your knowledge of multiplication facts (or study Appendix A.2) to review quotients of one-digit divisors if necessary.

- **Example 1** Find each quotient. Check by multiplying.
- **a.** $42 \div 7$ **b.** $\frac{64}{8}$ **c.** $3\overline{)21}$ **Solution: a.** $42 \div 7 = 6$ because $6 \cdot 7 = 42$ **b.** $\frac{64}{8} = 8$ because $8 \cdot 8 = 64$ **c.** $3\overline{)21}$ because $7 \cdot 3 = 21$
- Work Practice 1

Find each quotient. Check by multiplying. 7

Practice 2

a.
$$\frac{1}{7}$$

b. $3 \div 1$
c. $1\overline{)11}$
d. $4 \div 1$
e. $\frac{10}{1}$
f. $21 \div 21$

 Example 2
 Find each quotient. Check by multiplying.

 a. $1\overline{)7}$ b. $12 \div 1$ c. $\frac{6}{6}$ d. $9 \div 9$ e. $\frac{20}{1}$ f. $19\overline{)19}$

 Solution:

 a. $1\overline{)7}$ because $7 \cdot 1 = 7$ b. $12 \div 1 = 12$ because $12 \cdot 1 = 12$

 c. $\frac{6}{6} = 1$ because $1 \cdot 6 = 6$ d. $9 \div 9 = 1$ because $1 \cdot 9 = 9$

 e. $\frac{20}{1} = 20$ because $20 \cdot 1 = 20$ f. $19\overline{)19}$ because $1 \cdot 19 = 19$

Work Practice 2

Example 2 illustrates the important properties of division described next:

Division Properties of 1

a. 9)0

Solution:

c. $\frac{0}{5} = 0$ because $0 \cdot 5 = 0$

The quotient of any number (except 0) and that same number is 1. For example,

$$8 \div 8 = 1$$
 $\frac{5}{5} = 1$ $4\overline{5}$

The quotient of any number and 1 is that same number. For example,

b. $0 \div 12$ **c.** $\frac{0}{5}$ **d.** $\frac{3}{0}$

a. 9)0 because $0 \cdot 9 = 0$ **b.** $0 \div 12 = 0$ because $0 \cdot 12 = 0$

$$9 \div 1 = 9$$
 $\frac{6}{1} = 6$ $1\overline{)3}$ $\frac{0}{1} = 0$

Example 3 Find each quotient. Check by multiplying.

Practice 3

Find each quotient. Check by multiplying.

a.
$$\frac{0}{7}$$
 b. $8)\overline{0}$

c.
$$5 \div 0$$
 d. $0 \div 14$

Answers

1. a. 8 **b.** 8 **c.** 4 **2. a.** 1 **b.** 5 **c.** 11 **d.** 4 **e.** 10 **f.** 1 **3. a.** 0 **b.** 0 **c.** undefined **d.** 0

Practice 1

c. $\frac{24}{6}$

Find each quotient. Check by multiplying. **a.** $9\overline{)72}$ **b.** $40 \div 5$ **d.** If $\frac{3}{0} = a$ number, then the number times 0 = 3. Recall from Section 1.6 that any number multiplied by 0 is 0 and not 3. We say, then, that $\frac{3}{0}$ is **undefined**.

Work Practice 3

Example 3 illustrates important division properties of 0.

Division Properties of 0

The quotient of 0 and any number (except 0) is 0. For example,

$$0 \div 9 = 0$$
 $\frac{0}{5} = 0$ $14\overline{)0}$

The quotient of any number and 0 is not a number. We say that

 $\frac{3}{0}$, $0\overline{)3}$, and $3 \div 0$

are undefined.

Objective **B** Performing Long Division 🕗



When dividends are larger, the quotient can be found by a process called **long division.** For example, let's divide 2541 by 3.

divisor
$$\rightarrow 3)2541$$

 \uparrow
dividend

We can't divide 3 into 2, so we try dividing 3 into the first two digits.

 $\frac{8}{3)2541}$ 25 ÷ 3 = 8 with 1 left, so our best estimate is 8. We place 8 over the 5 in 25.

Next, multiply 8 and 3 and subtract this product from 25. Make sure that this difference is less than the divisor.

 $\frac{8}{3)2541}$ $\frac{-24}{1}$ $\frac{8(3) = 24}{25 - 24 = 1, \text{ and } 1 \text{ is less than the divisor } 3.$

Bring down the next digit and go through the process again.

$$\begin{array}{r}
84 \\
3)\overline{2541} \\
-24 \\
14 \\
-12 \\
2 \\
14 \\
-12 \\
2
\end{array}$$
14 ÷ 3 = 4 with 2 left
14 = 12 \\
14 \\
-12 = 2

Once more, bring down the next digit and go through the process.

84 <mark>7</mark> 3)2541	$21 \div 3 = 7$
-24	
14	
-12	
21	
-21	7(3) = 21
0	21 - 21 = 0

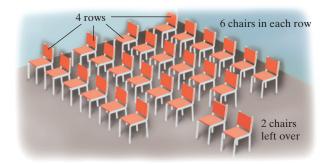
The quotient is 847. To check, see that $847 \times 3 = 2541$.

Chapter 1 | The Whole Numbers

Example 4 **Practice 4** Divide: $3705 \div 5$. Check by multiplying. Divide. Check by multiplying. Solution: **a.** 4908 ÷ 6 $37 \div 5 = 7$ with 2 left. Place this estimate, 7, over the 7 in 37. 7 **b.** 2212 ÷ 4 5)3705 **c.** 753 ÷ 3 -35 7(5) = 3520 37 - 35 = 2, and 2 is less than the divisor 5. Bring down the 0. 74 $20 \div 5 = 4$ 5)3705 -35 20 -204(5) = 2020 - 20 = 0, and 0 is less than the divisor 5. 05 Bring down the 5. 741 $5 \div 5 = 1$ 5)3705 -35 20 -20 5 __5 1(5) = 50 5 - 5 = 0Helpful Since division Check: and multiplication are re-741 verse operations, don't forget 5 \times that a division problem can 3705 be checked by multiplying. Work Practice 4 **Practice 5** Example 5 Divide and check: $1872 \div 9$ Divide and check by **Solution:** multiplying. 208 **a.** 7)2128 9)1872 **b.** 9)45,900 -18 2(9) = 1807 18 - 18 = 0; bring down the 7. -00(9) = 072 7 - 0 = 7; bring down the 2. _72 8(9) = 720 72 - 72 = 0Answers **Check:** $208 \cdot 9 = 1872$ **4. a.** 818 **b.** 553 **c.** 251 **5. a.** 304 **b.** 5100 Work Practice 5

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Naturally, quotients don't always "come out even." Making 4 rows out of 26 chairs, for example, isn't possible if each row is supposed to have exactly the same number of chairs. Each of 4 rows can have 6 chairs, but 2 chairs are still left over.

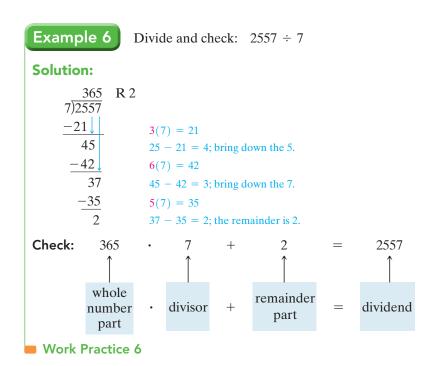


We signify "leftovers" or **remainders** in this way:

```
6 R 2
4)26
```

The **whole number part of the quotient** is 6; the **remainder part of the quotient** is 2. Checking by multiplying,

whole number part	•	divisor	+	remainder part	=	dividend
\downarrow		\downarrow		\downarrow		\downarrow
6	•	4	+	2		
	24		+	2	=	26



Practice 6
Divide and check.
a. 4)939
b. 5)3287

Answers 6. a. 234 R 3 **b.** 657 R 2

Chapter 1 | The Whole Numbers

Practice 7

Divide and check.

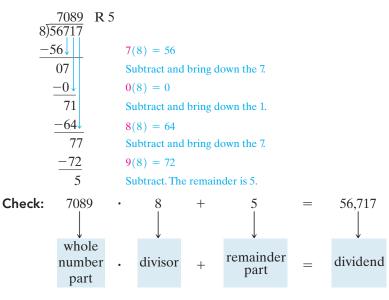
a. 9)81,605

b. 4)23,310

Example 7

Divide and check: $56,717 \div 8$

Solution:



Work Practice 7

When the divisor has more than one digit, the same pattern applies. For example, let's find 1358 \div 23.

5	$135 \div 23 = 5$ with 20 left over. Our estimate is 5.
23)1358	
-115	5 (23) = 115
208	135 - 115 = 20. Bring down the 8.

Now we continue estimating.

5 <mark>9</mark>	R 1	$208 \div 23 = 9$ with 1 left over.
23)1358		
-115		
208		
-207		9(23) = 207
1		208 - 207 = 1. The remainder is 1.

To check, see that $59 \cdot 23 + 1 = 1358$.

Example 8	Divide: 6819 ÷ 17
Solution:	
<u>401</u> R 17)6819	2
-68	4(17) = 68
01	Subtract and bring down the 1.
	0(17) = 0
19	Subtract and bring down the 9.
<u>-17</u>	1(17) = 17
2	Subtract. The remainder is 2.

To check, see that $401 \cdot 17 + 2 = 6819$.

Work Practice 8

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Practice 8 Divide: 8920 ÷ 17

Answers 7. a. 9067 R 2 b. 5827 R 2 8. 524 R 12

Example 9 Divide:	51,600 ÷ 403
Solution:	
<u>128</u> R 16 403)51600	
-403	1(403) = 403
1130	Subtract and bring down the 0.
-806	2(403) = 806
3240	Subtract and bring down the 0.
-3224	8(403) = 3224
16	Subtract. The remainder is 16.
To check, see that $128 \cdot 40$	3 + 16 = 51,600.
Work Practice 9	

Division Shown as Repeated Subtraction To further understand division, recall from Section 1.6 that addition and multiplication are related in the following manner:

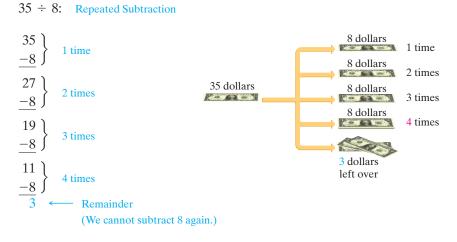
 $3 + 3 + 3 + 3 = 4 \times 3 = 12$ 4 addends; each addend is 3

In other words, multiplication is repeated addition. Likewise, division is repeated subtraction.

For example, let's find

35 ÷ 8

by repeated subtraction. Keep track of the number of times 8 is subtracted from 35. We are through when we can subtract no more because the difference is less than 8.



Thus, $35 \div 8 = 4 \text{ R} 3$.

To check, perform the same multiplication as usual and finish by adding in the remainder.

whole number part of quotient	•	divisor	+	remainder	=	dividend	
\downarrow 4	•	↓ 8	+	\downarrow 3	=	↓ 35	Answer 9. 49 R

. 60

67

Objective C Solving Problems by Dividing 🕗

Below are some key words and phrases that may indicate the operation of division:

Division					
Key Words or Phrases	Examples	Symbols			
divide	divide 10 by 5	$10 \div 5 \text{ or } \frac{10}{5}$			
quotient	the quotient of 64 and 4	$64 \div 4 \text{ or } \frac{64}{4}$			
divided by	9 divided by 3	$9 \div 3 \text{ or } \frac{9}{3}$			
divided or shared equally among	\$100 divided equally among five people	$100 \div 5 \text{ or } \frac{100}{5}$			
per	100 miles per 2 hours	$\frac{100 \text{ miles}}{2 \text{ hours}}$			

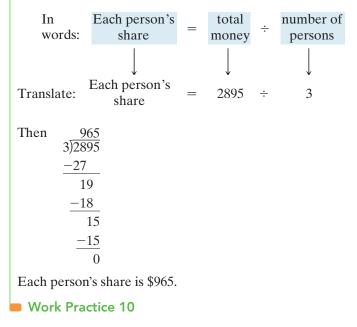
Concept Check Determine whether each of the following is the correct way to represent "the quotient of 60 and 12." Explain your answer.

```
a. 12 ÷ 60
b. 60 ÷ 12
```

Example 10 Finding Shared Earnings

Three college students share a paper route to earn money for expenses. The total in their fund after expenses was \$2895. How much is each person's equal share?

Solution:



Three students bought 171 blank CDs to share equally. How many CDs did each person get?

Answer 10. 57 CDs

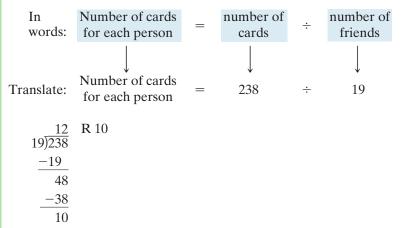
Concept Check Answers a. incorrect b. correct

Example 11

Dividing Number of Downloads

As part of a promotion, an executive receives 238 cards, each good for one free song download. If she wants to share them evenly with 19 friends, how many download cards will each friend receive? How many will be left over?

Solution:



Each friend will receive 12 download cards. The cards cannot be divided equally among her friends since there is a nonzero remainder. There will be 10 download cards left over.

Work Practice 11

Objective D Finding Averages

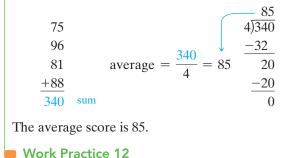
A special application of division (and addition) is finding the average of a list of numbers. The **average** of a list of numbers is the sum of the numbers divided by the *number* of numbers.

average = $\frac{\text{sum of numbers}}{number \text{ of numbers}}$

Example 12 Averaging Scores

A mathematics instructor is checking a simple program she wrote for averaging the scores of her students. To do so, she averages a student's scores of 75, 96, 81, and 88 by hand. Find this average score.

Solution: To find the average score, we find the sum of the student's scores and divide by 4, the number of scores.



Practice 11

Printers can be packed 12 to a box. If 532 printers are to be packed but only full boxes are shipped, how many full boxes will be shipped? How many printers are left over and not shipped?

Practice 12

To compute a safe time to wait for reactions to occur after allergy shots are administered, a lab technician is given a list of elapsed times between administered shots and reactions. Find the average of the times 4 minutes, 7 minutes, 35 minutes, 16 minutes, 9 minutes, 3 minutes, and 52 minutes.

Answers 11. 44 full boxes; 4 printers left over 12. 18 minutes

Calculator Explorations Dividing Numbers

To divide numbers on a calculator, find the keys marked
\div and $=$ or ENTER. For example, to find 435 \div 5
on a calculator, press the keys 435 \div 5 then $=$ or
ENTER. The display will read $\boxed{87}$. Thus, $435 \div 5 = 87$.

Use a calculator to divide.

1.	848 ÷ 16	2.	564 ÷ 12
3.	95)5890	4.	27)1053
5.	$\frac{32,886}{126}$	6.	$\frac{143,088}{264}$
7.	0 ÷ 315	8.	315 ÷ 0

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Some choices may be used more than once.

	1	number	divisor	dividend			
	0	undefined	average	quotient			
1.	$In 90 \div 2 = -$	45, the answer 45 is calle	d the	, 90 is called the	_, and 2 is called the		
2.	The quotient	of any number and 1 is t	he same				
3.	The quotient	of any number (except 0) and the same nur	nber is			
4.	4. The quotient of 0 and any number (except 0) is						
5.	The quotient	of any number and 0 is $_{-}$	·				
6.	The	of a list of numbers	is the sum of the n	umbers divided by the	of numbers.		

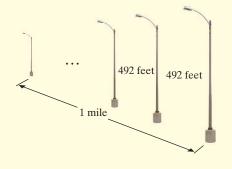
Martin-Gay Interactive Videos	Watch the section lecture	video and answer the following questions.
	Objective A 7.	Look at Examples 6–8. What number can never be the
See Video 1.7	Objective B 8.	divisor in division? In Example 10, how many 102s are in 21? How does this
	9.	result affect the quotient? >>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>
	Objective C 10.	In Example 10. What is the importance of knowing that the distance to each hole is the same?
	Objective D 11.	As shown in Example 12, what two operations are used when finding an average?

Objective A Find each quotient. See Examples I through 3. 1. $54 \div 9$ 2. $72 \div 9$ 0 3. $36 \div 3$ 4. $24 \div 3$ 5. $0 \div 8$ 6. $0 \div 4$ 0 7. $31 \div 1$ 8. $38 \div 1$ 0 9. $\frac{18}{18}$ 10. $\frac{49}{49}$ 11. $\frac{24}{3}$ 12. $\frac{45}{9}$ 0 13. $26 \div 0$ 14. $\frac{12}{0}$ 15. $26 \div 26$ 16. $6 \div 6$ 0 17. $0 \div 14$ 18. $7 \div 0$ 19. $18 \div 2$ 20. $18 \div 3$ Objectives A B Mixed Practice Divide and then check by multiplying. See Examples I through 5. 21. $3j87$ 22. $5j85$ 23. $3j222$ 24. $8j640$ 25. $3j1014$ 26. $4j2104$ 27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 7 33. $7j479$ 34. $7/426$ 35. $6j1421$ 36. $3j1240$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9. 41. $55/715$ 42. $23/736$ 43. $23)1127$ 44. $42/2016$ 45. $97/9417$ 46. $44/1938$ 47. $3146 \div 15$ 48	1. $54 \div 9$ 2. $72 \div 9$ 0.3. $36 \div 3$ 4. $24 \div 3$ 5. $0 \div 8$ 6. $0 \div 4$ 0.7. $31 \div 1$ 8. $38 \div 1$ 0.9. $\frac{18}{18}$ 10. $\frac{49}{49}$ 11. $\frac{24}{3}$ 12. $\frac{45}{9}$ 0. 13. $26 \div 0$ 14. $\frac{12}{0}$ 15. $26 \div 26$ 16. $6 \div 6$ 0. 17. $0 \div 14$ 18. $7 \div 0$ 19. $18 \div 2$ 20. $18 \div 3$ Objectives A B Mixed Practice Divide and then check by multiplying. See Examples 1 through 5.21. $3\overline{187}$ 22. $5\overline{185}$ 23. $3\overline{1222}$ 24. $8\overline{1640}$ 25. $3\overline{1014}$ 26. $4\overline{12104}$ 27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 733. $7\overline{1479}$ 34. $7\overline{1426}$ 35. $6\overline{11421}$ 36. $3\overline{11240}$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9.• 41. $5\overline{5715}$ 42. $23\overline{1736}$ 43. $23\overline{11127}$ 44. $42\overline{12016}$ 45. $97\overline{19417}$ 46. $44\overline{11038}$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12.744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10.297}{103}$	1.7 Exer	cise Set MyLab N	Math 🜔		
6. $0 \div 4$ 0 7. $31 \div 1$ 8. $38 \div 1$ 0 9. $\frac{18}{18}$ 10. $\frac{49}{49}$ 11. $\frac{24}{3}$ 12. $\frac{45}{9}$ 0 13. $26 \div 0$ 14. $\frac{12}{0}$ 15. $26 \div 26$ 16. $6 \div 6$ 0 17. $0 \div 14$ 18. $7 \div 0$ 19. $18 \div 2$ 20. $18 \div 3$ Objectives A B Mixed Practice Divide and then check by multiplying. See Examples 1 through 5.21. $3/87$ 22. $5/85$ 23. $3/222$ 24. $8/640$ 25. $3/1014$ 26. $4/2104$ 27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 733. $7/479$ 34. $7/426$ 35. $6/1421$ 36. $3/1240$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9.041. $55/715$ 42. $23/736$ 43. $23/1127$ 44. $42/2016$ 45. $97/9417$ 46. $44/1938$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9290 \div 46$ 52. $2505 \div 64$ 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10.297}{103}$	6. $0 \div 4$ 0 7. $31 \div 1$ 8. $38 \div 1$ 0 9. $\frac{18}{18}$ 10. $\frac{49}{49}$ 11. $\frac{24}{3}$ 12. $\frac{45}{9}$ 0 13. $26 \div 0$ 14. $\frac{12}{0}$ 15. $26 \div 26$ 16. $6 \div 6$ 0 17. $0 \div 14$ 18. $7 \div 0$ 19. $18 \div 2$ 20. $18 \div 3$ Objectives A B Mixed Practice Divide and then check by multiplying. See Examples 1 through 5.21. $3/87$ 22. $5/85$ 23. $3/222$ 24. $8/640$ 25. $3/1014$ 26. $4/2104$ 27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 733. $7/479$ 34. $7/426$ 35. $6/1421$ 36. $3/1240$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9.041. $55/715$ 42. $23/736$ 43. $23/1127$ 44. $42/2016$ 45. $97/9417$ 46. $44/1938$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9290 \div 46$ 52. $2505 \div 64$ 53. $\frac{12.744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10.297}{103}$	Objective A	find each quotient. See Exa	amples 1 through 3.		
11. $\frac{24}{3}$ 12. $\frac{45}{9}$ 013. $26 \div 0$ 14. $\frac{12}{0}$ 15. $26 \div 26$ 16. $6 \div 6$ 017. $0 \div 14$ 18. $7 \div 0$ 19. $18 \div 2$ 20. $18 \div 3$ Objectives A B Mixed Practice Divide and then check by multiplying. See Examples 1 through 5.21. $3)87$ 22. $5)85$ 23. $3)222$ 24. $8)640$ 25. $3)1014$ 26. $4)2104$ 27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 7.33. $7)479$ 34. $7/426$ 35. $6)1421$ 36. $3)1240$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9.• 41. $55)715$ 42. $23)736$ 43. $23)1127$ 44. $42)2016$ 45. $97)9417$ 46. $44)1938$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	11. $\frac{24}{3}$ 12. $\frac{45}{9}$ 013. $26 \div 0$ 14. $\frac{12}{0}$ 15. $26 \div 26$ 16. $6 \div 6$ 017. $0 \div 14$ 18. $7 \div 0$ 19. $18 \div 2$ 20. $18 \div 3$ Objectives A B Mixed Practice Divide and then check by multiplying. See Examples 1 through 5.21. $3)87$ 22. $5)85$ 23. $3)222$ 24. $8)640$ 25. $3)1014$ 26. $4)2104$ 27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 7.33. $7)479$ 34. $7/426$ 35. $6)\overline{1421}$ 36. $3)\overline{1240}$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9.• 41. $55)\overline{715}$ 42. $23/\overline{736}$ 43. $23)\overline{1127}$ 44. $42)\overline{2016}$ 45. $97)\overline{9417}$ 46. $44)\overline{1938}$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	1. 54 ÷ 9	2. 72 ÷ 9	3. 36 ÷ 3	4. 24 ÷ 3	5. 0 ÷ 8
16. $6 \div 6$ 17. $0 \div 14$ 18. $7 \div 0$ 19. $18 \div 2$ 20. $18 \div 3$ 16. $6 \div 6$ 17. $0 \div 14$ 18. $7 \div 0$ 19. $18 \div 2$ 20. $18 \div 3$ Objectives A B Mixed Practice Divide and then check by multiplying. See Examples 1 through 5. 21. $3)87$ 22. $5)85$ 23. $3)222$ 24. $8)640$ 25. $3)1014$ 26. $4)2104$ 27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 7 33. $7)479$ 34. $7)426$ 35. $6)1421$ 36. $3)1240$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9. • 41. $55)715$ 42. $23)736$ 43. $23)1127$ 44. $42)2016$ 45. $97)9417$ 46. $44)1938$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	16. $6 \div 6$ 17. $0 \div 14$ 18. $7 \div 0$ 19. $18 \div 2$ 20. $18 \div 3$ 16. $6 \div 6$ 17. $0 \div 14$ 18. $7 \div 0$ 19. $18 \div 2$ 20. $18 \div 3$ Objectives A B Mixed Practice Divide and then check by multiplying. See Examples 1 through 5. 21. $3)\overline{87}$ 22. $5)\overline{85}$ 23. $3)\overline{222}$ 24. $8)\overline{640}$ 25. $3)\overline{1014}$ 26. $4)\overline{2104}$ 27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 7 33. $7 \overline{479}$ 34. $7 \overline{426}$ 35. $6 \overline{1421}$ 36. $3 \overline{1240}$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9. • 41. $55 \overline{715}$ 42. $23 \overline{736}$ 43. $23 \overline{1127}$ 44. $42 \overline{2016}$ 45. $97 \overline{9417}$ 46. $44 \overline{1938}$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	6. 0 ÷ 4	● 7. 31 ÷ 1	8. 38 ÷ 1	9. $\frac{18}{18}$	10. $\frac{49}{49}$
Objectives A B Mixed Practice Divide and then check by multiplying. See Examples 1 through 5. 21. $3)87$ 22. $5)85$ 23. $3)222$ 24. $8)640$ 25. $3)1014$ 26. $4)2104$ 27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 7. 33. $7)479$ 34. $7)426$ 35. $6)1421$ 36. $3)1240$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9. • 41. $55)715$ 42. $23)736$ 43. $23)1127$ 44. $42)2016$ 45. $97)9417$ 46. $44)1938$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	Objectives A B Mixed Practice Divide and then check by multiplying. See Examples 1 through 5. 21. $3/87$ 22. $5/85$ 23. $3/222$ 24. $8/640$ 25. $3/1014$ 26. $4/2104$ 27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 7. 33. $7/479$ 34. $7/426$ 35. $6/1421$ 36. $3/1240$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9. • 41. $55/715$ 42. $23/736$ 43. $23/1127$ 44. $42/2016$ 45. $97/9417$ 46. $44)1938$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	11. $\frac{24}{3}$	12. $\frac{45}{9}$	● 13. 26 ÷ 0	14. $\frac{12}{0}$	15. 26 ÷ 26
21. $3)\overline{87}$ 22. $5)\overline{85}$ 23. $3)\overline{222}$ 24. $8)\overline{640}$ 25. $3)\overline{1014}$ 26. $4)\overline{2104}$ 27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 733. $7)\overline{479}$ 34. $7/\overline{426}$ 35. $6)\overline{1421}$ 36. $3)\overline{1240}$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9.O 41. $55)\overline{715}$ 42. $23)\overline{736}$ 43. $23)\overline{1127}$ 44. $42)\overline{2016}$ 45. $97)\overline{9417}$ 46. $44)\overline{1938}$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	21. $3)\overline{87}$ 22. $5)\overline{85}$ 23. $3)\overline{222}$ 24. $8)\overline{640}$ 25. $3)\overline{1014}$ 26. $4)\overline{2104}$ 27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 7.33. $7)\overline{479}$ 34. $7)\overline{426}$ 35. $6)\overline{1421}$ 36. $3)\overline{1240}$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9.O 41. $55)\overline{715}$ 42. $23)\overline{736}$ 43. $23)\overline{1127}$ 44. $42)\overline{2016}$ 45. $97)\overline{9417}$ 46. $44)\overline{1938}$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12.744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10.297}{103}$	16. 6 ÷ 6	● 17. 0 ÷ 14	18. 7 ÷ 0	19. 18 ÷ 2	20. 18 ÷ 3
21. $3)\overline{87}$ 22. $5)\overline{85}$ 23. $3)\overline{222}$ 24. $8)\overline{640}$ 25. $3)\overline{1014}$ 26. $4)\overline{2104}$ 27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 733. $7)\overline{479}$ 34. $7/\overline{426}$ 35. $6)\overline{1421}$ 36. $3)\overline{1240}$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9.O 41. $55)\overline{715}$ 42. $23)\overline{736}$ 43. $23)\overline{1127}$ 44. $42)\overline{2016}$ 45. $97)\overline{9417}$ 46. $44)\overline{1938}$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	21. $3)\overline{87}$ 22. $5)\overline{85}$ 23. $3)\overline{222}$ 24. $8)\overline{640}$ 25. $3)\overline{1014}$ 26. $4)\overline{2104}$ 27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 7.33. $7)\overline{479}$ 34. $7)\overline{426}$ 35. $6)\overline{1421}$ 36. $3)\overline{1240}$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9.O 41. $55)\overline{715}$ 42. $23)\overline{736}$ 43. $23)\overline{1127}$ 44. $42)\overline{2016}$ 45. $97)\overline{9417}$ 46. $44)\overline{1938}$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12.744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10.297}{103}$					
21. $3)\overline{87}$ 22. $5)\overline{85}$ 23. $3)\overline{222}$ 24. $8)\overline{640}$ 25. $3)\overline{1014}$ 26. $4)\overline{2104}$ 27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 733. $7)\overline{479}$ 34. $7/\overline{426}$ 35. $6)\overline{1421}$ 36. $3)\overline{1240}$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9.O 41. $55)\overline{715}$ 42. $23)\overline{736}$ 43. $23)\overline{1127}$ 44. $42)\overline{2016}$ 45. $97)\overline{9417}$ 46. $44)\overline{1938}$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	21. $3)\overline{87}$ 22. $5)\overline{85}$ 23. $3)\overline{222}$ 24. $8)\overline{640}$ 25. $3)\overline{1014}$ 26. $4)\overline{2104}$ 27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 7.33. $7)\overline{479}$ 34. $7)\overline{426}$ 35. $6)\overline{1421}$ 36. $3)\overline{1240}$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9.O 41. $55)\overline{715}$ 42. $23)\overline{736}$ 43. $23)\overline{1127}$ 44. $42)\overline{2016}$ 45. $97)\overline{9417}$ 46. $44)\overline{1938}$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12.744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10.297}{103}$					
27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 733. $7)\overline{479}$ 34. $7)\overline{426}$ 35. $6)\overline{1421}$ 36. $3)\overline{1240}$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9.O 41. $55)\overline{715}$ 42. $23)\overline{736}$ 43. $23)\overline{1127}$ 44. $42)\overline{2016}$ 45. $97)\overline{9417}$ 46. $44)\overline{1938}$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	27. $\frac{30}{0}$ 28. $\frac{0}{30}$ 29. $63 \div 7$ 30. $56 \div 8$ 31. $150 \div 6$ 32. $121 \div 11$ Divide and then check by multiplying. See Examples 6 and 7.33. $7)\overline{479}$ 34. $7)\overline{426}$ 35. $6)\overline{1421}$ 36. $3)\overline{1240}$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9.041. $55)\overline{715}$ 42. $23\overline{3736}$ 43. $23\overline{31127}$ 44. $42\overline{2016}$ 45. $97\overline{)9417}$ 46. $44\overline{)1938}$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	Objectives A	B Mixed Practice <i>I</i>	Divide and then check by r	nultiplying. See Example	es 1 through 5.
Divide and then check by multiplying. See Examples 6 and 733. $7\overline{)479}$ 34. $7\overline{)426}$ 35. $6\overline{)1421}$ 36. $3\overline{)1240}$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9. 0 41. $55\overline{)715}$ 42. $23\overline{)736}$ 43. $23\overline{)1127}$ 44. $42\overline{)2016}$ 45. $97\overline{)9417}$ 46. $44\overline{)1938}$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	Divide and then check by multiplying. See Examples 6 and 733. $7\overline{)479}$ 34. $7\overline{)426}$ 35. $6\overline{)1421}$ 36. $3\overline{)1240}$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9. 0 41. $55\overline{)715}$ 42. $23\overline{)736}$ 43. $23\overline{)1127}$ 44. $42\overline{)2016}$ 45. $97\overline{)9417}$ 46. $44\overline{)1938}$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	21. 3)87	22. 5)85 23	. 3)222 24. 8)6	25. 3)1014	26. 4)2104
Divide and then check by multiplying. See Examples 6 and 733. $7\overline{)479}$ 34. $7\overline{)426}$ 35. $6\overline{)1421}$ 36. $3\overline{)1240}$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9. 0 41. $55\overline{)715}$ 42. $23\overline{)736}$ 43. $23\overline{)1127}$ 44. $42\overline{)2016}$ 45. $97\overline{)9417}$ 46. $44\overline{)1938}$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	Divide and then check by multiplying. See Examples 6 and 733. $7\overline{)479}$ 34. $7\overline{)426}$ 35. $6\overline{)1421}$ 36. $3\overline{)1240}$ 37. $305 \div 8$ 38. $167 \div 3$ 39. $2286 \div 7$ 40. $3333 \div 4$ Divide and then check by multiplying. See Examples 8 and 9. 0 41. $55\overline{)715}$ 42. $23\overline{)736}$ 43. $23\overline{)1127}$ 44. $42\overline{)2016}$ 45. $97\overline{)9417}$ 46. $44\overline{)1938}$ 47. $3146 \div 15$ 48. $7354 \div 12$ 49. $6578 \div 13$ 50. $5670 \div 14$ 51. $9299 \div 46$ 52. $2505 \div 64$ 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$					
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Divide and then check by multiplying. See Examples 8 and 9. • 41. 55)715 42. 23)736 43. 23)1127 44. 42)2016 45. 97)9417 46. 44)1938 47. 3146 \div 15 48. 7354 \div 12 49. 6578 \div 13 50. 5670 \div 14 51. 9299 \div 46 52. 2505 \div 64 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	Divide and then check by multiplying. See Examples 8 and 9. • 41. 55)715 42. 23)736 43. 23)1127 44. 42)2016 45. 97)9417 46. 44)1938 47. 3146 \div 15 48. 7354 \div 12 49. 6578 \div 13 50. 5670 \div 14 51. 9299 \div 46 52. 2505 \div 64 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	33. 7)479	34. 7)426	35. 6)1	421 3	6. 3)1240
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51. 9299 ÷ 46 52. 2505 ÷ 64 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$	51. 9299 ÷ 46 52. 2505 ÷ 64 53. $\frac{12,744}{236}$ 54. $\frac{5781}{123}$ 55. $\frac{10,297}{103}$					
		46. 44)1938	47. 3146 ÷ 15	48. 7354 ÷ 12	49. 6578 ÷ 13	50. 5670 ÷ 14
				12 744	5781	10 297
23.002	56 $\frac{23,092}{57}$ 57 20.610 \div 102 58 40.853 \div 203 59 244.980 \div 423 60 164.592 \div 543	51. 9299 ÷ 46	52. 2505 ÷ 64	53. $\frac{12,711}{236}$	54. $\frac{3761}{123}$	55. $\frac{10,237}{103}$
	56 $\frac{23,022}{10}$ 57 20.610 \div 102 58 40.853 \div 203 59 244.080 \div 423 60 164.502 \div 543	23 092				
56. $\frac{23,092}{240}$ 57. 20,619 ÷ 102 58. 40,853 ÷ 203 59. 244,989 ÷ 423 60. 164,592 ÷ 543	240 240 240 240 240 240 240 240 240 240	56. $\frac{23,072}{240}$	57. 20,619 ÷ 102	58. 40,853 ÷ 203	59. 244,989 ÷ 423	60. 164,592 ÷ 543

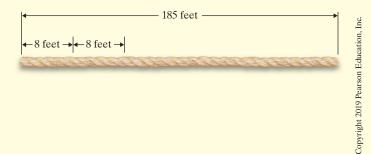
Divide. See Examples 1 through 9.						
61. 7)119	62. 8)104	63. 7)3580	64. 5)3017			
65. 40)85,312	66. 50)85,747	67. 142)863,360	68. 214)650,560			

Objective C Translating Solve. See Examples 10 and 11.

- **69.** Find the quotient of 117 and 5. **71.** Find 200 divided by 35.
- **73.** Find the quotient of 62 and 3.
- **75.** Martin Thieme teaches American Sign Language classes for \$65 per student for a 7-week session. He collects \$2145 from the group of students. Find how many students are in the group.
- **77.** The gravity of Jupiter is 318 times as strong as the gravity of Earth, so objects on Jupiter weigh 318 times as much as they weigh on Earth. If a person would weigh 52,470 pounds on Jupiter, find how much the person weighs on Earth.
- **79.** An 18-hole golf course is 5580 yards long. If the distance to each hole is the same, find the distance between holes.
 - 81. There is a bridge over highway I-35 every three miles. The first bridge is at the beginning of a 265-mile stretch of highway. Find how many bridges there are over 265 miles of I-35.
 - **83.** Ari Trainor is in the requisitions department of Central Electric Lighting Company. Light poles along a highway are placed 492 feet apart. The first light pole is at the beginning of a 1-mile strip. Find how many poles he should order for the 1-mile strip of highway. (A mile is 5280 feet.)



- **70.** Find the quotient of 94 and 7.
- **72.** Find 116 divided by 32.
- **74.** Find the quotient of 78 and 5.
- **76.** Kathy Gomez teaches Spanish lessons for \$85 per student for a 5-week session. From one group of students, she collects \$4930. Find how many students are in the group.
- **78.** Twenty-one people pooled their money and bought lottery tickets. One ticket won a prize of \$5,292,000. Find how many dollars each person received.
- **80.** A truck hauls wheat to a storage granary. It carries a total of 5768 bushels of wheat in 14 trips. How much does the truck haul each trip if each trip it hauls the same amount?
- **82.** The white stripes dividing the lanes on a highway are 25 feet long, and the spaces between them are 25 feet long. Let's call a "lane divider" a stripe followed by a space. Find how many whole "lane dividers" there are in 1 mile of highway. (A mile is 5280 feet.)
- **84.** Professor Lopez has a piece of rope 185 feet long that she wants to cut into pieces for an experiment in her physics class. Each piece of rope is to be 8 feet long. Determine whether she has enough rope for her 22-student class. Determine the amount extra or the amount short.



- **85.** Broad Peak in Pakistan is the twelfth-tallest mountain in the world. Its elevation is 26,400 feet. A mile is 5280 feet. How many miles tall is Broad Peak? (*Source:* National Geographic Society)
- **87.** Find how many yards are in 1 mile. (A mile is 5280 feet; a yard is 3 feet.)

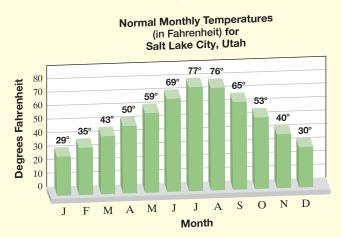
	$\leftarrow 1 \text{ foot} \rightarrow \leftarrow 1 \text{ foot} \rightarrow \leftarrow 1 \text{ foot} \rightarrow \leftarrow \cdots$
▲ 1 yard -	
4	5280 feet

- **86.** David Johnson of the Arizona Cardinals led the NFL in touchdowns during the 2016 regular football season, scoring a total of 120 points from touchdowns. If a touchdown is worth 6 points, how many touchdowns did Johnson make during 2016? (*Source:* National Football League)
- **88.** Find how many whole feet are in 1 rod. (A mile is 5280 feet; 1 mile is 320 rods.)

Objective D *Find the average of each list of numbers. See Example 12.*

89.	10, 24, 35, 22, 17, 12	90.	37, 26, 15, 29, 51, 22	91.	205, 972, 210, 161
92.	121, 200, 185, 176, 163	0 93.	86, 79, 81, 69, 80	94.	92, 96, 90, 85, 92, 79

The normal monthly temperatures in degrees Fahrenheit for Salt Lake City, Utah, are given in the graph. Use this graph to answer Exercises 95 and 96. (Source: National Climatic Data Center)



- **95.** Find the average temperature for June, July, and August.
- **96.** Find the average temperature for October, November, and December.

Mixed Practice (Sections 1.3, 1.4, 1.6, and 1.7) Perform each indicated operation. Watch the operation symbol.

97. 82 + 463 + 29	0 + 8704	98. 23 + 407 + 92 -	+ 7011
99. 546	100. 712	101. 722	102. 712
$\times 28$	$\times 54$	<u> </u>	<u> </u>
103. $\frac{45}{0}$	104. $\frac{0}{23}$	105. 228 ÷ 24	106. 304 ÷ 31

Concept Extensions

Match each word phrase to the correct translation. (Not all letter choices will be used.) See the Concept Check in this section.

107. The quotient of 40 and 8	108. The quotient of 200 and 20	a. 20 ÷ 200	b. 200 ÷ 20
		c. 40 ÷ 8	d. 8 ÷ 40
109. 200 divided by 20	110. 40 divided by 8		

The following table shows the top seven countries with the most Nobel Prize winners by country of birth. Use this table to answer Exercises 111 and 112. (Source: Nobel Prize Organization)

111.	Find the aver- age number of	Most Nobel Prize Winners by Country of Birth, 1901–2016									
	Nobel Prize winners		Country	Chemistry	Economics	Literature	Peace	Physics	Physiology & Medicine	Total	
	for United Kingdom,		United States	52	43	9	19	66	70	259	
	Germany, and France.		United Kingdom	24	8	7	11	23	26	99	
a b P fc R	Find the		Germany	24	1	7	5	23	17	77	
	average num- ber of Nobel Prize winners		France	9	4	11	10	9	12	55	
	for Sweden, Russia, and Japan.		Sweden	4	2	7	5	4	7	29	
			Russia (USSR)	3	2	5	2	11	2	25	
			Japan	6	0	2	1	11	4	24	

In Example 12 in this section, we found that the average of 75, 96, 81, and 88 is 85. Use this information to answer *Exercises 113 and 114*.

- **113.** If the number 75 is removed from the list of numbers, does the average increase or decrease? Explain why.
- **115.** Without computing it, tell whether the average of 126, 135, 198, 113 is 86. Explain why it is possible or why it is not.
- \triangle **117.** If the area of a rectangle is 60 square feet and its width is 5 feet, what is its length?
 - **119.** Write down any two numbers whose quotient is 25.
 - **121.** Find 26 ÷ 5 using the process of repeated subtraction.

- **114.** If the number 96 is removed from the list of numbers, does the average increase or decrease? Explain why.
- **116.** Without computing it, tell whether the average of 38, 27, 58, and 43 is 17. Explain why it is possible or why it is not.
- \triangle **118.** If the area of a rectangle is 84 square inches and its length is 21 inches, what is its width?
 - **120.** Write down any two numbers whose quotient is 1.
 - **122.** Find $86 \div 10$ using the process of repeated subtraction.

		Sections 1.2-	-1.7 Integ	rated Review
Operations	on Whole N	umbers		
1. 23 46 +79	2. 7006 <u>- 451</u>	3. 36 <u>×45</u>	4. 8)4496	Answers 1. 2. 3.
5. 1 • 79	6. $\frac{36}{0}$	7. 9 ÷ 1	8. 9 ÷ 9	4. 5. 6. 7. 8.
9. 0 • 13	10. 7·0·8	11. 0 ÷ 2	12. 12 ÷ 4	9. 10. 11.
13. 4219 – 1786	14. 1861 + 7965	15. 5)1068	16. 1259 <u>× 63</u>	<u>12.</u> <u>13.</u> <u>14.</u> 15.
17. 3·9	18. 45 ÷ 5	19. 207 <u>- 69</u>	20. 207 + 69	16. 17. 18. 19. 20.
21. 7)7695	22. 9)1000	23. 32)21,222	24. 65)70,000	21. 22. 23. 24.
25. 4000 – 2976	26. 10,000 - 101	27. 303 <u>× 101</u>	28. (475) (100)	25. 26. 27. 28. 29.
29. Find the total of	57 and 8.	30. Find the product	t of 57 and 8.	30.

76	Chapter 1 The Whole Numbers						
<u>31.</u>	31. Find the quotient of 62 and 9.			32.	Find the difference of 62 and 9.		
32.			17 from 20 able by ro		given num		Find the difference of 432 and 201. <i>the given place value.</i>
33.	35.	9735	Tens	Hundreds	Thousands		
34.	36. 37. 38.	1429 20,801 432,198				}	
35		the perim	eter and a	rea of each			
36	∆ 39.	Square	6 feet	t		40.	14 inches Rectangle 7 inches
37.	Find	the perim	eter of eac	ch figure.			
38.	△ 41.	13 miles	9 mile	'S		42.	3 meters
<u>39.</u>		6 mile	es				3 meters
40.		<i>the avera</i> , 19, 15, 25,		list of num	bers.	44.	108, 131, 98, 159
<u>41.</u>		insulas of Lake Pon	Michigan tchartrain	across the Bridge is a	Straits of Material Straits of Material Straits of Material Strain Strai	Macki rete ti	at connects the lower and upper pen- nac. Its total length is 26,372 feet. The restle bridge in Slidell, Louisiana. Its
42.							er and by how much? (<i>Sources:</i> vay Administration, Bridge Division)
43.			K	ST.	STR.		Straits of Mackinac, MI
<u>44.</u>			A series		E.		Slidell,
45				A			LA
46.	46. The average teenage male American consumes 2 quarts of carbonated soft drinks per day. On average, how many quarts of carbonated soft drinks would be consumed in a year? (Use 365 for the number of days.) (<i>Source:</i> American Beverage Association)						

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1.8 An Introduction to Problem Solving 🔘

Objective A Solving Problems Involving Addition, Subtraction, Multiplication, or Division

In this section, we decide which operation to perform in order to solve a problem. Don't forget the key words and phrases that help indicate which operation to use. Some of these are listed below and were introduced earlier in the chapter. Also included are several words and phrases that translate to the symbol "=".

Addition (+)	Subtraction (-)	Multiplication (•)	Division (÷)	Equality (=)
sum	difference	product	quotient	equals
plus	minus	times	divide	is equal to
added to	subtract	multiply	shared equally	is/was
more than	less than	multiply by	among	yields
increased by	decreased by	of	divided by	
total	less	double/triple	divided into	

The following problem-solving steps may be helpful to you:

Problem-Solving Steps

- **1.** UNDERSTAND the problem. Some ways of doing this are to read and reread the problem, construct a drawing, and look for key words to identify an operation.
- **2.** TRANSLATE the problem. That is, write the problem in short form using words, and then translate to numbers and symbols.
- **3.** SOLVE the problem. It is helpful to estimate the solution by rounding. Then carry out the indicated operation from step 2.
- **4.** INTERPRET the results. *Check* the proposed solution in the stated problem and *state* your conclusions. Write your results with the correct units attached.

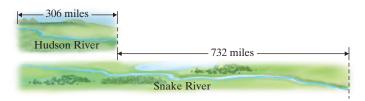
Example 1

Calculating the Length of a River

The Hudson River in New York State is 306 miles long. The Snake River in the northwestern United States is 732 miles longer than the Hudson River. How long is the Snake River? (*Source:* U.S. Department of the Interior)

Solution:

1. UNDERSTAND. Read and reread the problem, and then draw a picture. Notice that we are told that Snake River is 732 miles longer than the Hudson River. The phrase "longer than" means that we add.

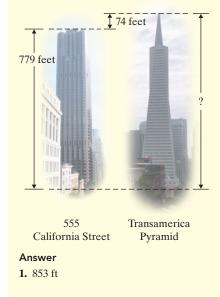


Objectives

- A Solve Problems by Adding, Subtracting, Multiplying, or Dividing Whole Numbers.
- B Solve Problems That Require More Than One Operation.

Practice 1

The building called 555 California Street is the thirdtallest building in San Francisco, California, at 779 feet. The second-tallest building in San Francisco is the Transamerica Pyramid, which is 74 feet taller than 555 California Street. How tall is the Transamerica Pyramid? (*Source: The World Almanac*)



(Continued on next page)

2. TRANSLATE.

In words:	Snake River	is	732 miles	longer than	the Hudson River
	\downarrow	Ļ	\downarrow	\downarrow	\downarrow
Translate:	Snake River	=	732	+	306

3. SOLVE: Let's see if our answer is reasonable by also estimating. We will estimate each addend to the nearest hundred.

732	rounds to	700	
+306	rounds to	+300	
1038	exact	1000	estimate

4. INTERPRET. Check your work. The answer is reasonable since 1038 is close to our estimated answer of 1000. State your conclusion: The Snake River is 1038 miles long.

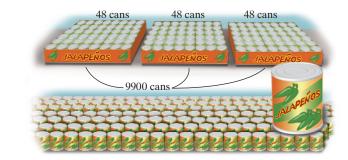
Work Practice 1

Example 2 Filling a Shipping Order

How many cases can be filled with 9900 cans of jalapeños if each case holds 48 cans? How many cans will be left over? Will there be enough cases to fill an order for 200 cases?

Solution:

1. UNDERSTAND. Read and reread the problem. Draw a picture to help visualize the situation.



Since each case holds 48 cans, we want to know how many 48s there are in 9900. We find this by dividing.

2. TRANSLATE.

In words:	Number of cases	is	9900	divided by	48
	\downarrow	\downarrow	\downarrow	\downarrow	\downarrow
Translate.	Number of cases	=	9900	÷	48

3. SOLVE: Let's estimate a reasonable solution before we actually divide. Since 9900 rounded to the nearest thousand is 10,000 and 48 rounded to the nearest ten is $50,10,000 \div 50 = 200$. Now find the exact quotient.

206 48)9900	R12
-96	
300	
-288	
12	

Practice 2

Four friends bought a lottery ticket and won \$65,000. If each person is to receive the same amount of money, how much does each person receive?

4. INTERPRET. *Check* your work. The answer is reasonable since 206 R 12 is close to our estimate of 200. *State* your conclusion: 206 cases will be filled, with 12 cans left over. There will be enough cases to fill an order for 200 cases.

Work Practice 2

Example 3 Calculating Budget Costs

The director of a computer lab at a local state college is working on next year's budget. Thirty-three new desktop computers are needed at a cost of \$487 each. What is the total cost of these desktops?

Solution:

1. UNDERSTAND. Read and reread the problem, and then draw a diagram.



From the phrase "total cost," we might decide to solve this problem by adding. This would work, but repeated addition, or multiplication, would save time.

2. TRANSLATE.

In words:	Total cost	is	number of desktops	times	cost of a desktop
	\downarrow	\downarrow	\downarrow	\downarrow	\downarrow
Translate:	Total cost	=	33	×	\$487

3. SOLVE: Once again, let's estimate a reasonable solution.

 $\begin{array}{c|cccc} 487 & \text{rounds to} & 500 \\ \underline{\times 33} & \text{rounds to} & \underline{\times 30} \\ \hline 1461 & 15,000 & \text{estimate} \\ \hline \underline{14610} \\ \hline 16,071 & \text{exact} \end{array}$

4. INTERPRET. *Check* your work. *State* your conclusion: The total cost of the desktops is \$16,071.

Work Practice 3

Example 4 Calculating a Public School Teacher's Salary

In 2017, the average salary for a public school teacher in California was \$69,320. For the same year, the average salary for a public school teacher in Iowa was \$20,370 less than this. What was the average public school teacher's salary in Iowa? (*Source:* National Education Association)

Solution:

1. UNDERSTAND. Read and reread the problem. Notice that we are told that the Iowa salary is \$20,370 less than the California salary. The phrase "less than" indicates subtraction.

(*Continued on next page*)

Practice 3

The director of the learning lab also needs to include in the budget a line for 425 flash drives at a cost of \$4 each. What is this total cost for the flash drives?

Practice 4

In 2017, the average salary for a public school teacher in New York was \$69,118. For the same year, the average salary for a public school teacher in Illinois was \$7774 less than this. What was the average public school teacher's salary in Illinois? (*Source:* National Education Association)

Answers 3. \$1700 4. \$61,344



2. TRANSLATE. Remember that order matters when subtracting, so be careful when translating.

In words:	Iowa salary	is	California salary	minus	\$20,370
	\downarrow		\downarrow	\downarrow	\downarrow
Translate:	Iowa salary	=	69,320	_	20,370

3. SOLVE. This time, instead of estimating, let's check by adding.

69,320	Check:	48,950
-20,370		+20,370
48,950		69,320

4. INTERPRET. *Check* your work. The check is above. *State* your conclusion: The average Iowa teacher's salary in 2017 was \$48,950.

```
Work Practice 4
```

Objective B Solving Problems That Require More Than One Operation 🜔

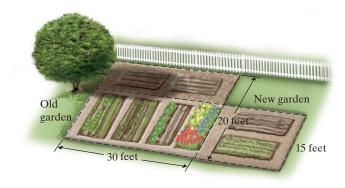
We must sometimes use more than one operation to solve a problem.

Example 5 Planting a New Garden

A gardener bought enough plants to fill a rectangular garden with length 30 feet and width 20 feet. Because of shading problems from a nearby tree, the gardener changed the width of the garden to 15 feet. If the area is to remain the same, what is the new length of the garden?

Solution:

1. UNDERSTAND. Read and reread the problem. Then draw a picture to help visualize the problem.



2. TRANSLATE. Since the area of the new garden is to be the same as the area of the old garden, let's find the area of the old garden.

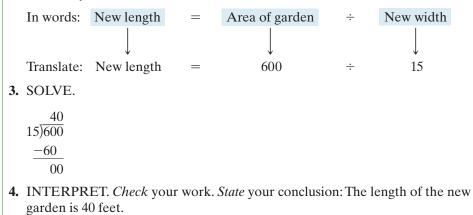
Area = length \times width = 30 feet \times 20 feet = 600 square feet

Practice 5

A gardener is trying to decide how much fertilizer to buy for his yard. He knows that his lot is in the shape of a rectangle that measures 90 feet by 120 feet. He also knows that the floor of his house is in the shape of a rectangle that measures 45 feet by 65 feet. How much area of the lot is not covered by the house?

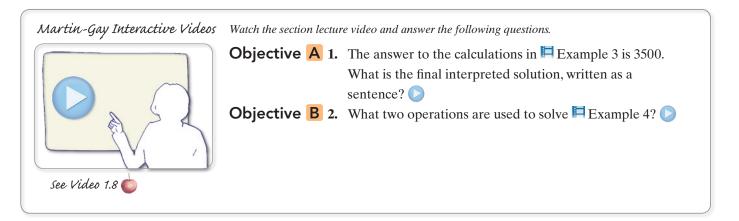


Answer 5. 7875 sq ft Since the area of the new garden is to be 600 square feet also, we need to see how many 15s there are in 600. This means division. In other words,



```
Work Practice 5
```

Vocabulary, Readiness & Video Check



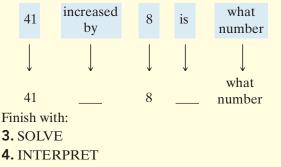
1.8 Exercise Set MyLab Math

Objective A Solve. Exercises 1, 2, 11, and 12 have been started for you. See Examples 1 through 4.

1. 41 increased by 8 is what number?

Start the solution:

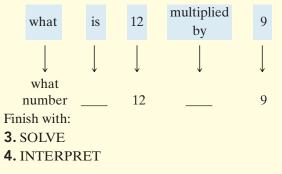
- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blanks below.)



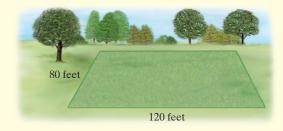
2. What is 12 multiplied by 9?

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blanks below.)



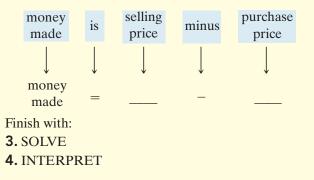
- **3.** What is the quotient of 1185 and 5?
- **5.** What is the total of 35 and 7?
 - **7.** 60 times 10 is what number?
- \triangle **9.** A vacant lot in the shape of a rectangle measures 120 feet by 80 feet.
 - **a.** What is the perimeter of the lot?
 - **b.** What is the area of the lot?



11. A family bought a house for \$185,700 and later sold the house for \$201,200. How much money did they make by selling the house?

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blanks below.)



13. There are 24 hours in a day. How many hours are in a week?

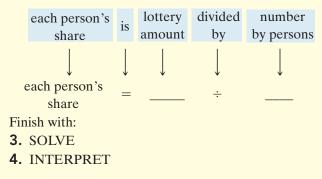
- **4.** 78 decreased by 12 is what number?
- **6.** What is the difference of 48 and 8?
- **8.** 60 divided by 10 is what number?
- \triangle **10.** A parking lot in the shape of a rectangle measures 100 feet by 150 feet.
 - **a.** What is the perimeter of the lot?
 - **b.** What is the area of the parking lot?



12. Three people dream of equally sharing a \$147 million lottery. How much would each person receive if they have the winning ticket?

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blanks below.)



14. There are 60 minutes in an hour. How many minutes are in a day?

●15. The Verrazano Narrows Bridge is the longest bridge in New York, measuring 4260 feet. The George Washington Bridge, also in New York, is 760 feet shorter than the Verrazano Narrows Bridge. Find the length of the George Washington Bridge.



16. In 2013, the Goodyear Tire & Rubber Company began replacing its fleet of nonrigid GZ-20 blimps with new Goodyear NT semi-rigid airships. The new Goodyear NT airship can hold 297,527 cubic feet of helium. Its GZ-20 predecessor held 94,827 fewer cubic feet of helium. How much helium did a GZ-20 blimp hold? (*Source:* Goodyear Tire & Rubber Company)



18. Razor scooters were introduced in 2000. Radio Flyer

Wagons were first introduced 83 years earlier. In what year were Radio Flyer Wagons introduced?

(Source: Toy Industry Association, Inc.)

17. Yellowstone National Park in Wyoming was the first national park in the United States. It was created in 1872. One of the more recent additions to the National Park System is First State National Monument. It was established in 2013. How much older is Yellowstone than First State? (*Source:* National Park Service)



- **19.** Since their introduction, the number of LEGO building bricks that have been sold is equivalent to the world's current population of approximately 6 billion people owning 62 LEGO bricks each. About how many LEGO bricks have been sold since their introduction? (*Source:* LEGO Company)
- **21.** The three most common city names in the United States are Fairview, Midway, and Riverside. There are 287 towns named Fairview, 252 named Midway, and 180 named Riverside. Find the total number of towns named Fairview, Midway, or Riverside.
- **20.** In 2016, the average weekly pay for a home health aide in the United States was about \$425. At this rate, how much will a home health aide earn working a 52-week year? (*Source:* Bureau of Labor Statistics)
- **22.** In the game of Monopoly, a player must own all properties in a color group before building houses. The yellow color-group properties are Atlantic Avenue, Ventnor Avenue, and Marvin Gardens. These cost \$260, \$260, and \$280, respectively, when purchased from the bank. What total amount must a player pay to the bank before houses can be built on the yellow properties? (*Source:* Hasbro, Inc.)

- **23.** In 2016, the average weekly pay for a fire inspector was \$1040. If such an inspector works 40 hours in one week, what is his or her hourly pay? (*Source:* Bureau of Labor Statistics)
- **25.** Three ounces of canned tuna in oil has 165 calories. How many calories does 1 ounce have? (*Source: Home and Garden Bulletin No.* 72, U.S. Department of Agriculture)
- 27. The average estimated 2016 U.S. population was 324,000,000. Between Memorial Day and Labor Day, 7 billion hot dogs are consumed. Approximately how many hot dogs were consumed per person between Memorial Day and Labor Day in 2016? Divide, but do not give the remainder part of the quotient. (*Source:* U.S. Census Bureau, National Hot Dog and Sausage Council)
- **29.** The Museum of Modern Art in New York City had approximately 268,300 visitors on average each month in a recent year. Use the fact that there are 12 months in a year to find the total number of visitors to this museum in one year.



- **31.** In 2015, Typhoon Lagoon at Walt Disney World in Orlando, Florida, hosted 2,294,000 visitors. Aquatica, also in Orlando, Florida, received 1,600,000. How many more people visited Typhoon Lagoon than Aquatica? (*Source:* Themed Entertainment Association)
- **33.** The length of the southern boundary of the conterminous United States is 1933 miles. The length of the northern boundary of the conterminous United States is 2054 miles longer than this. What is the length of the northern boundary? (*Source:* U.S. Geological Survey)



1933 miles

- **24.** In 2016, the average weekly pay for a paralegal was \$960. If the paralegal works 40 hours in one week, what is his or her hourly pay? (*Source:* Bureau of Labor Statistics)
- **26.** A whole cheesecake has 3360 calories. If the cheesecake is cut into 12 equal pieces, how many calories will each piece have? (*Source: Home and Garden Bulletin No.* 72, U.S. Department of Agriculture)
- **28.** In 2016, PetSmart employed approximately 55,000 associates and operated roughly 1500 stores. What is the average number of associates employed at each of its stores? Divide, but do not give the remainder part of the quotient. (*Source:* PetSmart)
- **30.** The National Air and Space Museum in Washington, D.C. had approximately 625,100 visitors on average each month in 2016. Use the fact that there are 12 months in a year to find the total number of visitors to this museum in 2016.



- **32.** In 2016, Target Corporation operated 1806 stores in the United States. Of these, 193 were in California. How many Target Stores were located in states other than California? (*Source:* Target Corporation)
- **34.** In humans, 14 muscles are required to smile. It takes 29 more muscles to frown. How many muscles does it take to frown?

35. An instructor at the University of New Orleans receives a paycheck every four weeks. Find how many paychecks he receives in a year. (A year has 52 weeks.)

Objective B *Solve. See Example 5.*

- 37. Find the total cost of 3 sweaters at \$38 each and 5 shirts at \$25 each.
 - **39.** A college student has \$950 in an account. She spends \$205 from the account on books and then deposits \$300 in the account. How much money is now in the account?

- **36.** A loan of \$6240 is to be paid in 48 equal payments. How much is each payment?
- **38.** Find the total cost of 10 computers at \$2100 each and 7 boxes of diskettes at \$12 each.
- **40.** The temperature outside was 57°F (degrees Fahrenheit). During the next few hours, it decreased by 18 degrees and then increased by 23 degrees. Find the new temperature.

The table shows the menu from a concession stand at the county fair. Use this menu to answer Exercises 41 and 42.

- **41.** A hungry college student is debating between the following two orders:
 - **a.** a hamburger, an order of onion rings, a candy bar, and a soda.

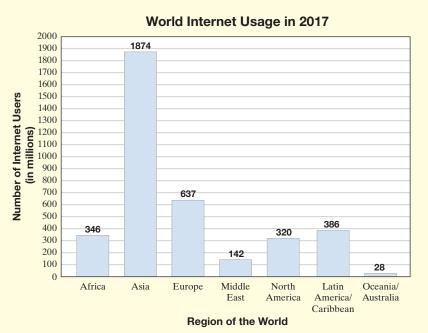
b. a hot dog, an apple, an order of french fries, and a soda. Which order will be cheaper? By how much?

- **42.** A family of four is debating between the following two orders:
 - a. 6 hot dogs, 4 orders of onion rings, and 4 sodas.

b. 4 hamburgers, 4 orders of french fries, 2 apples, and 4 sodas. Will the family save any money by ordering (**b**) instead of (**a**)? If so, how much?

Objectives A B Mixed Practice Use the bar graph to answer Exercises 43 through 50. (Source: Internet World Stats)

- **43.** Which region of the world listed had the greatest number of Internet users in 2017?
- **44.** Which region of the world listed had the least number of Internet users in 2017?
- **45.** How many more Internet users (in millions) did the world region with the most Internet users have than the world region with the fewest Internet users?
- **46.** How many more Internet users did Africa have than the Middle East in 2017?
- **47.** How many more Internet users did Latin America/Caribbean have than North America?
- **48.** Which region of the world had more Internet users, Europe or North America? How many more Internet users did it have?



Corky's Concession Stand Menu Item Price Hot dog \$3 Hamburger \$4 Soda \$1 Onion rings \$3 French fries \$2 Apple \$1 \$2 Candy bar

85

Find the average number of Internet users for the world regions listed in the graph.

- **49.** The world region with the greatest number of Internet users and the world region with the least number of Internet users.
- **50.** The four world regions with the least number of Internet users.

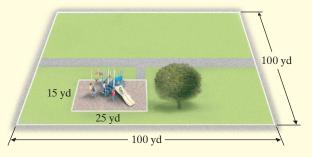
Solve.

- **51.** The learning lab at a local university is receiving new equipment. Twenty-two computers are purchased for \$615 each and three printers for \$408 each. Find the total cost for this equipment.
- **53.** The American Heart Association recommends consuming no more than 2400 milligrams of salt per day. (This is about the amount in 1 teaspoon of salt.) How many milligrams of sodium is this in a week?
- \triangle **55.** The Meishs' yard is in the shape of a rectangle and measures 50 feet by 75 feet. In their yard, they have a rectangular swimming pool that measures 15 feet by 25 feet.
 - **a.** Find the area of the entire yard.
 - **b.** Find the area of the swimming pool.
 - **c.** Find the area of the yard that is not part of the swimming pool.



52. The washateria near the local community college is receiving new equipment. Thirty-six washers are purchased for \$585 each and ten dryers are purchased for \$388 each. Find the total cost for this equipment.

- **54.** This semester a particular student pays \$1750 for room and board, \$709 for a meal ticket plan, and \$2168 for tuition. What is her total bill?
- **56.** The community is planning to construct a rectangular-shaped playground within the local park. The park is in the shape of a square and measures 100 yards on each side. The playground is to measure 15 yards by 25 yards.
 - **a.** Find the area of the entire park.
 - **b.** Find the area of the playground.
 - **c.** Find the area of the park that is not part of the playground.



Concept Extensions

- **57.** In 2016, United Parcel Service delivered about 4,893,000,000 packages worldwide, which generated revenue of approximately \$49,906,000,000. Round the revenue and number of packages to the nearest billion to estimate the average revenue generated by each package. (*Source:* UPS)
- **58.** In 2015, the United States Post Office received about 919,500,000 customer visits at its retail outlets. The total retail revenue for that year was approximately \$19,790,000,000. Round the retail revenue and customer visits to the nearest hundred million to estimate the average revenue generated by each customer. (*Source:* United States Postal Service)

1.9 Exponents, Square Roots, and Order of Operations

Objective A Using Exponential Notation 🜔

In the product $3 \cdot 3 \cdot 3 \cdot 3 \cdot 3 \cdot 3$, notice that 3 is a factor several times. When this happens, we can use a shorthand notation, called an **exponent**, to write the repeated multiplication.

 $\frac{3 \cdot 3 \cdot 3 \cdot 3 \cdot 3}{3 \text{ is a factor 5 times}}$ can be written as

- exponent

Read as "three to the fifth power."

— base

35

This is called **exponential notation.** The **exponent**, 5, indicates how many times the **base**, 3, is a factor.

The table below shows examples of reading exponential notation in words.

Expression	In Words
5 ²	"five to the second power" or "five squared"
5 ³	"five to the third power" or "five cubed"
54	"five to the fourth power"

Usually, an exponent of 1 is not written, so when no exponent appears, we assume that the exponent is 1. For example, $2 = 2^1$ and $7 = 7^1$.

Examples

Write using exponential notation.

1. $7 \cdot 7 \cdot 7 = 7^3$ **2.** $3 \cdot 3 = 3^2$ **3.** $6 \cdot 6 \cdot 6 \cdot 6 \cdot 6 = 6^5$ **4.** $3 \cdot 3 \cdot 3 \cdot 3 \cdot 17 \cdot 17 \cdot 17 = 3^4 \cdot 17^3$

Work Practice 1–4

Objective **B** Evaluating Exponential Expressions **C**

To **evaluate** an exponential expression, we write the expression as a product and then find the value of the product.

Examples

Evaluate.

5.
$$9^2 = 9 \cdot 9 = 81$$

6. $6^1 = 6$
7. $3^4 = 3 \cdot 3 \cdot 3 \cdot 3 = 81$
8. $5 \cdot 6^2 = 5 \cdot 6 \cdot 6 = 180$
Work Practice 5-8

Objectives

- A Write Repeated Factors Using Exponential Notation.
- B Evaluate Expressions Containing Exponents.
- C Evaluate the Square Root of a Perfect Square.
- D Use the Order of Operations.
- E Find the Area of a Square.

Practice 1–4

Write using exponential notation.
1. 8 · 8 · 8 · 8
2. 3 · 3 · 3
3. 10 · 10 · 10 · 10 · 10
4. 5 · 5 · 4 · 4 · 4 · 4 · 4 · 4

Practice 5-8Evaluate.5. 4^2 6. 7^3 7. 11^1 8. $2 \cdot 3^2$

Answers 1. 8⁴ 2. 3³ 3. 10⁵ 4. 5² · 4⁶ 5. 16 6. 343 7. 11 8. 18 Example 8 illustrates an important property: An exponent applies only to its base. The exponent 2, in $5 \cdot 6^2$, applies only to its base, 6.

Helpful Hint

An exponent applies only to its base. For example, $4 \cdot 2^3$ means $4 \cdot 2 \cdot 2 \cdot 2$.

Helpful Hint

Don't forget that 2^4 , for example, is *not* $2 \cdot 4$. The expression 2^4 means repeated multiplication of the same factor.

 $2^4 = 2 \cdot 2 \cdot 2 \cdot 2 = 16$, whereas $2 \cdot 4 = 8$

Concept Check Which of the following statements is correct?

- **a.** 3^6 is the same as $6 \cdot 6 \cdot 6$.
- **b.** "Eight to the fourth power" is the same as 8^4 .
- c. "Ten squared" is the same as 10^3 .
- **d.** 11^2 is the same as $11 \cdot 2$.

Objective C Evaluating Square Roots 🕑

A square root of a number is one of two identical factors of the number. For example,

 $7 \cdot 7 = 49$, so a square root of 49 is 7.

We use this symbol $\sqrt{}$ (called a radical sign) for finding square roots. Since

 $7 \cdot 7 = 49$, then $\sqrt{49} = 7$.

Examples Find each square root. 9. $\sqrt{25} = 5$ because $5 \cdot 5 = 25$ 10. $\sqrt{81} = 9$ because $9 \cdot 9 = 81$ 11. $\sqrt{0} = 0$ because $0 \cdot 0 = 0$ Work Practice 9–11

Helpful Hint

Make sure you understand the difference between squaring a number and finding the square root of a number.

 $9^2 = 9 \cdot 9 = 81$ $\sqrt{9} = 3$ because $3 \cdot 3 = 9$

Not every square root simplifies to a whole number. We will study this more in a later chapter. In this section, we will find square roots of perfect squares only.

Practice 9–11

Find each square root. 9. $\sqrt{100}$ 10. $\sqrt{4}$ 11. $\sqrt{1}$

Answers 9. 10 10. 2 11. 1

Concept Check Answer

Objective D Using the Order of Operations 🕗

Suppose that you are in charge of taking inventory at a local cell phone store. An employee has given you the number of a certain cell phone in stock as the expression

 $6 + 2 \cdot 30$

To calculate the value of this expression, do you add first or multiply first? If you add first, the answer is 240. If you multiply first, the answer is 66.



Mathematical symbols wouldn't be very useful if two values were possible for one expression. Thus, mathematicians have agreed that, given a choice, we multiply first.

 $6 + 2 \cdot 30 = 6 + 60$ Multiply. = 66 Add.

This agreement is one of several order of operations agreements.

Order of Operations

- **1.** Perform all operations within parentheses (), brackets [], or other grouping symbols such as fraction bars or square roots, starting with the innermost set.
- 2. Evaluate any expressions with exponents.
- **3.** Multiply or divide in order from left to right.
- 4. Add or subtract in order from left to right.

Below we practice using order of operations to simplify expressions.

Example 12 Simplify: $2 \cdot 4 - 3 \div 3$

Solution: There are no parentheses and no exponents, so we start by multiplying and dividing, from left to right.

 $2 \cdot 4 - 3 \div 3 = 8 - 3 \div 3$ Multiply. = 8 - 1 Divide. = 7 Subtract.

Work Practice 12

Example 13 Simplify: $4^2 \div 2 \cdot 4$

Solution: We start by evaluating 4^2 .

 $4^2 \div 2 \cdot 4 = 16 \div 2 \cdot 4$ Write 4^2 as 16.

Next we multiply or divide *in order* from left to right. Since division appears before multiplication from left to right, we divide first, then multiply.

 $16 \div 2 \cdot 4 = 8 \cdot 4 \quad \text{Divide.} \\ = 32 \quad \text{Multiply.}$

Practice 13 Simplify: $48 \div 3 \cdot 2^2$

Answers 12. 25 13. 64

Practice 12 Simplify: $9 \cdot 3 - 8 \div 4$

Work Practice 13

Practice 14 Simplify: $(10 - 7)^4 + 2 \cdot 3^2$

Example 14 Simplify:
$$(8-6)^2 + 2^3 \cdot 3$$

Solution: $(8-6)^2 + 2^3 \cdot 3 = 2^2 + 2^3 \cdot 3$ Simplify inside parentheses.
 $= 4 + 8 \cdot 3$ Write 2^2 as 4 and 2^3 as 8.
 $= 4 + 24$ Multiply.
 $= 28$ Add.

Work Practice 14

Example 15 Simplify:
$$4^3 + [3^2 - (10 \div 2)] - 7 \cdot 3$$

Practice 15 Simplify: $36 \div [20 - (4 \cdot 2)] + 4^3 - 6$

Practice 16

Simplify: $\frac{25 + 8 \cdot 2 - 3^3}{2(3-2)}$

Solution: Here we begin with the innermost set of parentheses.

$4^{3} + [3^{2} - (10 \div 2)] - 7 \cdot 3 = 4^{3} + [3^{2} - 5] - 7 \cdot 3$	Simplify inside parentheses.
$= 4^3 + [9-5] - 7 \cdot 3$	Write 3^2 as 9.
$= 4^3 + 4 - 7 \cdot 3$	Simplify inside brackets.
$= 64 + 4 - 7 \cdot 3$	Write 4^3 as 64.
= 64 + 4 - 21	Multiply.
= 47	Add and subtract from left to right.

Work Practice 15

Example 16 Simplify: $\frac{7-2\cdot 3+3^2}{5(2-1)}$

Solution: Here, the fraction bar is like a grouping symbol. We simplify above and below the fraction bar separately.

$$\frac{7-2\cdot 3+3^2}{5(2-1)} = \frac{7-2\cdot 3+9}{5(1)}$$
Evaluate 3² and (2-1).
$$= \frac{7-6+9}{5}$$
Multiply 2 · 3 in the numerator and multiply 5
and 1 in the denominator.
$$= \frac{10}{5}$$
Add and subtract from left to right.
$$= 2$$
Divide.

Work Practice 16

Example 17 Simplify: $64 \div \sqrt{64} \cdot 2 + 4$ **Solution:** $64 \div \sqrt{64} \cdot 2 + 4 = \underline{64} \div \underline{8} \cdot 2 + 4$ Find the square root. $= \underline{8 \cdot 2} + 4$ Divide. = 16 + 4 Multiply. = 20 Add.

Practice 17 Simplify: $81 \div \sqrt{81} \cdot 5 + 7$

Answers 14. 99 15. 61 16. 7 17. 52

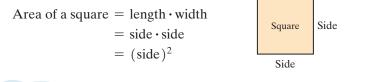
Work Practice 17

Objective E Finding the Area of a Square 🕑

Since a square is a special rectangle, we can find its area by finding the product of its length and its width.

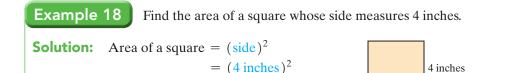
Area of a rectangle = length \cdot width

By recalling that each side of a square has the same measurement, we can use the following procedure to find its area:



Helpful Hint

Recall from Section 1.6 that area is measured in **square** units while perimeter is measured in units.



= 16 square inches

The area of the square is 16 square inches.

Work Practice 18

Calculator Explorations Exponents

To evaluate an exponent such as 4 ⁷ on a calculator, find
the keys marked y^x or \wedge and $=$ or ENTER. To
evaluate 4 ⁷ , press the keys 4 y^{x} (or \wedge) 7 then =
or ENTER . The display will read 16384. Thus,
$4^7 = 16,384.$

Use a calculator to evaluate.

1.	46	2.	5 ⁶	3.	5 ⁵
4.	7 ⁶	5.	2^{11}	6.	6 ⁸

Order of Operations

To see whether your calculator has the order of operations built in, evaluate $5 + 2 \cdot 3$ by pressing the keys $5 + 2 \times 3$ then = or ENTER. If the display reads 11, your calculator does have the order of operations built in. This means that most of the time, you can key in a problem exactly as it is written and

the calculator will perform operations in the proper order. When evaluating an expression containing parentheses, key in the parentheses. (If an expression contains brackets, key in parentheses.) For example, to evaluate 2[25 - (8 + 4)] - 11, press the keys $2 \times (25 - (8 + 4)] - 11$, press the keys $2 \times (25 - (8 + 4)] - 11$, press the keys $2 \times (125 - (18 + 4)) - 11$ then = or ENTER. The display will read 15.

Answer

18. 144 sq cm

Practice 18

Find the area of a square whose

side measures 12 centimeters.

Use a calculator to evaluate.

7. $7^4 + 5^3$ 8. $12^4 - 8^4$ 9. $63 \cdot 75 - 43 \cdot 10$ 10. $8 \cdot 22 + 7 \cdot 16$ 11. $4(15 \div 3 + 2) - 10 \cdot 2$ 12. 155 - 2(17 + 3) + 185

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank.

	addition subtraction	multiplication division	exponent square root	base
1.	In $2^5 = 32$, the 2 is call	alled the	and the 5 is called the	
2.	To simplify $8 + 2 \cdot 6$,	which operation shoul	d be performed first? _	
3.	To simplify $(8 + 2)$.	6, which operation sho	ould be performed first?	?
4.	To simplify $9(3-2)$	\div 3 + 6, which operation	tion should be perform	ed first?
5.	To simplify $8 \div 2 \cdot 6$,	which operation shoul	d be performed first? –	
6.	The of	a whole number is one	e of two identical factor	s of the number.

Martin-Gay Interactive Videos Watch the section lecture video and answer the following questions.

	Objective A 7.	In the 🖪 Example 1 expression, what is the 3 called and what
	Objective B 8.	is the 12 called? As mentioned in Example 4, what "understood exponent" does any number we've worked with before have?
	-	From Example 7, how do we know that $\sqrt{64} = 8?$
	Objective D 10.	List the three operations needed to evaluate 🖽 Example 9 in
see Video 1.9 🍅	Objective E 11.	the order they should be performed. 🕗 As explained in the lecture before 🛱 Example 12, why does
		the area of a square involve an exponent whereas the area of a rectangle usually does not?

1.9 Exercise Set MyLab Math 🕗

Objective A *Write using exponential notation. See Examples 1 through 4.*

1. 4·4·4	2. 5 • 5 • 5 • 5	3. 7 • 7 • 7 • 7 • 7 • 7	4. 6.6.6.6.6.6.6
5. 12 • 12 • 12	6. 10 • 10 • 10	○7. 6·6·5·5·5	8. 4·4·3·3·3
9. 9·8·8	10. 7 • 4 • 4 • 4	11. 3·2·2·2·2	12. 4·6·6·6·6
13. 3·2·2·2·2·5·5·	• 5 • 5 • 5	14. 6·6·2·9·9·9·9	

Objective B	Evaluate. See E	xamples 5 through 8.			
15. 8 ²	16. 6 ²	• 17. 5 ³	18. 6 ³	19. 2 ⁵	20. 3 ⁵
21. 1 ¹⁰	22. 1 ¹²	23. 7 ¹	24. 8 ¹	25. 2 ⁷	26. 5 ⁴
27. 2 ⁸	28. 3 ³	29. 4 ⁴	30. 4 ³	31. 9 ³	32. 8 ³
33. 12 ²	34. 11 ²	35. 10 ²	36. 10 ³	37. 20 ¹	38. 14 ¹
39. 3 ⁶	40. 4 ⁵	41. 3 · 2 ⁶	42. 5 · 3 ²	43. 2 · 3 ⁴	44. 2 • 7 ²
Objective C	Find each squa	re root. See Examples 9	9 through 11.		
○ 45. √9	40	5. $\sqrt{36}$	○47. √64	48.	$\sqrt{121}$
49. $\sqrt{144}$	50	D. $\sqrt{0}$	51. $\sqrt{16}$	52.	$\sqrt{169}$
Objective D	Simplify. See E:	xamples 12 through 16.	(This section does no	ot contain square root	ts.)
○ 53. 15 + 3 • 2	54	1. 24 + 6 · 3	○55. 14 ÷ 7 • 2	+ 3 56.	$100 \div 10 \cdot 5 + 4$
57. 32 ÷ 4 - 3	58	3. 42 ÷ 7 − 6	59. $13 + \frac{24}{8}$	60.	$32 + \frac{8}{2}$
61. 6 • 5 + 8 • 2	62	2. $3 \cdot 4 + 9 \cdot 1$	63. $\frac{5+12 \div}{1^7}$	<u>4</u> 64.	$\frac{6+9\div3}{3^2}$
65. $(7 + 5^2) \div$	$4 \cdot 2^3$	66. 6 ² · (10 -	- 8)	67. $5^2 \cdot (10 - $	8) + 2^3 + 5^2
68. 5 ³ ÷ (10 +	$(15) + 9^2 + 3^3$	69. $\frac{18+6}{2^4-2^2}$		70. $\frac{40+8}{5^2-3^2}$	
71. (3 + 5) • (9	- 3)	72. (9 – 7)	(12 + 18)	•73. $\frac{7(9-6)}{3^2-3}$	+3/3

74.
$$\frac{5(12-7)-4}{5^2-18}$$
75. $8 \div 0 + 37$
76. $18 - 7 \div 0$
77. $2^4 \cdot 4 - (25 \div 5)$
78. $2^3 \cdot 3 - (100 \div 10)$
79. $3^4 - [35 - (12 - 6)]$
80. $[40 - (8 - 2)] - 2^5$
81. $(7 \cdot 5) + [9 \div (3 \div 3)]$
82. $(18 \div 6) + [(3 + 5) \cdot 2]$

83.
$$8 \cdot [2^2 + (6-1) \cdot 2] - 50 \cdot 2$$

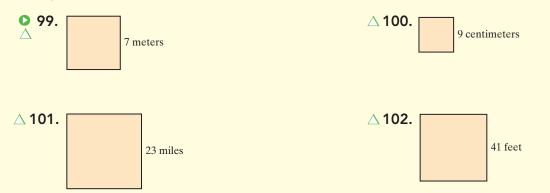
84. $35 \div [3^2 + (9-7) - 2^2] + 10 \cdot 3$

85.
$$\frac{9^2 + 2^2 - 1^2}{8 \div 2 \cdot 3 \cdot 1 \div 3}$$
86.
$$\frac{5^2 - 2^3 + 1^4}{10 \div 5 \cdot 4 \cdot 1 \div 4}$$

Simplify. See Examples 12 through 17. (This section does contain square roots.)

87. $6 \cdot \sqrt{9} + 3 \cdot \sqrt{4}$ **88.** $3 \cdot \sqrt{25} + 2 \cdot \sqrt{81}$ **89.** $4 \cdot \sqrt{49} - 0 \div \sqrt{100}$ **90.** $7 \cdot \sqrt{36} - 0 \div \sqrt{64}$ **91.** $\frac{\sqrt{4} + 4^2}{5(20 - 16) - 3^2 - 5}$ **92.** $\frac{\sqrt{9} + 9^2}{3(10 - 6) - 2^2 - 1}$ **93.** $\sqrt{81} \div \sqrt{9} + 4^2 \cdot 2 - 10$ **94.** $\sqrt{100} \div \sqrt{4} + 3^3 \cdot 2 - 20$ **95.** $[\sqrt{225} \div (11 - 6) + 2^2] + (\sqrt{25} - \sqrt{1})^2$ **96.** $[\sqrt{169} \div (20 - 7) + 2^5] - (\sqrt{4} + \sqrt{9})^2$ **97.** $7^2 - \{18 - [40 \div (4 \cdot 2) + \sqrt{4}] + 5^2\}$ **98.** $29 - \{5 + 3[8 \cdot (10 - \sqrt{64})] - 50\}$

Objective E Mixed Practice (Sections 1.3 and 1.6) Find the area and perimeter of each square. See Example 18.



Concept Extensions

Answer the following true or false. See the Concept Check in this section.

103. "Six to the fifth power" is the same as 6^5 . **104.** "Seven squared" is the same as 7^2 . **105.** 2^5 is the same as $5 \cdot 5$. **106.** 4^9 is the same as $4 \cdot 9$. Insert grouping symbols (parentheses) so that each given expression evaluates to the given number.

107. $2 + 3 \cdot 6 - 2$; evaluates to 28 **108.** $2 + 3 \cdot 6 - 2$; evaluates to 20 **109.** $24 \div 3 \cdot 2 + 2 \cdot 5$; evaluates to 14

- \triangle **111.** A building contractor is bidding on a contract to install gutters on seven homes in a retirement community, all in the shape shown. To estimate the cost of materials, she needs to know the total perimeter of all seven homes. Find the total perimeter.
 - **112.** The building contractor from Exercise **111** plans to charge \$4 per foot for installing vinyl gutters. Find the total charge for the seven homes given the total perimeter answer to Exercise 111.

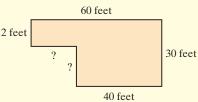
Simplify.

a 113. $(7 + 2^4)^5 - (3^5 - 2^4)^2$

115. Write an expression that simplifies to 5. Use multiplication, division, addition, subtraction, and at least one set of parentheses. Explain the process you would use to simplify the expression.

114.
$$25^3 \cdot (45 - 7 \cdot 5) \cdot 5$$

116. Explain why $2 \cdot 3^2$ is not the same as $(2 \cdot 3)^2$.



- **110.** $24 \div 3 \cdot 2 + 2 \cdot 5$; evaluates to 15
 - 12 feet

Chapter 1 Group Activity

Modeling Subtraction of Whole Numbers

A mathematical concept can be represented or modeled in many different ways. For instance, subtraction can be represented by the following symbolic model:

11 - 4

The following verbal models can also represent subtraction of these same quantities:

> "Four subtracted from eleven" or "Eleven take away four"

Physical models can also represent mathematical concepts. In these models, a number is represented by that many objects. For example, the number 5 can be represented by five pennies, squares, paper clips, tiles, or bottle caps.



A physical representation of the number 5

Take-Away Model for Subtraction: 11 – 4

- Start with 11 objects.
- Take 4 objects away.
- How many objects remain?

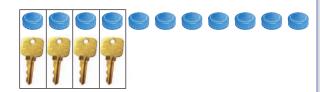
Start:



Comparison Model for Subtraction: 11 – 4

• Start with a set of 11 of one type of object and a set of 4 of another type of object.

• Make as many pairs that include one object of each type as possible.



• How many more objects left are in the larger set?

Missing Addend Model for Subtraction: 11 – 4

- Start with 4 objects.
- Continue adding objects until a total of 11 is reached.
- How many more objects were needed to give a total of 11?



Group Activity

Use an appropriate physical model for subtraction to solve each of the following problems. Explain your reasoning for choosing each model.

- **1.** Sneha has assembled 12 computer components so far this shift. If her quota is 20 components, how many more components must she assemble to reach her quota?
- **2.** Yuko has 14 daffodil bulbs to plant in her yard. She planted 5 bulbs in the front yard. How many bulbs does she have left for planting in the backyard?
- **3.** Todd is 19 years old and his sister Tanya is 13 years old. How much older is Todd than Tanya?

Chapter 1 Vocabulary Check

Fill in each blank with one of the words or phrases listed below.

difference	area	square root
place value	factor	quotient
sum	whole numbers	perimeter

- **1.** The _____ are 0, 1, 2, 3, . . .
- 2. The ______ of a polygon is its distance around or the sum of the lengths of its sides.
- **3.** The position of each digit in a number determines its _____.
- **4.** A(n) ______ is a shorthand notation for repeated multiplication of the same factor.
- 5. To find the ______ of a rectangle, multiply length times width.
- 6. A(n) ______ of a number is one of two identical factors of the number.
- 7. The ______ used to write numbers are 0, 1, 2, 3, 4, 5, 6, 7, 8, and 9.
- 8. The ______ of a list of numbers is their sum divided by the number of numbers.

addend	divisor	minuend
subtrahend	exponent	digits
dividend	average	product

Use the facts below for Exercises 9 through 18.

$$2 \cdot 3 = 6$$
 $4 + 17 = 21$ $20 - 9 = 11$ $\frac{7}{5)35}$

- 9. The 5 above is called the _____
- **10.** The 35 above is called the _____
- **11.** The 7 above is called the _____.
- **12.** The 3 above is called a(n) _____.
- **13.** The 6 above is called the _____
- 14. The 20 above is called the _____.
- **15.** The 9 above is called the _____
- **16.** The 11 above is called the _____
- **17.** The 4 above is called a(n) _____
- 18. The 21 above is called the _____

Helpful

To help, don't forget to take these:

- Chapter 1 Getting Ready for the Test on page 108
- Chapter 1 Test on page 109

Then check all of your answers at the back of this text. For further review, the step-by-step video solutions to any of these exercises are located in MyLab Math.

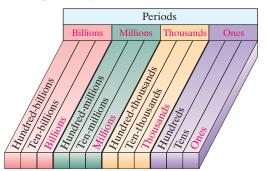
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Chapter Highlights

Definitions and ConceptsExamplesSection 1.2Place Value, Names for Numbers, and Reading TablesThe whole numbers are 0, 1, 2, 3, 4, 5,0, 14, 968, 5,268,619 are whole numbers.

The **natural numbers** are 1, 2, 3, 4, 5,

The position of each digit in a number determines its **place value.** A place-value chart is shown next with the names of the periods given.



Zero is a whole number but not a natural number.

	Definitions and Concepts	Examples
		umbers, and Reading Tables (continued)
in each	e a whole number in words, write the number period followed by the name of the period. ame of the ones period is not included.)	9,078,651,002 is written as nine billion, seventy-eight million, six hundred fifty-one thousand, two.
	e a whole number in standard form, write the r in each period, followed by a comma.	Four million, seven hundred six thousand, twenty-eight is written as 4,706,028.
	Section 1.3 Adding Who	le Numbers and Perimeter
then the	whole numbers, add the digits in the ones place, e tens place, then the hundreds place, and so on, g when necessary.	Find the sum: $\begin{array}{r} 211\\ 2689 \leftarrow addend\\ 1735 \leftarrow addend\\ \underline{+ \ 662} \leftarrow addend\\ \overline{5086} \leftarrow sum\end{array}$
The perimeter of a polygon is its distance around or the sum of the lengths of its sides.		\triangle Find the perimeter of the polygon shown. 2 feet 9 feet The perimeter is 5 feet + 3 feet + 9 feet + 2 feet = 19 feet.
	Section 1.4 Subtrac	ting Whole Numbers
To subtract whole numbers, subtract the digits in the ones place, then the tens place, then the hundreds place, and so on, borrowing when necessary.		Subtract: $79^{\$15}_{954} \leftarrow \text{minuend}$ $-5673 \leftarrow \text{subtrahend}$ $2281 \leftarrow \text{difference}$
	Section 1.5 Round	ding and Estimating
Rounding Whole Numbers to a Given Place Value		Round 15,721 to the nearest thousand.
Step 1: Step 2:	Locate the digit to the right of the given place value. If this digit is 5 or greater, add 1 to the digit in the given place value and replace each digit to its right with 0.	Add 1 $\xrightarrow{15}$, $\xrightarrow{7}$ 21 Replace with zeros. Since the circled digit is 5 or greater, add 1 to the given place value and replace digits to its right with zeros.
Step 3:	If this digit is less than 5, replace it and each digit to its right with 0.	15,721 rounded to the nearest thousand is 16,000.

Definitions and Concepts	Examples
Section 1.6 Multiplying	Whole Numbers and Area
To multiply 73 and 58, for example, multiply 73 and 8, then 73 and 50. The sum of these partial products is the product of 73 and 58. Use the notation to the right.	$73 \leftarrow \text{factor}$ $\frac{\times 58}{584} \leftarrow \text{factor}$ $\frac{3650}{4234} \leftarrow 73 \times 8$ $\frac{3650}{4234} \leftarrow \text{product}$
To find the area of a rectangle, multiply length times width.	△ Find the area of the rectangle shown. 11 meters 7 meters
	area of rectangle = length \cdot width
	= (11 meters)(7 meters)
	= 77 square meters
Section 1.7 Divid	ing Whole Numbers
Division Properties of 0	
The quotient of 0 and any number (except 0) is 0.	$\begin{vmatrix} \frac{0}{5} = 0 \\ 7 \\ \vdots \\ \vdots$
The quotient of any number and 0 is not a number. We say that this quotient is undefined.	$\frac{7}{0}$ is undefined
To divide larger whole numbers, use the process called long division as shown to the right.	$507 R \ 2 \leftarrow \text{ quotient and remainder}$ divisor $\rightarrow 14$)7100 $\leftarrow \qquad$ dividend $-70\downarrow \qquad 5(14) = 70$ Subtract and bring down the 0. $-0\downarrow \qquad 0(14) = 0$ 100 Subtract and bring down the 0. $-98 \qquad 7(14) = 98$ Subtract. The remainder is 2. To check, see that $507 \cdot 14 + 2 = 7100$.
The average of a list of numbers is	Find the average of 23, 35, and 38.
average = $\frac{\text{sum of numbers}}{\text{number}}$	average = $\frac{23 + 35 + 38}{3} = \frac{96}{3} = 32$

Definitions and Concepts	Examples
Section 1.8 An Introdu	ction to Problem Solving
Problem-Solving Steps1. UNDERSTAND the problem.	 Suppose that 225 tickets are sold for each performance of a play. How many tickets are sold for 5 performances? 1. UNDERSTAND. Read and reread the problem. Since we want the number of tickets for 5 performances, we multiply.
2. TRANSLATE the problem.	2. TRANSLATE. number of tickets is number of performances is
3. SOLVE the problem.4. INTERPRET the results.	 3. SOLVE: See if the answer is reasonable by also estimating. ¹²/₂₂₅ rounds to 200 × 5/1125 exact × 5/1000 estimate 4. INTERPRET. Check your work. The product is reasonable since 1125 is close to our estimated answer of 1000, and state your conclusion: There
Section 1.9 Exponents, Square	are 1125 tickets sold for 5 performances.
An exponent is a shorthand notation for repeated multiplication of the same factor. A square root of a number is one of two identical factors of the number.	$\sqrt[\bullet]{exponent}$ $3^{4} = \underbrace{3 \cdot 3 \cdot 3 \cdot 3}_{4 \text{ factors of } 3} = 81$ base 4 factors of 3 $\sqrt{36} = 6 \text{because} 6 \cdot 6 = 36$ $\sqrt{121} = 11 \text{because} 11 \cdot 11 = 121$ $\sqrt{0} = 0 \text{because} 0 \cdot 0 = 0$
 Order of Operations 1. Perform all operations within parentheses (), brackets [], or other grouping symbols such as square roots or fraction bars, starting with the innermost set. 2. Evaluate any expressions with exponents. 3. Multiply or divide in order from left to right. 4. Add or subtract in order from left to right. The area of a square is (side)². 	Simplify: $\frac{5+3^2}{2(7-6)}$ Simplify above and below the fraction bar separately. $\frac{5+3^2}{2(7-6)} = \frac{5+9}{2(1)}$ Evaluate 3 ² above the fraction bar. $= \frac{14}{2}$ Add. Multiply. = 7 Divide. Find the area of a square with side length 9 inches. Area of the square = (side) ² $= (9 \text{ inches})^2$ = 81 square inches

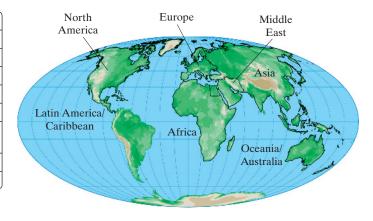
Chapter 1 Review

(1.2) Determine the place value of the digit 4 in each whole number.

1. 7640	2. 46,200,120
Write each whole number in words.	
3. 7640	4. 46,200,120
Write each whole number in expanded form.	
5. 3158	6. 403,225,000
Write each whole number in standard form.	
7. Eighty-one thousand, nine hundred	8. Six billion, three hundred four million

The following table shows the Internet and Facebook use of world regions as of June 2016. Use this table to answer *Exercises 9 through 12.*

Internet Users	Facebook Users
345,436,500	146,637,000
1,873,522,600	559,003,000
636,831,820	328,273,740
141,711,760	76,000,000
320,021,200	223,081,200
385,842,300	326,975,340
27,506,000	19,463,250
	345,436,500 1,873,522,600 636,831,820 141,711,760 320,021,200 385,842,300



- **9.** Find the number of Internet users in Europe.
- **11.** Which world region had the largest number of Facebook users?
- **(1.3)** *Add.*

- **10.** Find the number of Facebook users in Latin America/Caribbean.
- **12.** Which world region had the smallest number of Internet users?

13. 17 + 46 **14.** 28 + 39 **15.** 25 + 8 + 15 **16.** 27 + 9 + 41 **17.** 932 + 24

 18. 819 + 21 **19.** 567 + 7383 **20.** 463 + 6787 **21.** 91 + 3623 + 497 **22.** 82 + 1647 + 238

Solve.

- **23.** Find the sum of 86, 331, and 909.
- **25.** What is 26,481 increased by 865?
- **27.** The distance from Chicago to New York City is 714 miles. The distance from New York City to New Delhi, India, is 7318 miles. Find the total distance from Chicago to New Delhi if traveling by air through New York City.

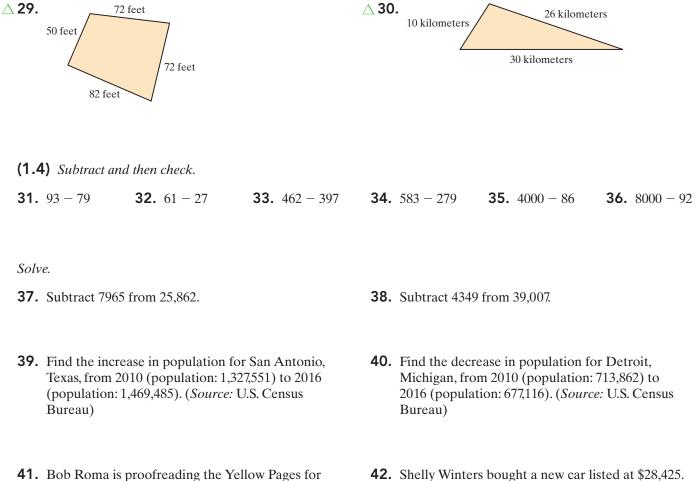
- **24.** Find the sum of 49, 529, and 308.
- **26.** What is 38,556 increased by 744?
- **28.** Susan Summerline earned salaries of \$62,589, \$65,340, and \$69,770 during the years 2014, 2015, and 2016, respectively. Find her total earnings during those three years.

She received a discount of \$1599 and a factory

rebate of \$1200. Find how much she paid for

the car.

Find the perimeter of each figure.



his county. If he has finished 315 pages of the total 712 pages, how many pages does he have left to proofread? Copyright 2019 Pearson Education, Inc.

February to April?

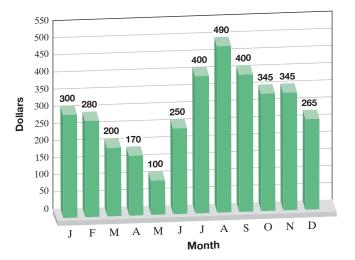
August?

43. During what month was the balance the least?

44. During what month was the balance the greatest?

46. By how much did his balance increase from June to

45. By how much did his balance decrease from



The following bar graph shows the monthly savings account balance for a freshman attending a local community college. Use this graph to answer Exercises 43 through 46.

- (1.5) Round to the given place.
- **47.** 93 to the nearest ten
- **49.** 467 to the nearest ten
- **51.** 4832 to the nearest hundred
- **53.** 49,683,712 to the nearest million
- **55.** In 2015, there were 263,610,220 registered vehicles in the United States. Round this number to the nearest million. (*Source:* U.S. Department of Transportation)

50. 493 to the nearest hundred

48. 45 to the nearest ten

- **52.** 57,534 to the nearest thousand
- **54.** 768,542 to the nearest hundred-thousand
- **56.** In 2013, there were 98,454 public elementary and secondary schools in the United States. Round this number to the nearest thousand. (*Source:* National Center for Education Statistics)

Estimate the sum or difference by rounding each number to the nearest hundred.

57. 4892 + 647 + 1876

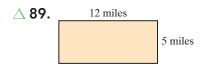
- **58.** 5925 1787
- **59.** A group of students took a week-long driving trip and traveled 628, 290, 172, 58, 508, 445, and 383 miles on seven consecutive days. Round each distance to the nearest hundred to estimate the distance they traveled.
- **60.** The estimated 2016 population of Houston, Texas, was 2,239,558, and for San Diego, California, it was 1,376,410. Round each number to be nearest hundred-thousand and estimate how much larger Houston is than San Diego. (*Source:* U.S. Census Bureau)

104	Chapter 1 The Whole N	Chapter 1 The Whole Numbers		
(1.6) <i>Multiply.</i>				
61. 273 <u>× 7</u>	62. 349 × 4	63. 47×30	64. 69 <u>× 42</u>	
65. 20(8)(5)	66. 25(9)(4)	67. 48 <u>× 77</u>	68. 77 × 22	
69. 49 • 49 • 0	70. 62 · 88 · 0	71. 586 <u>× 29</u>	72. 242 <u>× 37</u>	
73. 642 <u>×177</u>	74. 347 <u>× 129</u>	75. 1026 <u>× 401</u>	76. 2107 <u>× 302</u>	
77. 375 · 1000	78. 108 • 1000	79. 30 • 400	80. 50 • 700	
81. 1700 · 3000		82. 1900 • 4000		
Solve.				
83. Find the product of 5 ar	nd 230.	84. Find the product of 6 an	nd 820.	
85. Multiply 9 and 12.		86. Multiply 8 and 14.		

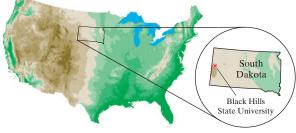
87. One ounce of Swiss cheese contains 8 grams of fat. How many grams of fat are in 3 ounces of Swiss cheese? (*Source: Home and Garden Bulletin No.* 72, U.S. Department of Agriculture)

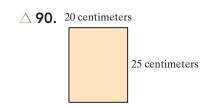


Find the area of each rectangle.



88. The cost for a South Dakota resident to attend Black Hills State University full-time is \$7949 per semester. Determine the cost for 20 students to attend full-time. (*Source:* Black Hills State University)





91. $\frac{18}{6}$	92. $\frac{36}{9}$	93. 42 ÷ 7	94. 35 ÷ 5	95. 27 ÷ 5
96. 18 ÷ 4	97. 16 ÷ 0	98. 0 ÷ 8	99. 9 ÷ 9	100. 10 ÷ 1
101. 0 ÷ 668	102. 918 ÷ 0	103. 5)167	104. 8)159	105. 26)626
106. 19)680	107. 47)23,792	108. 53)48,111	109. 207)578,291	110. 306)615,732

Solve.

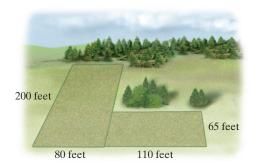
- **111.** Find the quotient of 92 and 5.
- **113.** One foot is 12 inches. Find how many feet there are in 5496 inches.
- **115.** Find the average of the numbers 76, 49, 32, and 47.
- **112.** Find the quotient of 86 and 4.
- **114.** One mile is 1760 yards. Find how many miles there are in 22,880 yards.
- **116.** Find the average of the numbers 23, 85, 62, and 66.

(1.8) Solve.

- **117.** A box can hold 24 cans of corn. How many boxes can be filled with 648 cans of corn?
- **119.** In 2015, General Motors spent \$3,500,000,000 on television advertising, while Toyota spent only \$1,800,000,000. How much more did General Motors spend on television advertising than Toyota? (*Source:* Automotive News)
- **121.** A golf pro orders shirts for the company sponsoring a local charity golfing event. Shirts size large cost \$32 while shirts size extra-large cost \$38. If 15 large shirts and 11 extra-large shirts are ordered, find the cost.



- **118.** If a ticket to a movie costs \$6, how much do 32 tickets cost?
- 120. The cost to banks when a person uses an ATM (Automatic Teller Machine) is 27¢. The cost to banks when a person deposits a check with a teller is 48¢ more. How much is this cost?
- **122.** Two rectangular pieces of land are purchased: one that measures 65 feet by 110 feet and one that measures 80 feet by 200 feet. Find the total area of land purchased. (*Hint:* Find the area of each rectangle, then add.)



106		Chapter 1 The Whole	Numbers		
(1.9)	Simplify.				
123.	7 ²	124. 5 ³	125.	$5 \cdot 3^2$	126. 4 · 10 ²
127.	18 ÷ 3 + 7	128. 12 – 8 ÷ 4	129.	$\frac{5(6^2-3)}{3^2+2}$	130. $\frac{7(16-8)}{2^3}$
131.	$48 \div 8 \cdot 2$		132.	$27 \div 9 \cdot 3$	
133.	$2 + 3[1^5 + (20 - 17)]$	$3] + 5 \cdot 2$	134.	$21 - [2^4 - (7 - 5) -$	$10] + 8 \cdot 2$
Simpl	ify. (These exercises conta	in square roots.)			
135.	$\sqrt{81}$	136. $\sqrt{4}$	137.	$\sqrt{1}$	138. $\sqrt{0}$
139.	$4\cdot\sqrt{25}-2\cdot7$		140.	$8\cdot\sqrt{49}-3\cdot9$	
141.	$(\sqrt{36} - \sqrt{16})^3 \cdot [10^2 \div$	(3 + 17)]	142.	$(\sqrt{49}-\sqrt{25})^3 \cdot [9^2 \div$	(2 + 7)]
143.	$\frac{5\cdot 7-3\cdot \sqrt{25}}{2(\sqrt{121}-3^2)}$		144.	$\frac{4\cdot 8-1\cdot \sqrt{121}}{3(\sqrt{81}-2^3)}$	
Find t	he area of each square.				
∆ 145 .	A square with side lengt	h of 7 meters.	∆ 146.	3 inches	

Mixed Review

Perform the indicated operati 147. 375 – 68	ions. 148. 729 – 47	149. 723 × 3	150. 629 × 4
151. 264 + 39 + 598	152. 593 + 52 + 766	153. 13)5962	154. 18)4267
155. 1968 × 36	156. 5324 × 18	157. 2000 – 356	158. 9000 - 519

Round to the	e given place.	
159. 736	o the nearest ten	160. 258,371 to the nearest thousand
161. 1999	to the nearest hundred	162. 44,499 to the nearest ten thousand
Write each	vhole number in words.	
163. 36,9	1	164. 154,863
Write each	whole number in standard form.	
	nty thousand, nine hundred -three	166. Forty-three thousand, four hundred one
Simplify.		
167. 4 ³	168. 5 ³	169. $\sqrt{144}$ 170. $\sqrt{100}$
171. 24 ÷	4.2 172. $\sqrt{256} - 3.5$	173. $\frac{8(7-4)-10}{4^2-3^2}$ 174. $\frac{(15+\sqrt{9})\cdot(8-5)}{2^3+1}$
Solve.		
175. 36 d	vided by 9 is what number?	176. What is the product of 2 and 12?
177. 16 ir	creased by 8 is what number?	178. 7 subtracted from 21 is what number?

The following table shows the 2015 and 2016 average Major League Baseball salaries (rounded to the nearest thousand) for the five teams with the largest payrolls for 2016. Use this table to answer Exercises 179 and 180. (Source: CBSSports.com, Associated Press)

Team	2016 Average Salary	2015 Average Salary
Los Angeles Dodgers	\$7,445,000	\$9,092,000
New York Yankees	\$7,361,000	\$7,309,000
Boston Red Sox	\$6,072,000	\$6,247,000
Detroit Tigers	\$6,891,000	\$5,794,000
San Francisco Giants	\$5,946,000	\$5,756,000

181. A manufacturer of drinking glasses ships his delicate stock in special boxes that can hold 32 glasses. If 1714 glasses are manufactured, how many full boxes are filled? Are there any glasses left over?

- **179.** How much more was the average salary for a San Francisco Giants player in 2016 than in 2015?
- **180.** How much less was the average Boston Red Sox salary in 2016 than the average New York Yankee salary in 2016?
- **182.** A teacher orders 2 small white boards for \$27 each and 8 boxes of dry erase pens for \$4 each. What is her total bill before taxes?

Chapter 1 Getting Ready for the Test C

MATCHING Exercises 1 through 16 are Matching exercises. Choices may be used more than once or not at all.

For Exercises 1 through 4, match the digit from the number 189, 570, 264 in the left column with the correct place value listed in the right columns.

A. hundreds place
B. thousands place
C. ten-thousands place
D. millions place
E. ten-millions place
F. billions place
4. 8

The number 5,726,953 is rounded to different place values. For Exercises 5 through 8, match each rounding of the number in the left column to the place it is rounded to in the right column. One exercise has 2 correct answers.

▶ 5. 6,000,000	A. the nearest ten
6. 5,726,950	B. the nearest hundred
○ 7. 5,727,000	C. the nearest million
, ,	D. the nearest ten-thousand
8 . 5,730,000	E. the nearest thousand

The number 27,600 is multiplied and divided by different powers of 10. For Exercises 9 through 12, match each number in the left column with the correct operation described in the right column.

09.	276,000	A.	27,600 divided by 10
0 10.	276	B.	27,600 multiplied by 10
0 11.	2760		27,600 divided by 100
● 12.	2,760,000	D.	27,600 multiplied by 100

For Exercises 13 through 16, match each exercise in the left column with its correct answer in the right column.

▶ 13. 9 ²	A. 3
○ 14. √9	B. 81
● 15. 9 ¹	C. 15
	D. 0
16. $16 - 4 \div 2^2$	E. 9

MULTIPLE CHOICE For Exercises 17 through 20, do not calculate, but use rounding to choose the best estimated answer.

● 17. 49 × 52			
A. 25	B. 250	C. 2500	D. 25,000
● 18. 3275 × 11			
A. 32,750	B. 3275	C. 327,500	D. 3,275,000
▶ 19. 87 + 86 + 91			
A. 27,000	B. 270	C. 2700	D. 27
20. 1000 − 62			
A. 940	B. 400	C. 40	D. 9400

Chapter 1

Answers

Test

Simplify.

1. Write 82,426 in words.

2. Write "four hundred two thousand, five hundred fifty" in standard form.

3. 59 + 82	● 4. 600 - 487	$\bigcirc 5. 496 \\ \times 30$
○ 6. 52,896 ÷ 69	•7. $2^3 \cdot 5^2$	$\bullet 8. \ \sqrt{4} \cdot \sqrt{25}$
▶ 9. 0 ÷ 49	● 10. 62 ÷ 0	Q11. $(2^4 - 5) \cdot 3$
○ 12. 16 + 9 ÷ 3 • 4 − 7	●13.	$\frac{64 \div 8 \cdot 2}{(\sqrt{9} - \sqrt{4})^2 + 1}$
$\mathbf{O} 1 1 = \mathbf{O} \begin{bmatrix} (\mathbf{c} + \mathbf{t})^2 + (\mathbf{c}) \end{bmatrix}$		

0 14.	2[(6 -	$(4)^2 +$	(22 -	$(19)^2] + 10$	0 15.	$5698 \cdot 1000$
--------------	--------	-----------	-------	-----------------	--------------	-------------------

● **16.** 8000 • 1400 ● **17.** Round 52,369 to the nearest thousand.

Estimate each sum or difference by rounding each number to the nearest hundred.

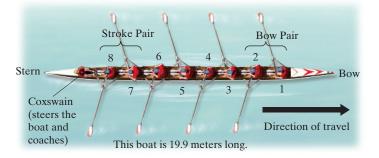
1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 11. 12. 13. 14. 15. 16. 17. 18.

| ▶ 18. 6289 + 5403 + 1957 | ▶ 19. 4267 - 2738 | |
|---------------------------------|-------------------|--|

19.

| 110 | Chapter 1 The Whole Numbers | | | | |
|-----|---|--|--|--|--|
| 20. | Solve. | | | | |
| 21. | ● 20. Subtract 15 from 107. ● 21. Find the sum of 15 and 107. | | | | |
| 22. | 22. Find the product of 15 and 107.23. Find the quotient of 107 and 15. | | | | |
| 23. | 24. Twenty-nine cans of Sherwin-Williams paint cost \$493. How much was each can? 25. Jo McElory is looking at two new refrigerators for her apartment. One costs \$599 and the other costs \$725. How much more expensive is the higher-priced one? | | | | |
| 24. | inglier priced oner | | | | |
| 25. | One tablespoon of white granulated sugar contains 45 calories. How many calories are in 8 tablespoons of white 27. A small business owner recently ordered 16 digital cameras that cost \$430 each and 5 printers that cost \$205 each | | | | |
| 26. | granulated sugar? (Source: Home
and Garden Bulletin No. 72, U.S.Find the total cost for these items.Department of Agriculture)Find the total cost for these items. | | | | |
| 27. | Find the perimeter and the area of each figure. | | | | |
| 28. | \circ 28. \circ 29. 20 yards \bigtriangleup \bigtriangleup \bigtriangleup | | | | |
| 29. | Rectangle 10 yards | | | | |

Multiplying and Dividing Fractions





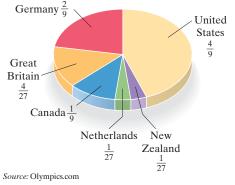
What Sport Uses the Terms Bow Pair, Stroke Pair, Stern, Bow, and Coxswain—Just to Name a Few?

his sport is rowing, and it is becoming more and more popular – from weekend athletes enjoying a team sport on the water to serious athletes competing in the Summer Olympics.

In the Summer Olympics, there are many categories of rowing, with both men and women, but one of the most watched categories is the "eight men with coxswain" division. Interestingly enough, in the entire history of the modern Olympic Games, only six nations have won the gold medal in this division.

In Section 2.3, Exercise 58, we will explore fractions relating to the gold medal– winning countries in this "eight men with coxswain" rowing division.





2

Fractions are numbers, and like whole numbers, they can be added, subtracted, multiplied, and divided. Fractions are very useful and appear frequently in everyday language, in common phrases like "half an hour," "quarter of a pound," and "third of a cup." This chapter introduces the concept of fractions, presents some basic vocabulary, and demonstrates how to multiply and divide fractions.

Sections

- 2.1 Introduction to Fractions and Mixed Numbers
- 2.2 Factors and Prime Factorization
- 2.3 Simplest Form of a Fraction

Integrated Review— Summary on Fractions, Mixed Numbers, and Factors

- 2.4 Multiplying Fractions and Mixed Numbers
- 2.5 Dividing Fractions and Mixed Numbers

Check Your Progress

Vocabulary Check Chapter Highlights Chapter Review Getting Ready for the Test Chapter Test Cumulative Review

2.1 Introduction to Fractions and Mixed Numbers 🕥

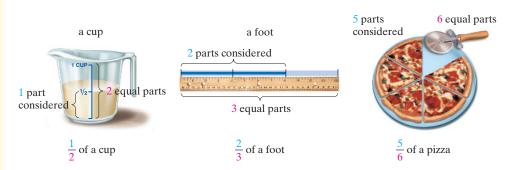
Objectives

A Identify the Numerator and the Denominator of a Fraction and Review Division Properties of 0 and 1.

- B Write a Fraction to Represent Parts of Figures or Real-Life Data.
- C Identify Proper Fractions, Improper Fractions, and Mixed Numbers.
- D Write Mixed Numbers as Improper Fractions.
- E Write Improper Fractions as Mixed Numbers or Whole Numbers.

Objective A Identifying Numerators and Denominators and Reviewing Division Properties of 0 and 1

Whole numbers are used to count whole things or units, such as cars, horses, dollars, and people. To refer to a part of a whole, fractions can be used. Here are some examples of **fractions.** Study these examples for a moment.



In a fraction, the top number is called the **numerator** and the bottom number is called the **denominator**. The bar between the numbers is called the **fraction bar**.

| Names | Fraction | Meaning |
|-------------------------------|----------|---|
| numerator \longrightarrow | 5 | ← number of parts being considered |
| denominator \longrightarrow | 6 | \leftarrow number of equal parts in the whole |



Identify the numerator and the denominator of each fraction.



Before we continue further, don't forget from Section 1.7 that the fraction bar indicates division. Let's review some division properties of 1 and 0.

| $\frac{9}{9} = 1$ because $1 \cdot 9 = 9$ | $\frac{11}{1} = 11$ because $11 \cdot 1 = 11$ |
|--|--|
| $\frac{0}{6} = 0 \text{ because } 0 \cdot 6 = 0$ | $\frac{6}{0}$ is undefined because there is no number that when multiplied by 0 gives 6. |

In general, we can say the following.

Let *n* be any whole number except 0.

| $\frac{n}{n} = 1$ | $\frac{0}{n} = 0$ |
|-------------------|-----------------------------|
| $\frac{n}{1} = n$ | $\frac{n}{0}$ is undefined. |

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Practice 1–2

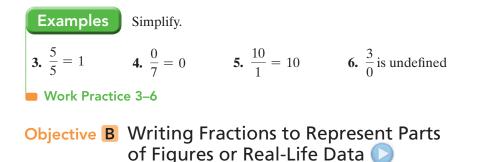
Identify the numerator and the denominator of each fraction.

1.
$$\frac{9}{2}$$
 2. $\frac{10}{17}$

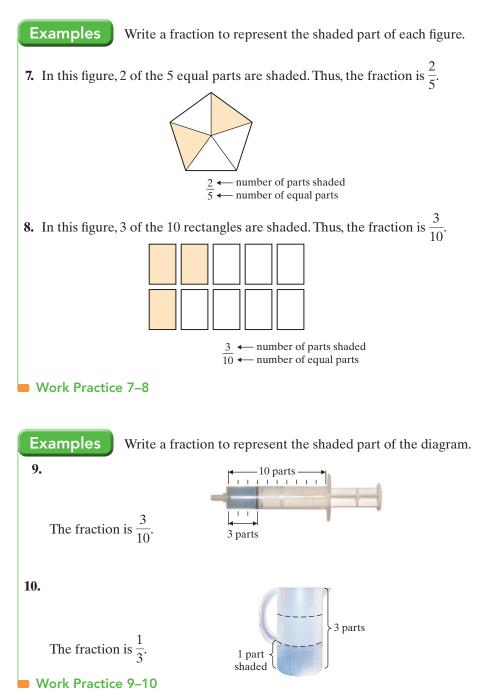
Answers

1. numerator = 9, denominator = 2

2. numerator = 10, denominator = 17



One way to become familiar with the concept of fractions is to visualize fractions with shaded figures. We can then write a fraction to represent the shaded area of the figure.

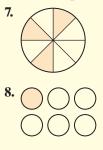


Practice 3–6 Simplify.



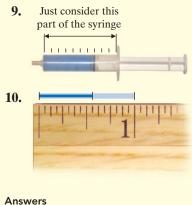
Practice 7–8

Write a fraction to represent the shaded part of each figure.



Practice 9–10

Write a fraction to represent the part of the whole shown.



| wers | | |
|------|---------------|--|
| 4. | 1 | 5. undefined 6. 20 |
| 8. | $\frac{1}{6}$ | 9. $\frac{7}{10}$ 10. $\frac{9}{16}$ |

3. 0

7. $\frac{3}{8}$

Practice 11–12

Draw and shade a part of a figure to represent each fraction.

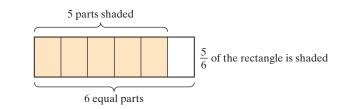
11.
$$\frac{2}{3}$$
 of a figure
12. $\frac{7}{11}$ of a figure

Examples

Draw a figure and then shade a part of it to represent each fraction.

11. $\frac{5}{6}$ of a figure

We will use a geometric figure such as a rectangle. Since the denominator is 6, we divide it into 6 equal parts. Then we shade 5 of the equal parts.

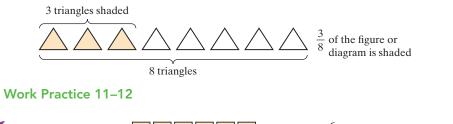


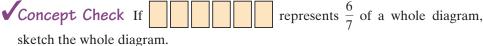
12. $\frac{3}{8}$ of a figure

Example 13

Sun than Mars?

If you'd like, our figure can consist of 8 triangles of the same size. We will shade 3 of the triangles.





Writing Fractions from Real-Life Data

Of the eight planets in our solar system (Pluto is now a dwarf planet), three

are closer to the Sun than Mars. What fraction of the planets are closer to the

Practice 13

Answers

13. $\frac{5}{8}$

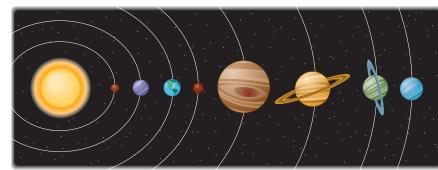
Of the eight planets in our solar system, five are farther from the Sun than Earth is. What fraction of the planets are farther from the Sun than Earth is?

11. answers may vary; for example,

12. answers may vary; for example,

()()

Concept Check Answer



Solution: The fraction of planets closer to the Sun than Mars is:

- $3 \leftarrow$ number of planets closer
- $\overline{8} \leftarrow$ number of planets in our solar system

Thus, $\frac{3}{8}$ of the planets in our solar system are closer to the Sun than Mars.

Work Practice 13

Objective C Identifying Proper Fractions, Improper Fractions, and Mixed Numbers ()

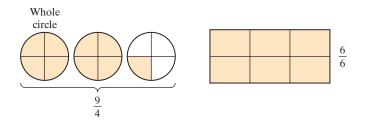
A **proper fraction** is a fraction whose numerator is less than its denominator. Proper fractions are less than 1. For example, the shad-

ed portion of the triangle's area is represented by $\frac{2}{3}$.

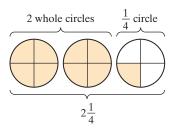
 $\frac{2}{3}$

An **improper fraction** is a fraction whose numerator is greater than or equal to its denominator. Improper fractions are greater than or equal to 1. The shaded part of the group of circles' area below

is $\frac{9}{4}$. The shaded part of the rectangle's area is $\frac{6}{6}$. (Recall from earlier that $\frac{6}{6}$ simplifies to 1 and notice that 1 whole figure or rectangle is shaded below.)



A **mixed number** contains a whole number and a fraction. Mixed numbers are greater than 1. Above, we wrote the shaded part of the group of circles as the improper fraction $\frac{9}{4}$. Now let's write the shaded part as a mixed number. The shaded part of the group of circles' area is $2\frac{1}{4}$. (Read "two and one-fourth.")



Helpful Hint

The mixed number $2\frac{1}{4}$ represents $2 + \frac{1}{4}$.

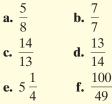


Identify each number as a proper fraction, improper fraction, or mixed number.

a. $\frac{6}{7}$ is a proper fraction**b.** $\frac{13}{12}$ is an improper fraction**c.** $\frac{2}{2}$ is an improper fraction**d.** $\frac{99}{101}$ is a proper fraction**e.** $1\frac{7}{8}$ is a mixed number**f.** $\frac{93}{74}$ is an improper fraction**Work Practice 14**

Practice 14

Identify each number as a proper fraction, improper fraction, or mixed number.



Answers

14. a. proper fraction b. improper fraction c. improper fractiond. proper fraction e. mixed number f. improper fraction

Chapter 2 | Multiplying and Dividing Fractions

Practice 15–16

Practice 17

fraction.

c. $9\frac{3}{10}$

Answers

Write each as an improper

d. $1\frac{1}{5}$

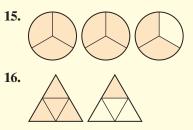
a. $2\frac{5}{7}$ **b.** $5\frac{1}{3}$

15. $\frac{8}{3}, 2\frac{2}{3}$ **16.** $\frac{5}{4}, 1\frac{1}{4}$

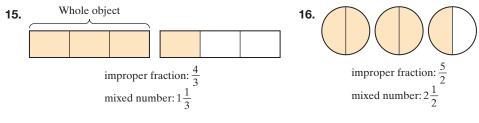
17. a. $\frac{19}{7}$ b. $\frac{16}{3}$ c. $\frac{93}{10}$ d. $\frac{6}{5}$

Concept Check Answer 2; answers may vary

Represent the shaded part of each figure group as both an improper fraction and a mixed number.



Represent the shaded part of each figure group's area as both an improper fraction and a mixed number.



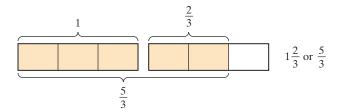
Work Practice 15–16

Examples

Concept Check If you were to estimate $2\frac{1}{8}$ by a whole number, would you choose 2 or 3? Why?

Objective D Writing Mixed Numbers as Improper Fractions

Notice from Examples 15 and 16 that mixed numbers and improper fractions were both used to represent the shaded area of the figure groups. For example,



The following steps may be used to write a mixed number as an improper fraction:

Writing a Mixed Number as an Improper Fraction

To write a mixed number as an improper fraction:

- Step 1: Multiply the denominator of the fraction by the whole number.
- **Step 2:** Add the numerator of the fraction to the product from Step 1.
- **Step 3:** Write the sum from Step 2 as the numerator of the improper fraction over the original denominator.

For ex

$$1\frac{2}{3} = \frac{3 \cdot 1 + 2}{3} = \frac{3 + 2}{3} = \frac{5}{3}$$

Step 3

Example 17

a.
$$4\frac{2}{9} = \frac{9 \cdot 4 + 2}{9} = \frac{36 + 2}{9} = \frac{38}{9}$$

b. $1\frac{8}{11} = \frac{11 \cdot 1 + 8}{11} = \frac{11 + 8}{11} = \frac{19}{11}$

Work Practice 17

7 Write each as an improper fraction.

```
roper fraction.
```

Objective E Writing Improper Fractions as Mixed Numbers or Whole Numbers

Just as there are times when an improper fraction is preferred, sometimes a mixed or a whole number better suits a situation. To write improper fractions as mixed or whole numbers, we use division. Recall once again from Section 1.7 that the fraction bar means division. This means that the fraction

- 5 numerator means $3\overline{)}$
- $\overline{3}$ denominator
- *5)5* ↑ ↑ denominator

Writing an Improper Fraction as a Mixed Number or a Whole Number

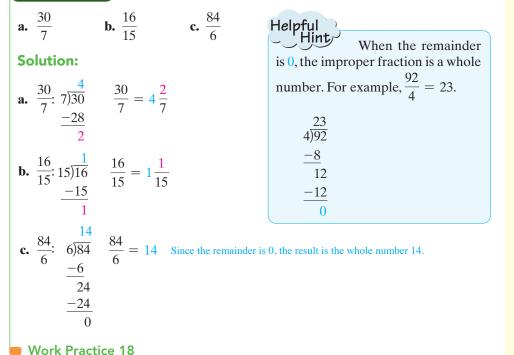
To write an improper fraction as a mixed number or a whole number:

- **Step 1:** Divide the denominator into the numerator.
- **Step 2:** The whole number part of the mixed number is the quotient. The fraction part of the mixed number is the remainder over the original denominator.

quotient remainder original denominator

For example,

Write each as a mixed number or a whole number.



Practice 18

Write each as a mixed number or a whole number.

| • | 9 | b. $\frac{23}{2}$ | | 48 |
|----|----|--------------------------|-----------|----|
| a. | 5 | b. <u>9</u> | c. | 4 |
| J | 62 | 51 | ſ | 21 |
| d. | 13 | e. <u>7</u> | f. | 20 |

Answers **18.** a. $1\frac{4}{5}$ b. $2\frac{5}{9}$ c. 12 d. $4\frac{10}{13}$ e. $7\frac{2}{7}$ f. $1\frac{1}{20}$

Vocabulary, Readiness & Video Check

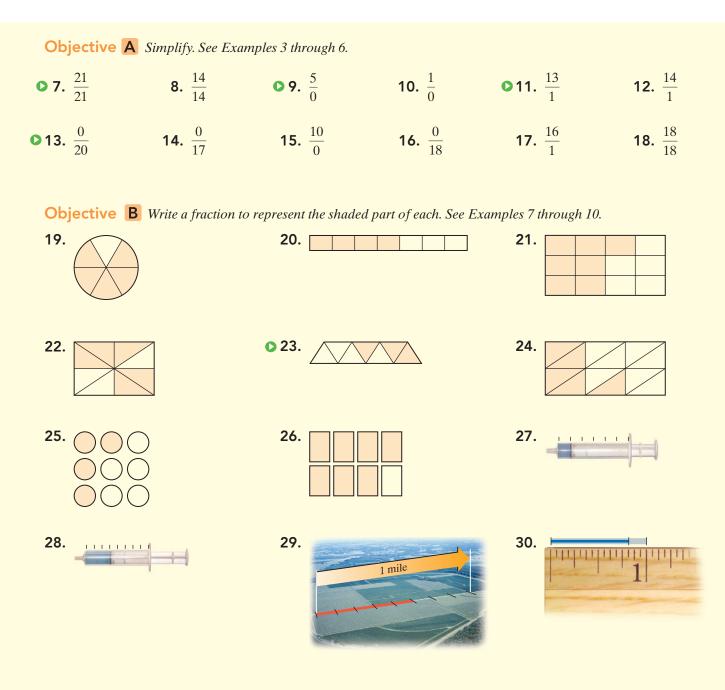
Use the choices below to fill in each blank.

| | improper
greater than or equal to 1 | fraction
denominator | proper
= 1 | is undefined
less than 1 | mixed number
numerator | = 0 |
|---|---|-------------------------|--------------------|----------------------------------|--|-----------|
| 1 | • The number $\frac{17}{31}$ is called $a(n)$ called its | | The numbe | r 31 is called its | | and 17 is |
| 2 | If we simplify each fraction, $\frac{9}{9}$ | | , <u>0</u> | , ar | nd we say | |
| 3 | The fraction $\frac{8}{3}$ is called $a(n)$ | | | fraction $\frac{3}{8}$ is called | a(n) | |
| 4 | fraction, and $10\frac{5}{8}$ is called $a(n)$
The value of an improper fractionalways | | | _, and the value of | f a proper fraction is | |
| | Martin-Gay Interactive Videos | Watch the section lectu | ure video and ans | wer the following que | stions. | |
| | | Objective A 5. | | | ou conclude about an minator are the same | - |
| | | - | In 🖪 Exampl | e 11, there are two | denominator 50 repro-
shapes in the diagram
have a denominator 3 | n, so why |
| | see Video 2.1 | Objective D 8. | Complete thi | s statement based | on the lecture before
f is un | |
| | | | in a mixed nu
1 | 1 | example, $1\frac{1}{3}$ means | |
| | | Objective E 9. | From the lect | ure before 🗖 Exam | mple 15, what operati
a mixed number? 🥑 | |

2.1 Exercise Set MyLab Math 🕗

Objectives A C Mixed Practice *Identify the numerator and the denominator of each fraction and identify each fraction as proper or improper. See Examples 1, 2, and 14.*

| • 1. $\frac{1}{2}$ | 2. $\frac{1}{4}$ | 3. $\frac{10}{3}$ |
|---------------------------|---------------------------|---------------------------|
| 4. $\frac{53}{21}$ | 5. $\frac{15}{15}$ | 6. $\frac{26}{26}$ |



Draw and shade a part of a figure to represent each fraction. See Examples 11 and 12.

31.
$$\frac{1}{5}$$
 of a figure **32.** $\frac{1}{16}$ of a figure **33.** $\frac{7}{8}$ of a figure **34.** $\frac{3}{5}$ of a figure

35.
$$\frac{6}{7}$$
 of a figure **36.** $\frac{7}{9}$ of a figure **37.** $\frac{4}{4}$ of a figure **38.** $\frac{6}{6}$ of a figure

Write each fraction. See Example 13.

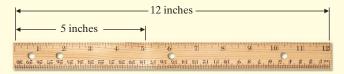
- **39.** Of the 131 students at a small private school, 42 are freshmen. What fraction of the students are freshmen?
- **41.** Use Exercise **39** to answer **a** and **b**.
 - a. How many students are *not* freshmen?
 - **b.** What fraction of the students are *not* freshmen?
- **43.** As of the beginning of 2017, the United States has had 45 different presidents. A total of seven U.S. presidents were born in the state of Ohio, second only to the state of Virginia in producing U.S. presidents. What fraction of U.S. presidents were born in Ohio? (*Source: World Almanac and Book of Facts*)
- **45.** Hurricane Sandy, which struck the East Coast in October 2012, is still the largest Atlantic hurricane ever documented. Sandy was one of 19 named tropical storms that formed during the 2012 Atlantic hurricane season. A total of 10 of these tropical storms turned into hurricanes. What fraction of the 2012 Atlantic tropical storms escalated into hurricanes? (*Source:* National Oceanic and Atmospheric Administration)



47. There are 31 days in the month of March. What fraction of the month does 11 days represent?

| Mon. | Tue. | Wed. | Thu. | Fri. | Sat. | Sun. |
|------|------|------|------|------|------|------|
| | | | | | 1 | 2 |
| 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| 17 | 18 | 19 | 20 | 21 | 22 | 23 |
| 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | | | | | | |

- **40.** Of the 63 employees at a new biomedical engineering firm, 22 are men. What fraction of the employees are men?
- **42.** Use Exercise 40 to answer a and b.
 - **a.** How many of the employees are women?
 - **b.** What fraction of the employees are women?
- **44.** Of the eight planets in our solar system, four have days that are longer than the 24-hour Earth day. What fraction of the planets have longer days than Earth has? (*Source:* National Space Science Data Center)
- **46.** There are 12 inches in a foot. What fractional part of a foot does 5 inches represent?



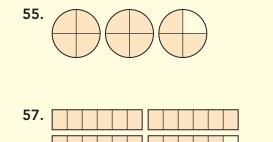
48. There are 60 minutes in an hour. What fraction of an hour does 37 minutes represent?



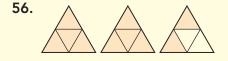
- **49.** In a basic college mathematics class containing 31 students, there are 18 freshmen, 10 sophomores, and 3 juniors. What fraction of the class is sophomores?
- **51.** Thirty-three out of the fifty total states in the United States contain federal Indian reservations.
 - **a.** What fraction of the states contain federal Indian reservations?
 - **b.** How many states do not contain federal Indian reservations?
 - **c.** What fraction of the states do not contain federal Indian reservations? (*Source:* Tiller Research, Inc., Albuquerque, NM)
- 53. A bag contains 50 red or blue marbles. If 21 marbles are blue,
 - **a.** What *fraction* of the marbles are blue?
 - **b.** How many marbles are red?
 - **c.** What *fraction* of the marbles are red?

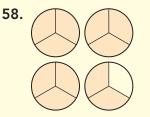
- **50.** In a sports team with 20 children, there are 9 boys and 11 girls. What fraction of the team is boys?
- **52.** Consumer fireworks are legal in 46 out of the 50 total states in the United States. (*Source:* USA.gov)
 - **a.** In what fraction of the states are consumer fire-works legal?
 - **b.** In how many states are consumer fireworks illegal?
 - **c.** In what fraction of the states are consumer fireworks illegal? (*Source:* United States Fireworks Safety Council)
- **54.** An art dealer is taking inventory. His shop contains a total of 37 pieces, which are all sculptures, watercolor paintings, or oil paintings. If there are 15 watercolor paintings and 17 oil paintings, answer each question.
 - **a.** What fraction of the inventory is watercolor paintings?
 - **b.** What fraction of the inventory is oil paintings?
 - **c.** How many sculptures are there?
 - **d.** What fraction of the inventory is sculptures?

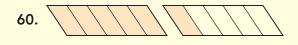
Objective C Write the shaded area in each figure group as **(a)** an improper fraction and **(b)** a mixed number. See *Examples 15 and 16.*

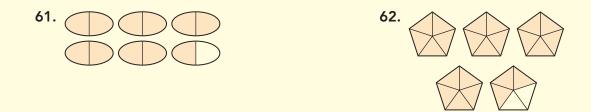


59.

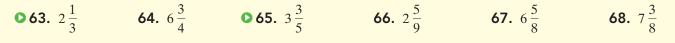








Objective D Write each mixed number as an improper fraction. See Example 17.



69.
$$2\frac{11}{15}$$
 70. $1\frac{13}{17}$ **71.** $11\frac{6}{7}$ **72.** $12\frac{2}{5}$ **73.** $6\frac{6}{13}$ **74.** $8\frac{9}{10}$

75. $4\frac{13}{24}$ **76.** $5\frac{17}{25}$ **77.** $17\frac{7}{12}$ **78.** $12\frac{7}{15}$ **79.** $9\frac{7}{20}$ **80.** $10\frac{14}{27}$
81. $2\frac{51}{107}$ **82.** $3\frac{27}{125}$ **83.** $166\frac{2}{3}$ **84.** $114\frac{2}{7}$

Objective E Write each improper fraction as a mixed number or a whole number. See Example 18.

| 85. $\frac{17}{5}$ | 86. $\frac{13}{7}$ | • 87. $\frac{37}{8}$ | 88. $\frac{64}{9}$ | 89. $\frac{47}{15}$ | 90. $\frac{65}{12}$ |
|-------------------------------|-------------------------------|-------------------------------|-------------------------------|------------------------------|------------------------------|
| 91. $\frac{46}{21}$ | 92. $\frac{67}{17}$ | 93. $\frac{198}{6}$ | 94. $\frac{112}{7}$ | 95. $\frac{225}{15}$ | 96. $\frac{196}{14}$ |
| 97. $\frac{200}{3}$ | 98. $\frac{300}{7}$ | 99. $\frac{247}{23}$ | 100. $\frac{437}{53}$ | 101. $\frac{319}{18}$ | 102. $\frac{404}{21}$ |
| 103. $\frac{182}{175}$ | 104. $\frac{149}{143}$ | 105. $\frac{737}{112}$ | 106. $\frac{901}{123}$ | | |

Review

| Simplify. See Section 1.9. | | | | | | | |
|----------------------------|----------------------------|----------------------------|----------------------------------|--|--|--|--|
| 107. 3 ² | 108. 4 ³ | 109. 5 ³ | 110. 3 ⁴ | | | | |
| Write each using exponents | | | | | | | |
| 111. 7·7·7·7·7 | 112. 5 • 5 • 5 • 5 | 113. 2·2·2·3 | 114. 4 • 4 • 10 • 10 • 10 | | | | |

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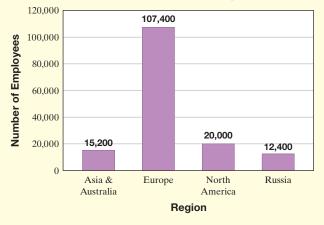
Concept Extensions

Write each fraction.

115. In your own words, explain how to write an improper 116. In your own words, explain how to write a mixed fraction as a mixed number.

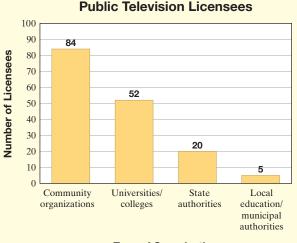
Identify the larger fraction for each pair.

- **117.** $\frac{1}{2}$ or $\frac{2}{3}$ (*Hint:* Represent each fraction by the shaded part of equivalent figures. Then compare the shaded areas.)
- Solve. See the first Concept Check in this section.
- **119.** If $\bigcirc \bigcirc \bigcirc \bigcirc$ represents $\frac{4}{9}$ of a whole diagram, sketch the whole diagram.
- **121.** IKEA Group employs workers in four different regions worldwide, as shown on the bar graph. What fraction of IKEA employees work in the North American region? (Source: IKEA Group)



IKEA Employees by Region, 2015

- number as an improper fraction.
- **118.** $\frac{7}{4}$ or $\frac{3}{5}$ (*Hint:* Identify each as a proper fraction or an improper fraction.)
- **120.** If \triangle represents $\frac{1}{3}$ of a whole diagram, sketch the whole diagram.
- **122.** The Public Broadcasting Service (PBS) provides programming to the noncommercial public TV stations of the United States. The bar graph shows a breakdown of the public television licensees by type. Each licensee operates one or more PBS member TV stations. What fraction of the public television licensees are universities or colleges? (*Source:* The Public Broadcasting Service)



- Type of Organization
- **124.** The United States Mint operates six facilities. One facility is headquarters, one facility is a depository, and four facilities mint coins. What fraction of the United States Mint facilities produces coins? (Source: United States Mint)
- **123.** Heifer International is a nonprofit world hunger relief organization that focuses on sustainable agriculture programs. Currently Heifer International is working in 6 North American countries, 5 South American countries, 4 Central/Eastern European countries, 14 African countries, and 7 Asian/South Pacific countries. What fraction of the total countries in which Heifer International works is located in North America? (Hint: First find the total number of countries) (Source: Heifer International)

2.2 Factors and Prime Factorization

Objectives

A Find the Factors of a Number.

B Identify Prime and Composite Numbers. (>

C Find the Prime Factorization of a Number.

Practice 1

Find all the factors of each number. **a.** 15 **b.** 7 **c.** 24

Answers

1. a. 1, 3, 5, 15 **b.** 1, 7 **c.** 1, 2, 3, 4, 6, 8, 12, 24

Concept Check Answer answers may vary

To perform many operations with fractions, it is necessary to be able to factor a number. In this section, only the **natural numbers**-1, 2, 3, 4, 5, and so on—will be considered.

Concept Check How are the natural numbers and the whole numbers alike? How are they different?

Objective 🗛 Finding Factors of Numbers 🕗

Recall that when numbers are multiplied to form a product, each number is called a factor. Since $5 \cdot 9 = 45$, both 5 and 9 are **factors** of 45, and $5 \cdot 9$ is called a **factorization** of 45.

The two-number factorizations of 45 are

1.45 3.15 5.9

Thus, we say that the factors of 45 are 1, 3, 5, 9, 15, and 45.

Helpful Hint

From our definition of factor above, notice that a **factor** of a number divides the number evenly (with a remainder of 0). For example,

| 45 | 15 | 9 | 5 | 3 | 1 |
|------|--------------|-------------|--------------|-------|--------------|
| 1)45 | <u>3)</u> 45 | <u>5)45</u> | <u>9)</u> 45 | 15)45 | <u>45)45</u> |

Example 1

Find all the factors of 20.

Solution: First we write all the two-number factorizations of 20.

 $1 \cdot 20 = 20$ $2 \cdot 10 = 20$ $4 \cdot 5 = 20$

The factors of 20 are 1, 2, 4, 5, 10, and 20.

Work Practice 1

Objective **B** Identifying Prime and Composite Numbers

Of all the ways to factor a number, one special way is called the **prime factorization.** To help us write prime factorizations, we first review prime and composite numbers.

Prime Numbers

A **prime number** is a natural number that has exactly two different factors, 1 and itself.

The first several prime numbers are

2, 3, 5, 7, 11, 13, 17

It would be helpful to memorize these.

If a natural number other than 1 is not a prime number, it is called a **composite number**.

Composite Numbers

A composite number is any natural number, other than 1, that is not prime.

Helpful Hint

The natural number 1 is neither prime nor composite.

Example 2

Determine whether each number is prime or composite. Explain your answers.

3, 9, 11, 17, 26

Solution: The number 3 is prime. Its only factors are 1 and 3 (itself). The number 9 is composite. It has more than two factors: 1, 3, and 9. The number 11 is prime. Its only factors are 1 and 11. The number 17 is prime. Its only factors are 1 and 17. The number 26 is composite. Its factors are 1, 2, 13, and 26.

Work Practice 2

Objective C Finding Prime Factorizations

Now we are ready to find prime factorizations of numbers.

Prime Factorization

The **prime factorization** of a number is the factorization in which all the factors are prime numbers.

For example, the prime factorization of 12 is $2 \cdot 2 \cdot 3$ because

 $12 = \underbrace{2 \cdot 2 \cdot 3}_{}$

This product is 12 and each number is a prime number.

Every whole number greater than 1 has exactly one prime factorization.

Helpful Hint

Don't forget that multiplication is commutative, so $2 \cdot 2 \cdot 3$ can also be written as $2 \cdot 3 \cdot 2$ or $3 \cdot 2 \cdot 2$ or $2^2 \cdot 3$. Any one of these can be called *the prime factorization of* 12.

Example 3

Find the prime factorization of 45.

Solution: The first prime number, 2, does not divide 45 evenly (with a remainder of 0). The second prime number, 3, does, so we divide 45 by 3.

15 3)45

Because 15 is not prime and 3 also divides 15 evenly, we divide by 3 again.

5 3)<u>15</u> 3)<u>45</u>

Practice 2

Determine whether each number is prime or composite. Explain your answers.

21, 13, 18, 29, 39

Practice 3 Find the prime factorization

Answers

(Continued on next page)

of 28.

2. 13 and 29 are prime. 21, 18, and 39 are composite. **3.** $2 \cdot 2 \cdot 7$ or $2^2 \cdot 7$

The quotient, 5, is a prime number, so we are finished. The prime factorization of 45 is

 $45 = 3 \cdot 3 \cdot 5$ or $45 = 3^2 \cdot 5$,

using exponents.

```
Work Practice 3
```

There are a few quick **divisibility tests** to determine whether a number is divisible by the primes 2, 3, or 5. (A number is divisible by 2, for example, if 2 divides it evenly.)

Divisibility Tests

Ţ

A whole number is divisible by:

- 2 if the last digit is 0, 2, 4, 6, or 8.
 - - 132 is divisible by 2 since the last digit is a 2.
- 3 if the sum of the digits is divisible by 3.

144 is divisible by 3 since 1 + 4 + 4 = 9 is divisible by 3.

• 5 if the last digit is 0 or 5.

↓

1115 is divisible by 5 since the last digit is a 5.

Helpful Hint

Here are a few other divisibility tests you may find interesting. A whole number is divisible by:

• 4 if its last two digits are divisible by 4.

1712 is divisible by 4.

• 6 if it's divisible by 2 and 3.

9858 is divisible by 6.

• 9 if the sum of its digits is divisible by 9.

5238 is divisible by 9 since 5 + 2 + 3 + 8 = 18 is divisible by 9.

We will usually begin the division process with the smallest prime number factor of the given number. Since multiplication is commutative, this is not necessary. As long as the divisor is any prime number factor, this process works.

Example 4

Find the prime factorization of 180.

Solution: We divide 180 by 2 and continue dividing until the quotient is no longer divisible by 2. We then divide by the next largest prime number, 3, until the quotient is no longer divisible by 3. We continue this process until the quotient is a prime number.

| | 5 |
|------------------|-----|
| 3) | 15 |
| 3) | 45 |
| 2) | 90 |
| $2\overline{)1}$ | .80 |

Practice 4

Find the prime factorization of 120.

Thus, the prime factorization of 180 is

 $180 = 2 \cdot 2 \cdot 3 \cdot 3 \cdot 5$ or $180 = 2^2 \cdot 3^2 \cdot 5$,

using exponents.

Work Practice 4

Example 5 Find the prime factorization of 945.

Solution: This number is not divisible by 2 but is divisible by 3. We will begin by dividing 945 by 3.

7 5) 35 3)105 3)315 3)945

Thus, the prime factorization of 945 is

 $945 = 3 \cdot 3 \cdot 3 \cdot 5 \cdot 7$ or $945 = 3^3 \cdot 5 \cdot 7$

```
Work Practice 5
```

Another way to find the prime factorization is to use a factor tree, as shown in the next example.

Example 6 Use a factor tree to find the prime factorization of 18.

Solution: We begin by writing 18 as a product of two natural numbers greater than 1, say $2 \cdot 9$.

 $\begin{array}{c}
18 \\
\checkmark \\
2 \cdot 9.
\end{array}$

The number 2 is prime, but 9 is not. So we write 9 as $3 \cdot 3$.

 $\begin{array}{c}
18 \\
2 \cdot 9 \\
\downarrow \downarrow \searrow \\
2 \cdot 3 \cdot 3
\end{array}$

Each factor is now prime, so the prime factorization is

 $18 = 2 \cdot 3 \cdot 3$ or $18 = 2 \cdot 3^2$,

using exponents.

Work Practice 6

In this text, we will write the factorization of a number from the smallest factor to the largest factor.

Practice 5

Find the prime factorization of 756.

Practice 6

Use a factor tree to find the prime factorization of 45.

Answers 5. $2 \cdot 2 \cdot 3 \cdot 3 \cdot 3 \cdot 7$ or $2^2 \cdot 3^3 \cdot 7$ 6. $3 \cdot 3 \cdot 5$ or $3^2 \cdot 5$

Practice 7

Use a factor tree to find the prime factorization of each number.

a. 30 **b.** 56 **c.** 72

Example 7

• 7 Use a factor tree to find the prime factorization of 80.

Solution: Write 80 as a product of two numbers. Continue this process until all factors are prime.

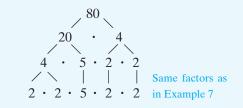
All factors are now prime, so the prime factorization of 80 is

 $2 \cdot 2 \cdot 2 \cdot 2 \cdot 5 \quad \text{or} \quad 2^4 \cdot 5.$

Work Practice 7

Helpful Hint

It makes no difference which factors you start with. The prime factorization of a number will be the same.



Concept Check True or false? Two different numbers can have exactly the same prime factorization. Explain your answer.

Example 8 Use a factor tree to find the prime factorization of 175.

Solution: We begin by writing 175 as a product of two numbers greater than 1, say $7 \cdot 25$.

$$\begin{array}{c}
175 \\
\checkmark \\
7 \cdot 25 \\
\downarrow \\
7 \cdot 5 \cdot 5
\end{array}$$

The prime factorization of 175 is

 $175 = 5 \cdot 5 \cdot 7$ or $175 = 5^2 \cdot 7$

Work Practice 8

Answers 7. a. $2 \cdot 3 \cdot 5$ b. $2 \cdot 2 \cdot 2 \cdot 7$ or $2^3 \cdot 7$ c. $2 \cdot 2 \cdot 2 \cdot 3 \cdot 3$ or $2^3 \cdot 3^2$ 8. $3 \cdot 3 \cdot 13$ or $3^2 \cdot 13$

Concept Check Answer false; answers may vary

Practice 8

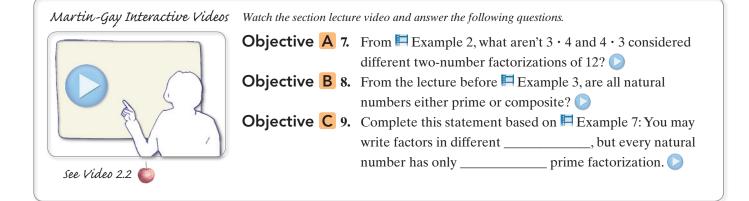
Use a factor tree to find the prime factorization of 117.

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank.

| factor(s) | prime factorization | prime |
|-----------|---------------------|-------|
| natural | composite | |

- **1.** The number 40 equals $2 \cdot 2 \cdot 2 \cdot 5$. Since each factor is prime, we call $2 \cdot 2 \cdot 2 \cdot 5$ the ______ of 40.
- 2. A natural number, other than 1, that is not prime is called a(n) ______ number.
- 3. A natural number that has exactly two different factors, 1 and itself, is called a(n) _____ number.
- **4.** The numbers 1, 2, 3, 4, 5,... are called the _____ numbers.
- 5. Since $30 = 5 \cdot 6$, the numbers 5 and 6 are _____ of 30.
- 6. Answer true or false: 5 · 6 is the prime factorization of 30.



| 2.2 Ex | ercise Set N | 1yLab Math 🜔 | | | | |
|---------------|---------------------|-----------------------|---------------|---------------|----------------|--|
| Objective | List all the factor | s of each number. See | Example 1. | | | |
| 1. 8 | 2. 6 | 3. 25 | 4. 30 | 5. 4 | 6. 9 | |
| | | | | | | |
| 7. 18 | 8. 48 | 9. 29 | 10. 37 | 11. 80 | 12. 100 | |
| | | | | | | |
| 13. 12 | 14. 28 | 15. 34 | 16. 26 | | | |

Objective B *Identify each number as prime or composite. See Example 2.*

| 17. 7 | 18. 5 | 019. 4 | 20. 10 | 21. 23 | 22. 13 |
|---------------|---------------|---------------|---------------|----------------|----------------|
| 23. 49 | 24. 45 | 25. 67 | 26. 89 | 27. 39 | 28. 21 |
| 29. 31 | 30. 27 | 31. 63 | 32. 51 | 33. 119 | 34. 147 |

Objective C *Find the prime factorization of each number. Write any repeated factors using exponents. See Examples 3 through 8.*

| 35. 32 | 36. 64 | 37. 15 | 38. 21 | 39. 40 | 40. 63 |
|-----------------|----------------|----------------|----------------|----------------|----------------|
| 0 41. 36 | 42. 80 | 43. 39 | 44. 56 | 45. 60 | 46. 84 |
| 47. 110 | 48. 130 | 49. 85 | 50. 93 | 51. 128 | 52. 81 |
| 53. 154 | 54. 198 | 55. 300 | 56. 360 | 57. 240 | 58. 836 |
| 59. 828 | 60. 504 | 61. 882 | 62. 405 | 63. 637 | 64. 539 |

Objectives **B C Mixed Practice** *Find the prime factorization of each composite number. Write any repeated factors using exponents. Write "prime" if the number is prime.*

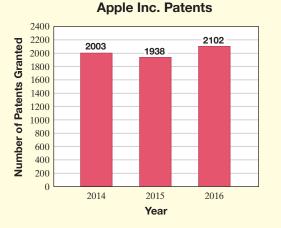
| 65. 33 | 66. 48 | 67. 98 | 68. 54 | 69. 67 | 70. 59 |
|----------------|----------------|---------------|----------------|----------------|-----------------|
| 71. 459 | 72. 208 | 73. 97 | 74. 103 | 75. 700 | 76. 1000 |

Review

Round each whole number to the indicated place value. See Section 1.5.

| 77. 4267 hundreds | 78. 32,465 thousands | 79. 7,658,240 ten-thousands |
|---------------------------|-----------------------------|------------------------------------|
| 80. 4,286,340 tens | 81. 19,764 thousands | 82. 10,292,876 millions |

The bar graph below shows the number of patents that Apple Inc. has been granted over a three-year period. Use this bar graph to answer the questions below. See Section 2.1. (Source: IFI CLAIMS Patent Services)





- **83.** Find the total number of patents received by Apple for the years shown.
- **84.** How many fewer patents were granted in 2015 than in 2014?
- **85.** What fraction of the patents were granted in 2014?
- **86.** What fraction of the patents were granted in 2016?

Concept Extensions

Find the prime factorization of each number.

87. 34,020

89. In your own words, define a prime number.

nonzero whole numbers only?

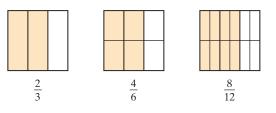
88. 131,625

- **90.** The number 2 is a prime number. All other even natural numbers are composite numbers. Explain why.
- **91.** Why are we interested in the prime factorizations of **92.** Two students have different prime factorizations for the same number. Is this possible? Explain.

Simplest Form of a Fraction

Objective A Writing Fractions in Simplest Form

Fractions that represent the same portion of a whole are called equivalent fractions.



For example, $\frac{2}{3}, \frac{4}{6}$, and $\frac{8}{12}$ all represent the same shaded portion of the rectangle's area, so they are equivalent fractions.

 $\frac{2}{3} = \frac{4}{6} = \frac{8}{12}$

There are many equivalent forms of a fraction. A special form of a fraction is called simplest form.

Simplest Form of a Fraction

A fraction is written in simplest form or lowest terms when the numerator and the denominator have no common factors other than 1.

For example, the fraction $\frac{2}{3}$ is in simplest form because 2 and 3 have no common factor other than 1. The fraction $\frac{4}{6}$ is not in simplest form because 4 and 6 both have a factor of 2. That is, 2 is a common factor of 4 and 6. The process of writing a fraction in simplest form is called **simplifying** the fraction.

To simplify $\frac{4}{6}$ and write it as $\frac{2}{3}$, let's first study a few properties. Recall from Section 2.1 that any nonzero whole number *n* divided by itself is 1.

Objectives

- A Write a Fraction in Simplest Form or Lowest Terms. 🕞
- **B** Determine Whether Two Fractions Are Equivalent.
- **C** Solve Problems by Writing Fractions in Simplest Form. 🜔

Any nonzero number *n* divided by itself is 1.

$$\frac{5}{5} = 1, \frac{17}{17} = 1, \frac{24}{24} = 1$$
, or, in general, $\frac{n}{n} = 1$

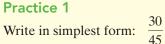
Also, in general, if $\frac{a}{b}$ and $\frac{c}{d}$ are fractions (with b and d not 0), the following is true.

 $\frac{a \cdot c}{b \cdot d} = \frac{a}{b} \cdot \frac{c}{d}^*$

**Note:* We will study this concept further in the next section.

These properties allow us to do the following:

 $\frac{4}{6} = \frac{2 \cdot 2}{2 \cdot 3} = \frac{2}{2} \cdot \frac{2}{3} = \frac{1}{2} \cdot \frac{2}{3} = \frac{2}{3}$ When 1 is multiplied by a number, the result is the same number.



Practice 2 Write in simplest form: 51

Example 1 Write in simplest form: $\frac{12}{20}$ **Solution:** Notice that 12 and 20 have a common factor of 4. $\frac{12}{20} = \frac{4 \cdot 3}{4 \cdot 5} = \frac{4}{4} \cdot \frac{3}{5} = \frac{4}{1} \cdot \frac{3}{5} = \frac{3}{5}$ Since 3 and 5 have no common factors (other than 1), $\frac{3}{5}$ is in simplest form. Work Practice 1

If you have trouble finding common factors, write the prime factorizations of the numerator and the denominator.

Example 2 Write in simplest form: $\frac{42}{66}$

Solution: Let's write the prime factorizations of 42 and 66.

 $\frac{42}{66} = \frac{2 \cdot 3 \cdot 7}{2 \cdot 3 \cdot 11} = \frac{2}{2} \cdot \frac{3}{3} \cdot \frac{7}{11} = 1 \cdot 1 \cdot \frac{7}{11} = \frac{7}{11}$

Work Practice 2

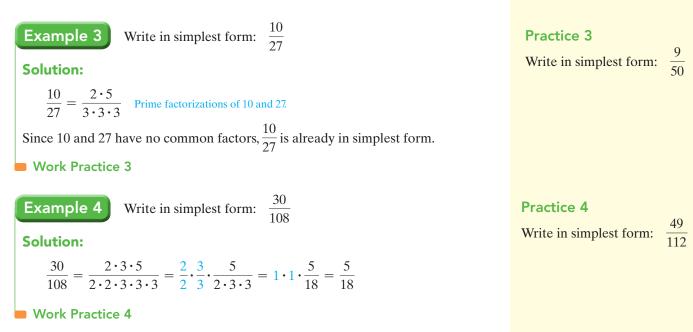
In the example above, you may have saved time by noticing that 42 and 66 have a common factor of 6.

$$\frac{42}{66} = \frac{6 \cdot 7}{6 \cdot 11} = \frac{6}{6} \cdot \frac{7}{11} = 1 \cdot \frac{7}{11} = \frac{7}{11}$$

Helpful Hint

Writing the prime factorizations of the numerator and the denominator is helpful in finding any common factors.

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We can use a shortcut procedure with common factors when simplifying.

 $\frac{4}{6} = \frac{2 \cdot 2}{2 \cdot 3} = \frac{1 \cdot 2}{1 \cdot 3} = \frac{2}{3}$ Divide out the common factor of 2 in the numerator and denominator.

This procedure is possible because dividing out a common factor in the numerator and denominator is the same as removing a factor of 1 in the product.

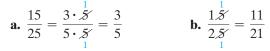
Writing a Fraction in Simplest Form

To write a fraction in simplest form, write the prime factorizations of the numerator and the denominator and then divide both by all common factors.

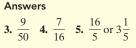
Example 5 Write in simplest form:
$$\frac{72}{26}$$

Solution:
 $\frac{72}{26} = \frac{\stackrel{1}{2} \cdot 2 \cdot 2 \cdot 3 \cdot 3}{\stackrel{2}{2} \cdot 13} = \frac{1 \cdot 2 \cdot 2 \cdot 3 \cdot 3}{1 \cdot 13} = \frac{36}{13}$
which can also be written as
 $2\frac{10}{13}$
Work Practice 5

Concept Check Which is the correct way to simplify the fraction $\frac{15}{25}$? Or are both correct? Explain.

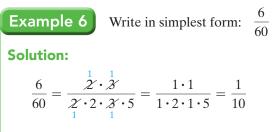


Practice 5 Write in simplest form: $\frac{64}{20}$



Concept Check Answers a. correct b. incorrect Practice 6

Write in simplest form:



Work Practice 6

Helpful Hint

Be careful when all factors of the numerator or denominator are divided out. In Example 6, the numerator was $1 \cdot 1 = 1$, so the final result was $\frac{1}{10}$

In the fraction of Example 6, $\frac{6}{60}$, you may have immediately noticed that the largest common factor of 6 and 60 is 6. If so, you may simply divide out that largest common factor.

$$\frac{6}{60} = \frac{\cancel{6}}{\cancel{6}} = \frac{1}{\cancel{1}} = \frac{1}{1 \cdot 10} = \frac{1}{10}$$
 Divide out the common factor of 6.

Notice that the result, $\frac{1}{10}$, is in simplest form. If it were not, we would repeat the same procedure until the result was in simplest form.

42 48

Write in simplest form: $\frac{45}{75}$ Example 7

Solution: You may write the prime factorizations of 45 and 75 or you may notice that these two numbers have a common factor of 15.

$$\frac{45}{75} = \frac{3 \cdot 15}{5 \cdot 15} = \frac{3 \cdot 1}{5 \cdot 1} = \frac{3}{5}$$

The numerator and denominator of $\frac{3}{5}$ have no common factors other than 1, so $\frac{3}{5}$ is in simplest form.

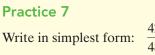
Work Practice 7

Objective B Determining Whether Two Fractions Are Equivalent 💟

Recall that two fractions are equivalent if they represent the same part of a whole. One way to determine whether two fractions are equivalent is to see whether they simplify to the same fraction.

Inc.

Answers 6. $\frac{1}{7}$ 7. $\frac{7}{8}$



Example 8 Determine whether
$$\frac{16}{40}$$
 and $\frac{10}{25}$ are equivalent.
Solution: Simplify each fraction.

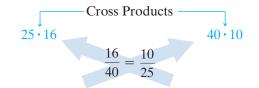
$$\frac{16}{40} = \frac{\cancel{8} \cdot 2}{\cancel{8} \cdot 5} = \frac{1 \cdot 2}{1 \cdot 5} = \frac{2}{5}$$
Since these fractions are the same, $\frac{16}{40} = \frac{10}{25}$.

$$\frac{10}{25} = \frac{2 \cdot \cancel{5}}{5 \cdot \cancel{5}} = \frac{2 \cdot 1}{5 \cdot 1} = \frac{2}{5}$$
Work Practice 8

There is a shortcut method you may use to check or test whether two fractions are equivalent. In the example above, we learned that the fractions are equivalent, or

 $\frac{16}{40} = \frac{10}{25}$

In the example above, we call $25 \cdot 16$ and $40 \cdot 10$ **cross products** because they are the products one obtains by multiplying across.



Notice that these cross products are equal

 $25 \cdot 16 = 400, \quad 40 \cdot 10 = 400$

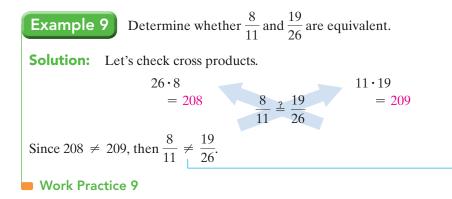
In general, this is true for equivalent fractions.

Equivalent Fractions

 $8 \cdot 6 \qquad 24 \cdot 2$ $\frac{6}{24} \stackrel{?}{=} \frac{2}{8}$

Since the cross products $(8 \cdot 6 = 48 \text{ and } 24 \cdot 2 = 48)$ are equal, the fractions are equivalent.

Note: If the cross products are not equal, the fractions are not equivalent.



Practice 9

Determine whether $\frac{4}{13}$ and $\frac{5}{18}$ are equivalent.



Answers8. equivalent9. not equivalent

Determine whether $\frac{7}{9}$ and $\frac{21}{27}$

Objective C Solving Problems by Writing Fractions in Simplest Form

Many real-life problems can be solved by writing fractions. To make the answers clearer, these fractions should be written in simplest form.

Example 10

Calculating Fraction of Parks in Pennsylvania

There are currently 46 national historical parks in the United States. Two of these historical parks are located in the state of Pennsylvania. What fraction of the United States' national historical parks can be found in Pennsylvania? Write the fraction in simplest form. (*Source:* National Park Service)



Solution: First we determine the fraction of parks found in Pennsylvania.

2← national historical parks in Pennsylvania46← total national historical parks

Next we simplify the fraction.

$$\frac{2}{46} = \frac{2}{2 \cdot 23} = \frac{1}{1 \cdot 23} = \frac{1}{23}$$

Thus, $\frac{1}{23}$ of the United States' national parks are in the state of Pennsylvania.

Work Practice 10

Calculator Explorations Simplifying Fractions

Scientific Calculator

Many calculators have a fraction key, such as $a_{b/c}$, that allows you to simplify a fraction on the calculator.

For example, to simplify $\frac{324}{612}$, enter

324*a*_{b/c}612=

The display will read

9 17

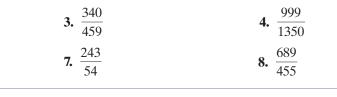
which represents $\frac{9}{17}$, the original fraction simplified.

Use your calculator to simplify each fraction.

| 1. $\frac{128}{224}$ | 2. $\frac{231}{396}$ |
|-----------------------------|-----------------------------|
| 5. $\frac{810}{432}$ | 6. $\frac{315}{225}$ |

Helpful

The Calculator Explorations boxes in this chapter provide only an introduction to fraction keys on calculators. Any time you use a calculator, there are both advantages and limitations to its use. Never rely solely on your calculator. It is very important that you understand how to perform all operations on fractions by hand in order to progress through later topics. For further information, talk to your instructor.



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Practice 10

There are four national historical parks in the state of Virginia. See Example 10 and determine what fraction of the United States' national historical parks can be found in Virginia. Write the fraction in simplest form.

Answer **10.** $\frac{2}{23}$

Vocabulary, Readiness & Video Check

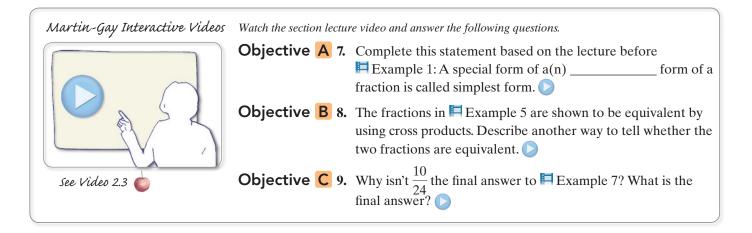
Use the choices below to fill in each blank.

1 simplest form n

1. In $\frac{11}{48}$, since 11 and 48 have no common factors other than 1, $\frac{11}{48}$ is in _____.

2. Fractions that represent the same portion of a whole are called ______ fractions.

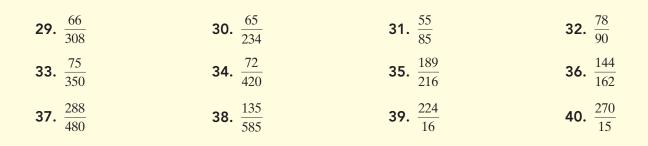
- 3. In the statement ⁵/₁₂ = ¹⁵/₃₆, 5 ⋅ 36 and 12 ⋅ 15 are called ______.
 4. The fraction ⁷/₇ simplifies to ______.
 5. The fraction ⁰/₇ simplifies to ______.
- 6. The fraction $\frac{n}{1}$ simplifies to _____



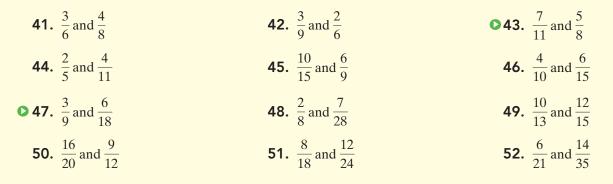
2.3 Exercise Set MyLab Math

Objective A Write each fraction in simplest form. See Examples 1 through 7.

| 1. $\frac{3}{12}$ | 2. $\frac{5}{30}$ | 3. $\frac{4}{42}$ | 4. $\frac{9}{48}$ |
|-----------------------------|-----------------------------|-----------------------------|-----------------------------|
| •5. $\frac{14}{16}$ | 6. $\frac{22}{34}$ | 7. $\frac{20}{30}$ | 8. $\frac{70}{80}$ |
| 9. $\frac{35}{50}$ | 10. $\frac{25}{55}$ | 11. $\frac{63}{81}$ | 12. $\frac{21}{49}$ |
| D13. $\frac{24}{40}$ | 14. $\frac{36}{54}$ | 15. $\frac{27}{64}$ | 16. $\frac{32}{63}$ |
| 17. $\frac{25}{40}$ | 18. $\frac{36}{42}$ | 19. $\frac{40}{64}$ | 20. $\frac{28}{60}$ |
| 21. $\frac{56}{68}$ | 22. $\frac{39}{42}$ | 23. $\frac{36}{24}$ | 24. $\frac{60}{36}$ |
| 25. $\frac{90}{120}$ | 26. $\frac{60}{150}$ | 27. $\frac{70}{196}$ | 28. $\frac{98}{126}$ |

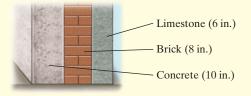


Objective B Determine whether each pair of fractions is equivalent. See Examples 8 and 9.



Objective C Solve. Write each fraction in simplest form. See Example 10.

- **53.** A work shift for an employee at McDonald's consists of 8 hours. What fraction of the employee's work shift is represented by 2 hours?
- 55. There are 5280 feet in a mile. What fraction of a mile is represented by 2640 feet?
 - **57.** There are 78 national monuments in the United States. Ten of these monuments are located in New Mexico. (*Source:* National Park Service)
 - **a.** What fraction of the national monuments in the United States can be found in New Mexico?
 - **b.** How many of the national monuments in the United States are found outside New Mexico?
 - **c.** Write the fraction of national monuments found in states other than New Mexico.
- ▶ 59. The outer wall of the Pentagon is 24 inches wide. Ten inches is concrete, 8 inches is brick, and 6 inches is limestone. What fraction of the wall is concrete? (Source: USA Today)



- **54.** Two thousand baseball caps were sold one year at the U.S. Open Golf Tournament. What fractional part of this total does 200 caps represent?
- **56.** There are 100 centimeters in 1 meter. What fraction of a meter is 20 centimeters?
- **58.** There have been 27 gold medals in men's eight plus coxswain rowing competition in the Olympic Summer Games. An American team has won 12 of them.
 - **a.** What fraction of these gold medals have been won by an American team?
 - **b.** How many of these gold medals have been won by non-American teams?
 - **c.** Write the fraction of gold medals in this competition that have been won by teams other than Americans.
- **60.** There are 35 students in a biology class. If 10 students made an A on the first test, what fraction of the students made an A?

- **61.** Albertsons Companies Inc. merged with Safeway Inc. and operates grocery stores under multiple banners in 33 states in the United States. (*Source:* Safeway, Inc.)
 - **a.** How many states do not have one of Albertsons Companies Inc. stores?
 - **b.** What fraction of states do not have an Albertsons Companies Inc. store?
- **63.** Worldwide, Hallmark employs about 9600 full-time employees. About 2700 employees work at the Hallmark headquarters in Kansas City, Missouri. What fraction of Hallmark full-time employees work in Kansas City? (*Source:* Hallmark)
- **62.** Katy Biagini just bought a brand-new 2017 Toyota Camry Hybrid for \$28,000. Her old car was traded in for \$12,000.
 - **a.** How much of her purchase price was not covered by her trade-in?
 - **b.** What fraction of the purchase price was not covered by her trade-in?
- **64.** Of the 20 most popular films released in 2016, eight had a movie rating of R. What fraction of 2016's most popular movies were R-rated? (*Source:* IMDB)

Review

Multiply. See Section 1.6.

| 65. 91 | 66. 73 | 67. 387 | 68. 562 | 69. 72 | 70. 238 |
|---------------|---------------|----------------|----------------|---------------|----------------|
| \times 4 | \times 8 | $\times 6$ | \times 9 | \times 35 | \times 26 |

Concept Extensions

71. In your own words, define equivalent fractions.

72. Given a fraction, say $\frac{3}{8}$, how many fractions are there that are equivalent to it? Explain your answer.

Write each fraction in simplest form.

73. $\frac{3975}{6625}$ **74.** $\frac{9506}{12,222}$

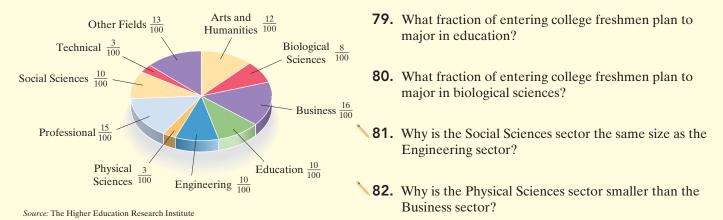
There are generally considered to be eight basic blood types. The table shows the number of people with the various blood types in a typical group of 100 blood donors. Use the table to answer Exercises 75 through 78. Write each answer in simplest form.

| | | B & X |
|--|----------|-----------|
| | | |
| | | |
| Stelling | A Martin | A Company |
| · ···································· | | |

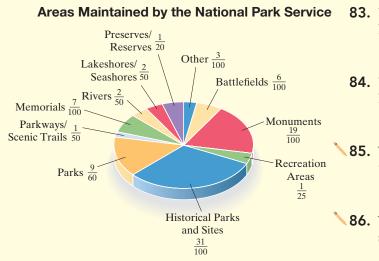
| Distribution of Blood Types in Blood Dor | | |
|--|------------------|--|
| Blood Type | Number of People | |
| O Rh-positive | 37 | |
| O Rh-negative | 7 | |
| A Rh-positive | 36 | |
| A Rh-negative | 6 | |
| 3 Rh-positive | 9 | |
| B Rh-negative | 1 | |
| AB Rh-positive | 3 | |
| AB Rh-negative | 1 | |

- **75.** What fraction of blood donors have blood type A Rh-positive?
- **77.** What fraction of blood donors have an AB blood type?
- **76.** What fraction of blood donors have an O blood type?
- **78.** What fraction of blood donors have a B blood type?

The following graph is called a **circle graph** or **pie chart**. Each sector (shaped like a piece of pie) shows the fraction of entering college freshmen who expect to major in each discipline shown. The whole circle represents the entire class of college freshmen. Use this graph to answer Exercises 79 through 82. Write each fraction answer in simplest form.



Use this circle graph to answer Exercises 83 through 86. Write each fraction answer in simplest form.



- **83.** What fraction of National Park Service areas are National Battlefields?
- **84.** What fraction of National Park Service areas are National Parks?
- **85.** Why is the National Battlefields sector smaller than the National Monuments sector?
- **86.** Why is the National Lakeshores/National Seashores sector the same size as the National Rivers sector?

Use the following numbers for Exercises 87 through 90.

8691 786 1235 2235 85 105 22

- **87.** List the numbers divisible by both 2 and 3.
- **89.** The answers to Exercise **87** are also divisible by what number? Tell why.

222 900 1470

- **88.** List the numbers that are divisible by both 3 and 5.
- **90.** The answers to Exercise **88** are also divisible by what number? Tell why.

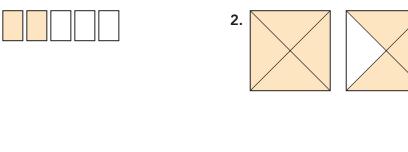
Integrated Review

Summary on Fractions, Mixed Numbers, and Factors

Use a fraction to represent the shaded area of each figure. If the fraction is improper, also write the fraction as a mixed number.

Sections 2.1–2.3

 $\frac{7}{0}$



Solve.

1.

3. In a survey, 73 people out of 85 get fewer than 8 hours of sleep each night. What fraction of people in the survey get fewer than 8 hours of sleep?

4. Sketch a diagram to represent $\frac{9}{13}$.

Simplify.

Write each mixed number as an improper fraction.

9. $3\frac{1}{8}$ **10.** $5\frac{3}{5}$ **11.** $9\frac{6}{7}$ **12.** $20\frac{1}{7}$

Write each improper fraction as a mixed number or a whole number.

| 13. $\frac{20}{7}$ 14. $\frac{55}{11}$ | 15. $\frac{39}{8}$ | 16. $\frac{98}{11}$ |
|--|---------------------------|----------------------------|
|--|---------------------------|----------------------------|

List the factors of each number.

17. 35 **18.** 40

Determine whether each number is prime or composite.

19. 72 **20.** 13

| Answers |
|------------|
| 1. |
| 2. |
| 3. |
| 4. |
| 5. |
| 6. |
| 7. |
| 8. |
| 9. |
| 10. |
| <u>11.</u> |
| 12. |
| 13. |
| 14. |
| 15. |
| 16. |
| 17. |
| 18. |
| 19. |
| 20. |

| 142 | Chapter 2 Multiplying and Dividing Fractions | | | | |
|--------------|--|--|-----------------------------|-----------------------------|--|
| 21. | Write the prime factorization of each composite number. Write "prime" if the number is prime. Write any repeated factors using exponents. | | | | |
| 22. | 21. 65 | 22. 70 | 23. 96 | 24. 132 | |
| 23. | | | | | |
| <u>24.</u> | 25. 252 | 26. 31 | 27. 315 | 28. 441 | |
| 25. | | | | | |
| 26. | 29. 286 | 30. 41 | | | |
| 27. | Write each fractio | on in simplest form. | | | |
| 28. | 31. $\frac{2}{14}$ | 32. $\frac{24}{20}$ | 33. $\frac{18}{38}$ | 34. $\frac{42}{110}$ | |
| 29. | 14 | 20 | 38 | 110 | |
| 30. | 35. $\frac{56}{60}$ | 36. $\frac{72}{80}$ | 37. $\frac{54}{135}$ | 38. $\frac{90}{240}$ | |
| 31. | 60 | 80 | 135 | 240 | |
| 32. | 165 | 245 | | | |
| 33. | 39. $\frac{165}{210}$ | 40. $\frac{245}{385}$ | | | |
| 34. | Determine wheth | ner each pair of fraction | ns is equivalent | | |
| 35. | | | | | |
| 36. | 41. $\frac{7}{8}$ and $\frac{9}{10}$ | 42. $\frac{10}{12}$ and $\frac{15}{18}$ | | | |
| 37. | Color Waite Const | | 4 G | | |
| 38. | Solve. Write fraction answers in simplest form.43. Of the 50 states, 2 states are not adjacent to any other states. | | | | |
| 39. | a. What fraction of the states are not adjacent to other states? | | | | |
| 40. | b. How many states are adjacent to other states?c. What fraction of the states are adjacent to other states? | | | | |
| 41. | | | | | |
| 42. | 44. Of the 42 to (<i>Source:</i> IM | | eleased in 2016, 22 had a | a rating of PG-13. | |
| 43. a. b. c. | a. What fra | ction were rated PG-1. | | | |
| 44. a. b. c. | b. How many of these films were rated other than PG-13?c. What fraction of these films were rated other than PG-13? | | | | |
| | | | | | |

2.4 Multiplying Fractions and Mixed Numbers

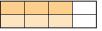
Objective A Multiplying Fractions 🕗

Let's use a diagram to discover how fractions are multiplied. For example, to multiply $\frac{1}{2}$ and $\frac{3}{4}$, we find $\frac{1}{2}$ of $\frac{3}{4}$. To do this, we begin with a diagram showing $\frac{3}{4}$ of a rectangle's area shaded.



 $\frac{3}{4}$ of the rectangle's area is shaded.

To find $\frac{1}{2}$ of $\frac{3}{4}$, we heavily shade $\frac{1}{2}$ of the part that is already shaded.



By counting smaller rectangles, we see that $\frac{3}{8}$ of the larger rectangle is now heavily shaded, so that

 $\frac{1}{2} \text{ of } \frac{3}{4} \text{ is } \frac{3}{8}, \text{ or } \frac{1}{2} \cdot \frac{3}{4} = \frac{3}{8} \text{ Notice that } \frac{1}{2} \cdot \frac{3}{4} = \frac{1 \cdot 3}{2 \cdot 4} = \frac{3}{8}.$

Multiplying Fractions

To multiply two fractions, multiply the numerators and multiply the denominators. If a, b, c, and d represent nonzero whole numbers, we have

$$\frac{a}{b} \cdot \frac{c}{d} = \frac{a \cdot c}{b \cdot d}$$

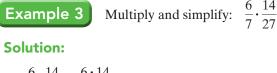
Examples Multiply.

1. $\frac{2}{3} \cdot \frac{5}{11} = \frac{2 \cdot 5}{3 \cdot 11} = \frac{10}{33}$ Multiply numerators. Multiply denominators.

This fraction is in simplest form since 10 and 33 have no common factors other than 1.

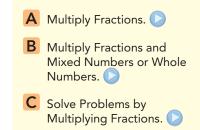
2. $\frac{1}{4} \cdot \frac{1}{2} = \frac{1 \cdot 1}{4 \cdot 2} = \frac{1}{8}$ This fraction is in simplest form.

Work Practice 1–2



```
\frac{6}{7} \cdot \frac{14}{27} = \frac{6 \cdot 14}{7 \cdot 27}
```

Objectives



Practice 1–2

Multiply.

1

$$1. \frac{3}{8} \cdot \frac{5}{7} \qquad 2. \frac{1}{3} \cdot \frac{1}{6}$$

Practice 3

Multiply and simplify:
$$\frac{6}{55}$$
.

Answers

1.
$$\frac{15}{56}$$
 2. $\frac{1}{18}$ **3.** $\frac{3}{44}$

(Continued on next page)

5

8

Chapter 2 | Multiplying and Dividing Fractions

We can simplify by finding the prime factorizations and using our shortcut procedure of dividing out common factors in the numerator and denominator.

$$\frac{6\cdot 14}{7\cdot 27} = \frac{2\cdot \cancel{3}\cdot 2\cdot \cancel{7}}{\cancel{7}\cdot \cancel{3}\cdot 3\cdot 3} = \frac{2\cdot 2}{3\cdot 3} = \frac{4}{9}$$

Work Practice 3

Helpful Hint

Remember that the shortcut procedure above is the same as removing factors of 1 in the product.

$$\frac{6 \cdot 14}{7 \cdot 27} = \frac{2 \cdot 3 \cdot 2 \cdot 7}{7 \cdot 3 \cdot 3 \cdot 3} = \frac{7}{7} \cdot \frac{3}{3} \cdot \frac{2 \cdot 2}{3 \cdot 3} = 1 \cdot 1 \cdot \frac{4}{9} = \frac{4}{9}$$

Helpful Hint

In simplifying a product, don't forget that it may be possible to identify common factors without actually writing the prime factorizations. For example,

$$\frac{10}{11} \cdot \frac{1}{20} = \frac{10 \cdot 1}{11 \cdot 20} = \frac{10 \cdot 1}{11 \cdot 10 \cdot 2} = \frac{1}{11 \cdot 20} = \frac{1}{22}$$

| Example | Multiply and simplify: | $\frac{23}{32} \cdot \frac{4}{7}$ |
|-----------|----------------------------|-----------------------------------|
| Solution: | otice that 4 and 32 have a | common factor of 4. |

$$\frac{23}{32} \cdot \frac{4}{7} = \frac{23 \cdot 4}{32 \cdot 7} = \frac{23 \cdot \cancel{4}}{\cancel{4} \cdot 8 \cdot 7} = \frac{23}{8 \cdot 7} = \frac{23}{56}$$

After multiplying two fractions, always check to see whether the product can be simplified.

7. $\frac{1}{6} \cdot \frac{3}{10} \cdot \frac{25}{16}$ Answers 4. $\frac{1}{10}$ 5. $\frac{8}{7}$ 6. $\frac{3}{4}$ 7. $\frac{5}{64}$

Practice 5–7

Multiply.

5. $\frac{2}{5} \cdot \frac{20}{7}$

6. $\frac{4}{11} \cdot \frac{33}{16}$

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Practice 4 Multiply and simplify: $\frac{4}{15} \cdot \frac{3}{8}$

Objective **B** Multiplying Fractions and Mixed Numbers or Whole Numbers

When multiplying a fraction and a mixed or a whole number, remember that mixed and whole numbers can be written as fractions.

Multiplying Fractions and Mixed Numbers or Whole Numbers

To multiply with mixed numbers or whole numbers, first write any mixed or whole numbers as fractions and then multiply as usual.

Example 8 Multiply:
$$3\frac{1}{3} \cdot \frac{7}{8}$$

Solution: The mixed number $3\frac{1}{3}$ can be written as the fraction $\frac{10}{3}$. Then,
 $3\frac{1}{3} \cdot \frac{7}{8} = \frac{10}{3} \cdot \frac{7}{8} = \frac{\frac{1}{2} \cdot 5 \cdot 7}{3 \cdot \frac{2}{1} \cdot 4} = \frac{35}{12}$ or $2\frac{11}{12}$

Work Practice 8

Don't forget that a whole number can be written as a fraction by writing the whole number over 1. For example,

 $20 = \frac{20}{1}$ and $7 = \frac{7}{1}$

Example 9 Multiply. $\frac{3}{4} \cdot 20 = \frac{3}{4} \cdot \frac{20}{1} = \frac{3 \cdot 20}{4 \cdot 1} = \frac{3 \cdot \cancel{4} \cdot 5}{\cancel{4} \cdot 1} = \frac{15}{1}$ or 15

Work Practice 9

When both numbers to be multiplied are mixed or whole numbers, it is a good idea to estimate the product to see if your answer is reasonable. To do this, we first practice rounding mixed numbers to the nearest whole. If the fraction part of the mixed number is $\frac{1}{2}$ or greater, we round the whole number part up. If the fraction part of the mixed number is less than $\frac{1}{2}$, then we do not round the whole number part up. Study the table below for examples.

| Mixed Number | Rounding | |
|---|------------------------------------|--|
| $5\frac{1}{4} \frac{1}{4} \text{ is less than } \frac{1}{2}$ | Thus, $5\frac{1}{4}$ rounds to 5. | |
| $3\frac{9}{16} \leftarrow 9$ is greater than 8
$3\frac{16}{16} \rightarrow \text{Half of 16 is 8.}$ | Thus, $3\frac{9}{16}$ rounds to 4. | |
| $1\frac{3}{7} \leftarrow 3 \text{ is less than } 3\frac{1}{2}.$
1 $\frac{3}{7} \rightarrow \text{Half of 7 is } 3\frac{1}{2}.$ | Thus, $1\frac{3}{7}$ rounds to 1. | |

Practice 9 Multiply.

$$\frac{2}{3} \cdot 18$$

Answers 8. $\frac{4}{3}$ or $1\frac{1}{3}$ 9. 12

Practice 8

Multiply and simplify:
$$2\frac{1}{2} \cdot \frac{3}{15}$$

Chapter 2 | Multiplying and Dividing Fractions

Examples Multiply. Check by estimating.

Practice 10–11 Multiply.

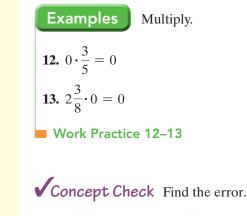
10. $3\frac{1}{5} \cdot 2\frac{3}{4}$ **11.** $5 \cdot 3\frac{11}{15}$

Practice 12–13 Multiply. **12.** $\frac{9}{11} \cdot 0$

13. $0 \cdot 4\frac{1}{8}$

10. $1\frac{2}{3} \cdot 2\frac{1}{4} = \frac{5}{3} \cdot \frac{9}{4} = \frac{5 \cdot 9}{3 \cdot 4} = \frac{5 \cdot \cancel{3} \cdot 3}{\cancel{3} \cdot 4} = \frac{15}{4} \text{ or } 3\frac{3}{4}$ Exact Let's check by estimating. $1\frac{2}{3}$ rounds to 2, $2\frac{1}{4}$ rounds to 2, and $2 \cdot 2 = 4$ Estimate The estimate is close to the exact value, so our answer is reasonable. 11. $7 \cdot 2\frac{11}{14} = \frac{7}{1} \cdot \frac{39}{14} = \frac{7 \cdot 39}{1 \cdot 14} = \frac{\cancel{7} \cdot 39}{1 \cdot 2 \cdot \cancel{7}} = \frac{39}{2} \text{ or } 19\frac{1}{2}$ Exact To estimate, $2\frac{11}{14}$ rounds to 3 and $7 \cdot 3 = 21$. Estimate The estimate is close to the exact value, so our answer is reasonable.

Recall from Section 1.6 that 0 multiplied by any number is 0. This is true of fractions and mixed numbers also.



| $2^{1}_{-}, \frac{1}{-} =$ | $2\frac{1\cdot 1}{2} = 2\frac{1}{2}$ |
|----------------------------|--------------------------------------|
| 4 2 | $4 \cdot 2 = 8$ |

Objective C Solving Problems by Multiplying Fractions

To solve real-life problems that involve multiplying fractions, we use our four problem-solving steps from Chapter 1. In Example 14, a key word that implies multiplication is used. That key word is "**of**."

Helpful Hint

"of" usually translates to multiplication.

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Answers

10. $\frac{44}{5}$ or $8\frac{4}{5}$ **11.** $\frac{56}{3}$ or $18\frac{2}{3}$ **12.** 0 **13.** 0

Concept Check Answer

forgot to change mixed number to fraction

Example 14 Finding the Number of Roller Coasters in an Amusement Park

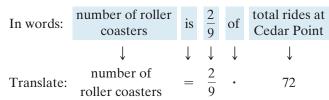
Cedar Point is an amusement park located in Sandusky, Ohio. Its collection of 72 rides is the largest in the world. Of the rides, $\frac{2}{9}$ are roller coasters. How many roller coasters are in Cedar Point's collection of rides? (*Source:* Cedar Fair Parks)

Solution:

1. UNDERSTAND the problem. To do so, read and reread the problem. We are told that $\frac{2}{9}$ of Cedar

Point's rides are roller coasters. The word "of" here means multiplication.

2. TRANSLATE.



3. SOLVE: Before we solve, let's estimate a reasonable answer. The fraction $\frac{2}{9}$ is less than $\frac{1}{3}$ (draw a diagram, if needed), and $\frac{1}{3}$ of 72 rides is 24 rides, so the number of roller coasters should be less than 24.

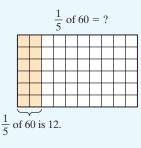
$$\frac{2}{9} \cdot 72 = \frac{2}{9} \cdot \frac{72}{1} = \frac{2 \cdot 72}{9 \cdot 1} = \frac{2 \cdot \cancel{9} \cdot 8}{\cancel{9} \cdot 1} = \frac{16}{1} \quad \text{or} \quad 16$$

4. INTERPRET. *Check* your work. From our estimate, our answer is reasonable. *State* your conclusion: The number of roller coasters at Cedar Point is 16.

Work Practice 14

Helpful Hint

To help visualize a fractional part of a whole number, look at the diagram below.





Practice 14

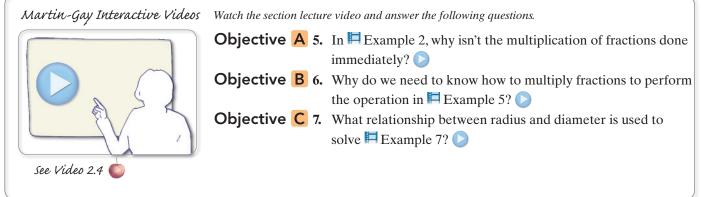
Kings Dominion is an amusement park in Doswell, Virginia.

Of its 48 rides, $\frac{5}{16}$ of them are roller coasters. How many roller coasters are in Kings Dominion? (*Source:* Cedar Fair Parks)

Answer 14. 15 roller coasters

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Not all choices will be used. multiplication $\frac{a \cdot d}{b \cdot c} = \frac{a \cdot c}{b \cdot d} = \frac{2 \cdot 2 \cdot 2}{7} = \frac{2}{7} \cdot \frac{2}{7} \cdot \frac{2}{7} \cdot \frac{2}{7}$ division 0 1. To multiply two fractions, we write $\frac{a}{b} \cdot \frac{c}{d} =$ _____. 2. Using the definition of an exponent, the expression $\frac{2^3}{7} =$ ______ while $\left(\frac{2}{7}\right)^3 =$ ______. 3. The word "of" indicates ______. 4. $\frac{1}{5} \cdot 0 =$ ______.



2.4 Exercise Set MyLab Math

Objective A *Multiply. Write each answer in simplest form. See Examples 1 through 7 and 12.*

| 1. $\frac{1}{3} \cdot \frac{2}{5}$ | 2. $\frac{2}{3} \cdot \frac{4}{7}$ | 3. $\frac{6}{5} \cdot \frac{1}{7}$ | 4. $\frac{7}{3} \cdot \frac{1}{4}$ | 5. $\frac{3}{10} \cdot \frac{3}{8}$ |
|---|---|---|--|--|
| 6. $\frac{2}{5} \cdot \frac{7}{11}$ | • 7. $\frac{2}{7} \cdot \frac{5}{8}$ | 8. $\frac{7}{8} \cdot \frac{2}{3}$ | 9. $\frac{16}{5} \cdot \frac{3}{4}$ | 10. $\frac{8}{3} \cdot \frac{5}{12}$ |
| 11. $\frac{5}{28} \cdot \frac{2}{25}$ | 12. $\frac{4}{35} \cdot \frac{5}{24}$ | 13. $0 \cdot \frac{8}{9}$ | 14. $\frac{11}{12} \cdot 0$ | 15. $\frac{1}{10} \cdot \frac{1}{11}$ |
| 16. $\frac{1}{9} \cdot \frac{1}{13}$ | 17. $\frac{18}{20} \cdot \frac{36}{99}$ | 18. $\frac{5}{32} \cdot \frac{64}{100}$ | 19. $\frac{3}{8} \cdot \frac{9}{10}$ | 20. $\frac{4}{5} \cdot \frac{8}{25}$ |
| 21. $\frac{11}{20} \cdot \frac{1}{7} \cdot \frac{5}{22}$ | 22. $\frac{27}{32} \cdot \frac{10}{13} \cdot \frac{16}{30}$ | 23. $\frac{1}{3} \cdot \frac{2}{7} \cdot \frac{1}{5}$ | 24. $\frac{3}{5} \cdot \frac{1}{2} \cdot \frac{3}{7}$ | 25. $\frac{9}{20} \cdot 0 \cdot \frac{4}{19}$ |
| 26. $\frac{8}{11} \cdot \frac{4}{7} \cdot 0$ | 27. $\frac{3}{14} \cdot \frac{6}{25} \cdot \frac{5}{27} \cdot \frac{7}{6}$ | 28. $\frac{7}{8} \cdot \frac{9}{20} \cdot \frac{12}{22} \cdot \frac{11}{14}$ | | |

Objective B Round each mixed number to the nearest whole number. See the table at the bottom of page 145.

29. $7\frac{7}{8}$ **30.** $11\frac{3}{4}$ **31.** $6\frac{1}{5}$ **32.** $4\frac{1}{9}$ **33.** $19\frac{11}{20}$ **34.** $18\frac{12}{22}$

Multiply. Write each answer in simplest form. For those exercises marked, find both an exact product and an estimated product. See Examples 8 through 13.

- **35.** $12 \cdot \frac{1}{4}$ **36.** $\frac{2}{3} \cdot 6$ **37.** $\frac{5}{8} \cdot 4$ **38.** $10 \cdot \frac{7}{8}$ **39.** $1\frac{1}{4} \cdot \frac{4}{25}$
- **40.** $\frac{3}{22} \cdot 3\frac{2}{3}$ **41.** $\frac{2}{5} \cdot 4\frac{1}{6}$ **42.** $2\frac{1}{9} \cdot \frac{6}{7}$ **43.** $\frac{2}{3} \cdot 1$ **44.** $1 \cdot \frac{5}{9}$
- **45.** $2\frac{1}{5} \cdot 3\frac{1}{2}$ **46.** $2\frac{1}{4} \cdot 7\frac{1}{8}$ **47.** $3\frac{4}{5} \cdot 6\frac{2}{7}$ **48.** $5\frac{5}{6} \cdot 7\frac{3}{5}$ **49.** $5 \cdot 2\frac{1}{2}$
 - Estimate: Estimate: Estimate: Estimate:
 - **50.** $4 \cdot 3\frac{1}{3}$ **51.** $1\frac{1}{5} \cdot 12\frac{1}{2}$ **52.** $1\frac{1}{6} \cdot 7\frac{1}{5}$ **53.** $\frac{3}{4} \cdot 16 \cdot \frac{1}{2}$ **54.** $\frac{7}{8} \cdot 24 \cdot \frac{1}{3}$

Exact:

Exact:

55. $\frac{3}{10} \cdot 15 \cdot 2\frac{1}{2}$ **56.** $\frac{11}{14} \cdot 6 \cdot 2\frac{2}{3}$ **57.** $3\frac{1}{2} \cdot 1\frac{3}{4} \cdot 2\frac{2}{3}$ **58.** $4\frac{1}{2} \cdot 2\frac{1}{9} \cdot 1\frac{1}{5}$

Exact:

Exact:

Objectives A B Mixed Practice Multiply and simplify. See Examples 1 through 13.

59. $\frac{1}{4} \cdot \frac{2}{15}$ **60.** $\frac{3}{8} \cdot \frac{5}{12}$ **61.** $\frac{19}{37} \cdot 0$ **62.** $0 \cdot \frac{3}{31}$ **63.** $2\frac{4}{5} \cdot 1\frac{1}{7}$
64. $3\frac{1}{5} \cdot 2\frac{11}{32}$ **65.** $\frac{3}{2} \cdot \frac{7}{3}$ **66.** $\frac{15}{2} \cdot \frac{3}{5}$ **67.** $\frac{6}{15} \cdot \frac{5}{16}$ **68.** $\frac{9}{20} \cdot \frac{10}{90}$
69. $\frac{7}{72} \cdot \frac{9}{49}$ **70.** $\frac{3}{80} \cdot \frac{2}{27}$ **71.** $20 \cdot \frac{11}{12}$ **72.** $30 \cdot \frac{8}{9}$ **73.** $9\frac{5}{7} \cdot 8\frac{1}{5} \cdot 0$
74. $4\frac{11}{13} \cdot 0 \cdot 12\frac{1}{13}$ **75.** $12\frac{4}{5} \cdot 6\frac{7}{8} \cdot \frac{26}{77}$ **76.** $14\frac{2}{5} \cdot 8\frac{1}{3} \cdot \frac{11}{16}$ **71.** $20 \cdot \frac{11}{16}$

Objective C Solve. Write each answer in simplest form. For Exercises 77 through 80, recall that "of" translates to multiplication. See Example 14.

77. Find
$$\frac{1}{4}$$
 of 200. **78.** Find $\frac{1}{5}$ of 200. **79.** Find $\frac{5}{6}$ of 24. **80.** Find $\frac{5}{8}$ of 24

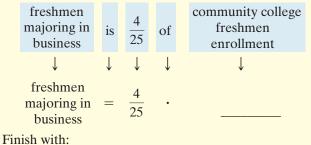
Solve. For Exercises 81 and 82, the solutions have been started for you. See Example 14.

81. In the United States, $\frac{4}{25}$ of college freshmen major in **82.** A patient was told that, at most, $\frac{1}{5}$ of his calories

business. A community college in Pennsylvania has a freshman enrollment of approximately 800 students. How many of these freshmen might we expect to major in business?

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blank below.)



- **3.** SOLVE
- **4.** INTERPRET
- **83.** In 2016, there were approximately 250 million moviegoers in the United States and Canada. Of these, about

 $\frac{12}{25}$ were male. Find the approximate number of

males who attended the movies in that year. (*Source:* Motion Picture Association of America)

▶ 85. The Oregon National Historic Trail is 2170 miles long. It begins in Independence, Missouri, and ends in Oregon City, Oregon. Manfred Coulon has hiked

 $\frac{2}{5}$ of the trail before. How many miles has he hiked?

(Source: National Park Service)



82. A patient was told that, at most, $\frac{1}{5}$ of his calories should come from fat. If his diet consists of 3000 calories a day, find the maximum number of calories that can come from fat.

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blank below.)

| patient's
fat calories | is | $\frac{1}{5}$ | of | his daily calories |
|---------------------------|--------------|---------------|--------------|--------------------|
| \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| patient's fat calories | = | $\frac{1}{5}$ | • | |

Finish with: **3.** SOLVE

- **4.** INTERPRET
- **84.** In 2016, cinemas in the United States and Canada sold about 1300 million movie tickets. About $\frac{12}{25}$ of

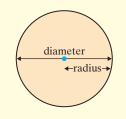
these tickets were purchased by frequent moviegoers who go to the cinema once or more per month. Find the number of tickets purchased by frequent moviegoers in 2016. (*Source:* Motion Picture Association of America)

86. Each turn of a screw sinks it $\frac{3}{16}$ of an inch deeper

into a piece of wood. Find how deep the screw is after 8 turns.



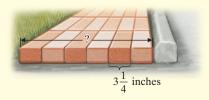
• 87. The radius of a circle is one-half of its diameter, as shown. If the diameter of a circle is $\frac{3}{8}$ of an inch, what is its radius?



89. A veterinarian's dipping vat holds 36 gallons of liquid. She normally fills it $\frac{5}{6}$ full of a medicated flea dip solution. Find how many gallons of solution are normally in the vat.

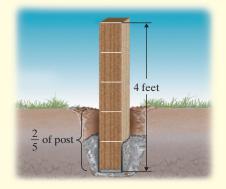


- **91.** An estimate for the measure of an adult's wrist is $\frac{1}{4}$ of the waist size. If Jorge has a 34-inch waist, estimate the size of his wrist.
- **93.** A sidewalk is built 6 bricks wide by laying each brick side by side. How many inches wide is the sidewalk if each brick measures $3\frac{1}{4}$ inches wide?



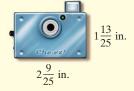
 \triangle 88. The diameter of a circle is twice its radius, as shown in the Exercise 87 illustration. If the radius of a circle is $\frac{7}{20}$ of a foot, what is its diameter?

90. The plans for a deck call for $\frac{2}{5}$ of a 4-foot post to be underground. Find the length of the post that is to be buried.



- **92.** An estimate for an adult's waist measurement is found by multiplying the neck size (in inches) by 2. Jock's neck measures $17\frac{1}{2}$ inches. Estimate his waist measurement.
- **94.** A recipe calls for $\frac{1}{3}$ of a cup of flour. How much flour should be used if only $\frac{1}{2}$ of the recipe is being made?

95. A Japanese company called Che-ez! manufactures a small digital camera, the SPYZ camera. The face of the camera measures $2\frac{9}{25}$ inches by $1\frac{13}{25}$ inches and is slightly bigger than a Zippo lighter. Find the area of the face of this camera. (Area = length · width)



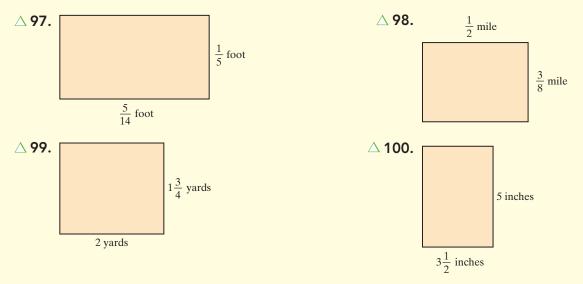
96. As part of his research, famous tornado expert Dr. T. Fujita studied approximately 31,050 tornadoes that occurred in the United States between 1916 and 7

1985. He found that roughly $\frac{7}{10}$ of these tornadoes

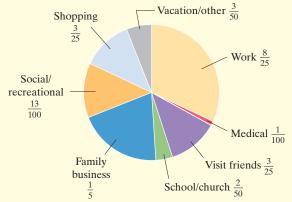
occurred during April, May, June, and July. How many of these tornadoes occurred during these four months? (*Source: U.S. Tornadoes Part 1*, T. Fujita, University of Chicago)



Find the area of each rectangle. Recall that area = $length \cdot width$.



Recall that the following graph is called a **circle graph** or **pie chart**. Each sector (shaped like a piece of pie) shows the fractional part of a car's total mileage that falls into a particular category. The whole circle represents a car's total mileage.



In one year, a family drove 12,000 miles in the family car. Use the circle graph to determine how many of these miles might be expected to fall in the categories shown in Exercises 101 through 104.

101. Work

102. Shopping

103. Family business

104. Medical

Source: The American Automobile Manufacturers Association and The National Automobile Dealers Association

| Review | | | |
|--------------------------|--------------------|---------------------|---------------------|
| Divide. See Section 1.7. | | | |
| 105. 8)1648 | 106. 7)3920 | 107. 23)1300 | 108. 31)2500 |

Concept Extensions

- **109.** In your own words, explain how to multiply **a.** fractions
 - **b.** mixed numbers

- **110.** In your own words, explain how to round a mixed number to the nearest whole number.
- Find the error in each calculation. See the Concept Check in this section.
- **111.** $3\frac{2}{3} \cdot 1\frac{1}{7} = 3\frac{2}{21}$ **112.** $5 \cdot 2\frac{1}{4} = 10\frac{1}{4}$

Choose the best estimate for each product.

- **114.** $\frac{11}{12} \cdot 4\frac{1}{16}$ **113.** $3\frac{1}{5} \cdot 4\frac{5}{8}$ **115.** $9 \cdot \frac{10}{11}$ **116.** $7\frac{1}{4} \cdot 4\frac{1}{5}$ **a.** 40 **a.** 7 **a.** 16 **a.** 9 **b.**15 **b.** 90 **b.** $\frac{7}{5}$ **b.** 1 **c.** 8 **c.** 4 **c.** 99 **c.** 35 **d.** $12\frac{1}{8}$ **d.** 0 **d.** 8 **d.** 28
- **117.** If $\frac{3}{4}$ of 36 students on a first bus are girls and $\frac{2}{3}$ of the 30 students on a second bus are *boys*, how many

students on the two buses are girls?

- **118.** In 2016, a survey found that about $\frac{14}{25}$ of all adults in the United States owned a smartphone. There were roughly 250 million U.S. adults at that time. How many U.S. adults owned a smartphone in 2016? (*Source:* Pew Research Center, U.S. Census Bureau)
- **119.** The estimated population of New Zealand was 4,565,000 in 2016. About $\frac{3}{20}$ of New Zealand's population is of Māori descent. How many Māori lived in New Zealand in 2016? (*Source:* Statistics New Zealand)
- **120.** Approximately $\frac{1}{9}$ of the U.S. population lived in the state of California in 2016. If the U.S. population was approximately 317,295,000, find the approxi-

mate population of California. (*Source:* U.S. Census Bureau)

Objectives

- A Find the Reciprocal of a Fraction.
- B Divide Fractions.
- C Divide Fractions and Mixed Numbers or Whole Numbers. 🕩
- D Solve Problems by Dividing Fractions. D

Practice 1–4

Find the reciprocal of each number.

1.
$$\frac{4}{9}$$
 2. $\frac{15}{7}$
3. 9 **4.** $\frac{1}{8}$

2.5 Dividing Fractions and Mixed Numbers

Objective A Finding Reciprocals of Fractions

Before we can divide fractions, we need to know how to find the reciprocal of a fraction or whole number.

Reciprocal of a Fraction

Two numbers are reciprocals of each other if their product is 1. The reciprocal of the fraction $\frac{a}{b}$ is $\frac{b}{a}$ because $\frac{a}{b} \cdot \frac{b}{a} = \frac{a \cdot b}{b \cdot a} = 1$.

Finding the Reciprocal of a Fraction

To find the reciprocal of a fraction, interchange its numerator and denominator.

For example,

| The reciprocal of $\frac{2}{5}$ is | $\frac{5}{2}$ because $\frac{2}{5}$ | $\frac{2}{5} \cdot \frac{5}{2} =$ | $\frac{10}{10} =$ | = 1. | |
|---|-------------------------------------|-----------------------------------|-------------------|-----------------------------|------|
| The reciprocal of 7, or $\frac{7}{1}$, i | s $\frac{1}{7}$ because | $7 \cdot \frac{1}{7} =$ | $\frac{7}{1}$ | $\frac{1}{7} = \frac{7}{7}$ | = 1. |

Examples

Find the reciprocal of each number.

1. The reciprocal of $\frac{5}{6}$ is $\frac{6}{5}$. $\frac{5}{6} \cdot \frac{6}{5} = \frac{5 \cdot 6}{6 \cdot 5} = \frac{30}{30} = 1$ 2. The reciprocal of $\frac{11}{8}$ is $\frac{8}{11}$. $\frac{11}{8} \cdot \frac{8}{11} = \frac{11 \cdot 8}{8 \cdot 11} = \frac{88}{88} = 1$ 3. The reciprocal of $\frac{1}{3}$ is $\frac{3}{1}$ or 3. $\frac{1}{3} \cdot \frac{3}{1} = \frac{1 \cdot 3}{3 \cdot 1} = \frac{3}{3} = 1$ 4. The reciprocal of 5, or $\frac{5}{1}$, is $\frac{1}{5}$. $\frac{5}{1} \cdot \frac{1}{5} = \frac{5 \cdot 1}{1 \cdot 5} = \frac{5}{5} = 1$ Work Practice 1–4

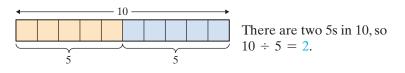
Helpful Hint

Every number except 0 has a reciprocal. The number 0 has no reciprocal because there is no number that when multiplied by 0 gives a result of 1.

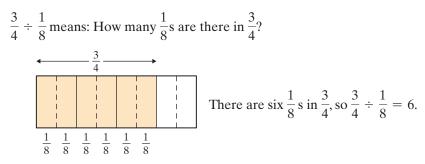
Objective **B** Dividing Fractions **C**

Division of fractions has the same meaning as division of whole numbers. For Copyright 2019 Pearson Education, example,

 $10 \div 5$ means: How many 5s are there in 10?



Answers **1.** $\frac{9}{4}$ **2.** $\frac{7}{15}$ **3.** $\frac{1}{9}$ **4.** 8



We use reciprocals to divide fractions.

Dividing Fractions

To divide two fractions, multiply the first fraction by the reciprocal of the second fraction.

If *a*, *b*, *c*, and *d* represent numbers, and *b*, *c*, and *d* are not 0, then

$$\frac{a}{b} \div \frac{c}{d} = \frac{a}{b} \cdot \frac{d}{c} = \frac{a \cdot d}{b \cdot c}$$
$$\downarrow_{\text{reciprocal}}^{\uparrow}$$

For example,

multiply by reciprocal

$$\frac{3}{4} \div \frac{1}{8} = \frac{3}{4} \cdot \frac{8}{1} = \frac{3 \cdot 8}{4 \cdot 1} = \frac{3 \cdot 2 \cdot \frac{1}{4}}{4 \cdot 1} = \frac{6}{1} \text{ or } 6$$

Just as when you are multiplying fractions, always check to see whether your answer can be simplified when you divide fractions.

Examples Divide and simplify.
5.
$$\frac{7}{8} \div \frac{2}{9} = \frac{7}{8} \cdot \frac{9}{2} = \frac{7 \cdot 9}{8 \cdot 2} = \frac{63}{16}$$

6. $\frac{5}{16} \div \frac{3}{4} = \frac{5}{16} \cdot \frac{4}{3} = \frac{5 \cdot 4}{16 \cdot 3} = \frac{5 \cdot \frac{1}{4}}{\frac{4}{1} \cdot 4 \cdot 3} = \frac{5}{12}$
7. $\frac{2}{5} \div \frac{1}{2} = \frac{2}{5} \cdot \frac{2}{1} = \frac{2 \cdot 2}{5 \cdot 1} = \frac{4}{5}$
Work Practice 5-7

Helpful Hint

When dividing fractions, do *not* look for common factors to divide out until you rewrite the division as multiplication.

Practice 5–7

Divide and simplify.

5.
$$\frac{3}{2} \div \frac{14}{5}$$
 6. $\frac{8}{7} \div \frac{2}{9}$
7. $\frac{4}{9} \div \frac{1}{2}$

Answers 5. $\frac{15}{28}$ 6. $\frac{36}{7}$ 7. $\frac{8}{9}$ Recall from Section 1.7 that the quotient of 0 and any number (except 0) is 0. This is true of fractions and mixed numbers also. For example,

$$0 \div \frac{7}{8} = \underbrace{0 \cdot \frac{8}{7}}_{7} = 0$$
 Recall that 0 multiplied by any number is 0.

Also recall from Section 1.7 that the quotient of any number and 0 is undefined. This is also true of fractions and mixed numbers. For example, to find $\frac{7}{8} \div 0$, or $\frac{7}{8} \div \frac{0}{1}$, we would need to find the reciprocal of $0 \left(\text{or } \frac{0}{1} \right)$. As we mentioned in the helpful hint at the beginning of this section, 0 has no reciprocal because there is no number that when multiplied by 0 gives a result of 1. Thus,

$$\frac{7}{8} \div 0$$
 is undefined

Examples Divide.

8. $0 \div \frac{2}{21} = 0 \cdot \frac{21}{2} = 0$ **9.** $\frac{3}{4} \div 0$ is undefined.

Work Practice 8–9

Concept Check Which of the following is the correct way to divide $\frac{2}{5}$ by $\frac{3}{4}$? Or are both correct? Explain.

a.
$$\frac{5}{2} \cdot \frac{5}{4}$$
 b. $\frac{2}{5} \cdot \frac{4}{3}$

Objective C Dividing Fractions and Mixed Numbers or Whole Numbers ()

Just as with multiplying, mixed or whole numbers should be written as fractions before you divide them.

Dividing Fractions and Mixed Numbers or Whole Numbers

To divide with a mixed number or a whole number, first write the mixed or whole number as a fraction and then divide as usual.

Examples Divide. 10. $\frac{3}{4} \div 5 = \frac{3}{4} \div \frac{5}{1} = \frac{3}{4} \cdot \frac{1}{5} = \frac{3 \cdot 1}{4 \cdot 5} = \frac{3}{20}$ 11. $\frac{11}{18} \div 2\frac{5}{6} = \frac{11}{18} \div \frac{17}{6} = \frac{11}{18} \cdot \frac{6}{17} = \frac{11 \cdot 6}{18 \cdot 17} = \frac{11 \cdot \frac{1}{6'}}{\frac{1}{6'} \cdot 3 \cdot 17} = \frac{11}{51}$ 12. $5\frac{2}{3} \div 2\frac{5}{9} = \frac{17}{3} \div \frac{23}{9} = \frac{17}{3} \cdot \frac{9}{23} = \frac{17 \cdot 9}{3 \cdot 23} = \frac{17 \cdot \frac{1}{3'} \cdot 3}{\frac{3'}{1} \cdot 23} = \frac{51}{23} \text{ or } 2\frac{5}{23}$ Work Practice 10–12

Divide. **10.** $\frac{4}{9} \div 7$ **11.** $\frac{8}{15} \div 3\frac{4}{5}$

12.
$$3\frac{2}{7} \div 2\frac{3}{14}$$

Practice 10–12

Answers 8. undefined 9. 0 10. $\frac{4}{63}$ 11. $\frac{8}{57}$ 12. $\frac{46}{31}$ or $1\frac{15}{31}$

Concept Check Answers a. incorrect b. correct

Divide.
8.
$$\frac{14}{17} \div 0$$
 9. $0 \div \frac{1}{8}$

Practice 8–9

Objective D Solving Problems by Dividing Fractions 🕑

To solve real-life problems that involve dividing fractions, we continue to use our four problem-solving steps.

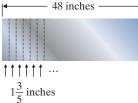
Example 13 Calculating Manufacturing Materials Needed

In a manufacturing process, a metal-cutting machine cuts strips $1\frac{3}{5}$ inches wide

from a piece of metal stock. How many such strips can be cut from a 48-inch piece of stock?

Solution:

1. UNDERSTAND the problem. To do so, read and reread the problem. Then draw a diagram:



We want to know how many $1\frac{3}{5}$ s there are in 48.

2. TRANSLATE.

| In words: | Number of strips | is | 48 | divided
by | $1\frac{3}{5}$ |
|------------|------------------|--------------|--------------|---------------|----------------|
| | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| Translate: | Number of strips | = | 48 | ÷ | $1\frac{3}{5}$ |

3. SOLVE: Let's estimate a reasonable answer. The mixed number $1\frac{3}{5}$ rounds to 2 and 48 \div 2 = 24.

$$48 \div 1\frac{3}{5} = 48 \div \frac{8}{5} = \frac{48}{1} \cdot \frac{5}{8} = \frac{48 \cdot 5}{1 \cdot 8} = \frac{\cancel{3} \cdot 6 \cdot 5}{1 \cdot \cancel{3}} = \frac{\cancel{3}}{1} \text{ or } 30$$

4. INTERPRET. *Check* your work. Since the exact answer of 30 is close to our estimate of 24, our answer is reasonable. *State* your conclusion: Thirty strips can be cut from the 48-inch piece of stock.

Work Practice 13

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Not all choices will be used.

| multiplication | $a \cdot d$ | $a \cdot c$ |
|----------------|-------------|------------------------|
| muniplication | $b \cdot c$ | $\overline{b \cdot d}$ |
| division | 0 | reciprocals |

1. Two numbers are ______ of each other if their product is 1.

2. Every number has a reciprocal except _____

3. To divide two fractions, we write $\frac{a}{b} \div \frac{c}{d} =$ _____.

4. The word "per" usually indicates _____.

Practice 13

A designer of clothing designs an outfit that requires $2\frac{1}{7}$ yards

of material. How many outfits can be made from a 30-yard bolt of material?

Answer 13. 14 outfits

| Martin-Gay Interactive Videos | Watch the section lectur | re video and answer the following questions. | |
|-------------------------------|--------------------------|--|--|
| | Objective A 5. | From 🗏 Example 2, what can we conclude is the reciprocal | |
| | | of any nonzero number <i>n</i> ? > | |
| | Objective B 6. | From Ħ Example 6, what number has no reciprocal? 🜔 | |
| | Objective C 7. | In 🖪 Example 8, why can't we divide out common factors | |
| | | once we've written the mixed numbers as fractions? > | |
| | Objective D 8. | In 🖪 Example 9, what phrase tells us that we have a | |
| see Video 2.5 🍥 | | division problem? > | |
| | | | |

2.5 Exercise Set MyLab Math 🔘

Objective A *Find the reciprocal of each number. See Examples 1 through 4.*

| •1. $\frac{4}{7}$ | 2. $\frac{9}{10}$ | 3. $\frac{1}{11}$ | 4. $\frac{1}{20}$ |
|--------------------------|--------------------------|--------------------------|--------------------------|
| 5. 15 | 6. 13 | 7. $\frac{12}{7}$ | 8. $\frac{10}{3}$ |

Objective B *Divide. Write each answer in simplest form. See Examples 5 through 9.*

| 9. $\frac{2}{3} \div \frac{5}{6}$ | 10. $\frac{5}{8} \div \frac{2}{3}$ | 11. $\frac{8}{9} \div \frac{1}{2}$ | 12. $\frac{10}{11} \div \frac{4}{5}$ |
|---|--|--|---|
| 13. $\frac{3}{7} \div \frac{5}{6}$ | 14. $\frac{16}{27} \div \frac{8}{15}$ | 15. $\frac{3}{5} \div \frac{4}{5}$ | 16. $\frac{11}{16} \div \frac{13}{16}$ |
| • 17. $\frac{1}{10} \div \frac{10}{1}$ | 18. $\frac{3}{13} \div \frac{13}{3}$ | 19. $\frac{7}{9} \div \frac{7}{3}$ | 20. $\frac{6}{11} \div \frac{6}{5}$ |
| 21. $\frac{5}{8} \div \frac{3}{8}$ | 22. $\frac{7}{8} \div \frac{5}{6}$ | 23. $\frac{7}{45} \div \frac{4}{25}$ | 24. $\frac{14}{52} \div \frac{1}{13}$ |
| 25. $\frac{2}{37} \div \frac{1}{7}$ | 26. $\frac{1}{3} \div \frac{6}{17}$ | 27. $\frac{3}{25} \div \frac{27}{40}$ | 28. $\frac{6}{15} \div \frac{7}{10}$ |
| 29. $\frac{11}{12} \div \frac{11}{12}$ | 30. $\frac{7}{13} \div \frac{7}{13}$ | •31. $\frac{8}{13} \div 0$ | 32. $0 \div \frac{4}{11}$ |
| 33. $0 \div \frac{7}{8}$ | 34. $\frac{2}{3} \div 0$ | 35. $\frac{25}{126} \div \frac{125}{441}$ | 36. $\frac{65}{495} \div \frac{26}{231}$ |

| Objective C Divide. Wr | rite each answer in simplest form | n. See Examples 10 through 12. | |
|---|---|---|--|
| • 37. $\frac{2}{3} \div 4$ | 38. $\frac{5}{6} \div 10$ | 39. $8 \div \frac{3}{5}$ | 40. $7 \div \frac{2}{11}$ |
| 41. $2\frac{1}{2} \div \frac{1}{2}$ | 42. $4\frac{2}{3} \div \frac{2}{5}$ | 43. $\frac{5}{12} \div 2\frac{1}{3}$ | 44. $\frac{4}{15} \div 2\frac{1}{2}$ |
| • 45. $3\frac{3}{7} \div 3\frac{1}{3}$ | 46. $2\frac{5}{6} \div 4\frac{6}{7}$ | 47. $1\frac{4}{9} \div 2\frac{5}{6}$ | 48. $3\frac{1}{10} \div 2\frac{1}{5}$ |
| 49. $0 \div 15\frac{4}{7}$ | 50. $\frac{33}{50} \div 1$ | 51. $1 \div \frac{13}{17}$ | 52. $0 \div 7\frac{9}{10}$ |
| 53. $1 \div \frac{18}{35}$ | 54. $\frac{17}{75} \div 1$ | 55. $10\frac{5}{9} \div 16\frac{2}{3}$ | 56. $20\frac{5}{6} \div 137\frac{1}{2}$ |

Objectives B C Mixed Practice Divide. Write each answer in simplest form. See Examples 5 through 12. **60.** $\frac{9}{20} \div \frac{2}{9}$ **58.** $\frac{4}{15} \div \frac{8}{3}$ **57.** $\frac{6}{15} \div \frac{12}{5}$ **59.** $\frac{11}{20} \div \frac{3}{11}$ **61.** $12 \div \frac{1}{8}$ **62.** $9 \div \frac{1}{6}$ **63.** $\frac{3}{7} \div \frac{4}{7}$ **64.** $\frac{3}{8} \div \frac{5}{8}$ **65.** $2\frac{3}{8} \div 0$ **66.** $20\frac{1}{5} \div 0$ **67.** $\frac{11}{85} \div \frac{7}{5}$ **68.** $\frac{13}{84} \div \frac{3}{16}$ **69.** $4\frac{5}{11} \div 1\frac{2}{5}$ **70.** $8\frac{2}{7} \div 3\frac{1}{7}$ **71.** $\frac{27}{100} \div \frac{3}{20}$ **72.** $\frac{25}{128} \div \frac{5}{32}$

Objective D Solve. For Exercises 73 and 74, the solutions have been started for you. Write each answer in simplest form. See Example 13.

73. A heart attack patient in rehabilitation walked on a treadmill $12\frac{3}{4}$ miles over 4 days. How many miles is this per day?

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- 2. TRANSLATE into an equation. (Fill in the blanks.)

| miles
per day | is | total
miles | divided
by | number
of days |
|------------------|--------------|----------------|---------------|-------------------|
| \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| miles
per day | = | | ÷ | |

Finish with:

- 3. SOLVE and
- **4.** INTERPRET
- 75. A patient is to take $3\frac{1}{3}$ tablespoons of medicine per day in 4 equally divided doses. How much medicine is to be taken in each dose?
 - **77.** The record for rainfall during a 24-hour period in Alaska is $15\frac{1}{5}$ inches. This record was set in Angoon, Alaska, in October 1982. How much rain fell per hour on average? (*Source:* National Climatic Data Center)
 - **79.** In March 2017, the average price of aluminum was $87\frac{1}{20}$ ¢ per pound. During that time, a family received 1741¢ for aluminum cans that they sold

for recycling at a scrap metal center. Assuming that they received the average price, how many pounds of aluminum cans did they recycle? (*Source:* London Metal Exchange) **74.** A local restaurant is selling hamburgers from a booth on Memorial Day. A total of $27\frac{3}{4}$ pounds of ham-

burger have been ordered. How many quarter-pound hamburgers can this make?

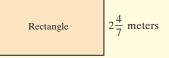
Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blanks.)

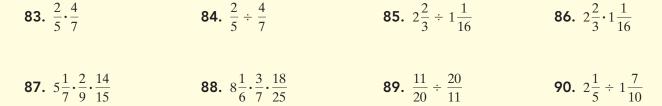
| how many
quarter-pound
hamburgers | is | total
pounds of
hamburger | divided
by | a
quarter-
pound |
|---|--------------|---------------------------------|---------------|------------------------|
| \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| how many
quarter-pound
hamburgers | = | | ÷ | |
| Finish with:
3. SOLVE a
4. INTERP | | | | |

- **76.** If there are $13\frac{1}{3}$ grams of fat in 4 ounces of lean hamburger meat, how many grams of fat are in an ounce?
- **78.** An order for 125 custom-made candle stands was placed with Mr. Levi, the manager of Just For You, Inc. The worker assigned to the job can produce $2\frac{3}{5}$ candle stands per hour. Using this worker, how many work hours will be required to complete the order?
- **80.** Yoko's Fine Jewelry paid \$450 for a $\frac{3}{4}$ -carat gem. At this price, what is the cost of one carat?

 \triangle 81. The area of the rectangle below is 12 square meters. \triangle 82. The perimeter of the square below is $23\frac{1}{2}$ feet. If its width is $2\frac{4}{7}$ meters, find its length. Find the length of each side.



Mixed Practice (Sections 2.4 and 2.5) Perform the indicated operation.



Review

Perform each indicated operation. See Sections 1.3 and 1.4.

| 91. | 27 9 | 2. 811 | 93. 968 |
|--------------|-------------|---------------|----------------|
| , | 76 | 42 | -772 |
| + | 98 | + 69 | |
| | | | |
| | | | |
| 94. 8 | 82 9 | 2000 | 96. 500 |
| 7 | 73 | - 431 | <u> </u> |

Concept Extensions

A student asked you to find the error in the work below. Find the error and correct it. See the Concept Check in this section.

97.
$$20\frac{2}{3} \div 10\frac{1}{2} = 2\frac{1}{3}$$
 98. $6\frac{1}{4} \div \frac{1}{2} = 3\frac{1}{8}$

Choose the best estimate for each quotient.

99.
$$20\frac{1}{4} \div \frac{5}{6}$$

a. 5 **b.** $5\frac{1}{8}$ **c.** 20 **d.** 10

100. $\frac{11}{12} \div 16\frac{1}{5}$
a. $\frac{1}{16}$ **b.** 4 **c.** 8 **d.** 16



101.
$$12\frac{2}{13} \div 3\frac{7}{8}$$

a. 4 **b.** 9 **c.** 36 **d.** 3

103. $\frac{42}{25} \cdot \frac{125}{36} \div \frac{7}{6}$

- **105.** In 2016, the FedEx Express air fleet includes approximately 100 Boeing MD planes. These Boeing MDs make up $\frac{2}{13}$ of the FedEx Express fleet. How many aircraft make up the entire FedEx Express air fleet? (*Source:* FedEx Corporation)
- **107.** In your own words, describe how to find the reciprocal of a number.

102. $10\frac{1}{4} \div 2\frac{1}{16}$ **a.** 8 **b.** 5 **c.** 20 **d.** 12

104.
$$\left(\frac{8}{13} \cdot \frac{39}{16} \cdot \frac{8}{9}\right)^2 \div \frac{1}{2}$$

106. One-third of all native flowering plant species in the United States are at risk of becoming extinct. That translates into 5144 at-risk flowering plant species. Based on this data, how many flowering plant species are native to the United States overall? (*Source:* The Nature Conservancy)

(*Hint:* How many $\frac{1}{3}$ s are in 5144?)

108. In your own words, describe how to divide fractions.

Chapter 2 Group Activity

Blood and Blood Donation (Sections 2.1, 2.2 and 2.3)

Blood is the workhorse of the body. It carries to the body's tissues everything they need, from nutrients to antibodies to heat. Blood also carries away waste products like carbon dioxide. Blood contains three types of cells—red blood cells, white blood cells, and platelets—suspended in clear, watery fluid called plasma. Blood is $\frac{11}{20}$ plasma, and plasma itself is $\frac{9}{10}$ water. In the average healthy adult human, blood accounts for $\frac{1}{11}$ of a person's body weight. Roughly every 2 seconds someone in the United States needs blood. Although only $\frac{1}{20}$ of eligible donors

donate blood, the American Red Cross is still able to collect nearly 6 million volunteer donations of blood each year. This volume makes Red Cross Biomedical Services the largest blood supplier for blood transfusions in the United States.

Group Activity

Contact your local Red Cross Blood Service office. Find out how many people donated blood in your area in the past two months. Ask whether it is possible to get a breakdown of the blood donations by blood type. (For more on blood types, see Exercises 75 through 78 in Section 2.3.)

- 1. Research the population of the area served by your local Red Cross Blood Service office. Write the fraction of the local population who gave blood in the past two months.
- **2.** Use the breakdown by blood type to write the fraction of donors giving each type of blood.

Chapter 2 Vocabulary Check

Fill in each blank with one of the words or phrases listed below.

0

simplest form

numerator

| equivalent |
|-------------------|
| improper fraction |
| proper fraction |
| cross products |
| |

- 1. Two numbers are ______ of each other if their product is 1.
- **2.** A(n) ______ is a natural number greater than 1 that is not prime.
- 3. Fractions that represent the same portion of a whole are called ______ fractions.
- **4.** A(n) ______ is a fraction whose numerator is greater than or equal to its denominator.
- _____ is a natural number that has **5.** A(n) ____ exactly two different factors, 1 and itself.
- 6. A fraction is in ______ when the numerator and the denominator have no factors in common other than 1.
- 7. A(n) ______ is one whose numerator is less than its denominator.

undefined prime factorization denominator

- 8. A(n) _____ contains a whole number part and a fraction part.
- 9. In the fraction $\frac{7}{9}$, the 7 is called the _____ and the 9 is called the _____
- _____ of a number is the factorization 10. The _ in which all the factors are prime numbers.
- **11.** The fraction $\frac{3}{0}$ is _____.
- **12.** The fraction $\frac{0}{5} =$ _____.

13. In
$$\frac{a}{b} = \frac{c}{d}$$
, $a \cdot d$ and $b \cdot c$ are called

Helpful Hint • Are you preparing for your test? To help, don't forget to take these:

- Chapter 2 Getting Ready for the Test on page 169
- Chapter 2 Test on page 170

Then check all of your answers at the back of this text. For further review, the step-by-step video solutions to any of these exercises are located in MyLab Math.

Chapter Highlights

| Definitions and Concepts | Examples | | |
|---|--|--|--|
| Section 2.1 Introduction to Fractions and Mixed Numbers | | | |
| A fraction is of the form:
$\frac{\text{numerator}}{\text{denominator}} \text{number of parts being considered}$ $\frac{\text{number of equal parts in the whole}}{\text{number of equal parts in the whole}}$ | Write a fraction to represent the shaded part of the figure.
$\frac{3}{8} \leftarrow \text{number of parts shaded}$ | | |
| A fraction is called a proper fraction if its numerator is less than its denominator. | $\frac{1}{3}, \frac{2}{5}, \frac{7}{8}, \frac{100}{101}$ | | |
| A fraction is called an improper fraction if its numerator is greater than or equal to its denominator. | $\frac{5}{4}, \frac{2}{2}, \frac{9}{7}, \frac{101}{100}$ | | |
| A mixed number contains a whole number and a fraction. | $1\frac{1}{2}, 5\frac{7}{8}, 25\frac{9}{10}$ (continued) | | |

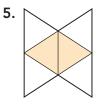
| Definitions and Concepts | Examples |
|---|--|
| Section 2.1 Introduction to Fraction | ons and Mixed Numbers (continued) |
| To Write a Mixed Number as an Improper Fraction1. Multiply the denominator of the fraction by the whole number. | $(5)^{+} \frac{5}{7} = \frac{7 \cdot 5 + 2}{7} = \frac{35 + 2}{7} = \frac{37}{7}$ |
| Add the numerator of the fraction to the product from step 1. Write the sum from step 2 as the numerator of the | |
| improper fraction over the original denominator.
To Write an Improper Fraction as a Mixed Number | $\frac{17}{3} = 5\frac{2}{3}$ |
| or a Whole Number | 3 3 |
| Divide the denominator into the numerator. The whole number part of the mixed number is the quotient. The fraction is the remainder over the original denominator. | $3)\overline{17}$ $-\underline{15}$ 2 |
| quotient remainder
original denominator | |
| Section 2.2 Factors a | nd Prime Factorization |
| A prime number is a natural number that has exactly two different factors, 1 and itself. | 2, 3, 5, 7, 11, 13, 17, |
| A composite number is any natural number other than 1 that is not prime. | 4, 6, 8, 9, 10, 12, 14, 15, 16, |
| The prime factorization of a number is the factorization
in which all the factors are prime numbers. | Write the prime factorization of 60.
$60 = 6 \cdot 10$ |
| | $= 2 \cdot 3 \cdot 2 \cdot 5$ or $2^2 \cdot 3 \cdot 5$ |
| Section 2.3 Simple | st Form of a Fraction |
| Fractions that represent the same portion of a whole are called equivalent fractions. | $\frac{3}{4} = \frac{12}{16}$ |
| A fraction is in simplest form or lowest terms when the numerator and the denominator have no common factors other than 1. | The fraction $\frac{2}{3}$ is in simplest form. |
| To write a fraction in simplest form, write the prime
factorizations of the numerator and the denominator and
then divide both by all common factors. | Write in simplest form: $\frac{30}{36}$
$\frac{30}{36} = \frac{2 \cdot 3 \cdot 5}{2 \cdot 2 \cdot 3 \cdot 3} = \frac{2}{2} \cdot \frac{3}{3} \cdot \frac{5}{2 \cdot 3} = 1 \cdot 1 \cdot \frac{5}{6} = \frac{5}{6}$
or $\frac{30}{36} = \frac{\frac{1}{2} \cdot \frac{1}{3} \cdot 5}{\frac{2}{1} \cdot 2 \cdot 3 \cdot 3} = \frac{5}{6}$ |
| | |

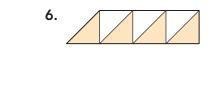
| Definitions and Concepts | Examples |
|--|---|
| • | m of a Fraction (<i>continued</i>) |
| Two fractions are equivalent ${\operatorname{if}}$ | Determine whether $\frac{7}{8}$ and $\frac{21}{24}$ are equivalent. |
| Method 1. They simplify to the same fraction. | Method 1. $\frac{7}{8}$ is in simplest form; $\frac{21}{24} = \frac{\frac{1}{3} \cdot 7}{\frac{3}{1} \cdot 8} = \frac{7}{8}$ |
| | Since both simplify to $\frac{7}{8}$, then $\frac{7}{8} = \frac{21}{24}$. |
| Method 2. Their cross products are equal. | Method 2. $24 \cdot 7$ $= 168$ $\frac{7}{8} = \frac{21}{24}$ $8 \cdot 21$ $= 168$ |
| | Since $168 = 168, \frac{7}{8} = \frac{21}{24}$ |
| Section 2.4 Multiplying Fr | actions and Mixed Numbers |
| To multiply two fractions, multiply the numerators and multiply the denominators. | Multiply.
$\frac{7}{8} \cdot \frac{3}{5} = \frac{7 \cdot 3}{8 \cdot 5} = \frac{21}{40}$ |
| To multiply with mixed numbers or whole numbers, first
write any mixed or whole numbers as fractions and then
multiply as usual. | $\frac{3}{4} \cdot \frac{1}{6} = \frac{3 \cdot 1}{4 \cdot 6} = \frac{3 \cdot 1}{4 \cdot 3 \cdot 2} = \frac{1}{8}$ $2\frac{1}{3} \cdot \frac{1}{9} = \frac{7}{3} \cdot \frac{1}{9} = \frac{7 \cdot 1}{3 \cdot 9} = \frac{7}{27}$ |
| Section 2.5 Dividing Frac | ctions and Mixed Numbers |
| To find the reciprocal of a fraction, interchange its numerator and denominator. | The reciprocal of $\frac{3}{5}$ is $\frac{5}{3}$. |
| To divide two fractions, multiply the first fraction by the reciprocal of the second fraction. | Divide.
$\frac{3}{10} \div \frac{7}{9} = \frac{3}{10} \cdot \frac{9}{7} = \frac{3 \cdot 9}{10 \cdot 7} = \frac{27}{70}$ |
| To divide with mixed numbers or whole numbers, first
write any mixed or whole numbers as fractions and then
divide as usual. | $2\frac{5}{8} \div 3\frac{7}{16} = \frac{21}{8} \div \frac{55}{16} = \frac{21}{8} \cdot \frac{16}{55} = \frac{21 \cdot 16}{8 \cdot 55}$ $= \frac{21 \cdot 2 \cdot \frac{1}{8}}{8 \cdot 55} = \frac{42}{55}$ |
| | 1 |

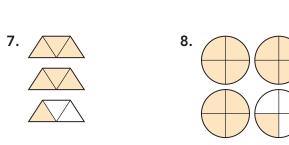
Chapter 2 Review

- (2.1) Determine whether each number is an improper fraction, a proper fraction, or a mixed number.
- **1.** $\frac{11}{23}$ **2.** $\frac{9}{8}$ **3.** $\frac{1}{2}$ **4.** $2\frac{1}{4}$

Write a fraction to represent the shaded area.







- **9.** A basketball player made 11 free throws out of 12 during a game. What fraction of free throws did the player make?
- **10.** A new car lot contained 23 blue cars out of a total of 131 cars.
 - **a.** How many cars on the lot are not blue?
 - **b.** What fraction of cars on the lot are not blue?

Write each improper fraction as a mixed number or a whole number.

| 11. $\frac{15}{4}$ | 12. $\frac{275}{6}$ | 13. $\frac{39}{13}$ | 14. $\frac{60}{12}$ |
|---------------------------|----------------------------|----------------------------|----------------------------|
|---------------------------|----------------------------|----------------------------|----------------------------|

Write each mixed number as an improper fraction.

15. $1\frac{1}{5}$ **16.** $1\frac{1}{21}$ **17.** $2\frac{8}{9}$ **18.** $3\frac{11}{12}$

(2.2) Identify each number as prime or composite.

| 19. 51 | | 20. 17 | | | |
|---|----------------------------|----------------------------|----------------------------|--|--|
| List all factors of each numb | er. | | | | |
| 21. 42 | | 22. 20 | | | |
| Find the prime factorization | of each number. | | | | |
| 23. 68 | 24. 90 | 25. 785 | 26. 255 | | |
| (2.3) Write each fraction in simplest form. | | | | | |
| 27. $\frac{12}{28}$ | 28. $\frac{15}{27}$ | 29. $\frac{25}{75}$ | 30. $\frac{36}{72}$ | | |
| 31. $\frac{29}{32}$ | 32. $\frac{18}{23}$ | 33. $\frac{48}{6}$ | 34. $\frac{54}{9}$ | | |

Solve.

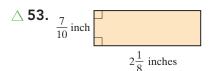
35. There are 12 inches in a foot. What fractional part of a foot does 8 inches represent?



Determine whether each pair of fractions is equivalent.

- **37.** $\frac{10}{34}$ and $\frac{4}{14}$ **38.** $\frac{30}{50}$ and $\frac{9}{15}$
- (2.4) Multiply. Write each answer in simplest form. Estimate where noted.
- **39.** $\frac{3}{5} \cdot \frac{1}{2}$ **40.** $\frac{6}{7} \cdot \frac{5}{12}$ **41.** $\frac{24}{5} \cdot \frac{15}{8}$ **42.** $\frac{27}{21} \cdot \frac{7}{18}$
 43. $5 \cdot \frac{7}{8}$ **44.** $6 \cdot \frac{5}{12}$ **45.** $\frac{39}{3} \cdot \frac{7}{13} \cdot \frac{5}{21}$ **46.** $\frac{42}{5} \cdot \frac{15}{6} \cdot \frac{7}{9}$
 47. $1\frac{5}{8} \cdot 3\frac{1}{5}$ **48.** $3\frac{6}{11} \cdot 1\frac{7}{13}$ **49.** $\frac{3}{4} \cdot 8 \cdot 4\frac{1}{8}$ **50.** $2\frac{1}{9} \cdot 3 \cdot \frac{1}{38}$

 Exact:
 Exact:
 Exact:
 Exact:
 Estimate:
- **51.** There are $7\frac{1}{3}$ grams of fat in each ounce of hamburger. How many grams of fat are in a 5-ounce hamburger patty?
- **52.** An art teacher needs 45 pieces of PVC piping for an art project. If each piece needs to be $\frac{3}{4}$ inch long, find the total length of piping she needs.



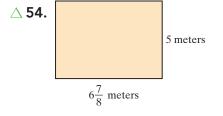
55. 7

59. $\frac{3}{4} \div \frac{3}{8}$

(2.5) Find the reciprocal of each number.

Divide. Write each answer in simplest form.

Find the area of each rectangle.





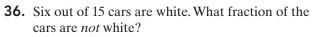
61. $\frac{5}{3} \div 2$

64. $5\frac{1}{2} \div 2\frac{1}{11}$

60. $\frac{21}{4} \div \frac{7}{5}$

62. $5 \div \frac{15}{8}$ **63.** $6\frac{3}{4} \div 1\frac{2}{7}$

56. $\frac{1}{8}$



65. A truck traveled 341 miles on $15\frac{1}{2}$ gallons of gas. How many miles might we expect the truck to travel on 1 gallon of gas?

66. Herman Heltznutt walks 5 days a week for a total distance of $5\frac{1}{4}$ miles per week. If he walks the same distance each day, find the distance he walks each day.

Mixed Review

Determine whether each number is an improper fraction, a proper fraction, or a mixed number.

67. $\frac{0}{3}$ **68.** $\frac{12}{12}$ **69.** $5\frac{6}{7}$ **70.** $\frac{13}{9}$

Write each improper fraction as a mixed number or a whole number. Write each mixed number as an improper fraction.

71. $\frac{125}{4}$ **72.** $\frac{54}{9}$ **73.** $5\frac{10}{17}$ **74.** $7\frac{5}{6}$

Identify each number as prime or composite.

75. 27 **76.** 23

Find the prime factorization of each number.

77. 180 **78.** 98

Write each fraction in simplest form.

79. $\frac{45}{50}$ **80.** $\frac{30}{42}$ **81.** $\frac{140}{150}$ **82.** $\frac{84}{140}$

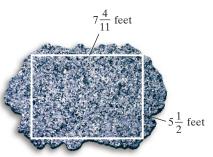
Multiply or divide as indicated. Write each answer in simplest form. Estimate where noted.

- 83. $\frac{7}{8} \cdot \frac{2}{3}$ 84. $\frac{6}{15} \cdot \frac{5}{8}$ 85. $\frac{18}{5} \div \frac{2}{5}$ 86. $\frac{9}{2} \div \frac{1}{3}$

 87. $4\frac{1}{6} \cdot 2\frac{2}{5}$ 88. $5\frac{2}{3} \cdot 2\frac{1}{4}$ 89. $\frac{7}{2} \div 1\frac{1}{2}$ 90. $1\frac{3}{5} \div \frac{1}{4}$

 Exact:
 Exact:
 Exact:
 Exact:
 Exact:
 Exact:

 Estimate:
 Exact:
 Exact:
 Exact:
 Exact:
 Exact:
- \triangle **91.** A slab of natural granite is purchased and a rectangle with length $7\frac{4}{11}$ feet and width $5\frac{1}{2}$ feet is cut from it. Find the area of the rectangle.



92. An area of Mississippi received $23\frac{1}{2}$ inches of rain in $30\frac{1}{2}$ hours. How many inches per 1 hour is this?

Chapter 2 Getting Ready for the Test

MULTIPLE CHOICE All of the exercises are Multiple Choice. Choose the correct letter.

For Exercises 1 through 4, simplify each fraction. Choices are below.

| A. 0 | B. 1 | C. undefined | D. 5 |
|---------------------------|---|--------------------------|---------------------------|
| • 1. $\frac{5}{5}$ | 2. $\frac{5}{0}$ | 03. $\frac{0}{5}$ | 04. $\frac{5}{1}$ |
| For Exercises 5 through | ugh 7, choose the correct letter. | | |
| 5 . Which of the b | elow is <i>not</i> a factorization of 20? | | |
| A. 2·10 | B. 2·2·5 | C. 10 • 10 | D. 20 • 1 |
| 6. Which of the fo | ollowing is <i>not</i> a prime number? | | |
| A. 14 | B. 13 | C. 2 | D. 7 |
| 7 . Which fraction | is <i>not</i> equivalent to $\frac{6}{5}$? | | |
| | | a . 1 | . 12 |
| A. $\frac{18}{15}$ | B. $\frac{30}{20}$ | C. $1\frac{1}{5}$ | D. $\frac{10}{10}$ |

For Exercises 8 through 11, two fractions and an answer are given. Choose the operation performed on the two fractions that lead to the given answers.

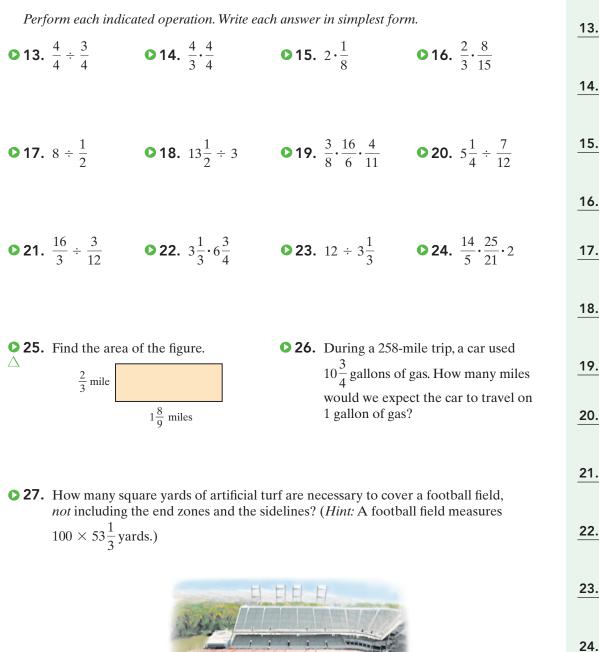
A. multiplication

B. division

• 9. $\frac{2}{5}$ and $\frac{1}{5}$; answer: $\frac{2}{1}$ or 2 **• 8.** $\frac{2}{5}$ and $\frac{1}{5}$; answer: $\frac{2}{25}$

• 10.
$$\frac{6}{11}$$
 and $\frac{6}{7}$ answer: $\frac{7}{11}$ • 11. $\frac{6}{11}$ and $\frac{6}{7}$ answer: $\frac{36}{77}$

Chapter 2 For additional practice go to your study plan Test MyLab Math or You Tube in MyLab Math. Answers Write a fraction to represent the shaded area. **0**1. €2. 1. Write each mixed number as an improper fraction. **3.** $7\frac{2}{3}$ **4.** $3\frac{6}{11}$ 2. 3. Write each improper fraction as a mixed number or a whole number. 4. **5.** $\frac{23}{5}$ **06.** $\frac{75}{4}$ 5. 6. Write each fraction in simplest form. **7.** $\frac{24}{210}$ **8.** $\frac{42}{70}$ 7. 8. Determine whether these fractions are equivalent. 9. • 9. $\frac{5}{7}$ and $\frac{8}{11}$ **•10.** $\frac{6}{27}$ and $\frac{14}{63}$ 10. 11. Find the prime factorization of each number. **12.** 495 **11.** 84 12.



○ 28. Prior to an oil spill, the stock in an oil company sold for \$120 per share. As a result of the liability that the company incurred from the spill, the price per share fell to $\frac{3}{4}$ of the price before the spill. What did the stock sell for after the spill?

100 yards

 $53\frac{1}{2}$ yard

14. 15. 16. 17. 18. 19. 20. 21. 22.

25.

26.

27.

28.

| Chapters 1–2 | Cumulative Review |
|------------------|---|
| Answers | Find the place value of the digit 3 in the whole number 396,418. Write 2036 in words. |
| 1. | 3. Write the number, eight hundred five, in standard form.
4. Add: $7 + 6 + 10 + 3 + 5$ |
| _2 | 5. Add: 34,285 + 149,761 6. Find the average of 56, 18, and 43. |
| 3. | \triangle 7. Find the perimeter of the polygon shown.
^{3 inches} 1 inch
^{3 inches} |
| 4. | 4 inches 3 inches |
| 5. | 9. In 2015, a total of 9,879,465 trucks were sold in the United States. In 2016, total trucks sales in the United States had increased by 712,397. Find the total number of trucks |
| 6. | sold in the United States in 2016. (Source: Alliance of Automobile Manufacturers) |
| 7. | 10. Find $\sqrt{25}$. 11. Subtract: 7826 - 505 12. Find 8 ² . Check by adding. |
| 8 | 13. In the following graph, each bar represents a country and the height of each bar represents the number of threatened mammal species identified in that country. |
| 9. | Number of Threatened Mammal Species, 2016 |
| 10. | So 160 So 140 120 120 95 92 |
| <u>11.</u> | 180
160
140
120
100
95
92
82
74
72
60
40
40
40
20 |
| 12. | 20
0
Indonesia Mexico India Brazil China Malaysia
Country |
| <u>13. a.</u> | <i>Source:</i> International Union for Conservation of Nature a. Which country shown has the greatest number of threatened mammal species? b. Find the total number of threatened mammal species for Malaysia, China, and |
| <u>b.</u>
172 | Indonesia. |

Cumulative Review

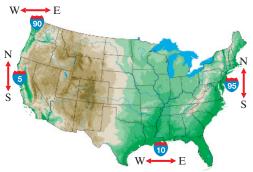
| | Cumulative Review | 175 |
|---|--|---------------|
| 14. Find 205 ÷ 8. | 15. Round 568 to the nearest ten. | 14. |
| | | 15. |
| 16. Round 2366 to the nearest hundred. | 17. Round each number to the nearest hundred to find an estimated difference. | 16. |
| | 4725
- <u>2879</u> | 17. |
| | | 18. |
| 18. Round each number to the nearest ten to find an estimated sum. | 19. Multiply.
a. 6×1 b. 0(18) | 19. a. |
| 38 + 43 + 126 + 92 | c. 1 • 45 d. (75)(0) | b. |
| 20. Simplify: $30 \div 3 \cdot 2$ | 21. Rewrite each using the distributive | C |
| | property.
a. $3(4+5)$ b. $10(6+8)$
c. $2(7+3)$ | d |
| | | 20. |
| 22. Multiply: 12×15 | 23. Find each quotient. Check by multiplying. | 21. a. |
| | a. 9) $\overline{0}$ b. 0 ÷ 12 | b. |
| | c. $\frac{0}{5}$ d. $\frac{3}{0}$ | c |
| 24. Find the area. | 25. Divide and check: 1872 ÷ 9 | 22. |
| 7 miles Rectangle | | <u>23. a.</u> |
| 22 miles | | b. |
| 26. Subtract: 5000 – 986 | 27. As part of a promotion, an executive | C |
| | receives 238 cards, each good for one free song download. If she wants to | d. |
| | share them evenly with 19 friends, how
many download cards will each friend
receive? How many will be left over? | <u>24.</u> |
| | receive: now many will be left over: | <u>25.</u> |
| 28. Find the product of 9 and 7. | | <u>26.</u> |
| 29. A gardener bought enough plants to t | fill a rectangular garden with length 30 feet and | 27. |
| width 20 feet. Because of shading pro
the width of the garden to 15 feet. If t | blems from a nearby tree, the gardener changed
he area is to remain the same, what is the new | 28. |
| length of the garden? | | <u>29.</u> |

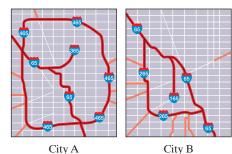
173

30.

| 31. | Write using exponential notation. | |
|---------------|--|---|
| 32. | 31. 7·7·7 | 32. 7 • 7 • 7 • 7 |
| 33. | | |
| 34. | 33. 3·3·3·3·17·17·17 | 34. 2·2·3·3·3·3 |
| 35. | | |
| 36. | 35. Simplify: $2 \cdot 4 - 3 \div 3$ | 36. Simplify: $8 \cdot \sqrt{100} - 4^2 \cdot 5$ |
| 37. | 37. Write a fraction to represent the | 38. Write the prime factorization of 156. |
| 38. | shaded part of the figure. | co. Write the prime factorization of 150. |
| <u>39. a.</u> | | |
| b. | | |
| 40. | 39. Write each as an improper fraction.
a. $4\frac{2}{9}$ b. $1\frac{8}{11}$ | 40. Write $7\frac{4}{5}$ as an improper fraction. |
| 41. | 7 11 | |
| 42. | 41. Find all the factors of 20. | 42. Determine whether $\frac{8}{20}$ and $\frac{14}{35}$ are |
| 43. | | equivalent. 20 35 |
| 44. | | |
| 45. | 43. Write in simplest form: $\frac{42}{66}$ | 44. Write in simplest form: $\frac{70}{105}$ |
| 46. | | |
| 47. | 45. Multiply: $3\frac{1}{3} \cdot \frac{7}{8}$ | 46. Multiply: $\frac{2}{3} \cdot 4$ |
| 48 | 47. Find the reciprocal of $\frac{1}{3}$. | 48. Find the reciprocal of 9. |
| 49. | - 3 | × |
| 50. | 5 3 | 1 3 |
| | 49. Divide and simplify: $\frac{5}{16} \div \frac{3}{4}$ | 50. Divide: $1\frac{1}{10} \div 5\frac{3}{5}$ |

Adding and Subtracting Fractions





<u>One- and Two-digit Numbers:</u> Odd numbers run northsouth (or south-north), while even numbers run eastwest (or west-east).

<u>Three-digit numbers:</u> Three digit numbers are usually given to loops or partial loops that serve a parent interstate. The last two digits are the same as the parent interstate, and the first digit (hundred's place) is usually even if it connects to the parent interstate at both ends or usually odd if it does not connect at both ends.

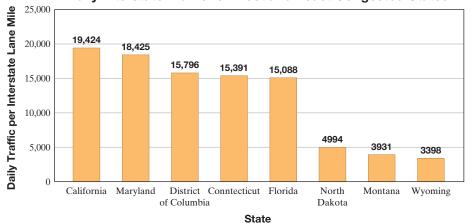
How Old Is the U.S. Interstate System?

he year 2016 was the 60th anniversary of the Interstate Highway System. Signed into law by President Dwight Eisenhower, the Federal-Aid Highway Act of 1956 set into motion the building of the giant network of interstate highways that links our country together.

The interstate highway system is now over 47,000 miles long. The federal government paid 90% of the cost to build approved highways, but each state owns and operates the highways within its borders.

Above, we show how most interstate highways are numbered. Below, the graph shows the most and least congested states, including the District of Columbia.

In Section 3.1, Exercises 53 and 55, we will explore some facts of highways in the United States.





Source: TRIP; tripnet.org

3

Having learned what fractions are and how to multiply and divide them in Chapter 2, we are ready to continue our study of fractions. In this chapter, we learn how to add and subtract fractions and mixed numbers. We then conclude this chapter with solving problems using fractions.

Sections

- **3.1** Adding and Subtracting Like Fractions
- 3.2 Least Common Multiple
- **3.3** Adding and Subtracting Unlike Fractions

Integrated Review— Operations on Fractions and Mixed Numbers

- 3.4 Adding and Subtracting Mixed Numbers
- **3.5** Order, Exponents, and the Order of Operations
- **3.6** Fractions and Problem Solving

Check Your Progress

Vocabulary Check Chapter Highlights Chapter Review Getting Ready for the Test Chapter Test Cumulative Review

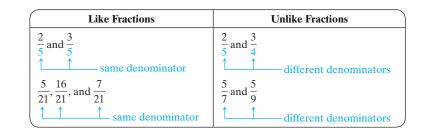
3.1 Adding and Subtracting Like Fractions

Objectives



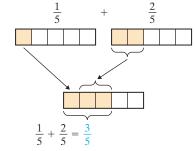
- B Subtract Like Fractions. 🜔
- C Solve Problems by Adding or Subtracting Like Fractions.

Fractions with the same denominator are called **like fractions.** Fractions that have different denominators are called **unlike fractions.**



Objective A Adding Like Fractions 🕑

To see how we add like fractions (fractions with the same denominator), study the figures below:



Adding Like Fractions (Fractions with the Same Denominator)

To add like fractions, add the numerators and write the sum over the common denominator.

If a, b, and c represent nonzero whole numbers, we have

 $\frac{a}{c} + \frac{b}{c} = \frac{a+b}{c}$

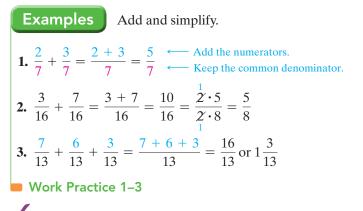
For example,

 $\frac{1}{4} + \frac{2}{4} = \frac{1+2}{4} = \frac{3}{4} \quad \longleftarrow \quad \text{Add the numerators.}$ Keep the denominator.

Helpful Hint

As usual, don't forget to write all answers in simplest form.

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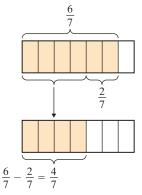


Concept Check Find and correct the error in the following:

 $\frac{1}{5} + \frac{1}{5} = \frac{2}{10}$

Objective **B** Subtracting Like Fractions

To see how we subtract like fractions (fractions with the same denominator), study the following figure:



Subtracting Like Fractions (Fractions with the Same Denominator)

To subtract like fractions, subtract the numerators and write the difference over the common denominator.

If *a*, *b*, and *c* represent nonzero whole numbers, then

 $\frac{a}{c} - \frac{b}{c} = \frac{a-b}{c}$

For example,

 $\frac{4}{5} - \frac{2}{5} = \frac{4-2}{5} = \frac{2}{5} \xleftarrow{} \text{Subtract the numerators.}}$ $\xleftarrow{} \text{Keep the denominator.}$

Examples Subtract and simplify.

4. $\frac{8}{9} - \frac{1}{9} = \frac{8-1}{9} = \frac{7}{9} \xleftarrow{}$ Subtract the numerators. 5. $\frac{7}{8} - \frac{5}{8} = \frac{7-5}{8} = \frac{2}{8} = \frac{\frac{1}{2}}{\frac{2}{1} \cdot 4} = \frac{1}{4}$

Work Practice 4–5

Practice 1–3 Add and simplify. 1. $\frac{5}{9} + \frac{2}{9}$ 2. $\frac{5}{8} + \frac{1}{8}$ 3. $\frac{10}{11} + \frac{1}{11} + \frac{7}{11}$

Practice 4–5

Subtract and simplify.

4.
$$\frac{7}{12} - \frac{2}{12}$$
 5. $\frac{9}{10} - \frac{1}{10}$
Answers
1. $\frac{7}{9}$ 2. $\frac{3}{4}$ 3. $\frac{18}{11}$ or $1\frac{7}{11}$
4. $\frac{5}{12}$ 5. $\frac{4}{5}$

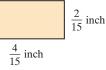
Concept Check Answer We don't add denominators together; correct solution: $\frac{1}{5} + \frac{1}{5} = \frac{2}{5}$.

Objective C Solving Problems by Adding or Subtracting Like Fractions

Many real-life problems involve finding the perimeters of square or rectangular areas such as pastures, swimming pools, and so on. We can use our knowledge of adding fractions to find perimeters.

Example <u>6</u>

Find the perimeter of the rectangle.



Solution: Recall that perimeter means distance around and that opposite sides of a rectangle are the same length.

$$\frac{\frac{4}{15} \text{ inch}}{\frac{2}{15} \text{ inch}} \frac{\frac{2}{15} \text{ inch}}{\frac{4}{15} \text{ inch}}$$
Perimeter = $\frac{2}{15} + \frac{4}{15} + \frac{2}{15} + \frac{4}{15} = \frac{2+4+2+4}{15}$

$$= \frac{12}{15} = \frac{\frac{3}{2} \cdot 4}{\frac{3}{15} \cdot 5} = \frac{4}{5}$$

The perimeter of the rectangle is $\frac{4}{5}$ inch.

Work Practice 6

We can combine our skills in adding and subtracting fractions with our four problem-solving steps from Chapter 1 to solve many kinds of real-life problems.

Example 7 Total Amount of an Ingredient in a Recipe

A recipe calls for $\frac{1}{3}$ of a cup of honey at the beginning and $\frac{2}{3}$ of a cup of honey later. How much total honey is needed to make the recipe?

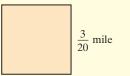


Solution:

1. UNDERSTAND the problem. To do so, read and reread the problem. Since we are finding total honey, we add.

Practice 6

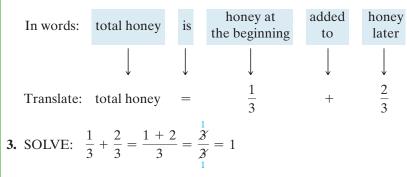
Find the perimeter of the square.



If a piano student practices the piano $\frac{3}{8}$ of an hour in the morning and $\frac{1}{8}$ of an hour in the evening, how long did she practice that day?

Answers 6. $\frac{3}{5}$ mi 7. $\frac{1}{2}$ hr

2. TRANSLATE.

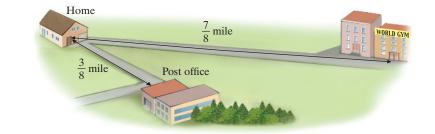


4. INTERPRET. *Check* your work. *State* your conclusion: The total honey needed for the recipe is 1 cup.

Work Practice 7

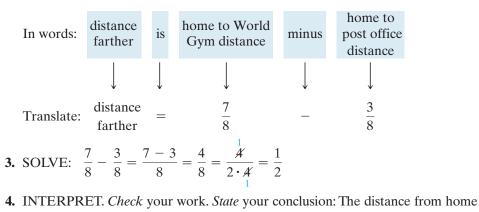
Example 8 Calculating Distance

The distance from home to the World Gym is $\frac{7}{8}$ of a mile and from home to the post office is $\frac{3}{8}$ of a mile. How much farther is it from home to the World Gym than from home to the post office?



Solution:

- **1.** UNDERSTAND. Read and reread the problem. The phrase "How much farther" tells us to subtract distances.
- 2. TRANSLATE.



to the World Gym is $\frac{1}{2}$ mile farther than from home to the post office.

```
Work Practice 8
```

Practice 8

A jogger ran $\frac{13}{4}$ miles on Monday and $\frac{7}{4}$ miles on Wednesday. How much farther

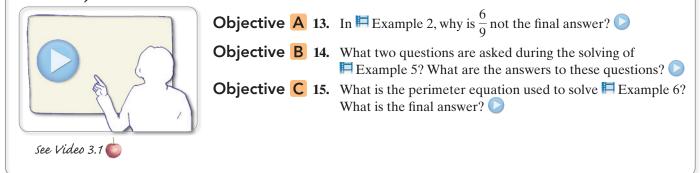
did he run on Monday than on Wednesday?

Answer 8. $\frac{3}{2}$ or $1\frac{1}{2}$ mi

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Not all choices will be used. $\frac{a-c}{b}$ $\frac{a+c}{b}$ perimeter like equivalent unlike 1. The fractions $\frac{9}{11}$ and $\frac{13}{11}$ are called ______ fractions while $\frac{3}{4}$ and $\frac{1}{3}$ are called ______ fractions. $2. \ \frac{a}{b} + \frac{c}{b} =$ _____. **3.** $\frac{a}{b} - \frac{c}{b} =$ 4. The distance around a figure is called its _ State whether the fractions in each list are like or unlike fractions. 6. $\frac{2}{2}, \frac{4}{2}$ 8. $\frac{8}{11}, \frac{2}{11}$ 5. $\frac{7}{8}, \frac{7}{10}$ 7. $\frac{9}{10}, \frac{1}{10}$ 9. $\frac{2}{31}, \frac{30}{31}, \frac{19}{31}$ **10.** $\frac{3}{10}, \frac{3}{11}, \frac{3}{13}$ **11.** $\frac{5}{12}, \frac{7}{12}, \frac{12}{11}$ **12.** $\frac{1}{5}, \frac{2}{5}, \frac{4}{5}$

Martin-Gay Interactive Videos Watch the section lecture video and answer the following questions.



3.1 Exercise Set MyLab Math 🕗

Objective A Add and simplify. See Examples 1 through 3.

0 1. $\frac{1}{7} + \frac{2}{7}$ **2.** $\frac{9}{17} + \frac{2}{17}$ **3.** $\frac{1}{10} + \frac{1}{10}$ **4.** $\frac{1}{4} + \frac{1}{4}$
0 5. $\frac{2}{9} + \frac{4}{9}$ **6.** $\frac{3}{10} + \frac{2}{10}$ **7.** $\frac{6}{20} + \frac{1}{20}$ **8.** $\frac{2}{8} + \frac{3}{8}$
9. $\frac{3}{14} + \frac{4}{14}$ **10.** $\frac{5}{24} + \frac{7}{24}$ **11.** $\frac{10}{11} + \frac{3}{11}$ **12.** $\frac{13}{17} + \frac{9}{17}$

• 13.
$$\frac{4}{13} + \frac{2}{13} + \frac{1}{13}$$
 14. $\frac{5}{11} + \frac{1}{11} + \frac{2}{11}$ **15.** $\frac{7}{18} + \frac{3}{18} + \frac{2}{18}$ **16.** $\frac{7}{15} + \frac{4}{15} + \frac{1}{15}$

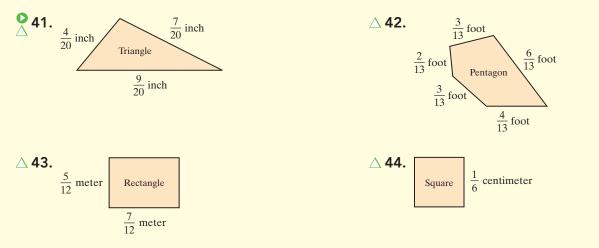
Objective B Subtract and simplify. See Examples 4 and 5.

0 17. $\frac{10}{11} - \frac{4}{11}$ **18.** $\frac{9}{13} - \frac{5}{13}$ **19.** $\frac{4}{5} - \frac{1}{5}$ **20.** $\frac{7}{8} - \frac{4}{8}$ **21.** $\frac{7}{4} - \frac{3}{4}$ **22.** $\frac{18}{5} - \frac{3}{5}$ **0 23.** $\frac{7}{8} - \frac{1}{8}$ **24.** $\frac{5}{6} - \frac{1}{6}$ **25.** $\frac{25}{12} - \frac{15}{12}$ **26.** $\frac{30}{20} - \frac{15}{20}$ **27.** $\frac{11}{10} - \frac{3}{10}$ **28.** $\frac{14}{15} - \frac{4}{15}$ **29.** $\frac{86}{90} - \frac{85}{90}$ **30.** $\frac{74}{80} - \frac{73}{80}$ **31.** $\frac{27}{33} - \frac{8}{33}$ **32.** $\frac{37}{45} - \frac{18}{45}$

Objectives A B Mixed Practice *Perform the indicated operation. See Examples 1 through 5.*

| 33. $\frac{8}{21} + \frac{5}{21}$ | 34. $\frac{7}{37} + \frac{9}{37}$ | 35. $\frac{99}{100} - \frac{9}{100}$ | 36. $\frac{85}{200} - \frac{15}{200}$ |
|--|--|---|---|
| 37. $\frac{13}{28} - \frac{13}{28}$ | 38. $\frac{15}{26} - \frac{15}{26}$ | 39. $\frac{3}{16} + \frac{7}{16} + \frac{2}{16}$ | 40. $\frac{5}{18} + \frac{1}{18} + \frac{6}{18}$ |

Objective C Find the perimeter of each figure. (Hint: Recall that perimeter means distance around.) See Example 6.



Solve. For Exercises 45 and 46, the solutions have been started for you. Write each answer in simplest form. See Examples 7 and 8.

45. A railroad inspector must inspect $\frac{19}{20}$ of a mile of railroad track. If she has already inspected $\frac{5}{20}$ of a mile, road track. If she has already inspected $\frac{5}{20}$ of a mile, **46.** Scott Davis has run $\frac{11}{8}$ miles already and plans to complete $\frac{16}{8}$ miles. To do this, how much farther how much more does she need to inspect?

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blanks.)

| distance
left to
inspect | is | distance
needed to
inspect | minus | distance
already
inspected |
|--------------------------------|--------------|----------------------------------|--------------|----------------------------------|
| \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| distance
left to
inspect | = | | _ | |

Finish with:

- 3. SOLVE. and
- 4. INTERPRET.
- 47. Emil Vasquez, a bodybuilder, worked out $\frac{7}{8}$ of an hour one morning before school and $\frac{5}{8}$ of an hour that evening. How long did he work out that day?

Full-Time College Students' Average

must he run?

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blanks.)

| distance
left to
run | is | distance
planned
to run | minus | distance
already
run |
|----------------------------|--------------|-------------------------------|--------------|----------------------------|
| \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| distance
left to
run | = | | _ | |

Finish with:

- 3. SOLVE. and
- 4. INTERPRET.
- **48.** A recipe for Heavenly Hash cake calls for $\frac{3}{4}$ cup of sugar and later $\frac{1}{4}$ cup of sugar. How much sugar is needed to make the recipe?

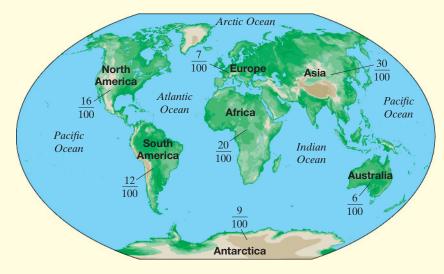
The circle graph below shows full-time U.S. college students' time use on an average weekday. Use this graph for *Exercises* 49–52. *Write your answers in simplest form.*



- **49.** What fraction of a full-time U.S. college student's weekday is spent on eating and drinking, grooming, and sleeping?
- **50.** What fraction of a full-time U.S. college student's weekday is spent on working and related activities and educational activities?
- **51.** How much greater is the fractional part of a college student's weekday that is spent on leisure and sports than on traveling?
- **52.** How much greater is the fractional part of a college student's weekday that is spent on sleeping than on educational activities?

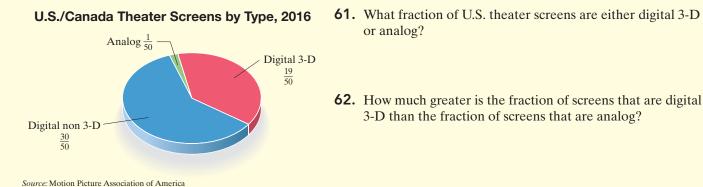
- **53.** Road congestion can be caused by a variety of problems. Approximately $\frac{3}{20}$ of all road congestion in the United States is caused by weather, while $\frac{5}{20}$ of all road congestion in the United States is caused by incidents such as accidents and disabled vehicles. What fraction of U.S. road congestion is caused by weather or incidents? (*Source:* Federal Highway Administration)
- **55.** As of March 2017, the fraction of states in the United States with maximum interstate highway speed limits up to and including 70 mph was $\frac{34}{50}$. The fraction of states with 70 mph speed limits was $\frac{21}{50}$. What fraction of states had speed limits that were less than 70 mph? (*Source:* Insurance Institute for Highway Safety)
- 54. In 2015, $\frac{5}{20}$ of Target's total retail sales were in the health, beauty, and household essentials category, and $\frac{4}{20}$ of Target's total retail sales were in the food and pet supplies category. What fraction of Target's total retail sales were made in these two categories combined? (*Source:* Target Corporation)
- **56.** When people take aspirin, $\frac{31}{50}$ of the time it is used to treat some type of pain. Approximately $\frac{7}{50}$ of all aspirin use is for treating headaches. What fraction of aspirin use is for treating pain other than headaches? (*Source:* Bayer Market Research)

The map of the world below shows the fraction of the world's surface land area taken up by each continent. In other words, the continent of Africa makes up $\frac{20}{100}$ of the land in the world. Use this map for Exercises 57 through 60. Write your answers in simplest form.



- **57.** Find the fractional part of the world's land area within the continents of North America and South America.
- **59.** How much greater is the fractional part of the continent of Antarctica than the fractional part of the continent of Europe?
- **58.** Find the fractional part of the world's land area within the continents of Asia and Africa.
- **60.** How much greater is the fractional part of the continent of Asia than the continent of Australia?

The theater industry is shifting away from analog movie screens toward digital and digital 3-D movie screens. Use the circle graph to answer Exercises 61 and 62. Write your answers in simplest form.



Review

Write the prime factorization of each number. See Section 2.2.

| 63. 10 | 64. 12 | 65. 8 |
|---------------|---------------|---------------|
| 66. 20 | 67. 55 | 68. 28 |

Concept Extensions

Perform each indicated operation.

- **69.** $\frac{3}{8} + \frac{7}{8} \frac{5}{8}$ **70.** $\frac{12}{20} \frac{1}{20} \frac{3}{20}$
- **71.** $\frac{4}{11} + \frac{5}{11} \frac{3}{11} + \frac{2}{11}$ **72.** $\frac{9}{12} + \frac{1}{12} \frac{3}{12} \frac{5}{12}$

Find and correct the error. See the Concept Check in this section.

- **73.** $\frac{2}{7} + \frac{9}{7} = \frac{11}{14}$ **74.** $\frac{3}{4} \frac{1}{4} = \frac{2}{8} = \frac{1}{4}$
- **75.** In your own words, explain how to add like fractions.
- . 4 4 8 4
- **76.** In your own words, explain how to subtract like fractions.

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Solve. For Exercises 77 through 80, write each answer in simplest form.

- **77.** Use the circle graph for Exercises 49 through 52 and find the sum of all the daily time-use fractions. Explain your answer.
 - **79.** Mike Cannon jogged $\frac{3}{8}$ of a mile from home and then rested. Then he continued jogging farther from home for another $\frac{3}{8}$ of a mile until he discovered his watch had fallen off. He walked back along the same path for $\frac{4}{8}$ of a mile until he found his watch. Find how far he was from his home.
- **78.** Use the map of the world for Exercises 57 through 60 and find the sum of all the continents' fractions. Explain your answer.
 - **80.** A trim carpenter needs the following lengths of boards: $\frac{5}{4}$ feet, $\frac{15}{4}$ feet, $\frac{9}{4}$ feet, and $\frac{13}{4}$ feet. Is a 10-foot board long enough for the carpenter to cut these lengths? If not, how much more length is needed?

3.2 Least Common Multiple

Objective A Finding the Least Common Multiple Using Multiples

A multiple of a number is the product of that number and a natural number. For example, multiples of 5 are

| 0 | $5 \cdot 1$ | $5 \cdot 2$ | <u>5·3</u> | $5 \cdot 4$ | $5 \cdot 5$ | $5 \cdot 6$ | <u>5 · 7</u> | $5 \cdot 8$ | |
|---|--------------|-------------|--------------|-------------|--------------|-------------|--------------|-------------|--|
| | \downarrow | ↓ | \downarrow | ↓ | \downarrow | Ļ | Ļ | V | |
| | 5, | 10, | 15, | 20, | 25, | 30, | 35, | 40,. | |

Multiples of 4 are

4, 8, 12, 16, **20**, 24, 28, 32, 36, **40**, 44, ...

Common multiples of both 4 and 5 are numbers that are found in both lists above. If we study the lists of multiples and extend them we have

Common multiples of 4 and 5: 20, 40, 60, 80, ...

We call the smallest number in the list of common multiples the **least common multiple (LCM).** From the list of common multiples of 4 and 5, we see that the LCM of 4 and 5 is 20.

Example 1 Find the LCM of 6 and 8.

Solution: Multiples of 6: 6, 12, 18, 24, 30, 36, 42, 48,...

Multiples of 8: 8, 16, 24, 32, 40, 48, 56,...

The common multiples are 24, 48,.... The least common multiple (LCM) is 24.

Work Practice 1

Objectives

- A Find the Least Common Multiple (LCM) Using Multiples.
- **B** Find the LCM Using Prime Factorization.
- C Write Equivalent Fractions.

Practice 1 Find the LCM of 15 and 50.

Answer 1. 150 Listing all the multiples of every number in a list can be cumbersome and tedious. We can condense the procedure shown in Example 1 with the following steps:

Method 1: Finding the LCM of a List of Numbers Using Multiples of the Largest Number

Step 1: Write the multiples of the largest number (starting with the number itself) until a multiple common to all numbers in the list is found.

Step 2: The multiple found in Step 1 is the LCM.

Example 2 Find the LCM of 9 and 12.

Solution: We write the multiples of 12 until we find a number that is also a multiple of 9.

 $12 \cdot 1 = 12$ Not a multiple of 9. $12 \cdot 2 = 24$ Not a multiple of 9. $12 \cdot 3 = 36$ A multiple of 9.

The LCM of 9 and 12 is 36.

Work Practice 2



Find the LCM of 7 and 14.

Find the LCM of 12 and 20.

Objective B Finding the LCM Using Prime Factorization 🕞

Solution: We write the multiples of 14 until we find one that is also a multiple of 7.

Solution: We write the multiples of 20 until we find one that is also a multiple

Method 1 for finding multiples works fine for smaller numbers, but may get tedious

for larger numbers. A second method that uses prime factorization may be easier to

For example, to find the LCM of 270 and 84, let's look at the prime factorization

 $14 \cdot 1 = 14$ A multiple of 7.

 $20 \cdot 1 = 20$ Not a multiple of 12. $20 \cdot 2 = 40$ Not a multiple of 12. $20 \cdot 3 = 60$ A multiple of 12.

The LCM of 7 and 14 is 14.

The LCM of 12 and 20 is 60.

Work Practice 4

Work Practice 3

Example 4

of 12.

Practice 4

Practice 3

Find the LCM of 25 and 30.

Answers **2.** 40 **3.** 16 **4.** 150 $270 = 2 \cdot 3 \cdot 3 \cdot 3 \cdot 5$ $84 = 2 \cdot 2 \cdot 3 \cdot 7$

use for larger numbers.

of each.

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Practice 2

Find the LCM of 8 and 10.

Find the LCM of 8 and 16.

Recall that the LCM must be a multiple of both 270 and 84. Thus, to build the LCM, we will circle the greatest number of factors for each different prime number. The LCM is the product of the circled factors.

Prime Number Factors



 $LCM = 2 \cdot 2 \cdot 3 \cdot 3 \cdot 3 \cdot 5 \cdot 7 = 3780$

The number 3780 is the smallest number that both 270 and 84 divide into evenly. This Method 2 is summarized below:

Method 2: Finding the LCM of a List of Numbers Using Prime Factorization

- Step 1: Write the prime factorization of each number.
- **Step 2:** For each different prime factor in step 1, circle the greatest number of times that factor occurs in any one factorization.
- **Step 3:** The LCM is the product of the circled factors.

Example 5 Find the LCM of 72 and 60.

Solution: First we write the prime factorization of each number.

 $72 = 2 \cdot 2 \cdot 2 \cdot 3 \cdot 3$ $60 = 2 \cdot 2 \cdot 3 \cdot 5$

For the prime factors shown, we circle the greatest number of prime factors found in either factorization.

 $72 = \underbrace{2 \cdot 2 \cdot 2}_{60} \cdot \underbrace{3 \cdot 3}_{60}$ $60 = 2 \cdot 2 \cdot 3 \cdot \underbrace{5}_{60}$

The LCM is the product of the circled factors.

 $LCM = 2 \cdot 2 \cdot 2 \cdot 3 \cdot 3 \cdot 5 = 360$

The LCM is 360.

Work Practice 5

Helpful Hint

If you prefer working with exponents, circle the factor with the greatest exponent. Example 5:

 $72 = (2^3 \cdot (3^2))$ $60 = 2^2 \cdot 3 \cdot (5)$ $LCD = 2^3 \cdot 3^2 \cdot 5 = 360$

Practice 5 Find the LCM of 40 and 108.

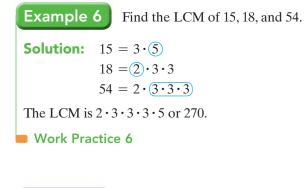
Answer 5. 1080

Helpful Hint

If the number of factors of a prime number are equal, circle either one, but not both. For example,

$$12 = (2 \cdot 2) \cdot (3)$$

$$15 = 3 \cdot (5)$$
- Circle either 3 but not both.
The LCM is $2 \cdot 2 \cdot 3 \cdot 5 = 60$.



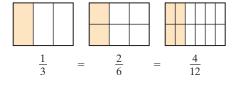
Practice 7 Find the LCM of 7 and 21.

Find the LCM of 20, 24, and 45.

Example 7 Find the LCM of 11 and 33. **Solution:** 11 = 11 $33 = 3 \cdot 11$ The LCM is $3 \cdot 11$ or 33. Work Practice 7

Objective C Writing Equivalent Fractions 🕗

To add or subtract unlike fractions in the next section, we first write equivalent fractions with the LCM as the denominator. Recall from Section 2.3 that fractions that represent the same portion of a whole are called "equivalent fractions."



To write $\frac{1}{3}$ as an equivalent fraction with a denominator of 12, we multiply by 1 in the form of $\frac{4}{4}$.

$$\frac{1}{3} = \frac{1}{3} \cdot \underbrace{1}_{4} = \frac{1}{3} \cdot \frac{4}{4} = \frac{1 \cdot 4}{3 \cdot 4} = \frac{4}{12}$$

$$\frac{4}{4} = 1$$
So $\frac{1}{3} = \frac{4}{12}$.

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Practice 6

To write an equivalent fraction,

$$\frac{a}{b} = \frac{a}{b} \cdot \frac{c}{c} = \frac{a \cdot c}{b \cdot c}$$

where *a*, *b*, and *c* are nonzero numbers.

Concept Check Which of the following is not equivalent to $\frac{3}{4}$? **a.** $\frac{6}{8}$ **b.** $\frac{18}{24}$ **c.** $\frac{9}{14}$ **d.** $\frac{30}{40}$ **Example 8** Write an equivalent fraction with the indicated denominator. $\frac{3}{4} = \frac{3}{20}$ **Solution:** In the denominators, since $4 \cdot 5 = 20$, we will multiply by 1 in the form of $\frac{5}{5}$. $\frac{3}{4} = \frac{3}{4} \cdot \frac{5}{5} = \frac{3 \cdot 5}{4 \cdot 5} = \frac{15}{20}$ Thus, $\frac{3}{4} = \frac{15}{20}$. **Work Practice 8**

Helpful Hint

To check Example 8, write $\frac{15}{20}$ in simplest form.

 $\frac{15}{20} = \frac{3 \cdot 5}{4 \cdot 5} = \frac{3}{4}$, the original fraction.

If the original fraction is in lowest terms, we can check our work by writing the new equivalent fraction in simplest form. This form should be the original fraction.

Concept Check True or false? When the fraction $\frac{2}{9}$ is rewritten as an equivalent fraction with 27 as the denominator, the result is $\frac{2}{27}$.

Example 9 Write an equivalent fraction with the indicated denominator.

 $\frac{1}{2} = \frac{1}{24}$ **Solution:** Since $2 \cdot 12 = 24$, we multiply by 1 in the form of $\frac{12}{12}$ $\frac{1}{2} = \frac{1}{2} \cdot \frac{12}{12} = \frac{1 \cdot 12}{2 \cdot 12} = \frac{12}{24}$ Thus, $\frac{1}{2} = \frac{12}{24}$.

Practice 8

Write an equivalent fraction with the indicated denominator: $\frac{7}{8} = \frac{1}{56}$

Practice 9

```
Write an equivalent fraction
with the indicated denominator.
\frac{3}{5} = \frac{1}{15}
Answers
8. \frac{49}{56} 9. \frac{9}{15}
\checkmark Concept Check Answers
```

false; the correct result would be $\frac{6}{27}$

190

Example 10



Write an equivalent fraction with the given denominator.

 $4 = \frac{1}{6}$

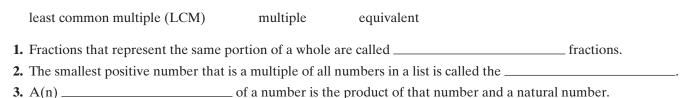


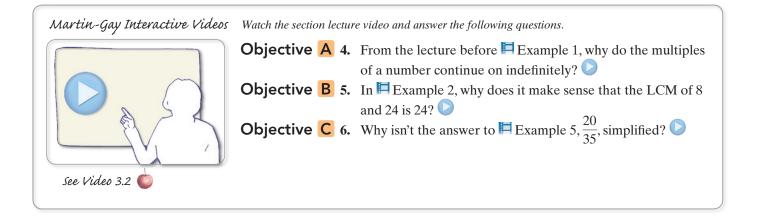
 $3 = \frac{1}{7}$ Solution: Recall that $3 = \frac{3}{1}$. Since $1 \cdot 7 = 7$, multiply by 1 in the form of $\frac{7}{7}$. $\frac{3}{1} = \frac{3}{1} \cdot \frac{7}{7} = \frac{3 \cdot 7}{1 \cdot 7} = \frac{21}{7}$ Work Practice 10

Write an equivalent fraction with the given denominator.

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank.





| 3.2 | Exercise | Set | MyLab Math | |
|-----|----------|-----|------------|--|
|-----|----------|-----|------------|--|

Objective A B Mixed Practice Find the LCM of each list of numbers. See Examples 1 through 7.

| 1. 3,4 | 2. 4,6 | 3. 9,15 | 4. 15, 20 | 5. 12, 18 | 6. 10, 15 |
|----------------------|----------------------|------------------|--------------------|---------------------|----------------------|
| 7. 24, 36 | 8. 42,70 | 9. 18, 21 | 10. 24, 45 | 11. 15,25 | 12. 21,14 |
| ▶ 13. 8,24 | 14. 15,90 | 15. 6,7 | 16. 13,8 | 17. 8, 6, 27 | 18. 6, 25, 10 |
| 19. 25, 15, 6 | 20. 4, 14, 20 | 21. 34,68 | 22. 25, 175 | 23. 84, 294 | 24. 48, 54 |

| 25. 30, 36, 50 | 26. 21, 28, 42 | 27. 50, 72, 120 | 28. 70, 98, 100 |
|------------------------|------------------------|-------------------------|--------------------------|
| 29. 11, 33, 121 | 30. 10, 15, 100 | 31. 4, 6, 10, 15 | 32. 25, 3, 15, 10 |

Objective C Write each fraction or whole number as an equivalent fraction with the given denominator. See Examples 8 through 10.

| 33. $\frac{4}{7} = \frac{1}{35}$ | 34. $\frac{3}{5} = \frac{1}{20}$ | 35. $\frac{2}{3} = \frac{1}{21}$ | 36. $6 = \frac{10}{10}$ | 37. $5 = \frac{1}{3}$ |
|--|--|---|--|--|
| 38. $\frac{9}{10} = \frac{1}{70}$ | 39. $\frac{1}{2} = \frac{1}{30}$ | 40. $\frac{1}{3} = \frac{1}{30}$ | 41. $\frac{10}{7} = \frac{1}{21}$ | 42. $\frac{5}{3} = \frac{1}{21}$ |
| 43. $\frac{3}{4} = \frac{1}{28}$ | 44. $\frac{4}{5} = \frac{45}{45}$ | 45. $\frac{2}{3} = \frac{1}{45}$ | 46. $\frac{2}{3} = \frac{1}{75}$ | • 47. $\frac{4}{9} = \frac{1}{81}$ |
| 48. $\frac{5}{11} = \frac{1}{88}$ | 49. $\frac{15}{13} = \frac{15}{78}$ | 50. $\frac{9}{7} = \frac{1}{84}$ | 51. $\frac{14}{17} = \frac{14}{68}$ | 52. $\frac{19}{21} = \frac{126}{126}$ |

A non-store retailer is a mail-order business that sells goods via catalogs, toll-free telephone numbers, or online media. The table shows the fraction of non-store retailers' goods that were sold online in 2016 by type of goods. Use this table to answer Exercises 53 through 56.

| Type of Goods Sold by
Non-Store Retailers | Fraction of Goods
That Were Sold
Online | Equivalent Fraction
with a Denominator
of 100 |
|--|---|---|
| Books and magazines | $\frac{43}{50}$ | |
| Clothing and accessories | $\frac{4}{5}$ | |
| Computer hardware | $\frac{29}{50}$ | |
| Computer software | $\frac{17}{25}$ | |
| Drugs, health and beauty aids | $\frac{3}{25}$ | |
| Electronics and appliances | $\frac{21}{25}$ | |
| Food, beer, and wine | $\frac{17}{25}$ | |
| Home furnishings | $\frac{81}{100}$ | |
| Music and videos | $\frac{9}{10}$ | |
| Office equipment and supplies | $\frac{79}{100}$ | |
| Sporting goods | $\frac{37}{50}$ | |
| Toys, hobbies, and games | $\frac{39}{50}$ | |
| (Source: U.S. Census Bureau) | | , |

- **53.** Complete the table by writing each fraction as an equivalent fraction with a denominator of 100.
- **54.** Which of these types of goods has the largest fraction sold online?
- **55.** Which of these types of goods has the smallest fraction sold online?
- **56.** Which of the types of goods has **more than** $\frac{4}{5}$ of the goods sold online? (*Hint:* Write $\frac{4}{5}$ as an equivalent fraction with a denominator of 100.)



Review

Add or subtract as indicated. See Section 3.1.

| 57. $\frac{7}{10} - \frac{2}{10}$ | 58. $\frac{8}{13} - \frac{3}{13}$ | 59. $\frac{1}{5} + \frac{1}{5}$ | 60. $\frac{1}{8} + \frac{3}{8}$ |
|--|--|--|---|
| 61. $\frac{23}{18} - \frac{15}{18}$ | 62. $\frac{36}{30} - \frac{12}{30}$ | 63. $\frac{2}{9} + \frac{1}{9} + \frac{6}{9}$ | 64. $\frac{2}{12} + \frac{7}{12} + \frac{3}{12}$ |

Concept Extensions

Write each fraction as an equivalent fraction with the indicated denominator.

65.
$$\frac{37}{165} = \frac{3630}{3630}$$

67. In your own words, explain how to find the LCM of two numbers.

66.
$$\frac{108}{215} = \frac{108}{4085}$$

- **68.** In your own words, explain how to write a fraction as an equivalent fraction with a given denominator.
- Solve. See the Concept Checks in this section. 69. Which of the following are equivalent to $\frac{2}{3}$?

| a. | $\frac{10}{15}$ | b. | $\frac{40}{60}$ |
|----|-----------------|----|-------------------|
| c. | $\frac{16}{20}$ | d. | $\frac{200}{300}$ |

70. True or False? When the fraction $\frac{7}{12}$ is rewritten with a denominator of 48, the result is $\frac{11}{48}$. If false, give the correct fraction.

3.3 Adding and Subtracting Unlike Fractions

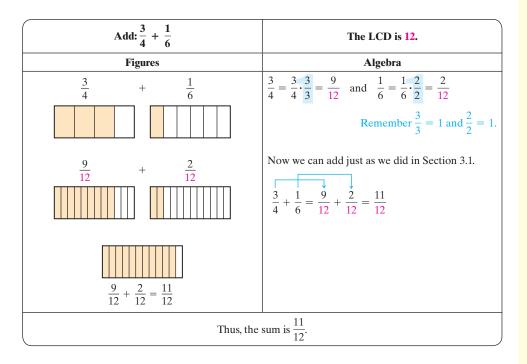
Objectives

- A Add Unlike Fractions. >
- B Subtract Unlike Fractions. 🜔
- C Solve Problems by Adding or Subtracting Unlike Fractions.

Objective 🗛 Adding Unlike Fractions 🕗

In this section we add and subtract fractions with unlike denominators. To add or subtract these unlike fractions, we first write the fractions as equivalent fractions with a common denominator and then add or subtract the like fractions. The common denominator that we use is the least common multiple (LCM) of the denominators. This denominator is called the **least common denominator (LCD)**.

To begin, let's add the unlike fractions $\frac{3}{4} + \frac{1}{6}$. The LCM of denominators 4 and 6 is 12. This means that the number 12 is also the LCD. So we write each fraction as an equivalent fraction with a denominator of 12, then add as usual. This addition process is shown next and also illustrated by figures.



Adding or Subtracting Unlike Fractions

- **Step 1:** Find the LCM of the denominators of the fractions. This number is the least common denominator (LCD).
- **Step 2:** Write each fraction as an equivalent fraction whose denominator is the LCD.
- Step 3: Add or subtract the like fractions.
- **Step 4:** Write the sum or difference in simplest form.

Example 1 Add:
$$\frac{2}{5} + \frac{4}{15}$$

Solution:

Step 1: The LCM of the denominators 5 and 15 is 15. Thus, the LCD is 15. In later examples, we shall simply say, for example, that the LCD of 5 and 15 is 15.

Step 3: $\frac{2}{5} + \frac{4}{15} = \frac{6}{15} + \frac{4}{15} = \frac{10}{15}$ Step 4: Write in simplest form. $\frac{10}{15} = \frac{2 \cdot \frac{5}{3}}{3 \cdot \frac{5}{3}} = \frac{2}{3}$

Work Practice 1

Practice 1

Add:
$$\frac{1}{6} + \frac{5}{18}$$

Answer 1. $\frac{4}{9}$ Chapter 3 | Adding and Subtracting Fractions

Example 3 Add: $\frac{2}{3} + \frac{1}{7}$

 $\frac{2}{3} + \frac{1}{7} = \frac{2}{3} \cdot \frac{7}{7} + \frac{1}{7} \cdot \frac{3}{3}$

 $=\frac{14}{21}+\frac{3}{21}$

Solution: The LCD of 3 and 7 is 21.

 $=\frac{17}{21}$ Simplest form.

Example 2 Add: $\frac{11}{15} + \frac{3}{10}$ Solution: **Step 1:** The LCD of 15 and 10 is 30. Step 2: $\frac{11}{15} = \frac{11}{15} \cdot \frac{2}{2} = \frac{22}{30}$ $\frac{3}{10} = \frac{3}{10} \cdot \frac{3}{3} = \frac{9}{30}$ Step 3: $\frac{11}{15} + \frac{3}{10} = \frac{22}{20} + \frac{9}{20} = \frac{31}{20}$ **Step 4:** $\frac{31}{30}$ is in simplest form. We can write the sum as $\frac{31}{30}$ or $1\frac{1}{30}$. Work Practice 2

Practice 3

Add: $\frac{2}{5} + \frac{4}{9}$

Practice 4 Add: $\frac{1}{2} + \frac{4}{5} + \frac{7}{10}$

Answers **2.** $\frac{19}{18}$ or $1\frac{1}{18}$ **3.** $\frac{38}{45}$ **4.** 2

Concept Check Answer When adding unlike fractions, we don't add the denominators. Correct solution:

| 2 | 4 | 22 | 36 | 58 |
|-----------------|-------------------|----------|------------------|----|
| $\frac{-}{9}$ + | $\frac{11}{11} =$ | ${99}$ + | $\frac{1}{99} =$ | 99 |

Example 4 Add: $\frac{1}{2} + \frac{2}{3} + \frac{5}{6}$ **Solution:** The LCD of 2, 3, and 6 is 6. $\frac{1}{2} + \frac{2}{3} + \frac{5}{6} = \frac{1}{2} \cdot \frac{3}{3} + \frac{2}{3} \cdot \frac{2}{2} + \frac{5}{6}$ $=\frac{3}{6}+\frac{4}{6}+\frac{5}{6}$ $=\frac{12}{6}=2$

Work Practice 4

Work Practice 3

Concept Check Find and correct the error in the following:

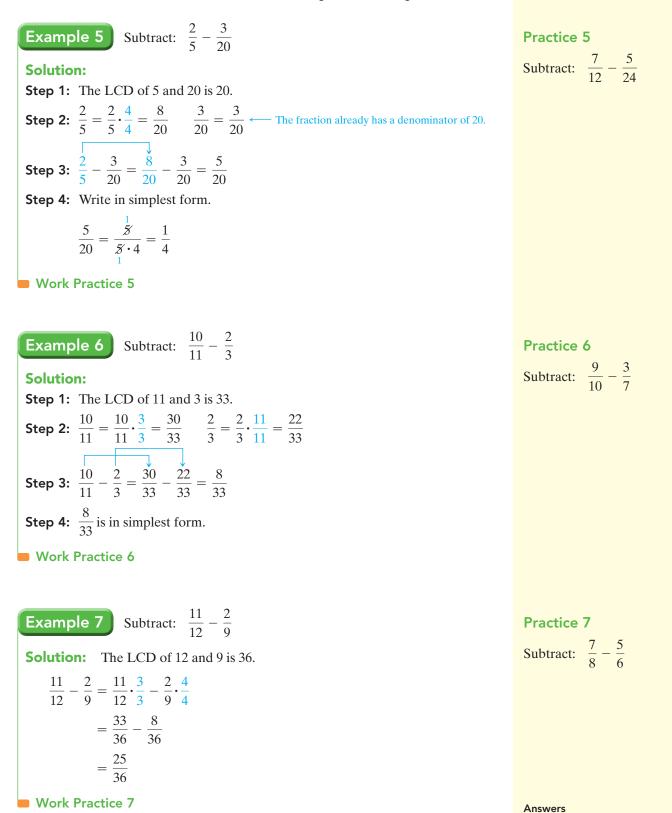
$$\frac{2}{9} + \frac{4}{11} = \frac{6}{20} = \frac{3}{10}$$

Objective **B** Subtracting Unlike Fractions

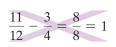
As indicated in the box on page 193, we follow the same steps when subtracting unlike fractions as when adding them.

Practice 2

Add: $\frac{5}{6} + \frac{2}{9}$

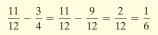


Concept Check Find and correct the error in the following:



5. $\frac{3}{8}$ 6. $\frac{33}{70}$ 7. $\frac{1}{24}$

Concept Check Answer When subtracting unlike fractions, we don't subtract the denominators. Correct solution:

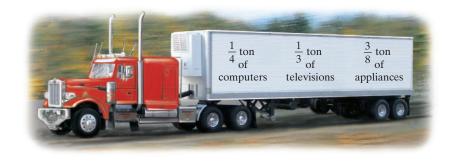


Objective C Solving Problems by Adding or Subtracting Unlike Fractions

Very often, real-world problems involve adding or subtracting unlike fractions.

Example 8 Finding Total Weight

A freight truck has $\frac{1}{4}$ ton of computers, $\frac{1}{3}$ ton of televisions, and $\frac{3}{8}$ ton of small appliances. Find the total weight of its load.



Solution:

- **1.** UNDERSTAND. Read and reread the problem. The phrase "total weight" tells us to add.
- 2. TRANSLATE.

| In w | ords: | total
weight | is | weight of computers | plus | weight of televisions | plus | weight of appliances |
|-------|--------|-----------------|--------------|---------------------|--------------|-----------------------|--------------|----------------------|
| | | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| Trar | slate: | total
weight | = | $\frac{1}{4}$ | + | $\frac{1}{3}$ | + | $\frac{3}{8}$ |
| 2 501 | | | ~ 24 | | | | | |

3. SOLVE: The LCD is 24.

$$\frac{1}{4} + \frac{1}{3} + \frac{3}{8} = \frac{1}{4} \cdot \frac{6}{6} + \frac{1}{3} \cdot \frac{8}{8} + \frac{3}{8} \cdot \frac{3}{3}$$
$$= \frac{6}{24} + \frac{8}{24} + \frac{9}{24}$$
$$= \frac{23}{24}$$

4. INTERPRET. *Check* the solution. *State* your conclusion: The total weight of the truck's load is $\frac{23}{24}$ ton.

Work Practice 8

Practice 8

owner needs.

To repair her sidewalk, a

homeowner must pour small amounts of cement in three

different locations. She needs

 $\frac{3}{5}$ of a cubic yard, $\frac{2}{10}$ of a cubic yard, and $\frac{2}{15}$ of a cubic yard for

these locations. Find the total

amount of cement the home-

Example 9 Calculating Flight Time

A flight from Tucson to Phoenix, Arizona, requires $\frac{5}{12}$ of an hour. If the plane has been flying $\frac{1}{4}$ of an hour, find how much time remains before landing.



Solution:

- **1.** UNDERSTAND. Read and reread the problem. The phrase "how much time remains" tells us to subtract.
- 2. TRANSLATE.

| In words: | time
remaining | is | flight time
from Tucson
of Phoenix | minus | flight time
already
passed |
|------------|-------------------|--------------|--|--------------|----------------------------------|
| | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| Translate: | time
remaining | = | $\frac{5}{12}$ | _ | $\frac{1}{4}$ |

3. SOLVE: The LCD is 12.

$$\frac{5}{12} - \frac{1}{4} = \frac{5}{12} - \frac{1}{4} \cdot \frac{3}{3}$$
$$= \frac{5}{12} - \frac{3}{12}$$
$$= \frac{2}{12}$$
$$= \frac{2}{12}$$
$$= \frac{\frac{1}{2}}{\frac{2}{2} \cdot 6}$$
$$= \frac{1}{6}$$

4. INTERPRET. *Check* the solution. *State* your conclusion: The flight time remaining is $\frac{1}{6}$ of an hour.

Work Practice 9

Practice 9

Find the difference in length of two boards if one board is $\frac{4}{5}$ of a foot long and the other is $\frac{11}{20}$ of a foot long.

Answer 9. $\frac{1}{4}$ ft

Calculator Explorations Performing Operations on Fractions

Scientific Calculator

Many calculators have a fraction key, such as $a_{b/c}$, that allows you to enter fractions and perform operations on them, and then it gives the result as a fraction. If your calculator has a fraction key, use it to calculate

$$\frac{3}{5}+\frac{4}{7}$$

Enter the keystrokes

 $3 a_{b/c} 5 + 4 a_{b/c} 7 =$

The display should read 1_{6} 3_{5} , which represents the mixed number $1\frac{6}{35}$. Let's write the result as a fraction.

To convert from mixed number notation to fractional notation, press



The display now reads 41 35, which represents 41 35, the sum in fractional notation.

Graphing Calculator

Graphing calculators also allow you to perform operations on fractions and will give exact fractional results. The fraction option on a graphing calculator may be found under the \boxed{MATH} menu. To perform the addition to the left, try the keystrokes.

 $3 \div 5 + 4 \div 7$ MATH ENTER ENTER

The display should read

 $3/5 + 4/7 \triangleright \text{Frac } 41/35$

Use a calculator to add the following fractions. Give each sum as a fraction.

| 1. $\frac{1}{16} + \frac{2}{5}$ | 2. $\frac{3}{20} + \frac{2}{25}$ | 3. $\frac{4}{9} + \frac{7}{8}$ |
|---|---|---|
| 4. $\frac{9}{11} + \frac{5}{12}$ | 5. $\frac{10}{17} + \frac{12}{19}$ | 6. $\frac{14}{31} + \frac{15}{21}$ |

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Any numerical answers are not listed.

least common denominator equivalent

1. To add or subtract unlike fractions, we first write the fractions as _______ fractions with a common denominator. The common denominator we use is called the ______.

4. $\frac{5}{8} - \frac{1}{6} = \frac{5}{8} \cdot \frac{3}{3} - \frac{1}{6} \cdot \frac{4}{4} = _ - _ = _$.

Martin-Gay Interactive VideosWatch the section lecture video and answer the following questions. $\overbrace{}$ \bigcirc \bigcirc

3.3 Exercise Set MyLab Math 🜔

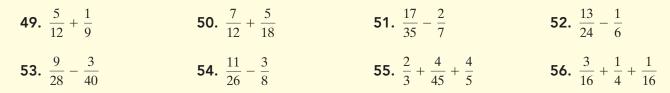
Objective A *Add and simplify. See Examples 1 through 4.*

| 1. $\frac{2}{3} + \frac{1}{6}$ | 2. $\frac{5}{6} + \frac{1}{12}$ | 3. $\frac{1}{2} + \frac{1}{3}$ | 4. $\frac{2}{3} + \frac{1}{4}$ |
|---|--|--|---|
| •5. $\frac{2}{11} + \frac{2}{33}$ | 6. $\frac{5}{9} + \frac{1}{3}$ | 7. $\frac{3}{14} + \frac{3}{7}$ | 8. $\frac{2}{5} + \frac{2}{15}$ |
| 9. $\frac{11}{35} + \frac{2}{7}$ | 10. $\frac{4}{5} + \frac{3}{40}$ | 11. $\frac{7}{20} + \frac{1}{15}$ | 12. $\frac{5}{14} + \frac{10}{21}$ |
| • 13. $\frac{7}{15} + \frac{5}{12}$ | 14. $\frac{5}{8} + \frac{3}{20}$ | 15. $\frac{3}{14} + \frac{2}{21}$ | 16. $\frac{6}{25} + \frac{7}{10}$ |
| 17. $\frac{9}{44} + \frac{17}{36}$ | 18. $\frac{2}{33} + \frac{2}{21}$ | 19. $\frac{5}{11} + \frac{3}{13}$ | 20. $\frac{3}{7} + \frac{9}{17}$ |
| 21. $\frac{1}{3} + \frac{1}{9} + \frac{1}{27}$ | 22. $\frac{1}{4} + \frac{1}{16} + \frac{1}{64}$ | 23. $\frac{5}{7} + \frac{1}{8} + \frac{1}{2}$ | 24. $\frac{10}{13} + \frac{7}{10} + \frac{1}{5}$ |
| 25. $\frac{5}{36} + \frac{3}{4} + \frac{1}{6}$ | 26. $\frac{7}{18} + \frac{2}{9} + \frac{5}{6}$ | 27. $\frac{13}{20} + \frac{3}{5} + \frac{1}{3}$ | 28. $\frac{2}{7} + \frac{13}{28} + \frac{2}{5}$ |

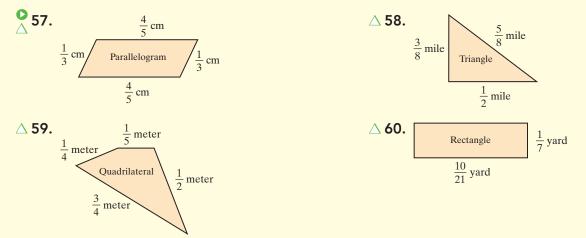
Objective B *Subtract and simplify. See Examples 5 through 7.*

| 29. $\frac{7}{8} - \frac{3}{16}$ | 30. $\frac{5}{13} - \frac{3}{26}$ | • 31. $\frac{5}{6} - \frac{3}{7}$ | 32. $\frac{3}{4} - \frac{1}{7}$ |
|---|---|--|--|
| 33. $\frac{5}{7} - \frac{1}{8}$ | 34. $\frac{10}{13} - \frac{7}{10}$ | 35. $\frac{9}{11} - \frac{4}{9}$ | 36. $\frac{7}{18} - \frac{2}{9}$ |
| 37. $\frac{11}{35} - \frac{2}{7}$ | 38. $\frac{2}{5} - \frac{3}{25}$ | 39. $\frac{5}{12} - \frac{1}{9}$ | 40. $\frac{7}{12} - \frac{5}{18}$ |
| 41. $\frac{7}{15} - \frac{5}{12}$ | 42. $\frac{5}{8} - \frac{3}{20}$ | 43. $\frac{3}{28} - \frac{2}{21}$ | 44. $\frac{9}{25} - \frac{7}{20}$ |
| 45. $\frac{1}{100} - \frac{1}{1000}$ | 46. $\frac{1}{50} - \frac{1}{500}$ | 47. $\frac{21}{44} - \frac{11}{36}$ | 48. $\frac{7}{18} - \frac{2}{45}$ |

Objectives A B Mixed Practice Perform the indicated operation. See Examples 1 through 7.



Objective C *Find the perimeter of each geometric figure. (Hint: Recall that perimeter means distance around.)*



Solve. For Exercises 61 and 62, the solutions have been started for you. See Examples 8 and 9.

61. The slowest mammal is the three-toed sloth from South America. The sloth has an average ground

speed of $\frac{1}{10}$ mph. In the trees, it can accelerate to $\frac{17}{100}$ mph. How much faster can a sloth travel in the trees? (*Source: Guinness World Records*)

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blanks.)

| | how much
faster sloth
travels in trees | is | sloth
speed in
trees | minus | sloth
speed on
ground |
|----|--|--------------|----------------------------|--------------|-----------------------------|
| | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| | how much
faster sloth
travels in trees | = | | _ | |
| Fi | nish with: | | | | |

3. SOLVE. and

4. INTERPRET.

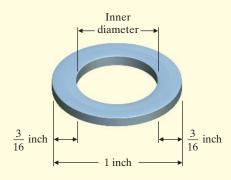
62. Killer bees have been known to chase people for up to $\frac{1}{4}$ of a mile, while domestic European honeybees will normally chase a person for no more than 100 feet, or $\frac{5}{264}$ of a mile. How much farther will a killer bee chase a person than a domestic honeybee? (*Source:* Coachella Valley Mosquito & Vector Control District)

Start the solution:

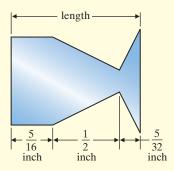
- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blanks.)

| how much
farther killer
bee will chase
than honeybee | is | distance
killer bee
chases | minus | distance
honeybee
chases |
|---|--------------|----------------------------------|--------------|--------------------------------|
| \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| how much
farther killer
bee will chase
than honeybee | = | | _ | |
| Finish with: | | | | |
| 3. SOLVE. and | | | | |
| 4. INTERPRET. | | | | |
| | | | | |

63. Find the inner diameter of the washer. (*Hint:* Use the outer diameter and subtract the washer widths.)



65. Given the following diagram, find its total length. (*Hint:* Find the sum of the partial lengths.)



- **67.** Together, Thin Mints and Samoas account for $\frac{11}{25}$ of the Girl Scout cookies sold each year. Thin Mints alone account for $\frac{1}{4}$ of all Girl Scout cookie sales. What fraction of Girl Scout cookies sold are Samoas? (*Source:* Girl Scouts of the United States of America)
- **68.** About $\frac{2}{5}$ of American students ages 13 to 17 name math, science, or industrial arts classes as they favorite subject in school. Industrial arts is the favorite subject for about $\frac{1}{20}$ of American students ages 13 to 17. For what fraction of students this age is math or science their favorite subject? (*Source:* Gallup Poll)

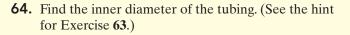
The table below shows the fraction of the Earth's water area taken up by each ocean. Use this table for Exercises 69 and 70.

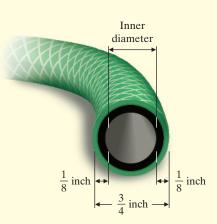
| Fraction of Earth's Water Area per Ocean | | |
|--|-----------------|--|
| Ocean | Fraction | |
| Arctic | $\frac{1}{25}$ | |
| Atlantic | $\frac{13}{50}$ | |
| Pacific | $\frac{1}{2}$ | |
| Indian | $\frac{1}{5}$ | |

69. What fraction of the world's water surface area is accounted for by the Pacific and Atlantic Oceans?

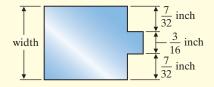


70. What fraction of the world's water surface area is accounted for by the Arctic and Indian Oceans?



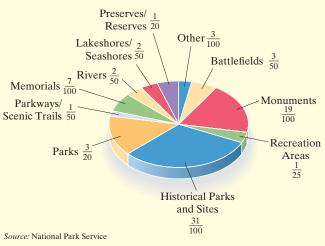


66. Given the following diagram, find its total width. (*Hint:* Find the sum of the partial widths.)



We first viewed this circle graph in Section 2.3. In this section we study it further. Use it to answer Exercises 71 through 74.





- **71.** What fraction of areas maintained by the National Park Service is designated as either National Parks or National Monuments?
- **72.** What fraction of areas maintained by the National Park Service is designated as either National Memorials or National Battlefields?
- **73.** What fraction of areas maintained by the National Park Service is not designated as National Monuments?
- **74.** What fraction of areas maintained by the National Park Service is not designated as National Preserves or National Reserves?

Review

Multiply or divide as indicated. See Sections 2.4 and 2.5.

75.
$$1\frac{1}{2} \cdot 3\frac{1}{3}$$
 76. $2\frac{5}{6} \div 5$ **77.** $4 \div 7\frac{1}{4}$ **78.** $4\frac{3}{4} \cdot 5\frac{1}{5}$ **79.** $3 \cdot 2\frac{1}{9}$ **80.** $6\frac{2}{7} \cdot 14$

Concept Extensions

For Exercises 81 and 82 below, do the following:

a. Draw three rectangles of the same size and represent each fraction in the sum or difference, one fraction per rectangle, by shading.

雪里

- **b.** Using these rectangles as estimates, determine whether there is an error in the sum or difference.
- c. If there is an error, correctly calculate the sum or difference.

See the Concept Checks in this section.

81.
$$\frac{3}{5} + \frac{4}{5} \stackrel{?}{=} \frac{7}{10}$$
 82. $\frac{3}{4} - \frac{5}{8} \stackrel{?}{=} \frac{2}{4}$

Subtract from left to right.

83.
$$\frac{2}{3} - \frac{1}{4} - \frac{2}{540}$$
 84. $\frac{9}{10} - \frac{7}{200} - \frac{1}{3}$

Perform each indicated operation.

85. $\frac{30}{55} + \frac{1000}{1760}$

87. In your own words, describe how to add or subtract two fractions with different denominators.

84.
$$\frac{9}{10} - \frac{7}{200} - \frac{1}{3}$$

86.
$$\frac{19}{26} - \frac{968}{1352}$$

88. Find the sum of the fractions in the circle graph above. Did the sum surprise you? Why or why not?

| | Sec | tions 3.1–3.3 | ntegrated Review |
|--|---|---|-------------------|
| Operations on I | Fractions and N | lixed Numbers | Answers |
| Find the LCM of each list of | numbers. | | |
| 1. 5,6 | 2. 3,7 | 3. 2,14 | |
| | | | |
| | | | |
| 4. 5,25 | 5. 4, 20, 25 | 6. 6, 18, 30 | |
| | | | |
| | | | 7. |
| Write each fraction as an equi | ivalent fraction with the indice | ated denominator. | 8. |
| 7. $\frac{3}{8} = \frac{1}{24}$ | 8. $\frac{7}{9} = \frac{1}{36}$ | 9. $\frac{1}{4} = \frac{1}{40}$ | |
| 8 24 | 9 30 | 4 40 | 9. |
| | | | 10. |
| 2 | 11 | 5 | <u>11.</u> |
| 10. $\frac{2}{5} = \frac{1}{30}$ | 11. $\frac{11}{15} = \frac{1}{75}$ | 12. $\frac{5}{6} = \frac{1}{48}$ | 12. |
| | | | |
| | | | 13. |
| Add or subtract as indicated. | Simplify if necessary. | | <u> </u> |
| 13. $\frac{3}{8} + \frac{1}{8}$ | 14. $\frac{7}{10} - \frac{3}{10}$ | 15. $\frac{17}{24} - \frac{3}{24}$ | 15. |
| 0 0 | 10 10 | 24 24 | 16. |
| | | | |
| 4 9 | 1 1 | . 1 1 | 17. |
| 16. $\frac{4}{15} + \frac{9}{15}$ | 17. $\frac{1}{4} + \frac{1}{2}$ | 18. $\frac{1}{3} - \frac{1}{5}$ | <u>18.</u> |
| | | | |
| | | | 20. |
| 19. $\frac{7}{9} - \frac{2}{5}$ | 20. $\frac{3}{10} + \frac{2}{25}$ | 21. $\frac{7}{8} + \frac{1}{20}$ | 21 |
| , , | 10 20 | 0 20 | <u>21.</u>
203 |

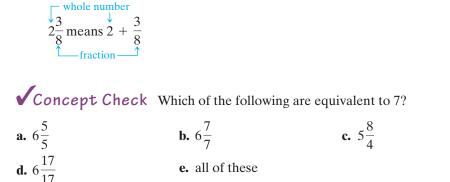
204

| 22. | 22. $\frac{5}{12} - \frac{2}{18}$ | 23. $\frac{1}{11} - \frac{1}{11}$ | - 24 | $\frac{3}{17} - \frac{2}{17}$ |
|-----|--|--|---|--|
| 23. | | | | |
| 24. | | | | |
| 25. | 0 2 | 1 1 | | 2 1 |
| 26. | 25. $\frac{9}{11} - \frac{2}{3}$ | 26. $\frac{1}{6} - \frac{1}{7}$ | 27 | $2 \cdot \frac{2}{9} + \frac{1}{18}$ |
| 27. | | | | |
| 28. | | | | |
| 29. | 28. $\frac{4}{13} + \frac{5}{26}$ | 20 2 1 | $+\frac{1}{3}$ 30 | 3 1 6 |
| 30. | 20. $\frac{1}{13} + \frac{1}{26}$ | 29. $\frac{1}{9} + \frac{1}{18}$ | $+\frac{1}{3}$ 30 | $\frac{1}{10} + \frac{1}{5} + \frac{1}{25}$ |
| 31. | | | | |
| 32. | | | | |
| 33. | Mixed Practice (S | Sections 2.4, 2.5, 3 | 8.1, 3.2, 3.3) Perfo | rm the indicated operation. |
| 34. | 31. $\frac{9}{10} + \frac{2}{3}$ | 32. $\frac{9}{10} - \frac{2}{3}$ | 33. $\frac{9}{10} \cdot \frac{2}{3}$ | 34. $\frac{9}{10} \div \frac{2}{3}$ |
| 35. | | | | |
| 36. | | | | |
| 37. | | | | |
| 38. | 35. $\frac{21}{25} - \frac{3}{70}$ | 36. $\frac{21}{25} + \frac{3}{70}$ | 37. $\frac{21}{25} \div \frac{3}{70}$ | 38. $\frac{21}{25} \cdot \frac{3}{70}$ |
| 39. | | | | |
| 40. | | | | |
| 41. | 7 2 | 7 2 | 2 5 1 | 3 11 2 |
| 42. | 39. $3\frac{7}{8} \cdot 2\frac{2}{3}$ | 40. $3\frac{7}{8} \div 2\frac{2}{3}$ | 41. $\frac{2}{9} + \frac{3}{27} + \frac{1}{2}$ | 42. $\frac{3}{8} + \frac{11}{16} + \frac{2}{3}$ |
| 43. | | | | |
| | | | | |
| 45. | 42 11 ⁷ . 2 ³ | $11 - 7^{1} - 7^{1}$ | 45 14 4 | 9 11 |
| 46. | 43. $11\frac{10}{10} \div 3\frac{100}{100}$ | 44. $7\frac{1}{4} \cdot 3\frac{1}{5}$ | 45. $\frac{1}{15} - \frac{1}{27}$ | 40. $\frac{1}{14} - \frac{1}{32}$ |

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3.4 Adding and Subtracting Mixed Numbers

Objective A Adding Mixed Numbers

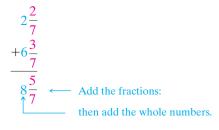


Recall that a mixed number has a whole number part and a fraction part.

Adding or Subtracting Mixed Numbers

To add or subtract mixed numbers, add or subtract the fraction parts and then add or subtract the whole number parts.





Example 1 Add: $2\frac{1}{3} + 5\frac{3}{8}$. Check by estimating. **Solution:** The LCD of 3 and 8 is 24. $2\frac{1 \cdot 8}{3 \cdot 8} = 2\frac{8}{24}$ $\frac{+5\frac{3 \cdot 3}{8 \cdot 3}}{\frac{7}{24}} = \frac{+5\frac{9}{24}}{\frac{7}{24}}$ Add the fractions. Add the whole numbers. To check by estimating, we round as usual. The fraction $2\frac{1}{3}$ rounds to 2, $5\frac{3}{8}$ rounds to 5, and 2 + 5 = 7, our estimate. Our exact answer is close to 7, so our answer is reasonable.

Work Practice 1

Objectives

- 🗛 Add Mixed Numbers. >
- B Subtract Mixed Numbers. >
- C Solve Problems by Adding or Subtracting Mixed Numbers.

Practice 1 Add: $4\frac{2}{5} + 5\frac{1}{6}$

1. $9\frac{17}{30}$

Answer

Helpful Hint

When adding or subtracting mixed numbers and whole numbers, it is a good idea to estimate to see if your answer is reasonable.

For the rest of this section, we leave most of the checking by estimating to you.

Practice 2

Add: $2\frac{5}{14} + 5\frac{6}{7}$

Example 2 Add: $3\frac{4}{5} + 1\frac{4}{15}$ **Solution:** The LCD of 5 and 15 is 15.

$$3\frac{4}{5} = 3\frac{12}{15}$$

$$\frac{+1\frac{4}{15}}{-\frac{4}{15}} = \frac{+1\frac{4}{15}}{-\frac{416}{15}}$$
 Add the fractions; then add the whole numbers.

Since $\frac{16}{15}$ is $1\frac{1}{15}$ we can write the sum as

$$4\frac{16}{15} = 4 + 1\frac{1}{15} = 5\frac{1}{15}$$

Work Practice 2

Concept Check Explain how you could estimate the following sum: $5\frac{1}{9} + 14\frac{10}{11}$.

Practice 3

Add: $10 + 2\frac{6}{7} + 3\frac{1}{5}$

Answers

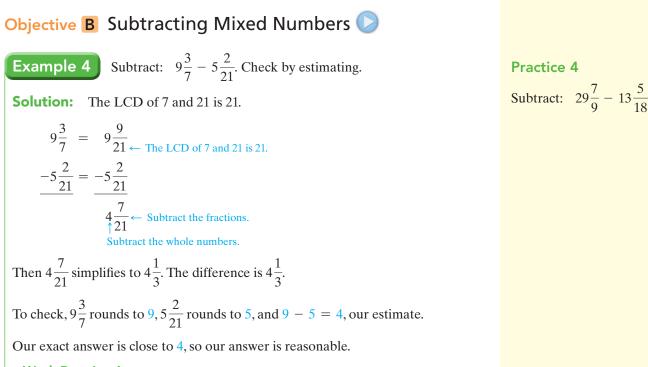
2.
$$8\frac{3}{14}$$
 3. $16\frac{2}{35}$

Concept Check Answer

Round each mixed number to the nearest whole number and add. $5\frac{1}{9}$ rounds to 5 and $14\frac{10}{11}$ rounds to 15, and the estimated sum is 5 + 15 = 20. Example 3 Add: $1\frac{4}{5} + 4 + 2\frac{1}{2}$ Solution: The LCD of 5 and 2 is 10. $1\frac{4}{5} = 1\frac{8}{10}$ 4 = 4 $\frac{+2\frac{1}{2}}{2} = \frac{+2\frac{5}{10}}{7\frac{13}{10}} = 7 + 1\frac{3}{10} = 8\frac{3}{10}$

Work Practice 3

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Work Practice 4

When subtracting mixed numbers, borrowing may be needed, as shown in the next example.

Example 5 Subtract: $7\frac{3}{14} - 3\frac{6}{7}$ Solution: The LCD of 7 and 14 is 14. $7\frac{3}{14} = 7\frac{3}{14}$ Notice that we cannot subtract $\frac{12}{14}$ from $\frac{3}{14}$, so we borrow from the whole number 7. $-3\frac{6}{7} = -3\frac{12}{14}$ borrow 1 from 7. $7\frac{3}{14} = 6 + 1\frac{3}{14} = 6 + \frac{17}{14}$ or $6\frac{17}{14}$. Now subtract. $7\frac{3}{14} = 7\frac{3}{14} = 6\frac{17}{14}$ $-3\frac{6}{7} = -3\frac{12}{14} = -3\frac{12}{14}$ $3\frac{5}{14} \leftarrow$ Subtract the fractions. Subtract the whole numbers.

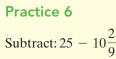
Concept Check In the subtraction problem $5\frac{1}{4} - 3\frac{3}{4}, 5\frac{1}{4}$ must be rewritten because $\frac{3}{4}$ cannot be subtracted from $\frac{1}{4}$. Why is it incorrect to rewrite $5\frac{1}{4}$ as $5\frac{5}{4}$?

Practice 5 Subtract: $9\frac{7}{15} - 5\frac{3}{5}$

Answers

1.
$$16\frac{1}{2}$$
 5. $3\frac{13}{15}$

Concept Check Answer Rewrite $5\frac{1}{4}$ as $4\frac{5}{4}$ by borrowing from the 5. Chapter 3 | Adding and Subtracting Fractions



Example 6 Subtract: $12 - 8\frac{3}{7}$ **Solution:** $12 = 11\frac{7}{7}$ Borrow 1 from 12 and write it as $\frac{7}{7}$. $-8\frac{3}{7} = -8\frac{3}{7}$ $3\frac{4}{7}$ \leftarrow Subtract the fractions. Subtract the whole numbers

Work Practice 6

Objective C Solving Problems by Adding or Subtracting Mixed Numbers

Now that we know how to add and subtract mixed numbers, we can solve real-life problems.

What is the total weight of the



Example 7 Calculating Total Weight

Two packages of ground round are purchased. One package weighs $2\frac{3}{8}$ pounds and the other $1\frac{4}{5}$ pounds. What is the combined weight of the ground round?

Solution:

- 1. UNDERSTAND. Read and reread the problem. The phrase "combined weight" tells us to add.
- 2. TRANSLATE.

| In words: | combined
weight | is | weight
of one
package | plus | weight of
second
package |
|------------|--------------------|--------------|-----------------------------|--------------|--------------------------------|
| | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| Translate: | combined
weight | = | $2\frac{3}{8}$ | + | $1\frac{4}{5}$ |

3. SOLVE: Before we solve, let's estimate. The fraction $2\frac{3}{8}$ rounds to 2, $1\frac{4}{5}$ rounds to 2, and 2 + 2 = 4. The combined weight should be close to 4.

$$2\frac{3}{8} = 2\frac{15}{40}$$
$$\frac{+1\frac{4}{5}}{-\frac{1}{5}} = \frac{+1\frac{32}{40}}{-\frac{1}{3}\frac{47}{40}} = 4\frac{7}{40}$$

7

4. INTERPRET. Check your work. Our estimate of 4 tells us that the exact answer of $4\frac{7}{40}$ is reasonable. *State* your conclusion: The combined weight of the ground round is $4\frac{7}{40}$ pounds.

Work Practice 7

Practice 7

Two rainbow trout weigh $2\frac{1}{2}$ pounds and $3\frac{2}{3}$ pounds. two trout?



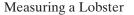


Example 8 Finding Legal Lobster Size

Lobster fishermen must measure the upper body shells of the lobsters they catch. Lobsters that are too small are thrown back into the ocean to help control the breeding stock. As of January 2017, Massachusetts divided its waters into four Lobster Conservation Management Areas, with a different minimum and maximum lobster size permitted in each area. In management Area 3, the legal minimum lobster size

is $3\frac{17}{32}$ inches and the maximum size is $6\frac{3}{4}$ inches. What is the difference in these sizes? (*Source:* mass.gov)





Solution:

1. UNDERSTAND. Read and reread the problem carefully. The phrase "difference in these sizes" tells us to subtract.

2. TRANSLATE.

In words: difference is
$$\begin{array}{c} maximum \\ lobster \\ size \end{array}$$
 minus $\begin{array}{c} minimum \\ lobster \\ size \end{array}$
Translate: difference = $6\frac{3}{4}$ - $3\frac{17}{32}$

3. SOLVE. Before we solve, let's estimate. The fraction $6\frac{3}{4}$ can be rounded to 7, $3\frac{17}{32}$ can be rounded to 4, and 7 - 4 = 3. The difference is not 3 but should be close to it.

$$6\frac{3}{4} = 6\frac{24}{32}$$
$$-3\frac{17}{32} = -3\frac{17}{32}$$
$$-3\frac{17}{32}$$

4. INTERPRET. *Check* your work. Our estimate tells us that the exact difference of $3\frac{7}{32}$ is reasonable. *State* your conclusion: The difference in lobster size is $3\frac{7}{32}$ inches.

Work Practice 8

Practice 8

The measurement around the trunk of a tree just below shoulder height is called its girth. The largest known American beech tree in the United States has a

girth of $24\frac{1}{6}$ feet. The largest known sugar maple tree in the United States has a girth of

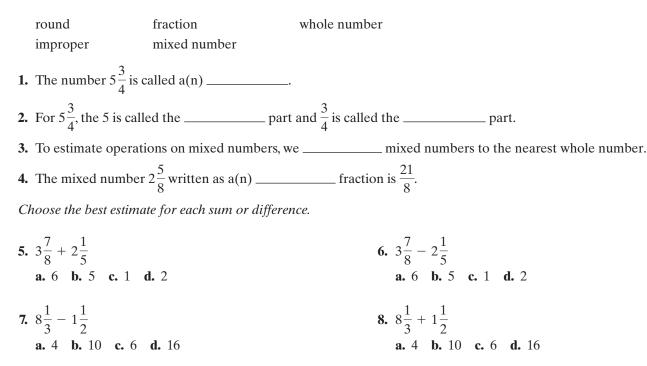
 $19\frac{5}{12}$ feet. How much larger is the girth of the largest known American beech tree than the girth of the largest known sugar maple tree? (*Source: American Forests*)

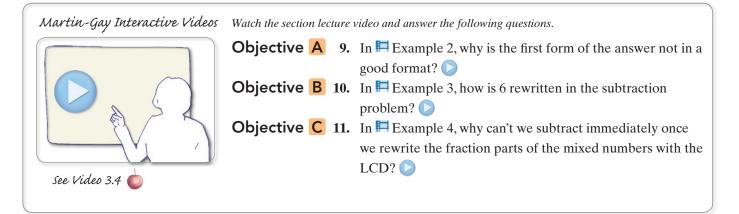


Answer 8. $4\frac{3}{4}$ ft

Vocabulary, Readiness & Video Check

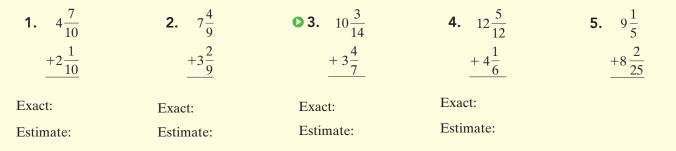
Use the choices below to fill in each blank.

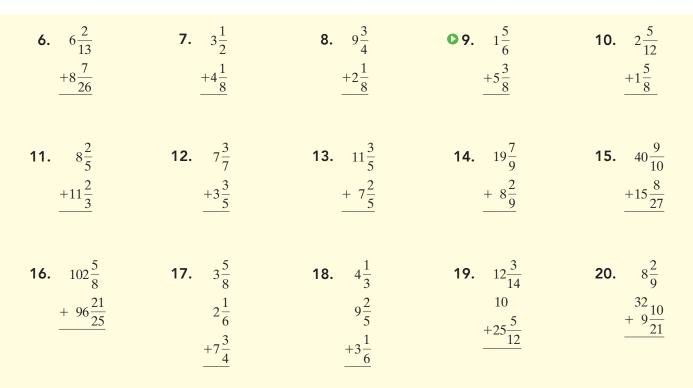




3.4 Exercise Set MyLab Math 💭

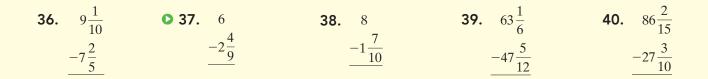
Objective 🗚 Add. For those exercises marked, find an exact sum and an estimated sum. See Examples 1 through 3.



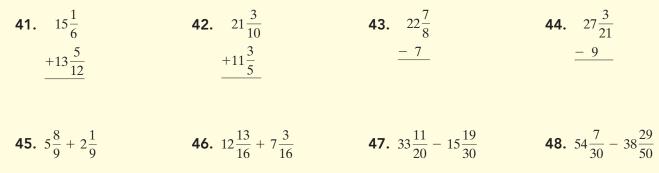


Objectives B *Subtract. For those exercises marked, find an exact difference and an estimated difference. See Examples 4 through 6.*

| 21. $4\frac{7}{10}$
$\frac{-2\frac{1}{10}}{10}$ | 22. $7\frac{4}{9}$ $\frac{-3\frac{2}{9}}{9}$ | 23. $10\frac{13}{14}$
$-3\frac{4}{7}$ | 24. $12\frac{5}{12}$
$-4\frac{1}{6}$ | 25. $9\frac{1}{5}$
$\frac{-8\frac{6}{25}}{}$ |
|---|---|--|--|--|
| Exact: | Exact: | Exact: | Exact: | |
| Estimate: | Estimate: | Estimate: | Estimate: | |
| 26. $5\frac{2}{13}$
$-4\frac{7}{26}$ | 27. $5\frac{2}{3} - 3\frac{1}{5}$ | 28. $23\frac{3}{5}$
$-8\frac{8}{15}$ | 29. $15\frac{4}{7}$
- $9\frac{11}{14}$ | 30. $5\frac{3}{8} - 2\frac{13}{20}$ |
| 31. $47\frac{4}{18} - 23\frac{19}{24}$ | 32. $6\frac{1}{6} - 5\frac{11}{14}$ | 33. 10 $-\frac{8\frac{1}{5}}{-\frac{1}{5}}$ | 34. 23 $-17\frac{3}{4}$ | 35. $11\frac{3}{5}$
$-9\frac{11}{15}$ |



Objectives A B Mixed Practice Perform the indicated operation. See Examples 1 through 6.



Objective C Solve. For Exercises 49 and 50, the solutions have been started for you. Write each answer in simplest form. See Examples 7 and 8.

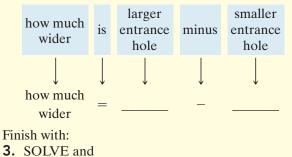
49. To prevent intruding birds, birdhouses built for Eastern Bluebirds should have an entrance hole

measuring $1\frac{1}{2}$ inches in diameter. Entrance holes in birdhouses for Mountain Bluebirds should measure $1\frac{9}{16}$ inches in diameter. How much wider should

entrance holes for Mountain Bluebirds be than for Eastern Bluebirds? (*Source:* North American Bluebird Society)

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- 2. TRANSLATE into an equation. (Fill in the blanks.)

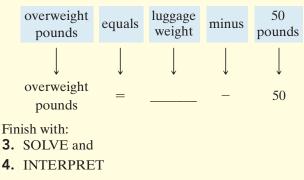


- **4.** INTERPRET

50. If the total weight allowable without overweight charges is 50 pounds and the traveler's luggage weighs $60\frac{5}{8}$ pounds, on how many pounds will the traveler's overweight charges be based?

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blanks.)



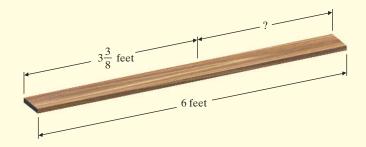
51. Charlotte Dowlin has $15\frac{2}{3}$ feet of plastic pipe. She cuts off a $2\frac{1}{2}$ -foot length and then a $3\frac{1}{4}$ -foot length. If she now needs a 10-foot piece of pipe, will the remaining piece do? If not, by how much will the piece be short?



- 53. If Tucson's average annual rainfall is 11¹/₄ inches and Yuma's is 3³/₅ inches, how much more rain, on average, does Tucson get than Yuma?
 - **55.** On four consecutive days, a concert pianist practiced for $2\frac{1}{2}$ hours, $1\frac{2}{3}$ hours, $2\frac{1}{4}$ hours, and $3\frac{5}{6}$ hours. Find his total practice time.
 - **57.** Jerald Divis, a tax consultant, takes $3\frac{1}{2}$ hours to prepare a personal tax return and $5\frac{7}{8}$ hours to prepare a small business return. How much longer does it take him to prepare the small business return?
 - **59.** The record for largest rainbow trout ever caught is 48 pounds and was set in Saskatchewan in 2009. The record for largest brown trout ever caught is $42\frac{1}{16}$ pounds and was set in New Zealand in 2013. How much more did the record-setting rainbow trout weigh than the record-setting brown trout? (*Source:* International Game Fish Association)



52. A trim carpenter cuts a board $3\frac{5}{8}$ feet long from one 6 feet long. How long is the remaining piece?



- **54.** A pair of crutches needs adjustment. One crutch is $43\frac{1}{3}$ inches and the other is $41\frac{3}{4}$ inches. Find how much the shorter crutch should be lengthened to make both crutches the same length.
- **56.** A tennis coach was preparing her team for a tennis tournament and enforced this practice schedule: Monday, $2\frac{1}{2}$ hours; Tuesday, $2\frac{2}{3}$ hours; Wednesday, $1\frac{3}{4}$ hours; and Thursday, $1\frac{9}{16}$ hours. How long did the team practice that weak before Eridau's

did the team practice that week before Friday's tournament?

- **58.** Jessica Callac takes $2\frac{3}{4}$ hours to clean her room. Her brother Matthew takes $1\frac{1}{3}$ hours to clean his room. If they start at the same time, how long does Matthew have to wait for Jessica to finish?
- **60.** Located on an island in New York City's harbor, the Statue of Liberty is one of the largest statues in the world. The copper figure is $46\frac{1}{20}$ meters tall from feet to tip of torch. The figure stands on a pedestal that is $46\frac{47}{50}$ meters tall. What is the overall height of the Statue of Liberty from the base of the pedestal to the tip of the torch? (*Source:* National Park Service)



61. The longest floating pontoon bridge in the United States is the Evergreen Point Bridge in Seattle, Washington. It is 2526 yards long. The second-longest pontoon bridge in the United States is the Lacey V. Murrow Memorial Bridge, also in Seattle.

It is $2206\frac{2}{3}$ yards long. How much longer is the

Evergreen Point Bridge than the Lacey V. Murrow Memorial Bridge? (*Source:* Federal Highway Administration) **62.** What is the difference between interest rates of $11\frac{1}{2}$ percent and $9\frac{3}{4}$ percent?

The following table lists some recent and upcoming total eclipses of the Sun that will be visible in North America. The duration of each eclipse is listed in the table. Use the table to answer Exercises 63 through 66.

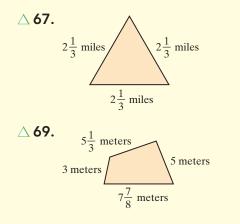
| Total Solar Eclipses Visible from
North America | | | |
|--|------------------------|--|--|
| Date of Eclipse | Duration (in Minutes) | | |
| August 21, 2017 | $2\frac{2}{3}$ | | |
| April 8, 2024 | $4\frac{7}{15}$ | | |
| March 30, 2033 $2\frac{37}{60}$ | | | |
| (Source: NASA/Goddar | d Space Flight Center) | | |

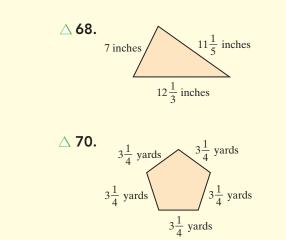
65. How much longer will the April 8, 2024, eclipse be than the August 21, 2017, eclipse?

- **63.** What is the total duration for the three eclipses?
- **64.** What is the total duration for the two eclipses occuring in odd-numbered years?
- **66.** How much longer will the April 8, 2024, eclipse be than the March 30, 2033, eclipse?



Find the perimeter of each figure.





Review

Evaluate each expression. See Section 1.9.

71. 2³ **72.** 3² **73.** 5² **74.** 2⁵ **76.** $36 - 5 \cdot 6 + 10$ **77.** $2 + 3(8 \cdot 7 - 1)$ **78.** $2(10 - 2 \cdot 5) + 13$ **75.** 20 ÷ 10 · 2

Simplify. Write any mixed number whose fraction part is not a proper fraction in simplest form. See Sections 2.1 and 2.3.

80. $10\frac{8}{7}$ **81.** $9\frac{10}{16}$ 82. $6\frac{7}{14}$ **79.** $3\frac{5}{5}$

Concept Extensions

Solve. See the Concept Checks in this section.

- **83.** Which of the following are equivalent to 10?
 - **a.** $9\frac{5}{5}$ **b.** $9\frac{100}{100}$ **c.** $6\frac{44}{11}$ **d.** $8\frac{13}{13}$
- **85.** Explain in your own words why $9\frac{13}{9}$ is equal to $10\frac{4}{9}$. **86.** In your own words, explain
- **84.** Which of the following are equivalent to $7\frac{3}{4}$?

a.
$$6\frac{7}{4}$$
 b. $5\frac{11}{4}$ **c.** $7\frac{12}{16}$ **d.** all of them

- a. when to borrow when subtracting mixed numbers, and
- **b.** how to borrow when subtracting mixed numbers.

Solve.

- **87.** Carmen's Candy Clutch is famous for its "Nutstuff," a special blend of nuts and candy. A Supreme box of Nutstuff has $2\frac{1}{4}$ pounds of nuts and $3\frac{1}{2}$ pounds of candy. A Deluxe box has $1\frac{3}{8}$ pounds of nuts and $4\frac{1}{4}$ pounds of candy. Which box is heavier and by how much?
- **88.** A student from the local college purchased three Supreme boxes and two Deluxe boxes of Nutstuff from Carmen's Candy Clutch. (See Exercise 87.) What is the total weight of the student's purchase?

3.5 Order, Exponents, and the Order of Operations

Objectives

A Compare Fractions. 🜔

B Evaluate Fractions Raised to Powers.

C Review Operations on Fractions.

D Use the Order of Operations.

Objective 🗛 Comparing Fractions 🕑

Recall that whole numbers can be shown on a number line using equally spaced distances.



From the number line, we can see the order of numbers. For example, we can see that 3 is less than 5 because 3 is to the left of 5.

For any two numbers on a number line, the number to the left is always the smaller number, and the number to the right is always the larger number.

We use the **inequality symbols** < or > to write the order of numbers.

Inequality Symbols

< means is less than.

> means is greater than.

For example,

 $3 \underbrace{\text{is less than 5}}_{3 < 5} \text{ or } 5 \underbrace{\text{is greater than 3}}_{5 > 3}$

We can compare fractions the same way. To see fractions on a number line, divide the spaces between whole numbers into equal parts.

2

For example, let's compare $\frac{2}{5}$ and $\frac{4}{5}$.

Helpful Hint Notice that to compare like fractions, we compare the numerators. The order of the like fractions is the same as the order of the numerators.

Comparing Fractions

Since $\frac{4}{5}$ is to the right of $\frac{2}{5}$,

 $\frac{2}{5} < \frac{4}{5}$

To determine which of two fractions is greater,

Step 1: Write the fractions as like fractions.

Notice that 2 < 4 also.

Step 2: The fraction with the greater numerator is the greater fraction.

| Examp | ble 1 Insert $<$ or $>$ to form a true statement. |
|------------------|--|
| $\frac{3}{10}$ | $\frac{2}{7}$ |
| Solutio | n: |
| Step 1: | The LCD of 10 and 7 is 70. |
| $\frac{3}{10} =$ | $\frac{3}{10} \cdot \frac{7}{7} = \frac{21}{70}; \qquad \frac{2}{7} = \frac{2}{7} \cdot \frac{10}{10} = \frac{20}{70}$ |

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Practice 1

Insert < or > to form a true statement.

| 8 | 10 |
|---|----|
| 9 | 11 |

Answer 1. < Step 2: Since 21 > 20, then $\frac{21}{70} > \frac{20}{70}$ or $\frac{3}{10} > \frac{2}{7}$

Work Practice 1

Example 2 Insert < or > to form a true statement.

 $\frac{9}{10}$ $\frac{11}{12}$

Solution:

Step 1: The LCD of 10 and 12 is 60.

 $\frac{9}{10} = \frac{9}{10} \cdot \frac{6}{6} = \frac{54}{60} \qquad \frac{11}{12} = \frac{11}{12} \cdot \frac{5}{5} = \frac{55}{60}$ Step 2: Since 54 < 55, then $\frac{54}{60} < \frac{55}{60}$ or $\frac{9}{10} < \frac{11}{12}$

Helpful Hint

If we think of < and > as arrowheads, a true statement is always formed when the arrow points to the smaller number.

 $\frac{2}{3} > \frac{1}{3}$ $\frac{5}{6} < \frac{7}{6}$ ↑ ↑ ↑ points to smaller number points to smaller number

Objective **B** Evaluating Fractions Raised to Powers

Recall from Section 1.9 that exponents indicate repeated multiplication.

exponent

$$5^3 = 5 \cdot 5 \cdot 5 = 125$$

 \uparrow
base 3 factors of 5

Exponents mean the same when the base is a fraction. For example,

$$\left(\frac{1}{3}\right)^4 = \underbrace{\frac{1}{3} \cdot \frac{1}{3} \cdot \frac{1}{3} \cdot \frac{1}{3}}_{4 \text{ factors of } \frac{1}{3}} = \frac{1}{81}$$

base

Examples

Evaluate each expression.

3.
$$\left(\frac{1}{4}\right)^2 = \frac{1}{4} \cdot \frac{1}{4} = \frac{1}{16}$$

4. $\left(\frac{3}{5}\right)^3 = \frac{3}{5} \cdot \frac{3}{5} \cdot \frac{3}{5} = \frac{27}{125}$
5. $\left(\frac{1}{6}\right)^2 \cdot \left(\frac{3}{4}\right)^3 = \left(\frac{1}{6} \cdot \frac{1}{6}\right) \cdot \left(\frac{3}{4} \cdot \frac{3}{4} \cdot \frac{3}{4}\right) = \frac{1 \cdot 1 \cdot \frac{1}{3} \cdot \frac{1}{3} \cdot 3}{2 \cdot \frac{3}{2} \cdot 2 \cdot \frac{3}{3} \cdot 4 \cdot 4 \cdot 4} = \frac{3}{256}$
Work Practice 3-5

Practice 2

Insert < or > to form a true statement.

 $\frac{3}{5}$ $\frac{2}{9}$

Practice 3–5

Evaluate each expression.

3.
$$\left(\frac{1}{5}\right)^2$$

4. $\left(\frac{2}{3}\right)^3$
5. $\left(\frac{1}{4}\right)^2 \left(\frac{2}{3}\right)^3$

Answers 2. > 3. $\frac{1}{25}$ 4. $\frac{8}{27}$ 5. $\frac{1}{54}$

Objective C Reviewing Operations on Fractions 🕗

To get ready to use the order of operations with fractions, let's first review the operations on fractions that we have learned.

| Review of Operations on Fractions | | | |
|-----------------------------------|--|---|--|
| Operation | Procedure | Example | |
| Multiply | Multiply the numerators and multiply the denominators. | $\frac{5}{9} \cdot \frac{1}{2} = \frac{5 \cdot 1}{9 \cdot 2} = \frac{5}{18}$ | |
| Divide | Multiply the first fraction by the reciprocal of the second fraction. | $\frac{2}{3} \div \frac{11}{13} = \frac{2}{3} \cdot \frac{13}{11} = \frac{2 \cdot 13}{3 \cdot 11} = \frac{26}{33}$ | |
| Add or
Subtract | Write each fraction as an equivalent fraction
whose denominator is the LCD Add or subtract numerators and write the
result over the common denominator. | $\frac{3}{4} + \frac{1}{8} = \frac{3}{4} \cdot \frac{2}{2} + \frac{1}{8} = \frac{6}{8} + \frac{1}{8} = \frac{7}{8}$ | |

Practice 6–9

Perform each indicated operation.

| 6. | $\frac{3}{7} \div \frac{10}{11}$ | 7. $\frac{4}{15} + \frac{4}{15}$ | 2
5 |
|----|----------------------------------|---|--------|
| 8. | $\frac{2}{3} \cdot \frac{9}{10}$ | 9. $\frac{11}{12}$ – | 2 |
| | $\overline{3}$ $\overline{10}$ | 9. $\frac{12}{12}$ | 5 |

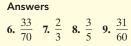
| Examples Perform each indicated operation. | | | |
|---|---|--|--|
| 6. $\frac{1}{2} \div \frac{8}{7} = \frac{1}{2} \cdot \frac{7}{8} = \frac{1 \cdot 7}{2 \cdot 8} = \frac{7}{16}$ | To divide: multiply by the reciprocal. | | |
| 7. $\frac{6}{35} + \frac{3}{7} = \frac{6}{35} + \frac{3}{7} \cdot \frac{5}{5} = \frac{6}{35} + \frac{15}{35} = \frac{21}{35}$ | To add: need the LCD. The LCD is 35. | | |
| $=\frac{\frac{1}{7}\cdot 3}{\frac{7}{5}\cdot 5}=\frac{3}{5}$ | | | |
| 8. $\frac{2}{9} \cdot \frac{3}{11} = \frac{2 \cdot 3}{9 \cdot 11} = \frac{2 \cdot 3}{3 \cdot 3 \cdot 11} = \frac{2}{33}$ | To multiply: multiply numerators and multiply denominators. | | |
| 9. $\frac{6}{7} - \frac{1}{3} = \frac{6}{7} \cdot \frac{3}{3} - \frac{1}{3} \cdot \frac{7}{7} = \frac{18}{21} - \frac{7}{21} = \frac{11}{21}$ | To subtract: need the LCD. The LCD is 21. | | |
| Work Practice 6–9 | | | |

Objective D Using the Order of Operations 🕑

The order of operations that we use on whole numbers applies to expressions containing fractions and mixed numbers also.

Order of Operations

- 1. Perform all operations within parentheses (), brackets [], or other grouping symbols such as square roots or fraction bars, starting with the innermost set.
- 2. Evaluate any expressions with exponents.
- **3.** Multiply or divide in order from left to right.
- 4. Add or subtract in order from left to right.



Example 10 Simplify: $\frac{1}{5} \div \frac{2}{3} \cdot \frac{4}{5}$ Simplify: $\frac{2}{9} \div \frac{4}{7} \cdot \frac{3}{10}$ **Solution:** Multiply or divide *in order* from left to right. We divide first. $\frac{1}{5} \div \frac{2}{3} \cdot \frac{4}{5} = \frac{1}{5} \cdot \frac{3}{2} \cdot \frac{4}{5}$ To divide, multiply by the reciprocal. $=\frac{3}{10}\cdot\frac{4}{5}$ $=\frac{3\cdot 4}{10\cdot 5}$ Multiply. $=\frac{3\cdot 2\cdot 2}{2\cdot 5\cdot 5}$ Simplify. $=\frac{6}{25}$ Simplify. Work Practice 10 **Example 11** Simplify: $\left(\frac{2}{3}\right)^2 \div \left(\frac{8}{27} + \frac{2}{3}\right)$ Practice 11 Simplify: $\left(\frac{2}{5}\right)^2 \div \left(\frac{3}{5} - \frac{11}{25}\right)$ Solution: Start within the right set of parentheses. We add. $\left(\frac{2}{3}\right)^2 \div \left(\frac{8}{27} + \frac{2}{3}\right) = \left(\frac{2}{3}\right)^2 \div \left(\frac{8}{27} + \frac{18}{27}\right)$ The LCD is 27. Write $\frac{2}{3}$ as $\frac{18}{27}$. $=\left(\frac{2}{3}\right)^2\div\frac{26}{27}$ Simplify inside the parentheses. $= \frac{4}{9} \div \frac{26}{27} \qquad \text{Write} \left(\frac{2}{3}\right)^2 \text{ as } \frac{4}{9}.$

Work Practice 11

Concept Check What should be done first to simplify $3\left[\left(\frac{1}{4}\right)^2 + \frac{3}{2}\left(\frac{6}{7} - \frac{1}{3}\right)\right]?$

Recall from Section 1.7 that the average of a list of numbers is their sum divided by the number of numbers in the list.

Example 12 Find the average of $\frac{1}{3}$, $\frac{2}{5}$, and $\frac{2}{5}$ **Solution:** The average is their sum, divided by 3. $\left(\frac{1}{3} + \frac{2}{5} + \frac{2}{9}\right) \div 3 = \left(\frac{15}{45} + \frac{18}{45} + \frac{10}{45}\right) \div 3$ The LCD is 45. $=\frac{43}{45} \div 3$ Add. $=\frac{43}{45}\cdot\frac{1}{3}$ $=\frac{43}{135}$ Multiply.

 $=\frac{4}{9}\cdot\frac{27}{26}$

 $=\frac{2\cdot 2\cdot 3\cdot 9}{9\cdot 2\cdot 13}$

Practice 12

Find the average of $\frac{1}{2}, \frac{3}{8}$, and $\frac{7}{24}$.

Answers **10.** $\frac{7}{60}$ **11.** 1 **12.** $\frac{7}{18}$ Concept Check Answer $\frac{6}{7} - \frac{1}{3}$

Practice 10

Work Practice 12

Vocabulary, Readiness & Video Check

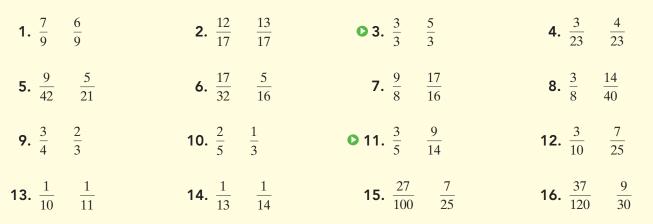
Use the choices below to fill in each blank. Not all choices will be used.

| | addition
subtraction | multiplication
division | evaluate the exponential expression |
|----|--|---|-------------------------------------|
| 1. | To simplify $\frac{1}{2} + \frac{2}{3} \cdot \frac{7}{8}$ | , which operation do we | perform first? |
| 2. | To simplify $\frac{1}{2} \div \frac{2}{3} \cdot \frac{7}{8}$ | , which operation do we | perform first? |
| 3. | To simplify $\frac{7}{8} \cdot \left(\frac{1}{2} - \right)$ | $\left(\frac{2}{3}\right)$, which operation do | we perform first? |
| 4. | To simplify 9 - $\left(\frac{3}{4}\right)^2$ | ² , which operation do we | e perform first? |

| Martin-Gay Interactive Videos | Videos Watch the section lecture video and answer the following questions. | | | |
|-------------------------------|--|--|--|--|
| | Objective A 5. | Complete this statement based on Example 1: When comparing fractions, as long as the are the same, | | |
| | Objective B 6. | we can just compare
Complete this statement based on Example 3: The meaning of an exponent is the same whether the base is a | | |
| see Video 3.5 🧅 | Objective C 7. | or the base is a
Fraction operations are reviewed in the lecture before
Example 4. How are denominators treated differently | | |
| | Objective D 8. | when adding and subtracting fractions than when
multiplying and dividing?
In Example 6, why did we subtract before applying the
exponent? | | |

3.5 Exercise Set MyLab Math 🜔

Objective A *Insert* < or > to form a true statement. See Examples 1 and 2.



Objective B Evaluate each expression. See Examples 3 through 5.

17.
$$\left(\frac{1}{2}\right)^4$$
 18. $\left(\frac{1}{7}\right)^2$ **0.19.** $\left(\frac{2}{5}\right)^3$ **20.** $\left(\frac{3}{4}\right)^3$

21.
$$\left(\frac{4}{7}\right)^3$$
 22. $\left(\frac{2}{3}\right)^4$ **23.** $\left(\frac{2}{9}\right)^2$ **24.** $\left(\frac{7}{11}\right)^2$

25. $\left(\frac{3}{4}\right)^2 \cdot \left(\frac{2}{3}\right)^3$ **26.** $\left(\frac{1}{6}\right)^2 \cdot \left(\frac{9}{10}\right)^2$ **27.** $\frac{9}{10} \left(\frac{2}{5}\right)^2$ **28.** $\frac{7}{11} \left(\frac{3}{10}\right)^2$

Objective C *Perform each indicated operation. See Examples 6 through 9.*

- **29.** $\frac{2}{15} + \frac{3}{5}$ **30.** $\frac{5}{12} + \frac{5}{6}$ **31.** $\frac{3}{7} \cdot \frac{1}{5}$ **32.** $\frac{9}{10} \div \frac{2}{3}$
- **33.** $1 \frac{4}{9}$ **34.** $5 \frac{2}{3}$ **35.** $4\frac{2}{9} + 5\frac{9}{11}$ **36.** $7\frac{3}{7} + 6\frac{3}{5}$
- **37.** $\frac{5}{6} \frac{3}{4}$ **38.** $\frac{7}{10} \frac{3}{25}$ **39.** $\frac{6}{11} \div \frac{2}{3}$ **40.** $\frac{3}{8} \cdot \frac{1}{11}$
- **41.** $0 \cdot \frac{9}{10}$ **42.** $\frac{5}{6} \cdot 0$ **43.** $0 \div \frac{9}{10}$ **44.** $\frac{5}{6} \div 0$
- **45.** $\frac{20}{35} \cdot \frac{7}{10}$ **46.** $\frac{18}{25} \div \frac{3}{5}$ **47.** $\frac{4}{7} \frac{6}{11}$ **48.** $\frac{11}{20} + \frac{7}{15}$

Objective D Use the order of operations to simplify each expression. See Examples 10 and 11.

O 49. $\frac{1}{5} + \frac{1}{3} \cdot \frac{1}{4}$ **50.** $\frac{1}{2} + \frac{1}{6} \cdot \frac{1}{3}$ **51.** $\frac{5}{6} \div \frac{1}{3} \cdot \frac{1}{4}$ **52.** $\frac{7}{8} \div \frac{1}{4} \cdot \frac{1}{7}$ **53.** $\frac{1}{5} \cdot \left(2\frac{5}{6} - \frac{1}{3}\right)$ **54.** $\frac{4}{7} \cdot \left(6 - 2\frac{1}{2}\right)$ **55.** $2 \cdot \left(\frac{1}{4} + \frac{1}{5}\right) + 2$ **56.** $\frac{2}{5} \cdot \left(5 - \frac{1}{2}\right) - 1$ **57.** $\left(\frac{3}{4}\right)^2 \div \left(\frac{3}{4} - \frac{1}{12}\right)$ **58.** $\left(\frac{8}{9}\right)^2 \div \left(2 - \frac{2}{3}\right)$ **659.** $\left(\frac{2}{3} - \frac{5}{9}\right)^2$ **60.** $\left(1 - \frac{2}{5}\right)^3$ **61.** $\frac{5}{9} \cdot \frac{1}{2} + \frac{2}{3} \cdot \frac{5}{6}$ **62.** $\frac{7}{10} \cdot \frac{1}{2} + \frac{3}{4} \cdot \frac{3}{5}$ **63.** $\frac{27}{16} \cdot \left(\frac{2}{3}\right)^2 - \frac{3}{20}$ **64.** $\frac{64}{27} \cdot \left(\frac{3}{4}\right)^2 - \frac{7}{10}$

65.
$$\frac{3}{13} \div \frac{9}{26} - \frac{7}{24} \cdot \frac{8}{14}$$

66. $\frac{5}{11} \div \frac{15}{77} - \frac{7}{10} \cdot \frac{5}{14}$
67. $\frac{3}{14} + \frac{10}{21} \div \left(\frac{3}{7}\right) \left(\frac{9}{4}\right)$
68. $\frac{11}{15} + \frac{7}{9} \div \left(\frac{14}{3}\right) \left(\frac{2}{3}\right)$
69. $\left(\frac{3}{4} + \frac{1}{8}\right)^2 - \left(\frac{1}{2} + \frac{1}{8}\right)$
70. $\left(\frac{1}{6} + \frac{1}{3}\right)^3 + \left(\frac{2}{5} \cdot \frac{3}{4}\right)^2$

Find the average of each list of numbers. See Example 12.

71. $\frac{5}{6}$ and $\frac{2}{3}$ **72.** $\frac{1}{2}$ and $\frac{4}{7}$ **73.** $\frac{1}{5}$, $\frac{3}{10}$, and $\frac{3}{20}$ **74.** $\frac{1}{3}$, $\frac{1}{4}$, and $\frac{1}{6}$

Objective C D Mixed Practice

- **75.** The average fraction of online sales of computer hardware is $\frac{23}{50}$, of computer software is $\frac{1}{2}$, and of movies and movies is $\frac{3}{5}$. Find the average of these
- 76. The average fraction of online sales of sporting goods is $\frac{12}{25}$, of toys and hobbies and games is $\frac{1}{2}$, and of computer hardware is $\frac{23}{50}$. Find the average of these

Review

Identify each key word with the operation it most likely translates to. After each word, write A for addition, S for subtraction, M for multiplication, and D for division. See Sections 1.3, 1.4, 1.6, and 1.7.

| 77. increased by | 78. sum | 79. triple | 80. product |
|----------------------------|-------------------------|-------------------|-----------------------|
| 81. subtracted from | 82. decreased by | 83. quotient | 84. divided by |
| 85. times | 86. difference | 87. total | 88. more than |

Concept Extensions

Solve.

89. Calculate $\frac{2^3}{3}$ and $\left(\frac{2}{3}\right)^3$. Do both of these expressions simplify to the same number? Explain why or why not.

these expressions simplify to the same number? Explain why or why not.

Each expression contains one addition, one subtraction, one multiplication, and one division. Write the operations in the order that they should be performed. Do not actually simplify. See the Concept Check in this section.

91. $[9+3(4-2)] \div \frac{10}{21}$ **92.** $[30 - 4(3 + 2)] \div \frac{5}{2}$

93.
$$\frac{1}{3} \div \left(\frac{2}{3}\right) \left(\frac{4}{5}\right) - \frac{1}{4} + \frac{1}{2}$$

Solve.

- **95.** In 2015, about $\frac{3}{5}$ of the total mail volume delivered by the United States Postal Service was first-class mail. That same year, about $\frac{8}{15}$ of the total volume of mail delivered by the United States Postal Service was standard mail. Which of these two categories accounts for a greater portion of the mail handled by volume? (*Source:* U.S. Postal Service)
- **97.** A recent survey reported that $\frac{2}{5}$ of the average college student's spending is for discretionary purchases, such as clothing, entertainment, and technology. About $\frac{13}{50}$ of the average college student's spending

is for room and board. In which category, discretionary purchases or room and board, does the average college student spend more? (*Source:* Nationwide Bank)

94.
$$\left(\frac{5}{6} - \frac{1}{3}\right) \cdot \frac{1}{3} + \frac{1}{2} \div \frac{9}{8}$$

- **96.** The National Park System (NPS) in the United States includes a wide variety of park types. National military parks account for $\frac{11}{500}$ of all NPS parks, and $\frac{9}{200}$ of NPS parks are classified as national preserves. Which category, national military park or national preserve, is bigger? (*Source:* National Park Service)
- **98.** On a normal workday in 2015, the average working parent in the United States spent $\frac{13}{80}$ of his or her day sleeping and $\frac{1}{20}$ of his or her day caring for others. Which did the average working parent spend more time doing, caring for others or sleeping? (*Source:* U.S. Bureau of Labor Statistics)

3.6 Fractions and Problem Solving 🔘

Objective A Solving Problems Containing Fractions or Mixed Numbers

Now that we know how to add, subtract, multiply, and divide fractions and mixed numbers, we can solve problems containing these numbers.

Don't forget the key words and phrases listed below that help indicate which operation to use. Also included are several words and phrases that translate to the symbol "=".

| Addition
(+) | Subtraction
(-) | Multiplication
(•) | Division
(÷) | Equality
(=) |
|-----------------|--------------------|-----------------------|-----------------|-----------------|
| sum | difference | product | quotient | equals |
| plus | minus | times | divide | is equal to |
| added to | subtract | multiply | shared equally | is/was |
| more than | less than | multiply by | among | yields |
| increased by | decreased by | of | divided by | |
| total | less | double/triple | divided into | |

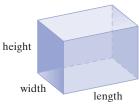
Objective

A Solve Problems by Performing Operations on Fractions or Mixed Numbers. Recall the following problem-solving steps introduced in Section 1.8. They may be helpful to you:

Problem-Solving Steps

- **1.** UNDERSTAND the problem. Some ways of doing this are to read and reread the problem, construct a drawing, and look for key words to identify an operation.
- **2.** TRANSLATE the problem. That is, write the problem in short form using words, and then translate to numbers and symbols.
- **3.** SOLVE the problem. It is helpful to estimate the solution by rounding. Then carry out the indicated operation from step 2.
- **4.** INTERPRET the results. *Check* the proposed solution in the stated problem and *state* your conclusions. Write your results with the correct units attached.

In the first example, we find the volume of a box. Volume measures the space enclosed by a region and is measured in cubic units. We study volume further in a later chapter.

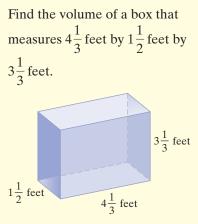


Volume of a box = length \cdot width \cdot height

Helpful Hint

Remember: Perimeter measures the distance around a figure. It is measured in units. Perimeter Area measures the amount of surface of a figure. It is measured in square units. Area Volume measures the amount of space enclosed by a region. It is measured in cubic units. Volume

Practice 1



Answer 1. $21\frac{2}{3}$ cu ft

Example 1 Finding Volume of a Camcorder Box

Toshiba recently produced a small camcorder. It measures approximately $1\frac{1}{2}$ inches by $1\frac{3}{5}$ inches by $1\frac{7}{25}$ inches. Find the volume of a box with these dimensions. (*Note:* The camcorder weighs only 65 grams—about the weight of 65 standard paper clips.) (*Source: Guinness World Records*)

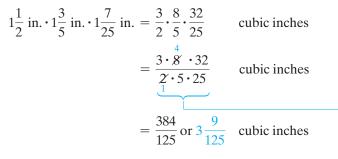
Solution:

1. UNDERSTAND. Read and reread the problem. The phrase "volume of a box" tells us what to do. The volume of a box is the product of its length, width, and height. Since we are multiplying, it makes no difference which measurement we call length, width, or height.

2. TRANSLATE.

In words: volume of the box is length \cdot width \cdot height \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow Translate: volume of the box = $1\frac{1}{2}$ in. \cdot $1\frac{3}{5}$ in. \cdot $1\frac{7}{25}$ in.

3. SOLVE: Before we multiply, let's estimate by rounding each dimension to a whole number. The number $1\frac{1}{2}$ rounds to 2, $1\frac{3}{5}$ rounds to 2, and $1\frac{7}{25}$ rounds to 1, so our estimate is $2 \cdot 2 \cdot 1$ or 4 cubic inches.



Helpful Hint Notice a shortcut taken when simplifying the fraction. Here, a common factor of 2 is recognized in 8 and 2. Then $8 \div 2$ is 4 in the numerator and $2 \div 2$ is 1 in the denominator.

4. INTERPRET. *Check* your work. The exact answer is close to our estimate, so it is reasonable. *State* your conclusion: The volume of a box that measures $1\frac{1}{2}$ inches by $1\frac{3}{5}$ inches by $1\frac{7}{25}$ inches is $3\frac{9}{125}$ cubic inches.

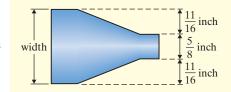
Example 2 Finding Unknown Length

Given the following diagram, find its total length.

length $\frac{1}{2}$ inch $\frac{11}{16}$ inch $\frac{11}{16}$ inch $\frac{9}{32}$ inch

Practice 2

Given the following diagram, find its total width.



Solution:

- **1.** UNDERSTAND. Read and reread the problem. Then study the diagram. The phrase "total length" tells us to add.
- **2.** TRANSLATE. It makes no difference which length we call first, second, or third length.

| In words: | total
length | is | first
length | + | second length | + | third length |
|------------|-----------------|--------------|-------------------|---|---------------------|---|--------------------|
| | \downarrow | \downarrow | \downarrow | | \downarrow | | \downarrow |
| Translate: | total
length | = | $\frac{1}{2}$ in. | + | $\frac{11}{16}$ in. | + | $\frac{9}{32}$ in. |

(Continued on next page)

Answer 2. 2 in.

3. SOLVE:

$$\frac{1}{2} + \frac{11}{16} + \frac{9}{32} = \frac{1 \cdot 16}{2 \cdot 16} + \frac{11 \cdot 2}{16 \cdot 2} + \frac{9}{32}$$

$$= \frac{16}{32} + \frac{22}{32} + \frac{9}{32}$$

$$= \frac{47}{32} \text{ or } 1\frac{15}{32}$$

4. INTERPRET. *Check* your work. *State* your conclusion: The total length is $1\frac{15}{32}$ inches.

Work Practice 2

Many problems require more than one operation to solve, as shown in the next application.

Example 3 Acreage for Single-Family Home Lots

A contractor is considering buying land to develop a subdivision for single-family homes. Suppose the contractor buys 44 acres and calculates

that $4\frac{1}{4}$ acres of this land will be used for roads

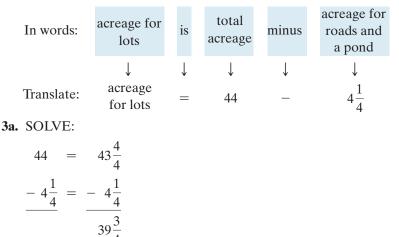
and a retention pond. How many $\frac{3}{4}$ -acre lots can



the contractor sell using the rest of the acreage?

Solution:

- **1a.** UNDERSTAND. Read and reread the problem. The phrase "using the rest of the acreage" tells us that initially we are to subtract.
- **2a.** TRANSLATE. First, let's calculate the amount of acreage that can be used for lots.



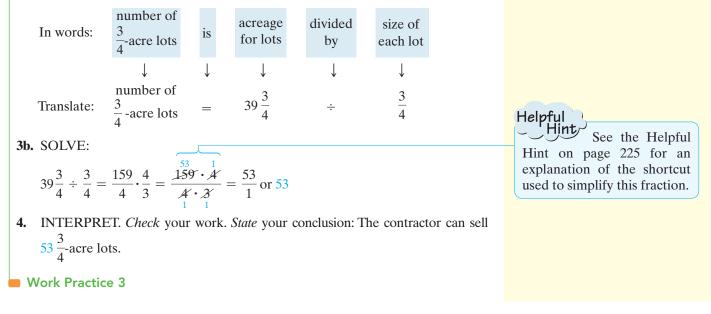
1b. UNDERSTAND. Now that we know $39\frac{3}{4}$ acres can be used for lots, we calculate how many $\frac{3}{4}$ acres are in $39\frac{3}{4}$. This means that we divide.

Practice 3

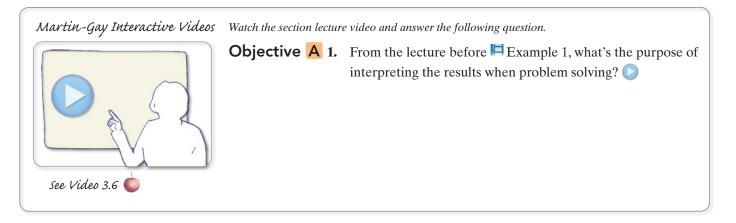
Suppose that 25 acres of land are purchased, but because of roads and wetlands concerns, $6\frac{2}{3}$ acres cannot be developed into lots. How many $\frac{5}{6}$ -acre

lots can the rest of the land be divided into?





Vocabulary, Readiness & Video Check



3.6 Exercise Set MyLab Math

To prepare for problem solving, translate each phrase to an expression. Do not simplify the expression.

1. The sum of
$$\frac{1}{2}$$
 and $\frac{1}{3}$.
 2. The product of $\frac{1}{2}$ and $\frac{1}{3}$.

 3. The quotient of 20 and $6\frac{2}{5}$.
 4. The difference of 20 and $6\frac{2}{5}$.

 5. Subtract $\frac{5}{8}$ from $\frac{15}{16}$.
 6. The total of $\frac{15}{36}$ and $\frac{18}{30}$.

- **7.** $\frac{21}{68}$ increased by $\frac{7}{34}$.
- **9.** The product of $8\frac{1}{3}$ and $\frac{7}{9}$.

Objective A Solve. Write any improper-fraction answers as mixed numbers. For Exercises 11 and 12, the solutions have been started for you. Write each answer in simplest form. See Examples 1 through 3.

1

11. A recipe for brownies calls for $1\frac{2}{3}$ cups of sugar. If you are doubling the recipe, how much sugar do you need?

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blanks below.)

| sugar
needed | is | double | recipe
amount
of sugar |
|-----------------|--------------|------------------|------------------------------|
| ↓
Sugor | \downarrow | \downarrow | \downarrow |
| sugar
needed | = | $\overline{2}$. | |

Finish with:

- **3**. SOLVE
- **4.** INTERPRET

^{*}Note: Another way to double a number is to add the number to the same number.

13. A decorative wall in a garden is to be built using bricks that are $2\frac{3}{4}$ inches wide and mortar joints that are $\frac{1}{2}$ inch wide. Use the diagram to find the height of the wall.



8.
$$\frac{21}{68}$$
 decreased by $\frac{7}{34}$.
0. $37\frac{1}{2}$ divided by $9\frac{1}{2}$.

12. A nacho recipe calls for $\frac{1}{3}$ cup cheddar cheese and $\frac{1}{2}$ cup jalapeño cheese. Find the total amount of cheese in the recipe.

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blanks below.)

| total
cheese | is | how
much
cheddar | added
to | how much
jalapeño
cheese |
|-----------------|--------------|------------------------|--------------|--------------------------------|
| \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| total | = | | + | |
| cheese | | | | |

Finish with:

- **3.** SOLVE
- **4.** INTERPRET
- **14.** Suppose that the contractor building the wall in Exercise **13** decides that he wants one more layer of bricks with a mortar joint below and above that layer. Find the new height of the wall.

- **15.** Doug and Claudia Scaggs recently drove $290\frac{1}{4}$ miles on $13\frac{1}{2}$ gallons of gas. Calculate how many miles per gallon they get in their vehicle.
- ▶ 17. The life expectancy of a circulating coin is 30 years. The life expectancy of a circulating dollar bill is only $\frac{1}{20}$ as long. Find the life expectancy of circulating paper money. (*Source:* The U.S. Mint)

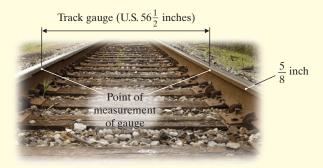


19. The Gauge Act of 1846 set the standard gauge for U.S. railroads at $56\frac{1}{2}$ inches. (See figure.) If the standard gauge in Spain is $65\frac{9}{10}$ inches, how much wider is Spain's standard gauge than the U.S. standard gauge? (*Source:* San Diego Railroad Museum)

- **16.** A contractor is using 18 acres of his land to sell $\frac{3}{4}$ -acre lots. How many lots can he sell?
- **18.** The Indian head one-cent coin of 1859–1864 was made of copper and nickel only. If $\frac{3}{25}$ of the coin was nickel, what part of the whole coin was copper? (*Source:* The U.S. Mint)



20. The standard railroad track gauge (see figure) in Spain is $65\frac{9}{10}$ inches, while in neighboring Portugal it is $65\frac{11}{20}$ inches. Which gauge is wider and by how much? (*Source:* San Diego Railroad Museum)

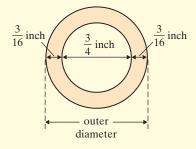


21. Mark Nguyen is a tailor making costumes for a play. He needs enough material for 1 large shirt that requires $1\frac{1}{2}$ yards of material and 5 small shirts that

each require $\frac{3}{4}$ yard of material. He finds a 5-yard remnant of material on sale. Is 5 yards of material enough to make all 6 shirts? If not, how much more material does he need?

22. A beanbag manufacturer makes a large beanbag requiring $4\frac{1}{3}$ yards of vinyl fabric and a smaller size requiring $3\frac{1}{4}$ yards. A 100-yard roll of fabric is to be used to make 12 large beanbags. How many smaller beanbags can be made from the remaining piece?

- 23. A plumber has a 10-foot piece of PVC pipe. How many $\frac{9}{5}$ -foot pieces can be cut from the 10-foot piece?
- 25. Suppose that the cross section of a piece of pipe looks like the diagram shown. Find the total outer diameter.

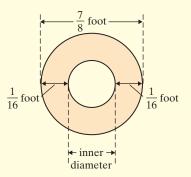


- **27.** A recipe for chocolate chip cookies calls for $2\frac{1}{2}$ cups of flour. If you are making $1\frac{1}{2}$ recipes, how many cups of flour are needed?
- \triangle **29.** The Polaroid Pop Shot, the world's first disposable instant camera, can take color photographs measuring $4\frac{1}{2}$ inches by $2\frac{1}{2}$ inches. Find the area of a photograph. (Source: Guinness World Records)
 - **31.** A total solar eclipse on July 2, 2019, will last $4\frac{1}{2}$ minutes and can be viewed from Chile and Argentina. The next total solar eclipse, on December 14, 2020, will last $1\frac{1}{6}$ minutes and can be viewed from the south Pacific and south Atlantic Oceans and Argentina and Chile. How much longer is the 2019

eclipse? (Source: NASA)

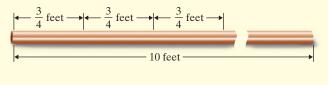
 \triangle 33. The Apple Watch Series Two measures approximately \triangle 34. Early cell phones were large and heavy. One $1\frac{2}{3}$ inches by $1\frac{2}{5}$ inches by $\frac{9}{20}$ inches. Find the volume of the watch. (Source: Apple, Inc.)

- **24.** A carpenter has a 12-foot board to be used to make windowsills. If each sill requires $2\frac{5}{16}$ feet, how many sills can be made from the 12-foot board?
- **26.** Suppose that the cross section of a piece of pipe looks like the diagram shown. Find the inner diameter.



- **28.** A recipe for a homemade cleaning solution calls for $1\frac{3}{4}$ cups of vinegar. If you are tripling the recipe, how much vinegar is needed?
- \triangle **30.** A model for a proposed computer chip measures $\frac{3}{4}$ inch by $1\frac{1}{4}$ inches. Find its area.
 - 32. The pole vault record for the 2012 Summer Olympics was a little over $19\frac{9}{16}$ feet. The record for the 2016 Summer Olympics was $20\frac{5}{24}$ feet. Find the difference in the heights. (Source: International Olympic Committee)
 - early model measured approximately 8 inches by $2\frac{1}{2}$ inches by $2\frac{1}{2}$ inches. Find the volume of a box with those dimensions.

- **35.** A stack of $\frac{5}{8}$ -inch-wide sheetrock has a height of $41\frac{7}{8}$ inches. How many sheets of sheetrock are in the stack?
- 37. William Arcencio is remodeling his home. In order to save money, he is upgrading the plumbing himself. He needs 12 pieces of copper tubing, each $\frac{3}{4}$ of a foot long.
 - **a.** If he has a 10-foot piece of tubing, will that be enough?
 - **b.** How much more does he need or how much tubing will he have left over?



- **36.** A stack of $\frac{5}{4}$ -inch-thick books has a height of $28\frac{3}{4}$ inches. How many books are in the stack?
- **38.** Trishelle Dallam is building a bookcase. Each shelf will be $2\frac{3}{8}$ feet long, and she needs wood for 7 shelves.
 - a. How many shelves can she cut from an 8-foot board?
 - **b.** Based on your answer for part **a**, how many 8-foot boards will she need?

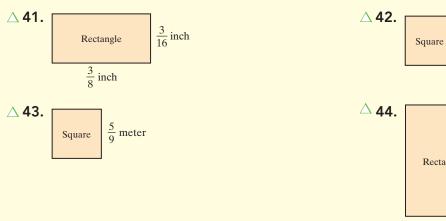


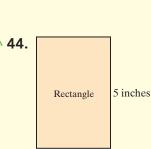
Recall that the average of a list of numbers is their sum divided by the number of numbers in the list. Use this procedure for Exercises 39 and 40.

39. A female lion had 4 cubs. They weighed $2\frac{1}{8}, 2\frac{7}{8}, 3\frac{1}{4},$ and $3\frac{1}{2}$ pounds. What is the average cub weight?

Find the area and perimeter of each figure.

40. Three brook trout were caught, tagged, and then released. They weighed $1\frac{1}{2}$, $1\frac{3}{8}$, and $1\frac{7}{8}$ pounds. Find their average weight.



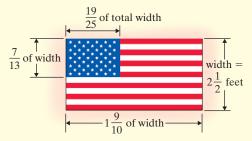


 $1\frac{7}{10}$ mile



For Exercises 45 through 48, see the diagram. (Source: www.usflag.org)

- **45.** The length of the U.S. flag is $1\frac{9}{10}$ its width. If a flag is being designed with a width of $2\frac{1}{2}$ feet, find its length.
- **46.** The width of the Union portion of the U.S. flag is $\frac{7}{13}$ of the width of the flag. If a flag is being designed with a width of $2\frac{1}{2}$ feet, find the width of the Union portion.



- **47.** There are 13 stripes of equal width in the flag. If the width of a flag is $2\frac{1}{2}$ feet, find the width of each stripe.
- **48.** The length of the Union portion of the flag is $\frac{19}{25}$ of the total width. If the width of a flag is $2\frac{1}{2}$ feet, find the length of the Union portion.

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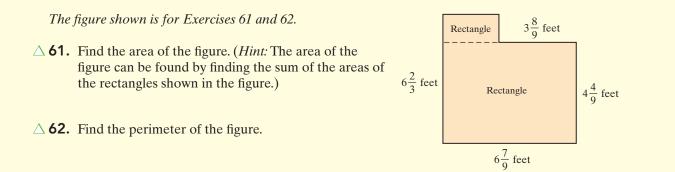
Review

Simplify. See Section 1.9.

| 49. $\sqrt{9}$ | 50. $\sqrt{4}$ | 51. 9 ² | 52. 4 ² |
|--------------------------------------|---------------------------------|------------------------------|------------------------------|
| 53. 8 ÷ 4 • 2 | 54. 20 ÷ 5 • 2 | 55. $3^2 - 2^2 + 5^2$ | 56. $8^2 - 6^2 + 7^2$ |
| 57. $5 + 3[14 - (12 \div 3)]$ | 58. 7 + 2[20 - (35 ÷ 5)] | | |

Concept Extensions

- **59.** Suppose you are finding the average of $7\frac{1}{9}$ and $12\frac{19}{20}$. Can the average be $1\frac{1}{2}$? Can the average be $15\frac{1}{2}$? Why or why not?
- **60.** Suppose that you are finding the average of $1\frac{3}{4}$, $1\frac{1}{8}$, and $1\frac{9}{10}$. Can the average be $2\frac{1}{4}$? Can the average be $\frac{15}{16}$? Why or why not?



63. On a particular day, 240 customers ate lunch at a local restaurant. If $\frac{3}{10}$ of them ordered a \$7 lunch, 5

 $\frac{5}{12}$ of them ordered a \$5 lunch, and the remaining

customers ordered a \$9 lunch, how many customers ordered a \$9 lunch?

65. Coins were practically made by hand in the late 1700s. Back then, it took 3 years to produce our

nation's first million coins. Today, it takes only $\frac{11}{13,140}$

as long to produce the same amount. Calculate how long it takes today in hours to produce one million coins. (*Hint:* First convert 3 years to equivalent hours. Use 365 days for each of the 3 years.) (*Source:* The U.S. Mint)

Chapter 3 Group Activity

Sections 3.1-3.6

This activity may be completed by working in groups or individually.

Lobsters are normally classified by weight. Use the weight classification table to answer the questions in this activity.

| Classification of Lobsters | | | |
|----------------------------|----------------------------------|--|--|
| Class | Weight (in Pounds) | | |
| Chicken | 1 to $1\frac{1}{8}$ | | |
| Eighths | $1\frac{1}{8}$ to $1\frac{1}{4}$ | | |
| Quarter | $1\frac{1}{4}$ to $1\frac{1}{2}$ | | |
| Large (or select) | $1\frac{1}{2}$ to $2\frac{1}{2}$ | | |
| Jumbo | Over $2\frac{1}{2}$ | | |
| (Source: The Maine Lobster | Marketing Collaborative) | | |

- 1. A lobster fisher has kept four lobsters from a lobster trap. Classify each lobster if they have the following weights:
 - **a.** $1\frac{7}{8}$ pounds

b.
$$1\frac{1}{16}$$
 pounds

- **64.** A baker purchased a case of 24 apples. He used $\frac{1}{3}$ of them to make an apple pie, $\frac{1}{4}$ of them to make apple crisp, and kept the rest for after-school snacks for his children. How many apples did he keep for snacks?
- **66.** The largest suitcase measures $13\frac{1}{3}$ feet by $8\frac{3}{4}$ feet by $4\frac{4}{25}$ feet. Find its volume. (*Source: Guinness World Records*)

c.
$$2\frac{3}{4}$$
 pounds
d. $1\frac{3}{8}$ pounds

- 2. A recipe requires 5 pounds of lobster. Using the minimum weight for each class, decide whether a chicken, a quarter, and a jumbo lobster will be enough for the recipe, and explain your reasoning. If not, suggest a better choice of lobsters to meet the recipe requirements.
- 3. A lobster market customer has selected two chickens,

a large and a jumbo. The jumbo lobster weighs $3\frac{1}{4}$ pounds. What is the most that these four lobsters could weigh? What is the least that these four lobsters sters could weigh?

- 4. A lobster market customer wishes to buy three quarters, each weighing $1\frac{1}{4}$ pounds. If lobsters sell for \$7 per pound, how much will the customer owe for her purchase?
- **5.** Why do you think there is no classification for lobsters weighing under 1 pound?

Chapter 3 Vocabulary Check

Fill in each blank with one of the words or phrases listed below.

| equivalent
mixed number | least commo | 1 | exponent
least common denominator | unlike
like | | |
|---|---|-------------------|--------------------------------------|-------------------------|--|--|
| 1. Fractions that hav | e the same den | ominator are ca | alled fractions. | | | |
| 2. The | is the | smallest numb | er that is a multiple of all number | s in a list of numbers. | | |
| 3 | fractions repre | esent the same | portion of a whole. | | | |
| 4. A(n) has a whole number part and a fraction part. | | | | | | |
| 5. The symbol | mea | ans is greater th | ian. | | | |
| 6. The symbol means is less than. | | | | | | |
| 7. The LCM of the d | 7. The LCM of the denominators in a list of fractions is called the | | | | | |
| 8. Fractions that have different denominators are called fractions. | | | | | | |
| 9. A shorthand nota | tion for repeate | d multiplicatio | n of the same factor is a(n) | | | |
| | | | | | | |

Helpful

Hint • Are you preparing for your test? To help, don't forget to take these:

- Chapter 3 Getting Ready for the Test on page 242
- Chapter 3 Test on page 243

Then check all of your answers at the back of this text. For further review, the step-by-step video solutions to any of these exercises are located in MyLab Math.

3 Chapter Highlights

| Definitions and Concepts | Examples | | | |
|---|---|--|--|--|
| Section 3.1 Adding and | Subtracting Like Fractions | | | |
| Fractions that have the same denominator are called like fractions. | $\frac{1}{3}$ and $\frac{2}{3}$; $\frac{5}{7}$ and $\frac{6}{7}$ | | | |
| To add or subtract like fractions, combine the numerators
and place the sum or difference over the common
denominator. | $\frac{2}{7} + \frac{3}{7} = \frac{5}{7} \leftarrow \text{ Add the numerators.} \\ \leftarrow \text{ Keep the common denominator.} \\ \frac{7}{8} - \frac{4}{8} = \frac{3}{8} \leftarrow \text{ Subtract the numerators.} \\ \leftarrow \text{ Keep the common denominator.} \end{cases}$ | | | |
| Section 3.2 Least Common Multiple | | | | |
| The least common multiple (LCM) is the smallest number that is a multiple of all numbers in a list of numbers. | The LCM of 2 and 6 is 6 because 6 is the smallest number that is a multiple of both 2 and 6. | | | |
| Method 1 for Finding the LCM of a List of Numbers
Using Multiples | Find the LCM of 4 and 6 using Method 1. | | | |
| Step 1: Write the multiples of the largest number (starting with the number itself) until a multiple common to all numbers in the list is found. | $6 \cdot 1 = 6$ Not a multiple of 4
$6 \cdot 2 = 12$ A multiple of 4 | | | |
| Step 2: The multiple found in step 1 is the LCM. | The LCM is 12. | | | |

| | Definitions and Concepts | Examples |
|----------------|---|---|
| | · · · · · · · · · · · · · · · · · · · | mon Multiple (<i>continued</i>) |
| | d 2 for Finding the LCM of a List of Numbers
Prime Factorization | Find the LCM of 6 and 20 using Method 2. |
| Step 1: | Write the prime factorization of each number. | $6 = 2 \cdot 3$ |
| Step 2: | For each different prime factor in step 1, circle
the greatest number of times that factor occurs | $20 = 2 \cdot 2 \cdot 5$ |
| | in any one factorization. | The LCM is |
| Step 3: | The LCM is the product of the circled factors. | $2 \cdot 2 \cdot 3 \cdot 5 = 60$ |
| Equival whole. | lent fractions represent the same portion of a | Write an equivalent fraction with the indicated denominator. |
| | | $\frac{2}{8} = \frac{1}{16}$ |
| | | $\frac{2 \cdot 2}{8 \cdot 2} = \frac{4}{16}$ |
| | | |
| To Add | * | ubtracting Unlike Fractions |
| | or Subtract Fractions with Unlike
inators | Add: $\frac{3}{20} + \frac{2}{5}$ |
| Step 1: | Find the LCD. | Step 1: The LCD of 20 and 5 is 20. |
| Step 2: | Write each fraction as an equivalent fraction whose denominator is the LCD. | Step 2: $\frac{3}{20} = \frac{3}{20}; \frac{2}{5} = \frac{2}{5} \cdot \frac{4}{4} = \frac{8}{20}$ |
| Step 3: | Add or subtract the like fractions. | Step 3: $\frac{3}{20} + \frac{2}{5} = \frac{3}{20} + \frac{8}{20} = \frac{11}{20}$ |
| Step 4: | Write the sum or difference in simplest form. | Step 4: $\frac{11}{20}$ is in simplest form. |
| | Section 3.4 Adding and S | ubtracting Mixed Numbers |
| | or subtract with mixed numbers, add or subtract ctions and then add or subtract the whole numbers. | Add: $2\frac{1}{2} + 5\frac{7}{8}$ |
| | | $2\frac{1}{2} = 2\frac{4}{8}$ |
| | | Add: $2\frac{1}{2} + 5\frac{1}{8}$
$2\frac{1}{2} = 2\frac{4}{8}$
$\frac{+5\frac{7}{8}}{-7\frac{11}{8}} = 7 + 1\frac{3}{8} = 8\frac{3}{8}$
s, and the Order of Operations |
| | | $7\frac{11}{8} = 7 + 1\frac{3}{8} = 8\frac{3}{8}$ |
| | Section 3.5 Order, Exponent | s, and the Order of Operations |
| | | 3 4 |
| | pare like fractions, compare the numerators.
ler of the fractions is the same as the order of the | Compare $\frac{3}{10}$ and $\frac{4}{10}$. |
| numera | | $\frac{3}{10} < \frac{4}{10}$ since $3 < 4$ |
| | | (continued) |

(continued)

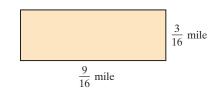
| Definitions and Concepts | Examples | | |
|---|---|--|--|
| Section 3.5 Order, Exponents, and | the Order of Operations (continued) | | |
| To compare unlike fractions, first write the fractions as like
fractions. Then the fraction with the greater numerator is
the greater fraction. | Compare $\frac{2}{5}$ and $\frac{3}{7}$.
$\frac{2}{5} = \frac{2}{5} \cdot \frac{7}{7} = \frac{14}{35}$ $\frac{3}{7} = \frac{3}{7} \cdot \frac{5}{5} = \frac{15}{35}$
Since 14 < 15, then
$\frac{14}{35} < \frac{15}{35}$ or $\frac{2}{5} < \frac{3}{7}$ | | |
| Exponents mean repeated multiplication whether the base is a whole number or a fraction. | $\left(\frac{1}{2}\right)^3 = \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{8}$ | | |
| Order of Operations | Perform each indicated operation. | | |
| 1. Perform all operations within parentheses (), brackets [], or other grouping symbols such as square roots or fraction bars. | $\frac{1}{2} + \frac{2}{3} \cdot \frac{1}{5} = \frac{1}{2} + \frac{2}{15}$ Multiply.
= $\frac{1}{2} \cdot \frac{15}{15} + \frac{2}{15} \cdot \frac{2}{2}$ The LCD is 30. | | |
| 2. Evaluate any expressions with exponents. | | | |
| 3. Multiply or divide in order from left to right. | $=\frac{15}{30}+\frac{4}{30}$ | | |
| 4. Add or subtract in order from left to right. | $=\frac{19}{30}$ Add. | | |
| Section 3.6 Fraction | s and Problem Solving | | |
| Problem-Solving Steps1. UNDERSTAND the problem.2. TRANSLATE the problem. | A stack of ³/₄-inch plywood has a height of 50¹/₄ inches.
How many sheets of plywood are in the stack? 1. UNDERSTAND. Read and reread the problem. We want to know how many ³/₄'s are in 50¹/₄, so we divide. 2. TRANSLATE. | | |
| 3. SOLVE the problem. | 2. TRANSLATE.
number of
sheets
in
stack
number of
sheets
in
stack
3. SOLVE. $50\frac{1}{4} \div \frac{3}{4} = \frac{201}{4} \cdot \frac{4}{3}$
$= \frac{207}{4} \cdot \frac{1}{4}$
= 67 | | |
| 4. INTERPRET the results. | 4. INTERPRET. <i>Check</i> your work and state your conclusion: There are 67 sheets of plywood in the stack. | | |

Chapter 3 Review

- (3.1) Add or subtract as indicated. Simplify your answers.
- **1.** $\frac{7}{11} + \frac{3}{11}$ **2.** $\frac{4}{50} + \frac{2}{50}$ **3.** $\frac{11}{15} \frac{1}{15}$ **4.** $\frac{4}{21} \frac{1}{21}$ **5.** $\frac{4}{15} + \frac{3}{15} + \frac{2}{15}$ **6.** $\frac{3}{20} + \frac{7}{20} + \frac{2}{20}$ **7.** $\frac{1}{12} + \frac{11}{12}$ **8.** $\frac{3}{4} + \frac{1}{4}$ **9.** $\frac{11}{25} + \frac{6}{25} + \frac{2}{25}$ **10.** $\frac{4}{21} + \frac{1}{21} + \frac{11}{21}$

Solve.

- **11.** One evening Mark Alorenzo did $\frac{3}{8}$ of his homework \triangle **12.** The Simpsons will be fencing in their land, which is before supper, another $\frac{2}{8}$ of it while his children did their homework, and $\frac{1}{8}$ after his children went to bed. What part of his homework did he do that evening?
 - in the shape of a rectangle. In order to do this, they need to find its perimeter. Find the perimeter of their land.



| (3.2) Find the LCM of each list of numbers. | | | | | | |
|---|-------------------|-------------------|------------------|-----------------------|---------------------|--|
| 13. 5,11 | 14. 20, 30 | 15. 20, 24 | 16. 16, 5 | 17. 12, 21, 63 | 18. 6, 8, 18 | |

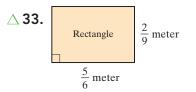
Write each fraction as an equivalent fraction with the given denominator.

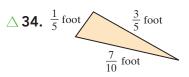
19. $\frac{7}{8} = \frac{1}{64}$ **20.** $\frac{2}{3} = \frac{1}{30}$ **21.** $\frac{7}{11} = \frac{1}{33}$ **22.** $\frac{10}{13} = \frac{1}{26}$ **23.** $\frac{4}{15} = \frac{1}{60}$ **24.** $\frac{5}{12} = \frac{1}{60}$

(3.3) Add or subtract as indicated. Simplify your answers.

- **26.** $\frac{4}{15} + \frac{1}{5}$ **25.** $\frac{7}{18} + \frac{2}{9}$ **27.** $\frac{4}{12} - \frac{1}{26}$ **28.** $\frac{7}{12} - \frac{1}{9}$
- **32.** $\frac{9}{14} \frac{3}{35}$ **30.** $\frac{7}{18} + \frac{5}{24}$ **31.** $\frac{11}{15} - \frac{4}{9}$ **29.** $\frac{1}{3} + \frac{9}{14}$

Find the perimeter of each figure.





- **35.** Find the difference in length of two scarves if one scarf is $\frac{5}{12}$ of a yard long and the other is $\frac{2}{3}$ of a vard long.
- **36.** Truman Kalzote cleaned $\frac{3}{5}$ of his house yesterday and $\frac{1}{10}$ of it today. How much of the house has been cleaned?
- (3.4) Add or subtract as indicated. Simplify your answers.

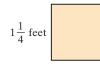
37.
$$31\frac{2}{7} + 14\frac{10}{21}$$

38. $24\frac{4}{5} + 35\frac{1}{5}$
39. $69\frac{5}{22} - 36\frac{7}{11}$
40. $36\frac{3}{20} - 32\frac{5}{6}$
41. $29\frac{2}{9}$
42. $7\frac{3}{8}$
43. $9\frac{3}{5}$
44. $8\frac{3}{11}$
 $-4\frac{1}{7}$
45. $-5\frac{1}{5}$

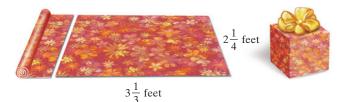
Solve.

+54

- **45.** The average annual snowfall at a certain ski resort is $62\frac{3}{10}$ inches. Last year it had $54\frac{1}{2}$ inches. How many inches below average was last year's snowfall?
- \triangle 47. Find the perimeter of a sheet of shelf paper needed \triangle 48. Find the perimeter of a rectangular sheet of gift wrap to fit exactly a square drawer $1\frac{1}{4}$ feet long on each side.



- 46. Dinah's homemade canned peaches contain $15\frac{3}{5}$ ounces per can. A can of Amy's brand contains $15\frac{5}{8}$ ounces per can. Amy's brand weighs how much more than Dinah's?
- that is $2\frac{1}{4}$ feet by $3\frac{1}{3}$ feet.



Chapter 3 Review

(3.5) Insert < or > to form a true statement.

49.
$$\frac{5}{11}$$
 $\frac{6}{11}$ **50.** $\frac{4}{35}$ $\frac{3}{35}$ **51.** $\frac{5}{14}$ $\frac{16}{42}$

52.
$$\frac{6}{35}$$
 $\frac{17}{105}$ **53.** $\frac{7}{8}$ $\frac{6}{7}$ **54.** $\frac{7}{10}$ $\frac{2}{3}$

Evaluate each expression. Use the order of operations to simplify.

55.
$$\left(\frac{3}{7}\right)^2$$
56. $\left(\frac{4}{5}\right)^3$
57. $\left(\frac{1}{2}\right)^4 \cdot \left(\frac{3}{5}\right)^2$
58. $\left(\frac{1}{3}\right)^2 \cdot \left(\frac{9}{10}\right)^2$
59. $\frac{5}{13} \div \frac{1}{2} \cdot \frac{4}{5}$
60. $\frac{8}{11} \div \frac{1}{3} \cdot \frac{11}{12}$
61. $\left(\frac{6}{7} - \frac{3}{14}\right)^2$
62. $\left(\frac{1}{3}\right)^2 - \frac{2}{27}$
63. $\frac{8}{9} - \frac{1}{8} \div \frac{3}{4}$
64. $\frac{9}{10} - \frac{1}{9} \div \frac{2}{3}$
65. $\frac{2}{7} \cdot \left(\frac{1}{5} + \frac{3}{10}\right)$
66. $\frac{9}{10} \div \left(\frac{1}{5} + \frac{1}{20}\right)$
67. $\left(\frac{3}{4} + \frac{1}{2}\right) \div \left(\frac{4}{9} + \frac{1}{3}\right)$
68. $\left(\frac{3}{8} - \frac{1}{16}\right) \div \left(\frac{1}{2} - \frac{1}{8}\right)$
69. $\frac{6}{7} \cdot \frac{5}{2} - \frac{3}{4} \cdot \frac{1}{2}$
70. $\frac{9}{10} \cdot \frac{1}{3} - \frac{2}{5} \cdot \frac{1}{11}$

Find the average of each list of fractions.

71.
$$\frac{2}{3}, \frac{5}{6}, \frac{1}{9}$$
 72. $\frac{4}{5}, \frac{9}{10}, \frac{3}{20}$

- (3.6)
- **73.** Our solar system has 146 known and officially confirmed moons. The planet Jupiter can claim $\frac{25}{73}$ of these moons. How many moons does Jupiter have? (*Source:* NASA)
- **74.** James Hardaway just bought $5\frac{7}{8}$ acres of land adjacent to the $9\frac{3}{4}$ acres he already owned. How much land does he now own?

Find the unknown measurements.



Find the perimeter and area of each rectangle. Attach the proper units to each. Remember that perimeter is measured in units and area is measured in square units.



Mixed Review

Find the LCM of each list of numbers.

79. 15, 30, 45 **80.** 6, 15, 20

Write each fraction as an equivalent fraction with the given denominator.

81.
$$\frac{5}{6} = \frac{1}{48}$$
 82. $\frac{7}{8} = \frac{1}{72}$

Add or subtract as indicated. Simplify your answers.

83. $\frac{5}{12} - \frac{3}{12}$ **84.** $\frac{3}{10} - \frac{1}{10}$ **85.** $\frac{2}{3} + \frac{1}{4}$ **86.** $\frac{5}{11} + \frac{2}{55}$

Chapter 3 Review



Evaluate each expression. Use the order of operations to simplify.

91. $\frac{2}{5} + \left(\frac{2}{5}\right)^2 - \frac{3}{25}$ **92.** $\frac{1}{4} + \left(\frac{1}{2}\right)^2 - \frac{3}{8}$ **93.** $\left(\frac{5}{6} - \frac{3}{4}\right)^2$

94.
$$\left(2-\frac{2}{3}\right)^3$$
 95. $\frac{2}{3} \div \left(\frac{3}{5}+\frac{5}{3}\right)$ **96.** $\frac{3}{8} \cdot \left(\frac{2}{3}-\frac{4}{9}\right)$

Insert < or > to form a true statement.

97. $\frac{3}{14}$ $\frac{2}{3}$ **98.** $\frac{7}{23}$ $\frac{3}{16}$

Solve.

- **99.** Gregor Krowsky studied math for $\frac{3}{8}$ of an hour and geography for $\frac{1}{8}$ of an hour. How long did he study?
- **100.** Two packages to be mailed weigh $3\frac{3}{4}$ pounds and $2\frac{3}{5}$ pounds. Find their combined weight.
- **101.** A ribbon $5\frac{1}{2}$ yards long is cut from a reel of ribbon with 50 yards on it. Find the length of the piece remaining on the reel.
- **103.** A recipe for pico de gallo calls for $1\frac{1}{2}$ tablespoons of cilantro. Five recipes will be made for a charity event. How much cilantro is needed?
- **102.** Linda Taneff has a board that is $10\frac{2}{3}$ feet in length. She plans to cut it into 5 equal lengths to use for a bookshelf. Find the length of each piece.
- **104.** Beryl Goldstein mixed $\frac{5}{8}$ of a gallon of water with $\frac{1}{8}$ of a gallon of punch concentrate. Then she and her friends drank $\frac{3}{8}$ of a gallon of the punch. How much of the punch was left?

Chapter 3 Getting Ready for the Test

MULTIPLE CHOICE All the exercises are **Multiple Choice**. Select the correct choice. Exercises 1, 2, and 10 have more than one correct answer.

LC

01. Choose the pair of fractions that are not like fractions.

A.
$$\frac{3}{7}$$
 and $\frac{3}{14}$ **B.** $\frac{2}{13}$ and $\frac{6}{13}$ **C.** $\frac{8}{15}$ and $\frac{15}{8}$

2. Which operation(s) on fractions requires like fractions?

A. multiplication B. division C. addition D. subtraction

O 3. Which addition of fractions has been performed correctly?

A.
$$\frac{2}{11} + \frac{3}{11} \stackrel{?}{=} \frac{5}{22}$$
 B. $\frac{2}{11} + \frac{3}{11} \stackrel{?}{=} \frac{5}{11}$ **C.** $\frac{2}{11} + \frac{3}{11} \stackrel{?}{=} \frac{6}{11}$

• 4. Which fraction is not equivalent to $\frac{5}{7}$?

A.
$$\frac{10}{14}$$
 B. $\frac{20}{28}$ **C.** $\frac{10}{12}$

- **5.** Which number is not a multiple of both 8 and 20?
 - **A.** 160 **B.** 80 **C.** 40 **D.** 20
- **6.** Which addition of fractions has been performed correctly?

A.
$$\frac{1}{2} + \frac{1}{3} \stackrel{?}{=} \frac{2}{5}$$
 B. $\frac{1}{2} + \frac{1}{3} \stackrel{?}{=} \frac{1}{6}$ **C.** $\frac{1}{2} + \frac{1}{3} \stackrel{?}{=} \frac{3}{6} + \frac{2}{6} = \frac{5}{6}$

• 7. Choose the fraction that is equivalent to $\frac{2}{15}$ but with a denominator of 60.

A.
$$\frac{6}{60}$$
 B. $\frac{8}{60}$ **C.** $\frac{60}{450}$

8. To evaluate the expression $\frac{7}{8} + \frac{1}{8} \cdot \frac{3}{8} - \frac{3}{16}$, which operation should be performed first? **A.** addition **B.** subtraction **C.** multiplication

For Exercises 9 and 10, the choices are below. Choices may be used more than once or not at all. Exercise 10 has more than one correct answer.

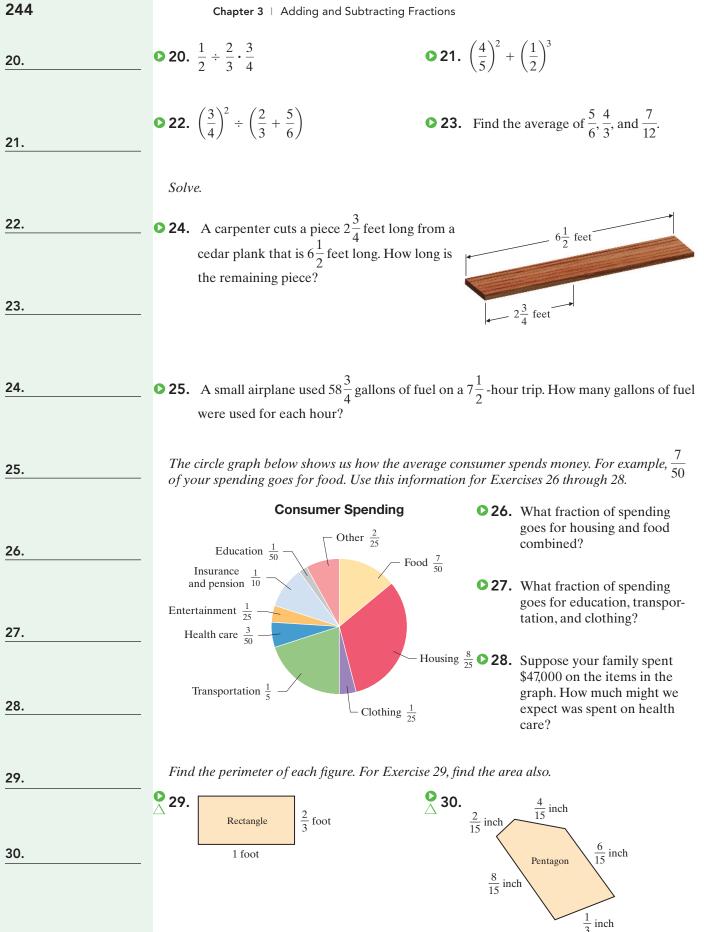
A. addition B. subtraction C. multiplication D. division

9. Which operation(s) on fractions requires the use of a reciprocal?

● 10. Which operation(s) on fractions requires common (the same) denominators?

- 11. The expression $\left(\frac{1}{8}\right)^2$ evaluates to: **A.** $\frac{1}{16}$ **B.** $\frac{2}{16} = \frac{1}{8}$ **C.** $\frac{1}{64}$
- 12. Choose the whole number that is closest to $18 8\frac{9}{10}$. A. 10 B. 9 C. 26

| For additional practice in MyLab Math. | go to your study plan MyLab I | Math or You Tube | Test Chapter 3 |
|--|---|--|----------------|
| 01. Find the LCM of | of 4 and 15. Q 2. Fi | nd the LCM of 8, 9, and 12. | Answers |
| Insert < or > to form | n a true statement. | | |
| 3. $\frac{5}{6}$ $\frac{26}{30}$ | • 4. $\frac{7}{8}$ | $\frac{8}{9}$ | _1. |
| 0 50 | 0 | , | 2. |
| | | | 3. |
| Perform each indicate | ed operation. Simplify your answe | rs. | 4. |
| 5. $\frac{7}{9} + \frac{1}{9}$ | 6. $\frac{8}{15} - \frac{2}{15}$ | 7. $\frac{9}{10} + \frac{2}{5}$ | |
| 99 | 15 15 | 10 5 | _6. |
| | | | 7. |
| 1 3 | 7 1 | 17 1 | 8. |
| • 8. $\frac{1}{6} + \frac{3}{14}$ | 9. $\frac{7}{8} - \frac{1}{3}$ | •10. $\frac{17}{21} - \frac{1}{7}$ | 9. |
| | | | |
| | | | <u>10.</u> |
| 11. $\frac{9}{20} + \frac{2}{3}$ | • 12. $\frac{16}{25} - \frac{1}{2}$ | D13. $\frac{11}{12} + \frac{3}{8} + \frac{5}{24}$ | <u>11.</u> |
| | | | <u>12.</u> |
| | | | <u>13.</u> |
| 14. $3\frac{7}{8}$ | • 15. $8\frac{2}{9}$ | • 16. $5\frac{1}{6}$ | <u>14.</u> |
| $7\frac{2}{5}$ $+2\frac{3}{4}$ | 12 | • 16. $5\frac{1}{6}$
- $3\frac{7}{8}$ | 15. |
| $+2\frac{3}{4}$ | $\frac{+10\frac{1}{15}}{}$ | | 16. |
| <u> </u> | | | |
| | | | <u>17.</u> |
| | | (2) 4 | <u>18.</u> |
| 17. 19
$-2\frac{3}{11}$ | • 18. $\frac{2}{7} \cdot \left(6 - \frac{1}{6}\right)$ | D 19. $\left(\frac{2}{3}\right)^{-1}$ | <u>19.</u> |
| 11 | | | |



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| | Cumulative Review | Chapters 1–3 |
|---|--|---------------|
| Write each number in words. | | Answers |
| 1. 85 | 2. 107 | |
| 3. 126 | 4. 5026 | _2 |
| | | 3. |
| 5. Add: 23 + 136 | 6. Find the perimeter. | 4. |
| | 3 in. 7 in.
9 in. | 5. |
| | | 6. |
| 7. Subtract: 543 – 29. Check by | 8. Divide: 3268 ÷ 27 | _7 |
| adding. | | 8 |
| 9. Round 278,362 to the nearest thousand. | 10. Find all the factors of 30. | 9. |
| | | <u>10.</u> |
| 11. Multiply: 236×86 | 12. Multiply: $236 \times 86 \times 0$ | <u>11.</u> |
| | | <u>12.</u> |
| 13. Find each quotient. Check by multiplying. | 14. Find the average of 25, 17, 19, and 39. | <u>13. a.</u> |
| a. 1)7
b. 12 ÷ 1 | | b |
| c. $\frac{6}{6}$ | | C |
| d. $9 \div 9$
e. $\frac{20}{1}$ | | d |
| f. 18)18 | | e |
| | | f |
| 15. The Hudson River in New York State is | 16. Evaluate: $\sqrt{121}$ | <u>14.</u> |
| 306 miles long. The Snake River in the
northwestern United States is 732 miles
longer than the Hudson River How | | <u>15.</u> |
| longer than the Hudson River. How
long is the Snake River? (<i>Source:</i> U.S.
Department of the Interior) | | <u>16.</u> |

| 246 | Chapter 3 Adding and Subtracting Frac | ctions | |
|------------|---|---|----------------------------|
| <u>17.</u> | Evaluate. | | |
| <u>18.</u> | 17. 9 ² 18. 5 ³ | 19. 3 ⁴ | 20. 10 ³ |
| <u>19.</u> | Write the shaded part of each diagram as an in | nproper fraction and a | mixed number. |
| 20. | 21. | 22. | |
| 21. | | | |
| 22 | 23. | 24. | |
| <u>23.</u> | 25. Of the numbers 3, 9, 11, 17, 26, which are p | prime and which are c | omposite? |
| <u>24.</u> | 26. Simplify: $\frac{6^2 + 4 \cdot 4 + 2^3}{37 - 5^2}$ | | |
| <u>25.</u> | 27. Find the prime factorization of 180. | | |
| <u>26.</u> | 28. Find the difference of 87 and 25. | | |
| 27. | 29. Write $\frac{72}{26}$ in simplest form. | | |
| 28. | _ | | |
| <u>29.</u> | 30. Write $9\frac{7}{8}$ as an improper fraction. | | |
| 30 | 31. Determine whether $\frac{16}{40}$ and $\frac{10}{25}$ are equivalent | alent. | |
| <u>31.</u> | 20 | 4 5 | |
| <u>32.</u> | 32. Insert $<$ or $>$ to form a true statement. | 7 9 | |
| <u>33.</u> | Multiply. | | |
| <u>34.</u> | 33. $\frac{2}{3} \cdot \frac{5}{11}$ | 34. $2\frac{5}{8} \cdot \frac{4}{7}$ | |
| 35 | 35. $\frac{1}{4} \cdot \frac{1}{2}$ | 36. 7.5 $\frac{2}{7}$ | |
| 36. | | - | |

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Cumulative Review

Divide.

37. $\frac{11}{18} \div 2\frac{5}{6}$ **38.** $\frac{15}{19} \div \frac{3}{5}$

39.
$$5\frac{2}{3} \div 2\frac{5}{9}$$
 40. $\frac{8}{11} \div \frac{1}{22}$

41. Add and simplify:
$$\frac{3}{16} + \frac{7}{16}$$
 42. Subtract and simplify: $\frac{11}{20} - \frac{7}{20}$

- **43.** Find the LCM of 6 and 8. **44.** Find the LCM of 7 and 5.
- **45.** Add: $\frac{1}{2} + \frac{2}{3} + \frac{5}{6}$ **46.** Evaluate: $\left(\frac{5}{9}\right)^2$
- **47.** Subtract: $9\frac{3}{7} 5\frac{2}{21}$ **48.** Subtract: $\frac{31}{100} \frac{5}{25}$
- **49.** Simplify: $\left(\frac{2}{3}\right)^2 \div \left(\frac{8}{27} + \frac{2}{3}\right)$ **50.** $\frac{1}{10} \div \frac{7}{8} \cdot \frac{2}{5}$

247

Decimals

Decimal numbers represent parts of a whole, just like fractions. In this chapter, we learn to perform arithmetic operations using decimals and to analyze the relationship between fractions and decimals. We also learn how decimals are used in the real world.

Mexico Cote d'Ivoire Ghana Nigeria Cameroon Brazil Malaysia

Places Where Cacao Trees Grow

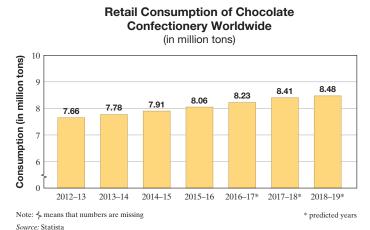


How Is Chocolate Made, and How Popular Is It?

hocolate-making begins with cacao beans found within pods that grow on a cacao tree. These harvested beans are roasted and processed until a liquid called cocoa liquor can be extracted. Cocoa liquor can be separated into cocoa powder and cocoa butter. Then all of these products can be blended with various ingredients to create an endless number of products, including chocolate.

Chocolate history begins in Latin America, where cacao trees grow wild. The Maya created a beverage from the cacao beans and used the beans themselves as a currency. From them, the secret of chocolate passed on to the Aztecs, and through interactions with Spanish explorers, chocolate made it to Spain. Eventually it made its way to the rest of Europe. In fact, chocolate was the first caffeine to reach Europe, predating the introduction of coffee and tea by a few years.

In Section 4.3, Exercises 79 through 84, we will explore the top chocolate-consuming nations in the world.



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Indonesia

Sections

- 4.1 Introduction to Decimals
- **4.2** Order and Rounding
- **4.3** Adding and Subtracting Decimals
- **4.4** Multiplying Decimals and Circumference of a Circle

Integrated Review— Operations on Decimals

- **4.5** Dividing Decimals and Order of Operations
- 4.6 Fractions and Decimals

Check Your Progress

Vocabulary Check Chapter Highlights

Chapter Review

Getting Ready for the Test

- Chapter Test
- **Cumulative Review**

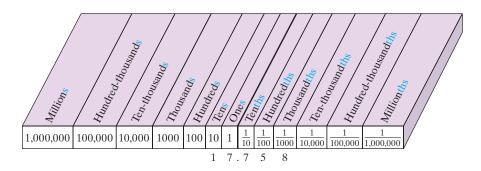
4.1 Introduction to Decimals

Objective A Decimal Notation and Writing Decimals in Words

Like fractional notation, decimal notation is used to denote a part of a whole. Numbers written in decimal notation are called **decimal numbers**, or simply **decimals**. The decimal 17.758 has three parts.

| 1 | 7 | | 7 | 5 | 8 |
|---------------|---|--|-----------|---|---|
| Whole 1 | | | ↑ Decimal | | |
| number | | | part | | |
| part | | | | | |
| Decimal point | | | | | |

In Section 1.2, we introduced place value for whole numbers. Place names and place values for the whole number part of a decimal number are exactly the same, as shown next. Place names and place values for the decimal part are also shown.



Notice that the value of each place is $\frac{1}{10}$ of the value of the place to its left. For example,

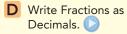
| $1 \cdot \frac{1}{10} =$ | $=\frac{1}{10}$ |
|-----------------------------------|------------------|
| ones | tenths |
| $\frac{1}{10} \cdot \frac{1}{10}$ | $=\frac{1}{100}$ |
| tenths | hundredths |

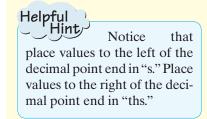
The decimal number 17.758 means

| | 1 ten | + | 7 ones | + | 7 tenths | + | 5 hundredths | + | 8 thousandths |
|----|--------------|---|--------------|---|------------------------|---|-------------------------|---|--------------------------|
| | \downarrow | ↓ | Ļ | ↓ | \downarrow | ↓ | \downarrow | ↓ | Ļ |
| | | | | | $\overline{1}$ | | 1 | | 1 |
| or | 1 • 10 | + | 7 · 1 | + | $7 \cdot \frac{1}{10}$ | + | $5 \cdot \frac{1}{100}$ | + | $8 \cdot \frac{1}{1000}$ |
| or | 10 | + | 7 | + | $\frac{7}{10}$ | + | $\frac{5}{100}$ | + | $\frac{8}{1000}$ |

Objectives

- A Know the Meaning of Place Value for a Decimal Number, and Write Decimals in Words.
- B Write Decimals in Standard Form.
- C Write Decimals as Fractions.





Writing (or Reading) a Decimal in Words

- Step 1: Write the whole number part in words.
- **Step 2:** Write "and" for the decimal point.
- **Step 3:** Write the decimal part in words as though it were a whole number, followed by the place value of the last digit.



Write the decimal 8.7 in words.

Practice 2

Write the decimal 97.28 in words.

Practice 3

Write the decimal 302.105 in words.

Practice 4

Write the decimal 72.1085 in words.

Helpful

Although the number of checks written in the United States is decreasing, there are still about 21 million checks written each day. (*Source:* Federal Reserve System)

Answers

 eight and seven tenths
 ninety-seven and twenty-eight hundredths
 three hundred two and one hundred five thousandths
 seventy-two and one thousand eighty-five ten-thousandths



Write the decimal 1.3 in words.

Solution: one and three tenths

Work Practice 1

Example 2

Write the decimal in the following sentence in words: The Golden Jubilee Diamond is a 545.67-carat cut diamond. (*Source: Guinness World Records*)



Solution: five hundred forty-five and sixty-seven hundredths

Work Practice 2



Write the decimal 19.5023 in words.

Solution: nineteen and five thousand twenty-three ten-thousandths

Work Practice 3

Example 4

Write the decimal in the following sentence in words: The oldest known fragments of the Earth's crust are zircon crystals; they were discovered in Australia and are thought to be 4.276 billion years old. (*Source: Guinness World Records*)

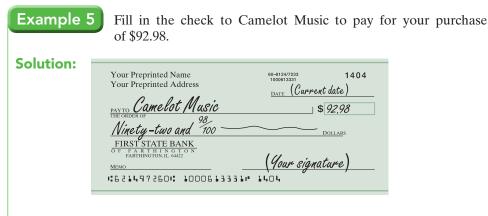


Solution: four and two hundred seventy-six thousandths

Work Practice 4

Suppose that you are paying \$368.42 for an automotive repair job at Jake's Body Shop by writing a check. Checks are usually written using the following format.

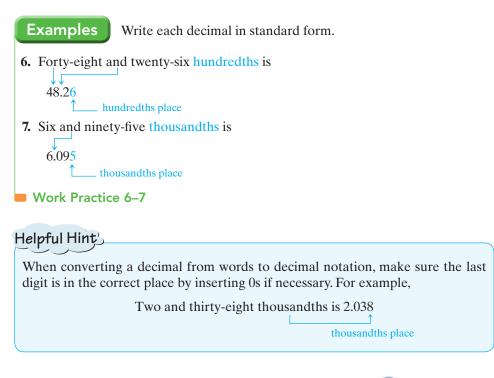
| 60-8124/7233
1000613331 | 1403 |
|----------------------------|--------------------------------------|
| hap | nt date)
\$ 368.42 |
| | Dollars |
| | |
| 0 | tin-Gay |
| | 1000613331
_{DATE} (Синне |



Work Practice 5

Objective **B** Writing Decimals in Standard Form 💽

A decimal written in words can be written in standard form by reversing the preceding procedure.



Objective C Writing Decimals as Fractions 🕗

Once you master reading and writing decimals, writing a decimal as a fraction follows naturally.

| Decimal | In Words | Fraction |
|---------|----------------------|--------------------------------|
| 0.7 | seven tenths | $\frac{7}{10}$ |
| 0.51 | fifty-one hundredths | $\frac{51}{100}$ |
| 0.009 | nine thousandths | $\frac{9}{1000}$ |
| 0.05 | five hundredths | $\frac{5}{100} = \frac{1}{20}$ |

Practice 5

Fill in the check to CLECO (Central Louisiana Electric Company) to pay for your monthly electric bill of \$207.40.

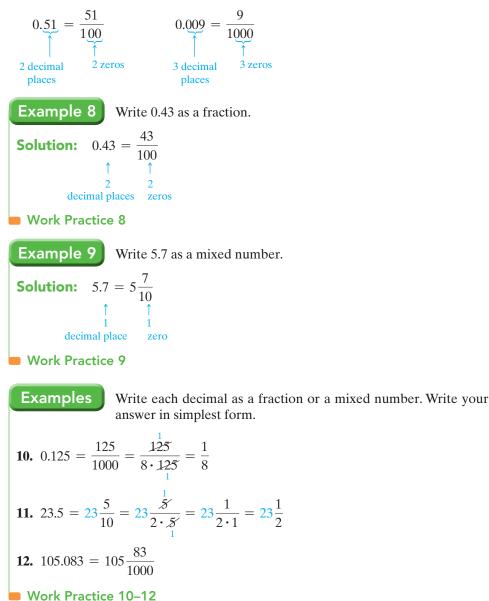
| Your Preprinted Name
Your Preprinted Address | 60-8124/7238
1000613331 | 1406 |
|---|----------------------------|---------|
| Four Preprinted Address | DATE | |
| PAYTO | | 5 |
| THE ORDER OF | | |
| | | DOLLARS |
| FIRST STATE BANK | | |
| MEMO | | |
| 621497260: 10006133 | | |

Practice 6–7

Write each decimal in standard form.

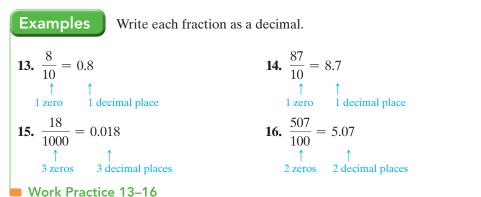
- 6. Three hundred and ninetysix hundredths
- **7.** Thirty-nine and forty-two thousandths

Answers 5. CLECO; 207.40; Two hundred seven and $\frac{40}{100}$ 6. 300.96 7. 39.042 Notice that the number of decimal places in a decimal number is the same as the number of zeros in the denominator of the equivalent fraction. We can use this fact to write decimals as fractions.



Objective D Writing Fractions as Decimals

If the denominator of a fraction is a power of 10, we can write it as a decimal by reversing the procedure above.



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Practice 8

Write 0.037 as a fraction.

Practice 9 Write 14.97 as a mixed number.

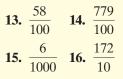
Practice 10–12

Write each decimal as a fraction or mixed number. Write your answer in simplest form.

10. 0.12
 11. 57.8
 12. 209.986

Practice 13–16

Write each fraction as a decimal.



Answers

| 8. | $\frac{37}{1000}$ | 9. | $14\frac{97}{100}$ | 10. | $\frac{3}{25}$ |
|-----|-------------------|-----|----------------------|-----|----------------|
| 11. | $57\frac{4}{5}$ | 12. | $209\frac{493}{500}$ | 13. | 0.58 |
| | | | 0.006 | 16. | 17.2 |

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank.

| words | decimals | and |
|-------|----------|---------------|
| tens | tenths | standard form |

1. The number "twenty and eight hundredths" is written in ______ and "20.08" is written in

- 2. Like fractions, ______ are used to denote parts of a whole.
- 3. When writing a decimal number in words, the decimal point is written as ______.
- 4. The place value ______ is to the right of the decimal point while ______ is to the left of the decimal point.

Determine the place value for the digit 7 in each number.

| 5. 70 | 6. 700 | 7. 0.7 | 8. 0.07 |
|--------------|---------------|---------------|----------------|
| | | | |

| Watch the section lecture video and answer the following questions. |
|--|
| Objective A 9. In Example 1, how is the decimal point written in |
| words? > |
| Objective B 10. Why is 9.8 not the correct answer to Example 3 ? |
| What is the correct answer? 🜔 |
| Objective C 11. From 🗏 Example 5, why does reading a decimal number |
| correctly help us write it as an equivalent fraction? 🜔 |
| Objective D 12. In 🗏 Examples 7–9, when writing a fraction as a decimal, and |
| the denominator of the fraction is a power of 10, what similar- |
| ity is there between the number of zeros in the denominator |
| and the number of decimal places in the decimal? 🕟 |
| |

| 4.1 Exercis | e Set MyLab Math 🌘 | | |
|--------------------------|-------------------------------|-------------------------------|-------------------|
| Objective A Write | e each decimal number in word | ls. See Examples 1 through 4. | |
| 1. 6.52 | 2. 7.59 | 3. 16.23 | 4. 47.65 |
| | | | |
| 5. 0.205 | 6. 0.495 | 7. 167.009 | 8. 233.056 |
| | | | |
| 9 200 005 | 10 5000 02 | 11 105 C | 12 410.20 |
| 9. 200.005 | 10. 5000.02 | 11. 105.6 | 12. 410.30 |

13. The Akashi Kaikyo Bridge, between Kobe and Awaji-Shima, Japan, is approximately 2.43 miles long.



- **15.** Mercury makes a complete orbit of the Sun every 87.97 days. (*Source:* National Space Science Data Center)
- **17.** The total number of households with televisions in the United States for the 2016–2017 season was estimated at 118.4 million. (*Source:* Nielsen Media Research)
- Fill in each check for the described purchase. See Example 5.
- **19.** Your monthly car loan of \$321.42 to R. W. Financial.

| Your Preprinted Name
Your Preprinted Address | 60-8124/7233
1000613331 | 1407 |
|---|----------------------------|---------|
| | DATE | |
| PAYTO | \$ | |
| THE ORDER OF | | |
| | | DOLLARS |
| FIRST STATE BANK | | |
| Мемо | | |
| 16214972601 1000613331 | ⊪ 1407 | |

21. Your cell phone bill of \$59.68 to Bell South.

| Your Preprinted Name
Your Preprinted Address | 60–8124/7233
1000613331
<u>Date</u> | 1409 |
|---|---|---------|
| PAY TO
THE ORDER OF | : | \$ |
| | | Dollars |
| FIRST STATE BANK | | |
| Мемо | | |
| ··621497260: 1000613333 | LI 1409 | |

14. The English Channel Tunnel is 31.04 miles long. (*Source: Railway Directory & Year Book*)



- **16.** Saturn makes a complete orbit of the Sun every 29.48 years. (*Source:* National Space Science Data Center)
- **18.** The longest U.S. Postal Service rural delivery route is 187.6 miles in Mangum, OK. (*Source:* U.S. Postal Service)
- **20.** Your part of the monthly apartment rent, which is \$213.70. You pay this to Amanda Dupre.

| Your Preprinted Name
Your Preprinted Address | 60-8124/7233
1000613331 | 1408 |
|---|----------------------------|---------|
| Tour Treprinted Address | DATE | |
| ΡΑΥΤΟ | 1.5 | \$ |
| THE ORDER OF | | |
| | | DOLLARS |
| FIRST STATE BANK | | |
| Мемо | | |
| :621497260: 1000613331 | 1408 | |

22. Your grocery bill of \$87.49 to Albertsons.

| 60-8124/7233
1000613331 | 1410 |
|----------------------------|---------|
| DATE | |
| | |
| | \$ |
| | |
| | |
| | DOLLARS |
| | |
| | |
| | |
| | |

Objective B *Write each decimal number in standard form. See Examples 6 and 7.*

- **23.** Six and five tenths
- **25.** Nine and eight hundredths

- **24.** Three and nine tenths
- **26.** Twelve and six hundredths

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- **27.** Seven hundred five and six hundred twenty-five thousandths
- **29.** Forty-six ten-thousandths

- **31.** The record rainfall amount for a 24-hour period in Alabama is thirty-two and fifty-two hundredths inches. This record was set at Dauphin Island Sea Lab in 1997. (*Source:* National Climatic Data Center)
- **33.** The average IndyCar burns one and threetenths gallons of fuel per lap at the Indianapolis Motor Speedway. (*Source:* Indianapolis Motor Speedway)

- **28.** Eight hundred four and three hundred ninety-nine thousandths
- **30.** Thirty-eight ten-thousandths
- **32.** For model year 2015, the average fuel economy for vehicles sold in the United States was twenty-four and eight tenths miles per gallon. (*Source:* U.S. Department of Transporation)
- **34.** The IZOD IndyCar series races at the Mid-Ohio Sports Car Course each season. The track length there is two and two hundred fifty-eight thousandths miles. (*Source:* IndyCar.com)

Objective C Write each decimal as a fraction or a mixed number. Write your answer in simplest form. See Examples 8 *through 12.*

| 35. 0.3 | 36. 0.9 | 37. 0.27 | 38. 0.39 |
|-------------------|-------------------|-------------------|-------------------|
| 39. 0.8 | 40. 0.4 | 41. 0.15 | 42. 0.64 |
| 43. 5.47 | 44. 6.3 | 45. 0.048 | 46. 0.082 |
| 47. 7.008 | 48. 9.005 | 49. 15.802 | 50. 11.406 |
| 51. 0.3005 | 52. 0.2006 | 53. 487.32 | 54. 298.62 |

Objective D Write each fraction as a decimal. See Examples 13 through 16.

| • 55. $\frac{6}{10}$ | 56. $\frac{3}{10}$ | 57. $\frac{45}{100}$ | 58. $\frac{75}{100}$ |
|------------------------------|------------------------------|--------------------------------|--------------------------------|
| 59. $\frac{37}{10}$ | 60. $\frac{28}{10}$ | 61. $\frac{268}{1000}$ | 62. $\frac{709}{1000}$ |
| 63. $\frac{9}{100}$ | 64. $\frac{7}{100}$ | 65. $\frac{4026}{1000}$ | 66. $\frac{3601}{1000}$ |
| 67. $\frac{28}{1000}$ | 68. $\frac{63}{1000}$ | 69. $\frac{563}{10}$ | 70. $\frac{206}{10}$ |

Objectives A B C D Mixed Practice *Fill in the chart. The first row is completed for you. See Examples 1 through 16.*

| | Decimal Number in
Standard Form | In Words | Fraction |
|-----|------------------------------------|-------------------------|------------------|
| | 0.37 | thirty-seven hundredths | $\frac{37}{100}$ |
| 71. | | | $\frac{43}{100}$ |
| 72. | | | $\frac{89}{100}$ |
| 73. | | eight tenths | |
| 74. | | five tenths | |
| 75. | 0.077 | | |
| 76. | 0.019 | | |

Review

Round 47,261 to the indicated place value. See Section 1.5.

77. tens

79. thousands

Concept Extensions

- **81.** In your own words, describe how to write a decimal as a fraction or a mixed number.
- **83.** Write 0.00026849576 in words.

78. hundreds

- 80. ten-thousands
- **82.** In your own words, describe how to write a fraction as a decimal.
- **84.** Write 0.00026849576 as a fraction. Do not simplify the resulting fraction.

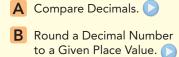
85. Write $17\frac{268}{1000}$ as a decimal.

86. Write
$$7\frac{12}{100}$$
 as a decimal.

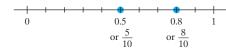
4.2 Order and Rounding 🔘

Objective A Comparing Decimals

Objectives



One way to compare decimals is to compare their graphs on a number line. Recall from Section 3.5 that for any two numbers on a number line, the number to the left is smaller and the number to the right is larger. The decimals 0.5 and 0.8 are graphed as follows:



Comparing decimals by comparing their graphs on a number line can be time consuming. Another way to compare the size of decimals is to compare digits in corresponding places.

Comparing Two Decimals

Compare digits in the same places from left to right. When two digits are not equal, the number with the larger digit is the larger decimal. If necessary, insert 0s after the last digit to the right of the decimal point to continue comparing.

| Compare hundredths-place digits | | | |
|---------------------------------|---|--------|--|
| 28.253 | | 28.263 | |
| 1 | | 1 | |
| 5 | < | 6 | |
| so 28.253 | < | 28.263 | |

Before we continue, let's take a moment and convince ourselves that inserting a zero after the last digit to the right of a decimal point does not change the value of the number.

For example, let's show that

0.7 = 0.70

If we write 0.7 as a fraction, we have

$$0.7 = \frac{7}{10}$$

Let's now multiply by 1. Recall that multiplying a number by 1 does not change the value of the number.

$$0.7 = \frac{7}{10} = \frac{7}{10} \cdot 1 = \frac{7}{10} \cdot \frac{10}{10} = \frac{7 \cdot 10}{10 \cdot 10} = \frac{70}{100} = 0.70$$

Thus 0.7 = 0.70 and so on.

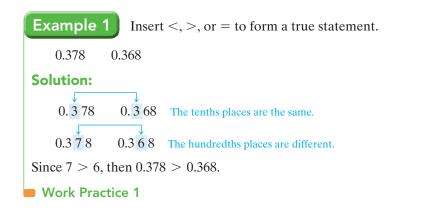
Helpful Hint

For any decimal, inserting 0s after the last digit to the right of the decimal point does not change the value of the number.

7.6 = 7.60 = 7.600, and so on

When a whole number is written as a decimal, the decimal point is placed to the right of the ones digit.

25 = 25.0 = 25.00, and so on



Practice 1

Answer

1. <

Insert <, >, or = to form a true statement.

13.208 13.281

Practice 2

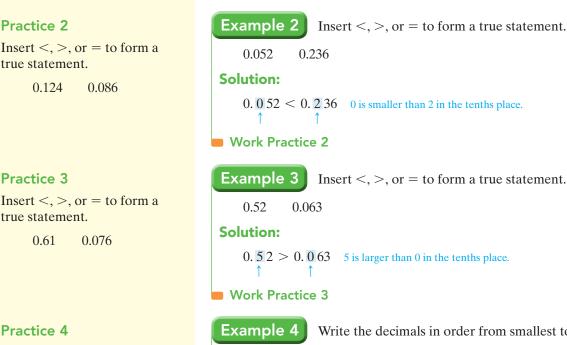
Practice 3

0.61

Practice 4

0.124

Chapter 4 | Decimals



Write the decimals in order from smallest to largest.

14.605, 14.65, 13.9, 14.006

Write the decimals in order from smallest to largest.

7.035, 8.12, 7.03, 7.1

Solution: By comparing the ones digits, the decimal 8.12 is the largest number. To write the rest of the decimals in order, we compare digits to the right of the decimal point. We will insert zeros to help us compare.

7.035 7.030 7.100

Helpful Hint

You may also immediately notice that 7.1 is larger than both 7.035 and 7.03.

By comparing digits to the right of the decimal point, we can now arrange the decimals from smallest to largest.

7.030, 7.035, 7.100, 8.12 or 7.03, 7.035, 7.1, 8.12

Work Practice 4

Objective **B** Rounding Decimals

We round the decimal part of a decimal number in nearly the same way as we round whole numbers. The only difference is that we delete digits to the right of the rounding place, instead of replacing these digits by 0s. For example,

24.954 rounded to the nearest hundredth is 24.95

1

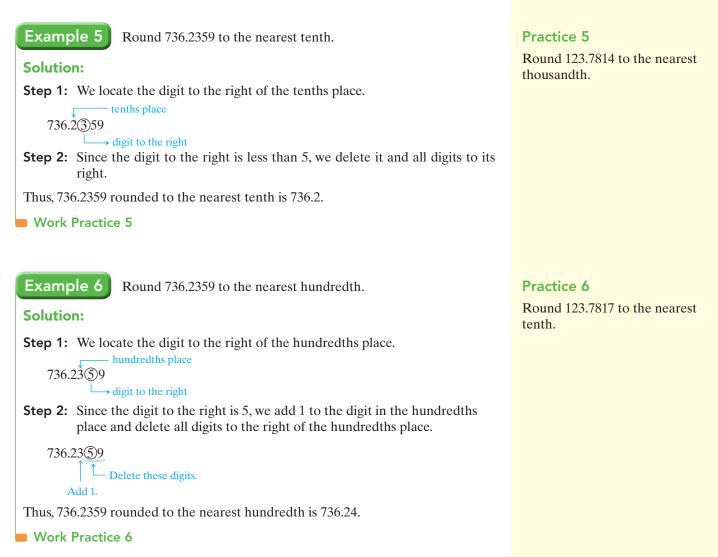
hundredths place

Rounding Decimals to a Place Value to the Right of the Decimal Point

- Step 1: Locate the digit to the right of the given place value.
- Step 2: If this digit is 5 or greater, add 1 to the digit in the given place value and delete all digits to its right. If this digit is less than 5, delete all digits to the right of the given place value.

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Answers 2. > 3. > 4. 13.9, 14.006, 14.605, 14.65



Rounding often occurs with money amounts. Since there are 100 cents in a dollar, each cent is $\frac{1}{100}$ of a dollar. This means that if we want to round to the nearest cent, we round to the nearest hundredth of a dollar.

Example 7

The price of a gallon of premium gasoline in Cross City is currently \$3.1779. Round this to the nearest cent.

Solution:

Since the digit to the right is greater than 5, we add 1 to the hundredths digit and delete all digits to the right of the hundredths digit.

Thus, \$3.1779 rounded to the nearest cent is \$3.18.

Work Practice 7

Practice 7

In Sandersville, the price of a gallon of premium gasoline is \$3.1589. Round this to the nearest cent.

260

Practice 8

nearest cent.

Round \$1.095 to the

Chapter 4 | Decimals



Round \$0.098 to the nearest cent.

Solution:

hundredths place ----- 8 is greater than 5 \$0.098 - Delete this digit. Add 1. Add 1.

9 + 1 = 10, so replace the digit 9 by 0 and carry the 1 to the place value to the left. Thus, \$0.098 rounded to the nearest cent is \$0.10.

A high school teacher's taxable income is \$41,567.72. The tax tables in the teacher's

state use amounts to the nearest dollar. Round the teacher's income to the nearest

Solution: Rounding to the nearest dollar means rounding to the ones place.

Work Practice 8

Concept Check 1756.0894 rounded to the nearest ten is

a. 1756.1 **b.** 1760.0894 **c.** 1760 **d.** 1750

Example 9 Determining State Taxable Income

Practice 9

Water bills in Gotham City are always rounded to the nearest dollar. Round a water bill of \$24.62 to the nearest dollar.

Thus, the teacher's income rounded to the nearest dollar is \$41,568.

 \uparrow \frown Delete these digits.

Work Practice 9

dollar.

In Section 4.4, we will introduce a formula for the distance around a circle. The distance around a circle is given the special name circumference.

The symbol π is the Greek letter pi, pronounced "pie." We use π to denote the following constant: circumference

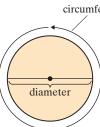
 $\pi = \frac{\text{circumference of } a \text{ circle}}{a \text{ circle}}$ diameter of a circle

ones place 7 is greater than 5

\$41,567.72

Add 1.

The value π is an **irrational number.** This means if we try to write it as a decimal, it neither ends nor repeats in a pattern.



Example 10 $\pi \approx 3.14159265$. Round π to the nearest hundredth.

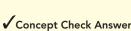
Solution:

hundredths place -1 is less than 5. 3.14159265 ↑____ Delete these digits.

Thus, 3.14159265 rounded to the nearest hundredth is 3.14. In other words, $\pi \approx 3.14$.

Work Practice 10





 $\pi \approx 3.14159265$. Round π to

the nearest ten-thousandth.

8. \$1.10 9. \$25 10. $\pi \approx 3.1416$

Practice 10

с

Answers

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Some choices may be used more than once or not at all.

before 7.0 diameter after 0.7 circumference

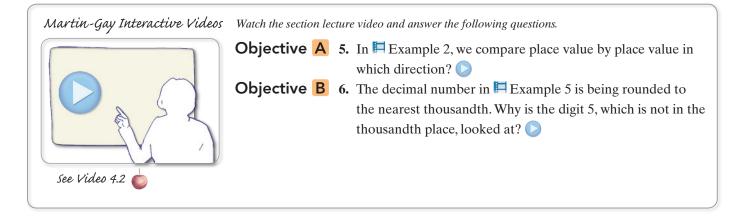
1. Another name for the distance around a circle is its _____

2. $\pi =$ of a circle

of a circle

3. The decimal point in a whole number is ______ the last digit.

4. The whole number 7 =_____.



| 4.2 Exercise Se | et MyLab Math 🜔 | | |
|--|-----------------------------------|------------------------------|-------------------------------|
| Objective A <i>Insert</i> <, > | , or $=$ to form a true statement | t. See Examples 1 through 3. | |
| 1. 0.15 0.16 | 2. 0.12 0.15 | 3. 0.57 0.54 | 4. 0.59 0.52 |
| 5. 0.098 0.1 | 6. 0.0756 0.2 | 7. 0.54900 0.549 | 8. 0.98400 0.984 |
| 9. 167.908 167.980 | 10. 519.3405 519.3054 | 11. 420,000 0.000042 | 12. 0.000987 987,000 |
| Write the decimals in order from smallest to largest. See Example 4. | | | |
| 13. 0.006, 0.06, 0.0061 | 14. 0.082, 0.008, | 0.080 15. 0. | 042, 0.36, 0.03 |
| 16. 0.21, 0.056, 0.065 | 17. 1.1, 1.16, 1.01 | 18. 3. | 6, 3.069, 3.09, 3.06 |
| 19. 21.001, 20.905, 21.03, 21.7 | 20. 36.050, 35.72 | 2, 35.702, 35.072 | |
| Objective B Round each decimal to the given place value. See Examples 5 through 10. | | | |
| 21. 0.57, to the nearest tenth | 22. 0.54, to the r | nearest tenth Q3. 0. | 234, to the nearest hundredth |

24. 0.452, to the nearest hundredth **25.** 0.5942, to the nearest thousandth **26.** 63.4523, to the nearest thousandth

| 27. 98,207.23, to the nearest ten | 28. 68,934.543, to the nearest ten | 29. 12.342, to the nearest tenth |
|---|---|--|
| 30. 42.9878, to the nearest thousandth | 31. 17.667, to the nearest hundredth | 32. 0.766, to the nearest hundredth |
| 33. 0.501, to the nearest tenth | 34. 0.602, to the nearest tenth | ● 35. 0.1295, to the nearest thousandth |
| 36. 0.8295, to the nearest thousandth | 37. 3829.34, to the nearest ten | 38. 4520.876, to the nearest hundred |

Round each monetary amount to the nearest cent or dollar as indicated. See Examples 7 through 9.

| 39. \$0.067, to the nearest cent | 40. \$0.025, to the nearest cent | 41. \$42,650.14, to the nearest dollar |
|--|---|---|
| 42. \$768.45, to the nearest dollar | 43. \$26.95, to the nearest dollar | 44. \$14,769.52, to the nearest dollar |
| 45. \$0.1992, to the nearest cent | 46. \$0.7633, to the nearest cent | |

Round each number to the given place value. See Examples 5 through 10.

47. The latest generation Apple MacBook Air, at its thinnest point, measures 0.2794 cm. Round this number to the nearest tenth. (*Source:* Apple, Inc.)



48. A large tropical cockroach of the family Dictyoptera is the fastest-moving insect. This insect was clocked at a speed of 3.36 miles per hour. Round this number to the nearest tenth. (*Source:* University of California, Berkeley)



49. During the 2016 Boston Marathon, Tatyana McFadden of America was the first female wheelchair competitor to cross the finish line. Her time was 1.725 hours. Round this time to the nearest hundredth. (*Source:* Boston Athletic Association)

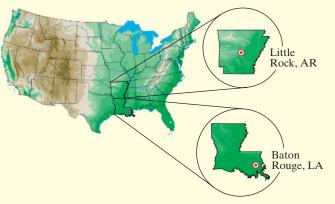


50. Mikaela Shiffrin of the U.S. Ski Team took first place in the women's giant slalom in the 2017 FIS World Cup in Squaw Valley, Idaho. Her winning time was 2.278 minutes. Round this time to the nearest hundredth of a minute. (*Source:* International Ski Federation)

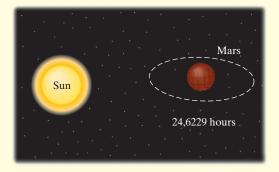


- **51.** A used biology textbook is priced at \$47.89. Round this price to the nearest dollar.
- **52.** A used office desk is advertised at \$49.95 by Drawley's Office Furniture. Round this price to the nearest dollar.

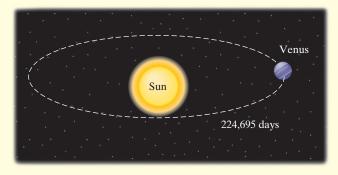
- **53.** The 2016 estimated population density of the state of Louisiana is 89.3559 people per square mile. Round this population density to the nearest tenth. (*Source:* U.S. Census Bureau)
- **54.** The 2016 estimated population density of the state of Arkansas is 56.0033 people per square mile. Round this population density to the nearest tenth. (*Source:* U.S. Census Bureau)



● 55. The length of a day on Mars is 24.6229 hours. Round this figure to the nearest thousandth. (*Source:* National Space Science Data Center)



57. Kingda Ka is a hydraulic-launch roller coaster at Six Flags Great Adventure, an amusement park in Jackson, New Jersey. Currently it is the world's tallest roller coaster. A ride on the Kingda Ka lasts about 0.4667 minute. Round this figure to the nearest tenth. (*Source:* Roller Coaster DataBase) **56.** Venus makes a complete orbit around the Sun every 224.695 days. Round this figure to the nearest whole day. (*Source:* National Space Science Data Center)



58. During the 2016 NFL season, the average length of a Los Angeles Ram's punt was 47.8 yards. Round this figure to the nearest whole yard. (*Source:* National Football League)

Review

Perform each indicated operation. See Sections 1.3 and 1.4.

| 59. 3452 + 2314 | 60. 8945 + 4536 | 61. 94 – 23 |
|------------------------|------------------------|------------------------|
| 62. 82 – 47 | 63. 482 – 239 | 64. 4002 - 3897 |

Concept Extensions

Solve. See the Concept Check in this section.

- 65. 2849.1738 rounded to the nearest hundred is
 a. 2849.17 b. 2800 c. 2850 d. 2849.174
- 66. 146.059 rounded to the nearest ten is
 a. 146.0 b. 146.1 c. 140 d. 150

- 67. 2849.1738 rounded to the nearest hundredth is
 a. 2849.17 b. 2800 c. 2850 d. 2849.174
- 68. 146.059 rounded to the nearest tenth isa. 146.0 b. 146.1 c. 140 d. 150

Mixed Practice (Sections 4.1 and 4.2) The table gives the average speed, in kilometers per hour, for the winners of the 24 Hours of Le Mans for each of the years listed. Use the table to answer Exercises 69 through 72. (Source: lemans-history.com)

| Year | Team | Average Speed (in kph) |
|------|--------------------------|------------------------|
| 2008 | Audi Sport North America | 216.300 |
| 2009 | Peugeot Sport Total | 216.664 |
| 2010 | Audi Sport North America | 225.228 |
| 2011 | Audi Sport Team Joest | 201.265 |
| 2012 | Audi Sport Team Joest | 214.500 |
| 2013 | Audi Sport Team Joest | 197.400 |
| 2014 | Audi Sport Team Joest | 214.927 |
| 2015 | Porsche Team | 224.200 |
| 2016 | Porsche Team | 217.503 |

- **73.** Write a 5-digit number that rounds to 1.7.
- **75.** Write a decimal number that is greater than 8 but less than 9.
- **77.** Which number(s) rounds to 0.26? 0.26559 0.26499 0.25786 0.25186

Write these numbers from smallest to largest.

| 79. 0.9 | 80. 0.01 |
|----------------|-----------------|
| 0.1038 | 0.0839 |
| 0.10299 | 0.09 |
| 0.1037 | 0.1 |

81. The all-time top six movies* (those that earned the most money in the World) along with the approximate amount of money they have earned are listed in the table. Estimate the total amount of money that these movies have earned by first rounding each earning to the nearest hundred million. (*Source:* The Internet Movie Database)

| Top All-Time Movies | |
|-------------------------------------|-------------------------|
| Movie | Gross Domestic Earnings |
| Avatar (2009) | \$2788.0 million |
| Titanic (1997) | \$2186.8 million |
| Star Wars: The Force Awakens (2015) | \$2068.2 million |
| Jurassic World (2015) | \$1670.4 million |
| Marvel's The Avengers (2012) | \$1518.8 million |
| Furious 7 | \$1516.0 million |

82. In 2016, 22.6 million Americans paid for subscriptions to various streaming music services. The revenue for these services was \$2479 million. Estimate the value of each subscription by rounding 22.6 and 2479 to the nearest ten million and then dividing. (*Source:* Recording Industry Association of America)

- **69.** What is the fastest average speed on the list? Write this speed as a mixed number. Which team achieved this average speed?
- **70.** What is the slowest average speed on the list? Write this speed as a mixed number. Which team achieved this average speed?
- **71.** Make a list of the average winning speeds in order from fastest to slowest for the years 2012 to 2015.
- **72.** Make a list of the average winning speed in order from fastest to slowest for the years 2008 to 2011.
- **74.** Write a 4-digit number that rounds to 26.3.
- **76.** Write a decimal number that is greater than 48.1, but less than 48.2.
- **78.** Which number(s) rounds to 0.06? 0.0612 0.066 0.0586 0.0506

264

4.3 Adding and Subtracting Decimals

Objective A Adding Decimals

Adding decimals is similar to adding whole numbers. We add digits in corresponding place values from right to left, carrying if necessary. To make sure that digits in corresponding place values are added, we line up the decimal points vertically.

Adding or Subtracting Decimals

- Step 1: Write the decimals so that the decimal points line up vertically.
- Step 2: Add or subtract as with whole numbers.
- Step 3: Place the decimal point in the sum or difference so that it lines up vertically with the decimal points in the problem.

In this section, we will insert zeros in decimal numbers so that place-value digits line up neatly. For instance, see Example 1.

| Example 1 Add: 23.85 + 1.604 |
|--|
| Solution: First we line up the decimal points vertically. |
| 23.850 Insert one 0 so that digits line up neatly. |
| + 1.604 |
| ↓
Line up decimal points. |
| Then we add the digits from right to left as for whole numbers. |
| 23.850 |
| + 1.604 |
| 25.454 |

Place the decimal point in the sum so that all decimal points line up.

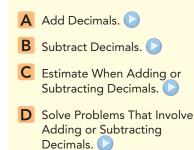
```
Work Practice 1
```

Helpful Hint

Recall that 0's may be placed after the last digit to the right of the decimal point without changing the value of the decimal. This may be used to help line up place values when adding decimals.

becomes 3.2 3.200 Insert two 0s. 15.567 15.567 + 0.110 Insert one 0. + 0.1118.877 Add.

Objectives



| Practice 1 | | |
|------------|----------------|--|
| A | ld. | |
| a. | 15.52 + 2.371 | |
| b. | 20.06 + 17.612 | |
| c. | 0.125 + 122.8 | |

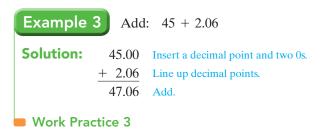
Chapter 4 | Decimals

Practice 2 Add. **a.** 34.567 + 129.43 + 2.8903 **b.** 11.21 + 46.013 + 362.526 Example 2 Add: 763.7651 + 22.001 + 43.89Solution: First we line up the decimal points. 763.765122.0010 Insert one 0. + 43.8900 Insert two 0s. 829.6561 Add.

Helpful Hint

Don't forget that the decimal point in a whole number is after the last digit.

Practice 3 Add: 26.072 + 119



Concept Check What is wrong with the following calculation of the sum of 7.03, 2.008, 19.16, and 3.1415?

| 7.03 |
|---------|
| 2.008 |
| 19.16 |
| +3.1415 |
| 3.6042 |

Objective B Subtracting Decimals

Subtracting decimals is similar to subtracting whole numbers. We line up digits and subtract from right to left, borrowing when needed.



Subtract: 35.218 – 23.65. Check your answer.

Solution: First we line up the decimal points.

| $4 \stackrel{11}{1} 11$ | |
|-------------------------|---------------|
| 3 <i>5.21</i> 8 | |
| -23.650 | Insert one 0. |
| 11.568 | Subtract. |

Recall that we can check a subtraction problem by adding.

| 11.568 | Difference |
|---------|------------|
| +23.650 | Subtrahend |
| 35.218 | Minuend |

Work Practice 4

Practice 4

Subtract. Check your answers. **a.** 82.75 - 15.9 **b.** 126.032 - 95.71

Answers

2. a. 166.8873 **b.** 419.749 **3.** 145.072 **4. a.** 66.85 **b.** 30.322

Concept Check Answer

The decimal points and places are not lined up properly.

| Example | 5 Subtract: 3.5 – 0.068. Ch | eck your answer. | F |
|-----------|--|--|-------------|
| Solution: | $\begin{array}{c} 4 \overset{\circ}{10} 10 \\ 3.5 \overset{\circ}{9} \overset{\circ}{9} \overset{\circ}{9} \end{array} \text{ Insert two 0s.} \\ \hline -0.0 \overset{\circ}{6} \overset{\circ}{8} \\ 3.4 \overset{\circ}{3} \overset{\circ}{2} \end{array} \text{ Line up decimal points.}$ | Check: 3.432 Difference
+0.068 Subtrahend
3.500 Minuend | s
a
t |
| Work Pra | ctice 5 | | |
| Example | 6 Subtract: 85 – 17.31. Cho | eck your answer. | F |
| Solution: | $ \begin{array}{r} 7 & 14 \\ $ | Check: $\begin{array}{c} 11 \ 1\\ 67.69 \end{array}$ Difference
$\begin{array}{c} +17.31\\ \hline 85.00 \end{array}$ Subtrahend | a |
| Work Pra | ctice 6 | | |

Practice 5 Subtract. Check your answers. **a.** 5.8 - 3.92 **b.** 9.72 - 4.068

Practice 6

Subtract. Check your answers. **a.** 53 - 29.31 **b.** 120 - 68.22

Objective C Estimating When Adding or Subtracting Decimals (>)

To help avoid errors, we can also estimate to see if our answer is reasonable when adding or subtracting decimals. Although only one estimate is needed per operation, we show two to show variety.

Example 7

Add or subtract as indicated. Then estimate to see if the answer is reasonable by rounding the given numbers and adding or subtracting the rounded numbers.

2

a. 27.6 + 519.25

Solution:

| Exact | | Estimate 1 | | Estimate 2 | |
|----------|-----------|------------|----|------------|--|
| 27.60 | rounds to | 30 | | 30 | |
| + 519.25 | rounds to | +500 | or | +520 | |
| 546.85 | | 530 | | 550 | |

Since the exact answer is close to either estimate, it is reasonable. (In the first estimate, each number is rounded to the place value of the leftmost digit. In the second estimate, each number is rounded to the nearest ten.)

b. 11.01 - 0.862

Work Practice 7

Solution:

| Exact | | Estimate 1 | | Estimate | |
|------------------|-----------|------------|----|------------|--|
| 091010
1X.ØXØ | rounds to | 10 | | 11 | |
| -0.862 | rounds to | <u>- 1</u> | or | <u>- 1</u> | |
| 10.148 | | 9 | | 10 | |

In the first estimate, we rounded the first number to the nearest ten and the second – number to the nearest one. In the second estimate, we rounded both numbers to the nearest one. Both estimates show us that our answer is reasonable.

Practice 7

Add or subtract as indicated. Then estimate to see if the answer is reasonable by rounding the given numbers and adding or subtracting the rounded numbers.

a. 48.1 + 326.97 **b.** 18.09 - 0.746

Helpful

Remember that estimates are for our convenience to quickly check the reasonableness of an answer.

Answers 5. a. 1.88 b. 5.652 6. a. 23.69 b. 51.78

7. a. 375.07 **b.** 17.344

Concept Check Why shouldn't the sum 21.98 + 42.36 be estimated as 30 + 50 = 80?

Objective D Solving Problems by Adding or Subtracting Decimals

Decimals are very common in real-life problems.

Practice 8

Find the total monthly cost of owning and operating a certain automobile given the expenses shown.

| Monthly car payment: | \$536.52 |
|----------------------------------|----------|
| Monthly | ¢550.52 |
| insurance cost: | \$ 52.68 |
| Average gasoline bill per month: | \$ 87.50 |

Answer 8. \$676.70

Concept Check Answer

Each number is rounded incorrectly. The estimate is too high.

Example 8

8 Calculating the Cost of Owning an Automobile

Find the total monthly cost of owning and operating a certain automobile given the expenses shown.

| Monthly car payment: | \$256.63 |
|----------------------------------|----------|
| Monthly insurance cost: | \$47.52 |
| Average gasoline bill per month: | \$95.33 |

Solution:

1. UNDERSTAND. Read and reread the problem. The phrase "total monthly cost" tells us to add.

2. TRANSLATE.

| In words: | total
monthly
cost | is | car
payment | plus | insurance
cost | plus | gasoline
bill |
|------------|--------------------------|--------------|----------------|--------------|-------------------|--------------|------------------|
| | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | |
| Translate: | total
monthly
cost | = | \$256.63 | + | \$47.52 | + | \$95.33 |

3. SOLVE: Let's also estimate by rounding each number to the nearest ten.

| 256.63 | rounds to | 260 | |
|---------|-----------|------|----------|
| 47.52 | rounds to | 50 | |
| + 95.33 | rounds to | +100 | |
| 399.48 | Exact | 410 | Estimate |

4. INTERPRET. *Check* your work. Since our estimate is close to our exact answer, our answer is reasonable. *State* your conclusion: The total monthly cost is \$399.48.

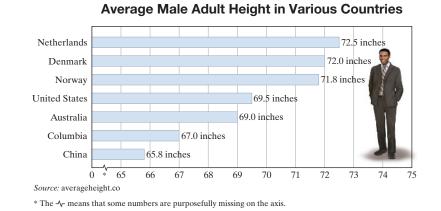
Work Practice 8

The bar graph in Example 9 has horizontal bars. Although the value of each bar in this example is labeled, to visualize the value represented by a bar, see how far it extends to the right. We will study bar graphs further in a later chapter.

Example 9

Comparing Average Heights

The bar graph on the next page shows the current average heights for male adults in various countries. How much greater is the average male height in the Netherlands than the average male height in Norway?

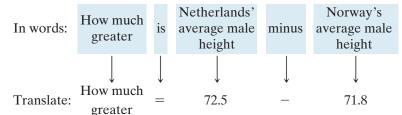


Practice 9

Use the bar graph in Example 9. How much greater is the average male height in Australia than the average male height in China?

Solution:

- **1.** UNDERSTAND. Read and reread the problem. Since we want to know "how much greater," we subtract.
- 2. TRANSLATE.



- 3. SOLVE: We also estimate by rounding each number to the nearest whole.
 - $\begin{array}{c|c} 7 \stackrel{1}{2} \stackrel{15}{,} \stackrel{15}{s} \quad \text{rounds to} \quad 73 \\ \hline -71.8 \quad \text{rounds to} \quad -72 \\ \hline 0.7 \quad \text{Exact} \quad 1 \text{ Estimate} \end{array}$
- **4.** INTERPRET. *Check* your work. Since our estimate is close to our exact answer, 0.7 inch is reasonable. *State* your conclusion: The average male height in the Netherlands is 0.7 inch greater than the Norway average male height.
- **Answer** 9. 3.2 in.

Work Practice 9

Calculator Explorations

Entering Decimal Numbers

To enter a decimal number, find the key marked \bigcirc . To enter the number 2.56, for example, press the keys $2 \bigcirc 5 6$.

The display will read 2.56.

Operations on Decimal Numbers

Operations on decimal numbers are performed in the same way as operations on whole numbers. For example, to find 8.625 - 4.29, press the keys $8.625 - 4.29 \equiv$ or ENTER.

The display will read 4.335. (Although entering 8.625, for example, requires pressing more than one key, we group numbers together here for easier reading.)

Use a calculator to perform each indicated operation.

| 1. | 315.782 + 12.96 |
|----|-----------------|
| 2. | 29.68 + 85.902 |
| 3. | 6.249 - 1.0076 |
| 4. | 5.238 - 0.682 |
| 5. | 12.555 |
| | 224.987 |
| | 5.2 |
| | +622.65 |
| 6. | 47.006 |
| | 0.17 |
| | 313.259 |
| | +139.088 |
| | |

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Not all choices will be used.

| minuend | vertically | first | true | 37.0 | horizontally |
|------------|------------|-------|-------|------|--------------|
| difference | subtrahend | last | false | 0.37 | |

1. The number 37 equals _____

the

2. The decimal point in a whole number is positioned after the ______ digit.

3. In 89.2 - 14.9 = 74.3, the number 74.3 is called the ______, 89.2 is the _____, and 14.9 is

- 4. To add or subtract decimals, we line up the decimal points _____
- 5. True or false: The number 5.6 is closer to 5 than 6 on a number line.

6. True or false: The number 10.48 is closer to 10 than 11 on a number line.

Martin-Gay Interactive Videos Watch the section lecture video and answer the following questions.

| | Objective A | 7. | From Example 2, what does lining up the decimal points |
|-----------------|-------------|-----|---|
| | Objective B | 8. | also line up? Why is this important?
From Example 3, where is the decimal point in a whole number? |
| | Objective C | 9. | In Example 5, estimating is used to check whether the answer to the subtraction problem is reasonable, but what is the best way to fully check? |
| see Video 4.3 🍅 | Objective D | 10. | Complete this statement based on Example 6: To calculate the amount of border material needed, we are actually calculating the of the triangle. |
| | | | calculating the of the triangle. |

4.3 Exercise Set MyLab Math 🜔

Objectives A C Mixed Practice *Add. See Examples 1 through 3 and 7. For those exercises marked, also estimate to see if the answer is reasonable.*

| 0 1. | 1.3 + 2.2 | 2. 2.5 + 4.1 | 3. 5.7 + 1.13 | 4. 2.31 + 6.4 | 5. 0.003 + 0.091 |
|-------------|--------------------|---------------------------|---------------------------|-----------------------|--------------------------|
| 6. | 0.004 + 0.085 | 7. 19.23 + 602.782 | 8. 47.14 + 409.567 | 9. 490 + 93.09 | 10. 600 + 83.0062 |
| 11. | 234.89
+ 230.67 | 12. | 734.89
+ 640.56 | 13. | 100.009
6.08 |
| | | Estimate: E | Exact: Estimate: | | + 9.034 |
| | | | | Exact: | Estimate: |
| 14. | 200.89 | • 15. 24 | 4.6 + 2.39 + 0.0678 | 16. 32.4 + | 1.58 + 0.0934 |
| | 7.49
+ 62.83 | | | | |
| | Exact: E | Estimate: | | | |

17. Find the sum of 45.023, 3.006, and 8.403

Objectives B C Mixed Practice *Subtract and check. See Examples 4 through 7. For those exercises marked, also estimate to see if the answer is reasonable.*

| 19. 8.8 – 2.3 | 20. 7.6 – 2.1 | ○ 21. 18 - 2.7 | 22. 28 - 3.3 | | | | |
|---|--|--|--|--|--|--|--|
| 23. 654.9
<u>- 56.67</u> | 24. 863.23
<u>- 39.453</u> | 25. 5.9 – 4.07
Exact:
Estimate: | 26. 6.4 – 3.04
Exact:
Estimate: | | | | |
| 27. 923.5 - 61.9 | 28. 845.93 - 45.8 | 29. 500.34 - 123.45 | 30. 600.74 - 463.98 | | | | |
| • 31. 1000
<u>- 123.4</u>
Exact: | 32. 2000
<u>– 327.47</u>
Exact: | 33. 200 – 5.6 | 34. 800 – 8.9 | | | | |
| Estimate: | Estimate: | | | | | | |
| 35. 3 - 0.0012 | 36. 7 - 0.097 | 37. Subtract 6.7 from 23. | 38. Subtract 9.2 from 45. | | | | |
| Objectives A B Mixed Practice Perform the indicated operation. See Examples 1 through 6. | | | | | | | |

| 39. 86.05 + 1.978 | 40. 95.07 + 4.216 | 41. 86.05 - 1.978 | 42. 95.07 - 4.216 |
|-------------------------------------|-------------------------------|-------------------------------------|--------------------------|
| 43. Add 150 and 93.17. | 44. Add 250 and 86.07. | 45. 150 - 93.17 | 46. 250 - 86.07 |
| 47. Subtract 8.94 from 12.1. | | 48. Subtract 6.73 from 20.2. | |

Objective D Solve. For Exercises 49 and 50, the solutions have been started for you. See Examples 8 and 9.

49. Ann-Margaret Tober bought a book for \$32.48. If she paid with two \$20 bills, what was her change?

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blank.)

| change | is | two
\$20 bills | minus | cost of
book |
|--------|--------------|-------------------|--------------|-----------------|
| | \downarrow | \downarrow | \downarrow | \downarrow |
| change | = | 40 | _ | |

Finish with

3. SOLVE and **4.** INTERPRET

50. Phillip Guillot bought a car part for \$18.26. If he paid with two \$10 bills, what was his change?

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blank.)

| change | is | two
\$10 bills | minus | cost of car part |
|--------|----------------------------|-------------------|--------------|------------------|
| change | $\stackrel{\downarrow}{=}$ | \downarrow 20 | \downarrow | \downarrow |

Finish with

3. SOLVE and **4.** INTERPRET

51. Find the total monthly cost of owning and maintaining a car given the information shown.

| Monthly car payment: | \$275.36 |
|-------------------------------------|----------|
| Monthly insurance cost: | \$ 83.00 |
| Average cost of gasoline per month: | \$ 81.60 |
| Average maintenance cost per month: | \$ 14.75 |

- **53.** Gasoline was \$2.839 per gallon one week and \$2.979 per gallon the next. By how much did the price change?
- **55.** Find the perimeter.

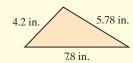


- **57.** The top face of an Apple iPod shuffle measures 1.14 inches by 1.24 inches. Find the perimeter of the rectangular face. (*Source:* Apple Inc.)
- **59.** The normal monthly average wind speed for April at the weather station on Mt. Washington in New Hampshire is 34.7 miles per hour. The highest speed ever recorded at the station, in April 1934, was 231.0 miles per hour. How much faster was the highest speed than the average April wind speed? (*Source:* Mount Washington Observatory)
- **61.** The average temperature for the contiguous United States during February 2017 was 41.2° Fahrenheit. This is 7.3° Fahrenheit above the 20th-century average temperature for February. What is the United States 20th-century average temperature for February? (*Source:* National Centers for Environmental Information)
- **63.** Andy Green still holds the record for one-mile land speed. This record was 129.567 miles per hour faster than a previous record of 633.468 set in 1983. What was Green's record-setting speed? (*Source:* United States Auto Club; this record was made in October 1997)

52. Find the total monthly cost of owning and maintaining a car given the information shown.

| Monthly car payment: | \$306.42 |
|-------------------------------------|----------|
| Monthly insurance cost: | \$ 53.50 |
| Average cost of gasoline per month: | \$123.00 |
| Average maintenance cost per month: | \$ 23.50 |

- **54.** A pair of eyeglasses costs a total of \$347.89. The frames of the glasses are \$97.23. How much do the lenses of the eyeglasses cost?
- **56.** Find the perimeter.



- **58.** The top face of the Apple iPad Mini 4 measures 8 inches by 5.3 inches. Find the perimeter of this rectangular face. (*Source:* Apple Inc.)
- **60.** In 2016, the average full-time American college student spent 3.65 hours on educational activities and 4.25 hours per day on leisure and sports. How much more time on average do American college students spend on leisure and sports activities than on educational activities? (*Source:* U.S. Bureau of Labor Statistics)
- **62.** Historically, the average rainfall for the month of May in Omaha, Nebraska, is 4.79 inches. In May 2016, Omaha received 4.84 inches of rain. By how much was Omaha's rain above average? (*Source:* Weather Underground)
- **64.** It costs \$7.20 to send a 2-pound package locally via Priority Mail at a U.S. Post Office. To send the same package as Express Mail, it costs \$23.75. How much more does it cost to send a package as Express Mail? (*Source:* USPS)

65. The face of the Apple iPhone 7 is a rectangle measuring 5.44 inches by 2.64 inches. Find the perimeter of this rectangular phone. (*Source:* Apple Inc.)



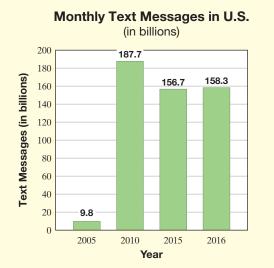
67. The average U.S. movie theater ticket price in 2016 was \$8.65. In 2015 it was \$8.43. Find the increase in the average movie theater ticket price from 2015 to 2016. (*Source:* Motion Picture Association of America)

66. The Samsung Galaxy S8, an Android-based smartphone and a leading iPhone competitor, measures 2.68 inches by 5.86 inches. Find the perimeter of this rectangular phone. (*Source:* Samsung Electronics Co)



68. The average U.S. movie theater ticket price in 2007 was \$6.88. For 2017, it was estimated to be \$8.87. Find the increase in the average movie theater ticket price for this 10-year period. (*Source:* Motion Picture Association of America)

This bar graph shows the average number of text messages sent each month in the United States for the years shown. Use this graph to answer Exercises 69 and 70. (Source: CTIA – The Wireless Association)



71. The snowiest city in the United States is Valdez, Alaska, which receives an average of 85.7 more inches of snow than the second snowiest city. The second snowiest city in the United States is Blue Canyon, California. Blue Canyon receives an average of 240.3 inches of snow annually. How much snow does Valdez receive on average each year? (Source: National Climatic Data Center)

- **69.** Find the decrease in monthly text messages from 2010 to 2016.
- **70.** Find the increase in monthly text messages from 2005 to 2010.

72. The driest city in the world is Aswan, Egypt, which receives an average of only 0.02 inch of rain per year. Yuma, Arizona, is the driest city in the United States. Yuma receives an average of 2.63 more inches of rain each year than Aswan. What is the average annual rainfall in Yuma? (*Source:* National Climatic Data Center)

- ▶ 73. A landscape architect is planning a border for a flower garden shaped like a triangle. The sides of the garden measure 12.4 feet, 29.34 feet, and 25.7 feet. Find the amount of border material needed.
 - 29.34 feet 12.4 feet 25.7 feet
- \triangle **74.** A contractor purchased enough railing to completely enclose the newly built deck shown below. Find the amount of railing purchased.



The table shows the average retail price of a gallon of gasoline (all grades and formulations) in the United States in each of the years shown. Use this table to answer Exercises 75 and 76. (Source: Energy Information Administration)

| Year | Gasoline Price (dollars per gallon) |
|------|-------------------------------------|
| 2012 | 3.695 |
| 2013 | 3.505 |
| 2014 | 3.358 |
| 2015 | 2.429 |
| 2016 | 2.143 |

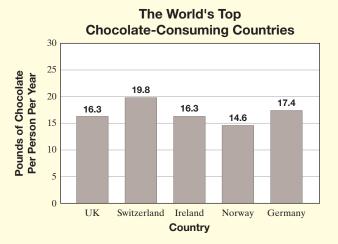
- **75.** How much less was the average cost of a gallon of gasoline in 2016 than in 2012?
- **76.** How much more was the average cost of a gallon of gasoline in 2013 than in 2014?

The following table shows spaceflight information for astronaut James A. Lovell. Use this table to answer Exercises 77 and 78.

| Spaceflights of James A. Lovell | | | |
|---------------------------------|-----------|---------------------|--|
| Year | Mission | Duration (in hours) | |
| 1965 | Gemini 6 | 330.583 | |
| 1966 | Gemini 12 | 94.567 | |
| 1968 | Apollo 8 | 147.0 | |
| 1970 | Apollo 13 | 142.9 | |
| (Source: NASA) | | | |

- **77.** Find the total time spent in spaceflight by astronaut James A. Lovell.
- **78.** Find the total time James A. Lovell spent in spaceflight on all Apollo missions.

The bar graph shows the top five chocolate-consuming nations in the world in 2016. Use this table to answer Exercises 79 through 84.



- **79.** Which country in the bar graph has the greatest chocolate consumption per person?
- **80.** Which country in the bar graph has the least chocolate consumption per person?
- **81.** How much more is the greatest chocolate consumption than the least chocolate consumption shown in the bar graph?
- **82.** How much more chocolate does the average German citizen consume per year than the average Irish?

- **83.** Make a table listing the countries and their corresponding chocolate consumptions in order from greatest to least.
- **84.** Find the sum of the five bar heights shown in the graph. What type of company might be interested in this sum?

| Revi | ew | |
|------|----|--|
| | | |

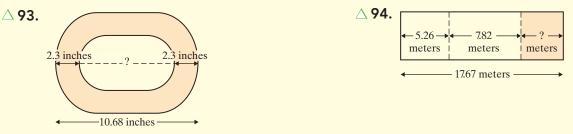
| Multiply. See Sections 1.6 and 3.5. | | | | | |
|-------------------------------------|-----------------|--------------------|--------------------|---|---|
| 85. 23 · 2 | 86. 46·3 | 87. 43 • 90 | 88. 30 · 32 | 89. $\left(\frac{2}{3}\right)^2$ | 90. $\left(\frac{1}{5}\right)^3$ |

Concept Extensions

A friend asks you to check his calculations for Exercises 91 and 92. Are they correct? If not, explain your friend's errors and correct the calculations. See the first Concept Check in this section.

| 91. | 9.2 | 92. | 8999
900.0 |
|-----|-------|-----|---------------|
| | 8.63 | | - 96.4 |
| 4 | 4.005 | | 803.5 |
| | 4.960 | | |

Find the unknown length in each figure.



Let's review the values of these common U.S. coins in order to answer the following exercises.



For Exercises 95 and 96, write the value of each group of coins. To do so, it is usually easiest to start with the coin(s) of greatest value and end with the coin(s) of least value.





- **97.** Name the different ways that coins can have a value of \$0.17 given that you may use no more than 10 coins.
- 99. Why shouldn't the sum

82.95 + 51.26be estimated as 90 + 60 = 150? See the second Concept Check in this section.

101. Explain how adding or subtracting decimals is similar to adding or subtracting whole numbers.

- **98.** Name the different ways that coin(s) can have a value of \$0.25 given that there are no pennies.
- **100.** Laser beams can be used to measure the distance to the moon. One measurement showed the distance to the moon to be 256,435.235 miles. A later measurement showed that the distance is 256,436.012 miles. Find how much farther away the moon is in the second measurement as compared to the first.
- **102.** Explain how adding or subtracting decimals is different from adding or subtracting whole numbers.

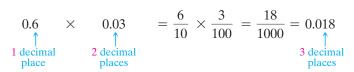
Objectives

- A Multiply Decimals. >
- B Estimate When Multiplying Decimals.
- C Multiply by Powers of 10. 🜔
- **D** Find the Circumference of a Circle.
- E Solve Problems by Multiplying Decimals. (>

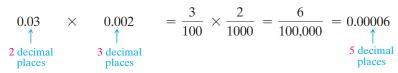
4.4 Multiplying Decimals and Circumference of a Circle

Objective 🗛 Multiplying Decimals 🕗

Multiplying decimals is similar to multiplying whole numbers. The only difference is that we place a decimal point in the product. To discover where a decimal point is placed in the product, let's multiply 0.6×0.03 . We first write each decimal as an equivalent fraction and then multiply.



Notice that 1 + 2 = 3, the number of decimal places in the product. Now let's multiply 0.03×0.002 .



Again, we see that 2 + 3 = 5, the number of decimal places in the product. Instead of writing decimals as fractions each time we want to multiply, we notice a pattern from these examples and state a rule that we can use:

Multiplying Decimals

- Step 1: Multiply the decimals as though they are whole numbers.
- **Step 2:** The decimal point in the product is placed so that the number of decimal places in the product is equal to the *sum* of the number of decimal places in the factors.

| Example 1 Multiply: 23.6×0.78 | Practice 1 |
|---|--|
| Solution: 23.6 1 decimal place
$\frac{\times 0.78}{1888} = 2 \text{ decimal places}$ $\frac{16520}{18.408}$ Since 1 + 2 = 3, insert the
decimal point in the product so
that there are 3 decimal places. | Multiply: 45.9 × 0.42 |
| Work Practice 1 | |
| Example 2 Multiply: 0.283×0.3 | Practice 2Multiply: 0.112×0.6 |
| Solution: 0.283 3 decimal places
\times 0.3 1 decimal place | Multiply: 0.112×0.0 |
| 0.0849 Since $3 + 1 = 4$, insert the
decimal point in the product so
that there are 4 decimal places.
Insert one 0 since the product
must have 4 decimal places. | |
| Work Practice 2 | |
| Example 3 Multiply: 0.0531×16 | Practice 3 |
| Solution: 0.0531 4 decimal places
$\frac{\times 16}{3186} 0 \text{ decimal places}$ $\frac{5310}{0.8496}$ $1 \text{ decimal places } (4 + 0 = 4)$ | Multiply: 0.0721 × 48 |
| Work Practice 3 | |
| | |

✓ Concept Check True or false? The number of decimal places in the product of 0.261 and 0.78 is 6. Explain.

Objective B Estimating When Multiplying Decimals 🕗

Just as for addition and subtraction, we can estimate when multiplying decimals to check the reasonableness of our answer.

Example 4 M

Multiply: 28.06×1.95 . Then estimate to see whether the answer is reasonable by rounding each factor, then multiplying the rounded numbers.

Solution:

| Exact: | Estim | ate 1 | Estima | te 2 | |
|---|------------|-----------------|------------|-----------------|--|
| 28.06 | 28 | Rounded to ones | 30 | Rounded to tens | |
| × 1.95 | $\times 2$ | Rounded to ones | \times 2 | Rounded to ones | |
| 14030 | 56 | | 60 | | |
| 252540 | | | | | |
| 280600 | | | | | |
| 54.7170 | | | | | |
| The answer 54.7170 (or 54.717) is reasonable. | | | | | |

Work Practice 4

277

Practice 4

Multiply: 30.26×2.98 . Then estimate to see whether the answer is reasonable.

Answers

1. 19.278 **2.** 0.0672 **3.** 3.4608 **4.** 90.1748

Concept Check Answer

false: 3 decimal places and 2 decimal places means 5 decimal places in the product

Chapter 4 | Decimals

As shown in Example 4, estimated results will vary depending on what estimates are used. Notice that estimating results is a good way to see whether the decimal point has been correctly placed.

Objective C Multiplying by Powers of 10 🕑

There are some patterns that occur when we multiply a number by a power of 10 such as 10, 100, 1000, 10,000, and so on.

| $23.6951 \times 10 = 236.951$ | Move the decimal point 1 place to the right. |
|---------------------------------------|--|
| | |
| 1 zero | |
| $23.6951 \times 100 = 2369.51$ | Move the decimal point 2 places to the right. |
| $\uparrow \qquad $ | |
| 2 zeros | |
| $23.6951 \times 100,000 = 2,369,510.$ | Move the decimal point 5 places to the right (insert a 0). |
| \uparrow | |
| 5 zeros | |

Notice that we move the decimal point the same number of places as there are zeros in the power of 10.

Multiplying Decimals by Powers of 10 such as 10, 100, 1000, 10,000...

Move the decimal point to the *right* the same number of places as there are *zeros* in the power of 10.

| Examples Multiply. | |
|--|--------|
| 5. $7.68 \times 10 = 76.8$ | 7.68 |
| 6. $23.702 \times 100 = 2370.2$ | 23.702 |
| 7. $76.3 \times 1000 = 76,300$ | 76.300 |
| Work Practice 5–7 | |

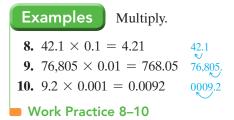
There are also powers of 10 that are less than 1. The decimals 0.1, 0.01, 0.001, 0.0001, and so on are examples of powers of 10 less than 1. Notice the pattern when we multiply by these powers of 10:

| $569.2 \times 0.1 = 56.92$
$\uparrow \qquad \swarrow$
1 decimal place | Move the decimal point <i>1 place</i> to the <i>left</i> . |
|---|---|
| $569.2 \times 0.01 = 5.692$ \uparrow 2 decimal places | Move the decimal point 2 <i>places</i> to the <i>left</i> . |
| $569.2 \times 0.0001 = 0.05692$ \uparrow 4 decimal places | Move the decimal point <i>4 places</i> to the <i>left</i> (insert one 0). |

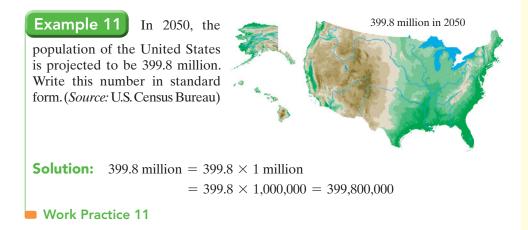
Multiplying Decimals by Powers of 10 such as 0.1, 0.01, 0.001, 0.0001...

Move the decimal point to the *left* the same number of places as there are *decimal places* in the power of 10.

Practice 5–7
Multiply.
5. 23.7 × 10
6. 203.004 × 100
7. 1.15 × 1000

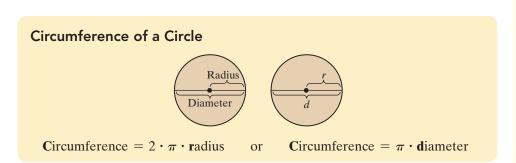


Many times we see large numbers written, for example, in the form 451.8 million rather than in the longer standard form. The next example shows us how to interpret these numbers.

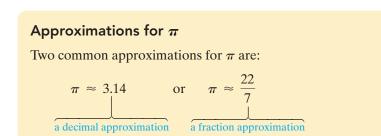


Objective D Finding the Circumference of a Circle 💟

Recall from Section 1.3 that the distance around a polygon is called its perimeter. The distance around a circle is given the special name **circumference**, and this distance depends on the radius or the diameter of the circle.



In Section 4.2, we learned about the symbol π as the Greek letter pi, pronounced "pie." It is a constant between 3 and 4.



Practice 8–10
Multiply.
8. 7.62 × 0.1
9. 1.9 × 0.01
10. 7682 × 0.001

Practice 11

In 2020, the population of the United States is projected to be 333.9 million. Write this number in standard form. (*Source:* U.S. Census Bureau)

Answers 8. 0.762 9. 0.019 10. 7.682 11. 333,900,000

Practice 12

Find the circumference of a circle whose radius is 11 meters. Then use the approximation 3.14 for π to approximate this circumference.

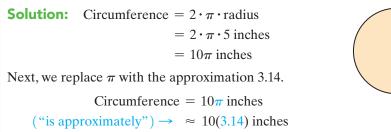
Practice 13

A biology major is fertilizing her garden. She uses 5.6 ounces of fertilizer per square yard. The garden measures 60.5 square yards. How much fertilizer does she need?

Chapter 4 | Decimals

Example 12 Circumference of a Circle

Find the circumference of a circle whose radius is 5 inches. Then use the approximation 3.14 for π to approximate the circumference.



= 31.4 inches

5 inche

The *exact* circumference or distance around the circle is 10π inches, which is *approximately* 31.4 inches.

Work Practice 12

Objective E Solving Problems by Multiplying Decimals 📀

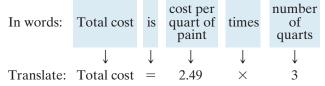
The solutions to many real-life problems are found by multiplying decimals. We continue using our four problem-solving steps to solve such problems.

Example 13 Finding the Total Cost of Materials for a Job

A college student is hired to paint a billboard with paint costing \$2.49 per quart. If the job requires 3 quarts of paint, what is the total cost of the paint?

Solution:

- **1.** UNDERSTAND. Read and reread the problem. The phrase "total cost" might make us think addition, but since this problem requires repeated addition, let's multiply.
- 2. TRANSLATE.



3. SOLVE. We can estimate to check our calculations. The number 2.49 rounds to $2 \text{ and } 2 \times 3 = 6$.

 $\begin{array}{r}
 \begin{array}{r}
 1 & 2 \\
 2.49 \\
 \times & 3 \\
 \overline{7.47}
\end{array}$

4. INTERPRET. *Check* your work. Since 7.47 is close to our estimate of 6, our answer is reasonable. *State* your conclusion: The total cost of the paint is \$7.47.

```
Work Practice 13
```

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Vocabulary, Readiness & Video Check

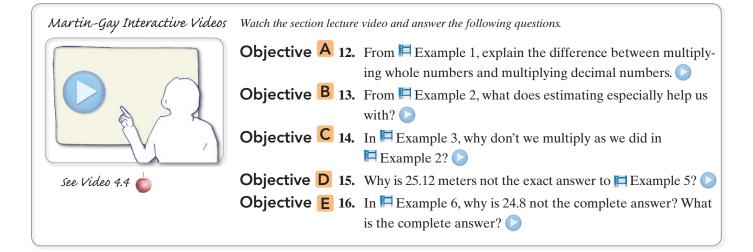
Use the choices below to fill in each blank.

| circumference | left | sum | zeros |
|----------------|-------|---------|--------|
| decimal places | right | product | factor |

- 1. When multiplying decimals, the number of decimal places in the product is equal to the ______ of the number of decimal places in the factors.
- 2. In $8.6 \times 5 = 43$, the number 43 is called the _____, while 8.6 and 5 are each called a(n) _____
- **3.** When multiplying a decimal number by powers of 10, such as 10, 100, 1000, and so on, we move the decimal point in the number to the ______ the same number of places as there are ______ in the power of 10.
- 4. When multiplying a decimal number by powers of 10, such as 0.1, 0.01, and so on, we move the decimal point in the number to the ______ the same number of places as there are ______ in the power of 10.
- 5. The distance around a circle is called its _____

Do not multiply. Just give the number of decimal places in the product. See the Concept Check in this section.

| 6. 0.46 | 7. 57.9 | 8. 0.428 | 9. 0.0073 | 10. 0.028 | 11. 5.1296 |
|----------------|----------------|-----------------|------------------|------------------|-------------------|
| $\times 0.81$ | $\times 0.36$ | \times 0.2 | \times 21 | \times 1.36 | ×7.3987 |



4.4 Exercise Set MyLab Math

Objectives A B Mixed Practice *Multiply. See Examples 1 through 4. For those exercises marked, also estimate to see if the answer is reasonable.*

| 1. 0.2 $\times 0.6$ | 2. 0.7 $\times 0.9$ | 3. 1.2 $\times 0.5$ | 4. 6.8 $\times 0.3$ |
|------------------------------|----------------------------|---|---|
| 5. 0.26 × 5 | 6. 0.19 × 6 | 7. 5.3 × 4.2
Exact:
Estimate: | 8. 6.2 × 3.8
Exact:
Estimate: |
| 9. 0.576 \times 0.7 | 10. 0.971
× 0.5 | Q11. 1.0047
$\times 8.2$ Exact: Estimate: | 12. 2.0005
\times 5.5
Exact: Estimate: |

| 13. 490.2
<u>× 0.023</u> | 14. 300.9
<u>× 0.032</u> | 15. Multiply 16.003 and 5.31 | 16. Multiply 31.006 and 3.71 |
|------------------------------------|------------------------------------|-------------------------------------|-------------------------------------|
| Objective C Multiply. Se | e Examples 5 through 10. | | |
| 17. 6.5 × 10 | 18. 7.2 × 10 | 19. 6.5 × 0.1 | 20. 4.7 × 0.1 |
| 21. 7.2 × 0.01 | 22. 0.06 × 0.01 | ○23. 7.093 × 100 | 24. 0.5 × 100 |
| 25. 6.046 × 1000 | 26. 9.1 × 1000 | ○27. 37.62 × 0.001 | 28. 14.3 × 0.001 |
| Objectives A B C Mi | ixed Practice Multiply. S | ee Examples 1 through 10. | |
| 29. 0.123 × 0.4 | 30. 0.216 × 0.3 | 31. 0.123 × 100 | 32. 0.216 × 100 |
| 33. 8.6 × 0.15 | 34. 0.42 × 5.7 | 35. 9.6 × 0.01 | 36. 5.7 × 0.01 |
| 37. 562.3 × 0.001 | 38. 993.5 × 0.001 | 39. 5.62 | 40. 8.03 |

Chapter 4 | Decimals

Write each number in standard form. See Example 11.

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- **41.** The storage silos at the main Hershey chocolate factory in Hershey, Pennsylvania, can hold enough cocoa beans to make 5.5 billion Hershey's milk chocolate bars. (*Source:* Hershey Foods Corporation)
- **43.** The Racer is the most-ridden roller coaster at King's Island, an amusement park near Cincinnati, Ohio. Since 1972, it has given more than 97.8 million rides. (*Source:* Cedar Fair, L.P.)
- **45.** The most-visited national park in the United States in 2016 was the Golden Gate National Recreation Area in San Francisco, California. An estimated 292.3 thousand people visited the park each week that year. (*Source:* National Park Service)



42. The total domestic revenue collected by Netflix in 2016 was \$8.831 billion. (*Source:* Netflix, Inc.)

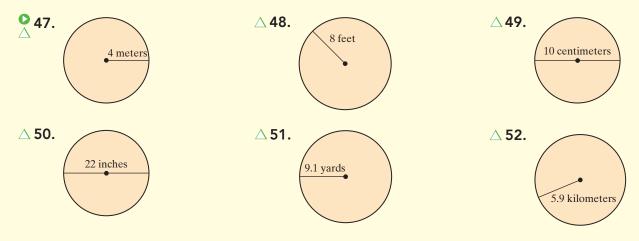
 \times 5.5

 \times 7.7

- **44.** In 2016, about 60.2 million American households owned at least one dog. (*Source:* American Pet Products Association)
- **46.** In 2016, approximately 13.1 thousand vessels passed through the Panama Canal. (*Source:* Autoridad del Canal de Panama)



Objective D *Find the circumference of each circle. Then use the approximation 3.14 for* π *and approximate each circumference. See Example 12.*

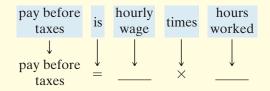


Objectives D E Mixed Practice Solve. For Exercises 53 and 54, the solutions have been started for you. See Examples 12 and 13. For circumference applications, find the exact circumference and then use 3.14 for π to approximate the circumference.

53. An electrician for Central Power and Light worked 40 hours last week. Calculate his pay before taxes for last week if his hourly wage is \$17.88.

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blanks.)



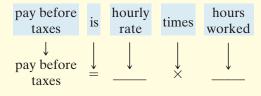
Finish with: **3.** SOLVE and **4.** INTERPRET.

- **55.** Under certain conditions, the average cost of driving a medium sedan in 2016 was \$0.59 per mile. How much would it have cost to drive such a car 15,000 miles in 2016? (*Source:* American Automobile Association)
- ▶ 57. A 1-ounce serving of cream cheese contains 6.2 grams of saturated fat. How much saturated fat is in 4 ounces of cream cheese? (*Source: Home and Garden Bulletin No. 72;* U.S. Department of Agriculture)

54. An assembly line worker worked 20 hours last week. Her hourly rate is \$19.52 per hour. Calculate her pay before taxes.

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blanks.)



Finish with:**3.** SOLVE and **4.** INTERPRET.

- **56.** In 2015, a U.S. airline passenger paid an average of \$0.1302, disregarding taxes and fees, to fly 1 mile. Use this number to calculate the cost before taxes and fees to fly from Atlanta, Georgia, to Minneapolis, Minnesota, a distance of 905 miles. Round to the nearest cent. (*Source:* Airlines for America)
- **58.** A 3.5-ounce serving of lobster meat contains 0.1 gram of saturated fat. How much saturated fat do 3 servings of lobster meat contain? (*Source:* The National Institutes of Health)

 \triangle **59.** Recall that the face of the Apple iPhone 7 (see Section 4.3) is a rectangle measuring 5.44 inches by 2.64 inches. Find the area of the face of the Apple iPhone 7. Round to the nearest hundredth. (*Source:* Apple, Inc.)



- \triangle **61.** In 1893, the first ride called a Ferris wheel was constructed by Washington Gale Ferris. Its diameter was 250 feet. Find its circumference. Give the exact answer and an approximation using 3.14 for π . (*Source: The Handy Science Answer Book,* Visible Ink Press, 1994)
- \triangle **63.** The London Eye, built for the Millennium celebration in London, resembles a gigantic Ferris wheel with a diameter of 135 meters. If Adam Hawn rides the Eye for one revolution, find how far he travels. Give the exact answer and an approximation using 3.14 for π . (*Source:* Londoneye.com)



 \triangle **60.** Recall that the rectangular face of the Samsung Galaxy S8 smartphone (see Section 4.3) measures 2.68 inches by 5.86 inches. Find the area of the face of the Samsung Galaxy S8. Round to the nearest hundredth. (*Source:* Samsung Electronics Co.)

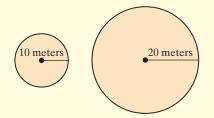


- \triangle **62.** The radius of Earth is approximately 3950 miles. Find the distance around Earth at the equator. Give the exact answer and an approximation using 3.14 for π . (*Hint:* Find the circumference of a circle with radius 3950 miles.)
- \triangle **64.** The world's longest suspension bridge is the Akashi Kaikyo Bridge in Japan. This bridge has two circular caissons, which are underwater foundations. If the diameter of a caisson is 80 meters, find its circumference. Give the exact answer and an approximation using 3.14 for π . (*Source: Scientific American;* How Things Work Today)



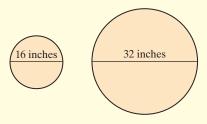
- **65.** A meter is a unit of length in the metric system that is approximately equal to 39.37 inches. Sophia Wagner is 1.65 meters tall. Find her approximate height in inches.
- **66.** The doorway to a room is 2.15 meters tall. Approximate this height in inches. (*Hint:* See Exercise **65**.)

 \triangle 67. a. Approximate the circumference of each circle.



- **b.** If the radius of a circle is doubled, is its corresponding circumference doubled?
- **69.** The top face of the Apple iPad Mini 4 (see Section 4.3) measures 8 inches by 5.3 inches. Find the area of the face of the iPad Mini 4. (*Source:* Apple, Inc.)

 \triangle **68. a.** Approximate the circumference of each circle.



- **b.** If the diameter of a circle is doubled, is its corresponding circumference doubled?
- **70.** The top face of the Apple iPod shuffle (see Section 4.3) measures 1.14 inches by 1.24 inches. Find the area of the face of the iPod shuffle. Round to the nearest hundredth. (*Source:* Apple, Inc.)

Review

Divide. See Sections 1.7 and 2.5.

| 71. 130 ÷ 5 | 72. 486 ÷ 27 | 73. 2016 ÷ 56 | 74. 1863 ÷ 69 |
|-----------------------|---------------------|---|---|
| 75. 2920 ÷ 365 | 76. 2916 ÷ 6 | 77. $\frac{24}{7} \div \frac{8}{21}$ | 78. $\frac{162}{25} \div \frac{9}{75}$ |

Concept Extensions

| Mixed Practice | (Sections 4. | 3 and 4.4) | Perform the in | ndicated operations. |
|-----------------------|--------------|------------|----------------|----------------------|
|-----------------------|--------------|------------|----------------|----------------------|

| 79. 3.6 + 0.04 | 80. 7.2 + 0.14 + 98.6 | 81. 3.6 - 0.04 |
|-----------------------|------------------------------|-----------------------|
| 82. 100 - 48.6 | 83. 0.221 × 0.5 | 84. 3.6 × 0.04 |

- **85.** Find how far radio waves travel in 20.6 seconds. (Radio waves travel at a speed of 1.86 × 100,000 miles per second.)
- **87.** In your own words, explain how to find the number of decimal places in a product of decimal numbers.
- **89.** Write down two decimal numbers whose product will contain 5 decimal places. Without multiplying, explain how you know your answer is correct.
- **86.** If it takes radio waves approximately 8.3 minutes to travel from the Sun to the Earth, find approximately how far it is from the Sun to the Earth. (*Hint:* See Exercise **85**.)
- **88.** In your own words, explain how to multiply by a power of 10.
- **90.** Explain the process for multiplying a decimal number by a power of 10.

Integrated Review

Sections 4.1–4.4

Operations on Decimals

| Answers | Perform the indicated | d operations. | | |
|---------|--------------------------------|-----------------------|--------------------------------|--------------------------|
| 1. | 1. 1.6 + 0.97 | 2. 3.2 + 0.85 | 3. 9.8 - 0.9 | 4. 10.2 - 6.7 |
| 2. | | | | |
| 3. | | | | |
| 4. | 5. 0.8 | 6. 0.6 | 7. 8 + 2.16 + 0.9 | 8. 6 + 3.12 + 0.6 |
| 5. | $\times 0.2$ | $\times 0.4$ | 7. 6 + 2.10 + 0.9 | 0. 0 + 3.12 + 0.0 |
| 6. | | | | |
| 7. | | | | |
| 8. | 9. 9.6 | 10. 8.7 | 11. 123.6 | 12. 325.2 |
| 9. | $\times 0.5$ | $\times 0.7$ | - 48.04 | - 36.08 |
| 10. | | | | |
| 11. | | | | |
| 12. | 13. 25 + 0.026 | 14. 0.125 + 44 | 15. 100 - 17.3 | 16. 300 - 26.1 |
| 13. | | | | |
| 14. | | | | |
| 15. | 17. 2.8 × 100 | 18. 1.6 × 1000 | 19. 96.21 | 20. 0.268 |
| 16. | | | 7.028
+ 121.7 | 1.93
+ 142.881 |
| 17. | | | | |
| 18. | | | | |
| 19. | 21. Find the produce | ct of 1.2 and 5 | 22. Find the sum of | 12 and 5 |
| 20. | | | | |
| 21. | | | | |
| 22. | 22 12 004 | | 24 20.000 | |
| 23. | 23. 12.004 \times 2.3 | | 24. 28.006×5.2 | |
| 24. | | | | |
| 25. | | | | |
| 26. | 25. Subtract 4.6 fro | om 10. | 26. Subtract 0.26 from | om 18. |

Integrated Review

| | | integrated Keview | 207 |
|-----|---|--|------------|
| 27. | 268.19
+ 146.25 | 28. 860.18
+ 434.85 | 27 |
| | | | 28. |
| 29. | 160 - 43.19 | 30. 120 - 101.21 | 29 |
| | | | 30. |
| 31. | 15.62×10 | 32. 15.62 + 10 | 31. |
| 22 | 15 (2) 10 | 24 117 26 24 2 6 | 32. |
| 33. | 15.62 - 10 | 34. 117.26 × 2.6 | 33. |
| 35. | 117.26 - 2.6 | 36. 117.26 + 2.6 | 34 |
| | | | 35 |
| 37. | 0.0072×0.06 | 38. 0.0025 × 0.03 | <u>36.</u> |
| | | | 37. |
| 39. | 0.0072 + 0.06 | 40. 0.03 - 0.0025 | 38 |
| | | | 39. |
| 41. | 0.862×1000 | 42. 2.93 × 0.01 | 40. |
| 43. | Estimate the distance in miles between | Garden City | 41. |
| | Garden City, Kansas, and Wichita,
Kansas, by rounding each given
distance to the nearest ten. | 53.7 miles 60 miles 6 | 42. |
| | | Kansas | 43. |
| | | | |

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4.5 Dividing Decimals and Order of Operations

Objective A Dividing Decimals

Dividing decimal numbers is similar to dividing whole numbers. The only difference is that we place a decimal point in the quotient. If the divisor is a whole number, we place the decimal point in the quotient directly above the decimal point in the dividend, and then divide as with whole numbers. Recall that division can be checked by multiplication.

Dividing by a Whole Number

Step 1: Place the decimal point in the quotient directly above the decimal point in the dividend.

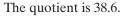
Step 2: Divide as with whole numbers.



Divide: $270.2 \div 7$. Check your answer.

Solution: We divide as usual. The decimal point in the quotient is directly above the decimal point in the dividend.

| Write the decimal point. | | | |
|---|--------|------------|-------------------------|
| divisor $\rightarrow 7)\overline{270.2} \leftarrow 4$ dividend
$\underline{-21}$ | Check: | \times 7 | ← quotient
← divisor |
| $\begin{array}{c c} 60 \\ -56 \\ 42 \end{array}$ | | 270.2 | ← dividend |
| $\frac{-42}{0}$ | | | |
| he quotient is 38.6. | | | |
| Wark Dreatics 1 | | | |



Work Practice 1



Divide: $32\overline{)8.32}$

Solution: We divide as usual. The decimal point in the quotient is directly above the decimal point in the dividend.

| $0.26 \leftarrow \text{quotient}$ | Check: | 0.26 | quotient |
|--|--------|-------------|----------|
| divisor $\rightarrow 32\overline{)8.32} \leftarrow dividend$ | _ | \times 32 | divisor |
| 64 | | 52 | |
| 1 92 | - | 7 80 | |
| <u>-1 92</u> | | 8.32 | dividend |
| 0 | | | |

Work Practice 2

Sometimes to continue dividing we need to insert zeros after the last digit in the dividend.

Objectives

- 🗛 Divide Decimals. >
- B Estimate When Dividing Decimals. D
- C Divide Decimals by Powers of 10. D
- **D** Solve Problems by Dividing Decimals. D
- **E** Review Order of Operations by Simplifying Expressions Containing Decimals. >

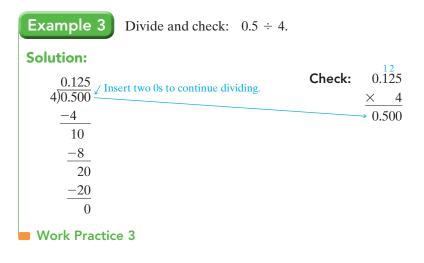
Practice 1

Divide: $370.4 \div 8$. Check your answer.

Practice 2

Divide: $48\overline{)34.08}$. Check your answer.

Answers **1.** 46.3 **2.** 0.71



Practice 3
Divide and check.
a. 0.4 ÷ 8
b. 13.62 ÷ 12

If the divisor is not a whole number, before we divide we need to move the decimal point to the right until the divisor is a whole number.

 $1.5\overline{)64.85}$ divisor $_$ $_$ $_$ dividend

To understand how this works, let's rewrite

 $(1.5)\overline{64.85}$ as $\frac{64.85}{1.5}$

and then multiply by 1 in the form of $\frac{10}{10}$. We use the form $\frac{10}{10}$ so that the denominator (divisor) becomes a whole number.

$$\frac{64.85}{1.5} = \frac{64.85}{1.5} \cdot 1 = \frac{64.85}{1.5} \cdot \frac{10}{10} = \frac{64.85 \cdot 10}{1.5 \cdot 10} = \frac{648.5}{15},$$

which can be written as $15.\overline{)648.5}$. Notice that

 $1.5\overline{)64.85}$ is equivalent to $15.\overline{)648.5}$

The decimal points in the dividend and the divisor were both moved one place to the right, and the divisor is now a whole number. This procedure is summarized next:

Dividing by a Decimal

- **Step 1:** Move the decimal point in the divisor to the right until the divisor is a whole number.
- **Step 2:** Move the decimal point in the dividend to the right the *same number of places* as the decimal point was moved in Step 1.
- **Step 3:** Divide. Place the decimal point in the quotient directly over the moved decimal point in the dividend.

Chapter 4 | Decimals

Practice 4 Divide: 166.88 ÷ 5.6



Divide: 10.764 ÷ 2.3

Solution: We move the decimal points in the divisor and the dividend one place to the right so that the divisor is a whole number.

| 2.3)10.764 | becomes | $ \begin{array}{r} 4.68 \\ 23.\overline{)107.64} \\ \underline{-92} \\ \overline{156} \end{array} $ | |
|---------------|----------------------|---|---------------|
| | | -13 8 | |
| | | 1 84 | |
| | | <u>-1 84</u> | |
| | | 0 | |
| Work Practice | e 4 | | |
| Example 5 | Divide: 5.264 ÷ 0.32 | | |
| Solution: | | 16.45 | |
| 0.32)5.264 | becomes | · · · · · · | Insert one 0. |
| | | $\frac{-32}{206}$ | |
| | | -192 | |
| | | 14 4 | |

Practice 5

Divide: 1.976 ÷ 0.16

Work Practice 5

Concept Check Is it always true that the number of decimal places in a quotient equals the sum of the decimal places in the dividend and divisor?

Example 6

Divide: $17.5 \div 0.48$. Round the quotient to the nearest hundredth.

 $\frac{-128}{160}$ $\frac{-160}{0}$

Solution: First we move the decimal points in the divisor and the dividend two places. Then we divide and round the quotient to the nearest hundredth.

| hundredths pla | * |
|-------------------------------------|---|
| | When rounding to the nearest |
| $\frac{36.458}{1000} \approx 36.46$ | 6 |
| 48.)1750.000 | hundredth, carry the division |
| -144 "is approximately" | process out to one more decimal place, the thousandths place. |
| 310 | |
| 288↓ | |
| 22 0 | |
| <u>−19 2↓</u> | |
| 2 80 | |
| $-240\downarrow$ | |
| 400 | |
| <u>-384</u> | |
| 16 | |
| Work Practice 6 | |

Practice 6

Divide $23.4 \div 0.57$. Round the quotient to the nearest hundredth.

Answers 4. 29.8 5. 12.35 6. 41.05

Concept Check Answer

Estimate 2 10 30)300

Objective **B** Estimating When Dividing Decimals 🕗

Just as for addition, subtraction, and multiplication of decimals, we can estimate when dividing decimals to check the reasonableness of our answer.

Example 7

Divide: $272.356 \div 28.4$. Then estimate to see whether the proposed result is reasonable.

Solution:

| Exact: | Estimate 1 | |
|--------------|------------|----|
| 9.59 | 9 | or |
| 284.)2723.56 | 30)270 | 01 |
| -2556 | | |
| 167 5 | | |
| -1420 | | |
| 25 56 | | |
| -2556 | | |
| 0 | | |

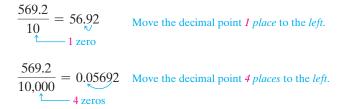
The estimate is 9 or 10, so 9.59 is reasonable.

Work Practice 7

Concept Check If a quotient is to be rounded to the nearest thousandth, to what place should the division be carried out? (Assume that the division carries out to your answer.)

Objective C Dividing Decimals by Powers of 10 🜔

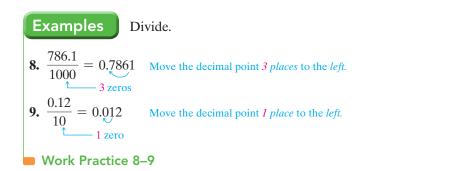
As with multiplication, there are patterns that occur when we divide decimals by powers of 10 such as 10, 100, 1000, and so on.



This pattern suggests the following rule:

Dividing Decimals by Powers of 10 such as 10, 100, or 1000

Move the decimal point of the dividend to the *left* the same number of places as there are *zeros* in the power of 10.



Practice 7

Divide: $713.7 \div 91.5$. Then estimate to see whether the proposed answer is reasonable.

Practice 8–9 Divide.

8. $\frac{128.3}{1000}$ **9.** $\frac{0.56}{10}$

Answers 7. 7.8 8. 0.1283 9. 0.056

Concept Check Answer ten-thousandths place

Objective D Solving Problems by Dividing Decimals 🕗

Many real-life problems involve dividing decimals.

Example 10

Calculating Materials Needed for a Job

A gallon of paint covers a 250-square-foot area. How many gallons of paint are needed to cover a wall that measures 1450 square feet? If only gallon containers of paint are available, how many gallon containers are needed?

Solution:

- **1.** UNDERSTAND. Read and reread the problem. We need to know how many 250s are in 1450, so we divide.
- 2. TRANSLATE.

| In words: | number of gallons | is | square
feet | divided
by | square feet per gallon |
|------------|-------------------|--------------|----------------|---------------|------------------------|
| | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| Translate: | number of gallons | = | 1450 | ÷ | 250 |

3. SOLVE. Let's see if our answer is reasonable by estimating. The dividend 1450 rounds to 1500 and divisor 250 rounds to 300. Then $1500 \div 300 = 5$.

| 5.8 |
|------------|
| 250)1450.0 |
| - 1250 |
| 200 0 |
| -200 0 |
| 0 |

- **4.** INTERPRET. *Check* your work. Since our estimate is close to our answer of 5, our answer is reasonable. *State* your conclusion: To paint the wall, 5.8 gallons of paint are needed. If only gallon containers of paint are available, then 6 gallon containers of paint are needed to complete the job.
- Work Practice 10

Objective E Simplifying Expressions with Decimals 🕑

In the remaining examples, we will review the order of operations by simplifying expressions that contain decimals.

Order of Operations

- 1. Perform all operations within parentheses (), brackets [], or other grouping symbols such as square roots or fraction bars, starting with the innermost set.
- 2. Evaluate any expressions with exponents.
- **3.** Multiply or divide in order from left to right.
- 4. Add or subtract in order from left to right.

Example 11

Simplify: $723.6 \div 1000 \times 10$

Solution: Multiply or divide in order from left to right.

 $723.6 \div 1000 \times 10 = 0.7236 \times 10$ Divide. = 7.236 Multiply.

Simplify: $897.8 \div 100 \times 10$

Practice 11

Answers 10. 11.84 bags; 12 bags 11. 89.78

Practice 10

A bag of fertilizer covers 1250

lawn measures 14,800 square

whole bags of fertilizer, how

square feet of lawn. Tim Parker's

feet. How many bags of fertilizer

does he need? If he can buy only

many whole bags does he need?



2 Simplify:
$$0.5(8.6 - 1.2)$$

Solution: According to the order of operations, we simplify inside the parentheses first.

0.5(8.6 - 1.2) = 0.5(7.4) Subtract. = 3.7 Multiply.

Work Practice 12

Example 1

Example 13 Simplify: $\frac{5.68 + (0.9)^2 \div 100}{0.2}$

Solution: First we simplify the numerator of the fraction. Then we divide.

| $5.68 + (0.9)^2 \div 100$ | $0 = 5.68 + 0.81 \div 100$ | $(0,0)^2$ |
|---------------------------|----------------------------|----------------------|
| 0.2 | 0.2 | Simplify $(0.9)^2$. |
| | $=\frac{5.68+0.0081}{0.2}$ | Divide. |
| | $=\frac{5.6881}{0.2}$ | Add. |
| | = 28.4405 | Divide. |
| M. I. D | | |

```
Practice 12
Simplify: 8.69(3.2 - 1.8)
```

Practice 13 Simplify: $\frac{20.06 - (1.2)^2 \div 10}{0.02}$

Answers 12. 12.166 13. 995.8

Work Practice 13

Calculator Explorations

Calculator errors can easily be made by pressing an incorrect key or by not pressing a correct key hard enough. Estimation is a valuable tool that can be used to check calculator results.

Example

Use estimation to determine whether the calculator result is reasonable or not. (For example, a result that is not reasonable can occur if proper keys are not pressed.)

Simplify: 82.064 ÷ 23

```
Calculator display: 35.68
```

Solution: Round each number to the nearest 10. Since $80 \div 20 = 4$, the calculator display 35.68 is not reasonable.

Use estimation to determine whether each result is reasonable or not.

- **1.** 102.62 × 41.8 Result: 428.9516
- **2.** 174.835 ÷ 47.9 Result: 3.65
- **3.** 1025.68 125.42 Result: 900.26
- **4.** 562.781 + 2.96 Result: 858.781

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Some choices may be used more than once, and some not used at all.

| dividend | divisor | quotient | true | | |
|--|-------------------|-------------------|------------|------------------|--|
| zeros | left | right | false | | |
| 1. In 6.5 ÷ 5 = | = 1.3, the number | 1.3 is called the | , 5 is the | , and 6.5 is the | |
| 2. To check a division exercise, we can perform the following multiplication: quotient \cdot = | | | | | |

Chapter 4 | Decimals

3. To divide a decimal number by a power of 10, such as 10, 100, 1000, and so on, we move the decimal point in the number to the ______ the same number of places as there are ______ in the power of 10.

4. True or false: If $1.058 \div 0.46 = 2.3$, then $2.3 \times 0.46 = 1.058$.

Recall properties of division and simplify.

| 5. $\frac{5.9}{1}$ | 6. $\frac{0.7}{0.7}$ | 7. $\frac{0}{9.86}$ | 8. $\frac{2.36}{0}$ |
|---------------------------------|-----------------------------|-----------------------------|------------------------------|
| 9. $\frac{7.261}{7.261}$ | 10. $\frac{8.25}{1}$ | 11. $\frac{11.1}{0}$ | 12. $\frac{0}{89.96}$ |

| Martin-Gay Interactive Videos | Watch the section lecture video and answer the following questions. |
|-------------------------------|---|
| | Objective A 13. From the lecture before Example 2, what must we make |
| | sure the divisor is before dividing decimals? 🕟 |
| | Objective B 14. In E xample 4, what is the estimated answer and what is |
| | the exact answer? |
| | Objective C 15. In E Example 6, why don't we divide as we did in |
| | Examples 1–3? |
| Can Liidan d.F. | Objective D 16. In E Example 7, why is the division carried to the |
| see Video 4.5 🍅 | hundredths place? 🕟 |
| | Objective E 17. In E Example 9, besides meaning division, what other |
| | purpose does the fraction bar serve? |

4.5 Exercise Set MyLab Math 🜔

Objectives A B Mixed Practice *Divide. See Examples 1 through 5 and 7. For those exercises marked, also estimate to see if the answer is reasonable.*

| 1. 3)13.8 | 2. 2)11.8 | 3. 5)0.47 | 4. 6)0.51 | 5. 0.06)18 |
|-------------------------------|-----------------------|-----------------------|---|---|
| 6. 0.04)20 | ▶7. 0.82)4.756 | 8. 0.92)3.312 | 9. 5.5) <u>36.3</u>
Exact:
Estimate: | 10. 2.2)21.78
Exact:
Estimate: |
| 11. 6.195 ÷ 15 | 12. 8.823 ÷ 17 | 13. 0.54 ÷ 12 | 14. 1.35 ÷ 18 | 15. Divide 4.2 by 0.6. |
| 16. Divide 3.6 by 0.9. | 17. 0.27)1.296 | 18. 0.34)2.176 | 19. 0.02)42 | 20. 0.03)24 |
| 21. 0.6)18 | 22. 0.4)20 | 23. 0.005)35 | 24. 0.0007)35 | 25. 7.2)70.56
Exact:
Estimate:
Bation 100
Equation 100 |

| 26. | 6.3)54.18
Exact: | 27. 5.4)51.84 | 28. 7.7)33.88 | 29. $\frac{1.215}{0.027}$ | 30. $\frac{3.213}{0.051}$ |
|-----|---------------------|------------------------|-------------------------|----------------------------------|----------------------------------|
| | Estimate: | | | | |
| 31. | 0.25)13.648 | 32. 0.75)49.866 | 33. 3.78)0.02079 | 34. 2.96)0.01332 | |

Divide. Round the quotients as indicated. See Example 6.

- **35.** Divide 429.34 by 2.4 and round the quotient to the nearest whole number.
- **37.** Divide 0.549 by 0.023 and round the quotient to the nearest hundredth.
 - **39.** Divide 45.23 by 0.4 and round the quotient to the nearest tenth.

Objective C *Divide. See Examples 8 and 9.*

| 54.982 | 42 <u>342.54</u> | $43 \frac{26.87}{}$ | 13.49 | A 1 1 2 . 9 | 46 $\frac{0.27}{0.27}$ |
|--------|-------------------------|---------------------|------------|--------------------|-------------------------------|
| 100 | 42. 100 | 43. 10 | 1 0 | 1000 | 40. 1000 |

Objectives A C Mixed Practice *Divide. See Examples 1 through 5, 8, and 9.*

| 47. 7)88.2 | 48. 9)130.5 | 49. $\frac{13.1}{10}$ | 50. $\frac{17.7}{10}$ |
|----------------------|-----------------------|------------------------------------|------------------------------------|
| 51. 6.8)83.13 | 52. 4.8)123.72 | 53. $\frac{456.25}{10,000}$ | 54. $\frac{986.11}{10,000}$ |

Objective D Solve. For Exercises 55 and 56, the solutions have been started for you. See Example 10.

55. Josef Jones is painting the walls of a room. The walls have a total area of 546 square feet. A quart of paint covers 52 square feet. If he must buy paint in whole quarts, how many quarts does he need?

Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blanks.)

| numbe | | | divided | square feet |
|--------------|------------------|--------------|--------------|--------------|
| of quar | ts ^{is} | feet | by | per quart |
| \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| number c | of = | | ÷ | |
| quarts | _ | | ÷ | |

- **3.** SOLVE. Don't forget to round up your quotient.
- **4.** INTERPRET.

56. A shipping box can hold 36 books. If 486 books must be shipped, how many boxes are needed?

36. Divide 54.8 by 2.6 and round the quotient to the

38. Divide 0.0453 by 0.98 and round the quotient to the

40. Divide 83.32 by 0.6 and round the quotient to the

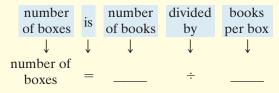
nearest whole number.

nearest thousandth.

nearest tenth.

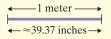
Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into an equation. (Fill in the blanks.)



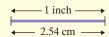
- **3.** SOLVE. Don't forget to round up your quotient.
- 4. INTERPRET.

- \triangle **57.** A pound of fertilizer covers 39 square feet of lawn. Vivian Bulgakov's lawn measures 7883.5 square feet. How much fertilizer, to the nearest tenth of a pound, does she need to buy?
 - **59.** There are approximately 39.37 inches in 1 meter. How many meters, to the nearest tenth of a meter, are there in 200 inches?



● 61. In the United States, an average child will wear down 730 crayons by his or her tenth birthday. Find the number of boxes of 64 crayons this is equivalent to. Round to the nearest tenth. (*Source:* Binney & Smith Inc.)

- **58.** A page of a book contains about 1.5 kilobytes of information. If a computer disk can hold 740 kilobytes of information, how many pages of a book can be stored on one computer disk? Round to the nearest tenth of a page.
- **60.** There are 2.54 centimeters in 1 inch. How many inches are there in 50 centimeters? Round to the nearest tenth.



62. During a recent year, American farmers received an average of \$81.10 per hundred pounds of turkey. What was the average price per pound for turkeys? Round to the nearest cent. (*Source:* National Agricultural Statistics Service)

A child is to receive a dose of 0.5 teaspoon of cough medicine every 4 hours. If the bottle contains 4 fluid ounces, answer *Exercises* 63 through 66.



Solve.

- **67.** Americans ages 20–34 drive, on average, 15,098 miles per year. About how many miles each week is that? Round to the nearest tenth. (*Note:* There are 52 weeks in a year.) (*Source:* U.S. Office of Highway Policy Information)
- **69.** During the 24 Hours of Le Mans endurance auto race, the winning team of Romain Dumas, Neel Jani, and Marc Lieb drove a total of 5233.5 kilometers in 24.06 hours. What was their average speed in kilometers per hour? Round to the nearest tenth. (*Source:* based on data from lemans-history.com)

- **63.** A fluid ounce equals 6 teaspoons. How many teaspoons are in 4 fluid ounces?
- **64.** The bottle of medicine contains how many doses for the child? (*Hint:* See Exercise **63**.)
- **65.** If the child takes a dose every four hours, how many days will the medicine last?
- **66.** If the child takes a dose every six hours, how many days will the medicine last?
- **68.** Drake Saucier was interested in the gas mileage on his "new" used car. He filled the tank, drove 423.8 miles, and filled the tank again. When he refilled the tank, it took 19.35 gallons of gas. Calculate the miles per gallon for Drake's car. Round to the nearest tenth.
- **70.** During the 2016 Summer Olympics, Kenyan runner Vivian Cheruiyot took the gold medal in the women's 5000-meter event. Her time for the event was 866.28 seconds. What was her average speed in meters per second? Round to the nearest tenth. (*Source:* International Olympic Committee)

- **71.** Breanna Stewart of the Seattle Storm was the WNBA's Rookie of the Year for 2016. She scored a total of 622 points in the 34 games she played in the 2016 regular season. What was the average number of points she scored per game? Round to the nearest tenth. (*Source:* Women's National Basketball Association)
- **72.** During the 2016 National Football League regular season, the top-scoring team was the Atlanta Falcons with a total of 540 points throughout the season. The Falcons played 16 games. What was the average number of points the team scored per game? (*Source:* National Football League)

Objective E *Simplify each expression. See Examples 11 through 13.*

0 73. 0.7(6-2.5)**74.** 1.4(2-1.8)**75.** $\frac{0.29+1.69}{3}$ **76.** $\frac{1.697-0.29}{0.7}$ **77.** $30.03 + 5.1 \times 9.9$ **78.** $60 - 6.02 \times 8.97$ **79.** $7.8 - 4.83 \div 2.1 + 9.2$ **80.** $90 - 62.1 \div 2.7 + 8.6$ **81.** $93.07 \div 10 \times 100$ **82.** $35.04 \div 100 \times 10$ **83.** $\frac{7.8 + 1.1 \times 100 - 3.6}{0.2}$ **84.** $\frac{9.6 - 7.8 \div 10 + 1.2}{0.02}$ **85.** $5(20.6 - 2.06) - (0.8)^2$ **86.** $(10.6 - 9.8)^2 \div 0.01 + 8.6$ **87.** $6 \div 0.1 + 8.9 \times 10 - 4.6$ **88.** $8 \div 10 + 7.6 \times 0.1 - (0.1)^2$

Review

 Write each decimal as a fraction. See Section 4.1.

 89. 0.9
 90. 0.7
 91. 0.05
 92. 0.08

Concept Extensions

| Mixed Practice (Sections 4.3, 4.4, and 4.5) Perform the indicat | ted operation. |
|---|----------------|
|---|----------------|

| 93. 1.278 ÷ 0.3 | 94. 1.278 × 0.3 | 95. 1.278 + 0.3 | 96. 1.278 - 0.3 |
|--------------------------------|------------------------------|-----------------------------------|-----------------------------------|
| 97. 8.6
<u>× 3.1</u> | 98. 7.2 + 0.05 + 49.1 | 99. 1000
<u>- 95.71</u> | 100. $\frac{87.2}{10,000}$ |

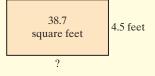
Choose the best estimate.

| 101. 8.62 × 41.7 | 102. 1.437 + 20.69 | 103. 78.6 ÷ 97 | 104. 302.729 - 28.697 |
|-------------------------|---------------------------|-----------------------|------------------------------|
| a. 36 | a. 34 | a. 7.86 | a. 270 |
| b. 32 | b. 22 | b. 0.786 | b. 20 |
| c. 360 | c. 3.4 | c. 786 | c. 27 |
| d. 3.6 | d. 2.2 | d. 7860 | d. 300 |

Recall from Section 1.7 that the average of a list of numbers is their total divided by how many numbers there are in the list. Use this procedure to find the average of the test scores listed in Exercises 105 and 106. If necessary, round to the nearest tenth.

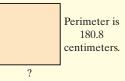
105. 86, 78, 91, 87

- **106.** 56, 75, 80
- \triangle **107.** The area of a rectangle is 38.7 square feet. If its width is 4.5 feet, find its length.



109. When dividing decimals, describe the process you use to place the decimal point in the quotient.

 \bigtriangleup 108. The perimeter of a square is 180.8 centimeters. Find the length of a side.



110. In your own words, describe how to quickly divide a number by a power of 10 such as 10, 100, 1000, etc.

To convert wind speeds in miles per hour to knots, divide by 1.15. Use this information and the Saffir-Simpson Hurricane Intensity chart below to answer Exercises 111 and 112. Round to the nearest tenth.

| Saffir-Simpson Hurricane Intensity Scale | | | | | |
|--|-------------|-----------------|----------|---|--|
| Category Wind Speed Barometric Pressure
[inches of mercury (Hg)] Storm Surge Damage Potential | | | | | |
| 1 (Weak) | 75–95 mph | ≥28.94 in. | 4–5 ft | Minimal damage to vegetation | |
| 2 (Moderate) | 96–110 mph | 28.50-28.93 in. | 6–8 ft | Moderate damage to houses | |
| 3 (Strong) | 111–130 mph | 27.91–28.49 in. | 9–12 ft | Extensive damage to small buildings | |
| 4 (Very Strong) | 131–155 mph | 27.17–27.90 in. | 13–18 ft | Extreme structural damage | |
| 5 (Devastating) | > 155 mph | <27.17 in. | >18 ft | Catastrophic building failures possible | |

- **111.** The chart gives wind speeds in miles per hour. What is the range of wind speeds for a Category 1 hurricane in knots?
- **113.** A rancher is building a horse corral that's shaped like a rectangle with dimensions of 24.28 meters by 15.675 meters. He plans to make a four-wire fence; that is, he will string four wires around the corral. How much wire will he need?
- **112.** What is the range of wind speeds for a Category 4 hurricane in knots?
- **114.** A college student signed up for a new credit card that guarantees her no interest charges on transferred balances for a year. She transferred over a \$2523.86 balance from her old credit card. Her minimum payment is \$185.35 per month. If she only pays the minimum, will she pay off her balance before interest charges start again?

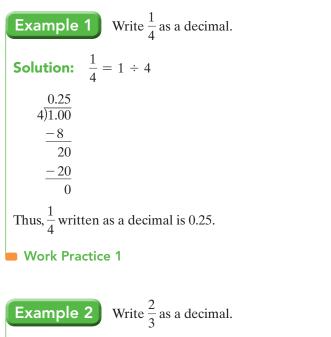
4.6 Fractions and Decimals

Objective A Writing Fractions as Decimals 🜔

To write a fraction as a decimal, we interpret the fraction bar to mean division and find the quotient.

Writing Fractions as Decimals

To write a fraction as a decimal, divide the numerator by the denominator.



| Solution: | <u>0.666</u>
3)2.000 | This pattern will continue because $\frac{2}{3} = 0.6666 \dots$ |
|-----------|-------------------------|---|
| | $\frac{-18}{20}$ | Remainder is 2, then 0 is brought down. |
| | -18 | |
| | 20 | Remainder is 2, then 0 is brought down. |
| | $\frac{-18}{2}$ | Remainder is 2. |

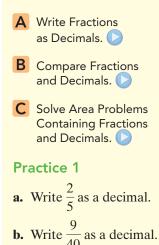
Notice the digit 2 keeps occurring as the remainder. This will continue so that the digit 6 will keep repeating in the quotient. We place a bar over the digit 6 to indicate that it repeats.

 $\frac{2}{3} = 0.666 \dots = 0.\overline{6}$

We can also write a decimal approximation for $\frac{2}{3}$. For example, $\frac{2}{3}$ rounded to the nearest hundredth is 0.67. This can be written as $\frac{2}{3} \approx 0.67$.

Work Practice 2

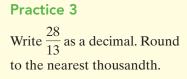
Objectives

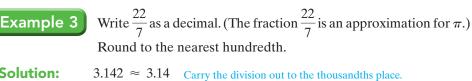


Practice 2

a. Write $\frac{5}{6}$ as a decimal. **b.** Write $\frac{2}{9}$ as a decimal.

Answers 1. a. 0.4 b. 0.225 2. a. 0.83 b. 0.2 Chapter 4 | Decimals



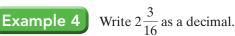


Solution:

 $\frac{-28}{20}$ $\frac{-14}{6}$ The fraction $\frac{22}{7}$ in decimal form is approximately 3.14. Thus, $\pi \approx \frac{22}{7}$ (a fraction

approximation for π) and $\pi \approx 3.14$ (a decimal approximation for π).

Work Practice 3



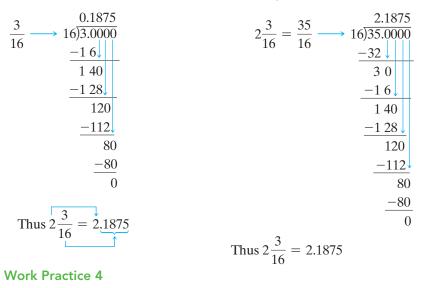
7)22.000 -21 10

 $\frac{-7}{30}$

Solution:

Option 1. Write the fractional part only as a decimal.

Option 2. Write $2\frac{3}{16}$ as an improper fraction, and divide.

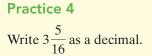


Some fractions may be written as decimals using our knowledge of decimals. From Section 4.1, we know that if the denominator of a fraction is 10, 100, 1000, or so on, we can immediately write the fraction as a decimal. For example,

$$\frac{4}{10} = 0.4$$
, $\frac{12}{100} = 0.12$, and so on.

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Answers **3.** 2.154 **4.** 3.3125



Example 5 Write
$$\frac{4}{5}$$
 as a decimal.
Solution: Let's write $\frac{4}{5}$ as an equivalent fraction with a denominator of 10.

$$\frac{4}{5} = \frac{4}{5} \cdot \frac{2}{2} = \frac{8}{10} = 0.8$$

Work Practice 5

Example 6 Write
$$\frac{1}{25}$$
 as a decimal.

Solution:
$$\frac{1}{25} = \frac{1}{25} \cdot \frac{4}{4} = \frac{4}{100} = 0.04$$

Work Practice 6

Concept Check Suppose you are writing the fraction $\frac{9}{16}$ as a decimal. How do you know you have made a mistake if your answer is 1.735?

Objective **B** Comparing Fractions and Decimals (

Now we can compare decimals and fractions by writing fractions as equivalent decimals.

Example 7 Insert <, >, or = to form a true statement. $\frac{1}{8}$ 0.12 **Solution:** First we write $\frac{1}{8}$ as an equivalent decimal. Then we compare decimal places. 0 1 25

| 0.125 | | | | |
|-------------------------|-------------|-------|-----------------|--------|
| 8)1.000 | Original nu | nbers | $\frac{1}{8}$ | 0.12 |
| -8 | Decimals | | 0.125 | 0.120 |
| 20 | Compare | | 0.125 | > 0.12 |
| $\frac{-16}{40}$
-40 | Thus, | | $\frac{1}{8} >$ | 0.12 |
| 0 | | | | |

Practice 7

Insert <, >, or = to form a true statement.

$$\frac{1}{5}$$
 0.25

Work Practice 7

Example 8 Insert <, >, or = to form a true statement. $\frac{7}{9}$ $0.\overline{7}$ **Solution:** We write $\frac{7}{9}$ as a decimal and then compare. $0.77 \ldots = 0.\overline{7}$ $0.\bar{7}$ **Original numbers** 9)7.00 -6.3 $0.\overline{7}$ $0.\overline{7}$ Decimals 70 $0.\overline{7} = 0.\overline{7}$ Compare -63 $0.\overline{7} = \frac{7}{9}$ Thus,

9

Practice 8

Insert <, >, or = to form a true statement.

b.
$$\frac{1}{2}$$
 0.54 **b.** $0.\overline{4}$ $\frac{4}{9}$
c. $\frac{5}{7}$ 0.72

Answers **5.** 0.6 **6.** 0.06 **7.** < 8. a. < b. = c. <

Concept Check Answer

 $\frac{9}{16}$ is less than 1 while 1.735 is greater than 1.

Practice 6 Write $\frac{3}{50}$ as a decimal.

Chapter 4 | Decimals

Practice 9

Practice 10

Find the area of the triangle.

2.1 meters 7 meters

Write the numbers in order from smallest to largest.

a.
$$\frac{1}{3}$$
, 0.302, $\frac{3}{8}$ **b.** 1.26, $1\frac{1}{4}$, $1\frac{2}{5}$
c. 0.4, 0.41, $\frac{5}{7}$



Write the numbers in order from smallest to largest.

$$\frac{9}{20}, \frac{4}{9}, 0.456$$

Solution:

| Original numbers | $\frac{9}{20}$ | $\frac{4}{9}$ | 0.456 |
|------------------|----------------|---------------|-------|
| Decimals | 0.450 | 0.444 | 0.456 |
| Compare in order | 2nd | 1st | 3rd |

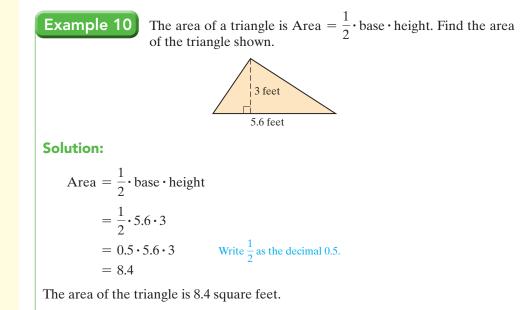
Written in order, we have

1st 2nd 3rd $\downarrow \qquad \downarrow \qquad \downarrow$ $\frac{4}{9}, \frac{9}{20}, 0.456$

Work Practice 9

Objective C Solving Area Problems Containing Fractions and Decimals

Sometimes real-life problems contain both fractions and decimals. In this section, we solve such problems concerning area. In the next example, we review the area of a triangle. This concept will be studied more in depth in a later chapter.



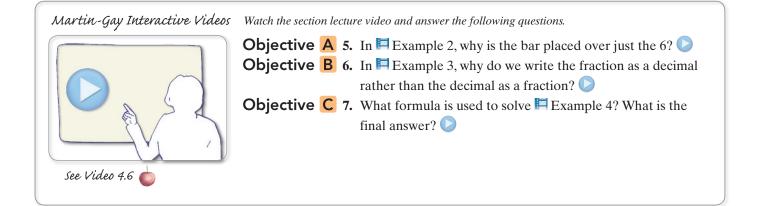
Work Practice 10

Answers 9. a. 0.302, $\frac{1}{3}$, $\frac{3}{8}$ b. $1\frac{1}{4}$, 1.26, $1\frac{2}{5}$ c. 0.4, 0.41, $\frac{5}{7}$ 10. 7.35 sq m

Vocabulary, Readiness & Video Check

Answer each exercise "true" or "false."

- **1.** The number $0.\overline{5}$ means 0.555.
- **2.** To write $\frac{9}{19}$ as a decimal, perform the division $9\overline{)19}$.
- **3.** $(1.2)^2$ means (1.2)(1.2) or 1.44.
- 4. The area of a figure is written in *square* units.



4.6 Exercise Set MyLab Math 🚺

Objective A Write each number as a decimal. See Examples 1 through 6.

| 1. $\frac{1}{5}$ | 2. $\frac{1}{20}$ | 3. $\frac{17}{25}$ | 4. $\frac{13}{25}$ | • 5. $\frac{3}{4}$ |
|------------------------------|---------------------------|-----------------------------|---|------------------------------|
| 6. $\frac{3}{8}$ | 7. $\frac{2}{25}$ | 8. $\frac{3}{25}$ | 9. $\frac{6}{5}$ | 10. $\frac{5}{4}$ |
| • 11. $\frac{11}{12}$ | 12. $\frac{5}{12}$ | 13. $\frac{17}{40}$ | 14. $\frac{19}{25}$ | 15. $\frac{9}{20}$ |
| 16. $\frac{31}{40}$ | 17. $\frac{1}{3}$ | 18. $\frac{7}{9}$ | 19. $\frac{7}{16}$ | 20. $\frac{9}{16}$ |
| 21. $\frac{7}{11}$ | 22. $\frac{9}{11}$ | 23. $5\frac{17}{20}$ | 24. $4\frac{7}{8}$ 25. $\frac{78}{125}$ | 26. $\frac{159}{375}$ |

Round each number as indicated.

- **27.** Round your decimal answer to Exercise **17** to the nearest hundredth.
- **29.** Round your decimal answer to Exercise **19** to the nearest hundredth.
- **31.** Round your decimal answer to Exercise **21** to the nearest tenth.
- **28.** Round your decimal answer to Exercise **18** to the nearest hundredth.
- **30.** Round your decimal answer to Exercise **20** to the nearest hundredth.
- **32.** Round your decimal answer to Exercise **22** to the nearest tenth.

Write each fraction as a decimal. If necessary, round to the nearest hundredth. See Examples 1 through 6.

- **33.** Of the U.S. mountains that are over 14,000 feet in elevation, $\frac{56}{91}$ are located in Colorado. (*Source:* U.S. Geological Survey)
- **35.** As of the end of 2016, $\frac{97}{200}$ of all U.S. households were wireless-only households, meaning they no longer subscribe to landline telephone services. (*Source:* CTIA – The Wireless Association)
- **37.** When first launched, the Hubble Space Telescope's primary mirror was out of shape on the edges by $\frac{1}{50}$ of a human hair. This very small defect made it difficult to focus on faint objects being viewed. Because the HST was in low Earth orbit, it was serviced by a shuttle and the defect was corrected.

- **34.** About $\frac{21}{50}$ of all blood donors have type A blood. (*Source:* American Red Cross Biomedical Services)
- **36.** Porsche is the auto manufacturer with the most wins at the 24 Hours of Le Mans endurance race. By $2016, \frac{18}{84}$ of Le Mans races had been won in Porsche vehicles. (*Source:* lemans-history.com)
- **38.** The two mirrors currently in use in the Hubble Space Telescope were ground so that they do not deviate from a perfect curve by more than $\frac{1}{800,000}$ of an inch. Do not round this number.



Objective B Insert <, >, or = to form a true statement. See Examples 7 and 8.

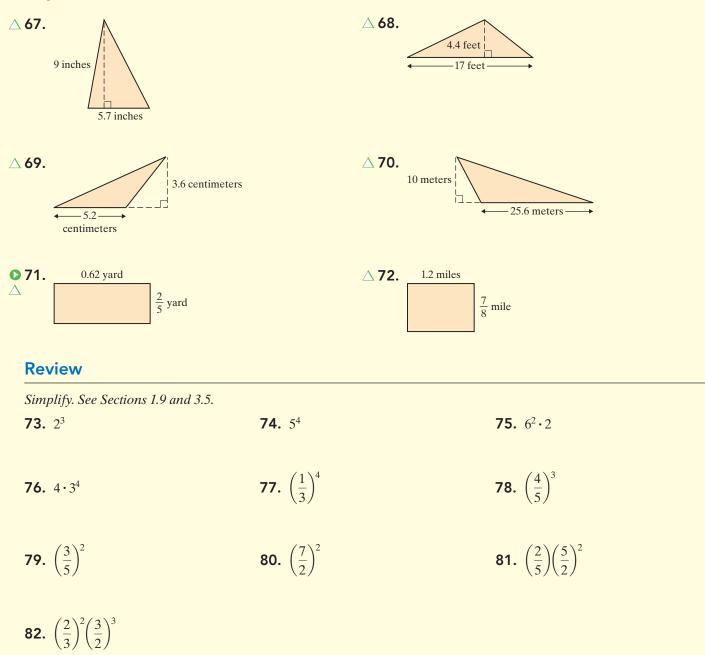
| 39. 0.562 0.569 | 40. 0.983 0.988 | 41. 0.215 $\frac{43}{200}$ | 42. $\frac{29}{40}$ 0.725 |
|--|--|---|--|
| 43. $\frac{9}{100}$ 0.0932 | 44. $\frac{1}{200}$ 0.00563 | 45. $0.\overline{6}$ $\frac{5}{6}$ | 46. $0.\overline{1}$ $\frac{2}{17}$ |
| 47. $\frac{51}{91}$ 0.56 $\overline{4}$ | 48. $0.58\overline{3}$ $\frac{6}{11}$ | 49. $\frac{1}{9}$ 0.1 | 50. 0.6 $\frac{2}{3}$ |
| • 51. 1.38 $\frac{18}{13}$ | 52. 0.372 $\frac{22}{59}$ | 53. 7.123 $\frac{456}{64}$ | 54. 12.713 $\frac{89}{7}$ |

Write the numbers in order from smallest to largest. See Example 9.

| 55. 0.34, 0.35, 0.32 | 56. 0.47, 0.42, 0.40 | 57. 0.49, 0.491, 0.498 | 58. 0.72, 0.727, 0.728 |
|---------------------------------------|---------------------------------------|---|---|
| 59. $\frac{3}{4}$, 0.78, 0.73 | 60. $\frac{2}{5}$, 0.49, 0.42 | 61. $\frac{4}{7}$, 0.453, 0.412 | 62. $\frac{6}{9}$, 0.663, 0.668 |

C

63. 5.23,
$$\frac{42}{8}$$
, 5.34 **64.** 7.56, $\frac{67}{9}$, 7.562 **65.** $\frac{12}{5}$, 2.37, $\frac{17}{8}$ **66.** $\frac{29}{16}$, 1.75, $\frac{59}{32}$



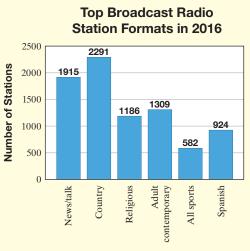
Objective C *Find the area of each triangle or rectangle. See Example 10.*

Concept Extensions

Without calculating, describe each number as < 1, = 1, or > 1. See the Concept Check in this section.

| 83. 1.0 | 84. 1.0000 | 85. 1.00001 |
|-----------------------------|-----------------------------|----------------------------|
| 86. $\frac{101}{99}$ | 87. $\frac{99}{100}$ | 88. $\frac{99}{99}$ |

In 2016, there were 10,181 broadcast radio stations in the United States. The most popular formats are shown in the graph along with their counts. Use this graph to answer Exercises 89 through 92. (Source: newsgeneration.com and Pew Research Center)



Format (Total stations: 10,181)

- **89.** Write the fraction of radio stations that are all sports as a decimal. Round to the nearest thousandth.
- **91.** Estimate, by rounding each number in the table to the nearest hundred, the total number of stations with the top six formats in 2016.
- **93.** Describe two ways to determine the larger of two fractions.
- **95.** Describe two ways to write mixed numbers as decimals.
- Find the value of each expression. Give the result as a decimal.

97.
$$(9.6)(5) - \frac{3}{4}$$
 98. $2(7.8) - \frac{1}{5}$

100. 8.25 $-\left(\frac{1}{2}\right)^2$ **101.** $\frac{3}{8}(5.9 - 4.7)$

- **90.** Write the fraction of radio stations with a Spanish format as a decimal. Round to the nearest hundredth.
- **92.** Use your estimate from Exercise **91** to write the fraction of radio stations accounted for by the top six formats as a decimal. Round to the nearest hundredth.
- **94.** Describe two ways to write fractions as decimals.
- **96.** Do you prefer performing operations on decimals or fractions? Why?

99.
$$\left(\frac{1}{10}\right)^2 + (1.6)(2.1)$$

102.
$$\frac{1}{4}(9.6 + 5.2)$$

Chapter 4 Group Activity

Maintaining a Checking Account

(Sections 4.1, 4.2, 4.3, 4.4)

This activity may be completed by working in groups or individually.

A checking account is a convenient way of handling money and paying bills. To open a checking account, the bank or savings and loan association requires a customer to make a deposit. Then the customer receives a checkbook that contains checks, deposit slips, and a register for recording checks written and deposits made. It is important to record all payments and deposits that affect the account. It is also important to keep the checkbook balance current by subtracting checks written and adding deposits made.

About once a month checking customers receive a statement from the bank listing all activity that the account has had in the last month. The statement lists a beginning balance, all checks and deposits, any service charges made against the account, and an ending balance. Because it may take several days for checks that a customer has written to clear the banking system, the check register may list checks that do not appear on the monthly bank statement. These checks are called **outstanding checks.** Deposits that are recorded in the check register but do not appear on the statement are called **deposits in transit.** Because of these differences,

it is important to balance, or reconcile, the checkbook against the monthly statement. The steps for doing so are listed below.

Balancing or Reconciling a Checkbook

- **Step 1:** Place a check mark in the checkbook register next to each check and deposit listed on the monthly bank statement. Any entries in the register without a check mark are outstanding checks or deposits in transit.
- **Step 2:** Find the ending checkbook register balance and add to it any outstanding checks and any interest paid on the account.
- **Step 3:** From the total in Step 2, subtract any deposits in transit and any service charges.
- **Step 4:** Compare the amount found in Step 3 with the ending balance listed on the bank statement. If they are the same, the checkbook balances with the bank statement. Be sure to update the check register with service charges and interest.
- **Step 5:** If the checkbook does not balance, recheck the balancing process. Next, make sure that the running checkbook register balance was calculated correctly. Finally, compare the checkbook register with the statement to make sure that each check was recorded for the correct amount.

For the checkbook register and monthly bank statement given:

a. *update the checkbook register* **b.** *list the outstanding checks and deposits in transit*

c. balance the checkbook – be sure to update the register with any interest or service fees

| | Checkbook Register | | | | | | |
|-----|--------------------|----------------------|---------|---|---------|---------|--|
| | | | | | | Balance | |
| # | Date | Description | Payment | 1 | Deposit | 425.86 | |
| 114 | 4/1 | Market Basket | 30.27 | | | | |
| 115 | 4/3 | Texaco | 8.50 | | | | |
| | 4/4 | Cash at ATM | 50.00 | | | | |
| 116 | 4/6 | UNO Bookstore | 121.38 | | | | |
| | 4/7 | Deposit | | | 100.00 | | |
| 117 | 4/9 | MasterCard | 84.16 | | | | |
| 118 | 4/10 | Salle's Watch Repair | 6.12 | | | | |
| 119 | 4/12 | Kroger | 18.72 | | | | |
| 120 | 4/14 | Parking sticker | 18.50 | | | | |
| | 4/15 | Direct deposit | | | 294.36 | | |
| 121 | 4/20 | Rent | 395.00 | | | | |
| 122 | 4/25 | Student fees | 20.00 | | | | |
| | 4/28 | Deposit | | | 75.00 | | |

| First Nationa | I Bank Monthly Statem | ent 4/30 |
|-----------------|-----------------------|----------|
| BEGINNING BAL | ANCE: | 425.86 |
| Date | Number | Amount |
| eneen | S AND ATM
DRAWALS | |
| 4/3 | 114 | 30.27 |
| 4/4 | ATM | 50.00 |
| 4/11 | 117 | 84.16 |
| 4/13 | 115 | 8.50 |
| 4/15 | 119 | 18.72 |
| 4/22 | 121 | 395.00 |
| DEPOSITS | | |
| 4/7 | | 100.00 |
| 4/15 | Direct deposit | 294.36 |
| SERVICE CHARGE | ES | |
| Low balance fee | | 7.50 |
| INTEREST | | |
| Credited 4/30 | | 1.15 |
| ENDING BALANC | E: | 227.22 |

Chapter 4 Vocabulary Check

Fill in each blank with one of the choices listed below. Some choices may be used more than once or not at all. vertically decimal right triangle and diameter standard form product circumference difference quotient denominator sum numerator _____ notation is used to denote a part of a whole. **1.** Like fractional notation, ____ 2. To write fractions as decimals, divide the _____ by the ____ 3. To add or subtract decimals, write the decimals so that the decimal points line up _ _____" for the decimal point. 4. When writing decimals in words, write "____ 5. When multiplying decimals, the decimal point in the product is placed so that the number of decimal places in the product is equal to the ______ of the number of decimal places in the factors. 6. The distance around a circle is called the _____ 7. When 2 million is written as 2,000,000, we say it is written in _____. of a circle 8. $\pi = =$ of a circle 9. In 3.4 - 2 = 1.4, the number 1.4 is called the _____ **10.** In 3.4 \div 2 = 1.7, the 1.7 is called the _____. **11.** In $3.4 \times 2 = 6.8$, the 6.8 is called the _____ **12.** In 3.4 + 2 = 5.4, the 5.4 is called the _____ Helpful Are you preparing for your test? To help, don't forget to take these: • Chapter 4 Getting Ready for the Test on page 315 • Chapter 4 Test on page 316 Then check all of your answers at the back of this text. For further review, the step-by-step video solutions to any of these exercises are located in MyLab Math.

4 Chapter Highlights

| Definitions and Concepts | | | Examples | | | | | |
|--------------------------|-------|------|------------------|----------------|-----------------|------------------|---|---------------------|
| Section 4.1 Intro | | | | on 4.1 Introd | duction to Dec | imals | | |
| lace-Value | Chart | | | | | | | |
| | | 4 | | 2 | 6 | 5 | | |
| hundreds | tens | ones | | | | | ten-thousandths | hundred-thousandths |
| 100 | 10 | 1 | decimal
point | $\frac{1}{10}$ | $\frac{1}{100}$ | $\frac{1}{1000}$ | 110,000 | 1 100,000 |
| | | | | | | or | $\frac{1}{10} + 6 \cdot \frac{1}{100} + 5 \cdot \frac{1}{100} + \frac{5}{1000}$ | $\frac{1}{1000}$ |

| Definitions and Concepts | | Examples | | |
|---|--|---|--|--|
| | Section 4.1 Introduction | to Decimals (continued) | | |
| Writing | (or Reading) a Decimal in Words | Write 3.08 in words. | | |
| Step 1: Write the whole number part in words. Step 2: Write "and" for the decimal point. Step 3: Write the decimal part in words as though it were a whole number, followed by the place value of the last digit. | | Three and eight hundredths | | |
| | mal written in words can be written in standard y reversing the above procedure. | Write "four and twenty-one thousandths" in standard form. 4.021 | | |
| | Section 4.2 Orc | ler and Rounding | | |
| from let | pare decimals, compare digits in the same place
ft to right. When two digits are not equal, the num-
n the larger digit is the larger decimal. | $3.0261 > 3.0186 \text{ because}$ $\uparrow \qquad \uparrow$ $2 \qquad > \qquad 1$ | | |
| | nd Decimals to a Place Value to the Right of
cimal Point | Round 86.1256 to the nearest hundredth. | | |
| | Locate the digit to the right of the given place value. | Step 1: 86.12(5)6
digit to the right | | |
| Step 2: | If this digit is 5 or greater, add 1 to the digit in
the given place value and delete all digits to its
right. If this digit is less than 5, delete all digits to
the right of the given place value. | Step 2: Since the digit to the right is 5 or greater, we add 1 to the digit in the hundredths place and delete all digits to its right. 86.1256 rounded to the nearest hundredth is 86.13. | | |
| | Section 4.3 Adding ar | d Subtracting Decimals | | |
| To Add or Subtract Decimals | | Add: 4.6 + 0.28 Subtract: 2.8 - 1.04 | | |
| Step 1: | Write the decimals so that the decimal points line up vertically. | $\begin{array}{ccc} 4.60 & 2.8 \cancel{0} \\ + 0.28 & -1.0 4 \end{array}$ | | |
| Step 2:
Step 3: | Add or subtract as with whole numbers.
Place the decimal point in the sum or difference
so that it lines up vertically with the decimal
points in the problem. | 4.88 1.76 | | |
| | Section 4.4 Multiplying Decima | als and Circumference of a Circle | | |
| To Mult | tiply Decimals | Multiply: 1.48×5.9 | | |
| Step 1:
Step 2: | Multiply the decimals as though they are whole
numbers.
The decimal point in the product is placed so
that the number of decimal places in the product
is equal to the <i>sum</i> of the number of decimal
places in the factors. | $ \begin{array}{rcl} 1.48 & \leftarrow 2 \text{ decimal places} \\ \times 5.9 & \leftarrow 1 \text{ decimal places} \\ \hline 1332 & \\ \hline 7400 \\ \hline 8.732 & \leftarrow 3 \text{ decimal places} \end{array} $ | | |
| The circumference of a circle is the distance around the circle. | | Find the exact circumference of a circle with radius 5 miles and an approximation by using 3.14 for π . | | |
| | $C = 2 \cdot \pi \cdot \text{radius or}$ $C = \pi \cdot \text{diameter},$ | $C = 2 \cdot \pi \cdot \text{radius}$
= $2 \cdot \pi \cdot 5$
= 10π
$\approx 10(3.14)$
= 31.4 | | |
| where 7 | $\tau \approx 3.14 \text{ or } \frac{22}{7}.$ | The circumference is exactly 10π miles and <i>approximately</i> 31.4 miles. | | |

| | Definitions and Concepts | Examples | | | |
|-------------------------------------|---|--|--|--|--|
| | Section 4.5 Dividing Decimals and Order of Operations | | | | |
| To Div | ide Decimals | Divide: 1.118 ÷ 2.6 | | | |
| Step 1: | If the divisor is not a whole number, move the decimal point in the divisor to the right until the divisor is a whole number. | $ \begin{array}{r} 0.43 \\ 2.6)\overline{1.118} \\ -1 04 \end{array} $ | | | |
| Step 2: | Move the decimal point in the dividend to the right the <i>same number of places</i> as the decimal point was moved in step 1. | $\frac{-78}{-78}$ | | | |
| Step 3: | Divide. The decimal point in the quotient is directly over the moved decimal point in the dividend. | | | | |
| Order | of Operations | | | | |
| [], o
fract
2. Eva
3. Mul | form all operations within parentheses (), brackets
or grouping symbols such as square roots or
tion bars.
luate any expressions with exponents.
tiply or divide in order from left to right.
I or subtract in order from left to right. | Simplify.
1.9(12.8 - 4.1) = 1.9(8.7) Subtract.
= 16.53 Multiply. | | | |
| | Section 4.6 Fract | tions and Decimals | | | |
| | te fractions as decimals, divide the numerator by nominator. | Write $\frac{3}{8}$ as a decimal.
$ \begin{array}{r} 0.375 \\ 8)\overline{3.000} \\ -2.4 \\ 60 \\ -56 \\ 40 \\ -40 \\ 0 \end{array} $ | | | |

Chapter 4 Review

| (4.1) Determine the place value of the digit 4 in each decimal. | | | | |
|---|-------------------|--------------------|------------------|--|
| 1. 23.45 | | 2. 0.000345 | | |
| | | | | |
| Write each decimal in words. | | | | |
| 3. 0.45 | 4. 0.00345 | 5. 109.23 | 6. 46.007 | |

Write each decimal in standard form.

7. Two and fifteen hundredths **8.** Five hundred three and one hundred two thousandths

Write the decimal as a fraction or a mixed number. Write your answer in simplest form.

| 9. 0.16 | 10. 12.023 | 11. 1.0045 | 12. 25.25 |
|----------------|-------------------|-------------------|------------------|
| | | | |

Write each fraction as a decimal.

13. $\frac{9}{10}$ **14.** $\frac{25}{100}$ **15.** $\frac{45}{1000}$ **16.** $\frac{261}{10}$

(4.2) Insert <, >, or = to make a true statement.**17.** 0.49 0.43

Write the decimals in order from smallest to largest.

19. 8.6, 8.09, 0.92 20. 0.09, 0.1, 0.091

Round each decimal to the given place value.

21. 0.623, nearest tenth

Round each money amount to the nearest cent.

23. \$0.259

Solve.

25. In a recent year, engaged couples in the United States spent an average of \$31,304.35 on their wedding. Round this number to the nearest dollar.

24. \$12.461

22. 0.9384, nearest hundredth

18. 0.973 0.9730

26. A certain kind of chocolate candy bar contains 10.75 teaspoons of sugar. Round this number to the nearest tenth.

(4.3) Add or subtract as indicated.

27. 2.4 + 7.12

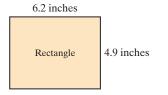
28. 3.9 – 1.2

29. 6.4 + 0.88

- **31.** 892.1 432.4 **32.** 100.342 0.064
- **35.** Find the total distance between Grove City and Jerome.



 \triangle **37.** Find the perimeter.

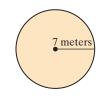


(4.4) Multiply.

| 39. 3.7
<u>× 5</u> | 40. 9.1 $\times 6$ | 41. 7.2 × 10 |
|------------------------------|---------------------------------|-----------------------------------|
| 42. 9.345 × 1000 | 43. 4.02
<u>× 2.3</u> | 44. 39.02
<u>× 87.3</u> |

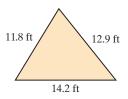
Solve.

 \triangle **45.** Find the exact circumference of the circle. Then use the approximation 3.14 for π and approximate the circumference.



- **33.** Subtract 34.98 from 100. **34.** Subtract 10.02 from 200.
- **36.** The price of oil was \$47.73 per barrel on a day in March 2017. It was \$52.56 on a day in April 2017. Find by how much the price of oil increased between those days.

 \triangle **38.** Find the perimeter.



46. A kilometer is approximately 0.625 mile. It is 102 kilometers from Hays to Colby. Write 102 kilometers in miles to the nearest tenth of a mile.

Write each number in standard form.

- **47.** Saturn is a distance of about 887 million miles from the Sun.
- **48.** The tail of a comet can be over 600 thousand miles long.
- (4.5) Divide. Round the quotient to the nearest thousandth if necessary.
- **49.** 3)0.261 **50.** 20)316.5

51. 21 ÷ 0.3

52. 0.0063 ÷ 0.03

57. There are approximately 3.28 feet in 1 meter. Find how many meters are in 24 feet to the nearest tenth of a meter.

| \leftarrow 1 meter \rightarrow | |
|------------------------------------|--|
| ← ≈3.28 feet → | |

Simplify each expression.

59. $7.6 \times 1.9 + 2.5$ **60.** $(2.3)^2 - 1.4$ **61.** $\frac{7 + 0.74}{0.06}$ **62.** $\frac{(1.5)^2 + 0.5}{0.05}$ **63.** 0.9(6.5 - 5.6)**64.** $0.0726 \div 10 \times 1000$

(4.6) Write each fraction as a decimal. Round to the nearest thousandth if necessary.

65. $\frac{4}{5}$ **66.** $\frac{12}{13}$ **67.** $2\frac{1}{3}$ **68.** $\frac{13}{60}$

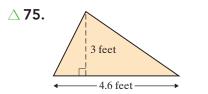
Insert <, >, *or* = *to make a true statement.*

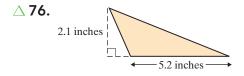
69. 0.392 0.3920 **70.** $0.\overline{4} \quad \frac{4}{9}$ **71.** 0.293 $\frac{5}{17}$ **72.** $\frac{4}{7}$ 0.625

Write the numbers in order from smallest to largest.

73.
$$0.839, \frac{17}{20}, 0.837$$
 74. $\frac{18}{11}, 1.63, \frac{19}{12}$

Find each area.





Mixed Review

- **77.** Write 200.0032 in words.
- **79.** Write 0.00231 as a fraction or a mixed number.

- **78.** Write sixteen thousand twenty-five and fourteen thousandths in standard form.
- **80.** Write the numbers $\frac{6}{7}$, $\frac{8}{9}$, 0.75 in order from smallest to largest.

- **55.** $\frac{2.67}{100}$ **56.** $\frac{93}{10}$
- **58.** George Strait pays \$69.71 per month to pay back a loan of \$3136.95. In how many months will the loan be paid off?

314 Chapter 4 | Decimals

Write each fraction as a decimal. Round to the nearest thousandth, if necessary.

| 81. $\frac{7}{100}$ | 82. $\frac{9}{80}$ (Do not round.) | 83. | $\frac{8935}{175}$ |
|----------------------------|---|-----|--------------------|
|----------------------------|---|-----|--------------------|

Insert <, >, *or* = *to make a true statement.*

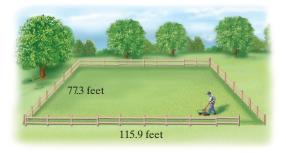
| 84. 402.00032 402 | 2.000032 | 85. 0.230505 | 0.23505 | 86. $\frac{6}{11}$ 0.55 |
|---|----------------------|---------------------|---------|--------------------------------|
| Round each decimal to | o the given place va | lue. | | |
| 87. 42.895, nearest | hundredth | | 88. | 16.34925, nearest thousandth |
| <i>Round each money an</i>
89. \$123.46 | nount to the nearest | t dollar. | 90. | \$3645.52 |
| Add or subtract as ind | licated. | | | |
| 91. 4.9 – 3.2 | | | 92. | 5.23 - 2.74 |
| 93. 200.49 + 16.82 | + 103.002 | | 94. | 0.00236 + 100.45 + 48.29 |

Multiply or divide as indicated. Round to the nearest thousandth, if necessary.

| 95. 2.54 | 96. 3.45 | 97. 0.005)24.5 | 98. 2.3)54.98 |
|-----------------|-----------------|-----------------------|----------------------|
| \times 3.2 | \times 2.1 | | |

Solve.

 \triangle **99.** Tomaso is going to fertilize his lawn, a rectangle that measures 77.3 feet by 115.9 feet. Approximate the area of the lawn by rounding each measurement to the nearest ten feet.



Simplify each expression.

101. $\frac{(3.2)^2}{100}$

100. Estimate the cost of the items to see whether the groceries can be purchased with a \$10 bill.



102. (2.6 + 1.4)(4.5 - 3.6)

Chapter 4 **Getting Ready for the Test** LC

MATCHING Exercises 1 through 12 are Matching exercises.

For Exercises 1 through 4, the number 8603.2855 is rounded to different place values. Match the rounded number in the left column to the correct place it is rounded to in the columns to the right.

| 1. 8603.3 | A. 8603.2855 rounded to ones | D. 8603.2855 rounded to hundredths |
|---------------------|---------------------------------------|--|
| 2. 8600 | B. 8603.2855 rounded to tens | E. 8603.2855 rounded to thousandths |
| 3 . 8603.286 | C. 8603.2855 rounded to tenths | |

```
4. 8603.29
```

For Exercises 5 through 8, Match each fraction or mixed number with its equivalent decimal representation in the right column.

| 5. $\frac{23}{1000}$ | A. 2.03 |
|------------------------------|-----------------|
| 6. $2\frac{3}{10}$ | B. 0.023 |
| • 7. $\frac{23}{100}$ | C. 0.23 |
| 0 8. $2\frac{3}{100}$ | D. 2.3 |

For Exercises 9 through 12, Match the multiplication or division with the correct product or quotient in the right column.

| ● 9. 23.6051 × 100 | А. | 0.0236051 |
|-------------------------------------|----|-----------|
| ● 10. 23.6051 × 10 | В. | 236.051 |
| • 11. $\frac{23.6051}{10}$ | C. | 2360.51 |
| • 12. $\frac{23.6051}{1000}$ | D. | 2.36051 |

MULTIPLE CHOICE Exercises 13 through 17 are all Multiple Choice. Choose the correct answer.

| ● 13. Find 10 - 0.08. | | | |
|------------------------------|------------------------------------|----------------------------------|--------------------------------|
| A. 2 | B. 9.2 | C. 9.02 | D. 9.92 |
| ● 14. Find 10 + 0.08. | | | |
| A. 10.08 | B. 10.8 | C. 18 | D. 10.008 |
| 15. Find 37 + 2.1 | | | |
| A. 58 | B. 39.1 | C. 37.21 | D. 3.91 |
| - | | ed except for placement of the d | ecimal point in the product. |
| Choose the correct | 1 | A. 348.90 | C. 3.4890 |
| | $\frac{\times 1.5}{11630}$ | B. 34.890 | D. 3489.0 |
| | 23260 | | |
| | 34890 | | |
| * | | ted except for placement of the | decimal point in the quotient. |
| Choose the correct | quotient. <u>186</u>
0.38)7.068 | A. 0.186 | C. 18.6 |

B. 1.86 **D.** 186

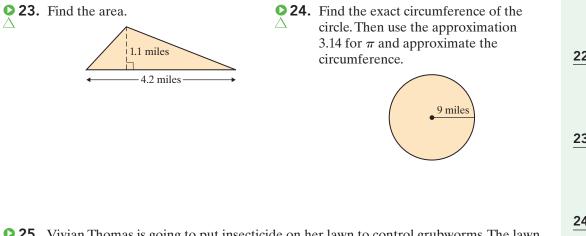
| Chapter 4 | Test MyLab Math or | You Tube For additional practice go to your study plan
in MyLab Math. |
|-------------------------------|---|--|
| Answers | <i>Write the decimal as indicated.</i> • 1. 45.092, in words | 2. Three thousand and fifty-nine thousandths, in standard form |
| _1 | <i>Round the decimal to the indicat</i>
3. 34.8923, nearest tenth | <i>ed place value.</i> 9 4. 0.8623, nearest thousandth |
| 2.
3.
4. | 5. Insert <, >, or = to make statement. 25.0909 25.909 | |
| 5.
6.
7. | Write the decimal as a fraction of 7. 0.345 | a mixed number in simplest form.
8. 24.73 |
| <u>8.</u>
<u>9.</u>
10. | | er as a decimal. If necessary, round to the nearest thousandth |
| <u>11.</u>
<u>12.</u> | 0 9. $\frac{13}{20}$ | 0. $5\frac{8}{9}$ 0.11. $\frac{16}{17}$ |
| <u>13.</u>
<u>14.</u> | | 3. Subtract 8.6 from 20. • 14. 10.2
\times 4.3 |
| <u>15.</u>
<u>16.</u> | | |
| <u>17.</u>
316 | ○15. 0.23)12.88 | 6. 0.165 $(\times 0.47)$ () 17. 7) 46.71 |

Chapter 4 Test

+ 1.63

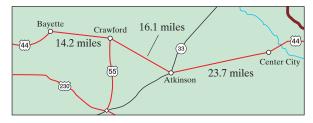
• 18.
$$126.9 \times 100$$
 • 19. $\frac{47.3}{10}$

20.
$$0.3[1.57 - (0.6)^2]$$
 21. $\frac{0.23 + 1}{0.3}$



▶ 25. Vivian Thomas is going to put insecticide on her lawn to control grubworms. The lawn is a rectangle that measures 123.8 feet by 80 feet. The amount of insecticide required is 0.02 ounce per square foot.

- **a.** Find the area of her lawn.
- **b.** Find how much insecticide Vivian needs to purchase.
- **26.** Find the total distance from Bayette to Center City.



| 18. | |
|--------|--|
| | |
| | |
| 19. | |
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| | |
| 20. | |
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| | |
| 21. | |
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| 22. | |
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| | |
| 23. | |
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| | |
| 24. | |
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| | |
| 25. a. | |
| | |
| | |
| b. | |
| | |
| | |
| 26. | |
| | |
| | |

317

| Chapters 1–4 | Cumulative Review | |
|-------------------------------------|---|--|
| Answers | 1. Write 106,052,447 in words. | 2. Write two hundred seventy-six thousand, four in standard form. |
| <u>1.</u>
<u>2.</u>
<u>3.</u> | 3. In 2015, a total of 9,879,465 trucks were sold in the United States. In 2016, total truck sales in the United States had increased by 712,397 vehicles. Find the total number of trucks sold in the United States in 2016. (<i>Source:</i> Alliance of Automobile Manufacturers) | 4. There are 12 fluid ounces of soda in a can. How many fluid ounces of soda are in a case (24 cans) of soda? |
| <u>4.</u>
<u>5.</u> | 5. Subtract: 900 – 174. Check by adding. | 6. Simplify: $5^2 \cdot 2^3$ |
| <u>6.</u>
<u>7.</u>
8. | 7. Round each number to the nearest hundred to find an estimated sum. 294 625 1071 + 349 | 8. Simplify: $7 \cdot \sqrt{144}$ |
| 9. 10. 11. | 9. A digital video disc (DVD) can hold about 4800 megabytes (MB) of information. How many megabytes can 12 DVDs hold? | 10. Find the perimeter and area of the square. |
| <u>12.</u>
<u>13.</u> | 11. Divide: 6819 ÷ 17 | 12. Write $2\frac{5}{8}$ as an improper fraction. |
| <u>14.</u> | 13. Simplify: $4^3 + [3^2 - (10 \div 2)] - 7 \cdot 3$ | 14. Write $\frac{64}{5}$ as a mixed number. |
| <u>15.</u>
<u>16.</u> | 15. Identify the numerator and the denominator: $\frac{3}{7}$ | 16. Simplify: 24 ÷ 8 • 3 |
| <u>17.</u>
<u>18.</u>
318 | 17. Write $\frac{6}{60}$ in simplest form. | 18. Simplify: $(8-5)^2 + (10-8)^3$ |

Cumulative Review

19. Multiply:
$$\frac{3}{4} \cdot 20$$
20. Simplify: $1 + 2[30 + (7 - 2)]$ 21. Divide: $\frac{7}{8} + \frac{2}{9}$ 22. Find the average of 117, 125, and 142.23. Multiply: $1\frac{2}{3} \cdot 2\frac{1}{4}$ 24. A total of \$324 is paid for 36 tickets to the Audubon Zoo. How much did each ticket cost?25. Divide: $\frac{3}{4} + 5$ 26. Simplify:27. $\frac{8}{9} - \frac{1}{9}$ 28. $\frac{4}{15} + \frac{2}{15}$ 29. $\frac{7}{8} - \frac{5}{8}$ 30. $\frac{1}{20} + \frac{3}{20} + \frac{4}{20}$ Write an equivalent fraction with the indicated denominator.31. $\frac{3}{4} = \frac{20}$ 32. $\frac{7}{9} = \frac{45}{45}$ Perform the indicated operations.33. $\frac{11}{15} + \frac{3}{10}$ 34. $\frac{7}{30} - \frac{2}{9}$ 36. A color cartridge for a business printer weighs $2\frac{3}{16}$ pounds. How much do 12 cartridges weigh?

| <u>19.</u> |
|------------|
| 20. |
| 21. |
| 22. |
| 23. |
| 24. |
| 25. |
| 26. |
| 27. |
| 28. |
| 29. |
| 30. |
| 31. |
| 32. |
| 33. |
| 34. |
| 35 |
| 36. |

| 320 | Chapter 4 Decimals | |
|--------------------------|--|--|
| <u>37.</u>
<u>38.</u> | Evaluate each expression.
37. $\left(\frac{1}{4}\right)^2$ | 38. $\left(\frac{7}{11}\right)^2$ |
| <u>39.</u>
<u>40.</u> | 39. $\left(\frac{1}{6}\right)^2 \cdot \left(\frac{3}{4}\right)^3$ | 40. $\left(\frac{1}{2}\right)^3 \cdot \left(\frac{4}{9}\right)^2$ |
| <u>41.</u>
<u>42.</u> | 41. Write 0.43 as a fraction. | 42. Write $\frac{3}{4}$ as a decimal. |
| <u>43.</u>
<u>44.</u> | 43. Insert <, >, or = to form a true statement. 0.378 0.368 | 44. Write "five and six hundredths" in standard form. |
| <u>45.</u>
<u>46.</u> | 45. Subtract: 35.218 – 23.65
Check your answer. | 46. Add: 75.1 + 0.229 |
| 47. | | |
| <u>48.</u> | <i>Multiply.</i>
47. 23.702 × 100 | 48. 1.7 × 0.07 |
| <u>49.</u>
<u>50.</u> | 49. 76,805 × 0.01 | 50. Divide: 0.1157 ÷ 0.013 |

Ratio and Proportion





One of many 3-D cameras

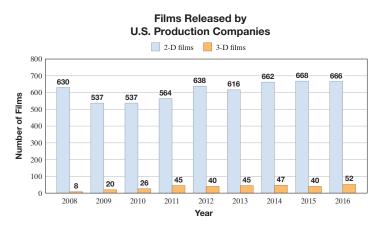
Note: To date, there continues to be much research and controversy over 3-D films. The main controversy is focused on inferior conversions of 2-D filmed movies to 3-D. The main research is focused on watching 3-D movies with adequate light and glasses or without glasses at all.

The 2-D Versus 3-D Film Controversy Continues ...

3-D (three-dimensional) film is a film that enhances the illusion of depth perception. Believe it or not, 3-D films have existed in some form since 1890, but because of high cost and lack of a standardized format, these films are only now starting to be widely shown and produced.

By looking at the graph below, we see an increase in the number of 3-D films released in 2016. Does this mean that more people are viewing them? Recently, opening weekend gross revenue for films in 2-D and 3-D shows that only 30% to 40% of the revenue comes from the 3-D version. The graph shows the trends in the releases of both 2-D and 3-D films in recent years.

In Section 5.1, Exercise 47, we calculate the ratio of 3-D to total films.



5

Having studied fractions in Chapters 2 and 3, we are ready to explore the useful notations of ratio and proportion. Ratio is another name for quotient and is usually written in fraction form. A proportion is an equation with two equal ratios.

Sections

- 5.1 Ratios
- 5.2 Rates

Integrated Review— Ratio and Rate

- 5.3 Proportions
- 5.4 Proportions and Problem Solving

Check Your Progress

Vocabulary Check Chapter Highlights Chapter Review Getting Ready for the Test Chapter Test Cumulative Review

5.1 Ratios

Objectives

🗛 Write Ratios as Fractions. 🕞

B Write Ratios in Simplest Form. 🜔

Objective A Writing Ratios as Fractions

A ratio is the quotient of two quantities. A ratio, in fact, is no different from a fraction, except that a ratio is sometimes written using notation other than fractional notation. For example, the ratio of 1 to 2 can be written as

1 to 2 or $\frac{1}{2}$ or 1:2fractional notation colon notation

These ratios are all read as, "the ratio of 1 to 2."

Concept Check How should each ratio be read aloud?

a. $\frac{8}{5}$ **b.** $\frac{5}{6}$

In this section, we write ratios using fractional notation. If the fraction happens to be an improper fraction, do not write the fraction as a mixed number. Why? The mixed number form is not a ratio or quotient of two quantities.

Writing a Ratio as a Fraction

The order of the quantities is important when writing ratios. To write a ratio as a fraction, write the first number of the ratio as the numerator of the fraction and the second number as the denominator.

Helpful Hint

The ratio of 6 to 11 is $\frac{6}{11}$, not $\frac{11}{6}$.



Example 1 Write the ratio of 12 to 17 using fractional notation.

Solution: The ratio is $\frac{12}{17}$

| Helpful
Hint | |
|--|---------------------|
| - 201111 | orget that order is |
| important when writ
$\frac{17}{12}$ is <i>not</i> the same as | - |

Work Practice 1



Write each ratio using fractional notation.

2. The ratio of 2.6 to 3.1 is
$$\frac{2.6}{3.1}$$
.
3. The ratio of $1\frac{1}{2}$ to $7\frac{3}{4}$ is $\frac{1\frac{1}{2}}{7\frac{3}{4}}$.
Work Practice 2-3



Practice 1

Write the ratio of 20 to 23 using fractional notation.

Practice 2–3

Write each ratio using fractional notation.

2. The ratio of 10.3 to 15.1

3. The ratio of $3\frac{1}{3}$ to $12\frac{1}{5}$

Answers

1.
$$\frac{20}{23}$$
 2. $\frac{10.3}{15.1}$ **3.** $\frac{3\frac{1}{3}}{12\frac{1}{5}}$

Concept Check Answers

a. "the ratio of eight to five" **b.** "the ratio of five to eight"

Objective **B** Writing Ratios in Simplest Form 💟

To simplify a ratio, we just write the fraction in simplest form. Common factors as well as common units can be divided out.

Example 4 Write the ratio of \$15 to \$10 as a fraction in simplest form.

 $\frac{\$15}{\$10} = \frac{15}{10} = \frac{3 \cdot \cancel{5}}{2 \cdot \cancel{5}} = \frac{3}{2}$

Work Practice 4

Helpful Hint

In the example above, although $\frac{3}{2} = 1\frac{1}{2}$, a ratio is a quotient of *two* quantities. For that reason, ratios are not written as mixed numbers.

If a ratio contains decimal numbers or mixed numbers, we simplify by writing the ratio as a ratio of whole numbers.

Write the ratio of 2.6 to 3.1 as a fraction in simplest form.

Solution: The ratio in fraction form is

 $\frac{2.6}{3.1}$

Example 5

Now let's clear the ratio of decimals.

$$\frac{2.6}{3.1} = \frac{2.6}{3.1} \cdot 1 = \frac{2.6}{3.1} \cdot \frac{10}{10} = \frac{2.6 \cdot 10}{3.1 \cdot 10} = \frac{26}{31}$$
 Simplest form

Work Practice 5

1

Example 6 Write the ratio of
$$1\frac{1}{5}$$
 to $2\frac{7}{10}$ as a fraction in simplest form.
 $1\frac{1}{2}$

Solution: The ratio in fraction form is $\frac{1\frac{5}{5}}{2\frac{7}{10}}$.

To simplify, remember that the fraction bar means division.

$$\frac{1\frac{1}{5}}{2\frac{7}{10}} = 1\frac{1}{5} \div 2\frac{7}{10} = \frac{6}{5} \div \frac{27}{10} = \frac{6}{5} \cdot \frac{10}{27} = \frac{6 \cdot 10}{5 \cdot 27} = \frac{2 \cdot \frac{1}{3} \cdot 2 \cdot \frac{1}{5}}{\frac{5}{1} \cdot \frac{3}{1} \cdot 3 \cdot 3} = \frac{4}{9}$$
 Simplest form.
Work Practice 6

Practice 4

Write the ratio of \$8 to \$6 as a fraction in simplest form.

Practice 5

Write the ratio of 3.9 to 8.8 as a fraction in simplest form.

Practice 6

Write the ratio of $2\frac{2}{3}$ to $1\frac{13}{15}$ as a fraction in simplest form.

Answers 4. $\frac{4}{3}$ 5. $\frac{39}{88}$ 6. $\frac{10}{7}$

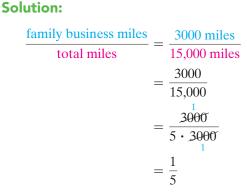
Practice 7

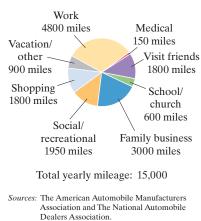
Use the circle graph for Example 7 to write the ratio of work miles to total miles as a fraction in simplest form.



Writing a Ratio from a Circle Graph

The circle graph at the right shows the part of a car's total mileage that falls into a particular category. Write the ratio of family business miles to total miles as a fraction in simplest form.

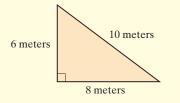




Work Practice 7

igtriangleq Practice 8

Given the triangle shown:



- **a.** Find the ratio of the length of the shortest side to the length of the longest side.
- **b.** Find the ratio of the length of the longest side to the perimeter of the triangle.

Example 8 Given the rectangle shown:

- **a.** Find the ratio of its width to its length.
- **b.** Find the ratio of its length to its perimeter.



Solution:

a. The ratio of its width to its length is

$$\frac{\text{width}}{\text{length}} = \frac{5 \text{ feet}}{8 \text{ feet}} = \frac{5}{8}$$

b. Recall that the perimeter of the rectangle is the distance around the rectangle: 8 + 5 + 8 + 5 = 26 feet. The ratio of its length to its perimeter is

$$\frac{\text{length}}{\text{perimeter}} = \frac{8 \text{ feet}}{26 \text{ feet}} = \frac{8}{26} = \frac{2 \cdot 2 \cdot 2}{2 \cdot 13} = \frac{4}{13}$$

- Work Practice 8
- Concept Check Explain why the answer $\frac{8}{5}$ would be incorrect for part **a** of Example 8.

Answers

7. $\frac{8}{25}$ **8. a.** $\frac{3}{5}$ **b.** $\frac{5}{12}$

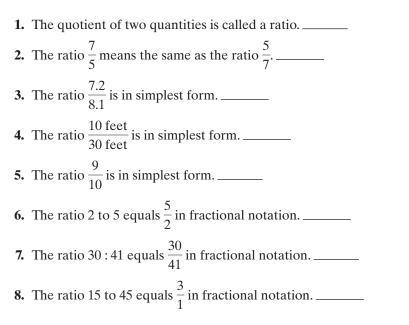
Concept Check Answer

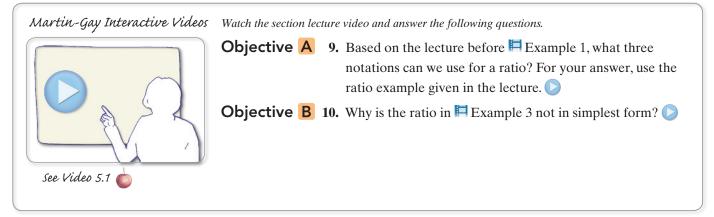
 $\frac{8}{5}$ would be the ratio of the rectangle's length to its width.

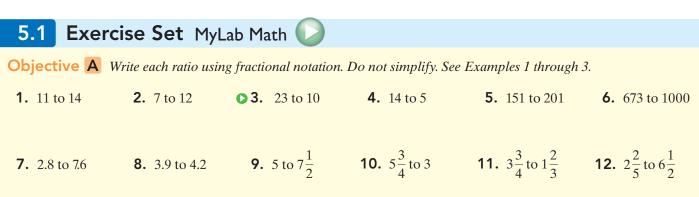
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Vocabulary, Readiness & Video Check

Answer each statement true or false.







Objectives A B Mixed Practice Write each ratio as a ratio of whole numbers using fractional notation. Write the fraction in simplest form. See Examples 1 through 6.

| 17. | 4.63 to 8.21 | 18. 9.61 to 7.62 | 19. | 9 inches to 12 inches | 20. | 14 centimeters to
20 centimeters |
|--------------|---|--|--------------|-----------------------------------|-----|-------------------------------------|
| 21. | 10 hours to 24 hours | 22. 18 quarts to 30 quarts | 23. | \$32 to \$100 | 24. | \$46 to \$102 |
| ○ 25. | 24 days to 14 days | 26. 80 miles to 120 miles | 27. | 32,000 bytes to
46,000 bytes | 28. | 65,000 copies to
15,000 copies |
| 29. | 8 inches to 20 inches | 30. 9 yards to 2 yards | 0 31. | $3\frac{1}{2}$ to $12\frac{1}{4}$ | 32. | $3\frac{1}{3}$ to $4\frac{1}{6}$ |
| 33. | $7\frac{3}{5}$ hours to $1\frac{9}{10}$ hours | 34. $25\frac{1}{2}$ days to $2\frac{5}{6}$ days | | | | |

Write the ratio described in each exercise as a fraction in simplest form. See Examples 7 and 8.

| 35. | Average Weight | of Mature Whales |
|-----|----------------|------------------|
| | Blue Whale | Fin Whale |
| | 145 tons | 50 tons |

Use the table to find the ratio of the weight of an average mature Fin Whale to the weight of an average mature Blue Whale.

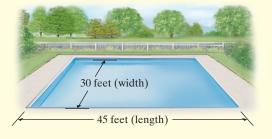
- **37.** The mural *Independence and the Opening of the West,* painted by Thomas Hart Benton on the wall of the lobby of the Harry Truman Presidential Library in Independence, Missouri, occupies a space that measures 32 feet wide by 19 feet high. Find the ratio of the width to the perimeter of this mural.
- \triangle **39.** Find the ratio of the width of a regulation size basketball court to its perimeter.



| 36. | Countries with Small Land Areas | | |
|-----|---------------------------------|------------|--|
| | Tuvalu | San Marino | |
| | 10 sq mi | 24 sq mi | |
| | (Source: World Almanac) | | |

Use the table to find the ratio of the land area of Tuvalu to the land area of San Marino.

- **38.** More than one billion people per year see Wyland's Whaling Wall murals throughout the United States, Canada, Japan, Australia, New Zealand, and Europe. The mural on the Marketplace Design Center in Philadelphia, *East Coast Humpbacks*, measures 125 feet long by 130 feet high. Find the ratio of the height to the perimeter of this mural.
- \triangle **40.** Find the ratio of the width to the perimeter shown of the swimming pool.



At the Hidalgo County School Board meeting one night, there were 125 women and 100 men present.

● **41.** Find the ratio of women to men.

8 feet

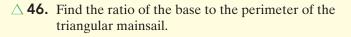
42. Find the ratio of men to the total number of people present.

Blood contains three types of cells: red blood cells, white blood cells, and platelets. For approximately every 600 red blood cells in healthy humans, there are 40 platelets and 1 white blood cell. Use this information for Exercises 43 and 44. (Source: American Red Cross Biomedical Services)

- **43.** Write the ratio of red blood cells to platelet cells.
- **44.** Write the ratio of white blood cells to red blood cells.
- \triangle **45.** Find the ratio of the longest side to the perimeter of the right-triangular-shaped billboard.

5 feet

7 feet





In 2016, 718 films by U.S. production companies were released. Use this information for Exercises 47 and 48.



Solve.

49. Of the U.S. mountains that are over 14,000 feet in elevation, 57 are located in Colorado and 19 are located in Alaska. Find the ratio of the number of mountains over 14,000 feet found in Alaska to the number of mountains over 14,000 feet found in Colorado. (*Source:* U.S. Geological Survey)



- **47.** In 2016, 718 total films were released. Of these, 52 were released in 3-D form. Find the ratio of 3-D films to total films. (*Source:* Motion Picture Association of America)
- **48.** In 2016, 718 total films were released. Of these, 139 were released by production companies who were members of the Motion Picture Association of America (MPAA). Find the ratio of MPAA films to total films. (*Source:* Motion Picture Association of America)
- **50.** Citizens of the United States eat an average of 25 pints of ice cream per year. Residents of the New England states eat an average of 39 pints of ice cream per year. Find the ratio of the amount of ice cream eaten by New Englanders to the amount eaten by the average U.S. citizen. (*Source:* International Dairy Foods Association)





53. As of 2016, Target stores operate in 49 states. Find the ratio of states without Target stores to states with Target stores. (*Source:* Target Corporation)

- **51.** At the 2016 Summer Olympics in Rio de Janeiro, Brazil, a total of 1118 gold medals were awarded, and United Kingdom athletes won a total of 27 gold medals. Find the ration of gold medals won by United Kingdom athletes to the total gold medals awarded. (*Source:* BBC.com)
- **52.** For the 2016 Boston Marathon, 14,463 men and 12,166 women completed the race. Find the ratio of female finishers to male finishers. (*Source:* Boston Athletic Association)
- 54. Four states in the United States officially designate themselves as "commonwealths": Kentucky, Massachusetts, Pennsylvania, and Virginia. Find the ratio of states that are designated as commonwealths to the states that are not designed as commonwealths.

Review

 Divide. See Section 4.5.

 55. 9)20.7
 56. 7)60.2

 57. 3.7)0.555
 58. 4.6)1.15

Concept Extensions

Solve. See the Concept Checks in this section. Write how each should be read as a ratio.

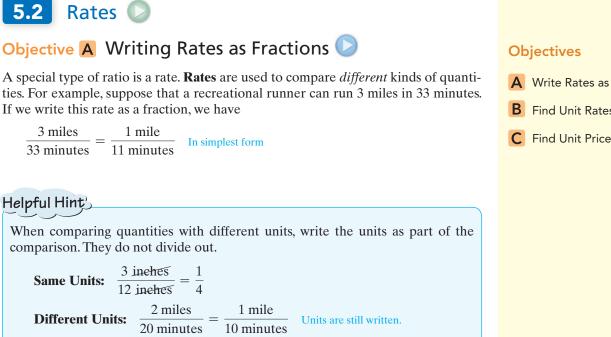
59. $\frac{7}{9}$ **60.** $\frac{12}{5}$ **61.** 30:1 **62.** 5 to 4

63. Is the ratio $\frac{11}{15}$ the same as the ratio of $\frac{15}{11}$? Explain **64.** Explain why the ratio $\frac{40}{17}$ is incorrect for your answer. Exercise 45.

Decide whether each value is a ratio written as a fraction in simplest form. If not, write it as a fraction in simplest form.

65.
$$\frac{\$3}{\$2}$$
 66. $\frac{7.1}{4.3}$ **67.** $\frac{1 \text{ foot}}{30 \text{ inches}}$ **68.** $\frac{2\frac{1}{10}}{3\frac{3}{14}}$ **69.** $4\frac{1}{2}$ **70.** $\frac{12 \text{ inches}}{2 \text{ feet}}$

- **71.** A grocer will refuse a shipment of tomatoes if the ratio of bruised tomatoes to the total batch is at least 1 to 10. A sample is found to contain 3 bruised tomatoes and 33 good tomatoes. Determine whether the shipment should be refused.
- **72.** A panty hose manufacturing machine will be repaired if the ratio of defective panty hose to good panty hose is at least 1 to 20. A quality control engineer found 10 defective panty hose in a batch of 200. Determine whether the machine should be repaired.
- **73.** In 2017, 14 states had primary laws prohibiting all drivers from using a hand-held cell phone while driving. These laws allow law enforcement officers to ticket a driver for using a hand-held cell phone, even if no other traffic offense has occurred. (*Source:* Governors Highway Safety Association)
 - a. Find the ratio of states with primary hand-held cell phone laws to total U.S. states.
 - **b.** Find the number of states with no primary law prohibiting hand-held cell phone use while driving.
 - c. Find the ration of states with primary hand-held cell phone laws to states without such laws.



Helpful Hint

When comparing quantities with different units, write the units as part of the comparison. They do not divide out.

Write the rate as a fraction in simplest form: 10 nails every 6 feet

Solution:

Example 1

 $\frac{10 \text{ nails}}{6 \text{ feet}} = \frac{5 \text{ nails}}{3 \text{ feet}}$

Work Practice 1

Examples

Write each rate as a fraction in simplest form.

2. \$2160 for 12 weeks is $\frac{2160 \text{ dollars}}{12 \text{ weeks}} = \frac{180 \text{ dollars}}{1 \text{ week}}$ **3.** 360 miles on 16 gallons of gasoline is $\frac{360 \text{ miles}}{16 \text{ gallons}} = \frac{45 \text{ miles}}{2 \text{ gallons}}$

Work Practice 2–3

Concept Check True or false? $\frac{16 \text{ gallons}}{4 \text{ gallons}}$ is a rate. Explain.

Objective **B** Finding Unit Rates

A unit rate is a rate with a denominator of 1. A familiar example of a unit rate is 55 mph (or 55 mi/hr), read as "55 miles per hour." This means 55 miles per 1 hour or



Helpful In this context, the word "per" translates to division.



Practice 1

Write the rate as a fraction in simplest form: 12 commercials every 45 minutes

Practice 2–3

Write each rate as a fraction in simplest form.

- **2.** \$1680 for 8 weeks
- 3. 236 miles on 12 gallons of gasoline

Answers

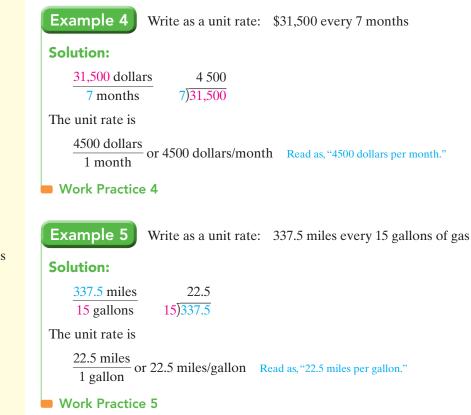
| 1. | 4 commercials | 2. | \$210 | 2 | 59 mi |
|----|---------------|----|-------|----|-------|
| | 15 min | | 1 wk | 3. | 3 gal |

Concept Check Answer

false; a rate compares different kinds of quantities

Writing a Rate as a Unit Rate

To write a rate as a unit rate, divide the numerator of the rate by the denominator.



Objective C Finding Unit Prices 🕑

Rates are used extensively in sports, business, medicine, and science. One of the most common uses of rates is in consumer economics. When a unit rate is "money per item," it is also called a **unit price**.

unit price = $\frac{\text{price}}{\text{number of units}}$

Example 6 Finding Unit Price

A store charges \$3.36 for a 16-ounce jar of picante sauce. What is the unit price in dollars per ounce?

Solution: $\begin{array}{l}
\text{unit} \\
\text{price} = \frac{\text{price}}{\text{number of units}} = \frac{\$3.36}{16 \text{ ounces}} = \frac{\$0.21}{1 \text{ ounce}} \text{ or }\$0.21 \text{ per ounce}
\end{array}$ Work Practice 6

Practice 4

Practice 5

Write as a unit rate: 3200 feet every 8 seconds

Write as a unit rate: 78 bushels of fruit from 12 trees

Practice 6

An automobile rental agency charges \$170 for 5 days for a certain model car. What is the unit price in dollars per day?

Answers

4. 400 ft/sec
5. 6.5 bushels/tree
6. \$34 per day

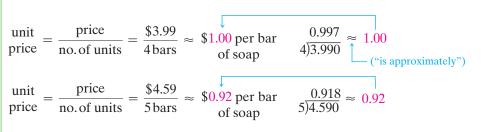
330

Example 7 Finding the Best Buy

Approximate each unit price to decide which is the better buy: 4 bars of soap for \$3.99 or 5 bars of soap for \$4.59.



Solution:



Since the 5-bar package has a cheaper price per bar, it is the better buy.

Work Practice 7

Answer 7. 11-oz bag

Practice 7

Approximate each unit price to

decide which is the better buy

for a bag of nacho chips: 11 ounces for \$3.99 or 16 ounces for \$5.99.

Vocabulary, Readiness & Video Check

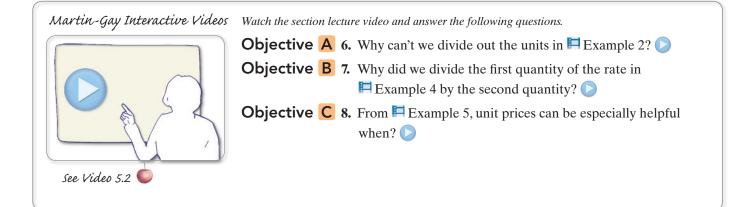
Use the choices below to fill in each blank. Not all choices will be used.

| | rate | division | unit price | unit | | | | |
|----|--|-----------|-------------|------|--|--|--|--|
| | numerator | different | denominator | | | | | |
| 1. | 1. A rate with a denominator of 1 is called a(n) rate. | | | | | | | |
| 2. | • When a rate is written as money per item, a unit rate is called a(n) | | | | | | | |
| • | | 1 | | | | | | |

3. The word *per* translates to "_____."

4. Rates are used to compare ______ types of quantities.

5. To write a rate as a unit rate, divide the ______ of the rate by the ______.



5.2 Exercise Set MyLab Math

Objective A Write each rate as a fraction in simplest form. See Examples 1 through 3.

- 1. 5 shrubs every 15 feet
 - **3.** 15 returns for 100 sales
- **5.** 6 laser printers for 28 computers
 - **7.** 18 gallons of pesticide for 4 acres of crops
 - 9. 6 flight attendants for 200 passengers
- **11.** 355 calories in a 10-fluid-ounce chocolate milkshake (*Source: Home and Garden Bulletin No. 72*, U.S. Department of Agriculture)

- **2.** 14 lab tables for 28 students
- 4. 8 phone lines for 36 employees
- **6.** 4 inches of rain in 18 hours
- **8.** 150 graduate students for 8 advisors
- **10.** 240 pounds of grass seed for 9 lawns
- **12.** 160 calories in an 8-fluid-ounce serving of cream of tomato soup (*Source: Home and Garden Bulletin No. 72*, U.S. Department of Agriculture)
- **Objective B** Write each rate as a unit rate. See Examples 4 and 5.
- **13.** 330 calories in a 3-ounce serving
- **15.** 375 riders in 5 subway cars
 - **17.** A hummingbird moves its wings at a rate of 5400 wingbeats a minute. Write this rate in wingbeats per second.
 - * *
- **19.** \$1,000,000 lottery winnings paid over 20 years
 - **21.** The 2020 projected population of Louisiana is approximately 4,758,720 residents for 64 parishes. (*Note:* Louisiana is the only U.S. state with parishes instead of counties.) (*Source:* Louisiana.gov)



- **14.** 275 miles in 11 hours
- **16.** 18 signs in 6 blocks
- **18.** A bat moves its wings at a rate of 1200 wingbeats a minute. Write this rate in wingbeats per second.



- **20.** 400,000 library books for 8000 students
- **22.** The state of Delaware has 681,950 registered voters for two senators. (*Source:* Delaware.gov)



- **23.** 12,000 good assembly-line products to 40 defective products
- **25.** The combined salary for the 20 highest-paid players of the 2016 World Series Champion Chicago Cubs was approximately \$164,007,000. (*Source:* baseballprospectus.com)
- **27.** Doug Mehrens uses more crayons annually than anyone else in the world. The Phoenix-based artist goes through about 24,000 a year, many of them melted, to complete his contemporary art works. If he works on his art every day, determine how many crayons Doug Mehrens uses each day. Round your answer to the nearest whole crayon. (*Note:* use 1 year = 365 days) (*Source:* Crayola, LLC)
- **29.** For fiscal year 2017, the Smithsonian National Zoological Park in Washington, D.C., requested an annual budget of roughly \$26,000,000 for its 400 different species. (*Source:* Smithsonian Institution)



31. On average, it cost \$1,080,000 to build 12 Habitat for Humanity homes in the Lafayette, Louisiana, area in 2016. (*Source:* habitatlafayette.org)

- **24.** 5,000,000 lottery tickets for 4 lottery winners
- **26.** The top-grossing concert tour of all time was the 2009–2011 U2 360° Tour, which grossed approximately \$737 million for 110 shows worldwide. (*Source:* Billboard)
- **28.** 12,000,000 tons of dust and dirt are trapped by the 25,000,000 acres of lawns in the United States each year. (*Source:* Professional Lawn Care Association of America)

30. On average in 2016, business class passengers spent \$2500 to travel internationally 5000 miles by plane. (*Source:* Airlines for America)



32. In 2016, the number of movie admissions (tickets) sold was about 1320 million for 246 million moviegoers in the United States and Canada. Find the number of tickets sold per moviegoer. Round the answer to the nearest whole. (*Source:* Motion Picture Association of America)

Find each unit rate.

33. The record number of tornadoes in the U.S. for a single calendar day is 209. Write this as a unit rate of tornadoes per hour rounded to the nearest tenth. (*Source:* Storm Prediction Center)



- **35.** Charlie Catlett can assemble 250 computer boards in an 8-hour shift while Suellen Catlett can assemble 402 computer boards in a 12-hour shift.
 - **a.** Find the unit rate of Charlie.
 - **b.** Find the unit rate of Suellen.
 - **c.** Who can assemble computer boards faster, Charlie or Suellen?

For Exercises 37 and 38, round the rates to the nearest tenth.

- **37.** One student drove 400 miles in his car on 14.5 gallons of gasoline. His sister drove 270 miles in her truck on 9.25 gallons of gasoline.
 - **a.** Find the unit rate of the car.
 - **b.** Find the unit rate of the truck.
 - c. Which vehicle gets better gas mileage?

Objective C Find each unit price. See Example 6.

- **39.** \$57.50 for 5 DVDs
- **41.** \$1.19 for 7 bananas

34. Joey Chestnut holds the world record for hot dog eating. In 2016, he ate 73 hot dogs and buns in 10 minutes at the Nathan's Hot Dog Eating Championship at Coney Island, New York. Find his unit rate of hot dogs per minute rounded to the nearest tenth. (*Source: Guinness Book of World Records*)



- **36.** Jerry Stein laid 713 bricks in 46 minutes while his associate, Bobby Burns, laid 396 bricks in 30 minutes.
 - **a.** Find the unit rate of Jerry.
 - **b.** Find the unit rate of Bobby.
 - **c.** Who is the faster bricklayer?
- **38.** Charlotte Leal is a grocery scanner who can scan an average of 100 items in 3.5 minutes while her cousin Leo can scan 148 items in 5.5 minutes.
 - **a.** Find the unit rate of Charlotte.
 - **b.** Find the unit rate of Leo.
 - **c.** Who is the faster scanner?
- **40.** \$0.87 for 3 apples
- **42.** \$73.50 for 6 lawn chairs

Find each unit price and decide which is the better buy. Round to three decimal places. Assume that we are comparing different sizes of the same brand. See Examples 6 and 7.

| 43. | Crackers: | 44. | Pickles: |
|-----|----------------------|-----|---|
| | \$1.19 for 8 ounces | | \$1.89 for 32 ounces |
| | \$1.59 for 12 ounces | | \$0.89 for 18 ounces |
| 45. | Frozen orange juice: | 46. | Eggs: |
| | \$1.69 for 16 ounces | | \$0.69 for a dozen |
| | \$0.69 for 6 ounces | | \$2.10 for a flat $\left(2\frac{1}{2} \text{ dozen}\right)$ |

| 0 47. | Soy sauce:
12 ounces for \$2.29
8 ounces for \$1.49 | 48. Shampoo:
20 ounces for \$1.89
32 ounces for \$3.19 |
|--------------|--|---|
| 49. | Napkins:
100 for \$0.59
180 for \$0.93 | 50. Crackers:
20 ounces for \$2.39
8 ounces for \$0.99 |
| Rev | view | |
| Mul | tiply or divide as indicated. See Sections 4.4 and 4.5. | |
| 51. | 1.7 52. 2.3 53. 3.7 $\times 6$ $\times 9$ $\times 1.2$ | 54. 6.6 55. 2.3) $\overline{4.37}$ 56. 3.5) $\overline{22.75}$ |

Concept Extensions

Fill in the table to calculate miles per gallon.

| (| Beginning Odometer
Reading | Ending Odometer
Reading | Miles Driven | Gallons of Gas
Used | Miles per Gallon
(round to the nearest tenth) |
|-----|-------------------------------|----------------------------|--------------|------------------------|--|
| 57. | 29,286 | 29,543 | | 13.4 | |
| 58. | 16,543 | 16,895 | | 15.8 | |
| 59. | 79,895 | 80,242 | | 16.1 | |
| 60. | 31,623 | 32,056 | | 11.9 | |

Find each unit rate.

- **61.** The longest stairway is the service stairway for the Niesenbahn Cable railway near Spiez, Switzerland. It has 11,674 steps and rises to a height of 7759 feet. Find the unit rate of steps per foot rounded to the nearest tenth of a step. (*Source: Guinness World Records*)
- **62.** In the United States in 2016, the total number of students enrolled in public schools was 50,400,000. There are about 98,300 public schools. Write a unit rate in students per school. Round to the nearest whole. (*Source:* National Center for Education Statistics)

- **65.** Should the rate $\frac{3 \text{ lights}}{2 \text{ feet}}$ be written as $\frac{3}{2}$? Explain why or why not.
- **64.** In your own words, define the phrase "unit price."
 - **66.** Find an item in the grocery store and calculate its unit price.



Integrated Review

Sections 5.1–5.2

Ratio and Rate

| Answers | Write each ratio as a r
simplest form. | atio of whole numbers ı | ising fi | ractional notatio | n. Write the fraction in |
|---------------|---|--|----------|---------------------------------|---|
| 1. | 1. 18 to 20 | 2. 36 to 100 | 3. | 8.6 to 10 | 4. 1.6 to 4.6 |
| 2. | 5. \$8.65 to \$6.95 | 6. 7.2 ounces to 8.4 ounces | 7. | $3\frac{1}{2}$ to 13 | 8. $1\frac{2}{3}$ to $2\frac{3}{4}$ |
| | 9. 8 inches to 12 inc | ches | 10. | 3 hours to 24 h | lours |
| 4. | Find the ratio describe | ed in each problem. | | | |
| 5. | full college profe
Institute of Tech | -2017 academic year, a
essor in Massachusetts
nology earned \$185.9 | 12. | powerhouse. T
the 111 Major | Yankees are a dynastic
hey have won 27 out of
League Baseball World |
| 6. | assistant profess
thousand. Find t | rage. By contrast, an
or averaged \$123.7
he ratio of full profes-
stant professor salary | | Series played f
Major League | through 2015. (<i>Source:</i> Baseball) |
| 7. | • | American Association | | | |
| 8. | | | | | |
| 9. | top 25 movies of | below shows how the 2016 were rated. Use wer the questions. | 14. | Find the ratio length of the s | of the width to the
ign below.
 ← 12 inches → |
| 10. | rated R?
b. Find the ratio | op 25 movies were
o of top 25 PG-rated | | Ì | |
| <u>11.</u> | 2016. | 3-13-rated movies for | | 18 inches | PARKING |
| | Тор 25 Мо | vies of 2016 | | | |
| 12. | R
3 films | PG
8 films | | ļ | 5 |
| <u>13. a.</u> | | | | · | |
| b | | PG-13
14 films | | | |
| 14. | Source: MPAA | | | | |

| Write each rate as a fraction in simplest form. | | |
|---|--|------------|
| 15. 5 offices for every 20 graduate assistants | 16. 6 lights every 15 feet | <u>15.</u> |
| | | <u>16.</u> |
| 17. 100 U.S. senators for 50 states | 18. 5 teachers for every 140 students | 17. |
| | | <u>18.</u> |
| 19. 64 computers every 100 households | 20. 45 students for every 10 computers | 19. |
| | | 20. |
| Write each rate as a unit rate. | | 24 |
| 21. 165 miles in 3 hours | 22. 560 feet in 4 seconds | <u>21.</u> |
| | | 22. |
| 23. 63 employees for 3 fax lines | 24. 85 phone calls for 5 teenagers | <u>23.</u> |
| | | 24. |
| 25. 115 miles every 5 gallons | 26. 112 teachers for 7 computers | 25. |
| | | 2/ |
| 27. 7524 books for 1254 college students | 28. 2002 pounds for 13 adults | <u>26.</u> |
| | | 27. |
| Write each unit price, rounded to the nearest | hundredth, and decide which is the better buy. | 28. |
| 29. Dog food:
\$2.16 for 8 pounds
\$4.99 for 18 pounds | 30. Paper plates:
\$1.98 for 100
\$8.99 for 500 | 29. |
| φ4.77 101 10 poullus | (Round to the nearest thousandth.) | 30. |
| | | |
| 31. Microwave popcorn: | 32. AA batteries: | 31. |
| 3 packs for \$2.39
8 packs for \$5.99 | 4 for \$3.69
10 for \$9.89 | 32. |

Objectives

- A Write Sentences as Proportions.
- B Determine Whether Proportions Are True.

C Find an Unknown Number in a Proportion.

Practice 1

Write each sentence as a proportion.

- **a.** 24 right is to 6 wrong as 4 right is to 1 wrong.
- **b.** 32 Cubs fans is to 18 Mets fans as 16 Cubs fans is to 9 Mets fans.

5.3 Proportions

Objective 🗛 Writing Proportions 🜔

A proportion is a statement that two ratios or rates are equal. For example,

 $\frac{5}{6} = \frac{10}{12}$

is a proportion. We can read this as, "5 is to 6 as 10 is to 12."

Example 1

Write each sentence as a proportion.

- a. 12 diamonds is to 15 rubies as 4 diamonds is to 5 rubies.
- **b.** 5 hits is to 9 at bats as 20 hits is to 36 at bats.

Solution:

| a. | diamonds
rubies | \rightarrow \rightarrow | $\frac{12}{15} = \frac{4}{5}$ | | diamonds
rubies |
|----|--------------------|-----------------------------|-------------------------------|---|--------------------|
| b. | - | \rightarrow | $\frac{5}{2} = \frac{20}{16}$ | ← | 11105 |
| | at bats | \rightarrow | 9 36 | - | at bats |
| | Nork Practi | ce 1 | | | |

Helpful Hint

Notice in the above examples of proportions that the numerators contain the same units and the denominators contain the same units. In this text, proportions will be written so that this is the case.

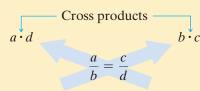
Objective **B** Determining Whether Proportions Are True

Like other mathematical statements, a proportion may be either true or false. A proportion is true if its ratios are equal. Since ratios are fractions, one way to determine whether a proportion is true is to write both fractions in simplest form and compare them.

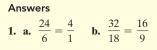
Another way is to compare cross products as we did in Section 2.3.

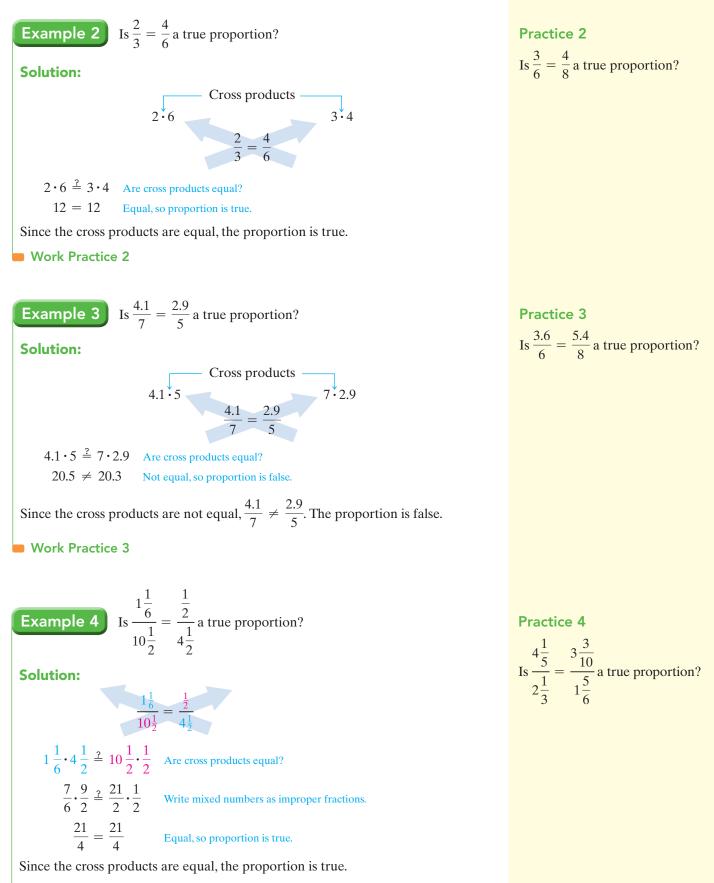
Note: In the box below, we are using letters to represent numbers. We later call these letters *variables*.

Using Cross Products to Determine Whether Proportions Are True or False



If cross products are *equal*, the proportion is *true*. If cross products are *not equal*, the proportion is *false*. Copyright 2019 Pearson Education, Inc.





Work Practice 4

Answers 2. yes 3. no 4. yes Concept Check Think about cross products and write the true proportion $\frac{5}{8} = \frac{10}{16}$ in two other ways so that each result is also a true proportion.

(*Note:* There are no units attached in this proportion.)

Objective C Finding Unknown Numbers in Proportions D

When one number of a proportion is unknown, we can use cross products to find the unknown number. For example, to find the unknown number n in the proportion

 $\frac{n}{30} = \frac{2}{3}$, we first find the cross products.



If the proportion is true, then cross products are equal.

 $n \cdot 3 = 30 \cdot 2$ Set the cross products equal to each other.

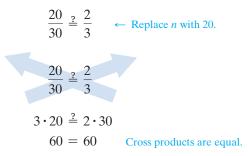
 $n \cdot 3 = 60$ Write $2 \cdot 30$ as 60.

To find the unknown number n, we ask ourselves, "What number times 3 is 60?" The number is 20 and can be found by dividing 60 by 3.

$$n = \frac{60}{3}$$
 Divide 60 by the number multiplied by *n*.
 $n = 20$ Simplify.

Thus, the unknown number is 20.

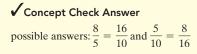
Check: To *check*, let's replace *n* with this value, 20, and verify that a true proportion results.

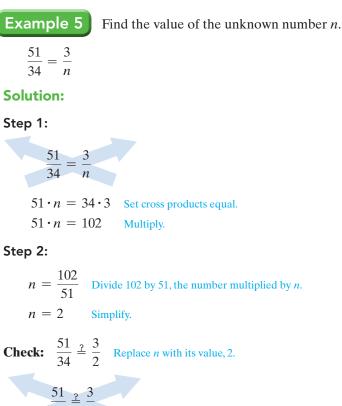


Finding an Unknown Value n in a Proportion

Step 1: Set the cross products equal to each other.

Step 2: Divide the number not multiplied by *n* by the number multiplied by *n*.





 $\frac{51}{34} \stackrel{?}{=} \frac{3}{2}$ $51 \cdot 2 \stackrel{?}{=} 34 \cdot 3$ Cross products are equal, 102 = 102 so the proportion is true.

Work Practice 5

Example 6 Find the unknown number *n*. $\frac{7}{n} = \frac{6}{5}$

Solution:

Step 1:

$$\frac{7}{n} = \frac{6}{5}$$

 $7 \cdot 5 = n \cdot 6$ Set the cross products equal to each other. $35 = n \cdot 6$ Multiply.

Step 2:

$$\frac{35}{6} = n$$
 Divide 35 by 6, the number multiplied by *n*.
$$5\frac{5}{6} = n$$

Check: Check to see that $5\frac{5}{6}$ is the unknown number.

Work Practice 6

Practice 5

Find the value of the unknown number *n*.

$$\frac{15}{2} = \frac{60}{n}$$

Practice 6 Find the unknown number *n*.

$$\frac{8}{n} = \frac{5}{9}$$

Answers

5.

$$n = 8$$
 6. $n = 14\frac{2}{5}$

Chapter 5 | Ratio and Proportion

Practice 7

Find the unknown number *n*.

$$\frac{n}{6} = \frac{0.7}{1.2}$$

Example 7 Find the unknown number *n*. $\frac{n}{3} = \frac{0.8}{1.5}$ **Solution: Step 1:** $n \cdot 1.5 = 3 \cdot 0.8$ Set the cross products equal to each other. $n \cdot 1.5 = 2.4$ Multiply. **Step 2:** $n = \frac{2.4}{1.5}$ Divide 2.4 by 1.5, the number multiplied by *n*. n = 1.6 Simplify.

Check: Check to see that 1.6 is the unknown number.

Example 8 Find the unknown number *n*.

Work Practice 7



Answers

7. n = 3.5 **8.** $n = 11\frac{1}{7}$

Find the unknown number *n*.

$$\frac{n}{4\frac{1}{3}} = \frac{4\frac{1}{2}}{1\frac{3}{4}}$$

 $\frac{1\frac{2}{3}}{3\frac{1}{4}} = \frac{n}{2\frac{3}{5}}$

Solution:

Step 1: $\frac{1\frac{2}{3}}{3\frac{1}{4}} = \frac{n}{2\frac{3}{5}}$ $1\frac{2}{3} \cdot 2\frac{3}{5} = 3\frac{1}{4} \cdot n \quad \text{Set the cross products equal to each other.}$ $\frac{13}{3} = 3\frac{1}{4} \cdot n \quad \text{Multiply.} \ 1\frac{2}{3} \cdot 2\frac{3}{5} = \frac{5}{3} \cdot \frac{13}{5} = \frac{\frac{1}{3} \cdot 13}{3 \cdot \frac{3}{5}} = \frac{13}{3}$ $\frac{13}{3} = \frac{13}{4} \cdot n \quad \text{Write } 3\frac{1}{4} \text{ as } \frac{13}{4}.$

Step 2:

$$\frac{13}{3} \div \frac{13}{4} = n$$
 Divide $\frac{13}{3}$ by $\frac{13}{4}$, the number multiplied by *n*.

or

 $n = \frac{13}{3} \cdot \frac{4}{13} = \frac{4}{3}$ or $1\frac{1}{3}$ Divide by multiplying by the reciprocal. **Check:** Check to see that $1\frac{1}{3}$ is the unknown number.

Work Practice 8

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Vocabulary, Readiness & Video Check

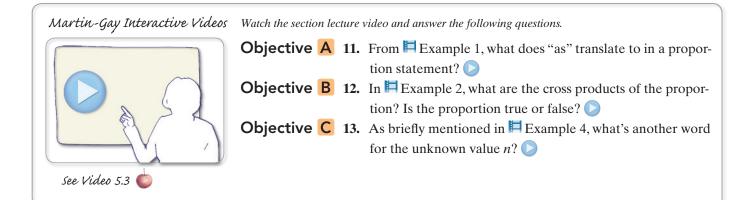
Use the words and phrases below to fill in each blank.

| ratio | cross products | true |
|-------|----------------|------|
| false | proportion | |

- **1.** $\frac{4.2}{8.4} = \frac{1}{2}$ is called a ______ while $\frac{7}{8}$ is called a(n) ______.
- 2. In $\frac{a}{b} = \frac{c}{d}$, $a \cdot d$ and $b \cdot c$ are called in _____.
- 3. In a proportion, if cross products are equal, the proportion is ______.
- 4. In a proportion, if cross products are not equal, the proportion is _____

Use cross products and mentally determine whether each proportion is true or false.

5.
$$\frac{2}{1} = \frac{6}{3}$$
 6. $\frac{3}{1} = \frac{15}{5}$ **7.** $\frac{1}{2} = \frac{3}{5}$ **8.** $\frac{2}{11} = \frac{1}{5}$ **9.** $\frac{2}{3} = \frac{40}{60}$ **10.** $\frac{3}{4} = \frac{6}{8}$



Exercise Set MyLab Math 5.3

Objective A *Write each sentence as a proportion. See Example 1.*

- ▶ 1. 10 diamonds is to 6 opals as 5 diamonds is to 3 opals.
 - **3.** 3 printers is to 12 computers as 1 printer is to 4 computers.
 - **5.** 6 eagles is to 58 sparrows as 3 eagles is to 29 sparrows.
 - 7. $2\frac{1}{4}$ cups of flour is to 24 cookies as $6\frac{3}{4}$ cups of flour is **8.** $1\frac{1}{2}$ cups of milk is to 10 bagels as $\frac{3}{4}$ cup of milk is to to 72 cookies.

- **2.** 8 books is to 6 courses as 4 books is to 3 courses.
- 4. 4 hit songs is to 16 releases as 1 hit song is to 4 releases.
- **6.** 12 errors is to 8 pages as 1.5 errors is to 1 page.
- 5 bagels.

- **9.** 22 vanilla wafers is to 1 cup of cookie crumbs as 55 vanilla wafers is to 2.5 cups of cookie crumbs. (*Source:* Based on data from *Family Circle* magazine)
- **10.** 1 cup of instant rice is to 1.5 cups of cooked rice as 1.5 cups of instant rice is to 2.25 cups of cooked rice. (*Source:* Based on data from *Family Circle* magazine)

| Objective B Determine whether each proportion is a true proportion. See Examples 2 through 4. | | | | | | |
|--|---|--|---|--|---|--|
| 11. $\frac{15}{9} = \frac{5}{3}$ | 12. $\frac{8}{6} = \frac{20}{15}$ | • 13. $\frac{8}{6} = \frac{9}{7}$ | 14. $\frac{7}{12} = \frac{4}{7}$ | • 15. $\frac{9}{36} = \frac{2}{8}$ | 16. $\frac{8}{24} = \frac{3}{9}$ | |
| 17. $\frac{5}{8} = \frac{625}{1000}$ | 18. $\frac{30}{50} = \frac{600}{1000}$ | 19. $\frac{0.8}{0.3} = \frac{0.2}{0.6}$ | 20. $\frac{0.7}{0.4} = \frac{0.3}{0.1}$ | 21. $\frac{8}{10} = \frac{5.6}{0.7}$ | 22. $\frac{4.2}{8.4} = \frac{5}{10}$ | |
| 23. $\frac{\frac{3}{4}}{\frac{4}{3}} = \frac{\frac{1}{2}}{\frac{8}{9}}$ | 24. $\frac{\frac{2}{5}}{\frac{2}{7}} = \frac{\frac{1}{10}}{\frac{1}{\frac{1}{3}}}$ | 25. $\frac{2\frac{2}{5}}{\frac{2}{3}} = \frac{1\frac{1}{9}}{\frac{1}{4}}$ | 26. $\frac{5\frac{5}{8}}{\frac{5}{3}} = \frac{4\frac{1}{2}}{1\frac{1}{5}}$ | 27. $\frac{\frac{4}{5}}{\frac{6}{6}} = \frac{\frac{6}{5}}{\frac{9}{9}}$ | 28. $\frac{\frac{6}{7}}{\frac{7}{3}} = \frac{\frac{10}{7}}{\frac{7}{5}}$ | |

Objectives A B Mixed Practice—Translating Write each sentence as a proportion. Then determine whether *the proportion is a true proportion. See Examples 1 through 4.*

- **29.** eight is to twelve as four is to six
- **31.** five is to two as thirteen is to five
- **33.** one and eight tenths is to two as four and five tenths is to five
- **35.** two thirds is to one fifth as two fifths is to one ninth

- **30.** six is to eight as nine is to twelve
- **32.** four is to three as seven is to five
- **34.** fifteen hundredths is to three as thirty-five hundredths is to seven
- **36.** ten elevenths is to three fourths as one fourth is to one half

Objective C For each proportion, find the unknown number n. See Examples 5 through 8.

37. $\frac{n}{5} = \frac{6}{10}$ **38.** $\frac{n}{3} = \frac{12}{9}$ **39.** $\frac{18}{54} = \frac{3}{n}$ **40.** $\frac{25}{100} = \frac{7}{n}$ **41.** $\frac{n}{8} = \frac{50}{100}$ **42.** $\frac{n}{21} = \frac{12}{18}$ **43.** $\frac{8}{15} = \frac{n}{6}$ **44.** $\frac{12}{10} = \frac{n}{16}$

| 45. $\frac{24}{n} = \frac{60}{96}$ | 46. $\frac{26}{n} = \frac{28}{49}$ | 47. $\frac{3.5}{12.5} = \frac{7}{n}$ | 48. $\frac{0.2}{0.7} = \frac{8}{n}$ |
|--|---|---|--|
| 49. $\frac{0.05}{12} = \frac{n}{0.6}$ | 50. $\frac{7.8}{13} = \frac{n}{2.6}$ | • 51. $\frac{8}{\frac{1}{3}} = \frac{24}{n}$ | 52. $\frac{12}{\frac{3}{4}} = \frac{48}{n}$ |
| 53. $\frac{\frac{1}{3}}{\frac{3}{8}} = \frac{\frac{2}{5}}{\frac{1}{8}}$ | 54. $\frac{\frac{7}{9}}{\frac{8}{27}} = \frac{\frac{1}{4}}{\frac{1}{n}}$ | 55. $\frac{12}{n} = \frac{\frac{2}{3}}{\frac{6}{9}}$ | 56. $\frac{24}{n} = \frac{\frac{8}{15}}{\frac{5}{9}}$ |
| • 57. $\frac{n}{1\frac{1}{5}} = \frac{4\frac{1}{6}}{6\frac{2}{3}}$ | 58. $\frac{n}{3\frac{1}{8}} = \frac{7\frac{3}{5}}{2\frac{3}{8}}$ | 59. $\frac{25}{n} = \frac{3}{\frac{7}{30}}$ | 60. $\frac{9}{n} = \frac{5}{\frac{11}{15}}$ |

Review

Insert < or > to form a true statement. See Sections 3.5 and 4.2.

| 61. 8.01 | 8.1 | 62. 7.26 | 7.026 | 63. $2\frac{1}{2}$ | $2\frac{1}{3}$ |
|---------------------------|----------------|----------------------------|----------------|----------------------------|----------------|
| 64. $9\frac{1}{5}$ | $9\frac{1}{4}$ | 65. 5 $\frac{1}{3}$ | $6\frac{2}{3}$ | 66. 1 $\frac{1}{2}$ | $2\frac{1}{2}$ |

Concept Extensions

Use the numbers in each proportion to write two other true proportions. See the Concept Check in this section.

67. $\frac{9}{15} = \frac{3}{5}$ **68.** $\frac{1}{4} = \frac{5}{20}$

69.
$$\frac{6}{18} = \frac{1}{3}$$
 70. $\frac{2}{7} = \frac{4}{18}$

- **71.** If the proportion $\frac{a}{b} = \frac{c}{d}$ is a true proportion, write two other true proportions using the same letters.
- **73.** Explain the difference between a ratio and a proportion.

- 4
- 72. Write a true proportion.
- **74.** Explain how to find the unknown number in a proportion such as $\frac{n}{18} = \frac{12}{8}$.

For each proportion, find the unknown number n. For Exercises 75 through 80, round your answer to the given place value.

75.
$$\frac{3.2}{0.3} = \frac{n}{1.4}$$
Round to the nearest tenth

77. $\frac{n}{5.2} = \frac{0.08}{6}$ Round to the nearest hundredth.

76.
$$\frac{1.8}{n} = \frac{2.5}{8.4}$$

Round to the nearest tenth.

78. $\frac{4.25}{6.03} = \frac{5}{n}$

Round to the nearest hundredth.

86. $\frac{1425}{1062} = \frac{n}{177}$

79. $\frac{43}{17} = \frac{8}{n}$ Round to the nearest thousandth.

82.
$$\frac{0}{2} = \frac{n}{3.5}$$
 83. $\frac{n}{1150} = \frac{588}{483}$

85. $\frac{222}{1515} = \frac{37}{n}$

84. $\frac{585}{n} = \frac{117}{474}$

81. $\frac{n}{7} = \frac{0}{8}$

80. $\frac{n}{12} = \frac{18}{7}$ Round to the nearest hundredth.

5.4 Proportions and Problem Solving

Objective A Solving Problems by Writing Proportions

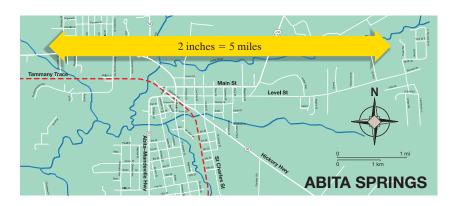
Writing proportions is a powerful tool for solving problems in almost every field, including business, chemistry, biology, health sciences, and engineering, as well as in daily life. Given a specified ratio (or rate) of two quantities, a proportion can be used to determine an unknown quantity.

In this section, we use the same problem-solving steps that we have used earlier in this text.

Example 1

1 Determining Distances from a Map

On a chamber of commerce map of Abita Springs, 5 miles corresponds to 2 inches. How many miles correspond to 7 inches?



Practice 1

Objective

On an architect's blueprint, 1 inch corresponds to 4 feet. How long is a wall represented

A Solve Problems by Writing Proportions.

by a $4\frac{1}{4}$ -inch line on the

blueprint?



Solution:

1. UNDERSTAND. Read and reread the problem. You may want to draw a diagram.

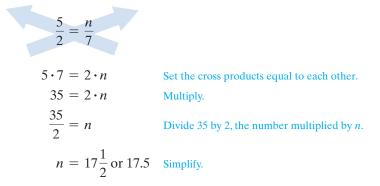
| | 15 miles | | betw | | 5 and 20 miles
0 miles |
|----------|----------|----------|------|------|---------------------------|
| 5 miles | 5 miles | 5 miles | 5 m | iles | |
| 2 inches | 2 inches | 2 inches | 2 in | ches | |
| | 6 inches | | 7 in | ches | 8 inches |

From the diagram we can see that a reasonable solution should be between 15 and 20 miles.

2. TRANSLATE. We will let *n* represent our unknown number. Since 5 miles corresponds to 2 inches as *n* miles corresponds to 7 inches, we have the proportion

miles $\rightarrow \frac{5}{2} = \frac{n}{7} \leftarrow \text{miles}$ inches $\rightarrow \frac{5}{2} = \frac{n}{7} \leftarrow \text{inches}$

3. SOLVE: In earlier sections, we estimated to obtain a reasonable answer. Notice we did this in Step 1 above.



- **4.** INTERPRET. *Check* your work. This result is reasonable since it is between 15 and 20 miles. *State* your conclusion: 7 inches corresponds to 17.5 miles.
- Work Practice 1

Helpful Hint

We can also solve Example 1 by writing the proportion

 $\frac{2 \text{ inches}}{5 \text{ miles}} = \frac{7 \text{ inches}}{n \text{ miles}}$

Although other proportions may be used to solve Example 1, we will solve by writing proportions so that the numerators have the same unit measures and the denominators have the same unit measures.

Example 2 Finding Medicine Dosage

The standard dose of an antibiotic is 4 cc (cubic centimeters) for every 25 pounds (lb) of body weight. At this rate, find the standard dose for a 140-lb woman.

Solution:

1. UNDERSTAND. Read and reread the problem. You may want to draw a diagram to estimate a reasonable solution.

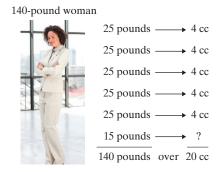
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Practice 2

An auto mechanic recommends that 3 ounces of isopropyl alcohol be mixed with a tankful of gas (14 gallons) to increase the octane of the gasoline for better engine performance. At this rate, how many gallons of gas can be treated with a 16-ounce bottle of alcohol?

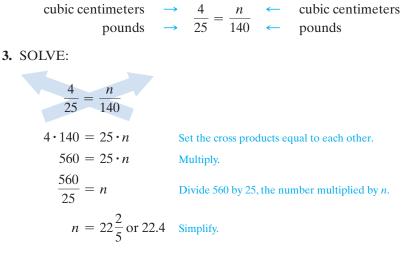
Answer

```
2. 74\frac{2}{3} or 74.\overline{6} gal
```



From the diagram, we can see that a reasonable solution is a little over 20 cc.

2. TRANSLATE. We will let *n* represent the unknown number. From the problem, we know that 4 cc is to 25 pounds as *n* cc is to 140 pounds, or



4. INTERPRET. *Check* your work. This result is reasonable since it is a little over 20 cc. *State* your conclusion: The standard dose for a 140-lb woman is 22.4 cc.

Work Practice 2

Example 3

3 Calculating Supplies Needed to Fertilize a Lawn

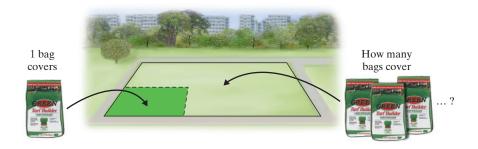
A 50-pound bag of fertilizer covers 2400 square feet of lawn. How many bags of fertilizer are needed to cover a town square containing 15,360 square feet of lawn? Round the answer up to the nearest whole bag.



If a gallon of paint covers 400 square feet, how many gallons are needed to paint a retaining wall that is 260 feet long and 4 feet high? Round the answer up to the nearest whole gallon.

Solution:

1. UNDERSTAND. Read and reread the problem. Draw a picture.



Since one bag covers 2400 square feet, let's see how many 2400's there are in 15,360. We will estimate. The number 15,360 rounded to the nearest thousand is 15,000 and 2400 rounded to the nearest thousand is 2000. Then

$$15,000 \div 2000 = 7\frac{1}{2}$$
 or 7.5.

2. TRANSLATE. We'll let *n* represent the unknown number. From the problem, we know that 1 bag is to 2400 square feet as *n* bags is to 15,360 square feet.

bags
$$\rightarrow \frac{1}{2400} = \frac{n}{15,360} \leftarrow \frac{1}{15,360}$$
 square feet

$$\frac{1}{2400} = \frac{n}{15,360}$$

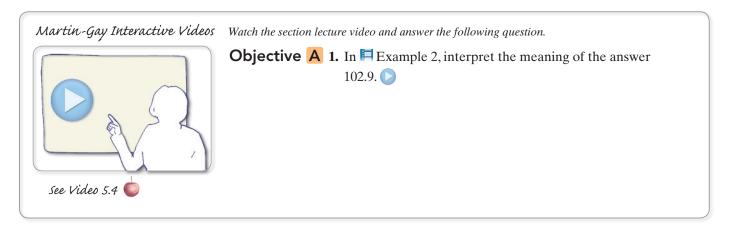
 $1 \cdot 15,360 = 2400 \cdot n$ Set the cross products equal to each other. $15,360 = 2400 \cdot n$ Multiply. $\frac{15,360}{2400} = n$ Divide 15,360 by 2400, the number multiplied by *n*. n = 6.4 Simplify.

4. INTERPRET. *Check* that replacing *n* with 6.4 makes the proportion true. Is the answer reasonable? Yes, because it's close to $7\frac{1}{2}$ or 7.5. Because we must buy whole bags of fertilizer, 7 bags are needed. *State* your conclusion: To cover 15,360 square feet of lawn, 7 bags are needed.

Work Practice 3

Concept Check You are told that 12 ounces of ground coffee will brew enough coffee to serve 20 people. How could you estimate how much ground coffee will be needed to serve 95 people?

Vocabulary, Readiness & Video Check



5.4 Exercise Set MyLab Math

Objective A Solve. For Exercises 1 and 2, the solutions have been started for you. See Examples 1 through 3.

An NBA basketball player averages 45 baskets for every 100 attempts.

1. If he attempted 800 field goals, how many field goals did he make?

Start the solution:

1. UNDERSTAND the problem. Reread it as many times as needed. Let's let

n = how many field goals he made

2. TRANSLATE into an equation.

baskets (field goals) $\rightarrow 45$ attempts $\rightarrow 100 = \frac{n}{800} \leftarrow$ baskets (field goals) \leftarrow attempts

3. SOLVE the equation. Set cross products equal to each other and solve.

$$\frac{45}{100} \times \frac{n}{800}$$

After SOLVING, then

4. INTERPRET.

It takes a word processor 30 minutes to word process and spell check 4 pages.

3. Find how long it takes her to word process and spell check 22 pages.

University Law School accepts 2 out of every 7 applicants.

5. If the school accepted 180 students, find how many applications they received.

2. If he made 225 baskets, how many did he attempt?

Start the solution:

- 1. UNDERSTAND the problem. Reread it as many times as needed. Let's let
- n = how many baskets attempted **2.** TRANSLATE into an equation

| I RANSLATE into an equation. | | | | | | |
|------------------------------|---------------|-----|-----|---|----------|--|
| baskets | \rightarrow | 45 | 225 | ← | baskets | |
| attempts | \rightarrow | 100 | n | ← | attempts | |

3. SOLVE the equation. Set cross products equal to each other and solve.

$$\frac{45}{100} \times \frac{225}{n}$$

After SOLVING, then **4.** INTERPRET.

- **4.** Find how many pages she can word process and spell check in 4.5 hours.
- **6.** If the school accepted 150 students, find how many applications they received.

- On an architect's blueprint, 1 inch corresponds to 8 feet.
- **7.** Find the length of a wall represented by a line
 - $2\frac{7}{8}$ inches long on the blueprint.

8. Find the length of a wall represented by a line $5\frac{1}{4}$ inches long on the blueprint.

A human-factors expert recommends that there be at least 9 square feet of floor space in a college classroom for every student in the class.

- \triangle **9.** Find the minimum floor space that 30 students require.
- \triangle **10.** Due to a lack of space, a university converts a 21-by-15-foot conference room into a classroom. Find the maximum number of students the room can accommodate.

A Honda Civic Hybrid car averages 627 miles on a 12.3-gallon tank of gas.

- **11.** Manuel Lopez is planning a 1250-mile vacation trip in his Honda Civic Hybrid. Find how many gallons of gas he can expect to burn. Round to the nearest gallon.
- **12.** Ramona Hatch has enough money to put 6.9 gallons of gas in her Honda Civic Hybrid. She is planning on driving home from college for the weekend. If her home is 290 miles away, should she make it home before she runs out of gas?

The scale on an Italian map states that 1 centimeter corresponds to 30 kilometers.

- Rome
- **13.** Find how far apart Milan and Rome are if their corresponding points on the map are 15 centimeters apart.
- 14. On the map, a small Italian village is located 0.4 centimeter from the Mediterranean Sea. Find the actual distance.

A bag of Scotts fertilizer covers 3000 square feet of lawn.

- \triangle **15.** Find how many bags of fertilizer should be purchased to cover a rectangular lawn 260 feet by 180 feet.
- \triangle **16.** Find how many bags of fertilizer should be purchased to cover a square lawn measuring 160 feet on each side.



- A Cubs baseball player gets 3 hits every 8 times at bat.
- **17.** If this Cubs player comes up to bat 40 times in the World Series, find how many hits he would be expected to get.
- **18.** At this rate, if he got 12 hits, find how many times he batted.
- A survey reveals that 2 out of 3 people prefer Coke to Pepsi.
- **19.** In a room of 40 people, how many people are likely to prefer Coke? Round the answer to the nearest person.
- **20.** In a college class of 36 students, find how many students are likely to prefer Pepsi.

A self-tanning lotion advertises that a 3-oz bottle will provide four applications.

- **21.** Jen Haddad found a great deal on a 14-oz bottle of the self-tanning lotion she had been using. Based on the advertising claims, how many applications of the self-tanner should Jen expect? Round down to the smaller whole number.
- **22.** The Community College thespians need fake tans for a play they are doing. If the play has a cast of 35, how many ounces of self-tanning lotion should the cast purchase? Round up to the next whole number of ounces.

The school's computer lab goes through 5 reams of printer paper every 3 weeks.

- ▶ 23. Find out how long a case of printer paper is likely to last (a case of paper holds 8 reams of paper). Round to the nearest week.
- **24.** How many cases of printer paper should be purchased to last the entire semester of 15 weeks? Round up to the next case.

A recipe for pancakes calls for 2 cups flour and $1\frac{1}{2}$ cups milk to make a serving for four people.

- **25.** Ming has plenty of flour, but only 4 cups milk. How many servings can he make?
- **26.** The swim team has a weekly breakfast after early practice. How much flour will it take to make pancakes for 18 swimmers?

Solve.

- **27.** In the Seattle Space Needle, the elevators whisk you to the revolving restaurant at a speed of 800 feet in 60 seconds. If the revolving restaurant is 500 feet up, how long will it take you to reach the restaurant by elevator? (*Source:* Seattle Space Needle)
- **28.** A 16-oz grande Tazo Black Iced Tea at Starbucks has 80 calories. How many calories are there in a 24-oz venti Tazo Black Iced Tea? (*Source:* Starbucks Coffee Company)

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- **29.** Mosquitos are annoying insects. To eliminate mosquito larvae, a certain granular substance can be applied to standing water in a ratio of 1 tsp per 25 sq ft of standing water.
 - **a.** At this rate, find how many teaspoons of granules must be used for 450 square feet.
 - **b.** If 3 tsp = 1 tbsp, how many tablespoons of granules must be used?



31. The daily supply of oxygen for one person is provided by 625 square feet of lawn. A total of 3750 square feet of lawn would provide the daily supply of oxygen for how many people? (*Source:* Professional Lawn Care Association of America)

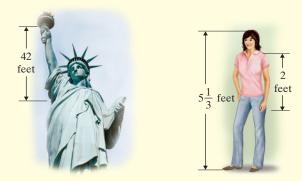
- **30.** Another type of mosquito control is liquid, where 3 oz of pesticide is mixed with 100 oz of water. This mixture is sprayed on roadsides to control mosquito breeding grounds hidden by tall grass.
 - a. If one mixture of water with this pesticide can treat 150 feet of roadway, how many ounces of pesticide are needed to treat one mile? (*Hint:* 1 mile = 5280 feet)
 - **b.** If 8 liquid ounces equals one cup, write your answer to part **a** in cups. Round to the nearest cup.
- **32.** In 2015, approximately \$23 billion of the \$60 billion Americans spent on their pets was spent on pet food. Petsmart had \$6,962,600,000 in net sales that year. How much of Petsmart's net sales would you expect to have been spent on pet food? Round to the nearest thousand. (*Source:* American Pet Products Manufacturers Association and Petsmart)



33. A student would like to estimate the height of the Statue of Liberty in New York City's harbor. The length of the Statue of Liberty's right arm is 42 feet. The student's right arm is 2 feet long and her height

is $5\frac{1}{3}$ feet. Use this information to estimate the

height of the Statue of Liberty. How close is your estimate to the statue's actual height of 111 feet, 1 inch from heel to top of head? (*Source:* National Park Service)



- **34.** The length of the Statue of Liberty's index finger is 8 feet while the height to the top of the head is about 111 feet. Suppose your measurements are proportionally the same as this statue and your height is 5 feet.
 - **a.** Use this information to find the proposed length of your index finger. Give an exact measurement and then a decimal rounded to the nearest hundredth.
 - **b.** Measure your index finger and write it as a decimal in feet rounded to the nearest hundredth. How close is the length of your index finger to the answer to part **a**? Explain why.

- **35.** There are 72 milligrams of cholesterol in a 3.5-ounce serving of lobster. How much cholesterol is in 5 ounces of lobster? Round to the nearest tenth of a milligram. (*Source:* The National Institutes of Health)
 - **37.** The Comcast Building in New York City is 850 feet tall and contains 69 stories. The Empire State Building contains 102 stories. If the Empire State Building has the same number of feet per floor as the Comcast Building, approximate its height rounded to the nearest foot. (*Source:* skyscrapers.com)
- **39.** Medication is prescribed in 7 out of every 10 hospital emergency room visits that involve an injury. If a large urban hospital had 620 emergency room visits involving an injury in the past month, how many of these visits would you expect included a prescription for medication? (*Source:* National Center for Health Statistics)
 - **41.** In 2016, six out every 20 vehicles sold in the United States were SUV crossovers. Approximately 7 million vehicles were sold in the United States in 2016. How many of them were SUV crossovers? Round to the nearest million. (*Source: Wall Street Journal*)

- **36.** There are 76 milligrams of cholesterol in a 3-ounce serving of skinless chicken. How much cholesterol is in 8 ounces of chicken? (*Source:* USDA)
- **38.** In 2017, approximately 125 million of the 152 million U.S. employees worked in service industries. In a town of 19,000 workers, how many would be expected to work in service-industry jobs? (*Source:* U.S. Bureau of Labor Statistics)
- **40.** One pound of firmly packed brown sugar yields $2\frac{1}{4}$ cups. How many pounds of brown sugar will be required in a recipe that calls for 6 cups of firmly packed brown sugar? (*Source:* Based on data from *Family Circle* magazine)
- **42.** In the first few months of 2017, three out of every 40 computers sold were Apple products. Approximately 65,000 computers were sold in the United States in February 2017. How many of these were Apple products? (*Source:* Gartner.com)

When making homemade ice cream in a hand-cranked freezer, the tub containing the ice cream mix is surrounded by a brine (water/salt) solution. To freeze the ice cream mix rapidly so that smooth and creamy ice cream results, the brine solution should combine crushed ice and rock salt in a ratio of 5 to 1. Use this information for Exercises 43 and 44. (Source: White Mountain Freezers, The Rival Company)

- **43.** A small ice cream freezer requires 12 cups of crushed ice. How much rock salt should be mixed with the ice to create the necessary brine solution?
- **45.** The gas/oil ratio for a certain chainsaw is 50 to 1.
 - **a.** How much oil (in gallons) should be mixed with 5 gallons of gasoline?
 - **b.** If 1 gallon equals 128 fluid ounces, write the answer to part **a** in fluid ounces. Round to the nearest whole ounce.
- **47.** The adult daily dosage for a certain medicine is 150 mg (milligrams) of medicine for every 20 pounds of body weight.
 - **a.** At this rate, find the daily dose for a man who weighs 275 pounds.
 - **b.** If the man is to receive 500 mg of this medicine every 8 hours, is he receiving the proper dosage?

- **44.** A large ice cream freezer requires $18\frac{3}{4}$ cups of crushed ice. How much rock salt will be needed to create the necessary brine solution?
- **46.** The gas/oil ratio for a certain tractor mower is 20 to 1.
 - **a.** How much oil (in gallons) should be mixed with 10 gallons of gas?
 - **b.** If 1 gallon equals 4 quarts, write the answer to part **a** in quarts.
- **48.** The adult daily dosage for a certain medicine is 80 mg (milligrams) for every 25 pounds of body weight.
 - **a.** At this rate, find the daily dose for a woman who weighs 190 pounds.
 - **b.** If she is to receive this medicine every 6 hours, find the amount to be given every 6 hours.

Review

| Find the | nrime | factorization | of each | numher | See Sec | tion 2.2 |
|-------------|-------|---------------|---------|---------|---------|------------|
| 1 1110 1110 | princ | Jucionzanon | oj cuch | number. | Dec Dec | 11011 2.2. |

49. 15 **50.** 21 **51.** 20 **52.** 24 **53.** 200 **54.** 300 **55.** 32 **56.** 81

Concept Extensions

As we have seen earlier, proportions are often used in medicine dosage calculations. The exercises below have to do with liquid drug preparations, where the weight of the drug is contained in a volume of solution. The description of mg and ml below will help. We will study metric units further in Chapter 7.

mg means milligrams (A paper clip weighs about a gram. A milligram is about the weight of $\frac{1}{1000}$ of a paper clip.)

ml means milliliter (A liter is about a quart. A milliliter is about the amount of liquid in $\frac{1}{1000}$ of a quart.)

One way to solve the applications below is to set up the proportion $\frac{\text{mg}}{\text{ml}} = \frac{\text{mg}}{\text{ml}}$.

A solution strength of 15 mg of medicine in 1 ml of solution is available.

- **57.** If a patient needs 12 mg of medicine, how many ml do you administer?
- **58.** If a patient needs 33 mg of medicine, how many ml do you administer?
- A solution strength of 8 mg of medicine in 1 ml of solution is available.
- **59.** If a patient needs 10 mg of medicine, how many ml do you administer?
- **60.** If a patient needs 6 mg of medicine, how many ml do you administer?

Estimate the following. See the Concept Check in this section.

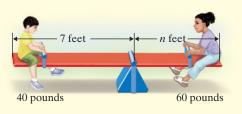
- **61.** It takes 1.5 cups of milk to make 11 muffins. Estimate the amount of milk needed to make 8 dozen muffins. Explain your calculation.
- **62.** A favorite chocolate chip recipe calls for $2\frac{1}{2}$ cups of flour to make 2 dozen cookies. Estimate the amount of flour needed to make 50 cookies. Explain your calculation.

A board such as the one pictured below will balance if the following proportion is true:

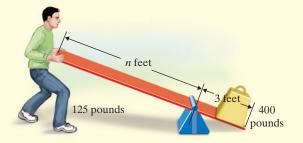


Use this proportion to solve Exercises 63 and 64.

63. Find the distance *n* that will allow the board to balance. **64.** Find the length *n* needed to lift the weight below.



65. Describe a situation in which writing a proportion might solve a problem related to driving a car.



Chapter 5 Group Activity

Consumer Price Index

Sections 5.1-5.4

Do you remember when the regular price of a candy bar was 5φ , 10φ , or 25φ ? It is certainly difficult to find a candy bar for that price these days. The reason is inflation: the tendency for the price of a given product to increase over time. Businesses and government agencies use the Consumer Price Index (CPI) to track inflation. The CPI measures the change in prices over time of basic consumer goods and services.

The CPI is very useful for comparing the prices of fixed items in various years. For instance, suppose an insurance company customer submits a claim for the theft of a fishing boat purchased in 1990. Because the customer's policy includes replacement cost coverage, the insurance company must calculate how much it would cost to replace the boat at the time of the theft. (Let's assume the theft took place in August 2016.) The customer has a receipt for the boat showing that it cost \$2058 in 1990. The insurance company can use the following proportion to calculate the replacement cost:

 $\frac{\text{price in earlier year}}{\text{price in later year}} = \frac{\text{CPI value in earlier year}}{\text{CPI value in later year}}$

The CPI value was 130.7 for 1990. In August 2016, the CPI value was 236.9. The insurance company would then use the following proportion for this situation. (We will let n represent the unknown price in August 2016.)

$$\frac{\text{price in 1990}}{\text{price in 2016}} = \frac{\text{CPI value in 1990}}{\text{CPI value in Aug. 2016}}$$
$$\frac{2058}{n} = \frac{130.7}{236.9}$$
$$130.7 \cdot n = 2058(236.9)$$
$$\frac{130.7 \cdot n}{130.7} = \frac{2058(236.9)}{130.7}$$
$$n \approx 3730$$

The replacement cost of the fishing boat at August 2016 prices is \$3730.

Critical Thinking

- **1.** What trends do you see in the CPI values in the table? Do you think these trends make sense? Explain.
- **2.** A piece of jewelry cost \$800 in 1985. What is its 2016 replacement value?

- **3.** In 2016, the cost of a loaf of bread was about \$2.50. What would an equivalent loaf of bread cost in 1950?
- **4.** Suppose a couple purchased a house for \$45,000 in 1970. At what price could they have been expected to sell the house in 2000?
- **5.** An original Ford Model T cost about \$850 in 1915. What is the equivalent cost of a Model T in 2010 dollars?

| Year | СРІ |
|------|-------|
| 1915 | 10.1 |
| 1920 | 20.0 |
| 1925 | 17.5 |
| 1930 | 16.7 |
| 1935 | 13.7 |
| 1940 | 14.0 |
| 1945 | 18.0 |
| 1950 | 24.1 |
| 1955 | 26.8 |
| 1960 | 29.6 |
| 1965 | 31.5 |
| 1970 | 38.8 |
| 1975 | 53.8 |
| 1980 | 82.4 |
| 1985 | 107.6 |
| 1990 | 130.7 |
| 1995 | 152.4 |
| 2000 | 172.2 |
| 2005 | 195.3 |
| 2010 | 218.1 |
| 2011 | 224.9 |
| 2012 | 229.6 |
| 2013 | 233.0 |
| 2014 | 233.9 |
| 2015 | 233.7 |
| 2016 | 236.9 |

Chapter 5 Vocabulary Check

Fill in each blank with one of the words or phrases listed below.

| not equal | equal | cross products | rate |
|-----------|-------|----------------|------------|
| unit rate | ratio | unit price | proportion |

- 1. A(n) _______ is the quotient of two numbers. It can be written as a fraction, using a colon, or using the word *to*.
- **2.** $\frac{n}{2} = \frac{7}{16}$ is an example of a(n) _____.
- **3.** A(n) ______ is a rate with a denominator of 1.
- **4.** A(n) ______ is a "money per item" unit rate.
- 5. A(n) _______ is used to compare different kinds of quantities.
- 6. In the proportion $\frac{n}{2} = \frac{7}{16}$, $n \cdot 16$ and $2 \cdot 7$ are called ______.
- 7. If cross products are _____, the proportion is true.
- 8. If cross products are _____, the proportion is false.

Helpful Hint • Are you preparing for your test? To help, don't forget to take these:

- Chapter 5 Getting Ready for the Test on page 363
- Chapter 5 Test on page 364

Then check all of your answers at the back of this text. For further review, the step-by-step video solutions to any of these exercises are located in MyLab Math.

Chapter Highlights

| Definitions and Concepts | Examples | | |
|--|---|--|--|
| Section 5.1 Ratios | | | |
| A ratio is the quotient of two quantities. | The ratio of 3 to 4 can be written as | | |
| | $\frac{3}{4}$ or $3:4$ | | |
| | fraction notation colon notation | | |
| Section 5.2 Rates | | | |
| Rates are used to compare different kinds of quantities. | Write the rate 12 spikes every 8 inches as a fraction in simplest form. | | |
| | $\frac{12 \text{ spikes}}{8 \text{ inches}} = \frac{3 \text{ spikes}}{2 \text{ inches}}$ | | |
| A unit rate is a rate with a denominator of 1. | Write as a unit rate: 117 miles on 5 gallons of gas | | |
| | $\frac{117 \text{ miles}}{5 \text{ gallons}} = \frac{23.4 \text{ miles}}{1 \text{ gallon}} \text{ or } \frac{23.4 \text{ miles per gallon}}{\text{ or } 23.4 \text{ miles/gallon}}$ | | |
| A unit price is a "money per item" unit rate. | Write as a unit price: \$5.88 for 42 ounces of detergent | | |
| | $\frac{\$5.88}{42 \text{ ounces}} = \frac{\$0.14}{1 \text{ ounce}} = \0.14 per ounce | | |

| Definitions and Concepts | Examples |
|--|---|
| Section 5.3 | Proportions |
| A proportion is a statement that two ratios or rates are equal. | $\frac{1}{2} = \frac{4}{8}$ is a proportion. |
| Using Cross Products to Determine Whether
Proportions Are True or False | Is $\frac{6}{10} = \frac{9}{15}$ a true proportion? |
| Cross products $b \cdot c$
$\frac{a}{b} = \frac{c}{d}$ | Cross products
$6 \cdot 15$ $\frac{6}{10} = \frac{9}{15}$ $10 \cdot 9$ |
| If cross products are equal, the proportion is true. | $6 \cdot 15 \stackrel{?}{=} 10 \cdot 9$ Are cross products equal? |
| If $ad = bc$, then the proportion is true. | 90 = 90 |
| If cross products are not equal, the proportion is false. | Since cross products are equal, the proportion is a true proportion. |
| If $ad \neq bc$, then the proportion is false. | |
| Finding an Unknown Value <i>n</i> in a Proportion | Find $n: \frac{n}{7} = \frac{5}{8}$ |
| Step 1: Set the cross products equal to each other. | Step 1: $\frac{n}{7} = \frac{5}{8}$ |
| | $n \cdot 8 = 7 \cdot 5$ Set the cross products equal to each other.
$n \cdot 8 = 35$ Multiply. |
| Step 2: Divide the number not multiplied by <i>n</i> by the number multiplied by <i>n</i> . | Step 2:
$n = \frac{35}{8}$ Divide 35 by 8, the number multiplied by <i>n</i> .
$n = 4\frac{3}{8}$ |
| Section 5.4 Proportio | ns and Problem Solving |
| Given a specified ratio (or rate) of two quantities, a pro-
portion can be used to determine an unknown quantity. | On a map, 50 miles corresponds to 3 inches. How many miles correspond to 10 inches? 1. UNDERSTAND. Read and reread the problem. 2. TRANSLATE. We let <i>n</i> represent the unknown number. We are given that 50 miles is to 3 inches as <i>n</i> miles is to 10 inches. miles → 50/3 = n ← miles inches |

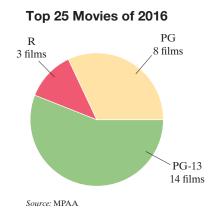
| Definitions and Concepts | Examples | |
|-----------------------------|---|--|
| Section 5.4 Proportions and | d Problem Solving (continued) | |
| | 3. SOLVE:
$ \frac{50}{3} = \frac{n}{10} $ $ 50 \cdot 10 = 3 \cdot n \text{Set the cross products equal to each other.} \\ 500 = 3 \cdot n \text{Multiply.} \\ \frac{500}{3} = n \text{Divide 500 by 3, the number multiplied by } n. $ $ n = 166\frac{2}{3} $ 4. INTERPRET. <i>Check</i> your work. <i>State</i> your conclusion:
On the map, $166\frac{2}{3}$ miles corresponds to 10 inches. | |

Chapter 5 Review

(5.1) Write each ratio as a fraction in simplest form.

| 1. 23 to 37 | 2. 14 to 51 | 3. 6000 people to 4800 people | 4. \$121 to \$143 |
|--|------------------------------------|--|---|
| 5. 3.5 centimeters to 7.5 centimeters | 6. 4.25 yards to 8.75 yards | 7. $2\frac{1}{4}$ to $4\frac{3}{8}$ | 8. $3\frac{1}{2}$ to $2\frac{7}{10}$ |

The circle graph below shows how the top 25 movies (or films) of 2016 were rated. Use this graph to answer the questions.



- **9. a.** How many top 25 movies were rated R?
 - **b.** Find the ratio of top 25 R-rated movies to total movies for that year.
- **10. a.** How many top 25 movies were rated PG-13?
 - **b.** Find the ratio of top 25 PG-13-rated movies to total movies for that year.

(5.2) Write each rate as a fraction in simplest form.
11. 8 stillborn births to 1000 live births
12. 6 professors for 20 graduate research assistants
13. 15 word processing pages printed in 6 minutes
14. 8 computers assembled in 6 hours
Write each rate as a unit rate.
15. 468 miles in 9 hours
16. 180 feet in 12 seconds
17. \$27.84 for 4 CDs
18. 8 gallons of pesticide for 6 acres of crops
19. \$234 for books for 5 college courses
20. 104 bushels of fruit from 8 trees

Find each unit price and decide which is the better buy. Round to 3 decimal places. Assume that we are comparing different sizes of the same brand.

21. Taco sauce: 8 ounces for \$0.99 or 12 ounces for \$1.69

360

- **23.** 2% milk: \$0.59 for 16 ounces, \$1.69 for 64 ounces, or \$2.29 for 1 gallon (1 gallon = 128 fluid ounces)
- (5.3) Write each sentence as a proportion.
- **25.** 20 men is to 14 women as 10 men is to 7 women.
- **27.** 16 sandwiches is to 8 players as 2 sandwiches is to 1 player.

22. Peanut butter: 18 ounces for \$1.49 or 28 ounces for \$2.39



- **24.** Coca-Cola: \$0.59 for 12 ounces, \$0.79 for 16 ounces, or \$1.19 for 32 ounces
- **26.** 50 tries is to 4 successes as 25 tries is to 2 successes.
- **28.** 12 tires is to 3 cars as 4 tires is to 1 car.

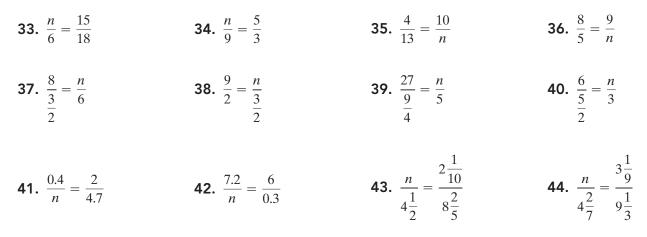
Determine whether each proportion is true.

29.
$$\frac{21}{8} = \frac{14}{6}$$
 30. $\frac{3}{5} = \frac{60}{100}$

31.
$$\frac{3.75}{3} = \frac{7.5}{6}$$
 32. $\frac{3.1}{6.2} = \frac{0.8}{0.16}$

Chapter 5 Review

Find the unknown number n in each proportion.



(5.4) Solve.

The ratio of a quarterback's completed passes to attempted passes is 3 to 7.

- **45.** If he attempted 32 passes, find how many passes he completed. Round to the nearest pass.
- **46.** If he completed 15 passes, find how many passes he attempted.
- One bag of pesticide covers 4000 square feet of garden.
- \triangle **47.** Find how many bags of pesticide should be purchased to cover a rectangular garden that is 180 feet by 175 feet.
- \triangle **48.** Find how many bags of pesticide should be purchased to cover a square garden that is 250 feet on each side.

An owner of a Ford Escort can drive 420 miles on 11 gallons of gas.

49. If Tom Aloiso runs out of gas in an Escort and AAA comes to his rescue with $1\frac{1}{2}$ gallons of gas, determine whether Tom can then drive to a gas station 65 miles away.

50. Find how many gallons of gas Tom can expect to burn on a 3000-mile trip. Round to the nearest gallon.

Yearly homeowner property taxes are figured at a rate of \$1.15 tax for every \$100 of house value.

- **51.** If a homeowner pays \$627.90 in property taxes, find the value of his home.
- **52.** Find the property taxes on a townhouse valued at \$89,000.

On an architect's blueprint, 1 inch = 12 feet.

- **53.** Find the length of a wall represented by a $3\frac{3}{8}$ -inch line on the blueprint.
- **54.** If an exterior wall is 99 feet long, find how long the blueprint measurement should be.

| Mixed Review | |
|-----------------------------------|--------------------------------|
| Write each ratio as a fraction in | simplest form. |
| 55. 15 to 25 | 56. 16 to 36 |
| 58. 25 feet to 60 feet | 59. 3 pints to 81 pints |
| | |

Write each rate as a fraction in simplest form. **61.** 2 teachers for 18 students **62.** 6 nurses for 24 patients

Write each rate as a unit rate.

| 63. 24 cups for 6 people | 64. 18 toys for 3 children |
|---------------------------------|---|
| 65. 136 miles in 4 hours | 66. 12 gallons of milk from 6 cows |

Find each unit price and decide which is the better buy. Round to 3 decimal places. Assume that we are comparing different sizes of the same brand.

| 67. | cold medicine: | 68. | juice: |
|-----|------------------|-----|-------------------|
| | \$4.94 for 4 oz, | | 12 oz for \$0.65, |
| | \$9.98 for 8 oz | | 64 oz for \$2.98 |

Write each sentence as a proportion.

- **69.** 2 cups of cookie dough is to 30 cookies as 4 cups of cookie dough is to 60 cookies
- **70.** 5 nickels is to 3 dollars as 20 nickels is to 12 dollars

57. 14 feet to 28 feet

60. 6 pints to 48 pints

Determine whether each proportion is a true proportion.

71. $\frac{3}{4} = \frac{87}{116}$ **72.** $\frac{2}{3} = \frac{4}{9}$

Find the unknown number n in each proportion.

76. $\frac{5}{4} = \frac{n}{20}$ **74.** $\frac{6}{n} = \frac{30}{24}$ **75.** $\frac{42}{5} = \frac{n}{10}$ **73.** $\frac{3}{n} = \frac{15}{8}$

Solve. The monthly loan payment for a car is \$39.75 for each \$1500 borrowed.

77. Find the monthly payment for a \$23,000 car loan.

An investment of \$1200 yields \$152 each year.

- **79.** At the same rate, how much will an investment of \$1350 yield in one year?
- **78.** Find the monthly payment for an \$18,000 car loan.
- Copyright 2019 Pearson Education, Inc.
- **80.** At the same rate, how much will an investment of \$750 yield in one year?

Chapter 5 **Getting Ready for the Test** LC

MULTIPLE CHOICE Exercises 1 through 8 are Multiple Choice. Choose the correct letter for each exercise.

• 1. The ratio of $\frac{9}{15}$ is the same as what ratio? **A.** $\frac{15}{9}$ **B.** $\frac{3}{5}$ C. $\frac{5}{3}$ **D.** 15:9 **2**. Given the rectangle, find the ratio of its width to its *perimeter*. 19 in. 12 in. **C.** $\frac{12}{62} = \frac{6}{31}$ **A.** $\frac{12}{19}$ **B.** $\frac{19}{12}$ **D.** $\frac{19}{31}$ **3**. The rate 3 trees every 45 feet in simplest form is: C. $\frac{15 \text{ ft}}{1 \text{ tree}}$ **B.** $\frac{45 \, \text{ft}}{3 \, \text{trees}}$ A. $\frac{1 \text{ tree}}{15 \text{ ft}}$

For Exercises 4 through 6, determine whether the proportions are true or false. Answer choices are

- A. True **• 4.** $\frac{5}{6} = \frac{4}{5}$ **5.** $\frac{15}{6} = \frac{5}{2}$ **06.** $\frac{\frac{8}{11}}{\frac{4}{5}} = \frac{\frac{10}{11}}{\frac{5}{5}}$

● 7. The phrase "6 is to 7 as 18 is to 21" translates to

A.
$$\frac{6}{7} = \frac{18}{21}$$
 B. $\frac{6}{18} = \frac{21}{7}$ **C.** $\frac{6}{21} = \frac{7}{18}$

B. False

▶ 8. Use cross products to determine which proportion is *not* equivalent to the proportion $\frac{3}{n} = \frac{5}{11}$

A.
$$\frac{3}{11} = \frac{n}{5}$$
 B. $\frac{n}{3} = \frac{11}{5}$ **C.** $\frac{3}{5} = \frac{n}{11}$ **D.** $\frac{11}{n} = \frac{5}{3}$

| Chapter 5 | Test MyLab Math or You Tube For additional practice go to your study plan in MyLab Math. |
|------------|---|
| Answers | Write each ratio or rate as a fraction in simplest form. |
| | ● 1. \$75 to \$10 ● 2. 4500 trees to 6500 trees ● 3. 28 men to every 4 women |
| | • 4. 9 inches of rain in 30 days • 5. 8.6 to 10 • 6. $5\frac{7}{8}$ to $9\frac{3}{4}$ |
| 1. | • 7. The world's largest yacht,
the <i>Azzam</i> , measures in at |
| 2 | 591 feet long. A Boeing
787-8 Dreamliner measures
186 feet long. Find the ratio |
| 3. | of the length of the <i>Azzam</i> to
the length of a 787-8. (<i>Source:</i>
Superyachts.com, Boeing) |
| 4. | ← 591 ft → |
| 5. | |
| 6. | <i>Find each unit rate.</i> 8. 650 kilometers 9. 8 inches of rain in 10. 140 students for |
| 7. | in 8 hours 12 hours 5 teachers |
| 8. | ● 11. QRIO (Quest for Curiosity) is the world's first bipedal robot capable of running (moving with both legs off the ground at the same time) at a rate of 108 inches each |
| 9. | 12 seconds. (Source: Guinness World Records) |
| 10. | Find each unit price and use them to decide which is the better buy. |
| <u>11.</u> | ▶ 12. Steak sauce: ▶ 13. Jelly: ▶ 13. Jelly: ▶ 149 for 16 ounces |
| 12. | 12 ounces for \$1.89 \$2.39 for 24 ounces |
| 13. | Determine whether each proportion is a true proportion. |
| <u>14.</u> | • 14. $\frac{28}{16} = \frac{14}{8}$ • 15. $\frac{3.6}{2.2} = \frac{1.9}{1.2}$ |
| 15. | 16. Write the sentence as a proportion. 25 computers is to 600 students as 1 computer is to 24 students. |
| 16. | 25 computers is to 666 students as 1 computer is to 24 students. |

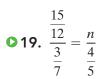
Find the unknown number n in each proportion.

• 17.
$$\frac{n}{3} = \frac{15}{9}$$
 • 18. $\frac{8}{n} = \frac{11}{6}$

20.
$$\frac{1.5}{5} = \frac{2.4}{n}$$

Solve.

- ▶ 22. On an architect's drawing, 2 inches corresponds to 9 feet. Find the length of a home represented by a line that is 11 inches long.
- ▶ 24. The standard dose of medicine for a dog is 10 grams for every 15 pounds of body weight. What is the standard dose for a dog that weighs 80 pounds?
- ▶ 25. Jerome Grant worked 6 hours and packed 86 cartons of books. At this rate, how many cartons can he pack in 8 hours?



21.
$$\frac{n}{2\frac{5}{8}} = \frac{1\frac{1}{6}}{3\frac{1}{2}}$$

▶ 23. If a car can be driven 80 miles in 3 hours, how long will it take to travel 100 miles?



● 26. Currently 3 out of every 4 American adults drink coffee at least once per week. In a town with a population of 7900 adults, how many of these adults would you expect to drink coffee at least once per week? (*Source:* National Coffee Association)



| | 365 |
|-----|-----|
| 17. | |
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| 18. | |
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| 19. | |
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| 05 | |
| 25. | |
| | |
| 26. | |
| | |

Chapters 1–5

Cumulative Review

| Answers
1. a.
b.
c. | 1. Subtract. Check each answer by adding. a. 12 - 9 b. 22 - 7 c. 35 - 35 d. 70 - 0 | 2. | Multiply
a. 20 · 0
b. 20 · 1
c. 0 · 20
d. 1 · 20 |
|------------------------------|--|-----|--|
| <u>d.</u>
<u>2. a.</u> | 3. Round 248,982 to the nearest hundred. | 4. | Round 248,982 to the nearest thousand. |
| b.
c.
d. | 5. Multiply:
a. 25 b. 246
$\times 8 \times 5$ | 6. | Divide: 10,468 ÷ 28 |
| 3.
4.
5. a.
b. | 7. The director of a computer lab at
a local state college is working on
next year's budget. Thirty-three new
desktops are needed at a cost of \$487
each. What is the total cost of these | 8. | A study is being conducted for erecting
soundproof walls along the interstate
of a metropolitan area. The following
lengths of walls are part of the propos-
al. Find their total: 4800 feet, 3270 feet, |
| 6. 7. 8. | desktops?
9. Find the prime factorization of 45. | 10. | 2761 feet, 5760 feet.
Find $\sqrt{64}$. |
| <u>9.</u>
10. | 11. Write $\frac{12}{20}$ in simplest form. | 12. | Find $9^2 \cdot \sqrt{9}$. |
| <u>11.</u>
<u>12.</u> | Multiply. | | 3 5 |
| <u>13.</u>
<u>14.</u> | 13. $\frac{3}{4} \cdot \frac{8}{5}$ | 14. | $3\frac{3}{8} \cdot 4\frac{5}{9}$ |
| <u>15.</u>
<u>16.</u> | 15. $\frac{6}{13} \cdot \frac{26}{30}$ | 16. | $\frac{2}{11} \cdot \frac{5}{8} \cdot \frac{22}{27}$ |
| <u>17.</u>
<u>18.</u> | Perform the indicated operation and simplify.
17. $\frac{2}{7} + \frac{3}{7}$ | 18. | $\frac{26}{30} - \frac{7}{30}$ |

Cumulative Review

24. Determine whether these fractions are

19.
$$\frac{7}{13} + \frac{6}{13} + \frac{3}{13}$$
 20. $\frac{7}{10} + \frac{3}{10} + \frac{3}{10}$

- **21.** Find the LCM of 9 and 12.
- **23.** Write an equivalent fraction with the indicated denominator. $\frac{1}{2} = \frac{1}{24}$
- **25.** Subtract: $\frac{10}{11} \frac{2}{3}$
- **27.** A flight from Tucson to Phoenix, Arizona, requires $\frac{5}{12}$ of an hour. If the plane has been flying $\frac{1}{4}$ of an hour, find how much time remains before landing.

- **28.** Simplify: $80 \div 8 \cdot 2 + 7$
- **30.** Find the average of $\frac{3}{5}$, $\frac{4}{9}$, and $\frac{11}{15}$.
- **32.** Multiply: $28,000 \times 500$
- **34.** Write "seventy-five thousandths" in standard form.
- **36.** Round 736.2359 to the nearest thousandth.

29. Add:
$$2\frac{1}{3} + 5\frac{3}{8}$$

31. Insert < or > to form a true statement. 3 2 $\overline{7}$ 10

- **33.** Write the decimal 1.3 in words.
- **35.** Round 736.2359 to the nearest tenth.
- **37.** Add: 23.85 + 1.604

| 21. | | |
|-----|------|------|
| 22 | | |
| 22. |
 |
 |
| 23. | | |
| | | |

19.

20.

24.

25.

- 26.

28.

- 29.
- 30.

31.

- 32.
- 33.
- 34.

35.

- 36.
- 37.



22. Add: $\frac{17}{25} + \frac{3}{10}$

equivalent.

6 55' 33

26. Subtract: $17\frac{5}{24} - 9\frac{5}{9}$

10

| 368 | Chapter 5 Ratio and Proportion | |
|--------------------------|---|---|
| <u>38.</u> | 38. Subtract: 700 – 18.76 | 39. Multiply: 0.283×0.3 |
| <u>39.</u>
<u>40.</u> | 40. Write $\frac{3}{8}$ as a decimal. | 41. Divide and check: 0.5 ÷ 4 |
| <u>41.</u>
<u>42.</u> | 42. Write 7.9 as an improper fraction. | 43. Simplify: 0.5(8.6 – 1.2) |
| <u>43.</u>
<u>44.</u> | 44. Find the unknown number <i>n</i> . $\frac{n}{4} = \frac{12}{16}$ | 45. Write the numbers in order from smallest to largest.
$\frac{9}{20}, \frac{4}{9}, 0.456$ |
| <u>45.</u>
<u>46.</u> | 46. Write the rate as a unit rate. 700 meters in 5 seconds | |
| <u>47.</u>
<u>48.</u> | Write each ratio using fractional notation. Simp | |
| <u>49.</u> | 47. The ratio of 2.6 to 3.1 | 48. The ratio of 7 to 21 |
| 50 | 49. The ratio of $1\frac{1}{2}$ to $7\frac{3}{4}$ | 50. The ratio of 900 to 9000 |

Percent





What Does Iceland Have to Do with Hydroelectricity and Geothermal Heat?

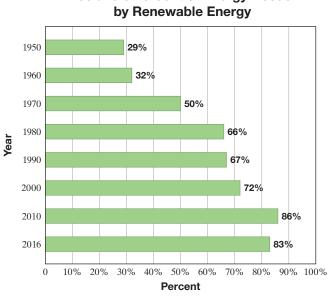
enewable energy is energy that is collected from renewable resources, which are naturally replenished, such as sunlight, wind, rain, tides, waves, waterfalls, and geothermal heat. Renewable energy often provides energy in electricity generation, air and water heating/cooling, and transportation.

Hydroelectricity is electricity produced from hydropower, or "water power." Geothermal energy or geothermal heat is heat energy generated and stored in the Earth.

Iceland, known as the land of fire and ice, is a small island between North America and Europe. It has massive glaciers, bubbling hot springs, green valleys, and spectacular waterfalls, among many other natural beauties.

Iceland is also unique in that a major effort has been made to use renewable energy when possible. Nearly 90% of Icelandic homes enjoy heating by geothermal energy, and even the streets of downtown Reykjavik are kept snow free by heated pipes running under the pavement.

Below, the graph shows the increase in percent of Iceland's energy needs met by renewable energy. In Section 6.2, Exercises 59 and 60, we will explore the percentage of energy Iceland obtains from geothermal and hydro forces.



Iceland's Percent of Energy Needs

This chapter is devoted to percent, a concept used virtually every day in ordinary and business life. Understanding percent and using it efficiently depend on understanding ratios because a percent is a ratio whose denominator is 100. We present techniques to write percents as fractions and as decimals and then solve problems relating to sales tax, commission, discounts, interest, and other real-life situations that use percents.

Sections

- 6.1 Introduction to Percent
- **6.2** Percents and Fractions
- **6.3** Solving Percent Problems Using Equations
- **6.4** Solving Percent Problems Using Proportions

Integrated Review— Percent and Percent Problems

- **6.5** Applications of Percent
- **6.6** Percent and Problem Solving: Sales Tax, Commission, and Discount
- 6.7 Percent and Problem Solving: Interest

Check Your Progress

Vocabulary Check Chapter Highlights **Chapter Review** Getting Ready for the Test Chapter Test **Cumulative Review**

6.1 Introduction to Percent 🔘

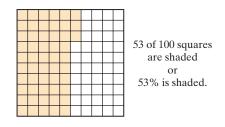
Objective 🗛 Understanding Percent 🕑

Objectives

A Understand Percent. >

B Write Percents as Decimals.

C Write Decimals as Percents. D The word **percent** comes from the Latin phrase *per centum*, which means "**per 100**." For example, 53% (percent) means 53 per 100. In the square below, 53 of the 100 squares are shaded. Thus, 53% of the figure is shaded.



Since 53% means 53 per 100, 53% is the ratio of 53 to 100, or $\frac{53}{100}$.

$$53\% = \frac{53}{100}$$

Also,

$$7\% = \frac{7}{100} \quad 7 \text{ parts per 100 parts}$$
$$73\% = \frac{73}{100} \quad 73 \text{ parts per 100 parts}$$
$$109\% = \frac{109}{100} \quad 109 \text{ parts per 100 parts}$$

Percent

Percent means per one hundred. The "%" symbol is used to denote percent.

Percent is used in a variety of everyday situations. For example,

- 88.5% of the U.S. population uses the Internet.
- The store is having a 25%-off sale.
- The enrollment in community colleges is predicted to increase 1.8% each year.
- The South is the home of 49% of all frequent paintball participants.



• 66% of chocolate consumed is milk chocolate.

Example 1

Since 2011, white has been the world's most popular color for cars.

For 2017 model cars, 25 out of every 100 were painted white. What percent of model-year 2017 cars were white? (*Source:* motorauthority.com)

Solution: Since 25 out of 100 cars were painted white, the fraction is $\frac{25}{100}$. Then

$$\frac{25}{100} = 25\%$$

Work Practice 1

Practice 1

Of 100 students in a club, 23 are freshmen. What percent of the students are freshmen?

Answer 1. 23%

Example 2

46 out of every 100 college students live at home. What percent of students live at home? (*Source:* Independent Insurance Agents of America)

Solution:

$$\frac{46}{100} = 46\%$$

Work Practice 2

Objective **B** Writing Percents as Decimals 🕗

Since percent means "per hundred," we have that

$$1\% = \frac{1}{100} = 0.01$$

In other words, the percent symbol means "per hundred" or, equivalently, " $\frac{1}{100}$ " or "0.01." Thus

$$87\% = 87 \times \frac{1}{100} = \frac{87}{100}$$
Results are the same

or

 $87\% = 87 \times (0.01) = 0.87$

Of course, we know that the end results are the same, that is,

 $\frac{87}{100} = 0.87$

The above gives us two options for converting percents. We can replace the percent symbol, %, by $\frac{1}{100}$ or 0.01 and then multiply.

For consistency, when we

- convert from a percent to a *decimal*, we will drop the % symbol and multiply by 0.01 (this section).
- convert from a percent to a *fraction*, we will drop the % symbol and multiply by $\frac{1}{100}$ (next section).

Thus, to write 53% (or 53.%) as a decimal,

53% = 53(0.01) = 0.53 Replace the percent symbol with 0.01. Then multiply.

Writing a Percent as a Decimal

Replace the percent symbol with its decimal equivalent, 0.01; then multiply.

43% = 43(0.01) = 0.43

Percer

Helpful Hint

If it helps, think of writing a percent as a decimal by

$$\begin{array}{c} \text{Remove the \% symbol and move} \\ \text{decimal point 2 places to the left} \end{array} \rightarrow \text{Decimal} \end{array}$$

Practice 2

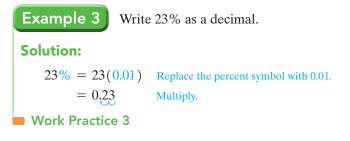
Answer

2. 29%

29 out of 100 executives are in their forties. What percent of executives are in their forties?

Chapter 6 | Percent

Examples



Practice 4–7

Write each percent as a decimal.

Write 89% as a decimal.

| 4. | 2.7% | 5. |
|----|-------|----|
| 6. | 0.69% | 7. |

5. 150% **7.** 800% Write each percent as a decimal.

4. 4.6% = 4.6(0.01) = 0.046 Replace the percent symbol with 0.01. Then multiply. 5. 190% = 190(0.01) = 1.90 or 1.9 6. 0.74% = 0.74(0.01) = 0.00747. 100% = 100(0.01) = 1.00 or 1 Work Practice 4-7

Concept Check Why is it incorrect to write the percent 0.033% as 3.3 in decimal form?

Objective C Writing Decimals as Percents 🕑

To write a decimal as a percent, we use the result of Example 7 above. In this example, we found that 1 = 100%.

0.38 = 0.38(1) = 0.38(100%) = 38%

Notice that the result is

0.38 = 0.38(100%) = 38% Multiply by 1 in the form of 100%.

Writing a Decimal as a Percent

Multiply by 1 in the form of 100%.

0.27 = 0.27(100%) = 27.%

Helpful Hint

If it helps, think of writing a decimal as a percent by reversing the steps in the Helpful Hint on the previous page.

Percent ← Move the decimal point 2 places to the right and attach a % symbol. ← Decimal

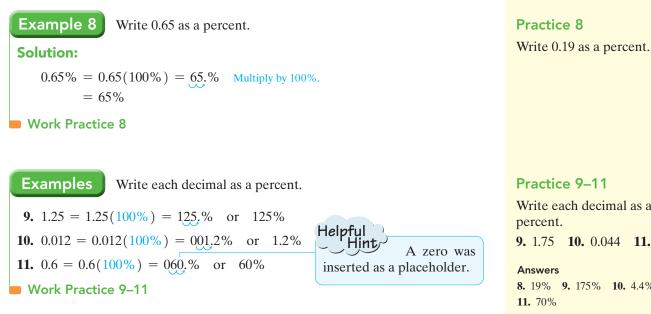
Answers

3. 0.89 **4.** 0.027 **5.** 1.5 **6.** 0.0069 **7.** 8.00 or 8

Concept Check Answer

To write a percent as a decimal, the decimal point should be moved two places to the left, not to the right. So the correct answer is 0.00033.

Practice 3



Concept Check Why is it incorrect to write the decimal 0.0345 as 34.5% in percent form?

Practice 9–11

Write each decimal as a **9.** 1.75 **10.** 0.044 **11.** 0.7

8. 19% **9.** 175% **10.** 4.4%

Concept Check Answer

To change a decimal to a percent, multiply by 100%, or move the decimal point only two places to the right. So the correct answer is 3.45%.

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Some choices may be used more than once or not at all.

1 0.01 100% percent $\overline{100}$

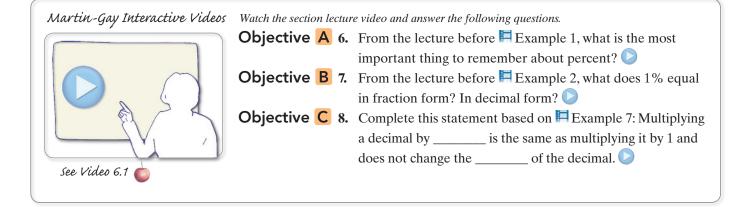
1. _____ means "per hundred."

2. = 1.

3. The % symbol is read as _____.

4. To write a decimal as a *percent*, multiply by 1 in the form of ______.

5. To write a percent as a *decimal*, drop the % symbol and multiply by ______.

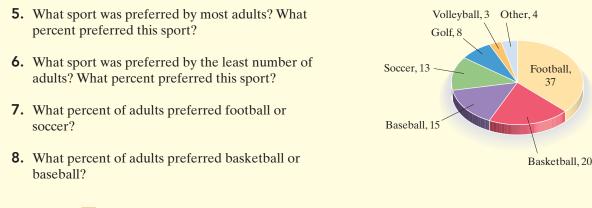


6.1 Exercise Set MyLab Math 🜔

Objective A Solve. See Examples 1 and 2.

- 1. In a survey of 100 college students, 96 use the Internet. What percent use the Internet?
 - **3.** Michigan leads the United States in tart cherry production, producing 75 out of every 100 tart cherries each year.
 - **a.** What percent of tart cherries are produced in Michigan?
 - **b.** What percent of tart cherries are *not* produced in Michigan? (*Source:* Cherry Marketing Institute)

- **2.** A basketball player makes 81 out of 100 attempted free throws. What percent of free throws are made?
- **4.** The United States is the world's second-largest producer of apples. Twenty-five out of every 100 apples harvested in the United States are exported (shipped to other countries). (*Source:* U.S. Apple Association)
 - **a.** What percent of U.S.-grown apples are exported?
 - **b.** What percent of U.S.-grown apples are not exported?



One hundred adults were asked to name their favorite sport, and the results are shown in the circle graph.

Objective B Write each percent as a decimal. See Examples 3 through 7.

| 9. 41% | 10. 62% | ▶11. 6% | 12. 3% |
|-------------------|-----------------|-------------------|-------------------|
| • 13. 100% | 14. 136% | 15. 73.6% | 16. 45.7% |
| 017. 2.8% | 18. 1.4% | 19. 0.6% | 20. 0.9% |
| 21. 300% | 22. 500% | 23. 32.58% | 24. 72.18% |

Write each percent as a decimal. See Examples 3 through 7.

- ▶ 25. People take aspirin for a variety of reasons. The most common use of aspirin is to prevent heart disease, accounting for 38% of all aspirin use. (*Source:* Bayer Market Research)
 - **27.** In 2016, 49.3% of households in the United States had no landline telephones, just cell phones. (*Source:* National Center for Health Statistics)
- **26.** In 2016, China accounted for 29.1% of all motorcycle exports in the world. (*Source:* China International Trade Center)
- **28.** Together, the Greenland and Antarctic ice sheets contain about 99.2% of the freshwater ice on earth. (*Source:* National Snow and Ice Data Center)

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29. A $\frac{1}{2}$ -cup serving of dried tart cherries delivers 45% of an adult's Daily Value of vitamin A. (*Source:* USDA Nutrient Data Laboratory)



30. From 2005 to 2015, use of smoked tobacco products in the United States decreased by 28.6%. (*Source:* Centers for Disease Control)



Objective C Write each decimal as a percent. See Examples 8 through 11.

| 31. 0.98 | 32. 0.75 | 33. 3.1 | 34. 4.8 | 35. 29 |
|-------------------|------------------|------------------|------------------|-------------------|
| 36. 56 | 37. 0.003 | 38. 0.006 | 39. 0.22 | 40. 0.45 |
| 41. 5.3 | 42. 1.6 | 43. 0.056 | 44. 0.027 | 45. 0.3328 |
| 46. 0.1115 | 047. 3 | 48. 5 | 49. 0.7 | 50. 0.8 |

Write each decimal as a percent. See Examples 8 through 11.

- **51.** Leisure travel accounted for 0.77 of all domestic trips in the United States. (*Source:* U.S. Travel Association)
- **53.** From 2017 to 2027, restaurant industry employment is expected to increase by 0.109. (*Source:* National Restaurant Asso.)
- **55.** Nearly 0.049 of the United States labor force was unemployed in 2016. (*Source:* Bureau of Labor Statistics)

- **52.** According to a recent survey, 0.34 of American adults reported having used the Internet to research nutritional information about restaurant foods. (*Source:* National Restaurant Association's 2013 Restaurant Industry Forecast)
- **54.** In 2017, food-and-beverage sales in table service restaurants are projected to increase 0.035. (*Source:* National Restaurant Asso.)
- **56.** In 2016, an estimated 0.803 of all American families had at least one employed member of their family. (*Source:* Bureau of Labor Statistics)

Review

Write each fraction as a decimal. See Section 4.6.

| 57. $\frac{1}{4}$ | 58. $\frac{3}{5}$ | 59. $\frac{13}{20}$ | 60. $\frac{11}{40}$ | 61. $\frac{9}{10}$ | 62. $\frac{7}{10}$ |
|--------------------------|--------------------------|----------------------------|----------------------------|---------------------------|---------------------------|
|--------------------------|--------------------------|----------------------------|----------------------------|---------------------------|---------------------------|

Concept Extensions

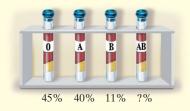
Solve. See the Concept Checks in this section.

- **63.** Which of the following are correct?
 - **a.** 6.5% = 0.65
 - **b.** 7.8% = 0.078
 - **c.** 120% = 0.12
 - **d.** 0.35% = 0.0035

- **64.** Which of the following are correct?
 - **a.** 0.231 = 23.1%
 - **b.** 5.12 = 0.0512%
 - **c.** 3.2 = 320%
 - **d.** 0.0175 = 0.175%

Recall that 1 = 100%. This means that 1 whole is 100%. Use this for Exercises 65 and 66. (Source: Some Body by *Dr. Pete Rowen*)

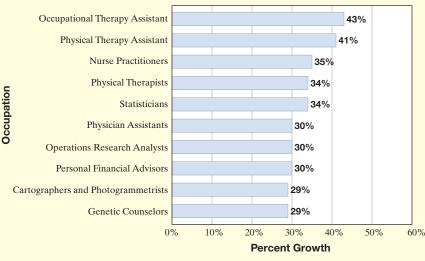
65. The four blood types are A, B, O, and AB. (Each blood type can also be further classified as Rh-positive or Rh-negative depending upon whether your blood contains protein or not.) Given the percent blood types for the United States below, calculate the percent of U.S. population with AB blood type.



- **66.** The components of bone are all listed in the categories below. Find the missing percent.
 - **1.** Minerals–45%
 - **2.** Living tissue–30%
 - **3.** Water–20%
 - **4.** Other-?



The bar graph shows the predicted fastest-growing occupations by percent that require an associate degree or more education. Use this graph for Exercises 67 through 70. (Source: Bureau of Labor Statistics)



Fastest-Growing Occupations 2014–2024 (projected)

Source: Bureau of Labor Statistics

- **67.** What occupation is predicted to be the fastest growing?
- **69.** Write the percent change for physician assistants as a decimal.
- **71.** In your own words, explain how to write a percent as a decimal.
- **68.** What occupation is predicted to be the second fastest growing?
- **70.** Write the percent change for statisticians as a decimal.
- **72.** In your own words, explain how to write a decimal as a percent.

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6.2 Percents and Fractions

Objective A Writing Percents as Fractions 🕗

Recall from Section 6.1 that percent means per hundred. Thus

$$1\% = \frac{1}{100} = 0.01$$

For example,

$$87\% = 87 \times \frac{1}{100} = \frac{87}{100}$$
 Writing 87% as a fraction.

or

 $87\% = 87 \times 0.01 = 0.87$ Writing 87% as a decimal.

In this section we are writing percents as fractions, so we do the following.

Writing a Percent as a Fraction

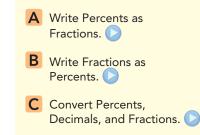
Replace the percent symbol with its fraction equivalent, $\frac{1}{100}$; then multiply. Don't forget to simplify the fraction if possible.

$$7\% = 7 \cdot \frac{1}{100} = \frac{7}{100}$$

Examples Write each percent as a fraction or mixed number in simplest form.
1. 40% = 40
$$\cdot \frac{1}{100} = \frac{40}{100} = \frac{2 \cdot \frac{20}{5}}{5 \cdot \frac{20}{1}} = \frac{2}{5}$$

2. 1.9% = $1.9 \cdot \frac{1}{100} = \frac{1.9}{100}$. We don't want the numerator of the fraction to contain a decimal, so we multiply by 1 in the form of $\frac{10}{10}$.
 $= \frac{1.9}{100} \cdot \frac{10}{10} = \frac{1.9 \cdot 10}{100 \cdot 10} = \frac{19}{1000}$
3. 125% = $125 \cdot \frac{1}{100} = \frac{125}{100} = \frac{5 \cdot \frac{25}{2}}{4 \cdot 25} = \frac{5}{4}$ or $1\frac{1}{4}$
4. $33\frac{1}{3}\% = 33\frac{1}{3} \cdot \frac{1}{100} = \frac{100}{3} \cdot \frac{1}{100} = \frac{100}{3 \cdot 100} = \frac{1}{3 \cdot 100}$
5. 100% = $100 \cdot \frac{1}{100} = \frac{100}{100} = 1$
4. Work Practice 1-5

Objectives



Practice 1–5

Write each percent as a fraction or mixed number in simplest form.

3. 225%

4.
$$66\frac{2}{3}\%$$

5. 8%

Objective **B** Writing Fractions as Percents 🕗

Recall that to write a percent as a fraction, we replace the percent symbol by its fraction equivalent, $\frac{1}{100}$. We reverse these steps to write a fraction as a percent.

Answers

1.
$$\frac{1}{4}$$
 2. $\frac{23}{1000}$ **3.** $\frac{9}{4}$ or $2\frac{1}{4}$
4. $\frac{2}{3}$ **5.** $\frac{2}{25}$

Writing a Fraction as a Percent

Multiply by 1 in the form of 100%.

$$\frac{1}{8} = \frac{1}{8} \cdot 100\% = \frac{1}{8} \cdot \frac{100}{1}\% = \frac{100}{8}\% = 12\frac{1}{2}\% \text{ or } 12.5\%$$

Helpful Hint

From Example 5, we know that

100% = 1

Recall that when we multiply a number by 1, we are not changing the value of that number. This means that when we multiply a number by 100%, we are not changing its value but rather writing the number as an equivalent percent.



Write each fraction or mixed number as a percent.

| 6. $\frac{9}{20} = \frac{9}{20} \cdot 100\% = \frac{9}{20} \cdot \frac{100}{1}\% = \frac{900}{20}\% = 45\%$
7. $\frac{2}{3} = \frac{2}{3} \cdot 100\% = \frac{2}{3} \cdot \frac{100}{1}\% = \frac{200}{3}\% = 66\frac{2}{3}\%$ | Helpful |
|---|---|
| 7. $\frac{2}{3} = \frac{2}{3} \cdot 100\% = \frac{2}{3} \cdot \frac{100}{1}\% = \frac{200}{3}\% = 66\frac{2}{3}\%$ | $\frac{200}{3} = 66.\overline{6}.$ Thus, another way to write |
| 8. $1\frac{1}{2} = \frac{3}{2} \cdot 100\% = \frac{3}{2} \cdot \frac{100}{1}\% = \frac{300}{2}\% = 150\%$ | $\frac{200}{3}\% \text{ is } 66.\overline{6}\%.$ |
| ■ Work Practice 6–8 | |

Concept Check Which digit in the percent 76.4582% represents

- a. A tenth percent?
- c. A hundredth percent?
- **b.** A thousandth percent? d. A whole percent?

Example 9 Write $\frac{1}{12}$ as a percent. Round to the nearest hundredth percent.

Solution:

Solution:

$$\frac{1}{12} = \frac{1}{12} \cdot 100\% = \frac{1}{12} \cdot \frac{100}{1}\% = \frac{100}{12}\% \approx 8.33\%$$

$$\frac{8.333}{12)\overline{100.000}} \approx 8.33$$

$$\frac{-96}{40}$$

$$\frac{-36}{40}$$

$$\frac{-36}{40}$$

$$\frac{-36}{40}$$
Thus, $\frac{1}{12}$ is approximately 8.33%.

Answers

Practice 9

6. 50% **7.** $17\frac{1}{2}$ % **8.** 225% **9.** 17.65%

Write $\frac{3}{17}$ as a percent. Round to

the nearest hundredth percent.

Concept Check Answers **a.** 4 **b.** 8 **c.** 5 **d.** 6

Practice 6–8

Write each fraction or mixed number as a percent.

6.
$$\frac{1}{2}$$
 7. $\frac{7}{40}$ **8.** $2\frac{1}{4}$

Objective C Converting Percents, Decimals, and Fractions 🕗

Let's summarize what we have learned so far about percents, decimals, and fractions:

Summary of Converting Percents, Decimals, and Fractions

- *To write a percent as a decimal*, replace the % symbol with its decimal equivalent, 0.01; then multiply.
- To write a percent as a fraction, replace the % symbol with its fraction equivalent, $\frac{1}{100}$; then multiply.
- *To write a decimal or fraction as a percent,* multiply by 100%.

If we let *p* represent a number, below we summarize using symbols.

| Write a percent as a decimal: | Write a percent as a fraction: | Write a number
as a percent: |
|-------------------------------|--------------------------------|---------------------------------|
| p% = p(0.01) | $p\% = p \cdot \frac{1}{100}$ | $p = p \cdot 100\%$ |

Example 10

39.8% of automobile thefts in the continental United States occur in the West, the greatest percent. Write this percent as a decimal and as a fraction. (*Source:* Insurance Information Institute)

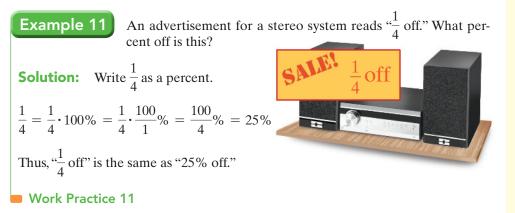
Solution:

As a decimal: 39.8% = 39.8(0.01) = 0.398

As a fraction:
$$39.8\% = 39.8 \cdot \frac{1}{100} = \frac{39.8}{100} = \frac{39.8}{100} \cdot \frac{10}{10} = \frac{398}{1000} = \frac{2 \cdot 199}{2 \cdot 500} = \frac{199}{500}.$$

Thus, 39.8% written as a decimal is 0.398 and written as a fraction is $\frac{199}{500}$

Work Practice 10



Note: It is helpful to know a few basic percent conversions. Appendix A.4 contains a handy reference of percent, decimal, and fraction equivalencies.

Also, Appendix A.5 shows how to find common percents of a number.

Practice 10

A family decides to spend no more than 22.5% of its monthly income on rent. Write 22.5% as a decimal and as a fraction.

Practice 11

Provincetown's budget for waste disposal increased by

 $1\frac{1}{4}$ times over the budget from

last year. What percent increase is this?

Answers

10. 0.225,
$$\frac{9}{40}$$
 11. 125%

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Some choices may be used more than once.

 $\frac{1}{100}$ 100% percent

 1. ______ means "per hundred."

 2. _______ = 1.

 3. To write a decimal or a fraction as a *percent*, multiply by 1 in the form of ______.

 4. To write a percent as a *fraction*, drop the % symbol and multiply by ______.

 Write each fraction as a percent.

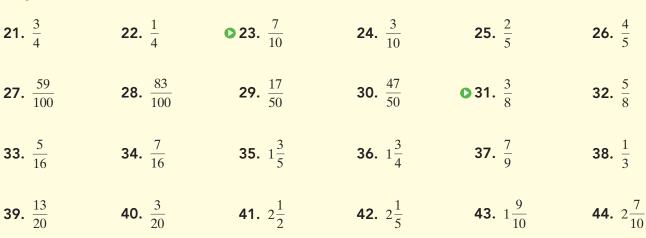
 5. $\frac{13}{100}$ 6. $\frac{92}{100}$ 7. $\frac{87}{100}$ 8. $\frac{71}{100}$ 9. $\frac{1}{100}$ 10. $\frac{2}{100}$

| Martin-Gay Interactive Videos | Watch the section lecture | video and answer the following questions. |
|-------------------------------|---------------------------|---|
| | Objective A 11. | In Example 1, since the % symbol is replaced with $\frac{1}{100}$, why doesn't the final answer have a denominator of 100? |
| | Objective B 12. | From the lecture before Example 4, how is writing a fraction as a percent similar to writing a decimal as a percent? |
| see Video 6.2 🍅 | Objective C 13. | From Example 7, what is the main difference between
writing a percent as an equivalent decimal and writing a
percent as an equivalent fraction? |

6.2 Exercise Set MyLab Math 🕗

Objective A Write each percent as a fraction or mixed number in simplest form. See Examples 1 through 5.

| 1. 12% | 2. 24% | 3. 4% | 4. 2% | 5. 4.5% |
|------------------|-------------------------|-----------------------------|------------------------------|------------------------------|
| 6. 7.5% | 7. 175% | 8. 250% | 9. 73% | 10. 86% |
| 11. 12.5% | 12. 62.5% | 13. 6.25% | 14. 3.75% | 15. 6% |
| 16. 16% | • 17. $10\frac{1}{3}\%$ | 18. $7\frac{3}{4}\%$ | 19. $22\frac{3}{8}\%$ | 20. $15\frac{5}{8}\%$ |



Objective B Write each fraction or mixed number as a percent. See Examples 6 through 8.

Write each fraction as a percent. Round to the nearest hundredth percent. See Example 9.

| 45. $\frac{7}{11}$ | 46. $\frac{5}{12}$ | ○ 47. $\frac{4}{15}$ | 48. $\frac{10}{11}$ |
|---------------------------|---------------------------|-----------------------------|----------------------------|
| 49. $\frac{1}{7}$ | 50. $\frac{1}{9}$ | 51. $\frac{11}{12}$ | 52. $\frac{5}{6}$ |

Objective C *Complete each table. See Examples 10 and 11.*

| 53. | Percent | Decimal | Fraction |
|-----|---------|---------|---------------|
| | 35% | | |
| | | | $\frac{1}{5}$ |
| | | 0.5 | |
| | 70% | | |
| | | | $\frac{3}{8}$ |

| 55. | Percent | Decimal | Fraction |
|-----|-------------------|---------|---------------|
| | 40% | | |
| | | 0.235 | |
| | | | $\frac{4}{5}$ |
| | $33\frac{1}{3}\%$ | | |
| | | | $\frac{7}{8}$ |
| | 7.5% | | |

| 54. | Percent | Decimal | Fraction |
|-----|---------|---------|----------------|
| | 60% | | |
| | | | $\frac{2}{5}$ |
| | | 0.25 | |
| | 12.5% | | |
| | | | $\frac{5}{8}$ |
| | | | $\frac{7}{50}$ |

| 56. | Percent | Decimal | Fraction |
|-----|-------------------|---------|---------------|
| | | 0.525 | |
| | | | $\frac{3}{4}$ |
| | $66\frac{2}{3}\%$ | | |
| | | | $\frac{5}{6}$ |
| | 100% | | |

| 57. [| Percent | Decimal | Fraction |
|--------------|---------|---------|------------------|
| | 200% | | |
| | | 2.8 | |
| | 705% | | |
| | | | $4\frac{27}{50}$ |

Solve. See Examples 10 and 11.

59. In 2016, 66% of Iceland's primary energy was geothermal. Write this percent as a decimal and a fraction. (*Source:* National Energy Authority of Iceland)



61. In 2016, 59.2% of all veterinarians in the United States were female. Write this percent as a decimal and a fraction. (*Source:* American Veterinary Medical Association)



- **63.** In 2016, the restaurant industry accounted for a $\frac{12}{25}$ share of U.S. dollars spent on food. Write this fraction as a percent. (*Source:* National Restaurant Association)
- **65.** The sales tax for Jefferson Parish, Louisiana, is 9.75%. Write this percent as a decimal.

| 58 . (| Percent | Decimal | Fraction |
|---------------|---------|---------|------------------|
| | 800% | | |
| | | 3.2 | |
| | 608% | | |
| | | | $9\frac{13}{50}$ |

60. In 2016, 20% of Iceland's primary energy was hydroelectric. Write this percent as a decimal and a fraction. (*Source:* National Energy Authority of Iceland)



62. The U.S. penny is 97.5% zinc. Write this percent as a decimal and a fraction. (*Source:* Americans for Common Cents)

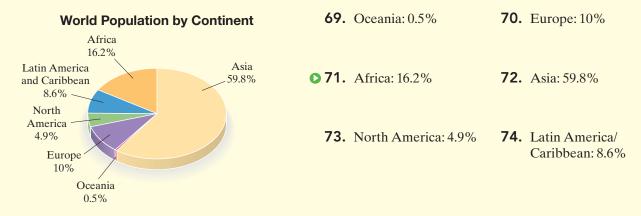


- **64.** Of all U.S. veterinarians in private practice in 2016, $\frac{3}{50}$ focused exclusively on horses. Write this fraction as a percent. (*Source:* American Veterinary Medical Association)
- **66.** A real estate agent receives a commission of 3% of the sale price of a house. Write this percent as a decimal.

- **67.** The average American wastes $\frac{9}{50}$ of all grain products brought into the home. Write this fraction as a percent. (*Source:* Natural Resources Defense
- **68.** Canada produces $\frac{1}{4}$ of the uranium produced in the world. Write this fraction as a percent. (*Source:* World Nuclear Association)



In Exercises 69 through 74, write the percent from the circle graph as a decimal and a fraction.



Review

Council)

Find the value of n. See Section 5.3.

| 75. $3 \cdot n = 45$ | 76. $7 \cdot n = 48$ | 77. $8 \cdot n = 80$ |
|------------------------------|-----------------------------|-----------------------------|
| 78. 2 · <i>n</i> = 16 | 79. $6 \cdot n = 72$ | 80. $5 \cdot n = 35$ |

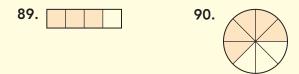
Concept Extensions

Solve. See the Concept Check in this section.

- **81.** Given the percent 52.8647%, round as indicated.
 - **a.** Round to a tenth of a percent.
 - **b.** Round to a hundredth of a percent.
- **83.** Write 1.07835 as a percent rounded to the nearest tenth of a percent.
- **85.** Write 0.65794 as a percent rounded to the nearest hundredth of a percent.
- **87.** Write 0.7682 as a percent rounded to the nearest percent.

- **82.** Given the percent 0.5269%, round as indicated.
 - **a.** Round to a tenth of a percent.
 - **b.** Round to a hundredth of a percent.
- **84.** Write 1.25348 as a percent rounded to the nearest tenth of a percent.
- **86.** Write 0.92571 as a percent rounded to the nearest hundredth of a percent.
- **88.** Write 0.2371 as a percent rounded to the nearest percent.

What percent of the figure is shaded?





| 92. | |
|-----|--|
| | |
| | |
| | |
| | |

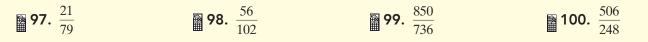
Fill in the blanks.

- **93.** A fraction written as a percent is greater than 100% when the numerator is ______ than the denominator. (greater/less)
- **95.** In your own words, explain how to write a percent as a fraction.
- **96.** In your own words, explain how to write a fraction as a decimal.

when the decimal is _____ than 1. (greater/less)

94. A decimal written as a percent is less than 100%

Write each fraction as a decimal and then write each decimal as a percent. Round the decimal to three decimal places (nearest thousandth) and the percent to the nearest tenth of a percent.



6.3 Solving Percent Problems Using Equations

Objectives

- A Write Percent Problems as Equations.
- B Solve Percent Problems

Note: Sections **6.3** and **6.4** introduce two methods for solving percent problems. It is not necessary that you study both sections. You may want to check with your instructor for further advice.

Throughout this text, we have written mathematical statements such as 3 + 10 = 13, or area = length · width. These statements are called "equations." An **equation** is a mathematical statement that contains an equal sign. To solve percent problems in this section, we translate the problems into such mathematical statements, or equations.

Objective A Writing Percent Problems as Equations 🕑

Recognizing key words in a percent problem is helpful in writing the problem as an equation. Three key words in the statement of a percent problem and their meanings are as follows:

of means multiplication (\cdot)

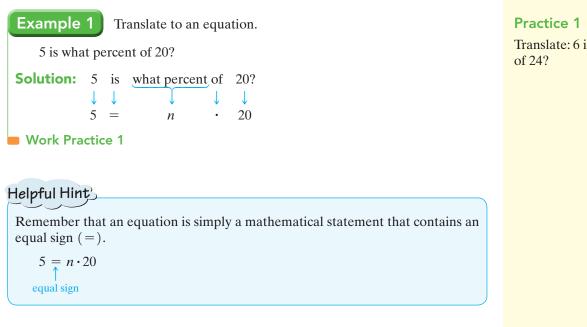
is means equals (=)

what (or some equivalent) means the unknown number

In our examples, we let the letter n stand for the unknown number.

Helpful Hint

Any letter of the alphabet can be used to represent the unknown number. In this section, we mostly use the letter n.



Example 2 Translate to an equation.

1.2 is 30% of what number?

Solution: 1.2 is 30% of what number? Ţ Ţ Ţ Ţ] 1.2 = 30%. п

Work Practice 2

Example 3 Translate to an equation.

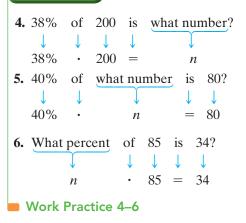
What number is 25% of 0.008?

Solution: What number is 25% of 0.008? Ţ = 25%0.008 п •

Work Practice 3



Translate each of the following to an equation:



Translate: 6 is what percent

Practice 2 Translate: 1.8 is 20% of what number?

Practice 3

Translate: What number is 40% of 3.6?

Practice 4–6

Translate each to an equation.

- 4. 42% of 50 is what number?
- 5. 15% of what number is 9?
- 6. What percent of 150 is 90?

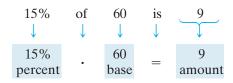
Answers **1.** $6 = n \cdot 24$ **2.** $1.8 = 20\% \cdot n$

3. $n = 40\% \cdot 3.6$ **4.** $42\% \cdot 50 = n$ **5.** $15\% \cdot n = 9$ **6.** $n \cdot 150 = 90$

Concept Check In the equation $2 \cdot n = 10$, what step should be taken to solve the equation for n?

Objective B Solving Percent Problems 💟

You may have noticed by now that each percent problem has contained three numbers—in our examples, two are known and one is unknown. Each of these numbers is given a special name.



We call this equation the percent equation.

Percent Equation

 $percent \cdot base = amount$

Helpful Hint

Notice that the percent equation given above is a true statement. To see this, simplify the left side as shown:

 $15\% \cdot 60 = 9$ $0.15 \cdot 60 = 9 \quad \text{Write } 15\% \text{ as } 0.15.$ $9 = 9 \quad \text{Multiply.}$ The statement 9 = 9 is true.

After a percent problem has been written as a percent equation, we can use the equation to find the unknown number. This is called **solving** the equation.

| Example 7 Solving Percent Equation for the Amount | | | | | | |
|--|-----------|--|--|--|--|--|
| | What numb | er is 35% of 40? | | | | |
| | ↓ | $\downarrow \downarrow \downarrow \downarrow \downarrow$ | | | | |
| Solution: | n | $= 35\% \cdot 40$ Translate to an equation. | | | | |
| | n | $= 0.35 \cdot 40$ Write 35% as 0.35. | | | | |
| | п | $= 14$ Multiply $0.35 \cdot 40 = 14$. | | | | |

Thus, 14 is 35% of 40.

Is this reasonable? To see, round 35% to 40%. Then 40% of 40 or 0.40(40) is 16. Our result is reasonable since 16 is close to 14.

Work Practice 7

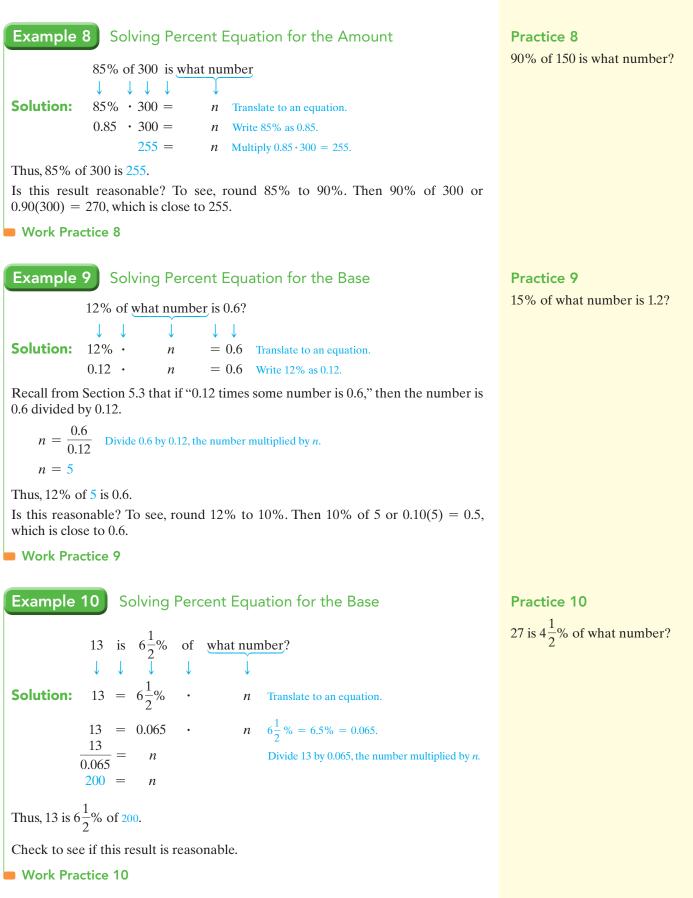
Helpful Hint

When solving a percent equation, write the percent as a decimal (or fraction).

Practice 7 What number is 20% of 85?

Answer 7. 17

Concept Check Answer If $2 \cdot n = 10$, then $n = \frac{10}{2}$, or n = 5.



Answers 8. 135 9. 8 10. 600

Chapter 6 | Percent

Practice 11 What percent of 80 is 8?



| | What percent | of | 12 | is | 9? | |
|-----------|--------------|--------------|--------------|--------------|----------------|---|
| | ľ. | \downarrow | \downarrow | \downarrow | \downarrow | |
| Solution: | n | • | 12 | = | 9 | Translate to an equation. |
| | | | п | = | <u>9</u>
12 | Divide 9 by 12, the number multiplied by <i>n</i> . |
| | | | п | = | 0.75 | |

Next, since we are looking for percent, we write 0.75 as a percent.

$$n = 75\%$$

So, 75% of 12 is 9. To check, see that $75\% \cdot 12 = 9$.

Work Practice 11

Helpful Hint

If your unknown in the percent equation is the percent, don't forget to convert your answer to a percent.

Example 12 Solving Percent Equation for the Percent

| | 78 is | what percent | of | 65? | |
|-----------|-------------------------|--------------|----|--------------|--|
| | $\downarrow \downarrow$ | Ť | ↓ | \downarrow | |
| Solution: | 78 = | n | • | 65 | Translate to an equation. |
| | $\frac{78}{65} =$ | п | | | Divide 78 by 65, the number multiplied by <i>n</i> . |
| | 1.2 = | п | | | |
| 12 | 20% = | n | | | Write 1.2 as a percent. |
| | | | | | |

So, 78 is 120% of 65. Check this result.

Work Practice 12

Concept Check Consider these problems.

| 1. | 75% of $50 =$ | | | |
|----|----------------|------------------------------------|----|-----------------------|
| | a. 50 | b. a number greater than 50 | c. | a number less than 50 |
| 2. | 40% of a num | ber is 10. Is the number | | |
| | a. 10? | b. less than 10? | c. | greater than 10? |
| 3. | 800 is 120% c | f what number? Is the number | | |
| | a. 800? | b. less than 800? | c. | greater than 800? |

Helpful Hint

Use the following to see if your answers are reasonable.

(100%) of a number = the number

 $\begin{pmatrix} a \text{ percent} \\ \text{greater than} \\ 100\% \end{pmatrix} \text{ of a number } = \begin{cases} a \text{ number greater} \\ \text{than the original number} \\ \\ \begin{pmatrix} a \text{ percent} \\ \text{less than 100\%} \end{pmatrix} \text{ of a number } = \begin{cases} a \text{ number less} \\ \text{than the original number} \end{cases}$

Practice 12

35 is what percent of 25?

```
Answers
11. 10% 12. 140%
```

Concept Check Answers 1. c 2. c 3. b

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank.

percent amount of less base the number is greater

1. The word ______ translates to " =".

2. The word ______ usually translates to "multiplication."

- 3. In the statement "10% of 90 is 9," the number 9 is called the _____, 90 is called the _____, and 10 is called the
- **4.** 100% of a number = _____
- 5. Any "percent greater than 100%" of "a number" = "a number ______ than the original number."
- 6. Any "percent less than 100%" of "a number" = "a number ______ than the original number."

Identify the percent, the base, and the amount in each equation. Recall that $percent \cdot base = amount$.

- **7.** $42\% \cdot 50 = 21$ **8.** $30\% \cdot 65 = 19.5$
- **9.** $107.5 = 125\% \cdot 86$ **10.** $99 = 110\% \cdot 90$

Martin-Gay Interactive Videos Watch the section lecture video and answer the following questions.

Objective A 11. From the lecture before Example 1, what are the key words and their translations that we need to remember?
 Objective B 12. What is the difference between the translated equation in Example 5 and those in Examples 4 and 6?

6.3 Exercise Set MyLab Math 🕗

Objective A Translating *Translate each to an equation. Do not solve. See Examples 1 through 6.*

▶ **1.** 18% of 81 is what number?

see Video 6.3 🛑

- **3.** 20% of what number is 105?
- **5.** 0.6 is 40% of what number?
- **7.** What percent of 80 is 3.8?
 - **9.** What number is 9% of 43?
 - **11.** What percent of 250 is 150?

- **2.** 36% of 72 is what number?
- **4.** 40% of what number is 6?
- **6.** 0.7 is 20% of what number?
- **8.** 9.2 is what percent of 92?
- **10.** What number is 25% of 55?
- **12.** What percent of 375 is 300?

| Objective B Solve. See Examples 7 | 7 and 8. | |
|---|--|--|
| • 13. 10% of 35 is what number? | 14. 25% of 68 is v | what number? |
| 15. What number is 14% of 205? | 16. What number | r is 18% of 425? |
| Solve. See Examples 9 and 10. | | |
| • 17. 1.2 is 12% of what number? | 18. 0.22 is 44% o | f what number? |
| 19. $8\frac{1}{2}\%$ of what number is 51? | 20. $4\frac{1}{2}\%$ of what | number is 45? |
| Solve. See Examples 11 and 12. | | |
| 21. What percent of 80 is 88? | 22. What percent | t of 40 is 60? |
| 23. 17 is what percent of 50? | 24. 48 is what per | rcent of 50? |
| Objectives A B Mixed Practi | ce Solve. See Examples 1 through 12. | |
| 25. 0.1 is 10% of what number? | 26. 0.5 is 5% of what number? | 27. 150% of 430 is what number? |
| 28. 300% of 56 is what number? | 29. 82.5 is $16\frac{1}{2}$ % of what number? | 30. 7.2 is $6\frac{1}{4}\%$ of what number? |
| 31. 2.58 is what percent of 50? | 32. 2.64 is what percent of 25? | 33. What number is 42% of 60? |
| 34. What number is 36% of 80? | 35. What percent of 184 is 64.4? | 36. What percent of 120 is 76.8? |
| 37. 120% of what number is 42? | 38. 160% of what number is 40? | 39. 2.4% of 26 is what number? |
| 40. 4.8% of 32 is what number? | 41. What percent of 600 is 3? | 42. What percent of 500 is 2? |
| 43. 6.67 is 4.6% of what number? | 44. 9.75 is 7.5% of what number? | 45. 1575 is what percent of 2500? |
| 46. 2520 is what percent of 3500? | 47. 2 is what percent of 50? | 48. 2 is what percent of 40? |

Review

Find the value of n in each proportion. See Section 5.3.

49. $\frac{27}{n} = \frac{9}{10}$ **50.** $\frac{35}{n} = \frac{7}{5}$ **51.** $\frac{n}{5} = \frac{8}{11}$

Write each phrase as a proportion.

53. 17 is to 12 as *n* is to 20 **54.** 20 is to 25 as *n* is to 10 **55.** 8 is to 9 as 14 is to *n* **56.** 5 is to 6 as 15 is to *n*

Concept Extensions

For each equation, determine the next step taken to find the value of n. See the first Concept Check in this section.

57. $5 \cdot n = 32$ **b.** $n = \frac{5}{32}$ **c.** $n = \frac{32}{5}$ **d.** none of these **a.** $n = 5 \cdot 32$ **58.** $n = 0.7 \cdot 12$ **b.** $n = \frac{12}{0.7}$ **c.** $n = \frac{0.7}{12}$ **d.** none of these **a.** *n* = 8.4 **59.** $0.06 = n \cdot 7$ **b.** $n = \frac{0.06}{7}$ **c.** $n = \frac{7}{0.06}$ **d.** none of these **a.** $n = 0.06 \cdot 7$ **60.** $0.01 = n \cdot 8$ **b.** $n = \frac{8}{0.01}$ **c.** $n = \frac{0.01}{8}$ **d.** none of these **a.** $n = 0.01 \cdot 8$ **61.** Write a word statement for the equation **62.** Write a word statement for the equation $20\% \cdot n = 18.6$. Use the phrase "some number" $n = 33\frac{1}{3}\% \cdot 24$. Use the phrase "some number" for "*n*". for "*n*". For each exercise, determine whether the percent, n, is (a) 100%, (b) greater than 100%, or (c) less than 100%. See the last Concept Check in this section. **63.** *n*% of 20 is 30 **64.** *n*% of 98 is 98 **65.** *n*% of 120 is 85 **66.** *n*% of 35 is 50 For each exercise, determine whether the number, n, is (a) equal to 45, (b) greater than 45, or (c) less than 45. **67.** 55% of 45 is *n* **68.** 230% of 45 is *n* **69.** 100% of 45 is *n* **70.** 30% of *n* is 45 **71.** 100% of *n* is 45 **72.** 180% of *n* is 45 **73.** In your own words, explain how to solve a percent $\mathbf{74.}$ Write a percent problem that uses the percent 50%. equation. Solve. **75.** 1.5% of 45,775 is what number? **76.** What percent of 75,528 is 27,945.36?

6.4 Solving Percent Problems Using Proportions

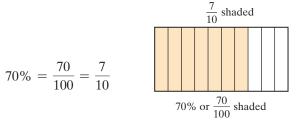
Objectives

- A Write Percent Problems as Proportions. D
- B Solve Percent Problems. >

There is more than one method that can be used to solve percent problems. (See the note at the beginning of Section 6.3.) In the last section, we used the percent equation. In this section, we will use proportions.

Objective A Writing Percent Problems as Proportions

To understand the proportion method, recall that 70% means the ratio of 70 to 100, or $\frac{70}{100}$.



Since the ratio $\frac{70}{100}$ is equal to the ratio $\frac{7}{10}$, we have the proportion

$$\frac{7}{10} = \frac{70}{100}$$

We call this proportion the "percent proportion." In general, we can name the parts of this proportion as follows:

Percent Proportion $\frac{\text{amount}}{\text{base}} = \frac{\text{percent}}{100} \leftarrow \text{always 100}$

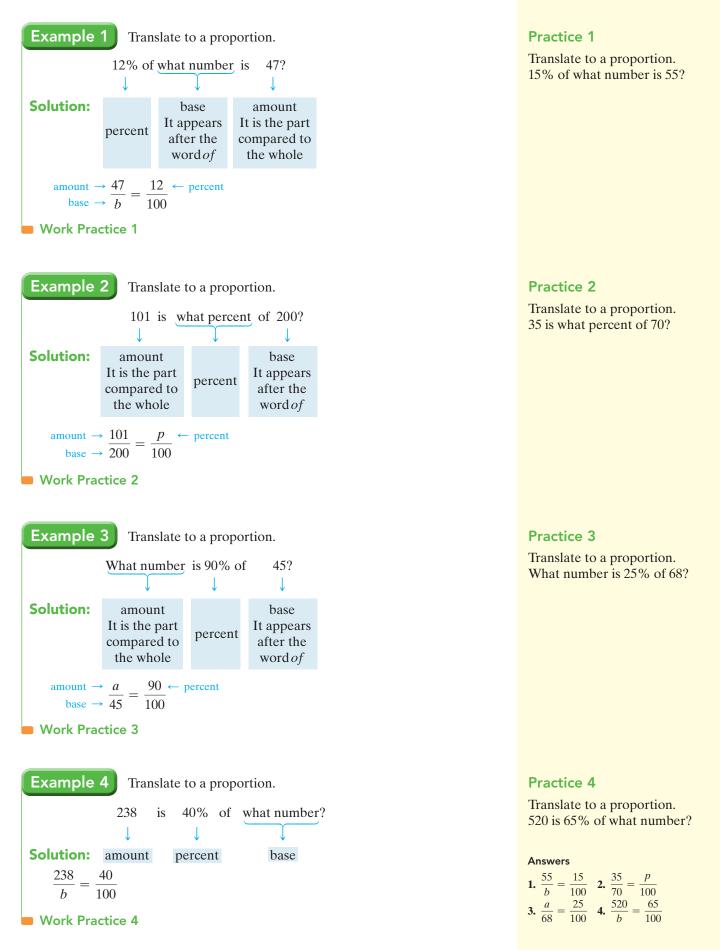
or $\begin{array}{l} \text{amount} \rightarrow \ \underline{a} \\ \text{base} \rightarrow \ \underline{b} \\ \end{array} = \frac{p}{100} \quad \leftarrow \text{percent} \end{array}$

When we translate percent problems to proportions, the **percent**, p, can be identified by looking for the symbol % or the word *percent*. The **base**, b, usually follows the word of. The **amount**, *a*, is the part compared to the whole.

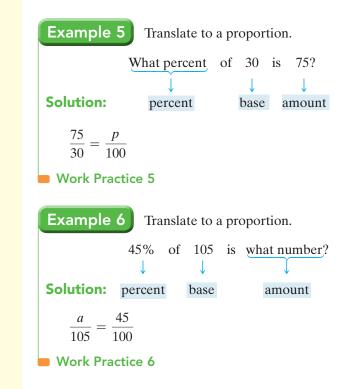
Helpful Hint

| Part of Proportion | How It's Identified |
|--------------------|------------------------|
| Percent | % or percent |
| Base | Appears after of |
| Amount | Part compared to whole |

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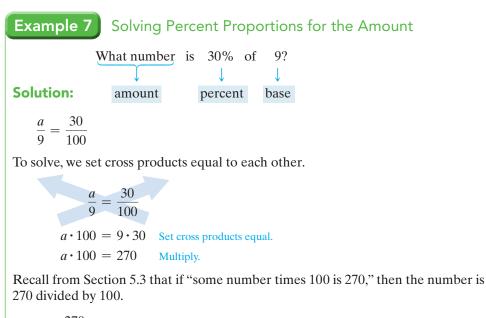


Chapter 6 | Percent



Objective B Solving Percent Problems 🕑

The proportions that we have written in this section contain three values that can change: the percent, the base, and the amount. If any two of these values are known, we can find the third (the unknown value). To do this, we write a percent proportion and find the unknown value as we did in Section 5.3.



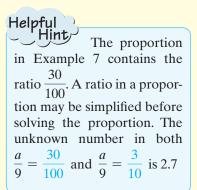
$$a = \frac{270}{100}$$
 Divide 270 by 100, the number multiplied by a.
 $a = 2.7$ Simplify.

Thus, 2.7 is 30% of 9.

Work Practice 7



What number is 8% of 120?



Answers 5. $\frac{65}{50} = \frac{p}{100}$ 6. $\frac{a}{80} = \frac{36}{100}$ 7. 9.6

What percent of 50 is 65?

Translate to a proportion.

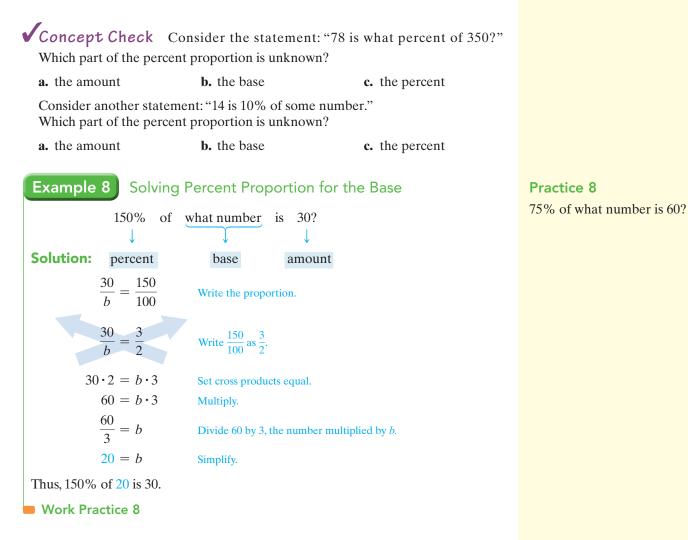
Translate to a proportion.

36% of 80 is what number?

Practice 5

Practice 6

394



Concept Check When solving a percent problem by using a proportion, describe how you can check the result.

Example 9 Solving Percent Proportion for the Base

20.8 is 40% of what number? Ţ **Solution:** amount percent base $\frac{20.8}{b} = \frac{40}{100} \quad \text{or} \quad \frac{20.8}{b} = \frac{2}{5} \quad \text{Write the proportion and simplify } \frac{40}{100}$ $20.8 \cdot 5 = b \cdot 2$ Set cross products equal. $104 = b \cdot 2$ Multiply. $\frac{104}{2} = b$ Divide 104 by 2, the number multiplied by b. 52 = bSimplify. So, 20.8 is 40% of 52. Work Practice 9

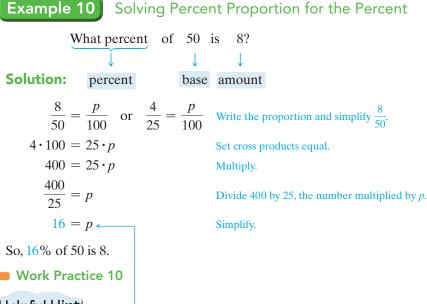
Practice 9 15.2 is 5% of what number?

Answers 8. 80 9. 304

Concept Check Answers **c**, **b**; by putting the result into the proportion and checking that the proportion is true

Chapter 6 | Percent

Practice 10 What percent of 40 is 6?



Helpful Hint

Recall from our percent proportion that this number already is a percent. Just keep the number as is and attach a % symbol.

Practice 11 336 is what percent of 160?

Example 11 Solving Percent Proportion for the Percent

| | 504 is | what percent of | 360? |
|----------------------|-------------------|--------------------------------------|---------------------------------|
| | \downarrow | ↓
↓ | \downarrow |
| Solution: | amount | percent | base |
| 200 | 100 | nplify the ratio $\frac{504}{360}$. | |
| | $= 360 \cdot p$ | | |
| 50,400 | $= 360 \cdot p$ | Multiply. | |
| $\frac{50,400}{360}$ | $\frac{0}{2} = p$ | Divide 50,400 by 360, the | number multiplied by <i>p</i> . |
| | p = p | Simplify. | |

Notice that by choosing not to simplify $\frac{504}{360}$, we had larger numbers in our equation. Either way, we find that 504 is 140% of 360.

Work Practice 11

You may have noticed the following while working examples.

Helpful Hint

Use the following to see whether your answers are reasonable.

100% of a number = the number

 $\begin{pmatrix} a \text{ percent} \\ \text{greater than} \\ 100\% \end{pmatrix} \text{ of a number } = \begin{array}{l} a \text{ number larger} \\ \text{than the original number} \\ \end{pmatrix}$ $\begin{pmatrix} a \text{ percent} \\ \text{less than 100\%} \end{pmatrix} \text{ of a number } = \begin{array}{l} a \text{ number less} \\ \text{than the original number} \\ \end{pmatrix}$

Vocabulary, Readiness & Video Check

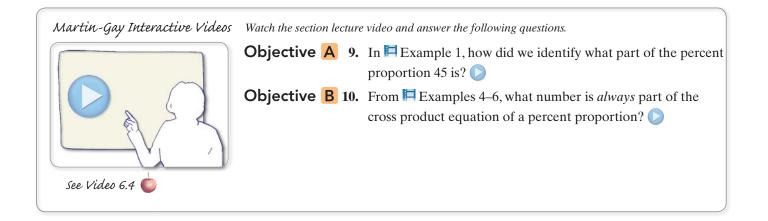
Use the choices below to fill in each blank. These choices will be used more than once.

amount base percent

- 1. When translating the statement "20% of 15 is 3" to a proportion, the number 3 is called the ______, 15 is the ______, and 20 is the ______.
- 2. In the question "50% of what number is 28?", which part of the percent proportion is unknown?
- 3. In the question "What number is 25% of 200?", which part of the percent proportion is unknown?
- 4. In the question "38 is what percent of 380?", which part of the percent proportion is unknown?

Identify the amount, the base, and the percent in each equation. Recall that $\frac{\text{amount}}{\text{base}} = \frac{\text{percent}}{100}$.

5. $\frac{12.6}{42} = \frac{30}{100}$ **6.** $\frac{201}{300} = \frac{67}{100}$ **7.** $\frac{20}{100} = \frac{102}{510}$ **8.** $\frac{40}{100} = \frac{248}{620}$



6.4 Exercise Set MyLab Math

Objective A Translating *Translate each to a proportion. Do not solve. See Examples 1 through 6.*

- 1. 98% of 45 is what number?
 - **3.** What number is 4% of 150?
 - **5.** 14.3 is 26% of what number?
 - **7.** 35% of what number is 84?
- **9.** What percent of 400 is 70?
- **11.** 8.2 is what percent of 82?

- **2.** 92% of 30 is what number?
- **4.** What number is 7% of 175?
- **6.** 1.2 is 47% of what number?
- **8.** 85% of what number is 520?
- **10.** What percent of 900 is 216?
- **12.** 9.6 is what percent of 96?

| Objective B Solve. See Example 7. | |
|---|---------------------------------------|
| 13. 40% of 65 is what number? | 14. 25% of 84 is what number? |
| 15. What number is 18% of 105? | 16. What number is 60% of 29? |
| Solve. See Examples 8 and 9. | |
| 17. 15% of what number is 90? | 18. 55% of what number is 55? |
| ● 19. 7.8 is 78% of what number? | 20. 1.1 is 44% of what number? |
| Solve. See Examples 10 and 11. | |
| 21. What percent of 35 is 42? | 22. What percent of 98 is 147? |
| 23. 14 is what percent of 50? | 24. 24 is what percent of 50? |
| Objectives A B Mixed Practice Solve. See Example | les 1 through 11. |
| 25. 3.7 is 10% of what number? | 26. 7.4 is 5% of what number? |
| 27. 2.4% of 70 is what number? | 28. 2.5% of 90 is what number? |
| 29. 160 is 16% of what number? | 30. 30 is 6% of what number? |

33. What number is 89% of 62? **34.** What number is 53% of 130?

- **35.** What percent of 6 is 2.7?
 - **37.** 140% of what number is 105?

31. 394.8 is what percent of 188?

- **39.** 1.8% of 48 is what number?
- **41.** What percent of 800 is 4?
- **43.** 3.5 is 2.5% of what number?
- **45.** 20% of 48 is what number?
 - **47.** 2486 is what percent of 2200?

32. 550.4 is what percent of 172?

- **36.** What percent of 5 is 1.6?
- **38.** 170% of what number is 221?
- **40.** 7.8% of 24 is what number?
- **42.** What percent of 500 is 3?
- **44.** 9.18 is 6.8% of what number?
- **46.** 75% of 14 is what number?
- **48.** 9310 is what percent of 3800?

| Review | | | |
|---|---|---|--|
| Add or subtract the free | actions or mixed numbers. See S | Sections 3.1, 3.3, and 3.4. | |
| 49. $\frac{11}{16} + \frac{3}{16}$ | 50. $\frac{5}{8} - \frac{7}{12}$ | 51. $3\frac{1}{2} - \frac{11}{30}$ | 52. $2\frac{2}{3} + 4\frac{2}{3}$ |
| Add or subtract the de | ecimals. See Section 4.3. | | |
| 53. 0.41 + 0.29 | 54. 10.78
4.3
+ 0.21 | 55. 2.38 <u>- 0.19</u> | 56. 16.37
<u>- 2.61</u> |

Concept Extensions

| 57. | Write a word statement for the proportion | \$ 58. | Write a percent statement that translates to |
|-----|---|---------------|--|
| | $\frac{x}{28} = \frac{25}{100}$. Use the phrase "what number" for "x." | | $\frac{16}{80} = \frac{20}{100}.$ |

Suppose you have finished solving four percent problems using proportions that you set up correctly. Check each answer to see if each makes the proportion a true proportion. If any proportion is not true, solve it to find the correct solution. See the Concept Checks in this section.

- **59.** $\frac{a}{64} = \frac{25}{100}$ Is the amount equal to 17?
- 61. $\frac{p}{100} = \frac{13}{52}$ Is the percent equal to 25 (25%)?
- **63.** In your own words, describe how to identify the percent, the base, and the amount in a percent problem.

Solve. Round to the nearest tenth, if necessary.

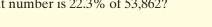
65. What number is 22.3% of 53,862?

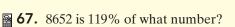
60.
$$\frac{520}{b} = \frac{65}{100}$$

Is the base equal to 800?

62. $\frac{36}{12} = \frac{p}{100}$ Is the percent equal to 50 (50%)?

- **64.** In your own words, explain how to use a proportion to solve a percent problem.
- **66.** What percent of 110,736 is 88,542?





 $4\frac{1}{2}$

Integrated Review

Answers

Percent and Percent Problems

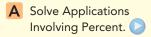
Sections 6.1-6.4

Write each number as a percent.

| | Write each numbe | r as a percent. | | |
|------------|--------------------------|---------------------------|---|------------------------------------|
| 1. | 1. 0.12 | 2. 0.68 | 3. $\frac{1}{8}$ | 4. $\frac{5}{2}$ |
| 2. | | | 0 | 2 |
| 3. | | | | |
| 4. | | | | |
| 5. | F . <i>c</i> . | | _ 3 | 1 1 |
| 6. | 5. 5.2 | 6. 8 | 7. $\frac{3}{50}$ | 8. $\frac{11}{25}$ |
| 7. | | | | |
| 8. | | | | |
| 9. | | | | |
| 10. | 9. $7\frac{1}{2}$ | 10. $3\frac{1}{4}$ | 11. 0.03 | 12. 0.05 |
| <u>11.</u> | | | | |
| 12. | | | | |
| 13. | | | | |
| <u>14.</u> | Write each percent | t as a decimal. | | |
| 15. | 13. 65% | 14. 31% | 15. 8% | 16. 7% |
| 16. | | | | |
| 17. | | | | |
| 18. | | | | |
| 19. | 17. 142% | 18. 400% | 19. 2.9% | 20. 6.6% |
| 20. | | | | |
| 21. | | | | |
| 22. | ¥¥7.* | | . | |
| 23. | | | raction or mixed numbe
o the nearest thousandth. | r in simplest form. (If nec-
.) |
| 24. | 21. 3% | 22. 5% | 23. 5.25% | 24. 12.75% |
| | | | | |

| 25. 38% | 26. 45% | 27. $12\frac{1}{3}\%$ | 28. $16\frac{2}{3}\%$ | 25. |
|----------------------------|-----------------|------------------------------|---------------------------------------|------------|
| | | | | 26. |
| Solve each percent | problem | | | 27 |
| 29. 12% of 70 is v | | 30. 36 is 36% of w | hat number? | 28. |
| | | | | 29. |
| 31. 212.5 is 85% of | of what number? | 32. 66 is what perc | cent of 55? | <u>30.</u> |
| | | | | 31 |
| | | | | 32. |
| 33. 23.8 is what p | ercent of 85? | 34. 38% of 200 is | what number? | 33. |
| | | | | 34. |
| 35. What number | is 25% of 44? | 36. What percent | of 99 is 128.7? | 35. |
| | | | | 36. |
| 37. What percent | of 250 is 2152 | 38. What number | is 45% of 84? | 37. |
| or. mat percent | 01 200 10 210 : | Jo. what humber | , , , , , , , , , , , , , , , , , , , | 38. |
| | | | | <u></u> |
| 39. 42% of what a | number is 63? | 40. 95% of what n | umber is 58.9? | 40. |

Objectives

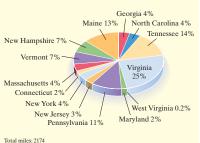


B Find Percent of Increase and Percent of Decrease.

Practice 1

If the total mileage of the Appalachian Trail is 2174, use the circle graph to determine the number of miles in the state of Virginia.

Appalachian Trail Mileage by State Percent



(*Due to rounding, these percents have a sum greater than 100%.) Source: purebound.com

6.5 Applications of Percent

Objective A Solving Applications Involving Percent 🕑

Percent is used in a variety of everyday situations. The next examples show just a few ways that percent occurs in real-life settings. (Each of these examples shows two ways of solving these problems. If you studied Section **6.3** only, see *Method 1*. If you studied Section **6.4** only, see *Method 2*.)

The first example has to do with the Appalachian Trail, a hiking trail conceived by a forester in 1921 and diagrammed to the right.



Example 1

The circle graph in the margin shows the Appalachian Trail mileage by state. If the total mileage of the trail is 2174, use the circle graph to determine the number of miles in the state of New York. Round to the nearest whole mile.

Solution: *Method 1.* First, we state the problem in words.

| In words: | What number | | 4% | of | 2174? |
|--|-------------|---|--------------|--------------|--------------|
| | | V | \downarrow | \downarrow | \downarrow |
| Translate: | n | = | 4% | • | 2174 |
| To solve for <i>n</i> , we find $4\% \cdot 2174$. | | | | | |

| $n = 0.04 \cdot 2174$ | Write 4% as a decimal. |
|-----------------------|-----------------------------|
| n = 86.96 | Multiply. |
| $n \approx 87$ | Round to the nearest whole. |

Rounded to the nearest whole mile, we have that approximately 87 miles of the Appalachian Trail are in New York state.

Method 2. State the problem in words; then translate.

| In words: | What number | is 4% of | 2174? | | |
|-------------------------------|---|---------------------------------------|--------------|--|--|
| | | \downarrow | \downarrow | | |
| | amount | percent | base | | |
| Translate: | $\begin{array}{c} \text{amount} \rightarrow \underline{a} \\ \text{base} \rightarrow \overline{2174} \end{array}$ | $=\frac{4}{100}$ \leftarrow percent | cent | | |
| Next, we solve for <i>a</i> . | | | | | |
| a • 100 | -2174.4 6.4 | | | | |

 $a \cdot 100 = 2174 \cdot 4$ Set cross products equal. $a \cdot 100 = 8696$ Multiply. $a = \frac{8696}{100}$ Divide 8696 by 100, the number multiplied by a. a = 86.96 Simplify. $a \approx 87$ Round to the nearest whole.

Rounded to the nearest whole mile, we have that approximately 87 miles of the Appalachian Trail are in New York state.

Work Practice 1

Answer

1. 543.5 mi

Example 2 Finding Percent of Nursing School Applications Accepted

There continues to be a shortage of nursing school facilities. In 2015, of the 266,000 applications to bachelor degree nursing schools, 120,000 of these were accepted. What percent of these applications were accepted? Round to the nearest percent. (*Source:* American Association of Colleges of Nursing)

| Solution: | Method 1. | First, we state the problem in words. | | | | |
|--|--|---------------------------------------|---|--------|--------------|--|
| In words: | 120,000 | is v | what percent | of | 266,000? | |
| Translate: | ↓
120,000 | • | ↓
n | ↓
• | ↓
266,000 | |
| Next, solve | | | | | , | |
| $\frac{120,000}{266,000}$ | $\frac{120,000}{266,000} = n$ Divide 120,000 by 266,000, the number multiplied by <i>n</i> . | | | | | |
| | | e and ro | ound to the neare | est hu | ndredth. | |
| 45% | $\approx n$ Write | as a pei | cent. | | | |
| About 45% | of nursing s | chool | applications v | were | accepted. | |
| Method 2. | Method 2. | | | | | |
| In words: | 120,000 is | what | percent of | 26 | 6,000? | |
| | | | | | | |
| | amount | pe | ercent | | base | |
| Translate: | amount $\rightarrow \frac{120}{260}$
base $\rightarrow \frac{120}{260}$ | 0,000
5,000 | $=\frac{p}{100} \leftarrow \text{perc}$ | ent | | |
| Next, solve | for <i>p</i> . | | | | | |
| 120,000 | $120,000 \cdot 100 = 266,000 \cdot p$ Set cross products equal. | | | | | |
| 12,00 | 0,000 = 266, | $000 \cdot p$ | Multiply. | | | |
| $\frac{12,000,000}{266,000} = p$ Divide 12,000,000 by 266,000, the number multiplied by <i>p</i> . | | | | | | |
| | $45 \approx p$ | | | | | |

About 45% of nursing school applications were accepted.

Work Practice 2

Example 3 Finding the Base Number of Absences

Mr. Buccaran, the principal at Slidell High School, counted 31 freshmen absent during a particular day. If this is 4% of the total number of freshmen, how many freshmen are there at Slidell High School?

Solution: *Method 1.* First we state the problem in words; then we translate.

In words: 31 is 4% of what number? $\downarrow \downarrow \downarrow \downarrow \downarrow \downarrow$ Translate: 31 = 4% \cdot n

(Continued on next page)

Practice 2

From 2014 to 2024, it is projected that the number of employed nurses will grow by 439,300. If the number of nurses employed in 2014 was 2,751,000, find the percent increase in nurses employed from 2014 to 2024. Round to nearest whole percent. (*Source:* Bureau of Labor Statistics)



Practice 3

The freshmen class of 775 students is 31% of all students at Euclid University. How many students go to Euclid University?

Answers 2. 16% 3. 2500

Chapter 6 | Percent

Next, we solve for *n*.

$$31 = 0.04 \cdot n \quad \text{Write 4\% as a decimal.}$$
$$\frac{31}{0.04} = n \qquad \text{Divide 31 by 0.04, the number multiplied by } n.$$
$$775 = n \qquad \text{Simplify.}$$

There are 775 freshmen at Slidell High School.

Method 2. First we state the problem in words; then we translate.

In words: 31 is 4% of what number? amount percent base Translate: $amount \rightarrow \frac{31}{b} = \frac{4}{100} \leftarrow percent$ Next, we solve for b. $31 \cdot 100 = b \cdot 4$ Set cross products equal.

 $3100 = b \cdot 4$ Multiply. $\frac{3100}{4} = b$ Divide 3100 by 4, the number multiplied by b. 775 = b Simplify.

There are 775 freshmen at Slidell High School.

Work Practice 3

Practice 4

From 2015 to 2016, the number of registered cars and light trucks on the road in the United States increased by 1.5%. In 2015, the number of registered cars and light trucks on the road was 260 million. (*Source:* Hedges Company and Federal Highway Administration)

- **a.** Find the increase in the number of registered cars and light trucks on the road in 2016.
- **b.** Find the total number of registered cars and light trucks on the road in 2016.

Example 4 Finding the Base Increase in Licensed Drivers

From 2015 to 2016, the number of licensed drivers on the road in the United States increased by 5.8%. In 2015, there were about 210 million licensed drivers on the road. (*Source:* Federal Highway Administration)

- a. Find the increase in licensed drivers from 2015 to 2016.
- **b.** Find the number of licensed drivers on the road in 2016.



Solution: Method 1. First we find the increase in the number of licensed drivers.

| In words: | What number | is | 5.8% | of | 210? |
|------------|-------------|--------------|--------------|----|--------------|
| | Ú. | \downarrow | \downarrow | ↓ | \downarrow |
| Translate: | n | = | 5.8% | • | 210 |

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Next, we solve for n.

 $n = 0.058 \cdot 210$ Write 5.8% as a decimal. n = 12.18 Multiply.

a. The increase in the number of licensed drivers was 12.18 million.

b. This means that the number of licensed drivers in 2016 was

Number of
licensed drivers
in 2016Number of
licensed drivers
in 2015Increase
in number of
licensed drivers= 210 million + 12.18 million
= 222.18 million

Method 2. First we find the increase in the number of licensed drivers.

In words: What number is 5.8% of 210? amount percent base Translate: $\frac{amount \rightarrow}{base \rightarrow} \frac{a}{210} = \frac{5.8}{100} \leftarrow percent$

Next, we solve for *a*.

 $a \cdot 100 = 210 \cdot 5.8$ Set cross products equal. $a \cdot 100 = 1218$ Multiply. $a = \frac{1218}{100}$ Divide 1218 by 100, the number multiplied by a. a = 12.18 Simplify.

a. The increase in the number of licensed drivers was 12.18 million.

b. This means that the number of licensed drivers in 2016 was

Number of
licensed driversNumber of
licensed driversIncrease
in 2015= 210 million= 210 million= 222.18 million

Work Practice 4

Objective B Finding Percent of Increase and Percent of Decrease

We often use percents to show how much an amount has increased or decreased. Suppose that the population of a town is 10,000 people and then it increases by 2000 people. The **percent of increase** is

amount of increase $\rightarrow \frac{2000}{10,000} = 0.2 = 20\%$

In general, we have the following.

Percent of Increase

percent of increase = $\frac{\text{amount of increase}}{\text{original amount}}$

Then write the quotient as a percent.

Practice 5

The number of people attending the local play, Peter Pan, increased from 285 on Friday to 333 on Saturday. Find the percent of increase in attendance. Round to the nearest tenth percent.

Helpful 🗋 Hint

Make sure that this number is the original number and not the new number.

Practice 6

A town's population of 20,200 in 1995 decreased to 18,483 in 2005. What was the percent of decrease?

Answers **5.** 16.8% **6.** 8.5%

Concept Check Answers

To find the percent of increase, you have to divide the amount of increase (20) by the original amount (180); 10% decrease.

Chapter 6 | Percent

Example 5 **Finding Percent of Increase**

The number of applications for a mathematics scholarship at Yale increased from 34 to 45 in one year. What is the percent of increase? Round to the nearest whole percent.

Solution: First we find the amount of increase by subtracting the original number of applicants from the new number of applicants.

amount of increase = 45 - 34 = 11

The amount of increase is 11 applicants. To find the percent of increase,

percent of increase = $\frac{\text{amount of increase}}{\text{original amount}} = \frac{11}{34} \approx 0.32 = 32\%$

The number of applications increased by about 32%.

Work Practice 5

Concept Check A student is calculating the percent of increase in enrollment from 180 students one year to 200 students the next year. Explain what is wrong with the following calculations:

| Amount
of increase = | 200 - 180 = 20 |
|-------------------------|-------------------------------|
| Percent of increase = | $\frac{20}{200} = 0.1 = 10\%$ |

Suppose that your income was \$300 a week and then it decreased by \$30. The percent of decrease is

amount of decrease $\rightarrow \frac{\$30}{\$300} = 0.1 = 10\%$

Percent of Decrease

percent of decrease = $\frac{\text{amount of decrease}}{\text{original amount}}$

Then write the quotient as a percent.

Example 6 Finding Percent of Decrease

In response to a decrease in sales, a company with 1500 employees reduces the number of employees to 1230. What is the percent of decrease?

Solution: First we find the amount of decrease by subtracting 1230 from 1500.

amount of decrease = 1500 - 1230 = 270

The amount of decrease is 270. To find the percent of decrease,

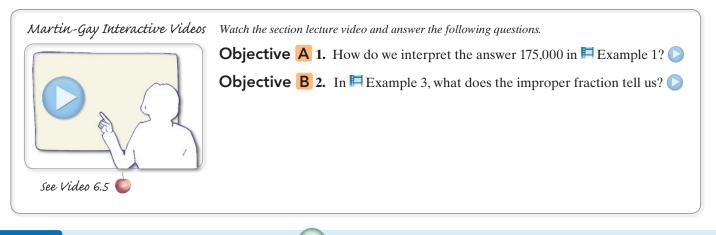
percent of decrease $= \frac{\text{amount of decrease}}{\text{original amount}} = \frac{270}{1500} = 0.18 = 18\%$

The number of employees decreased by 18%.

Work Practice 6

✓ Concept Check An ice cream stand sold 6000 ice cream cones last summer. This year the same stand sold 5400 cones. Was there a 10% increase, a 10% decrease, or neither? Explain.

Vocabulary, Readiness & Video Check



6.5 Exercise Set MyLab Math

Objective A Solve. For Exercises 1 and 2, the solutions have been started for you. See Examples 1 through 4. If necessary, round percents to the nearest tenth and all other answers to the nearest whole.

1. An inspector found 24 defective bolts during an inspection. If this is 1.5% of the total number of bolts inspected, how many bolts were inspected?

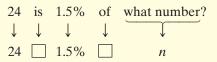
Start the solution:

1. UNDERSTAND the problem. Reread it as many times as needed.

Go to *Method 1* or *Method 2*.

Method 1.

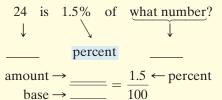
2. TRANSLATE into an equation. (Fill in the boxes.)



- **3.** SOLVE for *n*. (See Example 3, Method 1, for help.)
- **4.** INTERPRET. The total number of bolts inspected was _____.

Method 2.

2. TRANSLATE into a proportion. (Fill in the first two blanks with "amount" or "base.")



- **3.** SOLVE the proportion. (See Example 3, Method 2, for help.)
- **4.** INTERPRET. The total number of bolts inspected was _____.

2. A day care worker found 28 children absent one day during an epidemic of chicken pox. If this was 35% of the total number of children attending the day care center, how many children attend this day care center?

Start the solution:

1. UNDERSTAND the problem. Reread it as many times as needed.

Go to *Method 1* or *Method 2*.

Method 1.

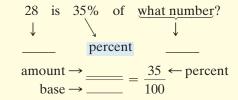
2. TRANSLATE into an equation. (Fill in the boxes.)

| 28 | is | 35% | of | what number? |
|--------------|--------------|--------------|--------------|--------------|
| \downarrow | \downarrow | \downarrow | \downarrow | Ļ |
| 28 | | 35% | | n |

- **3.** SOLVE for *n*. (See Example 3, Method 1, for help.)
- **4.** INTERPRET. The total number of children attending the day care center was _____.

Method 2.

2. TRANSLATE into a proportion. (Fill in the first two blanks with "amount" or "base.")



- **3.** SOLVE the proportion. (See Example 3, Method 2, for help.)
- 4. INTERPRET. The total number of children attending the day care center was _____

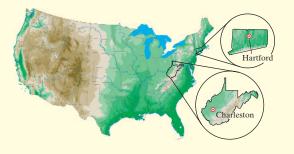
- **3.** The Total Gym provides weight resistance through adjustments of incline. The minimum weight resistance is 4% of the weight of the person using the Total Gym. Find the minimum weight resistance possible for a 220-pound man. (*Source:* Total Gym)
- **5.** A student's cost for last semester at her community college was \$2700. She spent \$378 of that on books. What percent of last semester's college costs was spent on books?
- 7. The United States' motion picture and television industry is made up of over 108,000 businesses. About 85% of these are small businesses with fewer than 10 employees. How many motion picture and television industry businesses have fewer than 10 employees? (*Source:* Motion Picture Association of America)
- **9.** In 2016, there were approximately 36,900 McDonald's restaurants worldwide, with about 14,250 of them located in the United States. Determine the percent of McDonald's restaurants that are in the United States. (*Source:* McDonald's Corporation)
- **11.** A furniture company currently produces 6200 chairs per month. If production decreases by 8%, find the decrease and the new number of chairs produced each month.
- **13.** From 2014 to 2024, the number of people employed as occupational therapy assistants in the United States is expected to increase by 43%. The number of people employed as occupational therapy assistants in 2014 was 41,900. Find the predicted number of occupational therapy assistants in 2024. (*Source:* Bureau of Labor Statistics)



- **4.** The maximum weight resistance for the Total Gym is 60% of the weight of the person using it. Find the maximum weight resistance possible for a 220-pound man. (See Exercise **3** if needed.)
- **6.** Pierre Sampeau belongs to his local food cooperative, where he receives a percentage of what he spends each year as a dividend. He spent \$3850 last year at the food cooperative store and received a dividend of \$154. What percent of his total spending at the food cooperative did he receive as a dividend?
- **8.** In 2015, there were approximately 43,700 cinema screens in the United States and Canada. If about 37.5% of the total screens in the United States and Canada were digital 3-D screens, find the approximate number of digital 3-D screens. Round to the nearest whole.
- **10.** Of the 66,800 veterinarians in private practice in the United States in 2015, approximately 30,100 are men. Determine the percent of male veterinarians in private practice in the United States in 2015. (*Source:* American Veterinary Medical Association)
- **12.** The enrollment at a local college decreased by 5% over last year's enrollment of 7640. Find the decrease in enrollment and the current enrollment.
- **14.** From the London Summer Olympics 2012 to the Rio Summer Olympics 2016, the number of medals awarded increased by 118.5%. If 962 medals were awarded in London, how many were awarded four years later in Rio? (*Source:* BBC Sports)



Two States, West Virginia and Connecticut, decreased in population from 2014 to 2017. Their locations are shown on the partial U.S. map below. Round each answer to the nearest thousand. (Source: United States Census Bureau)



- **15.** In 2014, the population of West Virginia was approximately 1853 thousand. If the population decrease was about 0.97%, find the population of West Virginia in 2017.
- **16.** In 2014, the population of Connecticut was approximately 3595 thousand. If the population decrease was about 0.22%, find the population of Connecticut in 2017.

A popular extreme sport is snowboarding. Ski trails are marked with difficulty levels of easy \bullet , intermediate \blacksquare , difficult \diamond , expert $\diamond \diamond$, and other variations. Use this information for Exercises 17 and 18. Round each percent to the nearest whole. See *Example 2.*

- **17.** At Keystone ski area in Colorado, 38 of the 131 total ski runs are rated intermediate. What percent of the runs are intermediate? (*Source:* Vail Resorts Management Company)
- **18.** At Telluride ski area in Colorado, 29 of the 127 total ski trails are rated easy. What percent of the trails are easy? (*Source:* Telluride Ski & Golf Resort)

For each food described, find the percent of total calories from fat. If necessary, round to the nearest tenth percent. See *Example 2.*

19. Ranch dressing serving size of 2 tablespoons

| | Calories |
|----------|----------|
| Total | 40 |
| From fat | 20 |

^{21.} Nutrition Facts

| Serving Size 1 pouch (20g)
Servings Per Container 6 | | | |
|---|--|--|--|
| Amount Per Serving | | | |
| | | | |
| Calories 80 | | | |
| Calories from fat 10 | | | |
| % Daily Value* | | | |
| Total Fat 1g 2% | | | |
| Sodium 45mg 2% | | | |
| Total
Carbohydrate 17g 6% | | | |
| Sugars 9g | | | |
| Protein 0g | | | |
| Vitamin C 25% | | | |
| Not a significant source of
saturated fat, cholesterol, dietary
fiber, vitamin A, calcium and iron. | | | |
| *Percent Daily Values are based
on a 2,000 calorie diet. | | | |

Artificial Fruit Snacks

20. Unsweetened cocoa powder serving size of 1 tablespoon

| | Calories |
|----------|----------|
| Total | 20 |
| From fat | 5 |

^{22.} Nutrition Facts

| Serving Size $\frac{1}{4}$ cup (33g)
Servings Per Container About 9 | | |
|--|-------------|--|
| Amount Per Serving | | |
| Calories 190 Calories from | Fat 130 | |
| % [| Daily Value | |
| Total Fat 16g | 24% | |
| Saturated Fat 3g | 16% | |
| Cholesterol 0mg | 0% | |
| Sodium 135mg | 6% | |
| Total Carbohydrate 9g | 3% | |
| Dietary Fiber 1g | 5% | |
| Sugars 2g | | |
| Protein 5g | | |
| | | |
| Vitamin A 0% • Vitamin C 0%
Calcium 0% • Iron 8% | | |

Peanut Mixture

| Nutrition Facts
Serving Size 18 crackers (29g)
Servings Per Container About 9 | | 24. Nutrition Facts
Serving Size 28 crackers (31
Servings Per Container Abo | g) |
|---|------------|---|--------------|
| Amount Per Serving | | Amount Per Serving | |
| Calories 120 Calories from | Fat 35 | Calories 130 Calories from F | at 35 |
| % Da | ily Value* | % Dail | y Value |
| Total Fat 4g | 6% | Total Fat 4g | 6% |
| Saturated Fat 0.5g | 3% | Saturated Fat 2g | 10% |
| Polyunsaturated Fat 0g | | Polyunsaturated Fat 1g | |
| Monounsaturated Fat 1.5g | | Monounsaturated Fat 1g | |
| Cholesterol Omg | 0% | Cholesterol Omg | 0% |
| Sodium 220mg | 9% | Sodium 470mg | 20% |
| Total Carbohydrate 21g | 7% | Total Carbohydrate 23g | 8% |
| Dietary Fiber 2g | 7% | Dietary Fiber 1g | 4% |
| Sugars 3g | | Sugars 4g | |
| Protein 2g | | Protein 2g | |
| | | | |
| Vitamin A 0% • Vitamin C 09 | 6 | Vitamin A 0% • Vitamin C 0% |) |
| Calcium 2% • Iron 4%
Phosphorus 10% | | Calcium 0% • Iron 2% | |
| Snack Crackers | | Snack Crackers | |

Solve. If necessary, round money amounts to the nearest cent and all other amounts to the nearest tenth. See Examples 1 through 4.

- 25. A family paid \$26,250 as a down payment for a home. If this represents 15% of the price of the home, find the price of the home.
 - **27.** An owner of a printer repair company estimates that for every 40 hours a repairperson is on the job, he can bill for only 78% of the hours. The remaining hours, the repairperson is idle or driving to or from a job. Determine the number of hours per 40-hour week the owner can bill for a repairperson.
 - **29.** A car manufacturer announced that next year the price of a certain model of car will increase by 4.5%. This year the price is \$19,286. Find the increase in price and the new price.

- **26.** A banker learned that \$842.40 is withheld from his monthly check for taxes and insurance. If this represents 18% of his total pay, find the total pay.
- **28.** A manufacturer of electronic components expects 1.04% of its products to be defective. Determine the number of defective components expected in a batch of 28,350 components. Round to the nearest whole component.
- **30.** A union contract calls for a 6.5% salary increase for all employees. Determine the increase and the new salary that a worker currently making \$58,500 under this contract can expect.

A popular extreme sport is artificial wall climbing. The photo shown is an artificial climbing wall. Exercises 31 and 32 are about the Footsloggers Climbing Tower in Boone, North Carolina.



- **31.** A climber is resting at a height of 24 feet while on the Footsloggers Climbing Tower. If this is 60% of the tower's total height, find the height of the tower.
- **32.** A group plans to climb the Footsloggers Climbing Tower at the group rate, once they save enough money. Thus far, \$175 has been saved. If this is 70% of the total amount needed for the group, find the total price.

Solve.

- **33.** Tuition for an Ohio resident at the Columbus campus of Ohio State University was \$8994 in 2010. The tuition increased by 11.6% during the period from 2010 to 2016. Find the increase and the tuition for the 2016–2017 school year. Round the increase to the nearest whole dollar. (*Source:* Ohio State University)
- **35.** From 2014–2015 to 2024–2025, the number of students enrolled in an associate degree program is projected to increase by 22.3%. If the enrollment in associate degree programs in 2014–2015 was 6,700,000, find the increase and the projected number of students enrolled in an associate degree program in 2024–2025. (*Source:* National Center for Educational Statistics)
- **34.** The population of Americans aged 65 and older was 46 million in 2014. That population is projected to increase by 57% by 2030. Find the increase and the projected 2030 population. (*Source:* Administration for Community Living, U.S. Department of Health and Human Services)
- **36.** From 2010–2011 to 2021–2022, the number of bachelor degrees awarded is projected to increase by 17.4%. If the number of bachelor degrees awarded in 2010–2011 was 1,703,000, find the increase and the projected number of bachelor degrees awarded in the 2021–2022 school year. (*Source:* National Center for Educational Statistics)

Objective B *Find the amount of increase and the percent of increase. See Example 5.*

| | Original Amount | New Amount | Amount of Increase | Percent of Increase |
|-----|-----------------|------------|--------------------|---------------------|
| 37. | 50 | 80 | | |
| 38. | 8 | 12 | | |
| 39. | 65 | 117 | | |
| 40. | 68 | 170 | | |

Find the amount of decrease and the percent of decrease. See Example 6.

| | Original Amount | New Amount | Amount of Decrease | Percent of Decrease |
|-----|-----------------|------------|--------------------|---------------------|
| 41. | 8 | 6 | | |
| 42. | 25 | 20 | | |
| 43. | 160 | 40 | | |
| 44. | 200 | 162 | | |

Solve. Round percents to the nearest tenth, if necessary. See Examples 5 and 6.

- 45. There are 150 calories in a cup of whole milk and only 84 in a cup of skim milk. In switching to skim milk, find the percent of decrease in number of calories per cup.
 - **47.** The number of cable TV systems recently decreased from 10,845 to 10,700. Find the percent of decrease.
- **46.** In reaction to a slow economy, the number of employees at a soup company decreased from 530 to 477. What was the percent of decrease in the number of employees?
- **48.** Before taking a typing course, Geoffry Landers could type 32 words per minute. By the end of the course, he was able to type 76 words per minute. Find the percent of increase.

- ◆ 49. In 1940, the average size of a privately owned farm in the United States was 174 acres. In a recent year, the average size of a privately owned farm in the United States had increased to 421 acres. Find the percent of increase. (*Source:* National Agricultural Statistics Service)
 - **51.** In 2016, there were approximately 71 million virtual reality devices in use worldwide. This is expected to grow to 337 million in 2020. Find the projected percent of increase. (*Source:* CTIA—The Wireless Association)



- **53.** In 2014, there were 3782 thousand elementary and secondary teachers employed in the United States. This number is expected to increase to 4151 thousand teachers in 2021. Find the percent of increase. (*Source:* National Center for Educational Statistics)
- **55.** In 1999, total revenue from U.S. music sales and licensing was \$14.6 billion. By 2015, this revenue had dropped to \$7.1 billion. Find this percent of decrease in music revenue. (*Source:* Recording Industry Association of America)
- **57.** The average U.S. movie theater ticket price in 2007 was \$6.88. For 2017, it was estimated to be \$8.87. Find the percent of increase in average move theater ticket price for this 10–year period. (*Source:* Motion Picture Association of America)
- **59.** The number of cell phone tower sites in the United States was 253,086 in 2010. By 2016, the number of cell sites had increased to 307,626. Find the percent of increase. (*Source:* CTIA—The Wireless Association)



- **50.** In 2012, there were 2109 thousand farms in the United States. In 2016, the number of farms in the United States had decreased to 2060 thousand farms. Find the percent of decrease. (*Source:* U.S. Dept. of Agriculture)
- **52.** Between 2014 and 2015, permanent digital downloads of singles decreased from approximately 1199 million to approximately 1021 million. Find the percent of decrease. (*Source:* Recording Industry Association of America)



- **54.** In 2014, approximately 475 thousand correctional officers were employed in the United States. By 2024, this number is expected to increase to 493 thousand correctional officers. Find the percent of increase. (*Source:* Bureau of Labor Statistics)
- **56.** As the largest health care occupation, registered nurses held about 3.1 million jobs in 2015. The number of registered nurses is expected to be 3.9 million by 2025. Find the percent of increase. (*Source:* American Association of Colleges of Nursing)
- **58.** The average temperature for the contiguous United States during February 2017 was 41.2° Fahrenheit. The 20th-century average temperature for February is 33.9° Fahrenheit. What is the percent of increase in average temperature for February? (*Source:* National Centers for Environmental Information)
- **60.** In 2014, Ford Motor Corporation sold 2386 thousand automobiles and trucks. In 2016, its sales were 2464 thousand vehicles. Find the percent of increase from 2014 to 2016. (*Source:* Ford Motor Company)



Review

Perform each indicated operation. See Sections 4.3 and 4.4.

| 61. 0.12
<u>× 38</u> | 62. 42×0.7 | 63. 9.20 + 1.98 |
|--------------------------------|----------------------------|--------------------------|
| 64. 46 + 7.89 | 65. 78 – 19.46 | 66. 64.80 - 10.72 |

Concept Extensions

- **67.** If a number is increased by 100%, how does the increased number compare with the original number? Explain your answer.
- **68.** In your own words, explain what is wrong with the following statement. "Last year we had 80 students attend. This year we have a 50% increase or a total of 160 students attending."

Explain what errors were made by each student when solving percent of increase or decrease problems and then correct the errors. See the Concept Checks in this section.

The population of a certain rural town was 150 in 1980, 180 in 1990, and 150 in 2000.

69. Find the percent of increase in population from 1980 to 1990.

Miranda's solution: Percent of increase $=\frac{30}{180}=0.1\overline{6}\approx 16.7\%$

70. Find the percent of decrease in population from 1990 to 2000.

Jeremy's solution: Percent of decrease $=\frac{30}{150}=0.20=20\%$

71. The percent of increase from 1980 to 1990 is the same as the percent of decrease from 1990 to 2000. True or false.

Chris's answer: True because they had the same amount of increase as the amount of decrease.

72. Refer to Exercises **49** and **50**. They are similar except one asks us to find the percent of increase in the size of U.S. privately owned farms and one asks us to find the percent of decrease. In your own words, explain how these can both be correct.

6.6 Percent and Problem Solving: Sales Tax, Commission, and Discount

Objective A Calculating Sales Tax and Total Price 💟

Percents are frequently used in the retail trade. For example, most states charge a tax on certain items when purchased. This tax is called a **sales tax**, and retail stores collect it for the state. Sales tax is almost always stated as a percent of the purchase price.

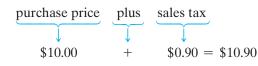
A 9% sales tax rate on a purchase of a \$10 calculator gives a sales tax of

sales tax = 9% of $10 = 0.09 \cdot 10.00 = 0.09$

Objectives



The total price to the customer would be



This example suggests the following equations:

Sales Tax and Total Price

sales $tax = tax rate \cdot purchase price$ total price = purchase price + sales tax

In this section we round dollar amounts to the nearest cent.

Example 1

Finding Sales Tax and Purchase Price

Find the sales tax and the total price on the purchase of an \$85.50 atlas in a city where the sales tax rate is 7.5%.



Solution: The purchase price is \$85.50 and the tax rate is 7.5%.

sales tax = tax rate · purchase price

$$\downarrow$$
 \downarrow \downarrow \downarrow
sales tax = 7.5% · \$85.50
= 0.075 · \$85.50 Write 7.5% as a decimal.
 \approx \$6.41 Round to the nearest cent.

Thus, the sales tax is \$6.41. Next find the total price.

total price = purchase price + sales tax

$$\downarrow \qquad \downarrow \qquad \checkmark \qquad \checkmark$$

total price = \$85.50 + \$6.41
= \$91.91

The sales tax on \$85.50 is \$6.41, and the total price is \$91.91.

Work Practice 1

Concept Check The purchase price of a textbook is \$150 and sales tax is 10%. If you are told by the cashier that the total price is \$195, how can you tell that a mistake has been made?

Practice 1

If the sales tax rate is 8.5%, what is the sales tax and the total amount due on a \$59.90 Goodgrip tire? (Round the sales tax to the nearest cent.)

Answer 1. tax: \$5.09; total: \$64.99

✓ Concept Check Answer

Since $10\% = \frac{1}{10}$, the sales tax is $\frac{\$150}{10} = \15 . The total price should have been \$165.

Example 2

2 Finding a Sales Tax Rate

The sales tax on a \$406 Sony flat-screen digital 27-inch television is \$34.51. Find the sales tax rate.

Solution: Let *r* represent the unknown sales tax rate. Then

sales tax = tax rate · purchase price \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow $\$34.51 = r \cdot \406 $\frac{34.51}{406} = r$ Divide 34.51 by 406, the number multiplied by r. 0.085 = r Simplify. 8.5% = r Write 0.085 as a percent.



The sales tax rate is 8.5%.



Objective **B** Calculating Commissions **C**

A **wage** is payment for performing work. Hourly wage, commissions, and salary are some of the ways wages can be paid. Many people who work in sales are paid a commission. An employee who is paid a **commission** is paid a percent of his or her total sales.

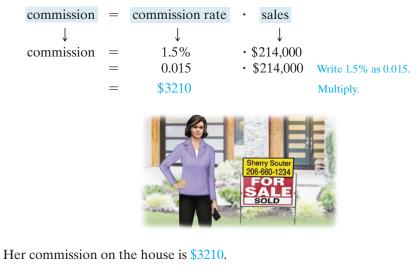
Commission

commission = commission rate \cdot sales

Example 3 Finding the Amount of Commission

Sherry Souter, a real estate broker for Wealth Investments, sold a house for \$214,000 last week. If her commission rate is 1.5% of the selling price of the home, find the amount of her commission.

Solution:



Work Practice 3

Practice 2

The sales tax on an \$18,500 automobile is \$1665. Find the sales tax rate.

Practice 3

A sales representative for Office Product Copiers sold \$47,632 worth of copy equipment and supplies last month. What is his commission for the month if he is paid a commission rate of 6.6% of his total sales for the month?

Answers 2. 9% 3. \$3143.71

Chapter 6 | Percent

Practice 4

A salesperson earns \$645 for selling \$4300 worth of appliances. Find the commission rate.

Example 4 Finding a Commission Rate

A salesperson earned \$1560 for selling \$13,000 worth of electronics equipment. Find the commission rate.

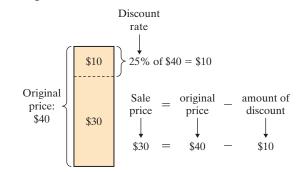
Solution: Let *r* stand for the unknown commission rate. Then

| commission | = | commission rat | e · sales |
|-----------------------|-------|----------------|---|
| \downarrow | | \downarrow | \downarrow |
| \$1560 | = | r | · \$13,000 |
| $\frac{1560}{13,000}$ | = | r Divid | e 1560 by 13,000, the number multiplied by <i>r</i> . |
| 0.12 | = | r Simpl | ify. |
| 12% | = | <i>r</i> Write | 0.12 as a percent. |
| The commission ra | ate i | is 12%. | |

Work Practice 4

Objective C Calculating Discount and Sale Price 📀

Suppose that an item that normally sells for \$40 is on sale for 25% off. This means that the **original price** of \$40 is reduced, or **discounted**, by 25% of \$40, or \$10. The **discount rate** is 25%, the **amount of discount** is \$10, and the **sale price** is \$40 - \$10, or \$30. Study the diagram below to visualize these terms.



To calculate discounts and sale prices, we can use the following equations:

Discount and Sale Price

amount of discount = discount rate \cdot original price

sale price = original price - amount of discount

Example 5 Finding a Discount and a Sale Price

An electric rice cooker that normally sells for \$65 is on sale for 25% off. What is the amount of discount and what is the sale price?

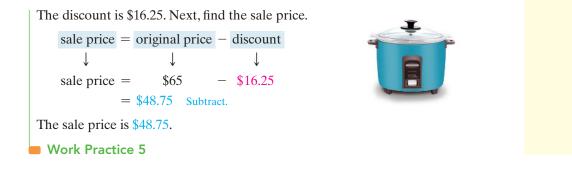
Solution: First we find the amount of discount, or simply the discount.

| amount of discount | = | discount r | ate • | original price |
|--------------------|---|--------------|-----------|----------------|
| \downarrow | | \downarrow | | \downarrow |
| amount of discount | = | 25% | • | \$65 |
| | = | 0.25 · \$65 | Write 25 | % as 0.25. |
| | = | \$16.25 | Multiply. | |

A discontinued washer and dryer combo is advertised on sale for 35% off the regular price of \$1600. Find the amount of discount and the sale price.



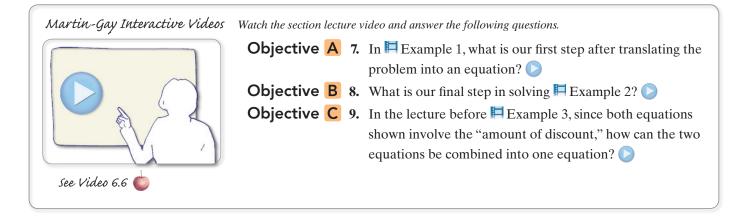
Answers 4. 15% 5. \$560; \$1040



Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Some choices may be used more than once.

| | amount of discount commission | sale price
total price | sales tax | | |
|----|-------------------------------|-------------------------------------|-----------------|--|--|
| 1. | | $t = tax rate \cdot purchase price$ | e. | | |
| 2. | = purchase price + sales tax. | | | | |
| 3. | | $=$ commission rate \cdot sales | | | |
| 4. | | $=$ discount rate \cdot original | price. | | |
| 5. | | = original price $-$ amoun | nt of discount. | | |
| 6. | sale price = original | price – | | | |



6.6 Exercise Set MyLab Math

Objective A Solve. See Examples 1 and 2.

- **1.** What is the sales tax on a jacket priced at \$150 if the sales tax rate is 5%?
- **3.** The purchase price of a camcorder is \$799. What is the total price if the sales tax rate is 7.5%?
- **5.** A new large-screen television has a purchase price of \$4790. If the sales tax on this purchase is \$335.30, find the sales tax rate.
- **2.** If the sales tax rate is 6%, find the sales tax on a microwave oven priced at \$188.
- **4.** A stereo system has a purchase price of \$426. What is the total price if the sales tax rate is 8%?
- **6.** The sales tax on the purchase of a \$6800 used car is \$374. Find the sales tax rate.

- 7. The sales tax on a table saw is \$22.95.
 - a. What is the purchase price of the table saw (before tax) if the sales tax rate is 8.5%? (*Hint:* Use the sales tax equation and insert the replacement values.)
 - **b.** Find the total price of the table saw.



- **9.** A gold-plated and diamond bracelet sells for \$1800. Find the sales tax and the total price if the sales tax rate is 6.5%.
- 11. The sales tax on the purchase of a futon is \$24.25. If the tax rate is 5%, find the purchase price of the futon (before tax).
 - **13.** The sales tax is \$98.70 on a stereo sound system purchase of \$1645. Find the sales tax rate.
 - **15.** A cell phone costs \$210, a battery charger costs \$15, and batteries cost \$5. What is the sales tax and total price for purchasing these items if the sales tax rate is 7%?



- **Objective B** Solve. See Examples 3 and 4.
- **17.** A sales representative for a large furniture warehouse is paid a commission rate of 4%. Find her commission if she sold \$1,329,401 worth of furniture last year.
- 19. A salesperson earned a commission of \$1380.40 for selling \$9860 worth of paper products. Find the commission rate.

- **8.** The sales tax on a one-half-carat diamond ring is \$76.
 - **a.** Find the purchase price of the ring (before tax) if the sales tax rate is 9.5%. (See the hint for Exercise **7a**.)
 - **b.** Find the total price of the ring.



- **10.** The purchase price of a laptop computer is \$1890. If the sales tax rate is 8%, what is the sales tax and the total price?
- **12.** The sales tax on the purchase of an LED television combination is \$59.85. If the tax rate is 9%, find the purchase price of the LED TV (before tax).
- **14.** The sales tax is \$103.50 on a necklace purchase of \$1150. Find the sales tax rate.
- **16.** Ms. Warner bought a blouse for \$35, a skirt for \$55, and a blazer for \$95. Find the sales tax and the total price she paid, given a sales tax rate of 6.5%.



- **18.** Rosie Davis-Smith is a beauty consultant for a home cosmetic business. She is paid a commission rate of 12.8%. Find her commission if she sold \$1638 in cosmetics last month.
- **20.** A salesperson earned a commission of \$3575 for selling \$32,500 worth of books to various bookstores. Find the commission rate.

- **21.** How much commission will Jack Pruet make on the sale of a \$325,900 house if he receives 1.5% of the selling price?
- **23.** A real estate agent earned a commission of \$5565 for selling a house. If his rate is 3%, find the selling price of the house. (*Hint:* Use the commission equation and insert the replacement values.)
- **22.** Frankie Lopez sold \$9638 of jewelry this week. Find her commission for the week if she receives a commission rate of 5.6%.
- **24.** A salesperson earned \$1750 for selling fertilizer. If her commission rate is 7%, find the selling price of the fertilizer. (See the hint for Exercise **23**.)

Objective C Find the amount of discount and the sale price. See Example 5.

| | Original Price | Discount Rate | Amount of Discount | Sale Price |
|-----|----------------|---------------|--------------------|------------|
| 25. | \$89 | 10% | | |
| 26. | \$74 | 20% | | |
| 27. | \$196.50 | 50% | | |
| 28. | \$110.60 | 40% | | |
| 29. | \$410 | 35% | | |
| 30. | \$370 | 25% | | |
| 31. | \$21,700 | 15% | | |
| 32. | \$17,800 | 12% | | |

■ **33.** A \$300 fax machine is on sale for 15% off. Find the amount of discount and the sale price.

Objectives A B Mixed Practice Complete each table.

| | Purchase Price | Tax Rate | Sales Tax | Total Price |
|-----|----------------|----------|-----------|-------------|
| 35. | \$305 | 9% | | |
| 36. | \$243 | 8% | | |
| 37. | \$56 | 5.5% | | |
| 38. | \$65 | 8.4% | | |

34. A \$4295 designer dress is on sale for 30% off. Find the amount of discount and the sale price.

| | Sale | Commission Rate | Commission |
|-----|-----------|-----------------|------------|
| 39. | \$235,800 | 3% | |
| 40. | \$195,450 | 5% | |
| 41. | \$17,900 | | \$1432 |
| 42. | \$25,600 | | \$2304 |

Review

Multiply. See Sections 4.4 and 4.6.

43. $2000 \cdot \frac{3}{10} \cdot 2$ **44.** $500 \cdot \frac{2}{25} \cdot 3$ **46.** $1000 \cdot \frac{1}{20} \cdot 5$ **47.** $600 \cdot 0.04 \cdot \frac{2}{3}$

45.
$$400 \cdot \frac{3}{100} \cdot 11$$

48.
$$6000 \cdot 0.06 \cdot \frac{3}{4}$$

Concept Extensions

Solve. See the Concept Check in this section.

- **49.** Your purchase price is \$68 and the sales tax rate is 9.5%. Round each amount and use the rounded amounts to estimate the total price. Choose the best estimate.
 - **a.** \$105 **b.** \$58 **c.** \$93 **d.** \$77

50. Your purchase price is \$200 and the tax rate is 10%. Choose the best estimate of the total price.
a. \$190 b. \$210 c. \$220 d. \$300

Tipping

One very useful application of percent is mentally calculating a tip. Recall that to find 10% of a number, simply move the decimal point one place to the left. To find 20% of a number, just double 10% of the number. To find 15% of a number, find 10% and then add to that number half of the 10% amount. Mentally fill in the chart below. To do so, start by rounding the bill amount to the nearest dollar.

| | Tipping Chart | | | | | | | |
|-----|-----------------------|--|--|--|--|--|--|--|
| | Bill Amount 10% 15% 2 | | | | | | | |
| 51. | \$40.21 | | | | | | | |
| 52. | \$15.89 | | | | | | | |
| 53. | \$72.17 | | | | | | | |
| 54. | \$9.33 | | | | | | | |

- **55.** Suppose that the original price of a shirt is \$50. Which is better, a 60% discount or a discount of 30% followed by a discount of 35% of the reduced price? Explain your answer.
- **57.** A diamond necklace sells for \$24,966. If the tax rate is 7.5%, find the total price.
- **56.** Which is better, a 30% discount followed by an additional 25% off or a 20% discount followed by an additional 40% off? To see, suppose an item costs \$100 and calculate each discounted price. Explain your answer.
- **58.** A house recently sold for \$562,560. The commission rate on the sale is 5.5%. If the real estate agent is to receive 60% of the commission, find the amount received by the agent.

Objectives

- 🗛 Calculate Simple Interest. >
- B Calculate Compound Interest.
- C Calculate Monthly Payments.

6.7 Percent and Problem Solving: Interest 🔘

Objective 🗛 Calculating Simple Interest 💟

Interest is money charged for using other people's money. When you borrow money, you pay interest. When you loan or invest money, you earn interest. The money borrowed, loaned, or invested is called the **principal amount**, or simply **principal**. Interest is normally stated in terms of a percent of the principal for a given period of time. The **interest rate** is the percent used in computing the interest. Unless stated otherwise, *the rate is understood to be per year*. When the interest is calculated using the following equation:

Simple Interest

Simple Interest = Principal \cdot Rate \cdot Time $I = P \cdot R \cdot T$ where the rate is understood to be per year and time is in years.

Example 1 Finding Simple Interest

Find the simple interest after 2 years on \$500 at an interest rate of 12%.

Solution: In this example, P = \$500, R = 12%, and T = 2 years. Replace the variables with values in the formula I = PRT.

$$I = P \cdot R \cdot T$$

 $I = $500 \cdot 12\% \cdot 2$ Let P = \$500, R = 12%, and T = 2.

= \$500 · (0.12) · 2 Write 12% as a decimal.

= \$120 Multiply.

The simple interest is \$120.

Work Practice 1

If time is not given in years, we need to convert the given time to years.

Example 2 Finding Simple Interest

Ivan Borski borrowed \$2400 at 10% simple interest for 8 months to help him buy a used Toyota Corolla. Find the simple interest he paid.

Solution: Since there are 12 months in a year, we first find what part of a year 8 months is.

8 months = $\frac{8}{12}$ year = $\frac{2}{3}$ year

Now we find the simple interest.

simple interest = principal · rate · time

$$\downarrow$$
 \downarrow \downarrow \downarrow \downarrow
simple interest = \$2400 · 10% · $\frac{2}{3}$
= \$2400 · 0.10 · $\frac{2}{3}$
= \$160

The interest on Ivan's loan is \$160.

Work Practice 2

Concept Check Suppose in Example 2 you had obtained an answer of \$16,000. How would you know that you had made a mistake in this problem?

When money is borrowed, the borrower pays the original amount borrowed, or the principal, as well as the interest. When money is invested, the investor receives the original amount invested, or the principal, as well as the interest. In either case, the **total amount** is the sum of the principal and the interest.

Finding the Total Amount of a Loan or Investment

total amount (paid or received) = principal + interest

Practice 1

Find the simple interest after 5 years on \$875 at an interest rate of 7%.

Practice 2

A student borrowed \$1500 for 9 months on her credit card at a simple interest rate of 20%. How much interest did she pay?

Answers 1. \$306.25 2. \$225

Concept Check Answer \$16,000 is too much interest.



Chapter 6 | Percent

Practice 3

If \$2100 is borrowed at a simple interest rate of 13% for 6 months, find the total amount paid.

Example 3 Finding the Total Amount of an Investment

An accountant invested \$2000 at a simple interest rate of 10% for 2 years. What total amount of money will she have from her investment in 2 years?

Solution: First we find her interest.

 $I = P \cdot R \cdot T$ = \$2000 \cdot (0.10) \cdot 2 Let P = \$2000, R = 10\% or 0.10, and T = 2. = \$400

The interest is \$400.

Next, we add the interest to the principal.

| total amount | = | principal | + | interest |
|--------------|---|--------------|---|--------------|
| \downarrow | | \downarrow | | \downarrow |
| total amount | = | \$2000 | + | \$400 |
| | = | \$2400 | | |

After 2 years, she will have a total amount of \$2400.

Work Practice 3

Concept Check Which investment would earn more interest: an amount of money invested at 8% interest for 2 years, or the same amount of money invested at 8% for 3 years? Explain.

Objective **B** Calculating Compound Interest 🕑

Recall that simple interest depends on the original principal only. Another type of interest is compound interest. **Compound interest** is computed not only on the principal, but also on the interest already earned in previous compounding periods. Compound interest is used more often than simple interest.

Let's see how compound interest differs from simple interest. Suppose that \$2000 is invested at 7% interest **compounded annually** for 3 years. This means that interest is added to the principal at the end of each year and that next year's interest is computed on this new amount. In this section, we round dollar amounts to the nearest cent.

| | Amount at
Beginning of
Year | Principal | • | Rate | • | Time | = Interest | Amount at End of Year |
|----------|-----------------------------------|-----------|---|------|---|------|------------|-----------------------------|
| 1st year | \$2000 | \$2000 | • | 0.07 | • | 1 | = \$140 | 2000 + 140 = 2140 |
| 2nd year | \$2140 | \$2140 | • | 0.07 | • | 1 | = \$149.80 | \$2140 + 149.80 = \$2289.80 |
| 3rd year | \$2289.80 | \$2289.80 | • | 0.07 | • | 1 | = \$160.29 | 2289.80 + 160.29 = 2450.09 |

The compound interest earned can be found by

· 0.07 ·

\$2000

| total amou | ınt – | origin | al princ | cipal | = | compound interest |
|-----------------|-----------------------------------|---|--|--|---|--|
| \downarrow | | | \downarrow | | | \downarrow |
| \$2450.09 |) — | | \$2000 | | = | \$450.09 |
| The simple inte | erest e | arned | would l | nave | beer | n |
| principal | • ra | te • | time | = | inte | erest |
| \downarrow | ` | Ļ | \downarrow | | | \downarrow |
| | ↓
\$2450.09
The simple inte | ↓
\$2450.09 –
The simple interest e | ↓
\$2450.09 –
The simple interest earned | \downarrow \downarrow \downarrow
\$2450.09 - \$2000
The simple interest earned would I | \downarrow \downarrow \downarrow
\$2450.09 - \$2000
The simple interest earned would have | total amount $-$ original principal $=$
\downarrow \downarrow
\$2450.09 - $$2000 =The simple interest earned would have beenprincipal \cdot rate \cdot time = interest\downarrow \downarrow \downarrow \downarrow$ |

3

=

\$420

Answer

3. \$2236.50

Concept Check Answer

8% for 3 years. Since the interest rate is the same, the longer you keep the money invested, the more interest you earn. *Since compound interest earns "interest on interest," compound interest earns more than simple interest.*

Computing compound interest using the method on the previous page can be tedious. We can use a calculator and the compound interest formula below to compute compound interest more quickly.

Compound Interest Formula

The total amount A in an account is given by

$$A = P\left(1 + \frac{r}{n}\right)^n$$

where P is the principal, r is the interest rate written as a decimal, t is the length of time in years, and n is the number of times compounded per year.

Example 4 \$1800 is invested at 2% interest compounded annually. Find the total amount after 3 years.

Solution: "Compounded annually" means 1 time a year, so

$$n = 1$$
. Also, $P = $1800, r = 2\% = 0.02$, and $t = 3$ years.

$$A = P\left(1 + \frac{r}{n}\right)^{1/3}$$

= $1800\left(1 + \frac{0.02}{1}\right)^{1/3}$
= $1800(1.02)^3$
 ≈ 1910.17
Remember order
of operations. First evaluate
 $(1.02)^3$, then multiply by 1800.

The total amount at the end of 3 years is \$1910.17.

Work Practice 4

Example 5 Finding Total Amount Received from an Investment

\$4000 is invested at 5.3% compounded quarterly for 10 years. Find the total amount at the end of 10 years.

Solution: "Compounded quarterly" means 4 times a year, so

$$n = 4$$
. Also, $P = $4000, r = 5.3\% = 0.053$, and $t = 10$ years.
 $A = P\left(1 + \frac{r}{n}\right)^{n \cdot t}$
 $= 4000\left(1 + \frac{0.053}{4}\right)^{4 \cdot 10}$

$$= 4000(1.01325)^{40}$$

≈ 6772.12

~ 0772.12

The total amount after 10 years is \$6772.12.

Work Practice 5

Note: Part of the compound interest formula, $\left(1 + \frac{r}{n}\right)^{n \cdot t}$, is called the **compound interest factor.** Appendix A.7 contains a table of various calculated compound interest factors. Another way to calculate the total amount, *A*, in the compound interest

Practice 4

\$3000 is invested at 4% interest compounded annually. Find the total amount after 6 years.

Practice 5

\$5500 is invested at $6\frac{1}{4}$ % compounded *daily* for 5 years. Find the total amount at the end of 5 years. (Use 1 year = 365 days.)

formula is to multiply the principal, P, by the appropriate compound interest factor found inAppendix A.7.

The Calculator Explorations box below shows how compound interest factors are calculated.

Objective C Calculating a Monthly Payment

We conclude this section with a method to find the monthly payment on a loan.

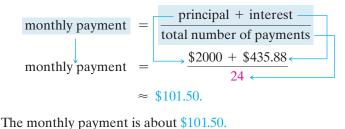
Finding the Monthly Payment of a Loan

principal + interest monthly payment = -total number of payments

Example 6 Finding a Monthly Payment

Find the monthly payment on a \$2000 loan for 2 years. The interest on the 2-year loan is \$435.88.

Solution: First we determine the total number of monthly payments. The loan is for 2 years. Since there are 12 months per year, the number of payments is $2 \cdot 12$, or 24. Now we calculate the monthly payment.



Answer 6. \$114.54

(

Practice 6

Find the monthly payment on a

\$3000 3-year loan if the interest

on the loan is \$1123.58.

Work Practice 6

Calculator Explorations Compound Interest Factor

A compound interest factor may be found by using your calculator and evaluating the formula

compound interest factor
$$= \left(1 + \frac{r}{n}\right)^{n \cdot t}$$

where r is the interest rate, t is the time in years, and n is the number of times compounded per year. For example, the compound interest factor for 10 years at 8% compounded semiannually is about 2.19112. Let's find this factor by evaluating the compound interest factor formula when r = 8% or 0.08, t = 10, and n = 2 (compounded semiannually means 2 times per year). Thus,

compound interest factor
$$= \left(1 + \frac{0.08}{2}\right)^{2 \cdot 10}$$

or $\left(1 + \frac{0.08}{2}\right)^{20}$
To evaluate, press the keys
 $\left(1 + 0.08 \div 2\right) \times x$ or $\land 20$ then $=$ or ENTER
The display will read 2.1911231 . Rounded to 5 decimal
places, this is 2.19112.

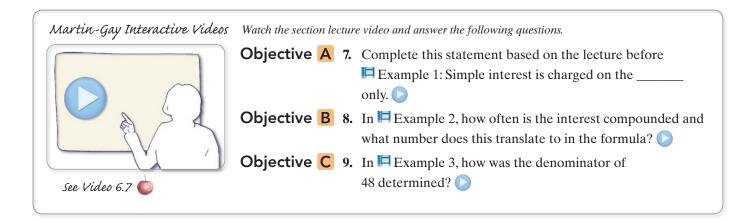
Find the compound interest factors. Use the table in Appendix A.7 to check your answers. For Exercises 1–4, round to 5 decimal places. For Exercises 5 and 6, round to 2 decimal places.

- 1. 5 years, 9%, compounded quarterly
- 2. 15 years, 14%, compounded daily
- 3. 20 years, 11%, compounded annually
- 4. 1 year, 7%, compounded semiannually
- 5. Find the total amount after 4 years when \$500 is invested at 6% compounded quarterly. (Multiply the appropriate compound interest factor by \$500.)
- 6. Find the total amount for 19 years when \$2500 is invested at 5% compounded daily.

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Choices may be used more than once.

- total amount simple principal amount compound
- **1.** To calculate ______ interest, use $I = P \cdot R \cdot T$.
- 2. To calculate _____ interest, use $A = P\left(1 + \frac{r}{n}\right)^{n \cdot t}$.
- **3.** ______ interest is computed not only on the original principal, but also on interest already earned in previous compounding periods.
- 4. When interest is computed on the original principal only, it is called ______ interest.
- **5.** _____ (paid or received) = principal + interest.
- 6. The ______ is the money borrowed, loaned, or invested.



6.7 Exercise Set MyLab Math

Objective A *Find the simple interest. See Examples 1 and 2.*

| | Principal | Rate | Time |
|----|-----------|-------|----------------------|
| 1. | \$200 | 8% | 2 years |
| 3. | \$160 | 11.5% | 4 years |
| 5. | \$5000 | 10% | $1\frac{1}{2}$ years |
| 7. | \$375 | 18% | 6 months |
| 9. | \$2500 | 16% | 21 months |

Solve. See Examples 1 through 3.

- 11. A company borrows \$162,500 for 5 years at a simple interest rate of 12.5%. Find the interest paid on the loan and the total amount paid back.
 - **13.** A money market fund advertises a simple interest rate of 9%. Find the total amount received on an investment of \$5000 for 15 months.

| | Principal | Rate | Time |
|-----|-----------|-------|----------------------|
| 2. | \$800 | 9% | 3 years |
| 4. | \$950 | 12.5% | 5 years |
| 6. | \$1500 | 14% | $2\frac{1}{4}$ years |
| 8. | \$775 | 15% | 8 months |
| 10. | \$1000 | 10% | 18 months |

- **12.** \$265,000 is borrowed to buy a house. If the simple interest rate on the 30-year loan is 8.25%, find the interest paid on the loan and the total amount paid back.
- **14.** The Real Service Company takes out a 270-day (9-month) short-term, simple interest loan of \$4500 to finance the purchase of some new equipment. If the interest rate is 14%, find the total amount that the company pays back.

- **15.** A 25-year-old is given a college graduation gift of \$5000. If this money is invested at 2% simple interest for 4 years, find the total amount.
- **16.** An 18-year-old is given a high school graduation gift of \$2000. If this money is invested at 8% simple interest for 5 years, find the total amount.

18. \$2060 is compounded annually at a rate of 15% for

20. \$1450 is compounded guarterly at a rate of 10% for

24. \$6375 is compounded semiannually at a rate of 10%

26. \$2000 is compounded semiannually at a rate of 8%

30. Jim Tillman borrows \$1800 for 9 months. If the inter-

28. \$2000 is compounded daily at a rate of 8% for

est is \$148.90, find his monthly payment.

32. \$105,000 is borrowed for 15 years. If the interest

on the loan is \$181,125, find the monthly

22. \$3500 is compounded daily at a rate of 8% for

10 years.

15 years.

10 years.

for 1 year.

for 5 years.

5 years.

payment.

Objective B Find the total amount in each compound interest account. See Examples 4 and 5.

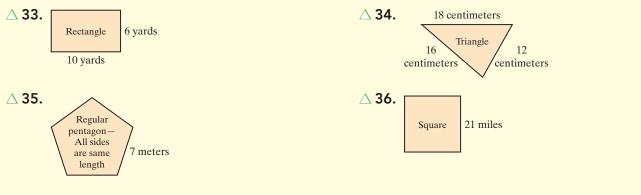
- ▶ 17. \$6150 is compounded semiannually at a rate of 14% for 15 years.
 - **19.** \$1560 is compounded daily at a rate of 8% for 5 years.
 - **21.** \$10,000 is compounded semiannually at a rate of 9% for 20 years.
 - **23.** \$2675 is compounded annually at a rate of 9% for 1 year.
 - **25.** \$2000 is compounded annually at a rate of 8% for 5 years.
 - **27.** \$2000 is compounded quarterly at a rate of 8% for 5 years.

Objective C Solve. See Example 6.

- **29.** A college student borrows \$1500 for 6 months to pay for a semester of school. If the interest is \$61.88, find the monthly payment.
- ▶ 31. \$20,000 is borrowed for 4 years. If the interest on the loan is \$10,588.70, find the monthly payment.

Review

Find the perimeter of each figure. See Section 1.3.



Concept Extensions

- > 37. Explain how to look up a compound interest factor > 38. Explain how to find the amount of interest in a comin the compound interest table.
- pounded account.
- **39.** Compare the following accounts: Account 1: \$1000 is invested for 10 years at a simple interest rate of 6%. Account 2: \$1000 is compounded semiannually at a rate of 6% for 10 years. Discuss how the interest is computed for each account. Determine which account earns more interest. Why?

Chapter 6 Group Activity

Fastest-Growing Occupations

According to U.S. Bureau of Labor Statistics projections, the careers listed below are the top ten fastest-growing jobs ranked by expected percent of increase through the year 2024. (*Source:* Bureau of Labor Statistics)

| \bigcap | Occupation | Employment in 2014 | Percent of Increase | Expected Employment in 2024 |
|-----------|---|--------------------|---------------------|-----------------------------|
| 1 | Wind turbine technician | 4400 | 108% | |
| 2 | Occupational therapy assistants and aides | 41,900 | 40% | |
| 3 | Physical therapist assistants and aides | 128,700 | 40% | |
| 4 | Home health aides | 913,500 | 38% | |
| 5 | Commercial divers | 3450 | 37% | |
| 6 | Nurse practitioners | 170,400 | 35% | |
| 7 | Physical therapists | 210,900 | 34% | |
| 8 | Statisticians | 30,000 | 34% | |
| 9 | Ambulance drivers and attendants but not EMTs | 19,950 | 33% | |
| 10 | Physician assistants | 94,400 | 30% | |

What do most of these fast-growing occupations have in common? They require knowledge of math! For some careers, such as nurse practitioners, and statisticians, the ways math is used on the job may be obvious. For other occupations, the use of math may not be quite as apparent. However, tasks common to many jobs—filling in a time sheet, writing up an expense or mileage report, planning a budget, figuring a bill, ordering supplies, and even making a work schedule—all require math.

This activity may be completed by working in groups or individually.

1. List the top five occupations by order of employment figures for 2014.

- **2.** Using the 2014 employment figures and the percent of increase from 2014 to 2024, find the expected 2024 employment figure for each occupation listed in the table. Round to the nearest hundred.
- **3.** List the top five occupations by order of employment figures for 2024. Did the order change at all from 2014? Explain.

Chapter 6 Vocabulary Check

Fill in each blank with one of the words or phrases listed below. Some choices may be used more than once.

| | percent | sales tax | is | 0.01 | $\frac{1}{100}$ | amount of discount | percent of decrease | total price |
|----|-----------|--------------|----------|------|-------------------|------------------------|---------------------|-------------|
| | base | of | amount | 100% | compound interest | percent of increase | sale price | commission |
| 1. | In a math | ematical sta | itement, | | usually m | eans "multiplication." | | |
| 2. | In a math | ematical sta | atement, | | means "ec | quals." | | |

3. _____ means "per hundred."

4. ______ is computed not only on the principal, but also on interest already earned in previous compounding periods.

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Chapter 6 | Percent

| 5. | In the percent proportion, = $\frac{\text{percent}}{100}$. | |
|-----|--|------------|
| 6. | To write a decimal or fraction as a percent, multiply by | |
| 7. | The decimal equivalent of the % symbol is | |
| 8. | The fraction equivalent of the % symbol is | _ · |
| 9. | The percent equation is \cdot percent = | |
| 10. | $\underline{\qquad} = \frac{\text{amount of decrease}}{\text{original amount}}.$ | |
| 11. | $\underline{\qquad} = \frac{\text{amount of increase}}{\text{original amount}}.$ | |
| 12. | $_$ = tax rate · purchase price. | |
| 13. | = purchase price + sales tax. | |
| 14. | $_$ = commission rate \cdot sales. | |
| 15. | $_$ = discount rate · original price. | |
| 16. | = original price – amount of discount. | |
| | | Helpf |

Helpful Hint

To help, don't forget to take these:

- Chapter 6 Getting Ready for the Test on page 435
- Chapter 6 Test on page 436

Then check all of your answers at the back of this text. For further review, the step-by-step video solutions to any of these exercises are located in MyLab Math.

6

Chapter Highlights

| Definitions and Concepts | Examples | | |
|--|---|--|--|
| Section 6.1 Intro | duction to Percent | | |
| Percent means "per hundred." The % symbol denotes percent. | $51\% = \frac{51}{100}$ 51 per 100 | | |
| To write a percent as a decimal, replace the % symbol with its decimal equivalent, 0.01, and multiply.
To write a decimal as a percent, multiply by 100%. | $7\% = \frac{7}{100} 7 \text{ per } 100$
32% = 32(0.01) = 0.32
0.08 = 0.08(100%) = 0.8.% = 8% | | |
| Section 6.2 Percents and Fractions | | | |
| To write a percent as a fraction, replace the % symbol
with its fraction equivalent, $\frac{1}{100}$, and multiply. | $25\% = \frac{25}{100} = \frac{\frac{25}{25}}{4 \cdot 25} = \frac{1}{4}$ | | |
| To write a fraction as a percent, multiply by 100%. | $\frac{1}{6} = \frac{1}{6} \cdot 100\% = \frac{1}{6} \cdot \frac{100}{1}\% = \frac{100}{6}\% = 16\frac{2}{3}\%$ | | |

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| Definitions and Concepts | Examples |
|--|---|
| Section 6.3 Solving Perc | ent Problems Using Equations |
| Three key words in the statement of a percent problem
are
of, which means multiplication (•)
is, which means equals (=)
what (or some equivalent word or phrase), which
stands for the unknown number | Solve:
$ \begin{array}{ccccccccccccccccccccccccccccccccccc$ |
| Section 6.4 Solving Perce | nt Problems Using Proportions |
| Percent Proportion | Solve: |
| $\frac{\text{amount}}{\text{base}} = \frac{\text{percent}}{100} \leftarrow \text{always 100}$ or $\frac{\text{amount} \rightarrow a}{\text{base} \rightarrow b} = \frac{p}{100} \leftarrow \text{percent}$ | 20.4 is what percent of 85?
amount percent base
amount $\rightarrow \frac{20.4}{85} = \frac{p}{100} \leftarrow \text{percent}$
$20.4 \cdot 100 = 85 \cdot p$ Set cross products equal.
$2040 = 85 \cdot p$ Multiply.
$\frac{2040}{85} = p$ Divide 2040 by 85, the number
multiplied by p.
24 = p Simplify. |
| | Thus, 20.4 is 24% of 85. |
| Section 6.5 Ap | plications of Percent |
| Percent of Increase
percent of increase $= \frac{\text{amount of increase}}{\text{original amount}}$
Percent of Decrease
percent of decrease $= \frac{\text{amount of decrease}}{\text{original amount}}$ | A town's population of 16,480 decreased to 13,870 over
a 12-year period. Find the percent of decrease. Round to
the nearest whole percent.
amount of decrease = 16,480 - 13,870
= 2610
percent of decrease = $\frac{\text{amount of decrease}}{\text{original amount}}$
= $\frac{2610}{16,480} \approx 0.16$
= 16% |
| | The town's population decreased by 16%. |
| Section 6.6 Percent and Problem Sol | ving: Sales Tax, Commission, and Discount |
| Sales Tax and Total Price
sales tax = sales tax rate • purchase price
total price = purchase price + sales tax | Find the sales tax and the total price on a purchase of \$42
if the sales tax rate is 9%.
sales tax = sales tax rate \cdot purchase price
$\downarrow \qquad \downarrow \qquad \downarrow \qquad \downarrow$
sales tax = 9% \cdot \$42
$= 0.09 \cdot 42
= \$3.78 |

| Definitions and Concepts | Examples |
|--|---|
| Section 6.6 Percent and Problem Solving: Section 6.6 | ales Tax, Commission, and Discount (continued) |
| Commission
commission = commission rate \cdot total sales | The total price is
total price = purchase price + sales tax
\downarrow \downarrow \downarrow
total price = \$42 + \$3.78
= \$45.78
A salesperson earns a commission of 3%. Find the commission from sales of \$12,500 worth of appliances.
commission = commission rate \cdot sales
\downarrow \downarrow \downarrow \downarrow
commission = 3% \cdot \$12,500
= 0.03 \cdot \$12,500 |
| Discount and Sale Price
amount of discount = discount rate • original price
sale price = original price – amount of discount | = \$375 A suit is priced at \$320 and is on sale today for 25% of
What is the sale price? $\begin{array}{cccccccccccccccccccccccccccccccccccc$ |
| | The sale price is \$240. |
| Simple Interest
interest = principal \cdot rate \cdot time
where the rate is understood to be per year. | Problem Solving: Interest Find the simple interest after 3 years on \$800 at an interest est rate of 5%.interest = principal \cdot rate \cdot time \downarrow <t< td=""></t<> |
| Compound interest is computed not only on the principal, but also on interest already earned in previous compounding periods. (SeeAppendix A7 for various compound interest factors.)
$A = P\left(1 + \frac{r}{n}\right)^{n \cdot t}$ where <i>n</i> is the number of times compounded per year. | The interest is \$120.
\$800 is invested at 5% compounded quarterly for
10 years. Find the total amount at the end of 10 years.
$A = \$800 \left(1 + \frac{0.05}{4}\right)^{4 \cdot 10}$ $= \$800 (1.0125)^{40}$ $\approx \$1314.90$ |

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Chapter 6 Review

(6.1) Solve.

| (0.1) Source. | | | | | | |
|--|--|---|--------------------------|--|--|--|
| 1. In a survey of 100 adults their pizzas. What percent | s, 37 preferred pepperoni on nt preferred pepperoni? | 2. A basketball player made 77 out of 100 attempted free throws. What percent of free throws was made? | | | | |
| Write each percent as a decim | al. | | | | | |
| 3. 83% | 4. 75% | 5. 3.5% | 6. 1.5% | | | |
| 7. 125% | 8. 145% | 9. 0.5% | 10. 0.7% | | | |
| 11. 200% | 12. 400% | 13. 26.25% | 14. 85.34% | | | |
| Write each decimal as a perce | nt. | | | | | |
| 15. 2.6 | 16. 1.02 | 17. 0.35 | 18. 0.055 | | | |
| 19. 0.725 | 20. 0.252 | 21. 0.076 | 22. 0.085 | | | |
| 23. 0.71 | 24. 0.65 | 25. 4 | 26. 9 | | | |
| (6.2) Write each percent as a | a fraction or mixed number in s | implest form. | | | | |
| 27. 1% | 28. 10% | 29. 25% | 30. 8.5% | | | |
| 31. 10.2% | 32. $16\frac{2}{3}\%$ | 33. $33\frac{1}{3}\%$ | 34. 110% | | | |
| Write each fraction or mixed number as a percent. | | | | | | |
| 35. $\frac{1}{5}$ | 36. $\frac{7}{10}$ | 37. $\frac{5}{6}$ | 38. $\frac{3}{5}$ | | | |
| 39. 1 ¹ / ₄ | 40. $1\frac{2}{3}$ | 41. $\frac{1}{16}$ | 42. $\frac{5}{8}$ | | | |

432 Chapter 6 | Percent (6.3) Translate each to an equation and solve. **44.** What number is $33\frac{1}{3}\%$ of 24,000? **43.** 1250 is 1.25% of what number? **46.** 22.9 is 20% of what number? **45.** 124.2 is what percent of 540? **47.** What number is 40% of 7500? **48.** 693 is what percent of 462? (6.4) Translate each to a proportion and solve. **49.** 104.5 is 25% of what number? **50.** 16.5 is 5.5% of what number? **51.** What number is 36% of 180? **52.** 63 is what percent of 35? **53.** 93.5 is what percent of 85? **54.** What number is 33% of 500?

- (6.5) Solve.
- **55.** In a survey of 2000 people, it was found that 1320 have a microwave oven. Find the percent of people who own microwaves.
- **57.** The number of violent crimes in a city decreased from 675 to 534. Find the percent of decrease. Round to the nearest tenth of a percent.
- **59.** This year the fund drive for a charity collected \$215,000. Next year, a 4% decrease is expected. Find how much is expected to be collected in next year's drive.
- (6.6) Solve.
- **61.** If the sales tax rate is 9.5%, what is the total amount charged for a \$250 coat?

- **56.** Of the 12,360 freshmen entering County College, 2000 are enrolled in basic college mathematics. Find the percent of entering freshmen who are enrolled in basic college mathematics. Round to the nearest whole percent.
- **58.** The current charge for dumping waste in a local landfill is \$16 per cubic foot. To cover new environmental costs, the charge will increase to \$33 per cubic foot. Find the percent of increase.
- **60.** A local union negotiated a new contract that increases the hourly pay 15% over last year's pay. The old hourly rate was \$11.50. Find the new hourly rate rounded to the nearest cent.
- **62.** Find the sales tax paid on a \$32 purchase if the sales tax rate is 10.5%.

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Chapter 6 Review

- **63.** Russ James is a sales representative for a chemical company and is paid a commission rate of 5% on all sales. Find his commission if he sold \$100,000 worth of chemicals last month.
- **65.** A \$3000 mink coat is on sale for 30% off. Find the discount and the sale price.
- (6.7) Solve.
- **67.** Find the simple interest due on \$4000 loaned for 4 months at 12% interest.
- **69.** Find the total amount in an account if \$5500 is compounded annually at 12% for 15 years.
- **71.** Find the total amount in the account if \$100 is compounded quarterly at 12% for 5 years.

- **64.** Carol Sell is a sales clerk in a clothing store. She receives a commission of 7.5% on all sales. Find her commission for the week if her sales for the week were \$4005. Round to the nearest cent.
- **66.** A \$90 calculator is on sale for 10% off. Find the discount and the sale price.
- **68.** Find the simple interest due on \$6500 loaned for 3 months at 20%.
- **70.** Find the total amount in an account if \$6000 is compounded semiannually at 11% for 10 years.
- **72.** Find the total amount in the account if \$1000 is compounded quarterly at 18% for 20 years.

Mixed Review

| Write each percent as a decimal. | | |
|----------------------------------|------------------|-----------------|
| 73. 3.8% | 74. 24.5% | 75. 0.9% |
| | | |
| Write each decimal as a percent. | | |
| 76. 0.54 | 77. 95.2 | 78. 0.3 |
| | | |
| | | |

Write each percent as a fraction or mixed number in simplest form.

79. 47% **80.** $6\frac{2}{5}$ % **81.** 5.6%

Write each fraction or mixed number as a percent.

82. $\frac{3}{8}$ **83.** $\frac{2}{13}$ **84.** $\frac{6}{5}$

434 Chapter 6 | Percent

- Translate each into an equation and solve.
- **85.** 43 is 16% of what number?
- **87.** What number is 36% of 1968?

Translate each into a proportion and solve.

- **89.** 75 is what percent of 25?
- **91.** 28 is 5% of what number?
- Solve.
- **93.** The total number of cans in a soft drink machine is 300. If 78 soft drinks have been sold, find the percent of soft drink cans that have been sold.
- **95.** A used printer sells for \$568.00. If the sales tax rate is 8.75%, find the purchase price of the printer.
- 97. A regional candy salesman makes a commission of \$1.60 from each case of candy he sells. If a case of candy costs \$12.80, what is his rate of commission?
- **99.** \$8800 is invested at 8% interest compounded quarterly. Find the total amount after 9 years.

- **94.** A home valued at \$96,950 last year has lost 7% of its value this year because of flooding. Find the loss in value.
- **96.** The original price to buy and download of a video game is \$63.00. It is on sale for 15% off. What is the amount of the discount?
- **98.** Find the total amount due on a 6-month loan of \$1400 at a simple interest rate of 13%.
- **100.** Find the total amount due on a loan of \$5500 for 9 years at 12.5% simple interest.

- **86.** 27.5 is what percent of 25?
- **88.** 67 is what percent of 50?
- **90.** What number is 16% of 240?
- **92.** 52 is what percent of 16?

Getting Ready for the Test

Chapter 6

| | | an halam an Mall | la Chaina Characht | |
|---|---|-----------------------------------|-------------------------------|--------------------|
| | DICE All of the exercise | - | | |
| - | ent" means "per hundr | | iber that does <i>not</i> equ | al 12%. |
| A. $\frac{12}{100}$ | B. 0.12 | C. $\frac{3}{25}$ | D. 1.2 | |
| | number that does not | 25 | | |
| A. 10 | B. 1 | C. 1.00 | D. $\frac{100}{100}$ | |
| 3 . Choose the | number that does not | equal 50%. | | |
| A. 0.5 | B. 5 | C. $\frac{1}{2}$ | D. $\frac{50}{100}$ | |
| 4 . Choose the | number that does not | equal 80%. | | |
| A. 0.80 | B. 0.8 | C. 8 | D. $\frac{4}{5}$ | |
| 25% of a nu 10% of a nu | mber is half that number is $\frac{1}{4}$ of that number is $\frac{1}{10}$ of tha | ber.
nber. | | |
| | hrough 8, choose the le | | | |
| A. 100% ○ 5. | B. 50% | C. 25% | D. 10% | |
| • 6 | | | | |
| • • • · · | | | | |
| • 7
• 8 | | | | |
| • • | 01 20 13 7. | | | |
| For Exercise 9, c | hoose the correct letter | : | | |
| | a restaurant is \$24.86.
B. \$20 | - | | mount is closest t |
| For Exercises 10 | and 11, an amount of | \$150 is to be discour | <i>ited by 10%.</i> | |
| ● 10. Find the am
A. \$15 | nount of discount.
B. \$45 | C. \$30 | D. \$10 | |
| • 11. Find the ne A. \$120 | w discounted price (or
B. \$10 | riginal price – disco
C. \$140 | ount).
D. \$135 | |
| For Exercise 12. | choose the correct lette | 21. | | |
| | al price of a pair of sh | | noe price is to be disco | ounted by 25% at |
| | | | 1 | 5 |

12. If the original price of a pair of shoes is \$40 and the shoe price is to be discounted by 25% at the register, choose the closest amount for your shoes before tax.

| А. | \$10 | B. \$20 | C. \$30 | D. \$40 |
|----|------|----------------|----------------|----------------|
| | | | | |

to 20%?

| Chapter 6 | Test MyLab Math or You Tube | For additional practice go to your study plan in MyLab Math. |
|------------|---|--|
| Answers | Write each percent as a decimal. | |
| | ○ 1. 85% ○ 2. 500% | 3. 0.8% |
| | | |
| | Write each decimal as a percent. | |
| 1. | • 4. 0.056 • 5. 6.1 | 6. 0.39 |
| 2. | | |
| 3. | | |
| 4. | Write each percent as a fraction or mixed n | umber in simplest form. |
| 5. | 07. 120% 08. 38.5% | 9. 0.2% |
| 6. | | |
| 7. | | |
| 8. | Write each fraction or mixed number as a p | |
| 9. | • 10. $\frac{11}{20}$ • 11. $\frac{3}{8}$ | • 12. $1\frac{5}{9}$ |
| 10. | | |
| <u>11.</u> | | |
| 12. | <i>Solve.</i> • 13. What number is 42% of 80? | • 14. 0.6% of what number is 7.5? |
| 13. | • 10. what humber is 42 /0 01 00? | |
| 14. | | |
| 15. | 15. 567 is what percent of 756? | |
| | • ••• oor is what percent of 750. | |

Chapter 6 Test

16.

● **16.** An alloy is 12% copper. How much **17.** A farmer in Nebraska estimates that copper is contained in 320 pounds of 20% of his potential crop, or \$11,350, this alloy? has been lost to a hard freeze. Find the total value of his potential crop. 17. 18. ● **18.** If the local sales tax rate is 1.25%, **19.** A town's population increased from 25,200 to 26,460. Find the percent of find the total amount charged for a stereo system priced at \$354. increase. 19. 20. **20.** A \$120 framed picture is on sale for **21.** Randy Nguyen is paid a commission 15% off. Find the discount and the rate of 4% on all sales. Find Randy's commission if his sales were \$9875. sale price. 21. 22. **22.** A sales tax of \$1.53 is added to an **23.** Find the simple interest earned on item's price of \$152.99. Find the sales \$2000 saved for $3\frac{1}{2}$ years at an intertax rate. Round to the nearest whole percent. est rate of 9.25%. 23. 24. ● **24.** \$1365 is compounded annually at 8%. **25.** A couple borrowed \$400 from a bank at 13.5% simple interest for 6 months Find the total amount in the account for car repairs. Find the total amount after 5 years. due the bank at the end of the 6-month 25. period.

Solve. Round all dollar amounts to the nearest cent.

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Chapters 1–6

Cumulative Review

Answers

| 1. |
|-------------|
| 2. |
| 3. a. |
| b. |
| c. |
| |
| <u>4.a.</u> |
| b. |
| C. |
| 5. |
| 6. |
| 7. |
| 8. |
| 9. |
| 10. |
| |
| <u>11.</u> |
| 12. |
| 13. |
| 14. |
| 15. |
| 16. |
| 17. |
| 18. |
| 19. |
| 20. |
| 21. |
| 22. |
| 438 |
| |

- 1. How many cases can be filled with 9900 cans of jalapeños if each case holds 48 cans? How many cans will be left over? Will there be enough cases to fill an order for 200 cases?
- **3.** Write each fraction as a mixed number or a whole number.

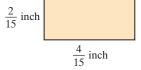
| 30 | 16 | 84 |
|------|---------------------------|---------------------|
| a. — | b. $\frac{15}{15}$ | c . <u>6</u> |

5. Use a factor tree to find the prime factorization of 80.

7. Write in simplest form: $\frac{10}{27}$

- **9.** Multiply and simplify: $\frac{23}{32} \cdot \frac{4}{7}$
- **11.** Find the reciprocal of $\frac{11}{8}$.

 \triangle **13.** Find the perimeter of the rectangle.



- **15.** Find the LCM of 12 and 20.
- **17.** Add: $\frac{2}{5} + \frac{4}{15}$

19. Subtract: $7\frac{3}{14} - 3\frac{6}{7}$

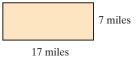
Perform each indicated operation.

21. $\frac{1}{2} \div \frac{8}{7}$

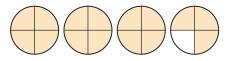
- **2.** Multiply: 409×76
- **4.** Write each mixed number as an improper fraction.

a.
$$2\frac{5}{7}$$
 b. $10\frac{1}{10}$ **c.** $5\frac{3}{8}$

 \triangle **6.** Find the area of the rectangle.



- **8.** Find the average of 28, 34, and 70.
- **10.** Round 76,498 to the nearest ten.
- **12.** Write the shaded part of the figure as an improper fraction and as a mixed number.



- **14.** Find $2 \cdot 5^2$
- **16.** Subtract $\frac{7}{9}$ from $\frac{10}{9}$. **18.** Find $\frac{2}{3}$ of 510.
- **20.** Simplify: $9 \cdot \sqrt{25} 6 \cdot \sqrt{4}$
- **22.** $20\frac{4}{5} + 12\frac{7}{8}$

23.
$$\frac{2}{9} \cdot \frac{3}{11}$$
 24. $1\frac{7}{8} \cdot 3\frac{2}{5}$

Write each fraction as a decimal.

| 25. $\frac{8}{10}$ 26. $\frac{9}{100}$ | 27. $\frac{87}{10}$ | 28. $\frac{48}{10,000}$ |
|---|-----------------------------------|---|
| 29. The price of a gallon of premiu line in Cross City is currently \$ Round this to the nearest cent. | 3.1779. | 38 - 10.06 |
| 31. Add: 763.7651 + 22.001 + 4 | 3. 89 32. Multiply: | 12.483 × 100 |
| 33. Multiply: 23.6×0.78 | 34. Multiply: | 76.3×1000 |
| Divide. | | |
| 35. $\frac{786.1}{1000}$ | 36. 0.5)0.638 | |
| 37. $\frac{0.12}{10}$ | 38. 0.23)11.64 | 495 |
| 39. Simplify: 723.6 ÷ 1000 × 10 | 40. Simplify: | $\frac{3.19 - 0.707}{13}$ |
| 41. Write $\frac{1}{4}$ as a decimal. | | as a decimal. Give the exact
nd a three-decimal-place
nation. |

Write the rates in Exercises 43 and 44 as fractions in simplest form.

44. 115 miles every 5 gallons

46. Approximate each unit price and

\$0.93 for 18 flour tortillas

\$1.40 for 24 flour tortillas

48. Write each percent as a decimal.

50. Write $\frac{3}{8}$ as a percent.

a. 7% **b.** 200% **c.** 0.5%

decide on the better buy. Round the unit prices to three decimal places.

43. 10 nails every 6 feet

Solve.

45. Is
$$\frac{4.1}{7} = \frac{2.9}{5}$$
 a true proportion?

- **47.** On a chamber of commerce map of Abita Springs, 5 miles corresponds to 2 inches. How many miles correspond to 7 inches?
- **49.** Translate to an equation: What number is 25% of 0.008?

| 23. | | |
|-----|------|------|
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| 24. |
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| 25. | | |
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| 42. | | |
| 43. | | |
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| 44. | | |
| 45. | | |
| | | |

46. 47. 48. a. b. c. 49. 50.

7

The use of measurements is common in everyday life. A sales representative records the number of miles she has driven when she submits her travel expense report. A respiratory therapist measures the volume of air exhaled by a patient. A measurement is necessary in each case.

Sections

- 7.1 Length: U.S. and Metric Systems of Measurement
- 7.2 Weight and Mass: U.S. and Metric Systems of Measurement
- 7.3 Capacity: U.S. and Metric Systems of Measurement

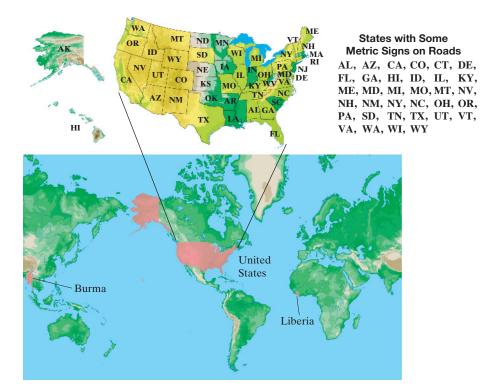
Integrated Review— Length, Weight, and Capacity

- 7.4 Conversions Between the U.S. and Metric Systems
- 7.5 Temperature: U.S. and Metric Systems of Measurement
- 7.6 Energy: U.S. and Metric Systems of Measurement

Check Your Progress

Vocabulary Check Chapter Highlights Chapter Review Getting Ready for the Test Chapter Test Cumulative Review

Measurement



What is SI? How Does SI Affect Me?

Stands for International System of Units, but you may know it as simply the metric system. There are only a few countries that have not completely converted to the metric system, and they are shown above. In 1975, the Congress passed the Metric Conversion Act. This act established the U.S. Metric Board to help plan the increasing and voluntary conversion to the metric system. In fact, every year the United States has a National Metric Week started by the National Council for Teachers of Mathematics (NCTM.) Look for this event every year during the week that contains October 10.

Metric system use is increasing in the United States. Take a moment and start noticing metric units around you. Throughout this chapter, we give examples of these.



(Source: U.S. Metric Association)

7.1 Length: U.S. and Metric Systems of Measurement

Objective A Defining and Converting U.S. System Units of Length

In the United States, two systems of measurement are commonly used. They are the **United States (U.S.), or English, measurement system** and the **metric system.** The U.S. measurement system is familiar to most Americans. Units such as feet, miles, ounces, and gallons are used. However, the metric system is also commonly used in fields such as medicine, sports, international marketing, and certain physical sciences. We are accustomed to buying 2-liter bottles of soft drinks, watching televised coverage of the 100-meter dash at the Olympic Games, or taking a 200-milligram dose of pain reliever.

The U.S. system of measurement uses the **inch**, **foot**, **yard**, and **mile** to measure **length**. The following is a summary of equivalencies between units of length:

U.S. Units of Length

12 inches (in.) = 1 foot (ft) 3 feet = 1 yard (yd) 36 inches = 1 yard 5280 feet = 1 mile (mi)

To convert from one unit of length to another, we will use **unit fractions.** We define a unit fraction to be a fraction that is equivalent to 1. Examples of unit fractions are as follows:

Unit Fractions

 $\frac{12 \text{ in.}}{1 \text{ ft}} = 1 \text{ or } \frac{1 \text{ ft}}{12 \text{ in.}} = 1 \text{ (since 12 in.} = 1 \text{ ft)}$ $\frac{3 \text{ ft}}{1 \text{ yd}} = 1 \text{ or } \frac{1 \text{ yd}}{3 \text{ ft}} = 1 \text{ (since 3 ft = 1 yd)}$ $\frac{5280 \text{ ft}}{1 \text{ mi}} = 1 \text{ or } \frac{1 \text{ mi}}{5280 \text{ ft}} = 1 \text{ (since 5280 ft = 1 mi)}$

Remember that multiplying a number by 1 does not change the value of the number.

Example 1 Convert 8 feet to inches.

Solution: We multiply 8 feet by a unit fraction that uses the equality 12 inches = 1 foot. The unit fraction should be in the form $\frac{\text{units to convert to}}{\text{original units}}$ or, in this case, $\frac{12 \text{ inches}}{1 \text{ foot}}$. We do this so that like units will divide out to 1, as shown.

$$8 \text{ ft} = \frac{8 \text{ ft}}{1} \cdot 1$$

$$= \frac{8 \text{ ft}}{1} \cdot \frac{12 \text{ in.}}{1 \text{ ft}}$$
Multiply by 1 in the form of $\frac{12 \text{ in.}}{1 \text{ ft}}$

$$= 8 \cdot 12 \text{ in.}$$

$$= 96 \text{ in.}$$
Multiply.

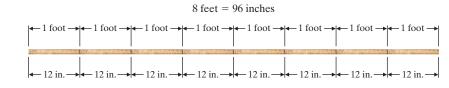
Objectives

- A Define U.S. Units of Length and Convert from One Unit to Another.
- B Use Mixed U.S. Units of Length.
- C Perform Arithmetic Operations on U.S. Units of Length.
- Define Metric Units of Length and Convert from One Unit to Another.
- E Perform Arithmetic Operations on Metric Units of Length.

Practice 1 Convert 6 feet to inches.

(Continued on next page)

Answer 1. 72 in. Thus, 8 ft = 96 in., as shown in the diagram:



Work Practice 1



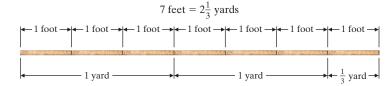
Convert 7 feet to yards.

Solution: We multiply by a unit fraction that compares 1 yard to 3 feet.

7 ft =
$$\frac{7 \text{ ft}}{1} \cdot 1$$

= $\frac{7 \text{ ft}}{1} \cdot \frac{1 \text{ yd}}{3 \text{ ft}} \leftarrow \text{Units to convert to}$
= $\frac{7}{3} \text{ yd}$
= $2\frac{1}{3} \text{ yd}$ Divide.

Thus, 7 ft = $2\frac{1}{3}$ yd, as shown in the diagram.



Finding the Length of a Pelican's Bill

The Australian pelican has the longest bill, measuring from 13 to 18.5 inches long.

The pelican in the photo has a 15-inch bill. Convert 15 inches to feet, using decimals

Work Practice 2

in your final answer.

Example 3

Solution:

Practice 3

Suppose a pelican's bill measures 18 inches. Convert 18 inches to feet, using decimals.

Answers 2. 24 ft 3. 1.5 ft

When convert-

ing from one unit to another, select a unit fraction with the

units you are converting to original units By using this unit fraction,

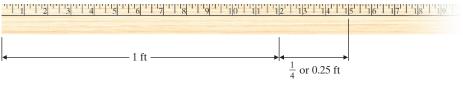
the original units will divide

$$15 \text{ in.} = \frac{15 \text{ jm.}}{1} \cdot \frac{1 \text{ ft}}{12 \text{ jm.}} \leftarrow \text{Units to convert to}$$
$$= \frac{15}{12} \text{ ft}$$
$$= \frac{5}{4} \text{ ft}$$
Simplify $\frac{15}{12}$.
$$= 1.25 \text{ ft}$$
Divide.



Thus, 15 in. = 1.25 ft, as shown in the diagram.

15 inches = 1.25 ft



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Practice 2

Helpful

Convert 8 yards to feet.

properties below:

out, as wanted.

Work Practice 3

Objective **B** Using Mixed U.S. System Units of Length 🕑

Sometimes it is more meaningful to express a measurement of length with mixed units such as 1 ft and 5 in. We usually condense this and write 1 ft 5 in.

In Example 2, we found that 7 feet is the same as $2\frac{1}{3}$ yards. The measurement can also be written as a mixture of yards and feet. That is,

$$7 \text{ ft} = __y \text{d} __f \text{t}$$

Because 3 ft = 1 yd, we divide 3 into 7 to see how many whole yards are in 7 feet. The quotient is the number of yards, and the remainder is the number of feet.

2 yd 1 ft 3)7 -6

Thus, 7 ft = 2 yd 1 ft, as seen in the diagram:



Example 4 Convert: 134 in. = _____ ft _____ in.

Solution: Because 12 in. = 1 ft, we divide 12 into 134. The quotient is the number of feet. The remainder is the number of inches. To see why we divide 12 into 134. notice that

$$134 \text{ in.} = \frac{134 \text{ in.}}{1} \cdot \frac{1 \text{ ft}}{12 \text{ in.}} = \frac{134}{12} \text{ ft}$$

$$111 \text{ ft } 2 \text{ in}$$

$$12\overline{)134}$$

$$-12$$

$$14$$

$$-12$$

$$2$$

Thus, 134 in. = 11 ft 2 in.

Work Practice 4

Example 5 Convert 3 feet 7 inches to inches.

Solution: First, we convert 3 feet to inches. Then we add 7 inches.

$$3 \text{ ft} = \frac{3 \text{ ft}}{1} \cdot \frac{12 \text{ in.}}{1 \text{ ft}} = 36 \text{ in.}$$

Then

$$3_{\uparrow}$$
 ft 7 in. = 36_{\uparrow} in. + 7 in. = 43 in.

Work Practice 5

Practice 4 Convert: 68 in. = _____ ft _____ in.

Practice 5 Convert 5 yards 2 feet to feet.

Answers 4. 5 ft 8 in. 5. 17 ft

Objective C Performing Operations on U.S. System Units of Length

Finding sums or differences of measurements often involves converting units, as shown in the next example. Just remember that, as usual, only like units can be added or subtracted.

Example 6 Add 3 ft 2 in. and 5 ft 11 in. **Solution:** To add, we line up the similar units. 3 ft 2 in. + 5 ft 11 in. 8 ft 13 in. Since 13 inches is the same as 1 ft 1 in., we have 8 ft 13 in. = 8 ft + 1 ft 1 in.= 9 ft 1 in.Work Practice 6 Concept Check How could you estimate the following sum? 7 yd 4 in. + 3 yd 27 in. **Example 7** Multiply 8 ft 9 in. by 3. **Solution:** By the distributive property, we multiply 8 ft by 3 and 9 in. by 3. 8 ft 9 in. × 3 24 ft 27 in. Since 27 in. is the same as 2 ft 3 in., we simplify the product as 24 ft 27 in. = 24 ft + 2 ft 3 in.= 26 ft 3 in. Work Practice 7 We divide in a similar manner as above.

Example 8 Finding the Length of a Piece of Rope

A rope of length 6 yd 1 ft has 2 yd 2 ft cut from one end. Find the length of the remaining rope.

Solution: Subtract 2 yd 2 ft from 6 yd 1 ft.

beginning length \rightarrow 6 yd 1 ft <u>- amount cut</u> \rightarrow <u>- 2 yd 2 ft</u> remaining length

We cannot subtract 2 ft from 1 ft, so we borrow 1 yd from the 6 yd. One yard is converted to 3 ft and combined with the 1 ft already there.

Practice 8

A carpenter cuts 1 ft 9 in. from a board of length 5 ft 8 in. Find the remaining length of the board.

Answers

6. 13 ft 7 in. 7. 18 ft 4 in. 8. 3 ft 11 in.

Concept Check Answer

round each to the nearest yard: 7 yd + 4 yd = 11 yd

Practice 7 Multiply 4 ft 7 in. by 4.

Add 4 ft 8 in. to 8 ft 11 in.

Practice 6

```
Borrow 1 yd = 3 ft

5 yd + 1 yd 3 ft

6 yd 1 ft = 5 yd 4 ft

-2 yd 2 ft = -2 yd 2 ft

3 yd 2 ft
```

The remaining rope is 3 yd 2 ft long.

Work Practice 8

Objective D Defining and Converting Metric System Units of Length D

The basic unit of length in the metric system is the **meter.** A meter is slightly longer than a yard. It is approximately 39.37 inches long. Recall that a yard is 36 inches long.

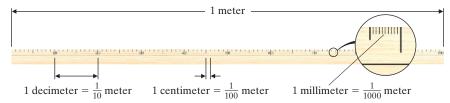
| 1 yard = 36 inches | |
|--|--|
| או איז אראר איז איז אראראריאריאריאריאריאריאריאריאריאריאריארי | |
| | |

1 meter \approx 39.37 inches

All units of length in the metric system are based on the meter. The following is a summary of the prefixes used in the metric system. Also shown are equivalencies between units of length. Like the decimal system, the metric system uses powers of 10 to define units.

| Metric Units of Length |
|---|
| 1 kilometer (km) = 1000 meters (m) |
| 1 hectometer (hm) = 100 m |
| 1 dekameter (dam) = 10 m |
| $1 \text{ meter } (\mathbf{m}) = 1 \text{ m}$ |
| 1 decimeter (dm) = 1/10 m or 0.1 m |
| 1 centimeter (cm) = 1/100 m or 0.01 m |
| 1 millimeter (mm) = 1/1000 m or 0.001 m |

The figure below will help you with decimeters, centimeters, and millimeters.



Helpful Hint

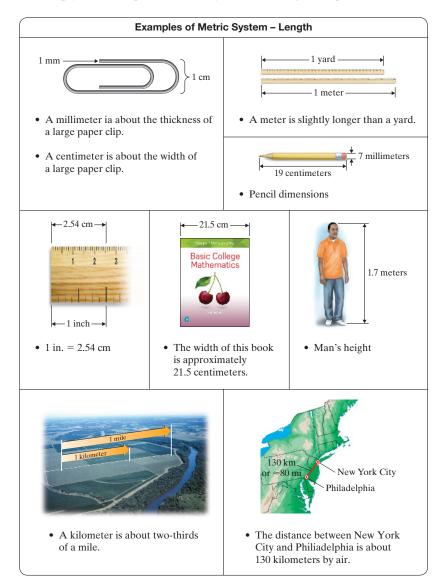
Study the figure above for other equivalencies between metric units of length.

10 decimeters = 1 meter10 millimeters = 1 centimeter100 centimeters = 1 meter10 centimeters = 1 decimeter1000 millimeters = 1 meter

These same prefixes are used in the metric system for mass and capacity. The most commonly used measurements of length in the metric system are the **meter**, **millimeter**, centimeter, and **kilometer**.

Concept Check Is this statement reasonable? "The screen of a home television set has a 30-meter diagonal." Why or why not?

Being comfortable with the metric units of length means gaining a "feeling" for metric lengths, just as you have a "feeling" for the lengths of an inch, a foot, and a mile. To help you accomplish this, study the following examples:

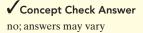


As with the U.S. system of measurement, unit fractions may be used to convert from one unit of length to another. For example, let's convert 1200 meters to kilometers. To do so, we will multiply by 1 in the form of the unit fraction

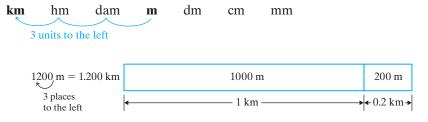
$$\frac{1 \text{ km}}{1000 \text{ m}} \leftarrow \text{Units to convert to}$$

$$1200 \text{ m} = \frac{1200 \text{ m}}{1} \cdot 1 = \frac{1200 \text{ m}}{1} \cdot \frac{1 \text{ km}}{1000 \text{ m}} = \frac{1200 \text{ km}}{1000} = 1.2 \text{ km}$$

The metric system does, however, have a distinct advantage over the U.S. system of measurement: the ease of converting from one unit of length to another. Since all units of length are powers of 10 of the meter, converting from one unit of length to another is as simple as moving the decimal point. Listing units of length in order from largest to smallest helps to keep track of how many places to move the decimal point. when converting.



Let's again convert 1200 meters to kilometers. This time, to convert from meters to kilometers, we move along the chart shown, 3 units to the left, from meters to kilometers. This means that we move the decimal point 3 places to the left.



Thus, 1200 m = 1.2 km, as shown in the diagram.

Example 9 Convert 2.3 m to centimeters.

Solution: First we will convert by using a unit fraction.

$$2.3 \text{ m} = \frac{2.3 \text{ m}}{1} \cdot \frac{100 \text{ cm}}{1 \text{ m}} = 230 \text{ cm}$$

Now we will convert by listing the units of length in order from left to right and moving from meters to centimeters.

km hm dam m dm cm mm 2 units to the right

2.30 m = 230. cm2 places to the right

With either method, we get 230 cm.

Work Practice 9

Example 10

Convert 450,000 mm to meters.

Solution: We list the units of length in order from left to right and move from millimeters to meters.

km hm dam m dm cm mm 3 units to the left

Thus, move the decimal point 3 places to the left.

450,000 mm = 450.000 m or 450 m

```
Work Practice 10
```

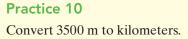
Concept Check What is wrong with the following conversion of 150 cm to meters?

150.00 cm = 15,000 m

Objective E Performing Operations on Metric System Units of Length 🕗

To add, subtract, multiply, or divide with metric measurements of length, we write all numbers using the same unit of length and then add, subtract, multiply, or divide as with decimals. Answers 9. 2500 mm 10. 3.5 km

Concept Check Answer decimal point should be moved two places to the left: 1.5 m



Practice 9 Convert 2.5 m to millimeters.

Chapter 7 | Measurement

Example 11

Subtract 430 m from 1.3 km.

Solution: First we convert both measurements to kilometers or both to meters.

| 430 m = 0.43 km | or | 1.3 km = 1300 m |
|-------------------|----|-------------------|
| 1.30 km | | 1300 m |
| <u>−0.43 km</u> ← | | <u>- 430 m</u> < |
| 0.87 km | | 870 m |

The difference is 0.87 km or 870 m.

Work Practice 11

Practice 12

Multiply 18.3 hm by 5.

Practice 13

A child was 55 centimeters at birth. Her adult height was 1.72 meters. Find how much she grew from birth to adult height.

Practice 14

A newly born male giraffe is 205 centimeters tall. If this male grows another 3.5 meters to adulthood, find the adult height of this giraffe.



Answers **11.** 1.46 km or 1460 m **12.** 91.5 hm **13.** 117 cm or 1.17 m 14. 555 cm or 5.55 m

Example 12 Multiply 5.7 mm by 4.

Solution: Here we simply multiply the two numbers. Note that the unit of measurement remains the same.

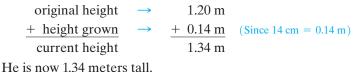


Work Practice 12

Example 13 Finding a Person's Height

A youth was 1.2 meters tall on his last birthday. Since then, he has grown 14 centimeters. Find his current height in meters.

Solution:



Work Practice 13

Example 14 Finding a Crocodile's Length

A newly hatched Nile crocodile averages 26 centimeters in length. This type of crocodile normally grows 4.74 meters to reach its adult length. What is the adult length of this type of crocodile?

Solution:

| original length | \rightarrow | 0.26 m | (since 26 cm | \rightarrow | 26 cm | (since 4.74 m |
|-----------------|---------------|----------|---------------|---------------|----------|---------------|
| + length grown | \rightarrow | + 4.74 m | = 0.26 m) or | \rightarrow | + 474 cm | = 474 cm) |
| adult length | | 5.00 m | | | 500 cm | |

The adult length is 5 meters or 500 centimeters.



Practice 11

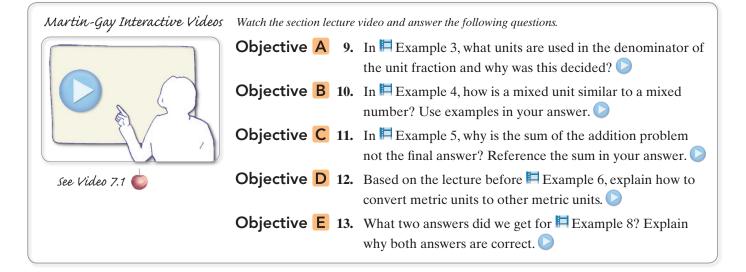
Subtract 640 m from 2.1 km.

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Some choices may be used more than once.

| inches | yard | unit fraction |
|--------|-------|---------------|
| feet | meter | |

- 1. The basic unit of length in the metric system is the _____
- **2.** The expression $\frac{1 \text{ foot}}{12 \text{ inches}}$ is an example of a(n) _____.
- **3.** A meter is slightly longer than a(n) _____
- **4.** One foot equals 12 _____
- **5.** One yard equals 3 _____.
- 6. One yard equals 36 _____
- **7.** One mile equals 5280 _____
- 8. One foot equals $\frac{1}{3}$ _____.



Exercise Set MyLab Math 7.1 **Objective A** *Convert each measurement as indicated. See Examples 1 through 3.* **1.** 60 in. to feet **2.** 84 in. to feet **3.** 12 yd to feet **4.** 18 yd to feet • 7. $8\frac{1}{2}$ ft to inches 8. $12\frac{1}{2}$ ft to inches **5.** 42,240 ft to miles **6.** 36,960 ft to miles **9.** 10 ft to yards **10.** 25 ft to yards **11.** 6.4 mi to feet **12.** 3.8 mi to feet **13.** 162 in. to yd (Write 14. 7216 yd to mi (Write **15.** 3 in. to ft (Write **16.** 129 in. to ft (Write answer as a decimal.) answer as a decimal.) answer as a decimal.) answer as a decimal.)

| Objective B Convert each measurer | nent as indicated. See Examples 4 and 5 | |
|--|---|-------------------------------------|
| 17. 40 ft = yd ft | 18. 100 ft = yd ft | 19. 85 in. = ft in. |
| 20. 47 in. = ft in. | 21. 10,000 ft = mi ft | 22. 25,000 ft = mi ft |
| 23. 5 ft 2 in. = in. | 24. 6 ft 10 in. = in. | 25. 8 yd 2 ft = ft |
| 26. 4 yd 1 ft = ft | 27. 2 yd 1 ft = in. | 28. 1 yd 2 ft = in. |
| Objective C Perform each indicated | l operation. Simplify the result if possibl | e. See Examples 6 through 8. |
| 29. 3 ft 10 in. + 7 ft 4 in. | 30. 12 ft 7 in. + 9 ft 11 in. | • 31. 12 yd 2 ft + 9 yd 2 ft |
| 32. 16 yd 2 ft + 8 yd 2 ft | 33. 22 ft 8 in. – 16 ft 3 in. | 34. 15 ft 5 in. – 8 ft 2 in. |
| 35. 18 ft 3 in. – 10 ft 9 in. | 36. 14 ft 8 in. – 3 ft 11 in. | 37. 28 ft 8 in. ÷ 2 |
| 38. 34 ft 6 in. ÷ 2 | 39. 16 yd 2 ft × 5 | 40. 15 yd 1 ft × 8 |
| Objective D Convert as indicated. S | ee Examples 9 and 10. | |
| 41. 60 m to centimeters | 42. 46 m to centimeters | 43. 40 mm to centimeters |
| 44. 14 mm to centimeters | 45. 500 m to kilometers | 46. 400 m to kilometers |
| 47. 1700 mm to meters | 48. 6400 mm to meters | • 49. 1500 cm to meters |
| 50. 6400 cm to meters | 51. 0.42 km to centimeters | 52. 0.95 km to centimeters |
| 53. 7 km to meters | 54. 5 km to meters | 55. 8.3 cm to millimeters |
| 56. 4.6 cm to millimeters | 57. 20.1 mm to decimeters | 58. 140.2 mm to decimeters |
| 59. 0.04 m to millimeters | 60. 0.2 m to millimeters | |

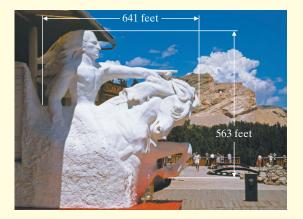
Objective E *Perform each indicated operation. Remember to insert units when writing your answers. See Examples 11 through 14.*

| 61. 8.6 m + 0.34 m | 62. 14.1 cm + 3.96 cm | 63. 2.9 m + 40 mm |
|---------------------------|--------------------------------|------------------------------|
| 64. 30 cm + 8.9 m | ● 65. 24.8 mm − 1.19 cm | 66. 45.3 m – 2.16 dam |
| 67. 15 km – 2360 m | 68. 14 cm – 15 mm | 69. 18.3 m × 3 |
| 70. 14.1 m × 4 | 71. 6.2 km ÷ 4 | 72. 9.6 m ÷ 5 |

Objectives A C D E Mixed Practice Solve. Remember to insert units when writing your answers. For Exercises 73 through 82, complete the charts. See Examples 1 through 14.

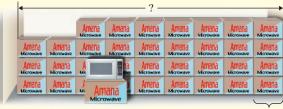
| | | Yards | Feet | Inches |
|-----|------------------------------------|-------|------|--------|
| 73. | Chrysler Building in New York City | | 1046 | |
| 74. | 4-story building | | | 792 |
| 75. | Python length | | 35 | |
| 76. | Ostrich height | | | 108 |

| | | Meters | Millimeters | Kilometers | Centimeters |
|-----|---------------------------------|--------|-------------|------------|-------------|
| 77. | Length of elephant | 5 | | | |
| 78. | Height of grizzly bear | 3 | | | |
| 79. | Tennis ball diameter | | | | 6.5 |
| 80. | Golf ball diameter | | | | 4.6 |
| 81. | Distance from London to Paris | | | 342 | |
| 82. | Distance from Houston to Dallas | | | 396 | |



- **83.** The total width of the Crazy Horse carving in Black Hills, South Dakota, is 641 feet. Convert this width to
 - **a.** yards
 - **b.** inches
- **84.** The total height of the Crazy Horse carving in Black Hills, South Dakota, is 563 feet. Convert this height to
 - a. yards
 - **b.** inches

- **85.** The National Zoo maintains a small patch of bamboo, which it grows as a food supply for its pandas. Two weeks ago, the bamboo was 6 ft 10 in. tall. Since then, the bamboo has grown 3 ft 8 in. How tall is the bamboo now?
- **87.** At its deepest point, the Grand Canyon of the Colorado River in Arizona is about 6000 ft. The Grand Canyon of the Yellowstone River, which is in Yellowstone National Park in Wyoming, is at most 900 feet deep. How much deeper is the Grand Canyon of the Colorado River than the Grand Canyon of the Yellowstone River? (*Source:* National Park Service)
- **89.** The tallest man in the world is recorded as Robert Pershing Wadlow of Alton, Illinois. Born in 1918, he measured 8 ft 11 in. at his tallest. The shortest man in the world is Chandra Bahadur Dangi of Nepal, who measures 21.5 in. How many times taller than Chandra was Robert? Round to one decimal place. (*Source: Guinness World Records*)
- **91.** The length of one of the Statue of Liberty's hands is 16 ft 5 in. One of the statue's eyes is 2 ft 6 in. across. How much longer is a hand than the width of an eye? (*Source:* National Park Service)
- **92.** The width of the Statue of Liberty's head from ear to ear is 10 ft. The height of the statue's head from chin to cranium is 17 ft 3 in. How much taller is the statue's head than its width? (*Source:* National Park Service)
- **93.** The ice on a pond is 5.33 cm thick. For safe skating, the owner of the pond insists that it must be 80 mm thick. How much thicker must the ice be before skating is allowed?
- **95.** The Amana Corporation stacks up its microwave ovens in a distribution warehouse. Each stack is 1 ft 9 in. wide. How far from the wall would 9 of these stacks extend?



1 ft 9 in.

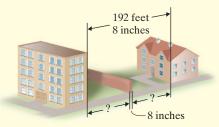
- **86.** While exploring in the Marianas Trench, a submarine probe was lowered to a point 1 mile 1400 feet below the ocean's surface. Later it was lowered an additional 1 mile 4000 feet below this point. How far was the probe below the surface of the Pacific?
- **88.** The Black Canyon of the Gunnison River is only 1150 ft wide at its narrowest point. At its narrowest, the Grand Canyon of the Yellowstone is $\frac{1}{2}$ mile wide. Find the difference in width between the Grand Canyon of the Yellowstone and the Black Canyon of the Gunnison. (*Note:* Notice that the dimensions are different.) (*Source:* National Park Service)
- **90.** A 3.4-m rope is attached to a 5.8-m rope. However, when the ropes are tied, 8 cm of length is lost to form the knot. What is the length of the tied ropes?



- **94.** The sediment on the bottom of the Towamencin Creek is normally 14 cm thick, but the recent flood washed away 22 mm of sediment. How thick is it now?
- **96.** The highway commission is installing concrete sound barriers along a highway. Each barrier is 1 yd 2 ft long. Find the total length of 25 barriers placed end to end.



97. A wall is erected exactly halfway between two buildings that are 192 ft 8 in. apart. If the wall is 8 in. wide, how far is it from the wall to either of the buildings?

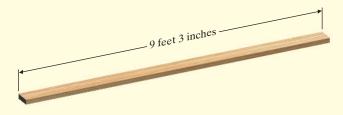


- **99.** An art class is learning how to make kites. The two sticks used for each kite have lengths of 1 m and 65 cm. What total length of wood must be ordered for the sticks if 25 kites are to be built?
- **101.** A logging firm needs to cut a 67-m-long redwood log into 20 equal pieces before loading it onto a truck for shipment. How long will each piece be?
- **103.** A 2.15-m-long sash cord has become frayed at both ends so that 1 cm is trimmed from each end. How long is the remaining cord?
- **105.** The giant Coca-Cola billboard in Times Square is lit by more than 2.6 million LEDs, which are completely powered by wind energy. This huge advertisement measures approximately 44 feet by 65 feet. Find the perimeter of the sign in yards. (Source: Coca-Cola Company)



107. A floor tile is 22.86 cm wide. How many tiles in a row are needed to cross a room 3.429 m wide?

98. A carpenter needs to cut a board into thirds. If the board is 9 ft 3 in. long originally, how long will each cut piece be?



- **100.** The total pages of a hardbound economics text are 3.1 cm thick. The front and back covers are each 2 mm thick. How high would a stack of 10 of these texts be?
- **102.** An 18.3-m-tall flagpole is mounted on a 65-cm-high pedestal. How far is the top of the flagpole from the ground?
- **104.** A 112.5-foot-tall dead pine tree is removed by starting at the top and cutting off 9-footlong sections. How many 9-foot sections are removed?
- **106.** The longest truck in the world is operated by Gould Transport in Australia, and is the 182-ft Road Train. How many *yards* long are 2 of these trucks? (Source: Guinness World Records)



108. A standard postcard is 1.6 times longer than it is wide. If it is 9.9 cm wide, what is its length?

113. $\frac{1}{4}$

Review

Write each decimal as a fraction and each fraction as a decimal. See Section 4.6.

109. 0.21

110. 0.86

 $\frac{3}{20}$

Concept Extensions

Determine whether the measurement in each statement is reasonable.

- **115.** The width of a twin-size bed is 20 meters. **117.** A drinking glass is made of glass 2 millimeters thick.
- **119.** The distance across the Colorado River is 50 kilometers.

Estimate each sum or difference. See the first Concept Check in this section.

- 121. 5 vd 2 in. + 7 yd 30 in.
- **123.** Using a unit other than the foot, write a length that is equivalent to 4 feet. (Hint: There are many possibilities.)
- **125.** To convert from meters to centimeters, the decimal point is moved two places to the right. Explain how this relates to the fact that the

prefix *centi* means $\frac{1}{100}$

- **116.** A window measures 1 meter by 0.5 meter.
- **118.** A paper clip is 4 kilometers long.
- **120.** A model's hair is 30 centimeters long.
- 122. 45 ft 1 in. - 10 ft 11 in.
- **124.** Using a unit other than the meter, write a length that is equivalent to 7 meters. (Hint: There are many possibilities.)
- **126.** Explain why conversions in the metric system are easier to make than conversions in the U.S. system of measurement.
- **127.** An advertisement sign outside Fenway Park in Boston measures 18.3 m by 18.3 m. What is the area of this sign?

Objectives

- A Define U.S. Units of Weight and Convert from One Unit to Another. 🜔
- **B** Perform Arithmetic Operations on U.S. Units of Weight. 🜔
- C Define Metric Units of Mass and Convert from One Unit to Another. D
- **D** Perform Arithmetic **Operations on Metric Units** of Mass. D

7.2 Weight and Mass: U.S. and Metric Systems of Measurement 🔘

Objective A Defining and Converting U.S. System Units of Weight D

Whenever we talk about how heavy an object is, we are concerned with the object's weight. We discuss weight when we refer to a 12-ounce box of Rice Krispies, a 15-pound tabby cat, or a barge hauling 24 tons of garbage.







24 tons of garbage

The most common units of weight in the U.S. measurement system are the ounce, the pound, and the ton. The following is a summary of equivalencies between units of weight:

| U.S. Units of Weight | Unit Fractions |
|-----------------------------------|---|
| 16 ounces $(oz) = 1$ pound (lb) | $\frac{16 \text{ oz}}{1 \text{ lb}} = \frac{1 \text{ lb}}{16 \text{ oz}} = 1$ |
| 2000 pounds = 1 ton | $\frac{2000 \text{ lb}}{1 \text{ ton}} = \frac{1 \text{ ton}}{2000 \text{ lb}} = 1$ |

Concept Check If you were describing the weight of a fully loaded semitrailer, which type of unit would you use: ounce, pound, or ton? Why?

Unit fractions that equal 1 are used to convert between units of weight in the U.S. system. When converting using unit fractions, recall that the numerator of a unit fraction should contain the units we are converting to and the denominator should contain the original units.

Example 1 Convert 9000 pounds to tons. **Solution:** We multiply 9000 lb by a unit fraction that uses the equality 2000 pounds = 1 ton.Remember, the unit fraction should be $\frac{\text{units to convert to}}{\text{original units}}$ or $\frac{1 \text{ ton}}{2000 \text{ lb}}$. 9000 lb = $\frac{9000 \text{ lb}}{1} \cdot 1 = \frac{9000 \text{ lb}}{1} \cdot \frac{1 \text{ ton}}{2000 \text{ lb}} = \frac{9000 \text{ tons}}{2000} = \frac{9}{2} \text{ tons or } 4\frac{1}{2} \text{ tons}$ 2000 lb 2000 lb 2000 lb 2000 lb 1000 lb 9000 lb = $4\frac{1}{2}$ tons 1 ton $\frac{1}{2}$ ton 1 ton 1 ton 1 ton

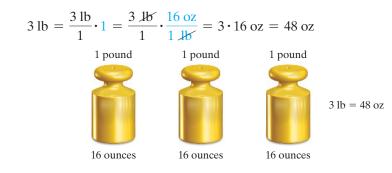
Practice 1 Convert 6500 pounds to tons.

Work Practice 1

Example 2 Con

Convert 3 pounds to ounces.

Solution: We multiply by the unit fraction $\frac{16 \text{ oz}}{1 \text{ lb}}$ to convert from pounds to ounces.



Work Practice 2

As with length, it is sometimes useful to simplify a measurement of weight by writing it in terms of mixed units.

Practice 2 Convert 72 ounces to pounds.

1. $3\frac{1}{4}$ tons **2.** $4\frac{1}{2}$ lb

Answers

Concept Check Answer ton

Chapter 7 | Measurement

Practice 3

Convert: 47 ounces =lb oz Example 3 Convert: 33 ounces = 1b oz

Solution: Because 16 oz = 1 lb, divide 16 into 33 to see how many pounds are in 33 ounces. The quotient is the number of pounds, and the remainder is the number of ounces. To see why we divide 16 into 33, notice that

$$33 \text{ oz} = 33 \text{ oz} \cdot \frac{1 \text{ lb}}{16 \text{ oz}} = \frac{33}{16} \text{ lb}$$

$$2 \text{ lb} 1 \text{ oz}$$

$$16\overline{)33}$$

$$-32$$

$$1 \text{ lb}$$

Thus, 33 ounces is the same as 2 lb 1 oz.



Work Practice 3

Objective B Performing Operations on U.S. System Units of Weight 🜔

Performing arithmetic operations on units of weight works the same way as performing arithmetic operations on units of length.

Example 4

Subtract 3 tons 1350 lb from 8 tons 1000 lb.

Solution: To subtract, we line up similar units.

8 tons 1000 lb

- 3 tons 1350 lb

Since we cannot subtract 1350 lb from 1000 lb, we borrow 1 ton from the 8 tons. To do so, we write 1 ton as 2000 lb and combine it with the 1000 lb.

 $7 \tan (1 \tan 2000 \text{ lb})$ 8 tons 1000 lb 7 tons 3000 lb =- 3 tons 1350 lb =- 3 tons 1350 lb 4 tons 1650 lb

To check, see that the sum of 4 tons 1650 lb and 3 tons 1350 lb is 8 tons 1000 lb.

Work Practice 4



Example 5 Divide 9 lb 6 oz by 2.

Solution: We divide each of the units by 2.

$$\frac{4 \text{ lb} \quad 11 \text{ oz}}{2 \text{ 9 lb} \quad 6 \text{ oz}}$$

$$\frac{-8}{1 \text{ lb}} = \frac{16 \text{ oz}}{22 \text{ oz}}$$
Divide 2 into 22 oz to get 11 oz.

To check, multiply 4 pounds 11 ounces by 2. The result is 9 pounds 6 ounces.

Work Practice 5



Subtract 5 tons 1200 lb from 8 tons 100 lb.

Practice 5 Divide 5 lb 8 oz by 4.

Answers **3.** 2 lb 15 oz **4.** 2 tons 900 lb 5. 1 lb 6 oz

457

Example 6

Finding the Weight of a Child

Bryan weighed 8 lb 8 oz at birth. By the time he was 1 year old, he had gained 11 lb 14 oz. Find his weight at age 1 year.

Solution:

| birth weight | \rightarrow | 8 lb 8 oz |
|-------------------------|---------------|---------------|
| + weight gained | \rightarrow | + 11 lb 14 oz |
| total weight | \rightarrow | 19 lb 22 oz |
| Since 22 oz equals 1 lb | o 6 oz, | |

$$19 \text{ lb } 22 \text{ oz} = 19 \text{ lb} + 1 \text{ lb } 6 \text{ oz}$$
$$= 20 \text{ lb } 6 \text{ oz}$$

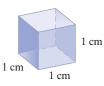
Bryan weighed 20 lb 6 oz on his first birthday.

Work Practice 6

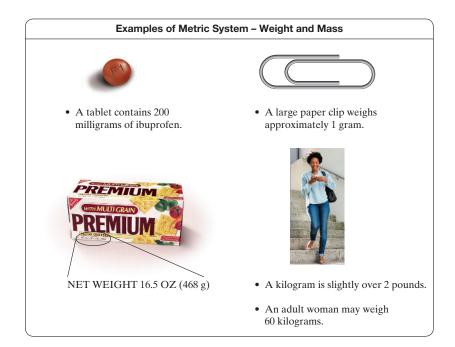
Objective C Defining and Converting Metric System Units of Mass

In scientific and technical areas, a careful distinction is made between **weight** and **mass. Weight** is really a measure of the pull of gravity. The farther from Earth an object gets, the less it weighs. However, **mass** is a measure of the amount of substance in the object and does not change. Astronauts orbiting Earth weigh much less than they weigh on Earth, but they have the same mass in orbit as they do on Earth. Here on Earth, weight and mass are the same, so either term may be used.

The basic unit of mass in the metric system is the **gram.** It is defined as the mass of water contained in a cube 1 centimeter (cm) on each side.



The following examples may help you get a feeling for metric masses:



Practice 6

A 5-lb 14-oz batch of cookies is packed into a 6-oz container before it is mailed. Find the total weight.

Answer 6. 6 lb 4 oz The prefixes for units of mass in the metric system are the same as for units of length, as shown in the following table:

| Metric Units of Mass |
|---|
| 1 kilogram (kg) = 1000 grams (g) |
| 1 hectogram (hg) = 100 g |
| 1 dekagram (dag) = 10 g |
| $1 \operatorname{gram}(g) = 1 \operatorname{g}$ |
| 1 decigram (dg) = 1/10 g or 0.1 g |
| 1 centi gram (cg) = $1/100$ g or 0.01 g |
| 1 milligram (mg) = 1/1000 g or 0.001 g |

Concept Check True or false? A decigram is larger than a dekagram. Explain.

The **milligram**, the **gram**, and the **kilogram** are the three most commonly used units of mass in the metric system.

As with lengths, all units of mass are powers of 10 of the gram, so converting from one unit of mass to another only involves moving the decimal point. To convert from one unit of mass to another in the metric system, list the units of mass in order from largest to smallest.

Let's convert 4300 milligrams to grams. To convert from milligrams to grams, we move along the list 3 units to the left.



This means that we move the decimal point 3 places to the left to convert from milligrams to grams.

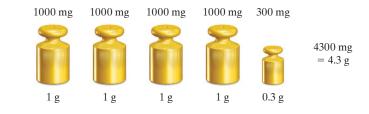
$$4300 \text{ mg} = 4.3 \text{ g}$$

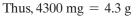
Don't forget, the same conversion can be done with unit fractions.

$$4300 \text{ mg} = \frac{4300 \text{ mg}}{1} \cdot 1 = \frac{4300 \text{ mg}}{1} \cdot \frac{0.001 \text{ g}}{1 \text{ mg}}$$
$$= 4300 \cdot 0.001 \text{ g}$$

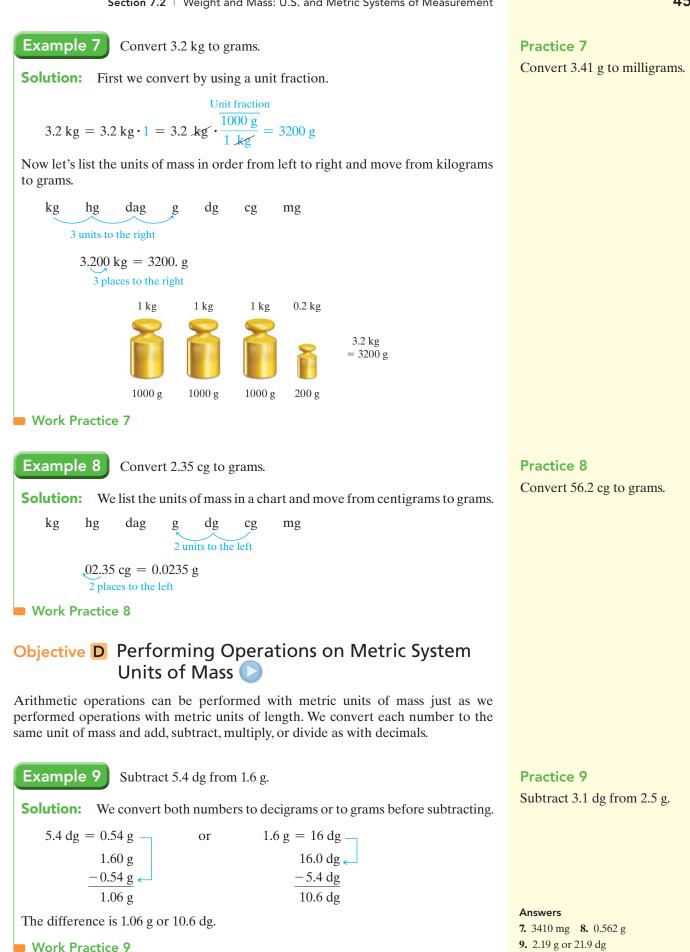
= 4.3 g To multiply by 0.001, move the decimal point 3 places to the left.

To see that this is reasonable, study the diagram:









Chapter 7 | Measurement

Practice 10

Twenty-four bags of cement weigh a total of 550 kg. Find the average weight of 1 bag, rounded to the nearest kilogram.

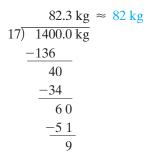


Example 10

0 Calculating Allowable Weight in an Elevator

An elevator has a weight limit of 1400 kg. A sign posted in the elevator indicates that the maximum capacity of the elevator is 17 persons. What is the average allowable weight for each passenger, rounded to the nearest kilogram?

Solution: To solve, notice that the total weight of 1400 kilograms \div 17 = average weight.





Each passenger can weigh an average of 82 kg. (Recall that a kilogram is slightly over 2 pounds, so 82 kilograms is over 164 pounds.)

Work Practice 10

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank.

mass weight gram

- 1. _____ is a measure of the amount of substance in an object. This measure does not change.
- **2.** ______ is the measure of the pull of gravity.
- 3. The basic unit of mass in the metric system is the _____.

Fill in these blanks with the correct number. Choices for these blanks are not shown in the list of terms above.

- 4. One pound equals _____ ounces.
- 5. One ton equals _____ pounds.

Convert without pencil or paper.

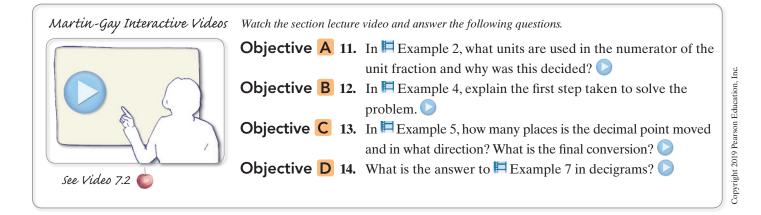
6. 3 tons to pounds

7. 32 ounces to pounds

8. 3 pounds to ounces

9. 4000 pounds to tons

10. 1 ton to pounds



Answer 10. 23 kg

| | | - | | |
|--------------|--|---|----------------------------------|---|
| 7 | .2 Exercise Set MyL | .ab Math 🜔 | | |
| Ob | jective A Convert as indicated. | . See Examples 1 through 3 | | |
| 1. | 2 pounds to ounces 2.5 p | pounds to ounces 3 | 5 tons to pounds | 4. 7 tons to pounds |
| 5. | 18,000 pounds to tons 6. 28 | $0,000 \text{ pounds to tons } \mathbf{O7}$ | . 60 ounces to pounds | 8. 90 ounces to pounds |
| 9. | 3500 pounds to tons 10. 11 | ,000 pounds to tons 11 | 12.75 pounds to oun | ces 12. 9.5 pounds to ounces |
| O 13. | 4.9 tons to pounds 14. 8.3 | 3 tons to pounds 15 | • $4\frac{3}{4}$ pounds to ounce | es 16. $9\frac{1}{8}$ pounds to ounces |
| 17. | 2950 pounds to the nearest tenth | of a ton 18 | 51 ounces to the near | arest tenth of a pound |
| 19. | $\frac{4}{5}$ oz to pounds | 20 | $\frac{1}{4}$ oz to pounds | |
| 21. | $5\frac{3}{4}$ lb to ounces | 22 | • $2\frac{1}{4}$ lb to ounces | |
| 23. | 10 lb 1 oz to ounces | 24 | • 7 lb 6 oz to ounces | |
| 0 25. | 89 oz = lboz | 26 | $100 \text{ oz} = \ \text{lb}$ | 0Z |
| Ob | jective B Perform each indicate | ed operation. See Example. | 4 through 6. | |
| | 34 lb 12 oz + 18 lb 14 oz | 28. 6 lb 10 oz + 10 lb | - | 3 tons 1820 lb + 4 tons 930 lb |
| 30. | 1 ton 1140 lb + 5 tons 1200 lb | 31. 5 tons 1050 lb - 2 | tons 875 lb 32. | 4 tons 850 lb – 1 ton 260 lb |
| • 33. | 12 lb 4 oz – 3 lb 9 oz | 34. 45 lb 6 oz – 26 lb | 10 oz 35 . | 5 lb 3 oz × 6 |
| 36. | 2 lb 5 oz × 5 | 37. 6 tons 1500 lb ÷ 5 | 38. | 5 tons 400 lb ÷ 4 |

| Objective C Convert as | Objective C Convert as indicated. See Examples 7 and 8. | | | |
|---------------------------------|--|----------------------------------|----------------------------------|--|
| 39. 500 g to kilograms | 40. 820 g to kilograms | ● 41. 4 g to milligrams | 42. 9 g to milligrams | |
| 43. 25 kg to grams | 44. 18 kg to grams | 45. 48 mg to grams | 46. 112 mg to grams | |
| • 47. 6.3 g to kilograms | 48. 4.9 g to kilograms | 49. 15.14 g to milligrams | 50. 16.23 g to milligrams | |
| 51. 6.25 kg to grams | 52. 3.16 kg to grams | 53. 35 hg to centigrams | 54. 4.26 cg to dekagrams | |

Objective D *Perform each indicated operation. Remember to insert units when writing your answers. See Examples 9 and 10.*

| 55. 3.8 mg + 9.7 mg | 56. 41.6 g + 9.8 g | 57. 205 mg + 5.61 g | 58. 2.1 g + 153 mg |
|----------------------------|----------------------------|----------------------------|---------------------------|
| ○ 59. 9 g − 7150 mg | 60. 6.13 g - 418 mg | 61. 1.61 kg – 250 g | 62. 4 kg - 2410 g |
| 63. 5.2 kg × 2.6 | 64. 4.8 kg × 9.3 | 65. 17 kg ÷ 8 | 66. 8.25 g ÷ 6 |

Objectives A B C D Mixed Practice Solve. Remember to insert units when writing your answers. For Exercises 67 through 74, complete the chart. See Examples 1 through 10.

| | Object | Tons | Pounds | Ounces |
|-----|---|------|--------|--------|
| 67. | Statue of Liberty-weight of copper sheeting | 100 | | |
| 68. | Statue of Liberty-weight of steel | 125 | | |
| 69. | A 12-inch cube of osmium
(heaviest metal) | | 1345 | |
| 70. | A 12-inch cube of lithium
(lightest metal) | | 32 | |

| | Object | Grams | Kilograms | Milligrams | Centigrams |
|-----|---|-------|-----------|------------|------------|
| 71. | Capsule of amoxicillin (antibiotic) | | | 500 | |
| 72. | Tablet of Topamax
(epilepsy and migraine uses) | | | 25 | |
| 73. | A six-year-old boy | | 21 | | |
| 74. | A golf ball | 45 | | | |

- **75.** A can of 7-Up weighs 336 grams. Find the weight in kilograms of 24 cans.
- **77.** Elizabeth Hamtini was amazed when she grew a 28-lb 10-oz zucchini in her garden, but later she learned that the heaviest zucchini ever grown weighed 64 lb 8 oz in Llanharry, Wales, by B. Lavery in 1990. How far below the record weight was Elizabeth's zucchini? (*Source:* Guinness World Records)



- **79.** The supermarket prepares hamburger in 450-gram market packages. When Leo Gonzalas gets home, he divides the package in fourths before refrigerating the meat. How much will each divided package weigh?
- **81.** A chef has two open containers of whole grain brown rice. If she combines 1 lb 10 oz from one container with 3 lb 14 oz from the other container, how much total rice does she have?
- **83.** The smallest surviving baby weighed only 8 ounces, less than an average grapefruit. She was born in Witten, Germany, in December 2015. How much lighter was she than an average European baby, who weighs about 7 lb 7.5 oz?
- **85.** Three milligrams of preservatives are added to a 0.5-kg box of dried fruit. How many milligrams of preservatives are in 3 cartons of dried fruit if each carton contains 16 boxes?
- **87.** A carton of 12 boxes of Quaker Oats Oatmeal weighs 6.432 kg. Each box includes 26 grams of packaging material. What is the actual weight of the oatmeal in the carton?
- **89.** The Shop 'n Bag supermarket chain ships hamburger meat by placing 10 packages of hamburger in a box, with each package weighing 3 lb 4 oz. How much will 4 boxes of hamburger weigh?
- **91.** A carton of Del Monte Pineapple weighs 55 lb 4 oz, but 2 lb 8 oz of this weight is due to packaging. Find the actual weight of the pineapple in 4 cartons.

- **76.** Guy Green normally weighs 73 kg, but he lost 2800 grams after being sick with the flu. Find Guy's new weight.
- **78.** A small can of Planters sunflower seeds weighs 177 g. If each can contains 6 servings, find the weight of one serving.



- **80.** Sudafed is a decongestant that comes in two strengths. Regular strength contains 60 mg of medication. Extra strength contains 0.09 g of medication. How much extra medication is in the extra-strength tablet?
- **82.** Dru Mizel maintains the records of the amount of coal delivered to his department in the steel mill. In January, 3 tons 1500 lb were delivered. In February, 2 tons 1200 lb were delivered. Find the total amount delivered in these two months.
- **84.** The heaviest baby born in good health weighed an incredible 22 lb 8 oz. He was born in Italy in September 1955. How much heavier is this than a 7-lb 12-oz baby? (*Source:* Guinness World Records)
- **86.** A large bottle of Hire's Root Beer weighs 1900 grams. If a carton contains 6 large bottles of root beer, find the weight in kilograms of 5 cartons.
- **88.** One box of Swiss Miss Cocoa Mix weighs 0.385 kg, but 39 grams of this weight is the packaging. Find the actual weight of the cocoa in 8 boxes.
- **90.** The Quaker Oats Company ships its 1-lb 2-oz boxes of oatmeal in cartons containing 12 boxes of oatmeal. How much will 3 such cartons weigh?
- **92.** The Hormel Corporation ships cartons of canned ham weighing 43 lb 2 oz each. Of this weight, 3 lb 4 oz is due to packaging. Find the actual weight of the ham found in 3 cartons.

Review

Write each fraction as a decimal. See Section 4.6.

93.
$$\frac{4}{25}$$
 94. $\frac{3}{5}$ **95.** $\frac{7}{8}$ **96.** $\frac{3}{16}$

Concept Extensions

Determine whether the measurement in each statement is reasonable.

- **97.** The doctor prescribed a pill containing 2 kg of medication.
- **99.** A bag of flour weighs 4.5 kg.
- **101.** A professor weighs less than 150 g.
- **103.** Use a unit other than centigram and write a mass that is equivalent to 25 centigrams. (*Hint:* There are many possibilities.)

True or false? See the second Concept Check in this section.

- **105.** A kilogram is larger than a gram.
- **107.** Why is the decimal point moved to the right when grams are converted to milligrams?

- **98.** A full-grown cat weighs approximately 15 g.
- **100.** A staple weighs 15 mg.
- **102.** A car weighs 2000 mg.
- **104.** Use a unit other than pound and write a weight that is equivalent to 4000 pounds. (*Hint:* There are many possibilities.)
- **106.** A decigram is larger than a milligram.
- **108.** To change 8 pounds to ounces, multiply by 16. Why is this the correct procedure?

7.3 Capacity: U.S. and Metric Systems of Measurement

Objectives

- A Define U.S. Units of Capacity and Convert from One Unit to Another.
- B Perform Arithmetic Operations on U.S. Units of Capacity.
- C Define Metric Units of Capacity and Convert from One Unit to Another.
- Perform Arithmetic
 Operations on Metric Units of Capacity.

Objective A Defining and Converting U.S. System Units of Capacity 🕗

Units of **capacity** are generally used to measure liquids. The number of gallons of gasoline needed to fill a gas tank in a car, the number of cups of water needed in a bread recipe, and the number of quarts of milk sold each day at a supermarket are all examples of using units of capacity. The following summary shows equivalencies between units of capacity:

U.S. Units of Capacity

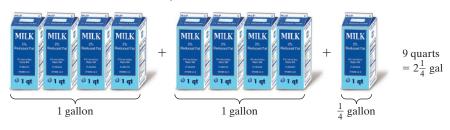
8 fluid ounces (fl oz) = 1 cup (c) 2 cups = 1 pint (pt) 2 pints = 1 quart (qt) 4 quarts = 1 gallon (gal) Just as with units of length and weight, we can form unit fractions to convert between different units of capacity. For instance,

$$\frac{2 c}{1 pt} = \frac{1 pt}{2 c} = 1$$
 and $\frac{2 pt}{1 qt} = \frac{1 qt}{2 pt} = 1$

Example 1 Convert 9 quarts to gallons.
Solution: We multiply by the unit fraction
$$\frac{1 \text{ gal}}{4 \text{ qt}}$$

9 qt = $\frac{9 \text{ qt}}{1} \cdot 1$
= $\frac{9 \text{ qt}}{1} \cdot \frac{1 \text{ gal}}{4 \text{ qt}}$
= $\frac{9 \text{ gal}}{4}$
= $2\frac{1}{4}$ gal
Thus 9 quarts is the same as $2\frac{1}{4}$ callons, as shown is

Thus, 9 quarts is the same as $2\frac{1}{4}$ gallons, as shown in the diagram:



Work Practice 1

Example 2

Convert 14 cups to quarts.

Solution: Our equivalency table contains no direct conversion from cups to quarts. However, from this table we know that

$$1 \text{ qt} = 2 \text{ pt} = \frac{2 \text{ pt}}{1} \cdot 1 = \frac{2 \text{ pt}}{1} \cdot \frac{2 \text{ c}}{1 \text{ pt}} = 4 \text{ c}$$

so 1 qt = 4 c. Now we have the unit fraction $\frac{1 \text{ qt}}{4 \text{ c}}$. Thus,

$$14 c = \frac{14 c}{1} \cdot 1 = \frac{14 c}{1} \cdot \frac{1 qt}{4 c} = \frac{14 qt}{4} = \frac{7}{2} qt \text{ or } 3\frac{1}{2} qt$$

$$\underbrace{1 \text{ quart}}_{1 \text{ quart}} + \underbrace{1 \text{ quart}}_{1 \text{ quart}} + \underbrace{1 \text{ quart}}_{1 \text{ quart}} + \underbrace{1 \text{ quart}}_{\frac{1}{2} \text{ quart}} + \underbrace{1 \text{ quart}}_{\frac{1}{2} \text{ quart}} = 3\frac{1}{2} \text{ qt}$$

Concept Check If 50 cups is converted to quarts, will the equivalent number of quarts be less than or greater than 50? Explain.

Practice 2 Convert 26 quarts to cups.

Answers 1. $21\frac{1}{2}$ qt **2.** 104 c

Concept Check Answer less than 50

Practice 1 Convert 43 pints to quarts.

Objective B Performing Operations on U.S. System Units of Capacity D

As is true of units of length and weight, units of capacity can be added, subtracted, multiplied, and divided.

Practice 3

Subtract 2 qt from 1 gal 1 qt.

Example 3 Subtract 3 qt from 4 gal 2 qt.

Solution: To subtract, we line up similar units.

4 gal 2 qt - 3 qt

We cannot subtract 3 qt from 2 qt. We need to borrow 1 gallon from the 4 gallons, convert it to 4 quarts, and then combine it with the 2 quarts.

| 3 gal + 1 gal 4 q | t | |
|----------------------|---|------------|
| 4 gal 2 qt | = | 3 gal 6 qt |
| <u>- 3 qt</u> | = | – 3 qt |
| | | 3 gal 3 qt |

To check, see that the sum of 3 gal 3 qt and 3 qt is 4 gal 2 qt.

Work Practice 3



Example 4 Divide 3 gal 2 qt by 2.

Solution: We divide each unit of capacity by 2.

$$\frac{1 \text{ gal } 3 \text{ qt}}{2)3 \text{ gal } 2 \text{ qt}}$$

$$\frac{-2}{1 \text{ gal}} = \frac{4 \text{ qt}}{6 \text{ qt}} \quad \text{Convert 1 gallon to 4 qt and add to 2 qt before continuing.}$$

Work Practice 4

Example 5 Finding the Amount of Water in an Aquarium

An aquarium contains 6 gal 3 qt of water. If 2 gal 2 qt of water is added, what is the total amount of water in the aquarium?

Solution:

beginning water \rightarrow 6 gal 3 qt water added \rightarrow + 2 gal 2 qt total water \rightarrow 8 gal 5 qt

Since 5 qt = 1 gal 1 qt, we have

$$= \frac{8 \text{ gal}}{8 \text{ gal}} + \frac{5 \text{ qt}}{1 \text{ gal } 1 \text{ qt}}$$
$$= 9 \text{ gal } 1 \text{ qt}$$

The total amount of water is 9 gal 1 qt.

Work Practice 5

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Practice 4 Divide 6 gal 3 qt by 2.

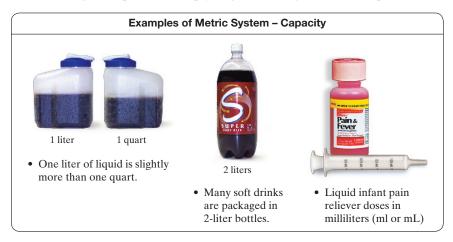
Practice 5

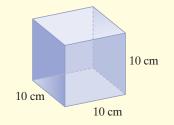
A large oil drum contains 15 gal 3 qt of oil. How much will be in the drum if an additional 4 gal 3 qt of oil is poured into it?

Objective C Defining and Converting Metric System Units of Capacity O

Thus far, we know that the basic unit of length in the metric system is the meter and that the basic unit of mass in the metric system is the gram. What is the basic unit of capacity? The **liter**. By definition, a **liter** is the capacity or volume of a cube measuring 10 centimeters on each side.

The following examples may help you get a feeling for metric capacities:





The metric system was designed to be a consistent system. Once again, the prefixes for metric units of capacity are the same as for metric units of length and mass, as summarized in the following table:

| Metric Units of Capacity | | |
|---|--|--|
| 1 kiloliter (kl) = 1000 liters (L) | | |
| 1 hectoliter (hl) = 100 L | | |
| 1 dekaliter (dal) = 10 L | | |
| 1 liter (L) = 1 L | | |
| 1 deciliter (dl) = 1/10 L or 0.1 L | | |
| 1 centi liter (cl) = $1/100$ L or 0.01 L | | |
| 1 milliliter (ml) = 1/1000 L or 0.001 L | | |

The milliliter and the liter are the two most commonly used metric units of capacity.

Converting from one unit of capacity to another involves multiplying by powers of 10 or moving the decimal point to the left or to the right. Listing units of capacity in order from largest to smallest helps to keep track of how many places to move the decimal point when converting.

Let's convert 2.6 liters to milliliters. To convert from liters to milliliters, we move along the chart 3 units to the right.

kl hl dal L dl cl ml

3 units to the right

This means that we move the decimal point 3 places to the right to convert from liters to milliliters.

2.600 L = 2600. ml

This same conversion can be done with unit fractions.

$$2.6 L = \frac{2.6 L}{1} \cdot 1$$
$$= \frac{2.6 \mathcal{L}}{1} \cdot \frac{1000 \text{ ml}}{1 \mathcal{L}}$$
$$= 2.6 \cdot 1000 \text{ ml}$$

= 2600 ml To multiply by 1000, move the decimal point 3 places to the right.

To visualize the result, study the diagram below:



Thus, 2.6 L = 2600 ml.

Example 6

Convert 3210 ml to liters.

Solution: Let's use the unit fraction method first.

$$3210 \text{ ml} = \frac{3210 \text{ ml}}{1} \cdot 1 = 3210 \text{ ml} \cdot \frac{1 \text{ L}}{1000 \text{ ml}} = 3.21 \text{ L}$$

Now let's list the unit measures in order from left to right and move from milliliters to liters.



3210 ml = 3.210 L, the same results as before and shown below in the diagram.





Work Practice 6



Convert 0.185 dl to milliliters.

Solution: We list the unit measures in order from left to right and move from deciliters to milliliters.



Objective D Performing Operations on Metric System Units of Capacity O

As was true for length and weight, arithmetic operations involving metric units of capacity can also be performed. Make sure that the metric units of capacity are the same before adding or subtracting.

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Answers 6. 2.1 L 7. 21.3 L

Practice 6

Convert 2100 ml to liters.

Example 8

Add 2400 ml to 8.9 L.

Solution: We must convert both to liters or both to milliliters before adding the capacities together.

| 2400 ml = 2.4 L | or | 8.9 L = 8900 ml |
|-----------------|----|-----------------|
| 2.4 L ← | | 2400 ml |
| +8.9 L | | +8900 ml < |
| 11.3 L | | 11,300 ml |

The total is 11.3 L or 11,300 ml. They both represent the same capacity.

```
Work Practice 8
```

Concept Check How could you estimate the following operation? Subtract 950 ml from 7.5 L.

Example 9 Finding the Amount of Medication a Person Has Received

A patient hooked up to an IV unit in the hospital is to receive 12.5 ml of medication every hour. How much medication does the patient receive in 3.5 hours?

Solution: We multiply 12.5 ml by 3.5.

| | medication per hour | \rightarrow | 12.5 ml |
|----------|---------------------|---------------|--------------|
| \times | hours | \rightarrow | \times 3.5 |
| | total medication | | 625 |
| | | | 3750 |
| | | | 43.75 ml |
| | | | |

The patient receives 43.75 ml of medication.

Work Practice 9

Practice 8 Add 1250 ml to 2.9 L.

Practice 9

If 28.6 L of water can be pumped every minute, how much water can be pumped in 85 minutes?

Answers 8. 4150 ml or 4.15 L 9. 2431 L

✓ Concept Check Answer 950 ml = 0.95 L; round 0.95 to 1; 7.5 − 1 = 6.5 L

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Some choices may be used more than once.

| cups | pints | liter |
|--------|--------------|----------|
| quarts | fluid ounces | capacity |

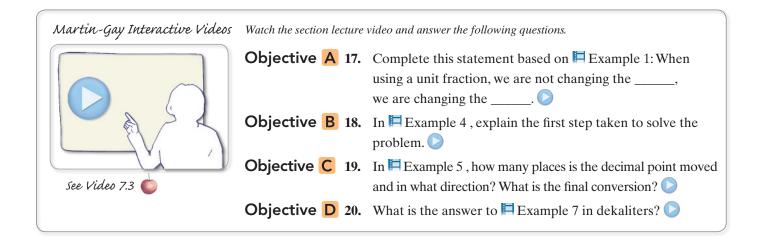
1. Units of ______ are generally used to measure liquids.

- 2. The basic unit of capacity in the metric system is the _____
- **3.** One cup equals 8 _____.
- 4. One quart equals 2 _____.
- 5. One pint equals 2 _____.
- 6. One quart equals 4 _____.
- 7. One gallon equals 4 _____.

Chapter 7 | Measurement

Convert as indicated without pencil and paper or calculator.

8. 2 c to pints
9. 4 c to pints
10. 4 qt to gallons
11. 8 qt to gallons
12. 2 pt to quarts
13. 6 pt to quarts
14. 8 fl oz to cups
15. 24 fl oz to cups
16. 3 pt to cups



7.3 Exercise Set MyLab Math 🕗

| Objective A Convert each measurement as indicated. See Examples 1 and 2. | | | |
|---|------------------------------------|--|---|
| 1. 32 fluid ounces to cups | 2. 16 quarts to gallons | 3. 8 quarts to pints | 4. 9 pints to quarts |
| 5. 14 quarts to gallons | 6. 11 cups to pints | 7. 80 fluid ounces to pints | 8. 18 pints to gallons |
| 9. 2 quarts to cups | 10. 3 pints to fluid ounces | 11. 120 fluid ounces to quarts | 12. 20 cups to gallons |
| • 13. 42 cups to quarts | 14. 7 quarts to cups | 15. $4\frac{1}{2}$ pints to cups | 16. $6\frac{1}{2}$ gallons to quarts |
| 17. 5 gal 3 qt to quarts | 18. 4 gal 1 qt to quarts | 19. $\frac{1}{2}$ cup to pints | 20. $\frac{1}{2}$ pint to quarts |
| 21. 58 qt = gal | _ qt | 22. 70 qt =gal | _ qt |
| 23. $39 \text{ pt} = \gal \$ | _ qt pt | 24. 29 pt = gal | _ qt pt |
| 25. $2\frac{3}{4}$ gallons to pints | | 26. $3\frac{1}{4}$ quarts to cups | |

| Objective B Perform each indicated operation. See Examples 3 through 5. | | | |
|--|------------------------------------|--------------------------------------|--|
| 27. 5 gal 3 qt + 7 gal 3 qt | 28. 2 gal 2 qt + 9 gal 3 qt | 29. 1 c 5 fl oz + 2 c 7 fl oz | |
| 30. 2 c 3 fl oz + 2 c 6 fl oz | ○ 31. 3 gal – 1 gal 3 qt | 32. 2 pt – 1 pt 1 c | |
| 33. 3 gal 1 qt - 1 qt 1 pt | 34. 3 qt 1 c - 1 c 4 fl oz | 35. 8 gal 2 qt \times 2 | |
| 36. 6 gal 1 pt × 2 | 37. 9 gal 2 qt ÷ 2 | 38. 5 gal 6 fl oz ÷ 2 | |

Objective C *Convert as indicated. See Examples 6 and 7.*

| 39. 5 L to milliliters | 40. 8 L to milliliters | 41. 0.16 L to kiloliters | 42. 0.127 L to kiloliters |
|--------------------------------|--------------------------------|---------------------------------|----------------------------------|
| 43. 5600 ml to liters | 44. 1500 ml to liters | 45. 3.2 L to centiliters | 46. 1.7 L to centiliters |
| 47. 410 L to kiloliters | 48. 250 L to kiloliters | 49. 64 ml to liters | 50. 39 ml to liters |
| 51. 0.16 kl to liters | 52. 0.48 kl to liters | 53. 3.6 L to milliliters | 54. 1.9 L to milliliters |

Objective D *Perform each indicated operation. Remember to insert units when writing your answers. See Examples 8 and 9.*

| 55. 3.4 L + 15.9 L | 56. 18.5 L + 4.6 L | 57. 2700 ml + 1.8 L | 58. 4.6 L + 1600 ml |
|---------------------------|---------------------------|------------------------------|----------------------------|
| 59. 8.6 L – 190 ml | 60. 4.8 L – 283 ml | 61. 17,500 ml - 0.9 L | 62. 6850 ml – 0.3 L |
| 63. 480 ml × 8 | 64. 290 ml × 6 | 65. 81.2 L ÷ 0.5 | 66. 5.4 L ÷ 3.6 |

Objectives A B C D Mixed Practice Solve. Remember to insert units when writing your answers. For Exercises 67 through 70, complete the chart. See Examples 1 through 9.

| | Capacity | Cups | Gallons | Quarts | Pints |
|-----|---|------|---------|--------|-------|
| 67. | An average-size bath of water | | 21 | | |
| 68. | A dairy cow's daily milk yield | | | | 38 |
| 69. | Your kidneys filter about this amount of blood every minute | 4 | | | |
| 70. | The amount of water needed in a punch recipe | 2 | | | |

- **71.** A student poured 410 ml of Mountain Dew from a 2-liter bottle. How much Mountain Dew remains in the bottle?
- **73.** A mechanic added 354 ml of Prestone gas treatment to the 18.6 L of gasoline in his client's car's tank. Find the total amount of gasoline in the tank.
- **72.** The Werners' Volvo has a 54.5-L gas tank. Only 38 deciliters of gasoline still remain in the tank. How many liters will be needed to fill it?
- **74.** Eight friends are equally sharing a 2-L bottle of Coca-Cola. How much will each person get?

- **75.** A garden tool engine requires a 30-to-1 gas-to-oil mixture. This means that $\frac{1}{30}$ of a gallon of oil should be mixed with 1 gallon of gas. Convert $\frac{1}{30}$ gallon to fluid ounces. Round to the nearest tenth.
- **77.** Can 5 pt 1 c of fruit punch and 2 pt 1 c of ginger ale be poured into a 1-gal container without it overflowing?
- **79.** Stanley Fisher paid \$28 to fill his car with 44.3 liters of gasoline. Find the price per liter of gasoline to the nearest thousandth of a dollar.

- **76.** Henning's Supermarket sells homemade soup in 1 qt 1 pt containers. How much soup is contained in three such containers?
- **78.** Three cups of prepared Jell-O are poured into 6 dessert dishes. How many fluid ounces of Jell-O are in each dish?
- **80.** A student carelessly misread the scale on a cylinder in the chemistry lab and added 40 cl of water to a mixture instead of 40 ml. Find the excess amount of water.

Review

Write each fraction in simplest form. See Section 2.3.

| 81. $\frac{20}{25}$ | 82. $\frac{75}{100}$ | 83. $\frac{27}{45}$ | 84. $\frac{56}{60}$ | 85. $\frac{72}{80}$ | 86. $\frac{18}{20}$ |
|----------------------------|-----------------------------|----------------------------|----------------------------|----------------------------|----------------------------|
| Concept Ex | xtensions | | | | |

Determine whether the measurement in each statement is reasonable.

- **87.** Clair took a dose of 2 L of cough medicine to cure her cough.
- **89.** Jeannie likes to relax in a tub filled with 3000 ml of hot water.
- Solve. See the Concept Checks in this section.
- **91.** If 70 pints are converted to gallons, will the equivalent number of gallons be less than or greater than 70? Explain why.
- **93.** Explain how to estimate the following operation: Add 986 ml to 6.9 L.
 - **95.** Find the number of fluid ounces in 1 gallon.

A cubic centimeter (cc) is the amount of space that a volume of 1 ml occupies. Because of this, we will say that 1 cc = 1 ml.

A common syringe is one with a capacity of 3 cc. Use the diagram and give the measurement indicated by each arrow.

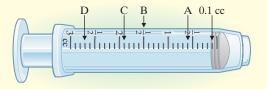
97. B **98.** A **99.** D

In order to measure small dosages, such as for insulin, u-100 syringes are used. For these syringes, 1 cc has been divided into 100 equal units (u). Use the diagram and give the measurement indicated by each arrow in units (u) and then in cubic centimeters. Use 100 u = 1 cc.

101. В **102.** А

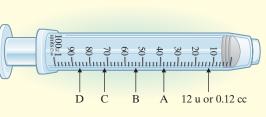
103. D **104.** C

- **88.** John drank 250 ml of milk for lunch.
- **90.** Sarah pumped 20 L of gasoline into her car yesterday.
- **92.** If 30 gallons are converted to quarts, will the equivalent number of quarts be less than or greater than 30? Explain why.
- **94.** Explain how to borrow in order to subtract 1 gal 2 qt from 3 gal 1 qt.
 - **96.** Find the number of fluid ounces in 1.5 gallons.



100.

C



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| | Sections 7.1–7.3 | Integrated Review |
|--|--|--------------------------|
| Length, Weight, and | Capacity | Answers
1. |
| Convert each measurement as indicated.
Length | | 2. |
| 1. 36 in. = ft | 2. 10,560 ft = mi | 3. |
| 3. $20 \text{ ft} = \y \text{ yd}$ | 4. $6\frac{1}{3}$ yd = ft | 4. |
| | | <u>5.</u>
6. |
| 5. 2.1 mi = ft | 6. 3.2 ft = in. | 7. |
| 7. $30 \text{ m} = ___ \text{ cm}$ | 8. 24 mm = cm | 8. |
| 9 2000 mm – m | 10 1800 cm - m | 9. |
| 9. 2000 mm = m | 10. $1800 \text{ cm} = ___ \text{m}$ | <u>10.</u> |
| 11. 7.2 cm = mm | 12. 600 m = km | <u>11.</u>
<u>12.</u> |
| Weight or Mass | | <u>13.</u> |
| 13. $7\frac{1}{2}$ tons = lb | 14. 11,000 lb =tons | |
| | | <u> </u> |
| 15. 8.5 lb = oz | 16. 72 oz = lb | 16. |

| 474 | Chapter 7 Measurement | |
|------------|---|---|
| 17. | 17. 104 oz = lb | 18. 5 lb = oz |
| 18. | | |
| 19. | 19. 28 kg =g | 20. 1400 mg = g |
| 20. | | |
| 21. | 21. 5.6 g = kg | 22. 6 kg = g |
| 22. | | |
| 23. | 23. 670 mg = g | 24. 3.6 g = kg |
| 24. | | |
| 25. | Capacity | |
| 26. | 25. $6 qt = \ pt$ | 26. 5 pt = qt |
| 27. | 07 | 00.45 |
| 28. | 27. $14 \text{ qt} = \ \text{gal}$ | 28. 17 c = pt |
| 29. | 1 | |
| 30. | 29. $3\frac{1}{2}$ pt = c | 30. $26 \text{ qt} = \ \text{gal}$ |
| <u>31.</u> | | |
| 32. | 31. 7 L = ml | 32. 350 L = kl |
| 33. | | |
| 34. | 33. 47 ml = L | 34. $0.97 \text{ kl} = _\L$ |
| 35. | | |
| 36. | 35. $0.126 \text{ kl} = ___L$ | 36. $75 \text{ ml} = ___L$ |
| 37. | | |
| 38 | 37. $\frac{1}{2}c = $ fl oz | 38. $\frac{3}{4}$ gal = c |

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7.4 Conversions Between the U.S. and Metric Systems

Objective A Converting Between the U.S. and Metric Systems

The metric system probably had its beginnings in France in the 1600s, but it was the Metric Act of 1866 that made the use of this system legal (but not mandatory) in the United States. Other laws have followed that allow for a slow, but deliberate, transfer to the modernized metric system. In April 2001, for example, the U.S. Stock Exchanges completed their change to decimal trading instead of fractions. By the end of 2009, all products sold in Europe (with some exceptions) were required to have only metric units on their labels. (*Source:* U.S. Metric Association and National Institute of Standards and Technology)

You may be surprised at the number of everyday items we use that are already manufactured in metric units. We easily recognize 1L and 2L soda bottles, but what about the following?

- Pencil leads (0.5 mm or 0.7 mm)
- Sporting events (5-km or 10-km races)
- Medicines (500-mg capsules)
- Labels on retail goods (dual-labeled since 1994)

Since the United States has not completely converted to the metric system, we need to practice converting from one system to the other. Below is a table of mostly approximate conversions.

| Length: | Capacity: | Weight (mass): |
|--|--|--|
| Metric U.S. System | n Metric U.S. System | Metric U.S. System |
| $1 \text{ m} \approx 1.09 \text{ yd}$ | $1 \text{ L} \approx 1.06 \text{ qt}$ | $1 \text{ kg} \approx 2.2 \text{ lb}$ |
| $1 \text{ m} \approx 3.28 \text{ ft}$ | $1 L \approx 0.26 \text{ gal}$ | $1 \text{ g} \approx 0.04 \text{ oz}$ |
| $1 \text{ km} \approx 0.62 \text{ mi}$ | $3.79 L \approx 1 \text{ gal}$ | $0.45 \text{ kg} \approx 1 \text{ lb}$ |
| 2.54 cm = 1 in. | $0.95 L \approx 1 qt$ | $28.35 \text{ g} \approx 1 \text{ oz}$ |
| $0.30 \text{ m} \approx 1 \text{ ft}$ | $29.57 \text{ ml} \approx 1 \text{ fl oz}$ | |

There are many ways to perform these metric-to-U.S. conversions. We will do so by using unit fractions.

Example 1

 $1.61 \text{ km} \approx 1 \text{ mi}$

Compact Discs

Standard-sized compact discs are 12 centimeters in diameter. Convert this length to inches. Round the result to two decimal places. (*Source:* usByte.com) $_{1.5 \text{ cm}}$

Solution: From our length conversion table, we know that 2.54 cm = 1 in. This fact gives us two unit fractions: $\frac{2.54 \text{ cm}}{1 \text{ in.}}$ and $\frac{1 \text{ in.}}{2.54 \text{ cm}}$. We use the unit fraction with cm in the denominator so that these units divide out.

$$12 \text{ cm} = \frac{12 \text{ cm}}{1} \cdot 1 = \frac{12 \text{ cm}}{1} \cdot \underbrace{\frac{11 \text{ in.}}{2.54 \text{ cm}}}_{\text{Coriginal units}} \leftarrow \text{Units to convert to} = \frac{12 \text{ cm}}{2.54 \text{ cm}} \leftarrow \text{Original units}$$
$$= \frac{12}{2.54} \text{ in.}$$
$$\approx 4.72 \text{ in.} \text{ Divide.} \qquad (Continued on next)$$

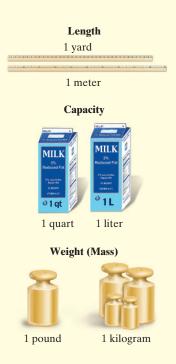
and Metric Systems. >

Pencil

Pencil

A Convert Between the U.S.

Objective



Practice 1

The center hole of a standard-sized compact disc is 1.5 centimeters in diameter. Convert this length to inches. Round the result to 2 decimal places.

Answer page) **1.** 0.59 in. Thus, the diameter of a standard compact disc is exactly 12 cm or approximately 4.72 inches. For a dimension this size, you can use a ruler to check. Another method is to approximate. Our result, 4.72 in., is close to 5 inches. Since 1 in. is about 2.5 cm, then 5 in. is about 5(2.5 cm) = 12.5 cm, which is close to 12 cm.

The liver is your largest internal organ. It weighs about 3.5 pounds in a grown man.

Convert this weight to kilograms. Round to the nearest tenth. (Source: Some Body!

Thus 3.5 pounds are approximately 1.6 kilograms. From the table of conversions, we know that 1 kg \approx 2.2 lb. So that means 0.5 kg \approx 1.1 lb and after adding, we

Unit fraction

Solution: $3.5 \text{ lb} \approx \frac{3.5 \text{ k}}{1} \cdot \frac{0.45 \text{ kg}}{1 \text{ k}} = 3.5(0.45 \text{ kg}) \approx 1.6 \text{ kg}$

Work Practice 1

Liver

have 1.5 kg \approx 3.3 lb. Our result is reasonable.

Postage Stamp

Australia converted to the metric system in 1973. In

that year, four postage stamps were issued to publi-

cize this conversion. One such stamp is shown. Let's check the mathematics on the stamp by converting

7 fluid ounces to milliliters. Round to the nearest

Rounded to the nearest hundred, 7 fl oz ≈ 200 ml.

Solution: $7 \text{ fl oz} \approx \frac{7 \text{ fl oz}}{1} \cdot \frac{29.57 \text{ ml}}{1 \text{ fl oz}}$

Unit fraction

= 7(29.57 ml) = 206.99 ml

Example 2

by Dr. Pete Rowan)

Work Practice 2

Example 3

hundred.

Work Practice 3

Practice 2

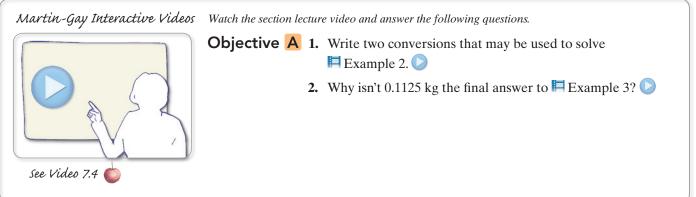
A full-grown human heart weighs about 8 ounces. Convert this weight to grams. If necessary, round your result to the nearest tenth of a gram.

Practice 3

Convert 237 ml to fluid ounces. Round to the nearest whole fluid ounce.

Answers 2. 226.8 g 3. 8 fl oz

Vocabulary, Readiness & Video Check



7c

Volume

Australia

Metric Conversion

floz

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7.4 Exercise Set MyLab Math

Note: Because approximations are used, your answers may vary slightly from the answers given in the back of the book.

Objective A *Convert as indicated. If necessary, round answers to two decimal places. See Examples 1 through 3.*

| 1. 756 milliliters to fluid ounces | 2. 18 liters to quarts | 03. 86 inches to centimeters |
|--|-----------------------------------|-------------------------------------|
| 4. 86 miles to kilometers | 5. 1000 grams to ounces | 6. 100 kilograms to pounds |
| 7. 93 kilometers to miles | 8. 9.8 meters to feet | 9. 14.5 liters to gallons |
| 10. 150 milliliters to fluid ounces | 11. 30 pounds to kilograms | 12. 15 ounces to grams |

Fill in the chart. Give exact answers or round to 1 decimal place. See Examples 1 through 3.

| (| | Meters | Yards | Centimeters | Feet | Inches |
|-----|----------------------------------|--------|-------|-------------|------|--------|
| 13. | The height of a woman | | | | 5 | |
| 14. | Statue of Liberty length of nose | 1.37 | | | | |
| 15. | Leaning Tower of Pisa | | 60 | | | |
| 16. | Blue whale | | 36 | | | |

Solve. If necessary, round answers to two decimal places. See Examples 1 through 3.

17. The balance beam for female gymnasts is 10 centimeters wide. Convert this width to inches.



- **19.** In many states, the maximum speed limit for recreational vehicles is 50 miles per hour. Convert this to kilometers per hour.
- **21.** Ibuprofen comes in 200-milligram tablets. Convert this to ounces. (Round your answer to this exercise to 3 decimal places.)

18. In men's gymnastics, the rings are 250 centimeters from the floor. Convert this height to inches, then to feet.



- **20.** In some states, the speed limit is 70 miles per hour. Convert this to kilometers per hour.
- **22.** Vitamin C tablets come in 500-milligram caplets. Convert this to ounces.

The 70-meter-diameter antenna is the largest and most sensitive Deep Space Network antenna. Use this for Exercises 23 through 26. (For more information about Deep Space Network, see the Chapter 8 Opener.)



27. A stone is a unit in the British customary system. Use the conversion 14 pounds = 1 stone to check the equivalencies in this 1973 Australian stamp. Is 100 kilograms approximately 15 stone 10 pounds?



- **29.** The Monarch butterfly migrates annually between the northern United States and central Mexico. The trip is about 4500 km long. Convert this to miles.
- **31.** A $3\frac{1}{2}$ -inch diskette is not really $3\frac{1}{2}$ inches. To find its actual width, convert this measurement to centimeters, then to millimeters. Round the result to the nearest ten.
- 33. For an average adult, the weight of the right lung is greater than the weight of the left lung. If the right lung weighs 1.5 pounds and the left lung weighs 1.25 pounds, find the difference in grams. (*Source: Some Body!*)
 - **35.** A fast sneeze has been clocked at about 167 kilometers per hour. Convert this to miles per hour. Round to the nearest whole.
 - **37.** The General Sherman giant sequoia tree has a diameter of about 8 meters at its base. Convert this to feet. (*Source: Fantastic Book of Comparisons*)
 - **39.** The total length of the track on a CD is about 4.5 kilometers. Convert this to miles. Round to the nearest whole mile.

- **23.** Convert 70 meters to feet.
- **24.** The Deep Space Network sites also have a 26-meter antenna. Convert 26 meters to feet.
- **25.** The 70-meter-diameter antenna can track a spacecraft traveling more than 16 billion kilometers from Earth. Convert this distance to miles.
- 26. The dish reflector and the mount atop the concrete pedestal of the 70-meter antenna weigh nearly 2.7 million kilograms. Convert this number to tons.
- **28.** Convert 5 feet 11 inches to centimeters and check the conversion on this 1973 Australian stamp. Is it correct?



- **30.** There is a species of African termite that builds nests up to 18 ft high. Convert this to meters.
- **32.** The average two-year-old is 84 centimeters tall. Convert this to feet and inches.
- **34.** The skin of an average adult weighs 9 pounds and is the heaviest organ. Find the weight in grams. (*Source: Some Body!*)
- **36.** A Boeing 747 has a cruising speed of about 980 kilometers per hour. Convert this to miles per hour. Round to the nearest whole.
- **38.** The largest crater on the near side of the moon is Billy Crater. It has a diameter of 303 kilometers. Convert this to miles. (*Source: Fantastic Book of Comparisons*)
- **40.** The distance between Mackinaw City, Michigan, and Cheyenne, Wyoming, is 2079 kilometers. Convert this to miles. Round to the nearest whole mile.

41. A doctor orders a dosage of 5 ml of medicine every **42.** A doctor orders a dosage of 12 ml of medicine 4 hours for 1 week. How many fluid ounces of every 6 hours for 10 days. How many fluid ounces of medicine should be purchased? Round up to the medicine should be purchased? Round up to the next next whole fluid ounce. whole fluid ounce. Without actually converting, choose the most reasonable answer. **44.** A mile is ______ a kilometer. **43.** This math book has a height of about _____. **b.** 28 cm **a.** 28 mm **a.** shorter than **b.** longer than **c.** 28 m **d.** 28 km **c.** the same length as **45.** A liter has _____ capacity than a quart. **46.** A foot is ______ a meter. a. less **b.** greater **a.** shorter than **b.** longer than **c.** the same **c.** the same length as **47.** A kilogram weighs ______ a pound. **48.** A football field is 100 yards, which is about **b.** less than **a.** the same as **b.** 90 m **a.** 9 m **c.** more than **c.** 900 m **d.** 9000 m **49.** An $8\frac{1}{2}$ -ounce glass of water has a capacity of about **50.** A 5-gallon gasoline can has a capacity of about **a.** 19 L **b.** 1.9 L **a.** 250 L **b.** 25 L **d.** 1.9 ml **d.** 250 ml **c.** 19 ml **c.** 2.5 L **51.** The weight of an average man is about _____. **52.** The weight of a pill is about _____ **b.** 7 kg **a.** 700 kg **a.** 200 kg **b.** 20 kg **c.** 0.7 kg **d.** 70 kg **d.** 200 mg **c.** 2 kg Review Perform the indicated operations. See Section 1.9. **53.** $6 \cdot 4 + 5 \div 1$ **54.** $10 \div 2 + 9(8)$ **55.** $\frac{10 + 8}{10 - 8}$ **56.** $\frac{14 + 1}{5(3)}$ **57.** 3 + 5(19 - 17) - 8 **58.** 1 + 4(19 - 9) + 5 **59.** $3[(1 + 5) \cdot (8 - 6)]$ **60.** 5[(18 - 8) - 9]

Concept Extensions

Body surface area (BSA) is often used to calculate dosages for some drugs. BSA is calculated in square meters using a person's weight and height.

$$BSA = \sqrt{\frac{(\text{weight in } kg) \times (\text{height in } cm)}{3600}}$$

For Exercises 61 through 66, calculate the BSA for each person. Round to the nearest hundredth. You will need to use the square root key on your calculator.

- **61.** An adult whose height is 182 cm and weight is 90 kg.
- **63.** A child whose height is 50 in. and weight is 40 kg. (*Hint:* Don't forget to first convert inches to centimeters)
- **62.** An adult whose height is 157 cm and weight is 63 kg.
- **64.** A child whose height is 26 in. and weight is 13 kg.

65. An adult whose height is 60 in. and weight is 150 lb.

Solve.

- **67.** Suppose the adult from Exercise **61** is to receive a drug that has a recommended dosage range of 10–12 mg per sq meter. Find the dosage range for the adult.
- **69.** A handball court is a rectangle that measures 20 meters by 40 meters. Find its area in square meters and square feet.

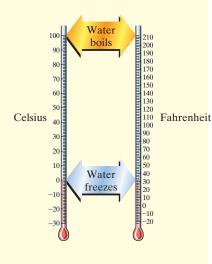
- **66.** An adult whose height is 69 in. and weight is 172 lb.
- **68.** Suppose the child from Exercise **64** is to receive a drug that has a recommended dosage of 30 mg per sq meter. Find the dosage for the child.
- **70.** A backpack measures 16 inches by 13 inches by 5 inches. Find the volume of a box with these dimensions. Find the volume in cubic inches and cubic centimeters. Round the cubic centimeters to the nearest whole cubic centimeter.

7.5 Temperature: U.S. and Metric Systems of Measurement

Objectives

A Convert Temperatures from Degrees Celsius to Degrees Fahrenheit.

B Convert Temperatures from Degrees Fahrenheit to Degrees Celsius.



When Gabriel Fahrenheit and Anders Celsius independently established units for temperature scales, each based his unit on the heat of water the moment it boils compared to the moment it freezes. One degree Celsius is 1/100 of the difference in heat. One degree Fahrenheit is 1/180 of the difference in heat. Celsius arbitrarily labeled the temperature at the freezing point at 0°C, making the boiling point 212°F. Water boils at 212°F and 100°C.

By comparing the two scales in the figure, we see that a 20°C day is as warm as a 68°F day. Similarly, a sweltering 104°F day in the Mojave Desert corresponds to a 40°C day.

Concept Check Which of the following statements is correct? Explain.

a. 6°C is below the freezing point of water.

b. 6°F is below the freezing point of water.

Objective A Converting Degrees Celsius to Degrees Fahrenheit 🕗

To convert from Celsius temperatures to Fahrenheit temperatures, we can use either of the equations in the box below.

Converting Celsius to Fahrenheit

$$F = \frac{9}{5} \cdot C + 32$$
 or $F = 1.8 \cdot C + 32$

(To convert to Fahrenheit temperature, multiply the Celsius temperature by $\frac{9}{5}$ or 1.8, and then add 32.)

In these equations, we use the symbol F to represent degrees Fahrenheit and the symbol C to represent degrees Celsius.

Concept Check Answer

Example 1 Convert 15°C to degrees Fahrenheit.

Solution:
$$F = \frac{9}{5} \cdot C + 32$$

 $= \frac{9}{5} \cdot 15 + 32$ Replace C with 15.
 $= 27 + 32$ Simplify.
 $= 59$ Add.

Thus, 15°C is equivalent to 59°F.

Work Practice 1

Example 2 Convert 29°C to degrees Fahrenheit.

Solution: $F = 1.8 \cdot C + 32$ = $1.8 \cdot 29 + 32$ Replace C with 29. = 52.2 + 32 Multiply 1.8 by 29. = 84.2 Add.

Therefore, 29°C is the same as 84.2°F.

Work Practice 2

Objective **B** Converting Degrees Fahrenheit to Degrees Celsius

To convert from Fahrenheit temperatures to Celsius temperatures, see the box below. The symbol C represents degrees Celsius and the symbol F represents degrees Fahrenheit.

Converting Fahrenheit to Celsius

$$C = \frac{5}{9}(F - 32)$$

(To convert to Celsius temperature, subtract 32 from the Fahrenheit temperature, and then multiply by $\frac{5}{9}$.)

Example 3

Convert 59°F to degrees Celsius.

Solution: We evaluate the formula
$$C = \frac{5}{9}(F - 32)$$
 when F is 59.
 $C = \frac{5}{9}(F - 32)$
 $= \frac{5}{9} \cdot (59 - 32)$ Replace F with 59.
 $= \frac{5}{9} \cdot (27)$ Subtract inside parentheses.
 $= 15$ Multiply

Therefore, 59° F is the same temperature as 15° C.

Work Practice 3

(Compare the results of Examples 1 and 3.)

Practice 1

Convert 50°C to degrees Fahrenheit.

Practice 2

An Australian stamp is shown with degrees Celsius and equivalent degrees Fahrenheit. Convert 38°C to degrees Fahrenheit to check the accuracy of the stamp. Round your answer to the nearest whole.



Practice 3

Convert 68°F to degrees Celsius.

Practice 4

Convert 113°F to degrees Celsius. If necessary, round to the nearest tenth of a degree.

Practice 5

During a bout with the flu, Albert's temperature reaches 102.8°F. What is his temperature measured in degrees Celsius? Round to the nearest tenth of a degree.

Answers 4. 45°C **5.** 39.3°C

Concept Check Answer

She used the conversion for Celsius to Fahrenheit instead of Fahrenheit to Celsius.



Convert 114°F to degrees Celsius. If necessary, round to the nearest tenth of a degree.

Solution:
$$C = \frac{5}{9}(F - 32)$$

 $= \frac{5}{9}(114 - 32)$ Replace F with 114.
 $= \frac{5}{9} \cdot (82)$ Subtract inside parentheses.
 ≈ 45.6 Multiply.

Therefore, 114°F is approximately 45.6°C.

Work Practice 4

Example 5 Body Temperature

Normal body temperature is 98.6°F. What is this temperature in degrees Celsius?

Solution: We evaluate the formula $C = \frac{5}{9}(F - 32)$ when F is 98.6.

 $C = \frac{5}{9}(F - 32)$ = $\frac{5}{9}(98.6 - 32)$ Replace F with 98.6. = $\frac{5}{9} \cdot (66.6)$ Subtract inside parentheses. = 37 Multiply.

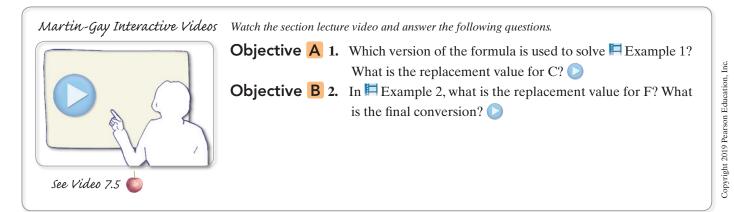
Therefore, normal body temperature is 37°C.

Work Practice 5

Concept Check Clarissa must convert 40°F to degrees Celsius. What is wrong with her work shown below?

 $F = 1.8 \cdot C + 32$ $F = 1.8 \cdot 40 + 32$ F = 72 + 32F = 104

Vocabulary, Readiness & Video Check



7.5 Exercise Set MyLab Math 🕗

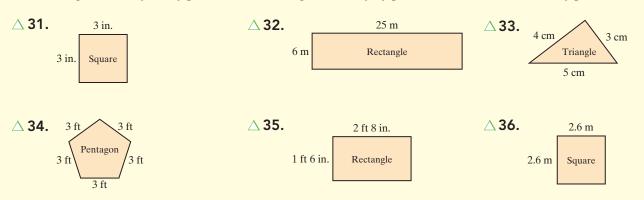
to be set.

Objectives A B Mixed Practice *Convert as indicated. When necessary, round to the nearest tenth of a degree. See Examples 1 through 5.*

| 1. | 41°F to degrees Celsius | 2. | 68°F to degree | es Cel | sius | 3. | 104°F to degrees Celsius |
|--------------|--|--------------------------|------------------------------------|--------|---|---------------|---|
| ₽4. | 77°F to degrees Celsius | 5. | 60°C to degree | es Fal | renheit | 6. | 80°C to degrees Fahrenheit |
| 7. | 115°C to degrees Fahrenheit | 8. | 35°C to degree | es Fał | renheit | 9. | 62°F to degrees Celsius |
| 10. | 182°F to degrees Celsius | 11. | 142.1°F to deg | rees (| Celsius | 12. | 43.4°F to degrees Celsius |
| 13. | 92°C to degrees Fahrenheit | | | 14. | 75°C to degrees | Fahr | renheit |
| 15. | 16.3°C to degrees Fahrenheit | | | 16. | 48.6°C to degree | es Fa | hrenheit |
| 17. | The hottest temperature ever recor
Mexico was 122°F. Convert this tem
degrees Celsius. (<i>Source:</i> National C
Center) | pera | ture to | 18. | Island was 104°I | F. Co | ture ever recorded in Rhode
nvert this temperature to
<i>urce:</i> National Climatic Data |
| 0 19. | A weather forecaster in Caracas pro-
temperature of 27°C. Find this mea
degrees Fahrenheit. | | | 20. | ture of 22°C flas | sh on
cori | k, Alan Olda notices a tempera-
the local bank's temperature
responding temperature in |
| 21. | Water boils at 212°F. Find this temp degrees Celsius. | eratu | ıre in | 22. | Water freezes at
degrees Fahrenh | | . Find this temperature in |
| 23. | Najib Tan is running a fever of 100.
temperature as it would be shown of
thermometer. | | | 24. | William Saylor g
ture of 98.2°F. F
on a Celsius the | ind v | rally has a subnormal tempera-
what this temperature would be neter. |
| 25. | In a European cookbook, a recipe r
ingredients for caramels to be heat
the cook has access only to a Fahre
eter. Find the temperature in degre
that should be used to make the car | ed to
nheit
es Fal | 118°C, but
thermom-
hrenheit | 26. | 127°C, but the c | andy
to d | livinity should be heated to
thermometer that Myung Kim
egrees Fahrenheit. Find how hot
gredients. |
| 27. | The surface temperature of Venus of Find this temperature in degrees Co | | | 28. | | the | Earth's core is estimated to corresponding temperature in |
| 29. | At Mack Trucks' headquarters, the
perature is to be set at 70°F, but the
calibrated in degrees Celsius. Find t | ther | mostat is | 30. | | ed to | at Merck, Sharp, and Dohm
66°F. Find the corresponding
ees Celsius. |

Review

Find the perimeter of each figure. Recall that the perimeter of a figure is the distance around the figure. See Section 1.3.



Concept Extensions

Solve. See the first Concept Check in this section. True or false?

- **37.** 10°F is above the freezing point of water.
- **39.** 102°C is above the boiling point of water.
- **41.** In August 2012, at the Cern, Large Hadron Collider in Switzerland, the highest temperature in a laboratory was achieved. The temperature was approximately 9,000,000,000°F. Convert this temperature to degrees Celsius. (*Note:* This is 250,000 times hotter than the center of the sun.) (*Source: Guinness Book of World Records*)
- **38.** 10°C is above the freezing point of water.
- **40.** 102°F is above the boiling point of water.
- **42.** The hottest-burning substance known is carbon subnitride. Its flame at one atmospheric pressure reaches 9010°F. Convert this temperature to degrees Celsius. (*Source: Guinness Book of Records*)

Determine whether the measurement in each statement is reasonable by answering yes or no.

- 43. A 72°F room feels comfortable.
 44. Water heated to 110°F will boil.
 45. Josiah has a fever if a thermometer shows his temperature to be 40°F.
 46. An air temperature of 20°F on a Vermont ski slope can be expected in the winter.
 47. When the temperature is 30°C outside, an overcoat is needed.
 48. An air-conditioned room at 60°C feels quite chilly.
 49. Barbara has a fever when a thermometer records her temperature at 40°C.
 50. Water cooled to 32°C will freeze.
- **51.** In your own words, describe how to convert from degrees Celsius to degrees Fahrenheit.
- **52.** In your own words, describe how to convert from degrees Fahrenheit to degrees Celsius.

7.6 Energy: U.S. and Metric Systems of Measurement

Many people think of energy as a concept that involves movement or activity. However, **energy** is defined as "the capacity to do work." Often energy is stored, awaiting use at some later point in time.

Objective A Defining and Using U.S. System Units of Energy

In the U.S. system of measurement, energy is commonly measured in foot-pounds. One **foot-pound (ft-lb)** is the amount of energy needed to move or lift a 1-pound object a distance of 1 foot. To determine the amount of energy necessary to move a 50-pound weight a distance of 100 feet, we simply multiply these numbers. That is,

 $50 \text{ pounds} \cdot 100 \text{ feet} = 5000 \text{ ft-lb of energy}$

Example 1

Finding the Amount of Energy Needed to Move a Carton

An employee for the Jif Peanut Butter company must lift a carton of peanut butter jars 16 feet to the top of the warehouse. In the carton are 24 jars, each of which weighs 1.125 pounds. How much energy is required to lift the carton?

Solution: First we determine the weight of the carton.

weight of carton = weight of a jar \cdot number of jars

 $= 1.125 \text{ pounds} \cdot 24$

= 27 pounds

Thus, the carton weighs 27 pounds.

To find the energy needed to move the 27-pound carton, we multiply the weight times the distance.

energy = $27 \text{ pounds} \cdot 16 \text{ feet} = 432 \text{ ft-lb}$

Thus, 432 ft-lb of energy are required to lift the carton.

Work Practice 1

✓ Concept Check Suppose you would like to find how many foot-pounds of energy are needed to move an object weighing 12 ounces a total of 14 yards. What adjustments should you make before computing the answer? Next, compute the answer.

Another form of energy is heat. In the U.S. system of measurement, heat is measured in **British Thermal Units (BTU).** A BTU is the amount of heat required to raise the temperature of 1 pound of water 1 degree Fahrenheit. To relate British Thermal Units to foot-pounds, we need to know that

1 BTU = 778 ft-lb

Objectives

A Define and Use U.S. Units of Energy and Convert from One Unit to Another.



Practice 1

Three bales of cardboard must be moved 340 feet. If each bale weighs 63 pounds, find the amount of work required to move the cardboard.

Answer 1. 64,260 ft-lb

Concept Check Answer convert 12 ounces to 0.75 pound and 14 yards to 42 feet; answer: 31.5 ft-lb

Practice 2

The FC-5 model furnace produced by Raywall uses 17,065 BTU every hour. Convert this energy requirement to foot-pounds.



Practice 3

It takes 30 calories each hour for Alan to fly a kite. How many calories will he use if he flies his kite for 2 hours?

Practice 4

It takes 200 calories for Melanie to play Frisbee for an hour. How many calories will she use playing Frisbee for an hour each day for 5 days?

Answers

2. 13,276,570 ft-lb **3.** 60 cal

4. 1000 cal



2 Converting BTU to Foot-Pounds

The Raywall Company produces several different furnace models. Their FC-4 model requires 13,652 BTU every hour to operate. Convert the required energy to foot-pounds.

Solution:

To convert BTU to foot-pounds, we multiply by the unit fraction $\frac{778 \text{ ft-lb}}{1 \text{ BTU}}$.

$$13,652 \text{ BTU} = 13,652 \text{ BFU} \cdot \frac{778 \text{ ft-lb}}{1 \text{ BFU}}$$

= 10,621,256 ft-lb

Thus, 13,652 BTU is equivalent to 10,621,256 ft-lb.

Work Practice 2

Objective **B** Defining and Using Metric System Units of Energy ()

In the metric system, heat is measured in calories. A **calorie (cal)** is the amount of heat required to raise the temperature of 1 kilogram of water 1 degree Celsius.

The fact that an apple contains 70 calories means that 70 calories of heat energy are stored in our bodies whenever we eat an apple. This energy is stored in fat tissue and is burned (or "oxidized") by our bodies when we require energy to do work. We need 20 calories each hour just to stand still. This means that 20 calories of heat energy will be burned by our bodies each hour that we spend standing.

Example 3 Finding the Number of Calories Needed

It takes 20 calories for Jim to stand for 1 hour. How many calories does he use when standing for 3 hours at a crowded party?

Solution: We multiply the number of calories used in 1 hour by the number of hours spent standing.

total calories = $20 \cdot 3 = 60$ calories

Therefore, Jim uses 60 calories to stand for 3 hours at the party.

Work Practice 3

Example 4 Finding the Number of Calories Needed

It takes 115 calories for Kathy to walk slowly for 1 hour. How many calories does she use walking slowly for 1 hour a day for 6 days?

Solution: We multiply the total number of calories used in 1 hour each day by the number of days.

total calories = $115 \cdot 6 = 690$ calories

Therefore, Kathy uses 690 calories walking slowly for 1 hour for 6 days.

Work Practice 4

Example 5 Finding the Number of Calories Needed

It requires 100 calories to play a game of cards for an hour. If Jason plays poker for 1.5 hours each day for 5 days, how many calories are required?

Solution: We first determine the number of calories Jason uses each day to play poker.

calories used each day = 100(1.5) = 150 calories

Then we multiply the number of calories used each day by the number of days.

calories used for 5 days = $150 \cdot 5 = 750$ calories

Thus, Jason uses 750 calories to play poker for 1.5 hours each day for 5 days.

Work Practice 5

Calories burned during exercise are affected by your body weight, the intensity of your workout, personal metabolism, and other factors. For example, the table below is for a 155-pound person.

| 1 Hour of Activity | Calories Burned |
|------------------------|-----------------|
| Raking lawn | 281 |
| Cross-country hiking | 422 |
| Golf (pulling clubs) | 352 |
| Ballroom dancing | 387 |
| Fishing | 281 |
| Playing catch football | 141 |
| Walking briskly | 281 |
| Running in general | 563 |
| Cleaning house | 246 |

Practice 5

To play volleyball for an hour requires 300 calories. If Martha plays volleyball 1.25 hours each day for 4 days, how many calories does Martha use?

Answer 5. 1500 calories

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank.

calorie energy British Thermal Unit foot-pound

1. ______ is defined as "the capacity to do work."

2. The amount of energy needed to move a 1-pound object a distance of 1 foot is called a(n)

3. The amount of heat required to raise the temperature of 1 pound of water 1 degree Fahrenheit is called a(n) ______.

4. The amount of heat required to raise the temperature of 1 kilogram of water 1 degree Celsius is called a(n) ______.

Solve mentally, without use of a pencil and paper or calculator.

- **5.** How many foot-pounds of energy are needed to move a 6-pound object 5 feet?
- **6.** How many foot-pounds of energy are needed to move a 10-pound object 4 feet?
- **7.** How many foot-pounds of energy are needed to lift a 3-pound object 20 feet?
- **8.** How many foot-pounds of energy are needed to lift a 5-pound object 9 feet?

- **9.** If 30 calories are burned by the body in 1 hour, how many calories are burned (at the same rate) in 3 hours?
- 11. If 20 calories are burned by the body in 1 hour, how many calories are burned (at the same rate) in $\frac{1}{4}$ of an hour?
- **10.** If 15 calories are burned by the body in 1 hour, how many calories are burned (at the same rate) in 2 hours?
- 12. If 50 calories are burned by the body in 1 hour, how many calories are burned (at the same rate) in $\frac{1}{2}$ of an hour?

| Martin-Gay Interactive Videos | Watch the section lecture | video and answer the following questions. |
|-------------------------------|---------------------------|--|
| See Video 7.6 | | Complete this statement based on the lecture before
Example 2: In the system of measurement, heat
is measured in Thermal Units (BTU). A BTU is
the amount of heat required to raise the temperature
of 1 of water 1 degree
Complete this statement based on the lecture before
Example 3: In the system of measurement, heat
is measured in (cal). A cal is the amount of heat
required to raise the temperature of 1 of water
1 degree |

7.6 Exercise Set MyLab Math 🜔

Objective A *Solve. See Examples 1 and 2.*

- 1. How much energy is required to lift a 3-pound math textbook 380 feet up a hill?
 - **3.** How much energy is required to lift a 168-pound person 22 feet?
 - **5.** How many foot-pounds of energy are needed to take 2.5 tons of topsoil 85 feet from the pile delivered by the nursery to the garden?
- **•7.** Convert 30 BTU to foot-pounds.
 - **9.** Convert 1000 BTU to foot-pounds.
- **11.** A 20,000-BTU air conditioner requires how many foot-pounds of energy to operate?
- **13.** The Raywall model FC-10 heater uses 34,130 BTU each hour to operate. How many foot-pounds of energy does it use each hour?
- **15.** 8,000,000 ft-lb is equivalent to how many BTU, rounded to the nearest whole number?

- **2.** How much energy is required to move a 20-pound sack of potatoes 55 feet?
- **4.** How much energy is needed to move a 2250-pound car a distance of 45 feet?
- **6.** How many foot-pounds of energy are needed to move 4.25 tons of coal 16 feet into a new coal bin?
- **8.** Convert 50 BTU to foot-pounds.
- **10.** Convert 10,000 BTU to foot-pounds.
- **12.** A 24,000-BTU air conditioner requires how many foot-pounds of energy to operate?
- **14.** The Raywall model FC-12 heater uses 40,956 BTU each hour to operate. How many foot-pounds of energy does it use each hour?
- **16.** 450,000 ft-lb is equivalent to how many BTU, rounded to the nearest whole number?

Objective B Solve. See Examples 3 through 5.

- **17.** While walking slowly, Janie Gaines burns 115 calories each hour. How many calories does she burn if she walks slowly for an hour every day of the week?
- ▶ 19. Approximately 300 calories are burned each hour skipping rope. How many calories are required to skip rope $\frac{1}{2}$ of an hour each day for 5 days?
 - **21.** Julius Davenport goes through a rigorous exercise routine each day. He burns calories at a rate of 720 calories per hour. How many calories does he need to exercise 20 minutes per day, 6 days a week?
 - **23.** A casual stroll burns 165 calories per hour. How long will it take to stroll off the 425 calories contained in a hamburger, to the nearest tenth of an hour?
 - **25.** One pound of body weight is lost whenever 3500 calories are burned off. If walking briskly burns 200 calories for each mile walked, how far must Sheila Osby walk to lose 1 pound?

- **18.** Dancing burns 270 calories per hour. How many calories are needed to go dancing an hour a night for 3 nights?
- **20.** Ebony Jordan burns 360 calories per hour while riding her stationary bike. How many calories does she burn when she rides her bicycle $\frac{1}{4}$ of an hour each day for 6 days?
- **22.** A roller skater can easily use 325 calories per hour while skating. How many calories are needed to roller skate 75 minutes per day for 3 days?
- **24.** Even when asleep, the body burns 15 calories per hour. How long must a person sleep to burn off the calories in an 80-calorie orange, to the nearest tenth of an hour?
- **26.** Bicycling can burn as much as 500 calories per hour. How long must a person ride a bicycle at this rate to use up the 3500 calories needed to lose 1 pound?

Review

 Subtract. See Section 1.4.

 27. 90 - 17
 28. 90 - 49

 29. 180 - 17
 30. 180 - 49
 31. 180 - 161
 32. 180 - 101

Concept Extensions

- **33.** A 123.9-pound pile of prepacked canned goods must be lifted 9 inches to permit a door to close. How much energy is needed to do the job?
- **35.** 6400 ft-lb of energy were needed to move an anvil 25 feet. Find the weight of the anvil.
- **37.** In your own words, define calorie.

- **34.** A 14.3-pound framed picture must be lifted 6 feet 3 inches. How much energy is required to move the picture?
- **36.** 825 ft-lb of energy were needed to move 40 pounds of apples to a new container. How far were the apples moved?

Chapter 7 Group Activity

Speeds

Section 7.1

A speed measures how far something travels in a given unit of time. You already learned in Section 5.2 that the speed 55 miles per hour is a rate that can be written as 55 miles

 $\frac{35 \text{ mmes}}{1 \text{ hour}}$. Just as there are different units of measure-

ment for length or distance, there are different units of measurement for speed as well. It is also possible to perform unit conversions on speeds. Before we learn about converting speeds, we will review units of time. The following is a summary of equivalencies between various units of time.

| Units of Time | Unit Fractions |
|--|---|
| $60 \text{ seconds } (s) = 1 \text{ minute } (\min)$ | $\frac{60 \text{ s}}{1 \text{ min}} = \frac{1 \text{ min}}{60 \text{ s}} = 1$ |
| 60 minutes = 1 hour (h) | $\frac{60\min}{1\text{ h}} = \frac{1\text{ h}}{60\min} = 1$ |
| 3600 seconds = 1 hour | $\frac{3600 \text{ s}}{1 \text{ h}} = \frac{1 \text{ h}}{3600 \text{ s}}$ |

Here are some common speeds.

Speeds

Miles per hour (mph) Miles per minute (mi/min) Miles per second (mi/s) Feet per second (ft/s) Feet per minute (ft/min) Kilometers per hour (kmph or km/h) Kilometers per second (kmps or km/s) Meters per second (m/s) Knots To convert from one speed to another, unit fractions may be used. To convert from mph to ft/s first write the original speed as a unit rate. Then multiply by a unit fraction that relates miles to feet and by a unit fraction that relates hours to seconds. The unit fractions should be written so that like units will divide out. For example, to convert 55 mph to ft/s:

$$55 \text{ mph} = \frac{55 \text{ miles}}{1 \text{ hour}} = \frac{55 \text{ miles}}{1 \text{ hour}} \cdot \frac{5280 \text{ ft}}{1 \text{ mile}} \cdot \frac{1 \text{ hour}}{3600 \text{ s}}$$
$$= \frac{55 \cdot 5280 \text{ ft}}{3600 \text{ s}}$$
$$= \frac{290,400 \text{ ft}}{3600 \text{ s}}$$
$$= 80\frac{2}{3} \text{ ft/s}$$

Group Activity

- **1.** Research the current world land speed record. Convert the speed from mph to feet per second.
- **2.** Research the current world water speed record. Convert from mph to knots.
- **3.** Research and then describe the Beaufort Wind Scale, its origins, and how it is used. Give the scale keyed to both miles per hour and knots. Why would both measures be useful?

Helpful

A **knot** is 1 nautical mile per hour and is a measure of speed used for ships.

1 nautical mile (nmi) \approx 1.15 miles (mi) 1 nautical mile (nmi) \approx 6076.12 feet (ft)

Chapter 7 Vocabulary Check

Fill in each blank with one of the words or phrases listed below.

| ma | | ons gram | energy | weight |
|---|--|--|---|---|
| me | | calorie | British Therma | al Unit |
| 2 3. The 4. To 5. A(1 6 7. In t is th 1 p 8. The me 9. In t | e basic unit of leng
convert from one
n) | th in the metric sys
unit of length to an
is the basic
is the capacity to
neasurement, $a(n)$
required to raise the
gree Fahrenheit.
is the basic u
a(n)
red to raise the tem | ne amount of subs
tem is the
other,
unit of mass in the
o do work.
e temperature of
unit of capacity in
is the | may be used. e metric system. Helpful Hint • Are you preparing for your test? To help, don't forget to take these: • Chapter 7 Getting Ready for the Test on page 499 |

7 Chapter Highlights

| Definitions and Concepts | Examples | |
|---|--|--|
| Section 7.1 Length: U.S. and I | Vetric Systems of Measurement | |
| To convert from one unit of length to another, multiply by a unit fraction in the form | $\frac{12 \text{ inches}}{1 \text{ foot}}, \frac{1 \text{ foot}}{12 \text{ inches}}, \frac{3 \text{ feet}}{1 \text{ yard}}$ | |
| $\frac{\text{units to convert to}}{\text{original units}}$ Length: U.S. System of Measurement $12 \text{ inches (in.)} = 1 \text{ foot (ft)} \\3 \text{ feet} = 1 \text{ yard (yd)} \\5280 \text{ feet} = 1 \text{ mile (mi)}$ The basic unit of length in the metric system is the meter. A meter is slightly longer than a yard. Length: Metric System of Measurement $\frac{\text{Metric Unit of Length}}{1 \text{ kilometer (km)} = 1000 \text{ meters (m)}} \\1 \text{ hectometer (hm)} = 10 \text{ m}} \\1 \text{ dekameter (dam)} = 1 \text{ m}} \\1 \text{ decimeter (dm)} = 1/10 \text{ m or } 0.1 \text{ m}}$ | Convert 6 feet to inches.
$6 \text{ ft} = \frac{6 \text{ ft}}{1} \cdot 1$ $= \frac{6 \text{ ft}}{1} \cdot \frac{12 \text{ in.}}{1 \text{ ft}} \leftarrow \text{units to convert to}$ $= 6 \cdot 12 \text{ in.}$ $= 72 \text{ in.}$ Convert 3650 centimeters to meters.
$3650 \text{ cm} = 3650 \text{ cm} \cdot 1$ $= \frac{3650 \text{ cm}}{1} \cdot \frac{0.01 \text{ m}}{1 \text{ cm}} = 36.5 \text{ m}$ or
km hm dam m dm cm mm
2 units to the left
3650 cm = 36.5 m 2 places to the left | |

| Definitions and Concepts | Examples |
|--|--|
| · · · · · · · · · · · · · · · · · · · | S. and Metric Systems of Measurement |
| Weight is really a measure of the pull of gravity. Mass is a measure of the amount of substance in an object and does not change. | - |
| Weight: U.S. System of Measurement | Convert 5 pounds to ounces. |
| 16 ounces (oz) = 1 pound (1b)
2000 pounds = 1 ton | $5 \text{ lb} = 5 \text{ lb} \cdot 1 = \frac{5 \text{ lb}}{1} \cdot \frac{16 \text{ oz}}{1 \text{ lb}} = 80 \text{ oz}$ |
| A gram is the basic unit of mass in the metric system.It is the mass of water contained in a cube 1 centimeter on each side. A paper clip weighs about 1 gram.Mass: Metric System of Measurement | Convert 260 grams to kilograms.
$260 \text{ g} = \frac{260 \text{ g}}{1} \cdot 1 = \frac{260 \text{ g}}{1} \cdot \frac{1 \text{ kg}}{1000 \text{ g}} = 0.26 \text{ kg}$ |
| Metric Unit of Mass 1 kilogram (kg) = 1000 grams (g) 1 hectogram (hg) = 100 g 1 dekagram (dag) = 10 g 1 gram (g) = 1 g 1 decigram (dg) = 1/10 g or 0.1 g 1 centigram (cg) = 1/100 g or 0.01 g 1 milligram (mg) = 1/1000 g or 0.001 g | or
kg hg dag g dg cg mg $3 units to the left$ $260 g = 0.260 kg$ $3 places to the left$ |
| Section 7.3 Capacity: U.S. a | nd Metric Systems of Measurement |
| Capacity: U.S. System of Measurement | Convert 5 pints to gallons. |
| 8 fluid ounces (fl oz) = $1 \text{ cup } (c)$ | 1 gal = 4 qt = 8 pt |
| 2 cups = 1 pint (pt) | 5 pt 1 gal 5 |

2 cups = 1 pint (pt)2 pints = 1 quart (qt)4 quarts = 1 gallon (gal)

The liter is the basic unit of capacity in the metric system. It is the capacity or volume of a cube measuring 10 centimeters on each side. A liter of liquid is slightly more than 1 quart.

Capacity: Metric System of Measurement

| Metric Unit of Capacity |
|---|
| 1 kiloliter (kl) = 1000 liters (L) |
| 1 hectoliter (hl) = 100 L |
| 1 dekaliter (dal) = 10 L |
| 1 liter (L) = 1 L |
| 1 deciliter (dl) = $1/10 L \text{ or } 0.1 L$ |
| 1 centiliter (cl) = $1/100 \text{ L}$ or 0.01 L |
| 1 milliliter (ml) = 1/1000 L or 0.001 L |
| |

1 gal = 4 qt = 8 pt
5 pt = 5 pt
$$\cdot$$
 1 = $\frac{5 \text{ pt}}{1} \cdot \frac{1 \text{ gal}}{8 \text{ pt}} = \frac{5}{8} \text{ gal}$

Convert 1.5 liters to milliliters.

$$1.5 \text{ L} = \frac{1.5 \text{ L}}{1} \cdot 1 = \frac{1.5 \text{ L}}{1} \cdot \frac{1000 \text{ ml}}{1 \text{ L}} = 1500 \text{ ml}$$

or
kl hl dal L dl cl ml
3 units to the right

$$1.500 \text{ L} = 1500 \text{ ml}$$
3 places to the right

| Definitions and Concepts | Examples | | | | |
|---|--|--|--|--|--|
| Section 7.4 Conversions Between the U.S. and Metric Systems | | | | | |
| To convert between systems, use approximate unit fractions. See page 475. | Convert 7 feet to meters.
$7 \text{ ft} \approx \frac{7 \text{ ft}}{1} \cdot \frac{0.30 \text{ m}}{1 \text{ ft}} = 2.1 \text{ m}$ | | | | |
| | Convert 8 liters to quarts. | | | | |
| | $8 L \approx \frac{8 \mathcal{L}}{1} \cdot \frac{1.06 \text{ qt}}{1 \mathcal{L}} = 8.48 \text{ qt}$ | | | | |
| | Convert 363 grams to ounces. | | | | |
| | $363 \text{ g} \approx \frac{363 \text{ g}}{1} \cdot \frac{0.04 \text{ oz}}{1 \text{ g}} = 14.52 \text{ oz}$ | | | | |
| Section 7.5 Temperature: U.S. an | d Metric Systems of Measurement | | | | |
| To Convert from Celsius Temperature to Fahrenheit
Temperature | Convert 35°C to degrees Fahrenheit. | | | | |
| $F = \frac{9}{5} \cdot C + 32$ or $F = 1.8 \cdot C + 32$ | $\mathbf{F} = \frac{9}{5} \cdot 35 + 32 = 63 + 32 = 95$ | | | | |
| To Convert from Fahrenheit Temperature to Celsius
Temperature
$C = \frac{5}{9} \cdot (F - 32)$ | $35^{\circ}C = 95^{\circ}F$
Convert 50°F to degrees Celsius.
$C = \frac{5}{9} \cdot (50 - 32) = \frac{5}{9} \cdot 18 = 10$
$50^{\circ}F = 10^{\circ}C$ | | | | |
| Section 7.6 Energy: U.S. and I | Metric Systems of Measurement | | | | |
| Energy is the capacity to do work.
In the U.S. system of measurement, a foot-pound (ft-lb) is the amount of energy needed to move or lift a 1-pound object a distance of 1 foot. | How much energy is needed to move a 20-pound object
35 feet?
20 pounds · 35 feet = 700 foot-pounds of energy | | | | |
| In the U.S. system of measurement, a British Thermal
Unit (BTU) is the amount of heat required to raise the
temperature of 1 pound of water 1 degree Fahrenheit.
(1 BTU = 778 ft-lb) | Convert 50 BTU to foot-pounds.
$50 \text{ BTU} = 50 \text{ BFU} \cdot \frac{778 \text{ ft-lb}}{1 \text{ BFU}} = 38,900 \text{ ft-lb}$ | | | | |
| In the metric system, a calorie is the amount of heat
required to raise the temperature of 1 kilogram of water
1 degree Celsius. | A stationary bicyclist uses 350 calories in 1 hour.
How many calories will the bicyclist use in $\frac{1}{2}$ of an hour?
calories used = $350 \cdot \frac{1}{2} = 175$ calories | | | | |

| Chapter 7 Review | v | |
|---|------------------------------------|---|
| (7.1) Convert. | | |
| 1. 108 in. to feet 2. 72 ft | t to yards 3. 1.5 mi to fee | et 4. $\frac{1}{2}$ yd to inches |
| | | |
| 5. $52 \text{ ft} = \y \text{d} \f \text{t}$ | 6. 46 in. =ftin. | 7. 42 m to centimeters |
| 0.00 | 2 10 10 | 40 |
| 8. 82 cm to millimeters | 9. 12.18 mm to meters | 10. 2.31 m to kilometers |
| Perform each indicated operation. | | |
| 11. 4 yd 2 ft + 16 yd 2 ft | 12. 12 ft 1 in. – | - 4 ft 8 in. |
| | | |
| 13. 8 ft 3 in. × 5 | 14. 7 ft 4 in. ÷ | 2 |
| 15. 8 cm + 15 mm | 16. 4 m - 126 | cm |
| | | |
| 17. 8.62 m × 4 | 18. 19.6 km ÷ 5 | 8 |
| | | |
| Solve. | | |

- 19. A bolt of cloth contains 333 yd 1 ft of cotton ticking. Find the amount of material that remains after 163 yd 2 ft is removed from the bolt.
- **20.** The local ambulance corps plans to award 20 framed certificates of valor to some of its outstanding members. If each frame requires 6 ft 4 in. of framing material, how much material is needed for all the frames?

21. The trip from Philadelphia to Washington, D.C., is 217 km each way. Four friends agree to share the driving equally. How far must each drive on this round-trip vacation?



(7.2) Convert.

 \triangle **22.** The college has ordered that NO SMOKING signs be placed above the doorway of each classroom. Each sign is 0.8 m long and 30 cm wide. Find the area of each sign. (*Hint:* Recall that the area of a rectangle = width · length.)



30 centimeters

- **23.** 66 oz to pounds **24.** 2.3 tons to pounds **25.** 52 oz = ____lb ___oz **26.** $10,300 \text{ lb} = ____ \text{tons} ___ \text{lb}$ **27.** 27 mg to grams **28.** 40 kg to grams **29.** 2.1 hg to dekagrams **30.** 0.03 mg to decigrams Perform each indicated operation. **31.** 6 lb 5 oz – 2 lb 12 oz **32.** $5 \tan 1600 \, \text{lb} + 4 \tan 1200 \, \text{lb}$ **33.** 6 tons 2250 lb ÷ 3 **34.** 8 lb 6 oz \times 4 **35.** 4.3 mg × 5 **36.** 4.8 kg - 4200 g Solve.
- **37.** Donshay Berry ordered 1 lb 12 oz of soft-center candies and 2 lb 8 oz of chewy-center candies for his party. Find the total weight of the candy ordered.
- **38.** Four local townships jointly purchase 38 tons 300 lb of cinders to spread on their roads during an ice storm. Determine the weight of the cinders each township receives if they share the purchase equally.

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| 39. Linda Holden ordered 8.3 kg of whole wheat flour from the health-food store, but she received 450 g less. How much flour did she actually receive? | 40. Eight friends spent a weekend in the Poconos tapping maple trees and preparing 9.3 kg of maple syrup. Find the weight each friend receives if they share the syrup equally. | | |
|--|--|--|--|
| (7.3) Convert. | | | |
| 41. 16 pints to quarts 42. 40 fluid ounces to cups | 43. 3 qt 1 pt to pints 44. 18 quarts to cups | | |
| 45. $9 \text{ pt} = \q \text{t}\p \text{t}$ 46. $15 \text{ qt} = \$ | _galqt 47. 3.8 L to milliliters | | |
| 48. 4.2 ml to deciliters 49. 14 hl to kilolit | 50. 30.6 L to centiliters | | |
| Perform each indicated operation. | | | |
| 51. 1 qt 1 pt + 3 qt 1 pt 52. 3 gal 2 qt \times 2 | 53. 0.946 L - 210 ml 54. 6.1 L + 9400 ml | | |
| Solve. | | | |
| 55. Carlos Perez prepares 4 gal 2 qt of iced tea for a block party. During the first 30 minutes of the party, 1 gal 3 qt of the tea is consumed. How much iced tea remains? | 56. A recipe for soup stock calls for 1 c 4 fl oz of beef broth. How much should be used if the recipe is cut in half? | | |
| 57. Each bottle of Kiwi liquid shoe polish holds 85 ml of the polish. Find the number of liters of shoe polish contained in 8 boxes if each box contains 16 bottles. | 58. Ivan Miller wants to pour three separate containers of saline solution into a single vat with a capacity of 10 liters. Will 6 liters of solution in the first container combined with 1300 milliliters in the second container and 2.6 liters in the third container fit into the larger vat? | | |
| (7 A) Note: Bacquese approximations are used in this section | source and the second start of the second since in | | |

(7.4) Note: Because approximations are used in this section, your answers may vary slightly from the answers given in the back of the book.

Convert as indicated. If necessary, round to two decimal places.

| 62. 7.8 liters to quarts 63. 15 ounces to grams 64. 23 pour | nds to kilograms |
|--|------------------|

- **65.** A 100-meter dash is being held today. How many yards is this?
- **66.** If a person weighs 82 kilograms, how many pounds is this?

67. How many quarts are contained in a 3-liter bottle of cola?



68. A compact disc is 1.2 mm thick. Find the height (in inches) of 50 discs.



- (7.5) Convert. Round to the nearest tenth of a degree, if necessary.
- 69. 245°C to degrees Fahrenheit
 70. 160°C to degrees Fahrenheit
 71. 42°C to degrees Fahrenheit
 72. 93.2°F to degrees Celsius
 73. 41.3°F to degrees Celsius
 74. 80°F to degrees Celsius

Solve. Round to the nearest tenth of a degree, if necessary.

75. A sharp dip in the jet stream caused the temperature in New Orleans to drop to 35°F. Find the corresponding temperature in degrees Celsius.

(7.6) Solve.

- **77.** How many foot-pounds of energy are needed to lift a 5.6-pound radio a distance of 12 feet?
- **79.** How much energy is used when a 1.2-ton pile of sand is moved 15 yards?
- **81.** Convert 2,000,000 foot-pounds to BTU, rounded to the nearest hundred.
- **83.** Qwanetta Sesson uses 210 calories each hour she spends mowing the grass. Find the number of calories needed to mow the grass if she spends 3 hours mowing each week for 24 weeks.

- **76.** The recipe for meat loaf calls for a 165°C oven. Find the setting used if the oven has a Fahrenheit thermometer.
- **78.** How much energy is required to lift a 21-pound carton of Rice-A-Roni a distance of 6.5 feet?
- **80.** The energy required to operate a 12,000-BTU air conditioner is equivalent to how many foot-pounds?
- **82.** Kip Yates burns off 450 calories each hour he plays handball. How many calories does he use to play handball for $2\frac{1}{2}$ hours?
- **84.** Four ounces of sirloin steak contain 420 calories. If Edith Lutrell uses 180 calories each hour she walks, how long must she walk to burn off the calories from this steak?

Mixed Review

| Convert the following. | | |
|--|---------------------------------------|--|
| 85. 2.5 mi to feet | 86. 6.25 ft to inches | 87. 23,760 ft to miles |
| 88. 129 in. to feet | 89. 8200 lb = tons lb | 90. $4300 \text{ lb} = ___ \text{tons} ___ \text{lb}$ |
| 91. 5 m to centimeters | 92. 286 mm to kilometers | 93. 1400 mg to grams |
| 94. 240 mg to grams | 95. 6.75 gallons to quarts | 96. 5.25 gallons to quarts |
| 97. 8.5 pints to cups | 98. 6.25 pints to cups | 99. 86°C to degrees Fahrenheit |
| 100. 15°C to degrees Fahrenheit | 101. 51.8°F to degrees Celsius | 102. 82.4°F to degrees Celsius |
| Perform the indicated operations and s | simplify. | |
| 103. 9.3 km – 183 m | 104. 8.6 km – | 247 m |
| 105. 7.4 L + 6500 ml | 106. 35 L + 70 | 00 ml |
| 107. 9.3 g - 1200 mg | 108. 3.4 g - 18 | 300 mg |
| 109. 6.3 kg × 8 | 110. 3.2 kg × 4 | 4 |
| 111. 3 gal 1 qt + 4 gal 2 qt | 112. 6 gal 1 qt | + 2 gal 1 qt |
| 113. 4100 mm – 3 dm | 114. 6300 mm | — 5 dm |
| | | |

Chapter 7

MULTIPLE CHOICE Exercises 1 through 13 are Multiple Choice. For each exercise, choose the best response.

| 01 . An inch is about | how many centimeters? | | |
|-------------------------------|-------------------------|----------------------|-------------------|
| A. 10 cm | B. 100 cm | C. 2.5 cm | D. 1 cm |
| 2. A meter is about | t how many yards? | | |
| A. 10 yd | B. 100 yd | C. 2.5 yd | D. 1 yd |
| 03. A ton is how mat | ny pounds? | | |
| A. 10 lb | B. 100 lb | C. 1000 lb | D. 2000 lb |
| 4. Which is longer, | a mile or a kilometer? | | |
| A. a mile | B. a kilometer | | |
| 5. A kilogram is ab | out how many pounds? | | |
| A. 1 lb | B. 2 lb | C. 10 lb | D. 100 lb |
| 6 . A liter is about h | low many quarts? | | |
| A. 1 qt | B. 2 qt | C. 10 qt | D. 100 qt |
| 7 . Water freezes at | what temperature? Two | choices are correct. | |
| A. 0°C | B. 100°C | C. 32°F | D. 212°F |
| 8. Water boils at wl | hat temperature? Two ch | pices are correct. | |
| A. 0°C | B. 100°C | C. 32°F | D. 212°F |
| | | | |
| | | | |

For Exercises 9 through 13, choose the most reasonable answer.

| 9 . A man is how tall? | | | |
|------------------------------------|-------------------------------|--------------------------|----------------------|
| A. 16 centimeters | B. 1.6 feet | C. 16 inches | D. 1.6 meters |
| ● 10. Choose a reasonable pencil l | ead widths for mechanical per | ncils. | |
| A. 7 millimeters | B. 7 centimeters | C. 7 decimeters | D. 7 meters |
| ● 11. Choose a reasonable mass fo | or an antibiotic tablet. | | |
| A. 500 grams | B. 500 kilograms | C. 500 milligrams | |
| ● 12. Choose a reasonable temper | ature for a summer day. | | |
| A. 85°C | B. 30°C | C. 0°C | |
| ● 13. A man weighs how much? | | | |
| A. 75 kilograms | B. 75 grams | C. 75 milligrams | |

| Chapter 7 | Test MyLab Math or You Tube For additional practice go to your study plan in MyLab Math. |
|---|--|
| Answers | Convert. |
| | 1. 280 in. = ft in. 2. $2\frac{1}{2}$ gal to quarts |
| | 3. 30 oz to pounds 4. 2.8 tons to pounds |
| | • 5. 38 pt to gallons • 6. 40 mg to grams |
| 2.
3. | ▶ 7. 2.4 kg to grams▶ 8. 3.6 cm to millimeters |
| <u>4.</u>
5. | •9. 4.3 dg to grams •10. 0.83 L to milliliters |
| <u> 6. </u> | Perform each indicated operation. |
| 8. | ● 11. 3 qt 1 pt + 2 qt 1 pt
● 12. 8 lb 6 oz - 4 lb 9 oz |
| <u>9.</u>
10. | • 13. 2 ft 9 in. \times 3 • 14. 5 gal 2 qt \div 2 |
| <u>11.</u> | ● 15. 8 cm - 14 mm ● 16. 1.8 km + 456 m |
| 12. | Convert. Round to the nearest tenth of a degree, if necessary. |
| <u>13.</u>
<u>14.</u> | ● 17. 84°F to degrees Celsius ● 18. 12.6°C to degrees Fahrenheit |
| <u>15.</u>
16. | • 19. The sugar maples in front of Bette
MacMillan's house are 8.4 meters tall.
Because they interfere with the phone
MacMillan's house are 8.4 meters tall. |
| 17. | Because they interfere with the phone much oil still remains in the container?
lines, the telephone company plans to
remove the top third of the trees. How |
| 18. | tall will the maples be after they are shortened? |
| 19. | |
| 20. | 21. The engineer in charge of bridge construction said that the span of a22. If 2 ft 9 in. of material is used to manufacture one scarf, how much material is |
| 21. | certain bridge would be 88 m. But needed for 6 scarves?
the actual construction required it to |
| 22. | be 340 cm longer. Find the span of
the bridge, in meters. |
| 500 | |

| • 23. | The Vietnam Veterans Memorial,
inscribed with the names of 58,226
deceased and missing U.S. soldiers
from the Vietnam War, is located on
the National Mall in Washington, D.C.
This memorial is formed from two
straight sections of wall that meet at
an angle at the center of the monu-
ment. Each wall is 246 ft 9 in. long.
What is the total length of the Vietnam
Veterans Memorial's wall? (<i>Source:</i>
National Park Service) | | Each panel making up the wall of
the Vietnam Veterans Memorial is
101.6 cm wide. There are a total of
148 panels making up the wall. What is
the total length of the wall in meters?
(<i>Source:</i> National Park Service) | 23.
24.
25. |
|--------------|---|--------------|---|--------------------------|
| 0 25. | The hottest temperature ever re-
corded was 134°F in Death Valley at
Furnace Creek Ranch, CA, on July
10, 1913. Convert this temperature to
degrees Celsius. Round your answer to
the nearest tenth of a degree. (<i>Source:</i>
National Climatic Data Center) | 0 26. | The doctors are quite concerned about
Lucia Gillespie, who is running a 41°C
fever. Find Lucia's temperature in
degrees Fahrenheit. | <u>26.</u>
<u>27.</u> |
| • 27. | The largest ice cream sundae ever
made in the United States was assem-
bled in Anaheim, California, in 1985.
This giant sundae used 4667 gallons
of ice cream. How many pints of ice
cream were used? | 0 28. | A piece of candy weighs 5 grams. How many ounces is this? | <u>28.</u>
29. |
| ○ 29. | A 5-kilometer race is being held today. How many miles is this? | 0 30. | A 5-gallon container holds how many liters? | 30. |
| • 31. | Phillipe Jordaine must lift a
48.5-pound carton of canned tomatoes
a distance of 14 feet. Find the energy
required to move the carton. | •32. | Energy used by a 26,000-BTU
heater is equivalent to how many
foot-pounds? | 31 |
| | | | | 32. |
| • 33. | Robin Nestle burns 180 calories each
hour when she swims. How many calo-
ries does she use if she swims 1 hour per
day for 5 days? | | | 33 |

501

Chapters 1–7 Cumulative Review Answers 1 Add: 1647 + 246 + 32 + 85 2

- 1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 11. 12. 13. 14. 15. 16. 17. 18. 19. 20. 21. 22. 23. 24. 25. **25.** Write $\frac{2}{3}$ as a decimal. 26. 502
- **2.** Subtract: 2000 469 **1.** Add: 1647 + 246 + 32 + 85**3.** Find the prime factorization of 945. 4. Find the area of the rectangle. 17 in. 9 in. **6.** Subtract: $\frac{8}{21} - \frac{2}{9}$ **5.** Find the LCM of 11 and 33. **7.** Add: $3\frac{4}{5} + 1\frac{4}{15}$ 8. Multiply: $2\frac{1}{2} \cdot 4\frac{2}{15}$ Write each decimal as a fraction or mixed number in simplest form. 9. 0.125 **10.** 1.2 **12.** Evaluate: $\left(\frac{2}{3}\right)^3$ 11.105.083 **13.** Insert <, >, or = to form a true **14.** Evaluate: $30 \div 6 \cdot 5$ statement. 0.052 0.236 **15.** Subtract: 85 – 17.31. Check your **16.** Add: 27.9 + 8.07 + 103.261 answer. Multiply. **17.** 42.1 × 0.1 **18.** 186.04 × 1000 **19.** 9.2 × 0.001 **20.** Find the average of 6.8, 9.7, and 0.9. **22.** Add: $\frac{3}{10} + \frac{3}{4}$ **21.** Divide: $8.32 \div 32$. Check your answer. **23.** Write $2\frac{3}{16}$ as a decimal. **24.** Round 7.2846 to the nearest tenth.

0.12 + 0.96

0.5

26. Simplify:

28. Write the ratio of $2\frac{2}{3}$ to $5\frac{1}{9}$ as a ratio

30. A square is 9 inches by 9 inches. Find

32. A recipe that makes 2 piecrusts calls for 3 cups of flour. How much flour is

needed to make 5 piecrusts?

34. Write 23% as a fraction.

36. Write $\frac{7}{8}$ as a percent.

38. 108 is what percent of 450?

40. Convert 4 gallons to pints.

42. Convert 8.6 meters to centimeters.

44. Convert 13,000 pounds to tons.

46. Convert $3\frac{1}{4}$ pounds to ounces.

the ratio of a side to its perimeter.

using fractional notation.

| 27. |
|------------|
| 28. |
| 29. |
| 30. |
| |
| 31. |
| 32. |
| 33. |
| 34. |
| 35. |
| |
| 36. |
| 37 |
| 37. |
| 38. |
| <u>39.</u> |
| 40. |
| 41. |
| 41. |
| 42. |
| 43. |
| 44. |
| |
| <u>45.</u> |
| <u>46.</u> |
| <u>47.</u> |
| 48. |
| |
| <u>49.</u> |
| 50. |
| |

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- **27.** Write the ratio of 12 to 17 using fractional notation.
- **29.** Write "337.5 miles every 15 gallons of gas" as a unit rate.
- **31.** Find the unknown number $n \cdot \frac{7}{n} = \frac{6}{5}$
- \triangle **33.** A 50-pound bag of fertilizer covers 2400 square feet of lawn. How many bags of fertilizer are needed to cover a town square containing 15,360 square feet of lawn? Round the answer up to the nearest whole bag.
 - **35.** Write 23% as a decimal.
 - **37.** Write $\frac{1}{12}$ as a percent. Round to the nearest hundredth percent.
 - **39.** What number is 35% of 40?
 - **41.** Translate to a proportion. What percent of 30 is 75?
 - **43.** In response to a decrease in sales, a company with 1500 employees reduces the number of employees to 1230. What is the percent of decrease?
 - **45.** An electric rice cooker that normally sells for \$65 is on sale for 25% off. What is the amount of discount and what is the sale price?
 - **47.** Find the simple interest after 2 years on \$500 at an interest rate of 12%.
 - **49.** Convert 9000 pounds to tons.
- **48.** The number of faculty at a local community college was recently increased from 240 to 276. What is the percent of increase?
- **50.** Convert 25° Celsius to degrees Fahrenheit.

8

The word geometry is formed from the Greek words geo, meaning Earth, and *metron*, meaning measure. Geometry literally means to measure the Earth. In this chapter we learn about various geometric figures and their properties such as perimeter, area, and volume. Knowledge of geometry can help us solve practical problems in reallife situations. For instance, knowing certain measures of a circular swimming pool allows us to calculate how much water it can hold.

Sections

- 8.1 Lines and Angles
- 8.2 Plane Figures and Solids
- 8.3 Perimeter
- 8.4 Area
- 8.5 Volume

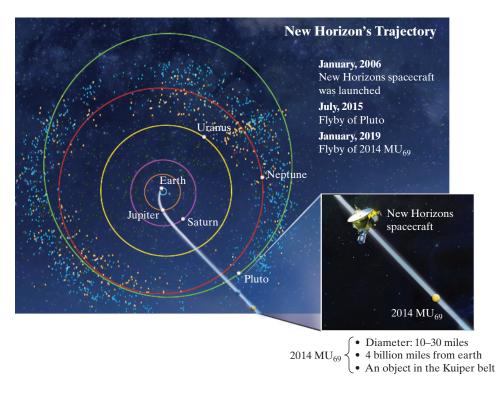
Integrated Review— Geometry Concepts

- 8.6 Square Roots and the Pythagorean Theorem
- 8.7 Congruent and Similar Triangles

Check Your Progress

Vocabulary Check Chapter Highlights Chapter Review Getting Ready for the Test Chapter Test Cumulative Review

Geometry

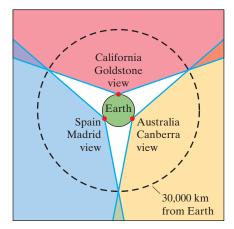


Where Is New Horizons Spacecraft Now, and How Do We Receive Data Collected?

ew Horizons is NASA's robotic spacecraft mission. This spacecraft is about the size and shape of a grand piano with a satellite dish attached. It was launched in January 2006 and is now headed for a January 1,2019, flyby past 2014 MU_{69} , a small object in the Kuiper asteroid belt. How do we receive the images of this spacecraft when it is so far into deep space?

The Deep Space Network (DSN) is a worldwide network of large antennas and communication facilities. When a mission is in deep space, fewer sites are needed for sending and receiving transmissions; thus, the DSN uses only three sites, shown below. The diagram below shows an overview of Earth from the vantage point of the North Pole and the location of these three sites.

We study some geometry of the DSN in Section 8.1, Exercises 65 and 66.



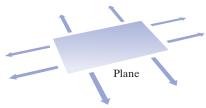
🛆 8.1 Lines and Angles 🔘

Objective A Identifying Lines, Line Segments, Rays, and Angles >

Let's begin with a review of two important concepts—space and plane.

Space extends in all directions indefinitely. Examples of objects in space are houses, grains of salt, bushes, your *Basic College Mathematics* textbook, and you.

A **plane** is a flat surface that extends indefinitely. Surfaces like a plane are a classroom floor or a blackboard or whiteboard.



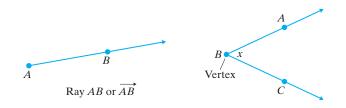
The most basic concept of geometry is the idea of a point in space. A **point** has no length, no width, and no height, but it does have location. We represent a point by a dot, and we usually label points with capital letters.



A **line** is a set of points extending indefinitely in two directions. A line has no width or height, but it does have length. We can name a line by any two of its points or by a single lowercase letter. A **line segment** is a piece of a line with two endpoints.

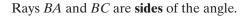


A **ray** is a part of a line with one endpoint. A ray extends indefinitely in one direction. An **angle** is made up of two rays that share the same endpoint. The common endpoint is called the **vertex.**



The angle in the figure above can be named

```
\angle ABC \ \angle CBA \ \angle B \text{ or } \ \angle x
\uparrow \qquad \uparrow
The vertex is the middle point.
```



A Identify Lines, Line Segments,

Objectives

Rays, and Angles.
B Classify Angles as Acute, Right, Obtuse, or Straight.
C Identify Complementary and Supplementary Angles.
D Find Measures of Angles.

*Although line *l* is also line *BA* or \overleftarrow{BA} , we will use only one order of points to name a line or line segment.

Helpful Hint

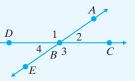
Naming an Angle

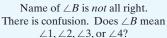
Example 1

When there is no confusion as to what angle is being named, you may use the vertex alone.



Name of $\angle B$ is all right. There is no confusion. $\angle B$ means $\angle 1$.

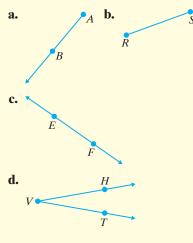




Identify each figure as a line, a ray, a line segment, or an angle.

Practice 1

Identify each figure as a line, a ray, a line segment, or an angle. Then name the figure using the given points.



Practice 2

Use the figure in Example 2 to list other ways to name $\angle z$.

Answers

1. a. ray; ray *AB* or \overrightarrow{AB} **b.** line segment; line segment *RS* or \overrightarrow{RS} **c.** line; line *EF* or \overrightarrow{EF} **d.** angle; $\angle TVH$ or $\angle HVT$ or $\angle V$ **2.** $\angle RTS$, $\angle STR$

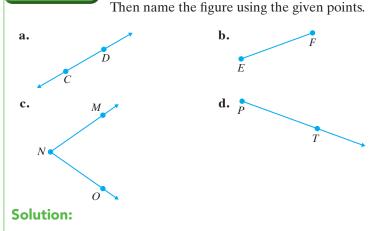
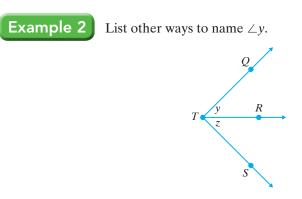


Figure (a) extends indefinitely in two directions. It is line CD or \overrightarrow{CD} . Figure (b) has two endpoints. It is line segment EF or \overline{EF} . Figure (c) has two rays with a common endpoint. It is $\angle MNO$, $\angle ONM$, or $\angle N$. Figure (d) is part of a line with one endpoint. It is ray PT or \overrightarrow{PT} .

Work Practice 1

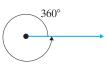


Solution: Two other ways to name $\angle y$ are $\angle QTR$ and $\angle RTQ$. We may *not* use the vertex alone to name this angle because three different angles have *T* as their vertex.

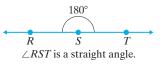
Work Practice 2

Objective **B** Classifying Angles as Acute, Right, Obtuse, or Straight

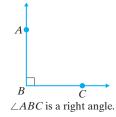
An angle can be measured in **degrees.** The symbol for degrees is a small, raised circle, °. There are 360° in a full revolution, or a full circle.



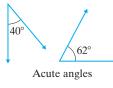
 $\frac{1}{2}$ of a revolution measures $\frac{1}{2}$ (360°) = 180°. An angle that measures 180° is called a **straight angle.**



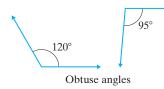
 $\frac{1}{4}$ of a revolution measures $\frac{1}{4}(360^\circ) = 90^\circ$. An angle that measures 90° is called a **right angle.** The symbol `` is used to denote a right angle.

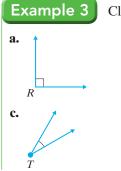


An angle whose measure is between 0° and 90° is called an **acute angle.**

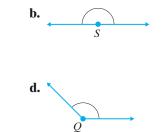


An angle whose measure is between 90° and 180° is called an **obtuse angle.**



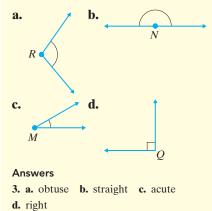


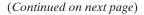
Classify each angle as acute, right, obtuse, or straight.



Practice 3

Classify each angle as acute, right, obtuse, or straight.





Solution:

- **a.** $\angle R$ is a right angle, denoted by \vdash . It measures 90°.
- **b.** $\angle S$ is a straight angle. It measures 180°.
- **c.** $\angle T$ is an acute angle. It measures between 0° and 90°.
- **d.** $\angle Q$ is an obtuse angle. It measures between 90° and 180°.

Work Practice 3

Let's look at $\angle B$ below, whose measure is 62° .



There is a shorthand notation for writing the measure of this angle. To write "The measure of $\angle B$ is 62°," we can write

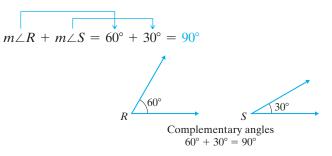
$$\overrightarrow{m} \perp B = 62^{\circ}.$$

By the way, note that $\angle B$ is an acute angle because $m \angle B$ is between 0° and 90°.

Objective C Identifying Complementary and Supplementary Angles

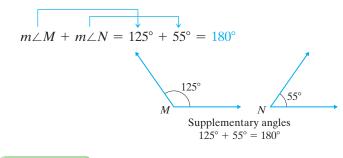
Two angles that have a sum of 90° are called **complementary angles.** We say that each angle is the **complement** of the other.

 $\angle R$ and $\angle S$ are complementary angles because



Two angles that have a sum of 180° are called **supplementary angles.** We say that each angle is the **supplement** of the other.

 $\angle M$ and $\angle N$ are supplementary angles because



Example 4

Find the complement of a 48° angle.

Solution: Two angles that have a sum of 90° are complementary. This means that the complement of an angle that measures 48° is an angle that measures $90^{\circ} - 48^{\circ} = 42^{\circ}$.

Work Practice 4

Practice 4

Find the complement of a 29° angle.

Answer 4. 61°

Example 5 Find the supplement of a 107° angle.

Solution: Two angles that have a sum of 180° are supplementary. This means that the supplement of an angle that measures 107° is an angle that measures $180^{\circ} - 107^{\circ} = 73^{\circ}$.

Work Practice 5

Concept Check True or false? The supplement of a 48° angle is 42°. Explain.

Objective **D** Finding Measures of Angles **D**

Measures of angles can be added or subtracted to find measures of related angles.

Example 6 Find the measure of $\angle x$. Then classify $\angle x$ as an acute, obtuse, or right angle.

52

Solution: $m \angle x = m \angle QTS - m \angle RTS$ $= 87^{\circ} - 52^{\circ}$ $= 35^{\circ}$

Thus, the measure of
$$\angle x \ (m \angle x)$$
 is 35°.

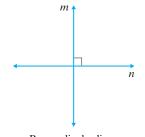
Since $\angle x$ measures between 0° and 90°, it is an acute angle.

Work Practice 6

Two lines in a plane can be either parallel or intersecting. Parallel lines never meet. **Intersecting lines** meet at a point. The symbol || is used to indicate "is parallel to." For example, in the figure, $p \parallel q$.



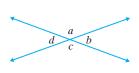
Some intersecting lines are perpendicular. Two lines are perpendicular if they form right angles when they intersect. The symbol \perp is used to denote "is perpendicular to." For example, in the figure below, $m \perp n$.





When two lines intersect, four angles are formed. Two angles that are opposite each other are called vertical angles. Vertical angles have the same measure.

Two angles that share a common side are called adjacent angles. Adjacent angles formed by intersecting lines are supplementary. That is, the sum of their measures is 180°.



Vertical angles: $\angle a$ and $\angle c$ $\angle d$ and $\angle b$

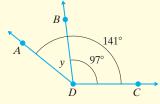
Adjacent angles: $\angle a$ and $\angle b$ $\angle b$ and $\angle c$ $\angle c$ and $\angle d$ $\angle d$ and $\angle a$

Practice 5

Find the supplement of a 67° angle.

Practice 6

a. Find the measure of $\angle y$.



b. Find the measure of $\angle x$.



c. Classify $\angle x$ and $\angle y$ as acute, obtuse, or right angles.

Answers **5.** 113° **6. a.** 44° **b.** 28°

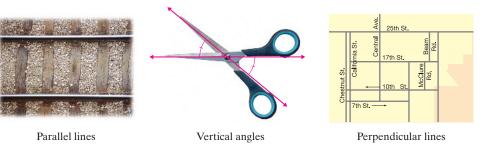
c. both acute

Concept Check Answer

false; the complement of a 48° angle is 42°; the supplement of a 48° angle is 132°

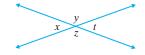
Chapter 8 | Geometry

Here are a few real-life examples of the lines we just discussed.





Find the measures of $\angle x$, $\angle y$, and $\angle z$ if the measure of $\angle t$ is 42°.



Solution: Since $\angle t$ and $\angle x$ are vertical angles, they have the same measure, so $\angle x$ measures 42°.

Since $\angle t$ and $\angle y$ are adjacent angles, their measures have a sum of 180°. So $\angle y$ measures $180^{\circ} - 42^{\circ} = 138^{\circ}$.

Since $\angle y$ and $\angle z$ are vertical angles, they have the same measure. So $\angle z$ measures 138°.

Work Practice 7

A line that intersects two or more lines at different points is called a **transversal.** Line l is a transversal that intersects lines m and n. The eight angles formed have special names. Some of these names are:

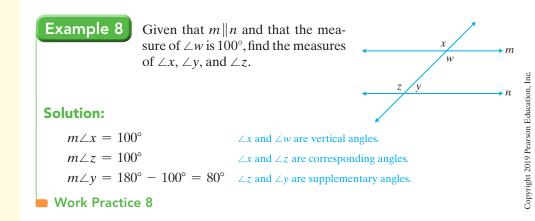
Corresponding angles: $\angle a$ and $\angle e$, $\angle c$ and $\angle g$, $\angle b$ and $\angle f$, $\angle d$ and $\angle h$

Alternate interior angles: $\angle c$ and $\angle f$, $\angle d$ and $\angle e$

When two lines cut by a transversal are *parallel*, the following statement is true:

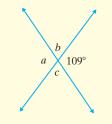
Parallel Lines Cut by a Transversal

If two parallel lines are cut by a transversal, then the measures of **corresponding angles are equal** and the measures of the **alternate interior angles are equal**.



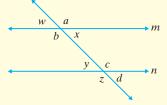
Practice 7

Find the measures of $\angle a$, $\angle b$, and $\angle c$.



Practice 8

Given that $m \parallel n$ and that the measure of $\angle w = 45^\circ$, find the measures of all the angles shown.



Answers

7. $m \angle a = 109^\circ; m \angle b = 71^\circ;$ $m \angle c = 71^\circ$

8. $m \angle x = 45^{\circ}; m \angle y = 45^{\circ};$ $m \angle z = 135^{\circ}; m \angle a = 135^{\circ};$ $m \angle b = 135^{\circ}; m \angle c = 135^{\circ};$ $m \angle d = 45^{\circ}$

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank.

| | acute | straight | degrees | adjacent | parallel | intersecting | | | |
|-----|--|--|-------------------|------------------|------------------------|-------------------------------------|--|--|--|
| | obtuse | space | plane | point | vertical | vertex | | | |
| | right | angle | ray | line | perpendicular | transversal | | | |
| | 1. A(n) | is | s a flat surface | that extends ind | definitely. | | | | |
| | | | | | • | | | | |
| | 3 | A(n) has no length, no width, and no height. extends in all directions indefinitely. | | | | | | | |
| | 4. A(n) | is | s a set of points | extending ind | efinitely in two direc | tions. | | | |
| | 5. A(n) | is | s part of a line | with one endpo | pint. | | | | |
| | 6. A(n) | is | s made up of tv | vo rays that sha | re a common endpo | int. The common endpoint is called | | | |
| | the | | | | | | | | |
| | 7. A(n) | a | ngle measures | 180°. | | | | | |
| | 8. A(n) | a | ngle measures | 90°. | | | | | |
| | 9. A(n) | a | ngle measures | between 0° and | 1 90°. | | | | |
| 1 | 0. A(n) | a | ngle measures | between 90° ar | nd 180°. | | | | |
| 1 | 1 | lines n | ever meet and | | _ lines meet at a po | int. | | | |
| 1 | 2. Two inte | 2. Two intersecting lines are if they form right angles when they intersect. | | | | | | | |
| 1 | 3. An angl | e can be measur | ed in | · | | | | | |
| 1 | 4. A line th | nat intersects two | o or more lines | at different po | ints is called a(n) | · | | | |
| 1 | 5. When tw | vo lines intersec | t, four angles a | re formed. The | angles that are oppo | osite each other are called | | | |
| | | angles. | | | | | | | |
| 1 | 6. Two ang | gles that share a | common side a | re called | angles. | | | | |
| ſ | A subin Can tubon sting lideas Well de sind and the state of the second | | | | | | | | |
| | Martin-Gay Interactive Videos Watch the section lecture video and answer the following questions. | | | | | | | | |
| | | Objective A 17. In the lecture after Example 2, what are the four ways | | | | | | | |
| | we can name the angle shown?
Objective B 18. In the lecture before Example 3 , what type of angle | | | | | | | | |
| | forms a line? What is its measure? | | | | | | | | |
| | | EL 1 | Obie | | | used to find the answer | | | |
| | to Example 6? | | | | | | | | |
| | C | | Obje | | | e 🖪 Example 7, two lines in a plane | | | |
| - E | VPP, VIAA | (op. Viden 81 | | | | | | | |

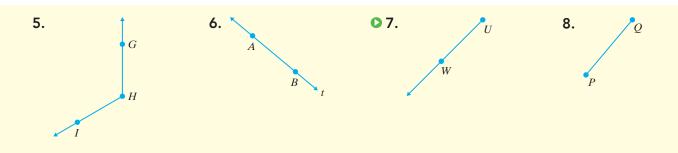
8.1 Exercise Set MyLab Math

see Video 8.1 🍅

Objective A *Identify each figure as a line, a ray, a line segment, or an angle. Then name the figure using the given points. See Examples 1 and 2.*

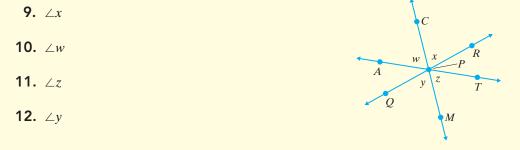
that aren't parallel must what? 🜔



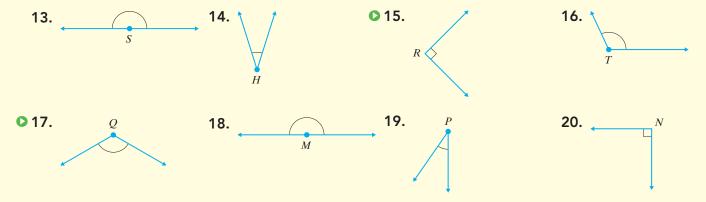


List two other ways to name each angle. See Example 2.

512

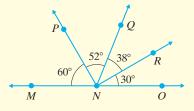


Objective B *Classify each angle as acute, right, obtuse, or straight. See Example 3.*

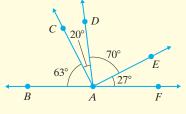


Objective C *Find each complementary or supplementary angle as indicated. See Examples 4 and 5.*

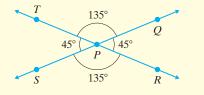
- **21.** Find the complement of a 23° angle.
- 23. Find the supplement of a 17° angle.
 - **25.** Find the complement of a 58° angle.
 - **27.** Find the supplement of a 150° angle.
 - **29.** Identify the pairs of complementary angles.



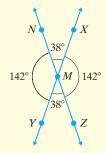
- **22.** Find the complement of a 77° angle.
- **24.** Find the supplement of a 77° angle.
- **26.** Find the complement of a 22° angle.
- **28.** Find the supplement of a 130° angle.
- **30.** Identify the pairs of complementary angles.



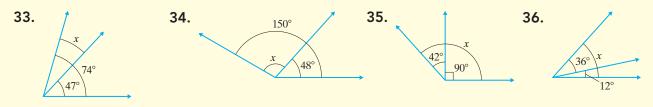
31. Identify the pairs of supplementary angles.



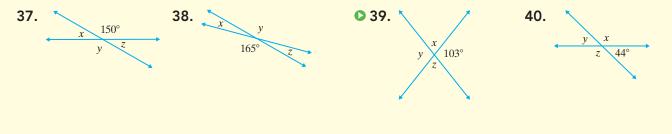
32. Identify the pairs of supplementary angles.

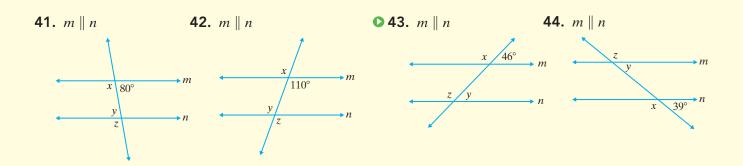


Objective D *Find the measure of* $\angle x$ *in each figure. See Example 6.*

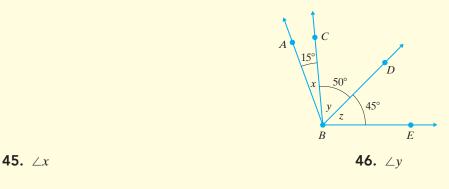


Find the measures of angles x, y, and z in each figure. See Examples 7 and 8.





Objectives A D Mixed Practice Find two other ways of naming each angle. See Example 2.



47. ∠*z*

48. $\angle ABE$ (just name one other way)

Find the measure of each angle in the figure above. See Example 6.

| ● 49. ∠ <i>ABC</i> | 50. ∠ <i>EBD</i> | 51. ∠ <i>CBD</i> | 52. ∠ <i>CBA</i> |
|---------------------------|-------------------------|-------------------------|-------------------------|
| ● 53. ∠ <i>DBA</i> | 54. ∠ <i>EBC</i> | 55. ∠ <i>CBE</i> | 56. ∠ <i>ABE</i> |

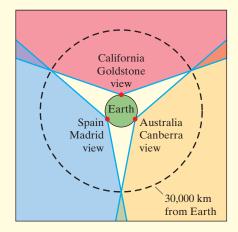
Review

Perform each indicated operation. See Sections 2.4, 2.5, 3.3, and 3.4.

| 57. $\frac{7}{8} + \frac{1}{4}$ | 58. $\frac{7}{8} - \frac{1}{4}$ | 59. $\frac{7}{8} \cdot \frac{1}{4}$ | 60. $\frac{7}{8} \div \frac{1}{4}$ |
|--|--|---|--|
| 61. $3\frac{1}{3} - 2\frac{1}{2}$ | 62. $3\frac{1}{3} + 2\frac{1}{2}$ | 63. $3\frac{1}{3} \div 2\frac{1}{2}$ | 64. $3\frac{1}{3} \cdot 2\frac{1}{2}$ |

Concept Extensions

Use this North Pole overhead view of the three sites of the Deep Space Network to answer Exercises 65 and 66. (See the Chapter Opener.)



65. How many degrees are there around the Earth at the equator?

66. If the three sites of the Deep Space Network (red dots shown) are about the same number of degrees apart, how many degrees apart are they?

67. The angle between the two walls of the Vietnam Veterans Memorial in Washington, D.C., is 125.2°. Find the supplement of this angle. (*Source:* National Park Service)



68. The faces of Khafre's Pyramid at Giza, Egypt, are inclined at an angle of 53.13°. Find the complement of this angle. (*Source:* PBS *NOVA* Online)



69. One great pyramid at Chichen Itza, Mexico, was the Temple of Kukulkan. The four faces of this pyramid have protruding stairways that rise at a 45° angle. Find the complement of this angle.



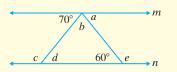
70. The UNESCO World Heritage Site of the Cahokia Mounds is located in Cahokia, Illinois. This site was once populated by the Mississippian People of North America and was built up on a series of mounds. These mounds were completely constructed of silt and dirt. The largest and best known of these is the Monk's Mound, which is considered a truncated pyramid, with the top being a flat base rather than extending to a point. On one side of this mound, modern archeologists have measured a 35° angle. Find the complement of this angle.



Answer true or false for Exercises 71 through 74. See the Concept Check in this section. If false, explain why.

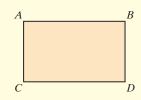
- **71.** The complement of a 100° angle is an 80° angle.
- **73.** It is possible to find the supplement of a 120° angle.
- **72.** It is possible to find the complement of a 120° angle.
- **74.** The supplement of a 5° angle is a 175° angle.

75. If lines *m* and *n* are parallel, find the measures of angles *a* through *e*.



- **77.** Can two supplementary angles both be acute? Explain why or why not.
 - **79.** Find two complementary angles with the same measure.

76. Below is a rectangle. List which segments, if extended, would be parallel lines.



- **78.** In your own words, describe how to find the complement and the supplement of a given angle.
- **80.** Is the figure below possible? Why or why not?

103° 87°

8.2 Plane Figures and Solids

Objectives

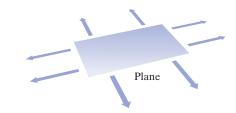
🗛 Identify Plane Figures. 🜔

🛚 Identify Solids. >

In order to prepare for the sections ahead in this chapter, we first review plane figures and solids.

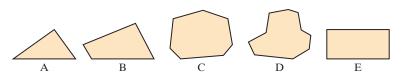
Objective 🗛 Identifying Plane Figures 🕑

Recall from Section 8.1 that a **plane** is a flat surface that extends indefinitely.



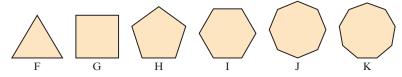
A **plane figure** is a figure that lies on a plane. Plane figures, like planes, have length and width but no thickness or depth.

A **polygon** is a closed plane figure that basically consists of three or more line segments that meet at their endpoints.



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A **regular polygon** is one whose sides are all the same length and whose angles are the same measure.



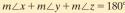
A polygon is named according to the number of its sides.

| Polygons | | | |
|-----------------|---------------|-----------------|--|
| Number of Sides | Name | Figure Examples | |
| 3 | Triangle | A, F | |
| 4 | Quadrilateral | B, E, G | |
| 5 | Pentagon | Н | |
| 6 | Hexagon | Ι | |
| 7 | Heptagon | С | |
| 8 | Octagon | J | |
| 9 | Nonagon | K | |
| 10 | Decagon | D | |

Some triangles and quadrilaterals are given special names, so let's study these polygons further. We begin with triangles.

The sum of the measures of the angles of a triangle is 180° .







Find the measure of $\angle a$.



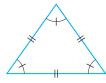
Solution: Since the sum of the measures of the three angles is 180°, we have

measure of $\angle a$, or $m \angle a = 180^\circ - 95^\circ - 35^\circ = 50^\circ$

To check, see that $95^{\circ} + 35^{\circ} + 50^{\circ} = 180^{\circ}$.

Work Practice 1

We can classify triangles according to the lengths of their sides. (We will use tick marks to denote the sides and angles of a figure that are equal.)



Equilateral triangle All three sides are the same length. Also, all three angles have the same measure.

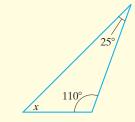


Isosceles triangle Two sides are the same length. Also, the angles opposite the equal sides have equal measure.



Scalene triangle No sides are the same length. No angles have the same measure.

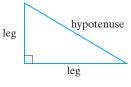
Practice 1 Find the measure of $\angle x$.

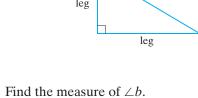


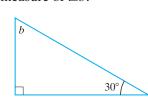
Answer 1. 45°

Example 2

One other important type of triangle is a right triangle. A right triangle is a triangle with a right angle. The side opposite the right angle is called the hypotenuse, and the other two sides are called legs.







Solution: We know that the measure of the right angle, b, is 90°. Since the sum of the measures of the angles is 180°, we have

measure of $\angle b$, or $m \angle b = 180^\circ - 90^\circ - 30^\circ = 60^\circ$

Work Practice 2

Helpful Hint

From the previous example, can you see that in a right triangle, the sum of the other two acute angles is 90°? This is because

 $90^{\circ} + 90^{\circ} = 180^{\circ}$ 1 1 _____ sum of right sum of angles' angle's other two measures measure angles' measures

Now we review some special quadrilaterals. A parallelogram is a special quadrilateral with opposite sides parallel and equal in length.

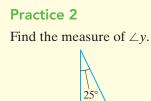


A rectangle is a special parallelogram that has four right angles.



A square is a special rectangle that has all four sides equal in length.





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A rhombus is a special parallelogram that has all four sides equal in length.

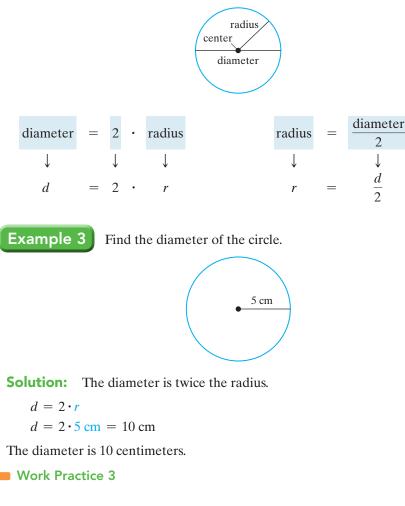


A trapezoid is a quadrilateral with exactly one pair of opposite sides parallel.



Concept Check True or false? All quadrilaterals are parallelograms. Explain.

In addition to triangles, quadrilaterals, and other polygons, circles are also plane figures. A **circle** is a plane figure that consists of all points that are the same fixed distance from a point c. The point c is called the **center** of the circle. The **radius** of a circle is the distance from the center of the circle to any point on the circle. The **diameter** of a circle is the distance across the circle passing through the center. Notice that the diameter is twice the radius, and the radius is half the diameter.

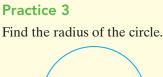


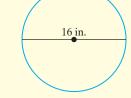
Objective B Identifying Solid Figures 💟



Recall from Section 8.1 that space extends in all directions indefinitely.

A solid is a figure that lies in space. Solids have length, width, and height or depth.

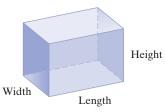




Answer 3. 8 in.

Concept Check Answer false

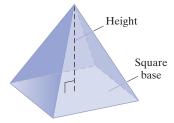
A **rectangular solid** is a solid that consists of six sides, or faces, all of which are rectangles.



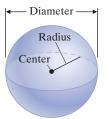
A cube is a rectangular solid whose six sides are squares.



A **pyramid** is shown below. The pyramids we will study have square bases and heights that are perpendicular to their base.



A **sphere** consists of all points in space that are the same distance from a point c. The point c is called the **center** of the sphere. The **radius** of a sphere is the distance from the center to any point on the sphere. The **diameter** of a sphere is the distance across the sphere passing through the center.



The radius and diameter of a sphere are related in the same way as the radius and diameter of a circle.

$$d = 2 \cdot r$$
 or $r = \frac{d}{2}$



4 Find the radius of the sphere.

Solution: The radius is half the diameter.

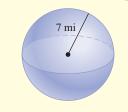
$$r = \frac{d}{2}$$
$$r = \frac{36 \text{ feet}}{2} = 18 \text{ feet}$$

The radius is 18 feet.

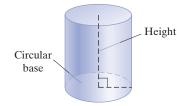
Work Practice 4



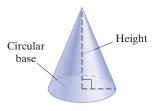
Practice 4 Find the diameter of the sphere.



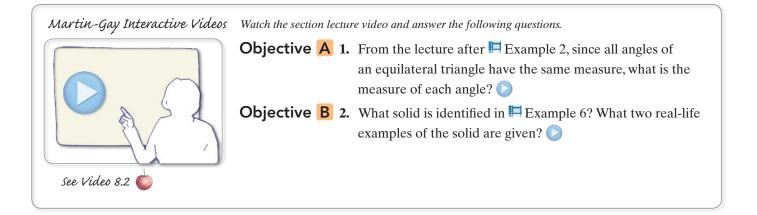
Answer 4. 14 mi The **cylinders** we will study have bases that are in the shape of circles and heights that are perpendicular to their base.



The **cones** we will study have bases that are circles and heights that are perpendicular to their base.

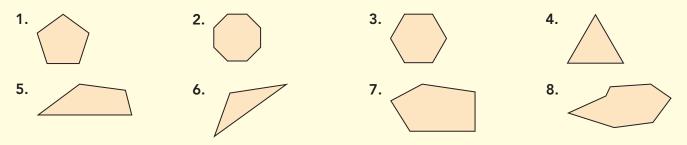


Vocabulary, Readiness & Video Check



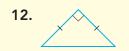
8.2 Exercise Set MyLab Math

Objective A *Identify each polygon. See the table at the beginning of this section.*

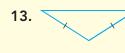


Classify each triangle as equilateral, isosceles, or scalene. Also identify any triangles that are also right triangles. See the triangle classification after Example 1.

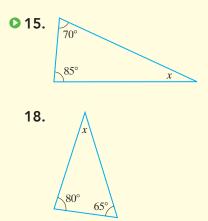


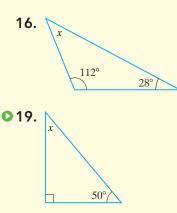


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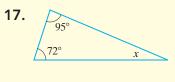


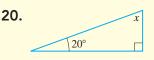
Find the measure of $\angle x$ *in each figure. See Examples 1 and 2.*











Fill in each blank.

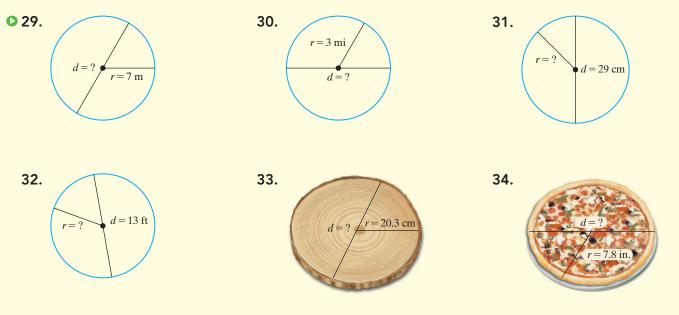
- **21.** Twice the radius of a circle is its
- **23.** A parallelogram with four right angles is a(n)
- **25.** A quadrilateral with opposite sides parallel is a(n)
 - **27.** The side opposite the right angle of a right triangle is called the _____.

22. A rectangle with all four sides equal is a(n)

_____.

- **24.** Half the diameter of a circle is its _____.
- **26.** A quadrilateral with exactly one pair of opposite sides parallel is a(n) _____.
- **28.** A triangle with no equal sides is a(n)

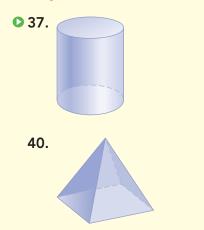
Find the unknown diameter or radius in each figure. See Example 3.



35. The normal pupil size in adults varies and even changes as one ages. The average diameter of a pupil in a 20-year-old is 4.6 mm. (*Source: National Geographic*)



Objective B *Identify each solid.*





38.

Identify the basic shape of each item.





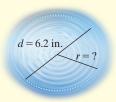


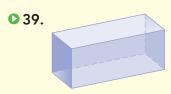


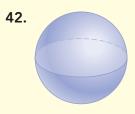
50.













48.



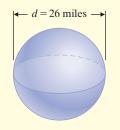
36. A ripple in the water has a diameter of 6.2 inches.

Find each unknown radius or diameter. See Example 4.

51. The radius of a sphere is 7.4 inches. Find its diameter.



53. Find the radius of the sphere.

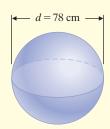


55. Saturn has a radius of approximately 36,184 miles. What is its diameter?

52. The radius of a sphere is 5.8 meters. Find its diameter.



54. Find the radius of the sphere.



56. A sphere-shaped wasp nest found in Japan had a radius of approximately 15 inches. What was its diameter? (*Source: Guinness World Records*)

Review

| Perform each indicated operation. See Sections 1.3, 1.6, 4.3, and 4.4. | | |
|--|-----|-----------------|
| 57. 2(18) + 2(36) | 58. | 4(87) |
| 59. 4(3.14) | 60. | 2(7.8) + 2(9.6) |

Concept Extensions

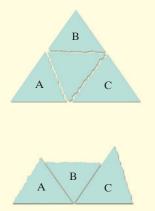
Determine whether each statement is true or false. See the Concept Check in this section.

- **61.** A square is also a rhombus.
- **63.** A rectangle is also a parallelogram.
 - **65.** A pentagon is also a quadrilateral.
- **67.** Is an isosceles right triangle possible? If so, draw one.
- **69.** The following demonstration is credited to the mathematician Pascal, who is said to have developed it as a young boy.

Cut a triangle from a piece of paper. The length of the sides and the size of the angles are unimportant. Tear the points off the triangle as shown in the top right figure.

Place the points of the triangle together, as shown in the bottom right figure. Notice that a straight line is formed. What was Pascal trying to show?

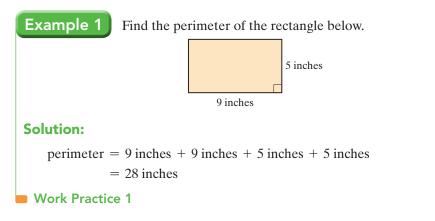
- **62.** A square is also a regular polygon.
- **64.** A trapezoid is also a parallelogram.
- **66.** A rhombus is also a parallelogram.
- **68.** In your own words, explain whether a rhombus is always a square.



8.3 Perimeter 🔘

Objective A Using Formulas to Find Perimeters 🕑

Recall from Section 1.3 that the perimeter of a polygon is the distance around the polygon. This means that the perimeter of a polygon is the sum of the lengths of its sides.



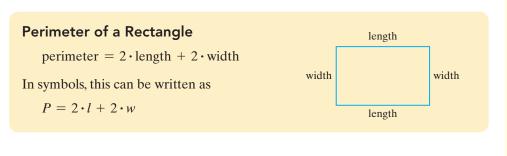
Notice that the perimeter of the rectangle in Example 1 can be written as $2 \cdot (9 \text{ inches}) + 2 \cdot (5 \text{ inches}).$

length width

In general, we can say that the perimeter of a rectangle is always

 $2 \cdot \text{length} + 2 \cdot \text{width}$

As we have just seen, the perimeters of some special figures such as rectangles form patterns. These patterns are given as **formulas.** The formula for the perimeter of a rectangle is shown next:



Example 2

Find the perimeter of a rectangle with a length of 11 inches and a width of 3 inches.

11 in.

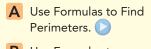
3 in.

Solution: We use the formula for perimeter and replace the letters by their known lengths.

 $P = 2 \cdot l + 2 \cdot w$ = 2 \cdot 11 in. + 2 \cdot 3 in. Replace l with 11 in. and w with 3 in. = 22 in. + 6 in. = 28 in. The perimeter is 28 inches.

Work Practice 2

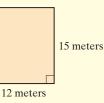
Objectives



B Use Formulas to Find Circumferences.

Practice 1

a. Find the perimeter of the rectangle.



b. Find the perimeter of the rectangular lot shown below:

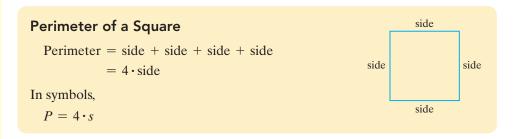


Practice 2

Find the perimeter of a rectangle with a length of 22 centimeters and a width of 10 centimeters.

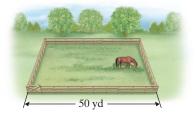
Chapter 8 | Geometry

Recall that a square is a special rectangle with all four sides the same length. The formula for the perimeter of a square is shown next:



Example 3 Finding the Perimeter of a Field

How much fencing is needed to enclose a square field 50 yards on a side?



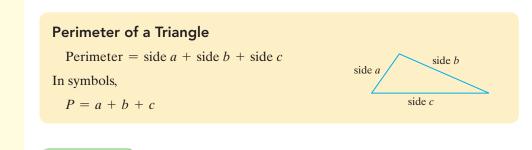
Solution: To find the amount of fencing needed, we find the distance around, or perimeter. The formula for the perimeter of a square is $P = 4 \cdot s$. We use this formula and replace s by 50 yards.

$$P = 4 \cdot s$$
$$= 4 \cdot 50 \text{ yd}$$
$$= 200 \text{ yd}$$

The amount of fencing needed is 200 yards.

Work Practice 3

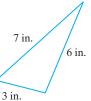
The formula for the perimeter of a triangle with sides of lengths a, b, and c is given next:



Example 4

Find the perimeter of a triangle if the sides are 3 inches, 7 inches, and 6 inches.

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Find the perimeter of a triangle if the sides are 5 centimeters, 10 centimeters, and 6 centimeters in length.

Answers 3. 20 ft 4. 21 cm

Practice 3

Find the perimeter of a square tabletop if each side is 5 feet long.



Solution: The formula for the perimeter is P = a + b + c, where a, b, and c are the lengths of the sides. Thus,

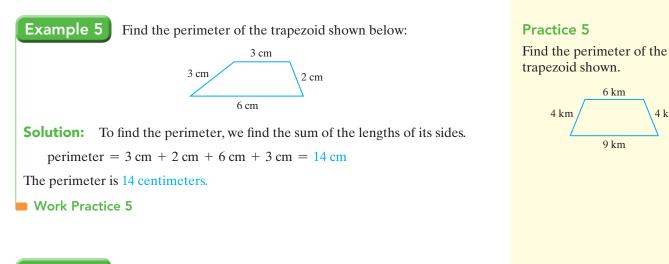
$$P = a + b + c$$

= 3 in. + 7 in. + 6 in.
= 16 in.

The perimeter of the triangle is 16 inches.

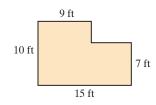
Work Practice 4

Recall that to find the perimeter of other polygons, we find the sum of the lengths of their sides.



Finding the Perimeter of a Room Example 6

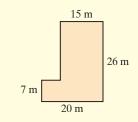
Find the perimeter of the room shown below:



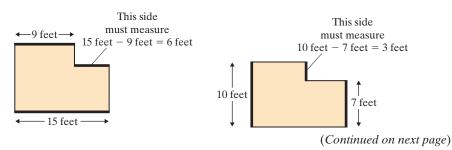


Find the perimeter of the room shown.

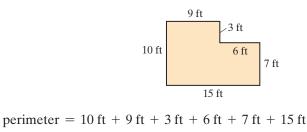
4 km



Solution: To find the perimeter of the room, we first need to find the lengths of all sides of the room.



Answers 5. 23 km 6. 92 m Now that we know the measures of all sides of the room, we can add the measures to find the perimeter.



$$= 50 \, \text{ft}$$

The perimeter of the room is 50 feet.

Work Practice 6

Example 7 Calculating the Cost of Wallpaper Border

A rectangular room measures 10 feet by 12 feet. Find the cost to hang a wallpaper border on the walls close to the ceiling if the cost of the wallpaper border is \$1.09 per foot.

Solution: First we find the perimeter of the room.

 $P = 2 \cdot l + 2 \cdot w$ = 2 \cdot 12 ft + 2 \cdot 10 ft Replace *l* with 12 feet and *w* with 10 feet. = 24 ft + 20 ft = 44 ft

The cost of the wallpaper is

 $\cos t = $1.09 \cdot 44 \text{ ft} = 47.96$

The cost of the wallpaper is \$47.96.

Work Practice 7

Objective **B** Using Formulas to Find Circumferences 🕑

Recall from Section 4.4 that the distance around a circle is called the **circumference**. This distance depends on the radius or the diameter of the circle.

The formulas for circumference are shown next:

Circumference of a Circle



Circumference = $2 \cdot \pi \cdot \text{radius}$ or Circumference = $\pi \cdot \text{diameter}$ In symbols,

$$C = 2 \cdot \pi \cdot r$$
 or $C = \pi \cdot d$

where
$$\pi \approx 3.14$$
 or $\pi \approx \frac{22}{7}$.

Practice 7

A rectangular lot measures 60 feet by 120 feet. Find the cost to install fencing around the lot if the cost of fencing is \$1.90 per foot. To better understand circumference and π (pi), try the following experiment. Take any can and measure its circumference and its diameter.



The can in the figure above has a circumference of 23.5 centimeters and a diameter of 7.5 centimeters. Now divide the circumference by the diameter.

$$\frac{\text{circumference}}{\text{diameter}} = \frac{23.5 \text{ cm}}{7.5 \text{ cm}} \approx 3.13$$

Try this with other sizes of cylinders and circles-you should always get a number close to 3.1. The exact ratio of circumference to diameter is π . (Recall that $\pi \approx 3.14$ or $\pi \approx \frac{22}{7}$.)

Example 8

Finding Circumference of Spa

Mary Catherine Dooley plans to install a border of new tiling around the circumference of her circular spa. If her spa has a diameter of 14 feet, find its exact circumference. Then use the approximation 3.14 for π to approximate the circumference.



Solution: Because we are given the diameter, we use the formula $C = \pi \cdot d$.

$$C = \pi \cdot d$$

= $\pi \cdot 14$ ft Replace *d* with 14 feet.
= 14π ft

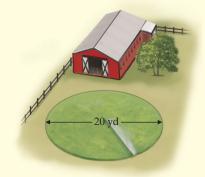
The circumference of the spa is *exactly* 14π feet. By replacing π with the *approximation* 3.14, we find that the circumference is *approximately* 14 feet $\cdot 3.14 = 43.96$ feet.

Work Practice 8

Concept Check The distance around which figure is greater: a square with side length 5 inches or a circle with radius 3 inches?

Practice 8

a. An irrigation device waters a circular region with a diameter of 20 yards. Find the exact circumference of the watered region, then use $\pi \approx 3.14$ to give an approximation.



b. A manufacturer of clocks is designing a new model. To help the designer calculate the cost of materials to make the new clock, calculate the circumference of a clock with a face diameter of 12 inches. Give the exact circumference; then use $\pi \approx 3.14$ to approximate.

Answers

8. a. exactly 20π yd ≈ 62.8 yd b. exactly 12π in. ≈ 37.68 in.

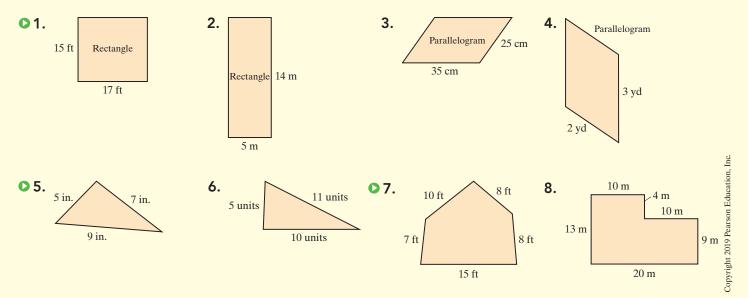
Concept Check Answer a square with side length 5 in.

Vocabulary, Readiness & Video Check

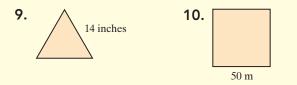
| 17 | Use the choices below to fill in each blank | | | |
|----|---|--------------|-------------------|-----------------------|
| U | Use the choices below to fill in each blank. | | | |
| | circumference | radius | π | $\frac{22}{7}$ |
| | diameter | perimeter | 3.14 | |
| 1. | The | of a polygon | is the sum of the | lengths of its sides. |
| 2. | . The distance around a circle is called the | | | |
| 3. | • The exact ratio of circumference to diameter is | | | |
| 4. | • The diameter of a circle is double its | | | |
| 5. | • Both and are approximations for π . | | | |
| 6. | • The radius of a circle is half its | | | |
| C | | | | |
| | Martin-Gay Interactive Videos Watch the section lecture video and answer the following questions. | | | |
| | Objective A 7. In Example 1, how can the perimeter be found if we forget the formula? | | | |
| | Objective B 8. From the lecture before Example 6, circumference is a special name for what? | | | |
| | see Video 8.3 🍅 | | | |

8.3 Exercise Set MyLab Math 🜔

Objective A *Find the perimeter of each figure. See Examples 1 through 6.*



Find the perimeter of each regular polygon. (The sides of a regular polygon have the same length.)

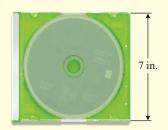


Solve. See Examples 1 through 7.

- **13.** A polygon has sides of length 5 feet, 3 feet, 2 feet, 7 feet, and 4 feet. Find its perimeter.
- **15.** A line-marking machine lays down lime powder to mark both foul lines on a baseball field. If each foul line for this field measures 312 feet, how many feet of lime powder will be deposited?
- **16.** A baseball diamond has 4 sides, with each side length 90 feet. If a baseball player hits a home run, how far does the player run (home plate, around the bases, then back to home plate)?
- **17.** If a football field is 53 yards wide and 120 yards long, what is the perimeter?

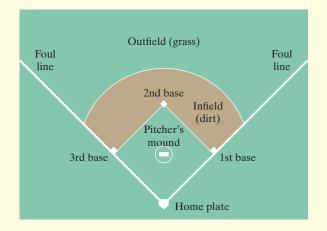


- **19.** A metal strip is being installed around a workbench that is 8 feet long and 3 feet wide. Find how much stripping is needed for this project.
- **21.** If the stripping in Exercise **19** costs \$2.50 per foot, find the total cost of the stripping.
- **23.** A regular octagon has a side length of 9 inches. Find its perimeter.
- 25. Find the perimeter of the top of a square compact disc case if the length of one side is 7 inches.





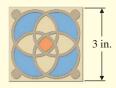
14. A triangle has sides of length 8 inches, 12 inches, and 10 inches. Find its perimeter.



18. A stop sign has eight equal sides of length 12 inches. Find its perimeter.

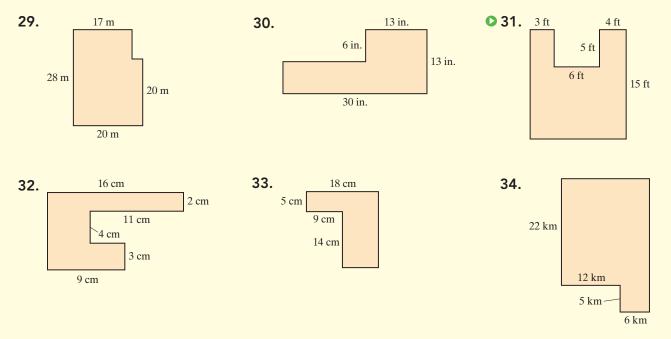


- **20.** Find how much fencing is needed to enclose a rectangular garden 70 feet by 21 feet.
- **22.** If the fencing in Exercise **20** costs \$2 per foot, find the total cost of the fencing.
- **24.** A regular pentagon has a side length of 14 meters. Find its perimeter.
- **26.** Find the perimeter of a square ceramic tile with a side of length 3 inches.

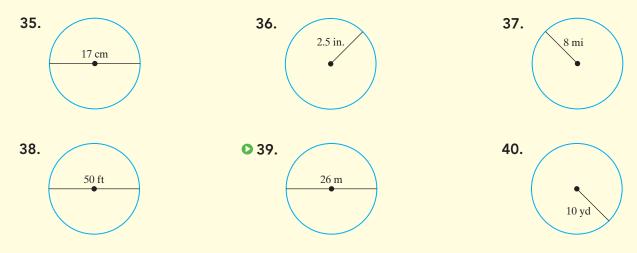


- **27.** A rectangular room measures 10 feet by 11 feet. Find the cost of installing a strip of wallpaper around the room if the wallpaper costs \$0.86 per foot.
- **28.** A rectangular house measures 85 feet by 70 feet. Find the cost of installing gutters around the house if the cost is \$2.36 per foot.

Find the perimeter of each figure. See Example 6.



Objective B *Find the circumference of each circle. Give the exact circumference and then an approximation. Use* $\pi \approx 3.14$ *. See Example 8.*



Solve.

- **41.** The largest round barn in the world is located at the Marshfield Fairgrounds in Wisconsin. The barn has a diameter of 150 ft. What is the circumference of the barn? Give the exact circumference and then an approximation using $\pi \approx 3.14$. (Source: The Milwaukee Journal Sentinel)
- **42.** Wyley Robinson just bought a trampoline for his children to use. The trampoline has a diameter of 15 feet. If Wyley wishes to buy netting to go around the outside of the trampoline, how many feet of netting does he need? Give the exact circumference and then an approximation using $\pi \approx 3.14$.

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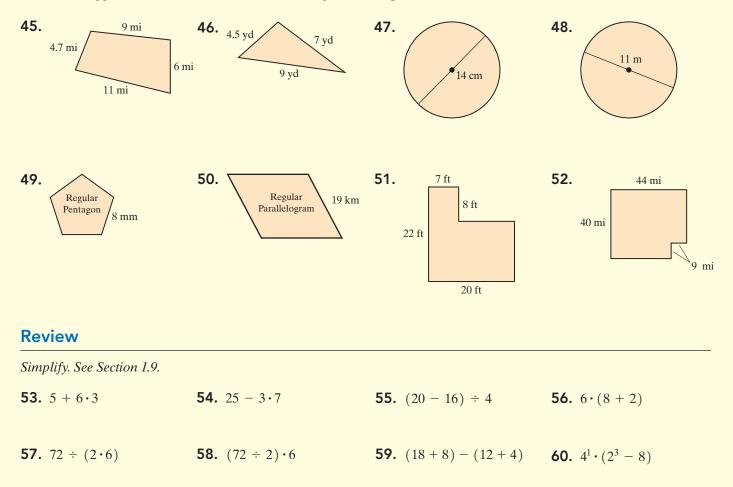
43. Meteor Crater, near Winslow, Arizona, is 4000 feet in diameter. Approximate the distance around the crater. Use 3.14 for π . (*Source: The Handy Science Answer Book*)



44. The largest pearl, the *Pearl of Lao-tze*, has a diameter of $5\frac{1}{2}$ inches. Approximate the distance around the pearl. Use $\frac{22}{7}$ for π . (*Source: The Guinness Book of World Records*)



Objectives A B Mixed Practice *Find the distance around each figure. For circles, give the exact circumference and then an approximation. Use* $\pi \approx 3.14$ *. See Examples 1 through 8.*



Concept Extensions

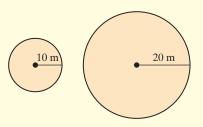
There are a number of factors that determine the dimensions of a rectangular soccer field. Use the table below to answer Exercises 61 and 62.

| Soccer Field Width and Length | | | |
|-------------------------------|---------------|----------------|--|
| Age | Width Min–Max | Length Min–Max | |
| Under 6/7: | 15–20 yards | 25-30 yards | |
| Under 8: | 20–25 yards | 30-40 yards | |
| Under 9: | 30-35 yards | 40–50 yards | |
| Under 10: | 40–50 yards | 60–70 yards | |
| Under 11: | 40–50 yards | 70–80 yards | |
| Under 12: | 40–55 yards | 100–105 yards | |
| Under 13: | 50–60 yards | 100–110 yards | |
| International: | 70–80 yards | 110-120 yards | |

- **61. a.** Find the minimum length and width of a soccer field for 8-year-old children. (Carefully consider the age.)
 - **b.** Find the perimeter of this field.
- **62. a.** Find the maximum length and width of a soccer field for 12-year-old children.
 - **b.** Find the perimeter of this field.

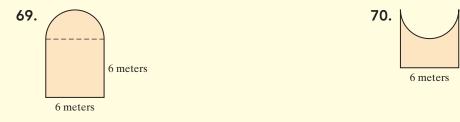
Solve. See the Concept Check in this section. Choose the figure that has the greater distance around.

- **63. a.** A square with side length 3 inches
 - **b.** A circle with diameter 4 inches
- **65. a.** Find the circumference of each circle. Approximate the circumference by using 3.14 for π .

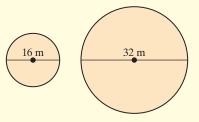


- **b.** If the radius of a circle is doubled, is its corresponding circumference doubled?
- **67.** In your own words, explain how to find the perimeter of any polygon.

Find the perimeter. Round your results to the nearest tenth.



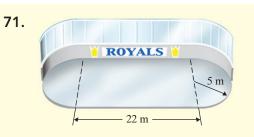
- **64. a.** A circle with diameter 7 inches
 - **b.** A square with side length 7 inches
- **66. a.** Find the circumference of each circle. Approximate the circumference by using 3.14 for π .



- **b.** If the diameter of a circle is doubled, is its corresponding circumference doubled?
- **68.** In your own words, explain how perimeter and circumference are the same and how they are different.

6 meters

72.



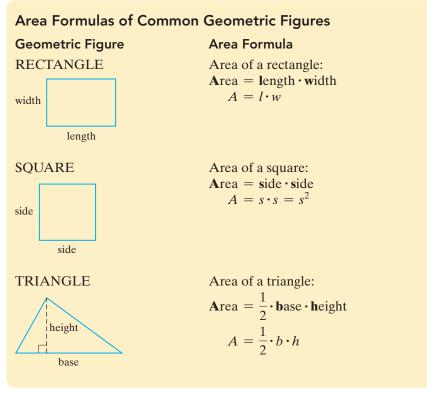
73. The perimeter of this rectangle is 31 feet. Find its width.

9 ft ?

8.4 Area 🔘

Objective 🗛 Finding Areas of Geometric Figures 🕑

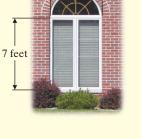
Recall that area measures the amount of surface of a region. Thus far, we know how to find the area of a rectangle and a square. These formulas, as well as formulas for finding the areas of other common geometric figures, are given next:



Objective

A Find the Areas of Geometric Figures.

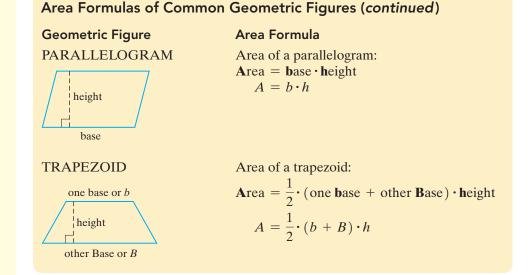
74. The perimeter of this square is 18 inches. Find the length of a side.



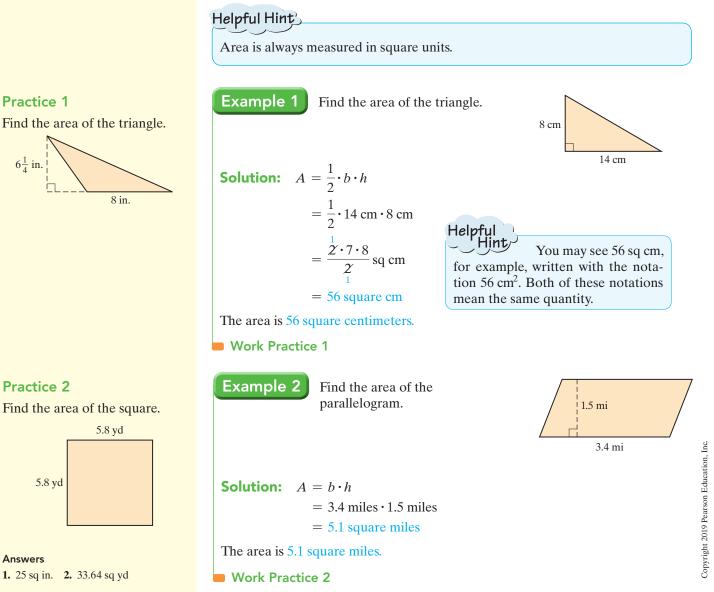
← 5 feet -



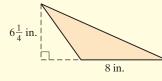
(Continued on next page)

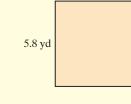


Use these formulas for the following examples.



Practice 1

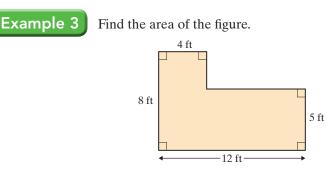


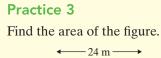


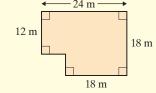
Answers 1. 25 sq in. 2. 33.64 sq yd

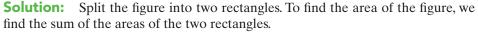
Helpful Hint

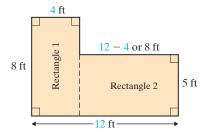
When finding the area of figures, be sure all measurements are changed to the same unit before calculations are made.











Area of Rectangle $1 = l \cdot w$

 $= 8 \text{ feet} \cdot 4 \text{ feet}$

= 32 square feet

Notice that the length of Rectangle 2 is 12 feet -4 feet, or 8 feet.

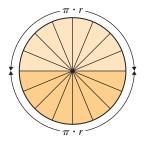
Area of Rectangle $2 = l \cdot w$ $= 8 \text{ feet} \cdot 5 \text{ feet}$ = 40 square feetArea of the Figure = Area of Rectangle 1 + Area of Rectangle 2 = 32 square feet + 40 square feet= 72 square feet





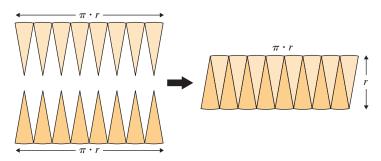
The figure in Example 3 can also be split into two rectangles as shown: 4 ft Rectangle 1 8 ft Rectangle 2 12 ft

Answer 3. 396 sq m To better understand the formula for area of a circle, try the following. Cut a circle into many pieces as shown:



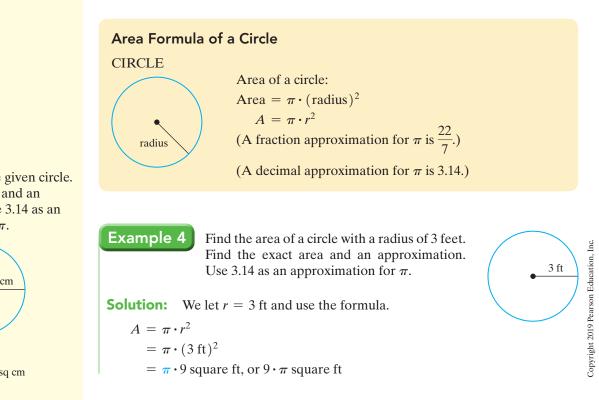
The circumference of a circle is $2 \cdot \pi \cdot r$. This means that the circumference of half a circle is half of $2 \cdot \pi \cdot r$, or $\pi \cdot r$.

Then unfold the two halves of the circle and place them together as shown:



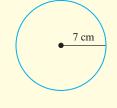
The figure on the right is almost a parallelogram with a base of $\pi \cdot r$ and a height of *r*. The area is

This is the formula for area of a circle.



Practice 4

Find the area of the given circle. Find the exact area and an approximation. Use 3.14 as an approximation for π .



Answer 4. 49π sq cm ≈ 153.86 sq cm To approximate this area, we substitute 3.14 for π .

 $9 \cdot \pi$ square feet $\approx 9 \cdot 3.14$ square feet = 28.26 square feet

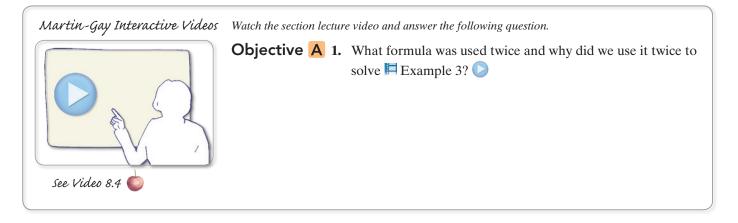
The *exact* area of the circle is 9π square feet, which is *approximately* 28.26 square feet.

Work Practice 4

Concept Check Use diagrams to decide which figure would have a larger area: a circle of diameter 10 inches or a square 10 inches long on each side.

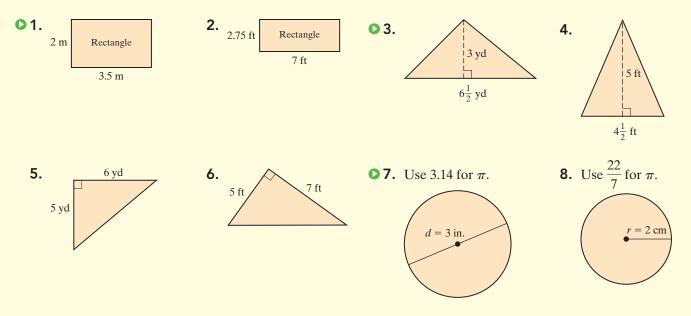
Concept Check Answer a square 10 in. long on each side

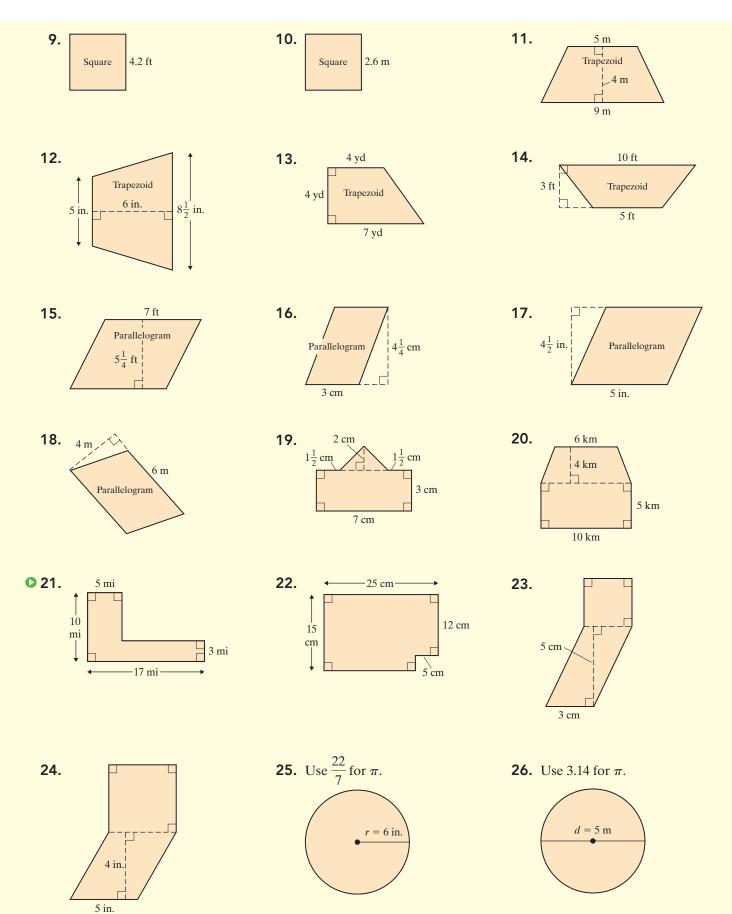
Vocabulary, Readiness & Video Check



8.4 Exercise Set MyLab Math

Objective A Find the area of the geometric figure. If the figure is a circle, give the exact area and then use the given approximation for π to approximate the area. See Examples 1 through 4.

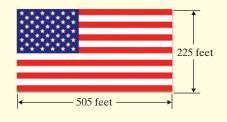




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Solve. See Examples 1 through 4.

- **27.** A $10\frac{1}{2}$ -foot by 16-foot concrete wall is to be built using concrete blocks. Find the area of the wall.
- **29.** The world's largest U.S. flag is the "Superflag," which measures 505 feet by 255 feet. Find its area. (*Source:* Superflag.com)



31. The face of a watch has a diameter of 2 centimeters. What is its area? Give the exact answer then an approximation using 3.14 for π .



- **28.** The floor of Terry's attic is 24 feet by 35 feet. Find how many square feet of insulation are needed to cover the attic floor.
- **30.** The world's largest illuminated indoor advertising sign is located in the Dubai International Airport in Dubai, UAE. It measures 28.0 meters in length by 6.2 meters in height. Find its area. (*Source:* World Record Academy)



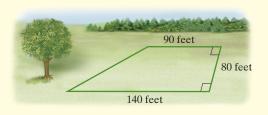
32. The world's largest commercially available pizza is sold by Big Mama's & Papa's Pizzeria in Los Angeles, CA. This huge square pizza, called "The Giant Sicilian," measures 54 inches on each side and sells for \$199.99 plus tax. Find the area of the top of the pizza. (*Source:* Guinness World Records, Big Mama's & Big Papa's Pizzeria Inc.)



- **34.** A standard *double* roll of wallpaper is $6\frac{5}{6}$ feet wide and 33 feet long. Find the area of the *double* roll.
 - **36.** A mat to go under a tablecloth is made to fit a round dining table with a 4-foot diameter. Approximate how many square feet of mat there are. Use 3.14 as an approximation for π .
 - **38.** A page in a book measures 27.5 centimeters by 20.5 centimeters. Find its area.

- **33.** One side of a concrete block measures 8 inches by 16 inches. Find the area of the side in square inches. Find the area in square feet (144 sq in. = 1 sq ft).
- **35.** A picture frame measures 20 inches by $25\frac{1}{2}$ inches. Find how many square inches of glass the frame requires.
- 37. A drapery panel measures 6 feet by 7 feet. Find how many square feet of material are needed for *four* panels.

39. Find how many square feet of land are in the plot shown:

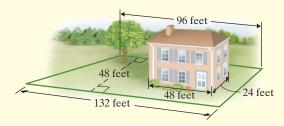


- **41.** The outlined part of the roof shown is in the shape of a trapezoid and needs to be shingled. The number of shingles to buy depends on the area.
 - **a.** Use the dimensions given to find the area of the outlined part of the roof to the nearest whole square foot.



b. Shingles are packaged in a unit called a "square." If a "square" covers 100 square feet, how many whole squares need to be purchased to shingle this part of the roof?

40. For Gerald Gomez to determine how much grass seed he needs to buy, he must know the size of his yard. Use the drawing to determine how many square feet are in his yard.



- **42.** The entire side of the building shaded in the drawing is to be bricked. The number of bricks to buy depends on the area.
 - **a.** Find the area.

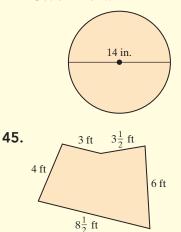


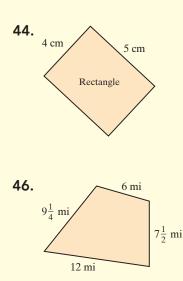
b. If the side area of each brick (including mortar room) is $\frac{1}{6}$ square foot, find the number of bricks needed to brick the end of the building.

Review

Find the perimeter or circumference of each geometric figure. See Section 8.3.

43. Give the exact circumference and an approximation. Use 3.14 for π .



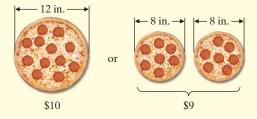




Concept Extensions

Given the following situations, tell whether you are more likely to be concerned with area or perimeter.

- **49.** ordering fencing to fence a yard
- **51.** buying carpet to install in a room
- **53.** ordering paint to paint a wall
- **55.** buying a wallpaper border to go on the walls around a room
- **57.** A pizza restaurant recently advertised two specials. The first special was a 12-inch diameter pizza for \$10. The second special was two 8-inch diameter pizzas for \$9. Determine the better buy. (*Hint:* First find and compare the areas of the pizzas in the two specials. Then find a price per square inch for the pizzas in both specials.)



- **59.** Find the area of a rectangle that measures 2 *feet* by 8 *inches*. Give the area in square feet and in square inches.
- **61.** Find the area of the shaded region. Use the approximation 3.14 for π .



48. Equilateral triangle 3 in.

- 50. ordering grass seed to plant in a yard
- **52.** buying gutters to install on a house
- **54.** ordering baseboards to install in a room
- 56. buying fertilizer for your yard
- **58.** Find the approximate area of the state of Utah.

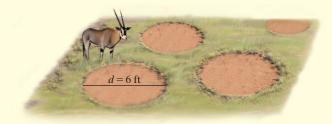


- **60.** In your own words, explain why perimeter is measured in units and area is measured in square units. (*Hint:* See Section 1.6 for an introduction on the meaning of area.)
 - **62.** Estimate the cost of a piece of carpet for a rectangular room 10 feet by 15 feet. The cost of the carpet is \$6.50 per yard.

63. The average pupil of a 20-year-old is 4.6 mm in diameter. Find the exact area of the average pupil and an approximation. Use $\pi \approx 3.14$. (*Source: National Geographic*)

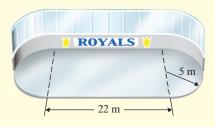


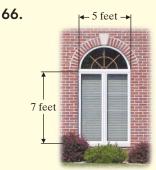
64. The desert grasslands of Namibia are dotted with tens of thousands of grassless spots, roughly circular in shape. These are naturally occurring patches, and the smallest of them measures about 6 feet in diameter. Calculate the exact area of this circle and an approximation. Use $\pi \approx 3.14$. (*Source: National Geographic*)



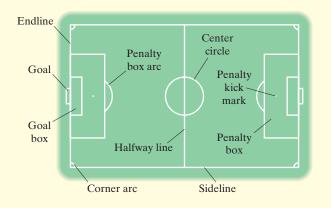
Find the area of each figure. Use $\pi \approx 3.14$ and round results to the nearest tenth.

65. Find the skating area.



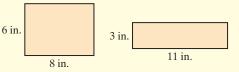


There are a number of factors that determine the dimensions of a rectangular soccer field. Use the table below to answer Exercises 67 and 68.



- Soccer Field Width and Length Width Min-Max Length Min-Max Age Under 6/7: 15-20 yards 25-30 yards Under 8: 20-25 yards 30-40 yards Under 9: 30-35 yards 40-50 yards Under 10: 40-50 yards 60-70 yards Under 11: 40-50 yards 70-80 yards Under 12: 40-55 yards 100-105 yards Under 13: 50-60 yards 100-110 yards 110-120 yards International: 70-80 yards
- **67. a.** Find the minimum length and width of a soccer field for 9-year-old children. (Carefully consider the age.)
 - **b.** Find the area of this field.

- **68. a.** Find the maximum length and width of a soccer field for 11-year-old children.
 - **b.** Find the area of this field.
- **69.** Do two rectangles with the same perimeter have the same area? To see, find the perimeter and the area of each rectangle.

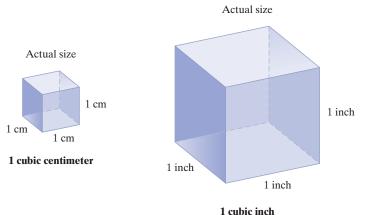


8.5 Volume 🔘

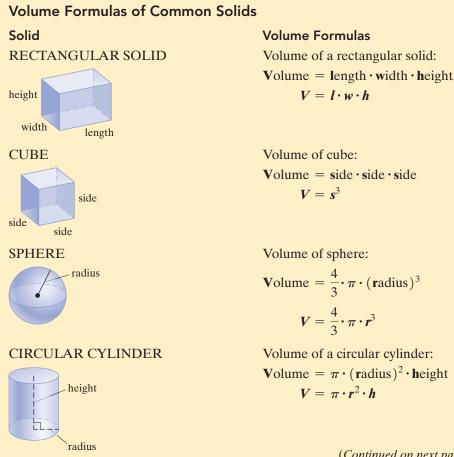
Objective A Finding Volumes of Solids

Volume is a measure of the space of a region. The volume of a box or can, for example, is the amount of space inside. Volume can be used to describe the amount of juice in a pitcher or the amount of concrete needed to pour a foundation for a house.

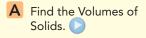
The volume of a solid is the number of cubic units in the solid. A cubic centimeter and a cubic inch are illustrated.



Formulas for finding the volumes of some common solids are given next:



Objective



(*Continued on next page*)

Volume Formulas of Common Solids (continued)

Solid CONE



SQUARE-BASED PYRAMID

height

side

Volume of a cone: Volume = $\frac{1}{3} \cdot \pi \cdot (\mathbf{r} \text{adius})^2 \cdot \mathbf{h}$ eight $V = \frac{1}{3} \cdot \pi \cdot \mathbf{r}^2 \cdot \mathbf{h}$

Volume Formulas

Volume of a square-based pyramid:

Volume =
$$\frac{1}{3} \cdot (\text{side})^2 \cdot \mathbf{h}$$
eight
 $V = \frac{1}{3} \cdot s^2 \cdot h$

Example 1

Find the volume of a rectangular box that is 12 inches long, 6 inches wide, and 3 inches high.



Solution:

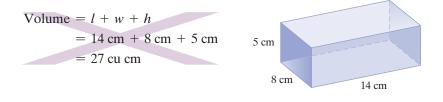
$$V = l \cdot w \cdot h$$

V = 12 in. $\cdot 6$ in. $\cdot 3$ in. = 216 cubic in.

The volume of the rectangular box is 216 cubic inches.

Work Practice 1

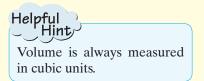
Concept Check Juan is calculating the volume of the following rectangular solid. Find the error in his calculation.





Find the volume of a ball of radius 2 inches. Give the exact answer and an approximate answer. Use the approximation $\frac{22}{7}$ for π .





Practice 1

Find the volume of a rectangular box that is 5 feet long, 2 feet wide, and 4 feet deep.

Practice 2

Find the volume of a ball of radius $\frac{1}{2}$ centimeter. Give the exact answer and an approximate answer. Use $\frac{22}{7}$ for π .



1. 40 cu ft **2.** $\frac{1}{6} \pi$ cu cm $\approx \frac{11}{21}$ cu cm **Concept Check Answer**

Volume = $l \cdot w \cdot h$

- $= 14 \text{ cm} \cdot 8 \text{ cm} \cdot 5 \text{ cm}$
 - = 560 cu cm

Solution:

$$V = \frac{4}{3} \cdot \pi \cdot r^{3}$$
$$= \frac{4}{3} \cdot \pi (2 \text{ in.})^{3}$$
$$= \frac{4}{3} \cdot \pi \cdot 8 \text{ cu in.}$$
$$= \frac{32}{3} \pi \text{ cu in.}$$

This is the exact volume. To approximate the volume, use the approximation $\frac{22}{7}$ for π .

$$V = \frac{32}{3}\pi \text{ cu in.}$$

$$\approx \frac{32}{3} \cdot \frac{22}{7} \text{ cu in.} \quad \text{Replace } \pi \text{ with } \frac{22}{7}.$$

$$= \frac{32 \cdot 22}{3 \cdot 7} \text{ cu in.}$$

$$= \frac{704}{21} \text{ or } 33\frac{11}{21} \text{ cubic inches.}$$
The volume is exactly $\frac{32}{3}\pi$ cubic inches and *approximately* 33 $\frac{11}{21}$ cubic inches.

Work Practice 2

Example 3

Approximate the volume of a can that has a $3\frac{1}{2}$ -inch radius and a height of 6 inches. Give the exact volume and an approximate volume. Use $\frac{22}{7}$ for π .

Chicken & Dumpling Chicken & Dumpling Grint Vegetables

Solution: Using the formula for a circular cylinder, we have

$$V = \pi \cdot r^2 \cdot h$$

$$= \pi \cdot \left(\frac{7}{2} \text{ in.}\right)^2 \cdot 6 \text{ in.}$$

$$= \pi \cdot \frac{49}{4} \text{ sq in.} \cdot 6 \text{ in.}$$

$$= \frac{\pi \cdot 49 \cdot \frac{1}{2} \cdot 3}{\frac{2}{1} \cdot 2} \text{ cu in.}$$

$$= 73 \frac{1}{2} \pi \text{ cu in. or } 73.5\pi \text{ cu in.}$$

Practice 3

Find the volume of a cylinder of radius 5 inches and height 7 inches. Give the exact answer and an approximate answer. Use 3.14 for π .

This is the exact volume. To approximate the volume, use the approximation $\frac{22}{7}$ for π .

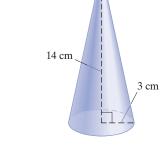
$$V = 73 \frac{1}{2} \pi \approx \frac{147}{2} \cdot \frac{22}{7} \text{ cu in.} \quad \text{Replace } \pi \text{ with } \frac{22}{7}.$$
$$= \frac{21 \cdot \frac{1}{7} \cdot \frac{1}{2} \cdot 11}{2 \cdot \frac{7}{1}} \text{ cu in.}$$
$$= 231 \text{ cubic in}$$

The volume is exactly 73.5 π cubic inches and approximately 231 cubic inches.

Work Practice 3

Example 4

Find the volume of a cone that has a height of 14 centimeters and a radius of 3 centimeters. Give the exact answer and an approximate answer. Use 3.14 for π .



Solution: Using the formula for volume of a cone, we have

$$V = \frac{1}{3} \cdot \pi \cdot r^2 \cdot h$$

= $\frac{1}{3} \cdot \pi \cdot (3 \text{ cm})^2 \cdot 14 \text{ cm}$ Replace *r* with 3 cm and *h* with 14 cm
= 42π cu cm

Thus, 42π cubic centimeters is the exact volume. To approximate the volume, use the approximation 3.14 for π .

$$V \approx 42 \cdot 3.14$$
 cu cm Replace π with 3.14.
= 131.88 cu cm

The volume is exactly 42π cubic centimeters and approximately 131.88 cubic centimeters.

Work Practice 4

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Some exercises are from Sections 8.3 and 8.4.

| cubic | perimeter | volume |
|-------|-----------|--------|
| units | area | square |

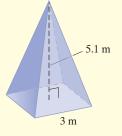
- 1. The measure of the amount of space inside a solid is its _____.
- 2. _____ measures the amount of surface of a region.
- **3.** Volume is measured in _____ units.

Practice 4

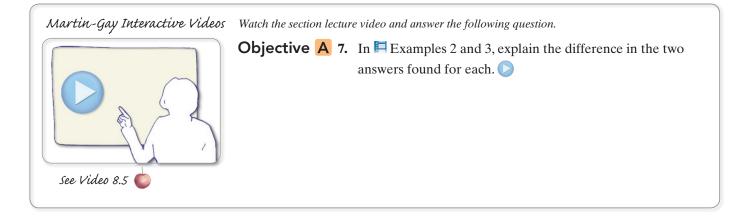
Answer

4. 15.3 cu m

Find the volume of a squarebased pyramid that has a 3-meter side and a height of 5.1 meters.

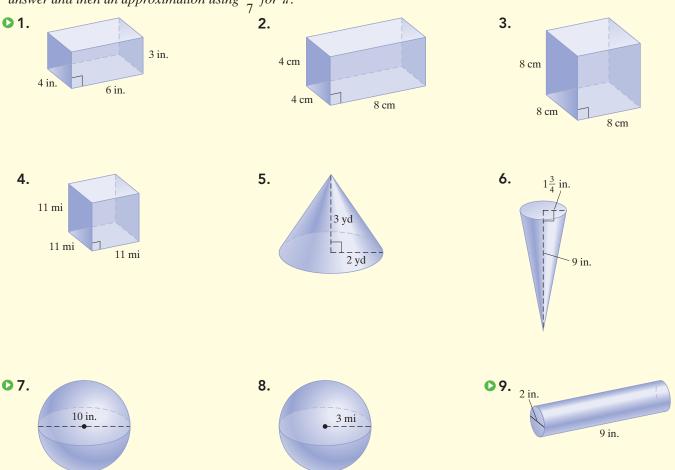


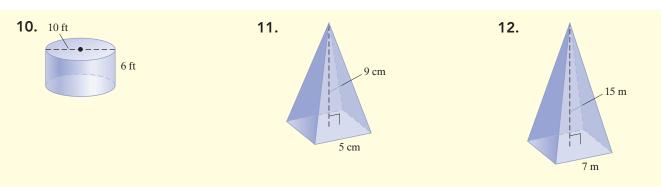
- 4. Area is measured in _____ units.
- 5. The ______ of a polygon is the sum of the lengths of its sides.
- 6. Perimeter is measured in _____



8.5 Exercise Set MyLab Math

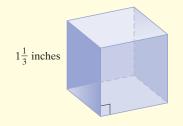
Objective A Find the volume of each solid. See Examples 1 through 4. For formulas containing π , give the exact answer and then an approximation using $\frac{22}{7}$ for π .





Solve.

• **13.** Find the volume of a cube with edges of $1\frac{1}{3}$ inches.



- **15.** Find the volume of a rectangular box 2 feet by 1.4 feet by 3 feet.
- 17. Find the volume of a pyramid with a square base 5 inches on a side and a height of $1 \frac{3}{10}$ inches.
- **19.** A paperweight is in the shape of a square-based pyramid 20 centimeters tall. If an edge of the base is 12 centimeters, find the volume of the paperweight.



- **21.** Find the exact volume of a sphere with a radius of 7 inches.
- **23.** Find the volume of a rectangular block of ice 2 feet by $2\frac{1}{2}$ feet by $1\frac{1}{2}$ feet.

14. A water storage tank is in the shape of a cone with the pointed end down. If the radius is 14 feet and the depth of the tank is 15 feet, approximate the volume

of the tank in cubic feet. Use $\frac{22}{7}$ for π .



- **16.** Find the volume of a box in the shape of a cube that is 5 feet on each side.
- **18.** Approximate to the nearest hundredth the volume of a sphere with a radius of 2 centimeters. Use 3.14 for π .
- **20.** A birdbath is made in the shape of a hemisphere (half-sphere). If its radius is 10 inches, approximate the volume. Use $\frac{22}{7}$ for π .



- **22.** A tank is in the shape of a cylinder 8 feet tall and 3 feet in radius. Find the exact volume of the tank.
- 24. Find the capacity (volume in cubic feet) of a rectangular ice chest with inside measurements of 3 feet

by
$$1\frac{1}{2}$$
 feet by $1\frac{3}{4}$ feet.

25. In 2013, the largest free-floating soap bubble made with a wand had a diameter between 11 and 12 feet. Calculate the exact volume of a sphere with a diameter of 12 feet. (*Source:* Guinness World Records)



● 27. Find the exact volume of a waffle ice cream cone with a 3-in. diameter and a height of 7 inches.



29. Zorbing is an extreme sport invented by two New Zealanders who joke that they were looking for a way to walk on water. A Zorb is a large sphere inside

a second sphere with the space between the spheres pumped full of air. There is a tunnel-like opening so a person can crawl into the inner sphere. You are strapped in and sent down a Zorbing hill. A standard Zorb is approximately 3 m in diameter. Find the exact volume of a Zorb, and approximate the volume using 3.14 for π .



31. An ice cream cone with a 4-centimeter diameter and 3-centimeter depth is filled exactly level with the top of the cone. Approximate how much ice cream (in cubic

centimeters) is in the cone. Use $\frac{22}{7}$ for π .

26. The largest inflatable beach ball was created in Poland in 2012. It has a diameter of just under 54 feet. Calculate the exact volume of a sphere with a diameter of 54 feet. (*Source:* Guinness World Records)



28. A snow globe has a diameter of 6 inches. Find its exact volume. Then approximate its volume using 3.14 for π .



30. Mount Fuji, in Japan, is considered the most beautiful composite volcano in the world. The mountain is in the shape of a cone whose height is about 3.5 kilometers and whose base radius is about 3 kilometers. Approximate the volume of Mt. Fuji

in cubic kilometers. Use $\frac{22}{7}$ for π .



32. A child's toy is in the shape of a square-based pyramid 10 inches tall. If an edge of the base is 7 inches, find the volume of the toy.

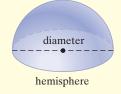
The Space Cube is supposed to be the world's smallest computer, with dimensions of 2 inches by 2 inches by 2.2 inches.

- **33.** Find the volume of the Space Cube.
- **35.** Find the volume of an actual cube that measures 2.2 inches by 2.2 inches by 2.2 inches.
- **34.** Find the volume of an actual cube that measures 2 inches by 2 inches by 2 inches.
- 36. Comment on the results of Exercises 33–35.Were you surprised when you compared volumes? Why or why not?

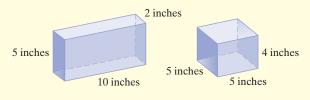
| Review | | | |
|----------------------------|---------------------------|---------------------------|----------------------------|
| Evaluate. See Section 1.9. | | | |
| 37. 5 ² | 38. 7 ² | 39. 3 ² | 40. 20 ² |
| 41. $1^2 + 2^2$ | 42. $5^2 + 3^2$ | 43. $4^2 + 2^2$ | 44. $1^2 + 6^2$ |

Concept Extensions

45. The Hayden Planetarium, at the Museum of Natural History in New York City, boasts a dome that has a diameter of 20 m. The dome is a hemisphere, or half a sphere. What is the volume enclosed by the dome at the Hayden Planetarium? Use 3.14 for π and round to the nearest hundredth. (*Source:* Hayden Planetarium)



47. Do two rectangular solids with the same volume have the same shape? To help, find the volume of each rectangular solid.

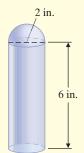


49. Two kennels are offered at a hotel. The kennels measurea. 2'1" by 1'8" by 1'7" and

b. 1'1" by 2' by 2'8"

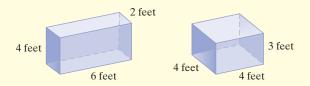
What is the volume of each kennel rounded to the nearest tenth of a cubic foot? Which is larger? (*Note:* 2'1" means 2 feet 1 inch)

51. Find the volume of the figure below. Give the exact measure and then a whole number approximation.



46. The Adler Museum in Chicago recently added a new planetarium, its StarRider Theater, which has a diameter of 55 feet. Find the volume of its hemispheric (half a sphere) dome. Use 3.14 for π and round to the nearest hundredth. (*Source:* The Adler Museum)

48. Do two rectangular solids with the same volume have the same surface area? To see, find the volume and surface area of each rectangular solid. Surface area is the area of the surface of the solid. To find the surface area of each rectangular solid, find the sum of the areas of the 6 rectangles that form each solid.



- **50.** The centerpiece of the New England Aquarium in Boston is its Giant Ocean Tank. This exhibit is a multistory cylindrical saltwater tank containing a coral reef and hundreds of Caribbean reef animals. The radius of the tank is 20 feet, and its height is 30 feet. What is the volume of the Giant Ocean Tank? Use $\pi \approx 3.14$. (*Source:* New England Aquarium)
- **52.** Can you compute the volume of a rectangle? Why or why not?

Integrated Review

Sections 8.1-8.5 **Geometry Concepts** Answers 1. \triangle **1.** Find the supplement and the complement of a 27° angle. Find the measures of angles x, y, and z in each figure. 2. **3.** *m*∥*n* 2. 105 3. < z. 52° 4. n 5. **4.** Find the measure of $\angle x$. **5.** Find the diameter. **6.** Find the radius. 6. 2.3 in. $8\frac{1}{2}$ in. 38° 7. 8. For Exercises 7 through 11, find the perimeter (or circumference) and area of each figure. For the circle give the exact circumference and area. Then use $\pi \approx 3.14$ to approximate each. Don't forget to attach correct units. 9. 7. 8. 9. 10. 4 ft 11 mi 5 cm Square 5 m Parallelogram 5 mi 3 ft 5 ft 4 mi 10. 11. 11. **12.** The smallest cathedral is in High-8 cm landville, Missouri. The rectangular floor 3 cm of the cathedral measures 14 feet by 12. 17 feet. Find its perimeter and its area. 7 cm (Source: The Guinness Book of Records) 17 cm 13. Find the volume of each solid. Don't forget to attach correct units.

- **13.** A cube with edges of 4 inches each.
- **15.** A pyramid with a square base 10 centimeters on a side and a height of 12 centimeters.
- **14.** A rectangular box 2 feet by 3 feet by 5.1 feet.
- **16.** A sphere with a diameter of 3 miles. Give the exact volume and then use

$$\pi \approx \frac{22}{7}$$
 to approximate.

553

14.

15.

16.

Square Roots and the PythagoreanTheorem

Objectives

- A Find the Square Root of a Number.
- B Approximate Square Roots.
- C Use the Pythagorean Theorem.

Practice 1

Find each square root. **a.** $\sqrt{100}$ **b.** $\sqrt{64}$ **c.** $\sqrt{121}$ **d.** $\sqrt{0}$

Practice 2

Find: $\sqrt{\frac{1}{4}}$

Practice 3 Find: $\sqrt{\frac{9}{16}}$ Answers 1. a. 10 b. 8 c. 11 d. 0 2. $\frac{1}{2}$ 3. $\frac{3}{4}$ 554

Objective 🗛 Finding Square Roots 🕑

The square of a number is the number times itself. For example:

The square of 5 is 25 because 5^2 or $5 \cdot 5 = 25$. The square of 4 is 16 because 4^2 or $4 \cdot 4 = 16$. The square of 10 is 100 because 10^2 or $10 \cdot 10 = 100$.

Recall from Chapter 1 that the reverse process of squaring is finding a **square root.** For example:

A square root of 16 is 4 because $4^2 = 16$.

A square root of 25 is 5 because $5^2 = 25$.

A square root of 100 is 10 because $10^2 = 100$.

We use the symbol $\sqrt{}$, called a **radical sign**, to name square roots. For example:

 $\sqrt{16} = 4$ because $4^2 = 16$ $\sqrt{25} = 5$ because $5^2 = 25$

Square Root of a Number

A square root of a number *a* is a number *b* whose square is *a*. We use the radical sign $\sqrt{}$ to name square roots. In symbols,

 $\sqrt{a} = b$ if $b^2 = a$ Also, $\sqrt{0} = 0$

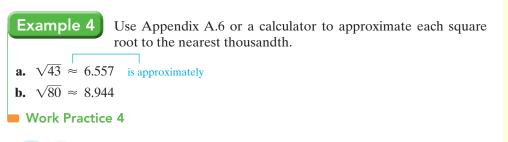
| Example 1 Find each square root. |
|---|
| a. $\sqrt{49}$ b. $\sqrt{1}$ c. $\sqrt{81}$ |
| Solution: |
| a. $\sqrt{49} = 7$ because $7^2 = 49$ |
| b. $\sqrt{1} = 1$ because $1^2 = 1$
c. $\sqrt{81} = 9$ because $9^2 = 81$ |
| Work Practice 1 |
| Example 2 Find: $\sqrt{\frac{1}{36}}$ |
| Solution: $\sqrt{\frac{1}{36}} = \frac{1}{6}$ because $\frac{1}{6} \cdot \frac{1}{6} = \frac{1}{36}$ |
| Work Practice 2 |
| Example 3 Find: $\sqrt{\frac{4}{25}}$ |
| Solution: $\sqrt{\frac{4}{25}} = \frac{2}{5}$ because $\frac{2}{5} \cdot \frac{2}{5} = \frac{4}{25}$ |
| Work Practice 3 |
| |

Objective **B** Approximating Square Roots 💟

Thus far, we have found square roots of perfect squares. Numbers like $\frac{1}{4}$, 36, $\frac{4}{25}$, and

1 are called **perfect squares** because their square root is a whole number or a fraction. A square root such as $\sqrt{5}$ cannot be written as a whole number or a fraction since 5 is not a perfect square.

Although $\sqrt{5}$ cannot be written as a whole number or a fraction, it can be approximated by estimating, by using a table (as in the appendix), or by using a calculator.



Helpful Hint

 $\sqrt{80}$, above, is *approximately* 8.944. This means that if we multiply 8.944 by 8.944, the product is *close* to 80.

 $8.944 \times 8.944 \approx 79.995$

It is possible to approximate a square root to the nearest whole number without the use of a calculator or table. To do so, study the number line below and look for patterns.

Above the number line, notice that as the numbers under the radical signs increase, their values, and thus their placement on the number line, increase also.

Example 5

Without a calculator or table:

- **a.** Determine which two whole numbers $\sqrt{78}$ is between.
- **b.** Use part **a** to approximate $\sqrt{78}$ to the nearest whole.

Solution:

a. Review perfect squares and recall that $\sqrt{64} = 8$ and $\sqrt{81} = 9$. Since 78 is between 64 and 81, $\sqrt{78}$ is between $\sqrt{64}$ (or 8) and $\sqrt{81}$ (or 9).



Thus, $\sqrt{78}$ is between 8 and 9.

- **b.** Since 78 is closer to 81, then (as our number line shows) $\sqrt{78}$ is closer to $\sqrt{81}$, or 9.
- Work Practice 5

Objective C Using the Pythagorean Theorem 🕑

One important application of square roots has to do with right triangles. Recall that a **right triangle** is a triangle in which one of the angles is a right angle, or measures 90° (degrees). The **hypotenuse** of a right triangle is the side opposite the right angle.

Practice 4

Use Appendix A.6 or a calculator to approximate each square root to the nearest thousandth.

a. $\sqrt{21}$ **b.** $\sqrt{52}$

Practice 5

Without a calculator or table, approximate $\sqrt{62}$ to the nearest whole.

Answers 4. a. 4.583 b. 7.211 5. 8

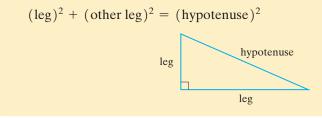
Chapter 8 | Geometry

The legs of a right triangle are the other two sides. These are shown in the following figure. The right angle in the triangle is indicated by the small square drawn in that angle.

The following theorem is true for all right triangles:

Pythagorean Theorem

In any right triangle,



Using the Pythagorean theorem, we can use one of the following formulas to find an unknown length of a right triangle:

Finding an Unknown Length of a Right Triangle

hypotenuse =
$$\sqrt{(\log)^2 + (\text{other leg})}$$

or

 $leg = \sqrt{(hypotenuse)^2 - (other leg)^2}$

Example 6

Find the length of the hypotenuse of the given right triangle.

Solution: Since we are finding the hypotenuse, we use the formula

hypotenuse =
$$\sqrt{(\log)^2 + (\text{other leg})^2}$$

The hypotenuse is 10 feet long.

Work Practice 6

Example 7

Putting the known values into the formula, we have

hypotenuse =
$$\sqrt{(6)^2 + (8)^2}$$
 The legs are 6 feet and 8 feet.
= $\sqrt{36 + 64}$
= $\sqrt{100}$
= 10

6 ft 8 ft

Practice 6

Find the length of the hypotenuse of the given right triangle.

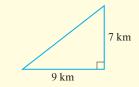
> 12 ft 16 ft

Practice 7

Answers

6. 20 ft 7. 11 km

Approximate the length of the hypotenuse of the given right triangle. Round to the nearest whole unit.



10 m Solution: hypotenuse = $\sqrt{(\log)^2 + (\text{other leg})^2}$ $=\sqrt{(17)^2+(10)^2}$ The legs are 10 meters 17 m and 17 meters. $=\sqrt{289+100}$ $=\sqrt{389}$ ≈ 20 From Appendix A.6 or a calculator

triangle. Round the length to the nearest whole unit.

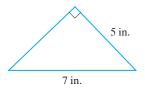
Approximate the length of the hypotenuse of the given right

The hypotenuse is exactly $\sqrt{389}$ meters, which is approximately 20 meters.

Work Practice 7



Find the length of the leg in the given right triangle. Give the exact length and a two-decimal-place approximation.



Solution: Notice that the hypotenuse measures 7 inches and the length of one leg measures 5 inches. Since we are looking for the length of the other leg, we use the formula

 $leg = \sqrt{(hypotenuse)^2 - (other leg)^2}$

Putting the known values into the formula, we have

leg =
$$\sqrt{(7)^2 - (5)^2}$$
 The hypotenuse is 7 inches, and the other leg is 5 inches.
= $\sqrt{49 - 25}$
= $\sqrt{24}$ Exact answer
 ≈ 4.90 From Appendix A.6 or a calculator

The length of the leg is exactly $\sqrt{24}$ inches, which is approximately 4.90 inches.

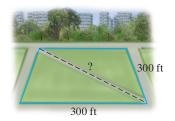
Work Practice 8

Concept Check The following lists are the lengths of the sides of two triangles. Which set forms a right triangle? Explain.

a. 8, 15, 17 **b.** 24, 30, 40

Example 9 Finding the Dimensions of a Park

An inner-city park is in the shape of a square that measures 300 feet on a side. A sidewalk is to be constructed along the diagonal of the park. Find the length of the sidewalk rounded to the nearest whole foot.



Solution: The diagonal is the hypotenuse of a right triangle, so we use the formula

hypotenuse = $\sqrt{(\log)^2 + (\text{other leg})^2}$

Putting the known values into the formula we have

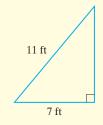
hypotenuse =
$$\sqrt{(300)^2 + (300)^2}$$
 The legs are both 300 feet.
= $\sqrt{90,000 + 90,000}$
= $\sqrt{180,000}$
 ≈ 424 From Appendix A.6 or a calculator

The length of the sidewalk is approximately 424 feet.

Work Practice 9

Practice 8

Find the length of the leg in the given right triangle. Give the exact length and a two-decimal-place approximation.



Practice 9

A football field is a rectangle measuring 100 yards by 53 yards. Draw a diagram and find the length of the diagonal of a football field to the nearest yard.

Answers 8. $\sqrt{72}$ ft ≈ 8.49 ft 9. 113 yd

Concept Check Answer set (a) forms a right triangle

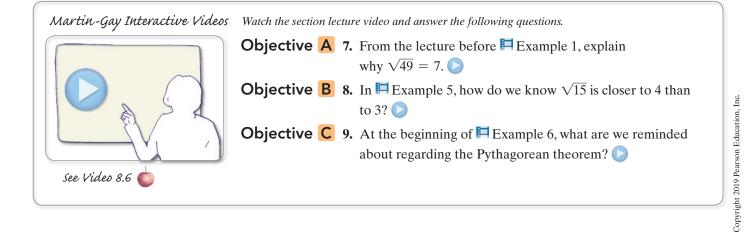
| Calculator Explorations Finding Square | Roots |
|--|--|
| To simplify or approximate square roots using a calculator, locate the key marked $$. | Is this answer reasonable? Since 10 is between perfect squares 9 and 16, $\sqrt{10}$ is between $\sqrt{9} = 3$ and $\sqrt{16} = 4$. |
| To simplify $\sqrt{64}$, for example, press the keys | Our answer is reasonable since 3.162 is between 3 and 4. |
| $\begin{bmatrix} 64 \end{bmatrix} \boxed{} \text{or} \boxed{} \boxed{64}$ | Simplify. |
| The display should read 8. Then | 1. $\sqrt{1024}$ |
| $\sqrt{64} = 8$ | 2. $\sqrt{676}$ |
| To <i>approximate</i> $\sqrt{10}$, press the keys | Approximate each square root. Round each answer to the |
| 10 $$ or $$ 10 | nearest thousandth. |
| The display should read 3.16227766. This is an | 3. $\sqrt{31}$ |
| approximation for $\sqrt{10}$. A three-decimal-place approximation is | 4. $\sqrt{19}$
5. $\sqrt{97}$ |
| $\sqrt{10} \approx 3.162$ | 6. $\sqrt{56}$ |

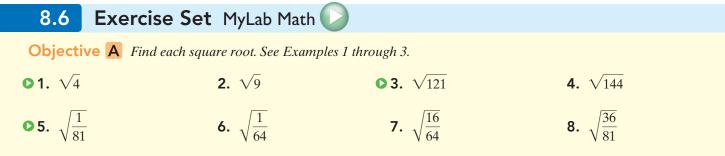
Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Some choices may be used more than once.

| squaring | Pythagorean theorem | radical | leg |
|------------|---------------------|---------|-----|
| hypotenuse | perfect squares | 10 | |

- **1.** $\sqrt{100} =$ ______ because $10 \cdot 10 = 100$.
- 2. The ______ sign is used to denote the square root of a number.
- 3. The reverse process of _______ a number is finding a square root of a number.
- 4. The numbers 9, 1, and ¹/₂₅ are called _____.
 5. Label the parts of the right triangle. ______
- 6. The _____ can be used for right triangles.





Objective B Use Appendix A.6 or a calculator to approximate each square root. Round the square root to the nearest thousandth. See Examples 4 and 5.

| 9. $\sqrt{3}$ | 10. $\sqrt{5}$ | 011. $\sqrt{15}$ | 12. $\sqrt{17}$ |
|------------------------|------------------------|-------------------------|------------------------|
| 13. $\sqrt{47}$ | 14. $\sqrt{85}$ | 15. $\sqrt{26}$ | 16. $\sqrt{35}$ |

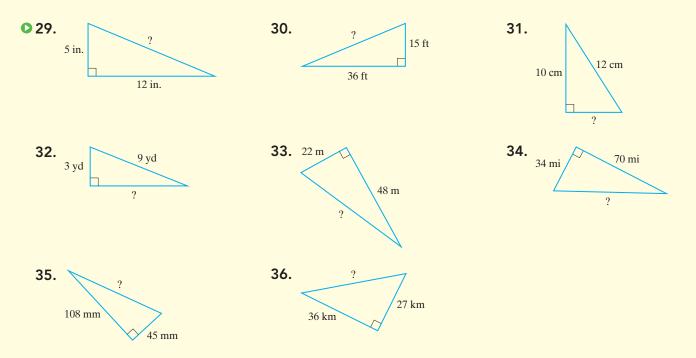
Determine what two whole numbers each square root is between without using a calculator or table. Then use a calculator or Appendix A.6 to check. See Example 5.

0 17. $\sqrt{38}$ 18. $\sqrt{27}$ 19. $\sqrt{101}$ 20. $\sqrt{85}$

Objectives A B Mixed Practice Find each square root. If necessary, round the square root to the nearest thousandth. See Examples 1 through 5.

| 21. $\sqrt{256}$ | 22. $\sqrt{625}$ | 23. $\sqrt{92}$ | 24. $\sqrt{18}$ |
|------------------------------------|-------------------------------------|------------------------|------------------------|
| 25. $\sqrt{\frac{49}{144}}$ | 26. $\sqrt{\frac{121}{169}}$ | 27. $\sqrt{71}$ | 28. $\sqrt{62}$ |

Objective C Find the unknown length in each right triangle. If necessary, approximate the length to the nearest thousandth. See Examples 6 through 8.

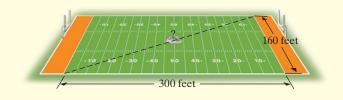


Sketch each right triangle and find the length of the side not given. If necessary, approximate the length to the nearest thousandth. (Each length is in units.) See Examples 6 through 8.

| 37. $leg = 3$, $leg = 4$ | 38. $\log = 9, \log = 12$ | 39. $\log = 5$, hypotenuse = 13 |
|--|------------------------------------|---|
| 40. $leg = 6$, hypotenuse = 10 | 41. $leg = 10$, $leg = 14$ | 42. $\log = 2, \log = 16$ |
| 43. $leg = 35, leg = 28$ | 44. $\log = 30, \log = 15$ | 45. $\log = 30, \log = 30$ |
| 46. $leg = 21, leg = 21$ | • 47. hypotenuse = 2 , leg = 1 | 48. hypotenuse = 9 , leg = 8 |
| 49. $leg = 7.5, leg = 4$ | 50. $leg = 12, leg = 22.5$ | |

Solve. See Example 9.

- **51.** A standard city block is a square with each side measuring 100 yards. Find the length of the diagonal of a city block to the nearest hundredth yard.
- **53.** Find the height of the tree. Round the height to one decimal place.
 - 20 feet
- **55.** The playing field for football is a rectangle that is 300 feet long by 160 feet wide. Find, to the nearest foot, the length of a straight-line run that started at one corner and went diagonally to end at the opposite corner.



Review

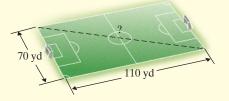
Find the value of n in each proportion. See Section 5.3.

| 57. | $\frac{n}{6} =$ | $\frac{2}{3}$ | 58. | $\frac{8}{n} = \frac{4}{8}$ |
|-----|-----------------|----------------|-----|------------------------------|
| 60. | $\frac{5}{6} =$ | $\frac{35}{n}$ | 61. | $\frac{3}{n} = \frac{7}{14}$ |

- **52.** A section of land is a square with each side measuring 1 mile. Find the length of the diagonal of the section of land to the nearest thousandth mile.
- **54.** Find the height of the antenna. Round the height to one decimal place.



56. A soccer field is in the shape of a rectangle and its dimensions depend on the age of the players. The dimensions of the soccer field below are the minimum dimensions for international play. Find the length of the diagonal of this rectangle. Round the answer to the nearest tenth of a yard.



59. $\frac{9}{11} = \frac{n}{55}$ **62.** $\frac{n}{9} = \frac{4}{6}$

| ~ | | | | - C. | • | |
|----------|----|----|----|--|-------|------|
| | nn | CO | nt | Exte | anci | onc |
| \smile | | | | LAU | 21131 | Ulis |
| | | | | | | |

Use the results of Exercises 17 through 20 and approximate each square root to the nearest whole number without using a calculator or table. Then use a calculator or Appendix A.6 to check. See Example 5.

63. $\sqrt{38}$

64. $\sqrt{27}$

66. $\sqrt{85}$

67. Without using a calculator, explain how you know that $\sqrt{105}$ is *not* approximately 9.875.

68. Without using a calculator, explain how you know that $\sqrt{27}$ is *not* approximately 3.296.

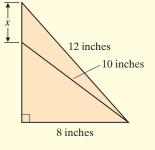
Does the set form the lengths of the sides of a right triangle? See the Concept Check in this section.

69. 25, 60, 65

70. 20, 45, 50

65. $\sqrt{101}$

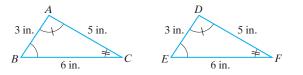
 \triangle **71.** Find the exact length of *x*. Then give a two-decimal-place approximation.



8.7 Congruent and Similar Triangles

Objective A Deciding Whether Two Triangles Are Congruent

Congruent angles are angles that have the same measure. Two triangles are **congruent** when they have the same shape and the same size. In congruent triangles, the measures of corresponding angles are equal and the lengths of corresponding sides are equal. The following triangles are congruent:



Since these triangles are congruent, the measures of corresponding angles are equal.

Angles with equal measure: $\angle A$ and $\angle D$, $\angle B$ and $\angle E$, $\angle C$ and $\angle F$. Also, the lengths of corresponding sides are equal.

Equal corresponding sides: \overline{AB} and \overline{DE} , \overline{BC} and \overline{EF} , \overline{CA} and \overline{FD}

Objectives

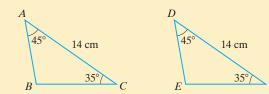
- A Decide Whether Two Triangles Are Congruent.
- B Find the Ratio of Corresponding Sides in Similar Triangles.
- C Find Unknown Lengths of Sides in Similar Triangles.

Any one of the following may be used to determine whether two triangles are congruent:

Congruent Triangles

Angle-Side-Angle (ASA)

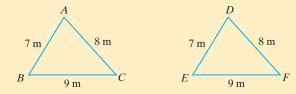
If the measures of two angles of a triangle equal the measures of two angles of another triangle, and the lengths of the sides between each pair of angles are equal, the triangles are congruent.



For example, these two triangles are congruent by Angle-Side-Angle.

Side-Side-Side (SSS)

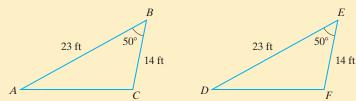
If the lengths of the three sides of a triangle equal the lengths of the corresponding sides of another triangle, the triangles are congruent.



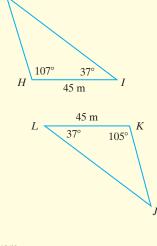
For example, these two triangles are congruent by Side-Side.

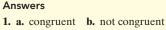
Side-Angle-Side (SAS)

If the lengths of two sides of a triangle equal the lengths of corresponding sides of another triangle, and the measures of the angles between each pair of sides are equal, the triangles are congruent.



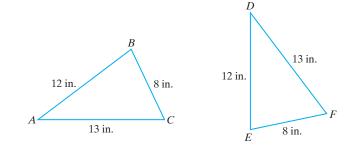
For example, these two triangles are congruent by Side-Angle-Side.





Example 1

Determine whether triangle ABC is congruent to triangle DEF.



Solution: Since the lengths of all three sides of triangle *ABC* equal the lengths of all three sides of triangle *DEF*, the triangles are congruent.

Work Practice 1

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Practice 1

a. Determine whether triangle

8 mi

8 mi

 90°

6 mi

b. Determine whether triangle *GHI* is congruent to triangle

MNO is congruent to

triangle RQS.

M

6 mi

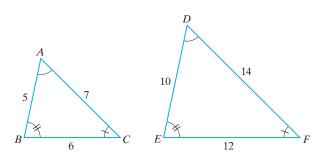
JKL.

G

In Example 1, notice that as soon as we know that the two triangles are congruent, we know that all three corresponding angles are congruent.

Objective **B** Finding the Ratio of Corresponding Sides in Similar Triangles

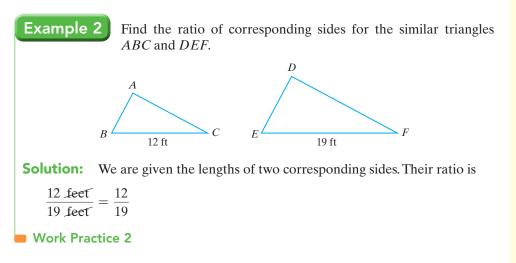
Two triangles are **similar** when they have the same shape but not necessarily the same size. In similar triangles, the measures of corresponding angles are equal and corresponding sides are in proportion. The following triangles are similar:



Since these triangles are similar, the measures of corresponding angles are equal. Angles with equal measure: $\angle A$ and $\angle D$, $\angle B$ and $\angle E$, $\angle C$ and $\angle F$. Also, the lengths of corresponding sides are in proportion.

Sides in proportion: $\frac{AB}{DE} = \frac{BC}{EF} = \frac{CA}{FD}$ or, in this particular case, $\frac{AB}{DE} = \frac{5}{10} = \frac{1}{2}, \frac{BC}{EF} = \frac{6}{12} = \frac{1}{2}, \frac{CA}{FD} = \frac{7}{14} = \frac{1}{2}$

The ratio of corresponding sides is $\frac{1}{2}$.

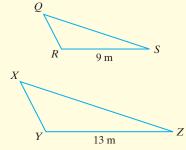


Objective C Finding Unknown Lengths of Sides in Similar Triangles

Because the ratios of lengths of corresponding sides are equal, we can use proportions to find unknown lengths in similar triangles.

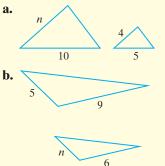
Practice 2

Find the ratio of corresponding sides for the similar triangles *QRS* and *XYZ*.



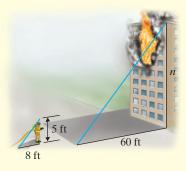
Practice 3

Given that the triangles are similar, find the missing length *n*.



Practice 4

Tammy Shultz, a firefighter, needs to estimate the height of a burning building. She estimates the length of her shadow to be 8 feet long and the length of the building's shadow to be 60 feet long. Find the approximate height of the building if she is 5 feet tall.



Answers **3. a.** n = 8 **b.** $n = \frac{10}{3}$ or $3\frac{1}{3}$

4. approximately 37.5 ft

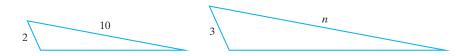
Concept Check Answer

A corresponds to O; B corresponds to N; C corresponds to M

Chapter 8 | Geometry

Example 3

Given that the triangles are similar, find the missing length *n*.



Solution: Since the triangles are similar, corresponding sides are in proportion. Thus, the ratio of 2 to 3 is the same as the ratio of 10 to n, or

$$\frac{2}{3} = \frac{10}{n}$$

0

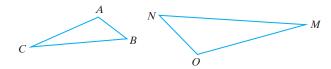
To find the unknown length *n*, we set cross products equal.

 $2 \cdot n = 3 \cdot 10$ Set cross products equal. $2 \cdot n = 30$ Multiply. $n = \frac{30}{2}$ Divide 30 by 2, the number multiplied by *n*. n = 15

The missing length is 15 units.

Work Practice 3

Concept Check The following two triangles are similar. Which vertices of the first triangle appear to correspond to which vertices of the second triangle?

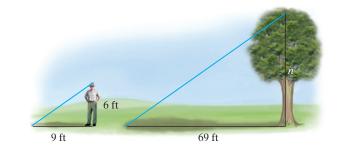


Many applications involve diagrams containing similar triangles. Surveyors, astronomers, and many other professionals continually use similar triangles in their work.

Example 4

Finding the Height of a Tree

Mel Rose is a 6-foot-tall park ranger who needs to know the height of a particular tree. He measures the shadow of the tree to be 69 feet long when his own shadow is 9 feet long. Find the height of the tree.



Solution:

1. UNDERSTAND. Read and reread the problem. Notice that the triangle formed by the Sun's rays, Mel, and his shadow is similar to the triangle formed by the Sun's rays, the tree, and its shadow.

2. TRANSLATE. Write a proportion from the similar triangles formed.

 $\frac{\text{Mel's height}}{\text{height of tree}} \xrightarrow{\rightarrow} \frac{6}{n} = \frac{9}{69} \xleftarrow{} \frac{\text{length of Mel's shadow}}{\text{length of tree's shadow}}$ or $\frac{6}{n} = \frac{3}{23}$ Simplify $\frac{9}{69}$. (ratio in lowest terms) **3.** SOLVE for *n*: $\frac{6}{n} = \frac{3}{23}$ $6 \cdot 23 = n \cdot 3$ Set cross products equal. $138 = n \cdot 3$ Multiply. $\frac{138}{3} = n$ Divide 138 by 3, the number multiplied by *n*. 46 = n**4.** INTERPRET. *Check* to see that replacing *n* with 46 in the proportion makes the proportion true. *State* your conclusion: The height of the tree is 46 feet.

Work Practice 4

Vocabulary, Readiness & Video Check

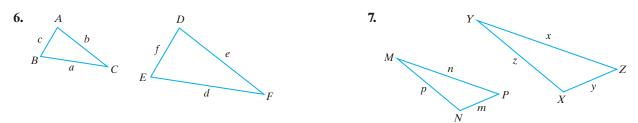
Answer each question true or false.

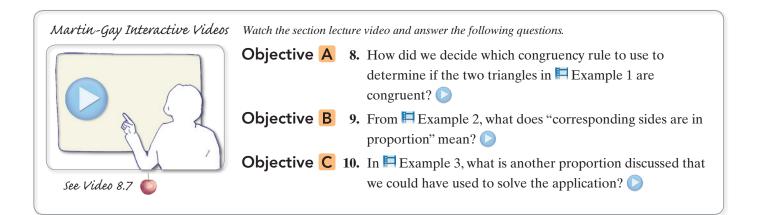
- 1. Two triangles that have the same shape but not necessarily the same size are congruent.
- 2. Two triangles are congruent if they have the same shape and size.
- 3. Congruent triangles are also similar.
- 4. Similar triangles are also congruent.
- 5. For the two similar triangles, the ratio of corresponding sides is $\frac{3}{6}$.

Each pair of triangles is similar. Name the congruent angles and the corresponding sides that are proportional.

15 in.

18 in.



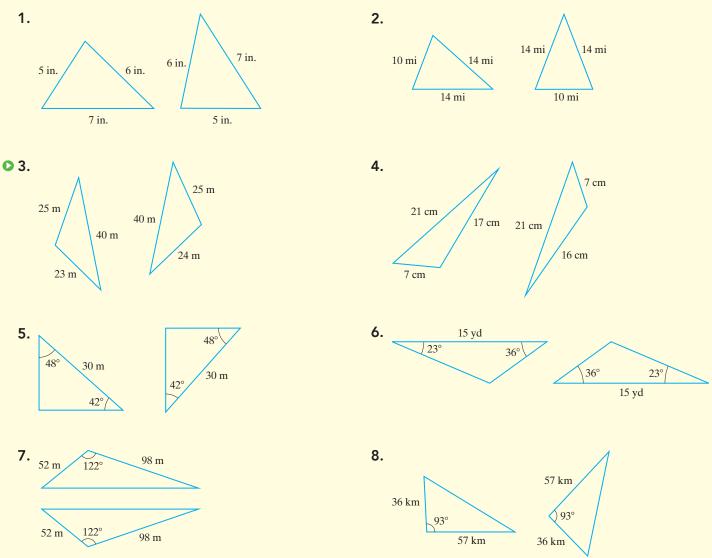


5 in.

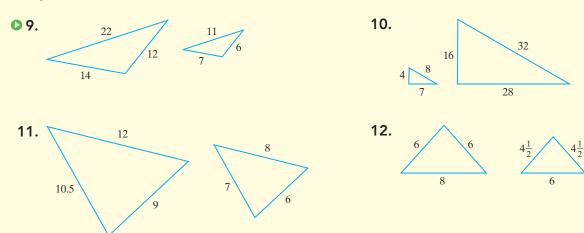
6 in.

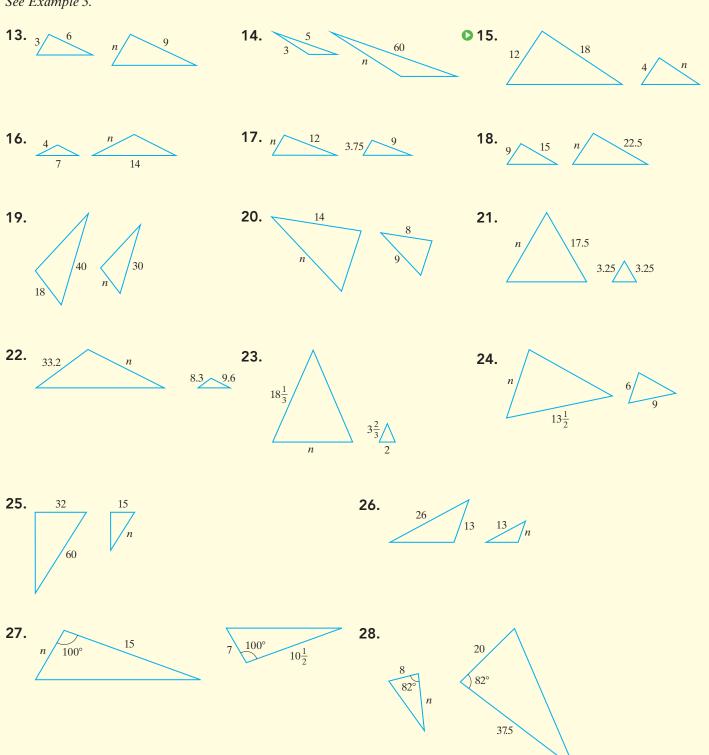
8.7 Exercise Set MyLab Math 🕗

Objective A Determine whether each pair of triangles is congruent. If congruent, state the reason why, such as SSS, SAS, or ASA. See Example 1.



Objective B Find each ratio of the corresponding sides of the given similar triangles. See Example 2.

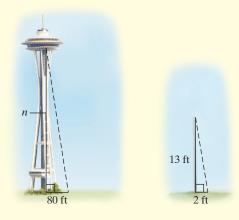




Objective C *Given that the pairs of triangles are similar, find the unknown length of the side labeled n. See Example 3.*

Solve. For Exercises 29 and 30, the solutions have been started for you. See Example 4.

29. Given the following diagram, approximate the height of the observation deck in the Seattle Space Needle in Seattle, Washington. (*Source:* Seattle Space Needle)



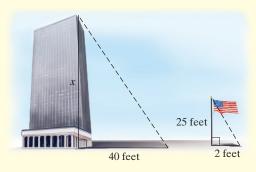
Start the solution:

- 1. UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into a proportion using the similar triangles formed. (Fill in the blanks.)

height of observation deck $\rightarrow \frac{n}{13}$ height of pole $\rightarrow 13$

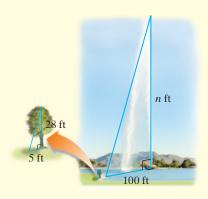
| | | length of Space |
|---|---|-----------------|
| | ← | Needle shadow |
| _ | ← | length of pole |
| | | shadow |

- **3.** SOLVE by setting cross products equal.
- 4. INTERPRET.
- **31.** Given the following diagram, approximate the height of the Chase Tower in Oklahoma City, Oklahoma. Here, we use *x* to represent the unknown number. (*Source:* Council on Tall Buildings and Urban Habitat)



33. Samantha Black, a 5-foot-tall park ranger, needs to know the height of a tree. She notices that when the shadow of the tree is 48 feet long, her shadow is 4 feet long. Find the height of the tree.

30. A fountain in Fountain Hills, Arizona, sits in a 28-acre lake and shoots up a column of water every hour. Based on the diagram below, what is the height of the fountain?

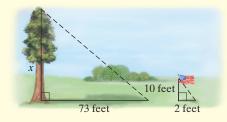


Start the solution:

- **1.** UNDERSTAND the problem. Reread it as many times as needed.
- **2.** TRANSLATE into a proportion using the similar triangles formed. (Fill in the blanks.)

| | | | | length of tree |
|--------------------|---------------|----|-------|--------------------|
| height of tree | \rightarrow | 28 |
← | shadow |
| height of fountain | \rightarrow | n |
← | length of fountain |
| | | | | shadow |

- **3.** SOLVE by setting cross products equal.
- **4.** INTERPRET.
- **32.** The tallest tree standing today is a redwood located in the Humboldt Redwoods State Park near Ukiah, California. Given the following diagram, approximate its height. Here, we use *x* to represent the unknown number. (*Source: Guinness World Records*)



34. Lloyd White, a firefighter, needs to estimate the height of a burning building. He estimates the length of his shadow to be 9 feet long and the length of the building's shadow to be 75 feet long. Find the approximate height of the building if he is 6 feet tall.

● **35.** If a 30-foot tree casts an 18-foot shadow, find the length of the shadow cast by a 24-foot tree.

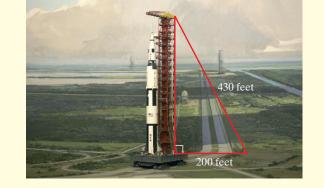
Review

Solve. See Section 5.3.

37. For the health of his fish, the owner of Pete's Sea World uses the standard that a 20-gallon tank should house only 19 neon tetras. Find the number of neon tetras that Pete would place into a 55-gallon tank.

Solve. See Section 8.6.

39. Launch Umbilical Tower 1 is the name of the gantry used for the *Apollo* launch that took Neil Armstrong and Buzz Aldrin to the moon. Find the height of the gantry to the nearest whole foot.



Perform the indicated operation. See Sections 4.3 through 4.5.

41. 3.6 + 0.41

42. 3.6 - 0.41

Concept Extensions

45. The print area on a particular page measures 7 inches by 9 inches. A printing shop is to copy the page and reduce the print area so that its length is 5 inches. What will its width be? Will the print now fit on a 3-by-5-inch index card?

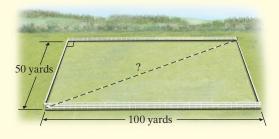
38. A local package express deliveryman is traveling the city expressway at 45 mph when he is forced to slow down due to traffic ahead. His truck slows at the rate of 3 mph every 5 seconds. Find his speed 8 seconds after braking.

36. If a 24-foot flagpole casts a 32-foot shadow, find

Round to the nearest tenth.

the length of the shadow cast by a 44-foot antenna.

40. Arena polo, popular in the United States and England, is played on a field that is 100 yards long and usually 50 yards wide. Find the length, to the nearest yard, of the diagonal of this field.

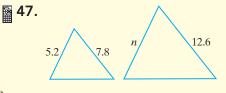


43. (0.41)(3)

44. 0.48 ÷ 3

46. The art sample for a banner measures $\frac{1}{3}$ foot in width by $1\frac{1}{2}$ feet in length. If the completed banner is to have a length of 9 feet, find its width.

Given that the pairs of triangles are similar, find the length of the side labeled n. Round your results to 1 decimal place.



49. In your own words, describe any differences in similar triangles and congruent triangles.



50. Describe a situation where similar triangles would be useful for a contractor building a house.

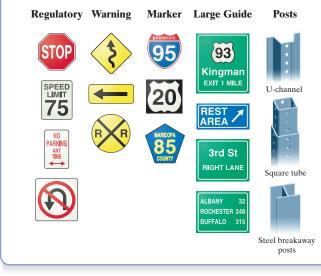
- **51.** A triangular park is planned and waiting to be approved by the city zoning commission. A drawing of the park shows sides of length 5 inches, $7\frac{1}{2}$ inches, and $10\frac{5}{8}$ inches. If the scale on the drawing is $\frac{1}{4}$ in. = 10 ft, find the actual proposed dimensions of the park.
 - Chapter 8 Group Activity

The Cost of Road Signs

Sections 8.1, 8.2, 8.4

There are nearly 4 million miles of streets and roads in the United States. With streets, roads, and highways comes the need for traffic control, guidance, warning, and regulation. Road signs perform many of these tasks. Just in our routine travels, we see a wide variety of road signs every day. Think how many road signs must exist on the 4 million miles of roads in the United States. Have you ever wondered how much signs like these cost?

The cost of a road sign generally depends on the type of sign. Costs for several types of signs and signposts are listed in the table. Examples of various types of signs are shown below.



| 52. | John and Robyn Costello draw a triangular deck on their house plans. Robyn measures sides of the deck | | |
|-----|---|--|--|
| | drawing on the plans to be 3 inches, $4\frac{1}{2}$ inches, and | | |
| | 6 inches. If the scale on the drawing is $\frac{1}{4}$ in. = 1 foot, | | |
| | find the lengths of the sides of the deck they want built. | | |

| Road Sign Costs | | | | | |
|-----------------------------|---------------------------|--|--|--|--|
| Type of Sign | Cost | | | | |
| Regulatory, warning, marker | \$15–\$18 per square foot | | | | |
| Large guide | \$20-\$25 per square foot | | | | |
| Type of Post | Cost | | | | |
| U-channel | \$125–\$200 each | | | | |
| Square tube | \$10–\$15 per foot | | | | |
| Steel breakaway posts | \$15-\$25 per foot | | | | |

The cost of a sign is based on its area. For diamond, square, or rectangular signs, the area is found by multiplying the length (in feet) times the width (in feet). Then the area is multiplied by the cost per square foot. For signs with irregular shapes, costs are generally figured *as if* the sign were a rectangle, multiplying the height and width at the tallest and widest parts of the sign.

Group Activity

Locate four different kinds of road signs on or near your campus. Measure the dimensions of each sign, including the height of the post on which it is mounted. Using the cost data given in the table, find the minimum and maximum costs of each sign, including its post. Summarize your results in a table, and include a sketch of each sign.

Chapter 8 Vocabulary Check

length. We name a line by any two of its points.

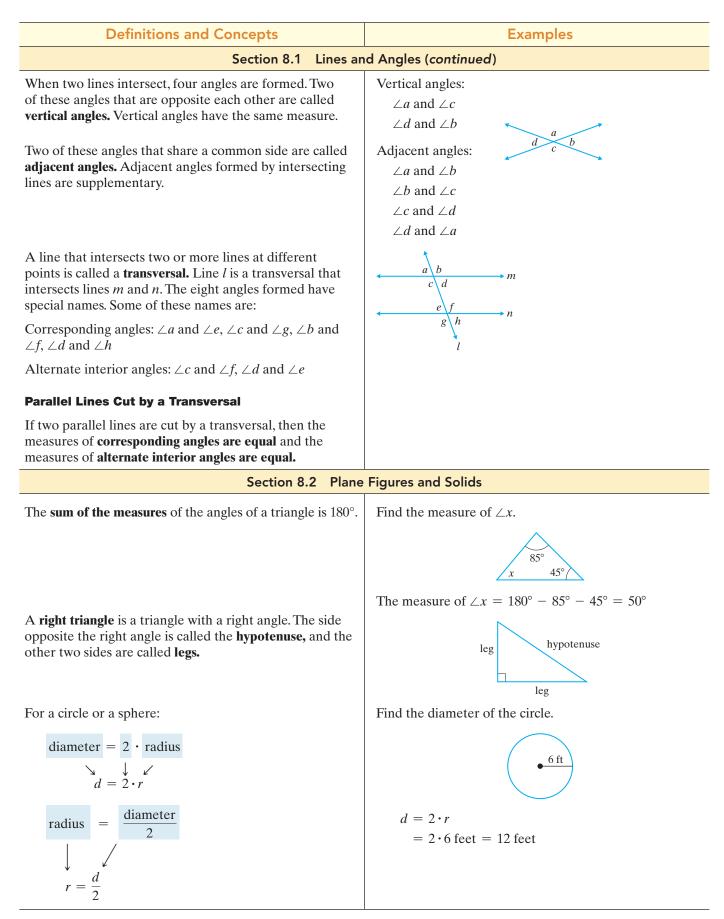
| | transversal | line | congruent | hypotenuse | legs | acute | |
|---|---|---|-----------------------------------|--------------------|-------------------|--------------------|--|
| | right | line segment | complementary | square root | vertical | supplementary | |
| | right triangle | volume | obtuse | vertex | ray | angle | |
| | similar | perimeter | area | straight | adjacent | | |
| 1. | A(n) is a triangle with a right angle. The side opposite the right angle is called the, and the other two sides are called | | | | | | |
| 2. | A(n) | is a piece of a | a line with two endpo | ints. | | | |
| 3. | Two angles that h | have a sum of 90° a | re called | angles. | | | |
| 4. | A(n) | is a set of poi | nts extending indefin | itely in two direc | tions. | | |
| 5. | The | of a polygon is | s the distance around | the polygon. | | | |
| 6. | | - | f two rays that share | the same endpoir | it. The common | endpoint is called | |
| - | the | | | | | | |
| | triangles have the same shape and the same size. measures the amount of surface of a region. | | | | | | |
| | | | | | · | | |
| | | | line with one endpoin | | indefinitely in c | one direction. | |
| | · · · | | a is a number b whos | • | | | |
| | | | ines at different point
l a(n) | . , | • | | |
| | e | | | 6 | | | |
| | | | is called its | | agita agah atha | are called | |
| 14. | | | es are formed. The an | gies that are opp | Usite each other | are called | |
| 15. | | | Exercise 14 share a co | mmon side, they | are called | angles. | |
| | | - | n 90° and 180° is calle | - | | C | |
| | - | | d a(n) | | C | | |
| | | | n 0° and 90° is called | | angle. | | |
| | - | | are called | | C | | |
| 20. | t | triangles have exac | ctly the same shape b | ut not necessarily | the same size. | | |
| Helpful
Hint Are you preparing for your test? To help, don't forget to take these: Chapter 8 Getting Ready for the Test on page 582 Chapter 8 Test on page 583 Then check all of your answers at the back of this text. For further review, the step-by-step video solutions to any of these exercises are located in MyLab Math. | | | | | | | |
| 8 Chapter Highlights | | | | | | | |
| | Defin | itions and Conc | epts | | Examp | les | |
| | | | Section 8.1 Li | nes and Angles | | | |
| dii | rections. A line has | nts extending inde
s no width or heigh | nt, but it does have | Line AB or 4 | A A | B | |

Line AB or \overrightarrow{AB}

Fill in each blank with one of the words or phrases listed below.

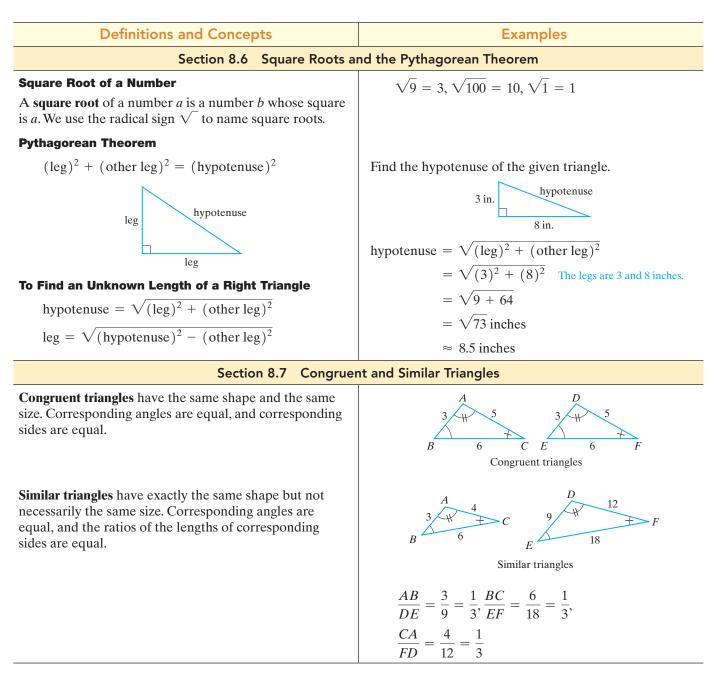
(continued)

| Definitions and Concepts | Examples | | | | |
|--|--|--|--|--|--|
| Section 8.1 Lines and Angles (continued) | | | | | |
| A line segment is a piece of a line with two endpoints. | Line segment AB or \overline{AB} A B | | | | |
| A ray is a part of a line with one endpoint. A ray extends indefinitely in one direction. | Ray AB or \overrightarrow{AB} \overrightarrow{A} \overrightarrow{B} | | | | |
| An angle is made up of two rays that share the same endpoint. The common endpoint is called the vertex . | Angle ABC , $\angle ABC$, $\angle CBA$, or $\angle B$
Vertex C | | | | |
| An angle that measures 180° is called a straight angle. | $\angle RST$ is a straight angle. | | | | |
| An angle that measures 90° is called a right angle. The symbol $``$ is used to denote a right angle. | $\angle ABC$ is a right angle. | | | | |
| An angle whose measure is between 0° and 90° is called an acute angle. | 45°
Acute angles | | | | |
| An angle whose measure is between 90° and 180° is called
an obtuse angle. | Obtuse angles | | | | |
| Two angles that have a sum of 90° are called complementary angles. We say that each angle is the complement of the other. | $R \xrightarrow{60^{\circ}}_{S} \xrightarrow{30^{\circ}}_{Complementary angles}} 60^{\circ} + 30^{\circ} = 90^{\circ}$ | | | | |
| Two angles that have a sum of 180° are called supplementary angles. We say that each angle is the supplement of the other. | $ \begin{array}{c} 125^{\circ} \\ M \\ \text{Supplementary angles} \\ 125^{\circ} + 55^{\circ} = 180^{\circ} \end{array} $ | | | | |



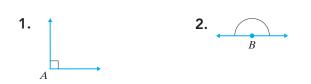
| Definitions and Concepts | Examples | | |
|--|--|--|--|
| Section 8.3 | Perimeter | | |
| Perimeter Formulas
Rectangle: $P = 2 \cdot l + 2 \cdot w$ | Find the perimeter of a rectangle with length 28 meters and width 15 meters. | | |
| Square: $P = 4 \cdot s$ | $P = 2 \cdot l + 2 \cdot w$ | | |
| Triangle: $P = a + b + c$ | $= 2 \cdot 28 \text{ m} + 2 \cdot 15 \text{ m}$ | | |
| Circumference of a Circle: $C = 2 \cdot \pi \cdot r$ or $C = \pi \cdot d$, | = 56 m + 30 m
= 86 m | | |
| | | | |
| where $\pi \approx 3.14$ or $\pi \approx \frac{22}{7}$ | The perimeter is 86 meters. | | |
| Section 8 | .4 Area | | |
| Area Formulas | Find the area of a square with side length 8 centimeters. | | |
| Rectangle: $A = l \cdot w$ | $A = s^2$ | | |
| Square: $A = s^2$ | $= (8 \text{ cm})^2$ | | |
| Triangle: $A = \frac{1}{2} \cdot b \cdot h$ | = 64 square centimeters | | |
| Triangle: $A = \frac{1}{2} \cdot b \cdot h$ | The area of the square is 64 square centimeters. | | |
| Parallelogram: $A = b \cdot h$ | | | |
| Trapezoid: $A = \frac{1}{2} \cdot (b + B) \cdot h$ | | | |
| Circle: $A = \pi \cdot r^2$ | | | |
| Section 8. | 5 Volume | | |
| Volume Formulas
Rectangular Solid: $V = l \cdot w \cdot h$ | Find the volume of the sphere. Use $\frac{22}{7}$ for π . | | |
| Cube: $V = s^3$ | | | |
| Sphere: $V = \frac{4}{3} \cdot \pi \cdot r^3$ | <u>4 in:</u> | | |
| Right Circular Cylinder: $V = \pi \cdot r^2 \cdot h$ | | | |
| Cone: $V = \frac{1}{3} \cdot \pi \cdot r^2 \cdot h$ | $V = \frac{4}{3} \cdot \pi \cdot r^3$ | | |
| Square-Based Pyramid: $V = \frac{1}{3} \cdot s^2 \cdot h$ | $\approx \frac{4}{3} \cdot \frac{22}{7} \cdot (4 \text{ inches})^3$ | | |
| - | $=\frac{4\cdot 22\cdot 64}{3\cdot 7}$ cubic inches | | |
| | $=\frac{5632}{21}$ or $268\frac{4}{21}$ cubic inches | | |

575



Chapter 8 Review

(8.1) Classify each angle as acute, right, obtuse, or straight.



5. Find the complement of a 25° angle.

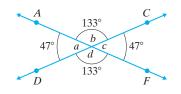


6. Find the supplement of a 105° angle.

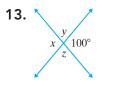
Find the measure of angle x in each figure.



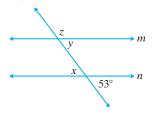
11. Identify the pairs of supplementary angles.



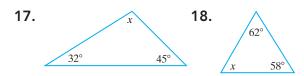
Find the measures of angles x, y, and z in each figure.



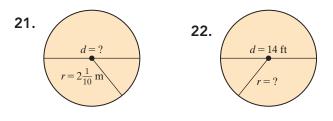
15. Given that $m \parallel n$.

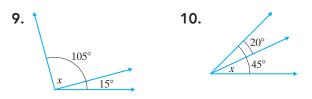


(8.2) Find the measure of $\angle x$ in each figure.

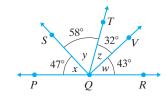


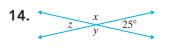
Find the unknown diameter or radius as indicated.



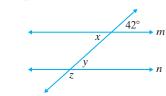


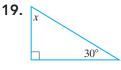
12. Identify the pairs of complementary angles.

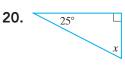


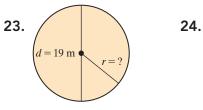


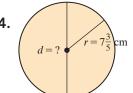
16. Given that $m \parallel n$.









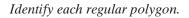


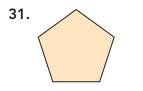
Identify each solid.



Find the unknown radius or diameter as indicated.

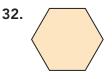
29. The radius of a sphere is 9 inches. Find its diameter.







30. The diameter of a sphere is 4.7 meters. Find its radius.

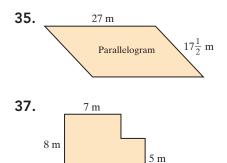


34.

Identify each triangle as equilateral, isosceles, or scalene. Also identify any triangle that is a right triangle.



(8.3) Find the perimeter of each figure.

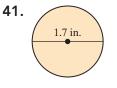


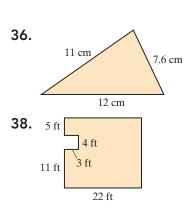
10 m

Solve.

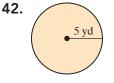
39. Find the perimeter of a rectangular sign that measures 6 feet by 10 feet.

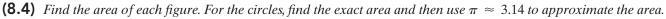
Find the circumference of each circle. Use $\pi \approx 3.14$.

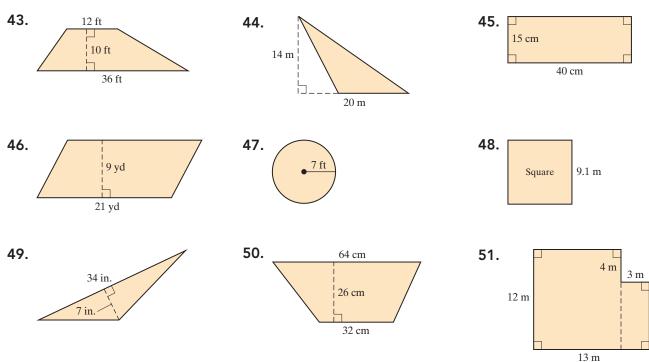




40. Find the perimeter of a town square that measures 110 feet on a side.



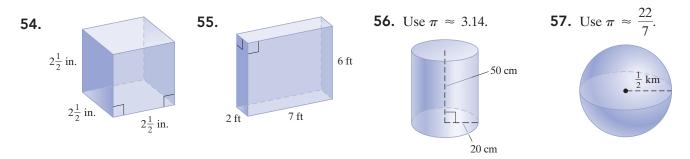




- **52.** The amount of sealant necessary to seal a driveway depends on the area. Find the area of a rectangular driveway 36 feet by 12 feet.
- **53.** Find how much carpet is necessary to cover the floor of the room shown.



(8.5) Find the volume of each solid. For Exercises 56 and 57, give the exact volume and an approximation.



- **58.** Find the volume of a pyramid with a square base 2 feet on a side and a height of 2 feet.
- **59.** Approximate the volume of a tin can 8 inches high and 3.5 inches in radius. Use 3.14 for π .

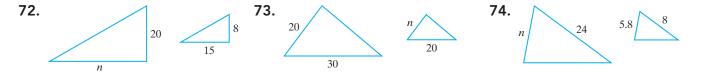
Chapter 8 Review

- **61.** A cylindrical canister for a shop vacuum is 2 feet tall and 1 foot in *diameter*. Find its exact volume.
- **60.** A chest has 3 drawers. If each drawer has inside measurements of $2\frac{1}{2}$ feet by $1\frac{1}{2}$ feet by $\frac{2}{3}$ foot, find the total volume of the 3 drawers.
- (8.6) *Simplify*.
- **62.** $\sqrt{64}$ **63.** $\sqrt{144}$

Find the unknown length of each given right triangle. If necessary, round to the nearest tenth.

- **66.** $\log = 12, \log = 5$
- **68.** leg = 9, hypotenuse = 14
- **70.** A baseball diamond is in the shape of a square and has sides of length 90 feet. Find the distance across the diamond from third base to first base, to the nearest tenth of a foot.

(8.7) Given that the pairs of triangles are similar, find the unknown length n.



Solve.

75. A housepainter needs to estimate the height of a condominium. He estimates the length of his shadow to be 7 feet long and the length of the building's shadow to be 42 feet long. Find the approximate height of the building if the housepainter is

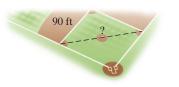
 $5\frac{1}{2}$ feet tall.

76. A toy company is making a triangular sail for a toy sailboat. The toy sail is to be the same shape as a real sailboat's sail. Use the following diagram to find the unknown lengths *x* and *y*.



- **64.** $\sqrt{\frac{4}{25}}$ **65.** $\sqrt{\frac{1}{100}}$
- **67.** $\log = 20$, $\log = 21$
- **69.** leg = 124, hypotenuse = 155
- **71.** Find the height of the building rounded to the nearest tenth of a foot.





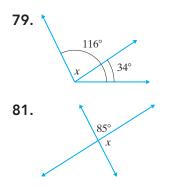
Mixed Review

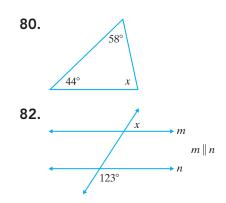
Find the following.

77. Find the supplement of a 72° angle.

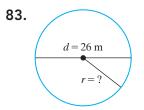
78. Find the complement of a 1° angle.

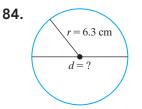
Find the measure of angle x in each figure.



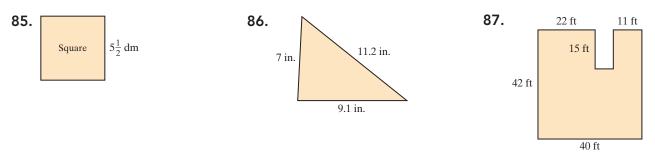


Find the unknown diameter or radius as indicated.





Find the perimeter of each figure.

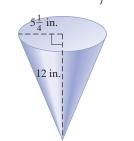


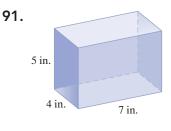
Find the area of each figure. For the circle, find the exact area and then use $\pi \approx 3.14$ to approximate the area.



Find the volume of each solid.

90. Give an approximation using $\frac{22}{7}$ for π .





Solve.

- **92.** Find the volume of air in a rectangular room 15 feet by 12 feet with a 7-foot ceiling.
- **93.** A mover has two boxes left for packing. Both are cubical, one 3 feet on a side and the other 1.2 feet on a side. Find their combined volume.

Simplify.

94. $\sqrt{1}$ **95.** $\sqrt{36}$ **96.** $\sqrt{\frac{16}{81}}$

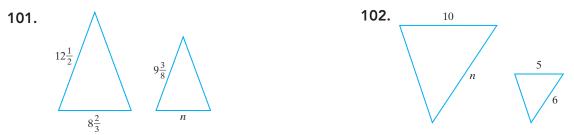
Find the unknown length of each given right triangle. If necessary, round to the nearest tenth.

97. $\log = 66$, $\log = 56$ **98.** $\log = 12$, hypotenuse = 24

99. leg = 17, hypotenuse = 51

100. leg = 10, leg = 17

Given that the pairs of triangles are similar, find the unknown length n.



Getting Ready for the Test

MATCHING Match each word in the first column with its illustration in the columns to the right.

- **1**. line
- **2.** line segment

Chapter 8

- **3.** ray
- **4.** right angle
- **5.** acute angle
- **6.** obtuse angle

MULTIPLE CHOICE Exercises 7–22 are Multiple Choice. Choose the correct letter for each exercise.

Use the given figure for Exercises 7 and 8.

- \circ 7. Choose two angles that have a sum of 180°.
- **A.** $\angle a$ and $\angle c$ **B.** $\angle a$ and $\angle d$ **C.** $\angle b$ and $\angle d$ **O. 8.** Choose two angles that have the same measure.
 - **A.** $\angle a$ and $\angle b$ **B.** $\angle c$ and $\angle d$ **C.** $\angle b$ and $\angle d$

Use the given figure for Exercises 9 and 10. For this figure, m||*n.*

- \bigcirc 9. Choose two angles that have a sum of 180°.
 - **A.** $\angle a$ and $\angle e$ **B.** $\angle a$ and $\angle d$ **C.** $\angle a$ and $\angle b$
- ▶ 10. Choose two angles that have the same measure. A. $\angle a$ and $\angle e$ B. $\angle a$ and $\angle c$ C. $\angle a$ and $\angle f$

For Exercises 11 through 16, the choices are below. Exercises 13 and 15 have two correct choices.

A. perimeter B. area C. volume D. circumference

- 11. Which calculation is measured in square units?
- 12. Which calculation is measured in cubic units?
- 13. Which calculation is measured in units?

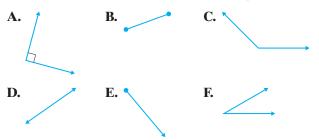
For Exercises 14 through 16 name the calculation (choices A., B., C., or D. above) to be used to solve each exercise.

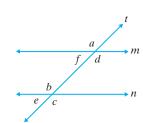
- 14. The amount of material needed for a rectangular tablecloth.
- 15. The amount of trim needed to go around the edge of a tablecloth.
- 16. The amount of soil needed to fill in a hole in the ground.
- 17. Which square root is between the numbers 8 and 10? A. $\sqrt{36}$ B. $\sqrt{25}$ C. $\sqrt{49}$ D. $\sqrt{81}$
- ▶ 18. Which square root is between the numbers 6 and 7? A. $\sqrt{10}$ B. $\sqrt{13}$ C. $\sqrt{50}$ D. $\sqrt{40}$

TRUE OR FALSE Answer Exercises 19 through 22

A. True or **B.** False

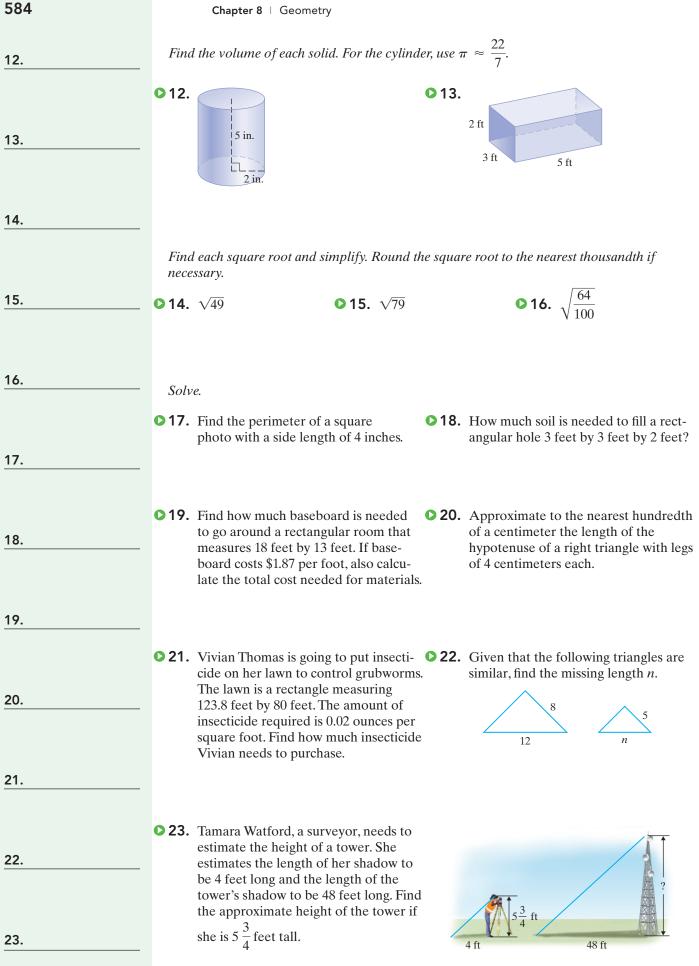
- **19.** The Pythagorean theorem applies to right triangles only.
- \bigcirc 20. A right triangle can have two 90° angles.
- 21. A right triangle has 3 sides; 1 side is called a leg and the other 2 sides are each called a hypotenuse.
- **22.** The hypotenuse of a right triangle is the longest side.







| For additional practice go to your study plan in MyLab Math. | ab Math or You Tube | Test | Chapter 8 |
|--|--|------------------------------------|------------|
| \bigcirc 1. Find the complement of a 78° angle. | • 2. Find the supplement of a | a 124° angle. | Answers |
| ● 3. Find the measure of $\angle x$. | | | 1. |
| Find the measures of x , y , and z in each figur | e. | | |
| $\begin{array}{c} 24. \\ y \\ z \\ z \\ \end{array}$ | • 5. Given: $m \parallel n$. | | |
| | x
y
z | $\rightarrow m$
$\rightarrow n$ | |
| Find the unknown diameter or radius as indi | icated. | | 4. |
| 6. $d = ?$ $r = 3.1 \text{ m}$ | 07. $\frac{1}{\sqrt{r}=?}$ $\frac{1}{d=20\frac{1}{2}\text{ in.}}$ | | 5. |
| | | | 6. |
| • 8. Find the measure of ∠x.
92°
62° x | | | 7. |
| Find the perimeter (or circumference) and an value and then use $\pi \approx 3.14$ for an approximation of the sector $\pi \approx 3.14$ for an approximation of the sector $\pi \approx 3.14$ for an approximation of the sector $\pi \approx 3.14$ for an approximation of the sector $\pi \approx 3.14$ for an approximation of the sector $\pi \approx 3.14$ for an approximation of the sector $\pi \approx 3.14$ for an approximation of the sector $\pi \approx 3.14$ for an approximation of the sector $\pi \approx 3.14$ for an approximation of the sector $\pi \approx 3.14$ for an approximation of the sector $\pi \approx 3.14$ for a sector $\pi \approx 3.14$ | | ve the exact | |
| ♥ 9. | P10. Rectangle 5.3 yd | | 9 |
| | 7 yd | | |
| ● 11. 6 in.
11 in. | | | 10. |
| 7 in. | | | <u>11.</u> |
| 23 in. | | | 583 |



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| | Cumulative Review | Chapters 1–8 |
|---|---|--------------------------|
| 1. Write the decimal 19.5023 in words. | 2. Add: $\frac{7}{11} + \frac{1}{6}$ | Answers |
| 3. Round 736.2359 to the nearest tenth. | 4. Round 736.2359 to the nearest hundred. | <u>1.</u>
<u>2.</u> |
| 5. Add: 45 + 2.06 | 6. Divide: $3\frac{1}{3} \div 1\frac{5}{6}$ | <u>3.</u>
<u>4.</u> |
| Multiply. | | <u>5.</u>
6. |
| 7. 7.68 × 10 | 8. $\frac{7}{11} \cdot \frac{1}{6}$ |
 |
| 9. 76.3 × 1000 | 10. $5\frac{1}{2} \cdot 2\frac{1}{11}$ | <u>8.</u>
9. |
| 11. Divide: 270.2 ÷ 7. Check your answer. | 12. Divide: $\frac{56.7}{100}$ | <u>10.</u>
11. |
| 13. Simplify: 0.5(8.6 - 1.2) | 14. Simplify: $\frac{5+2(8-3)}{30 \div 6 \cdot 5}$ | <u>12.</u>
13. |
| 15. Insert <, >, or = to form a true statement. $\frac{1}{8}$ 0.12 | 16. Insert <, >, or = to form a true statement. $\frac{3}{4}$ $\frac{13}{16}$ | 14. |
| 0 | . 10 | <u>15.</u>
<u>16.</u> |
| 17. Write the ratio of 2.6 to 3.1 as a fraction in simplest form. | 18. Find: $\frac{2}{9} + \frac{7}{15} - \frac{1}{3}$ | <u>17.</u>
<u>18.</u> |
| 19. Is $\frac{2}{3} = \frac{4}{6}$ a true proportion? | 20. Solve for <i>n</i> : $\frac{7}{8} = \frac{n}{20}$ | <u>19.</u>
20. |
| 21. Since 2011, white has been the world's most popular color for cars. For 2017 model-year cars, 25 out of every 100 were painted white. What percent of model-year 2017 cars were white? | 22. In a survey of 50 people, 34 people pre-
fer taking pictures with digital cameras.
What percent is this? | 21.
22. |

Chapter 8 | Geometry

Write each percent as a fraction or mixed number in simplest form.

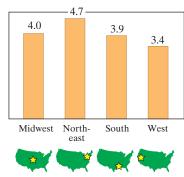
| 23. | 23. 1.9% 24. 26% | 25 | 125% 26. 560% |
|-----|---|-----|---|
| 24. | | | |
| | 27. 85% of 300 is what number? | 28. | What percent of 16 is 2.4? |
| 25. | 29. 20.8 is 40% of what number? | 30. | Find: $(7 - \sqrt{16})^2$ |
| 26. | 31. Mr. Buccaran, the principal at Slidell | 32. | Flooring tiles cost \$90 for a box with |
| 27. | High School, counted 31 freshmen
absent during a particular day. If this
is 4% of the total number of freshmen, | | 40 tiles. Each tile is 1 square foot. Find
the unit price in dollars per square
foot. |
| 28 | how many freshmen are there at Slidell
High School? | | 1001. |
| 29. | | 24 | A student con complete 7 eveniese |
| 30. | 33. Sherry Souter, a real estate broker for
Wealth Investments, sold a house for
\$214,000 last week. If her commis- | 54. | A student can complete 7 exercises
in 6 minutes. At this rate, how many
exercises can be completed in |
| 31. | sion rate is 1.5% of the selling price | | 30 minutes? |
| 32. | of the home, find the amount of her commission. | | |
| 33 | 35. Convert 8 feet to inches. | 36. | 100 inches = $\yd \ft \in.$ |
| 34 | 37. Convert 3.2 kilograms to grams. | 38. | Convert 70 mm to meters. |
| 35. | 39. Subtract 3 quarts from 4 gallons 2 quarts. | 40. | Write seventy thousand, fifty-two in standard form. |
| 36. | _ 1 | | |
| 37. | 41. Convert 29°C to degrees Fahrenheit. | 42. | Write $\frac{1}{8}$ as a percent. |
| 38 | 43. Find the measure of $\angle a$. | 44. | Find the perimeter of the triangle in Exercise 43 . |
| 39. | <i>a</i> 14.1 m | | Exercise 43. |
| 40. | 8.1 m | | |
| 41. | 93 35°
10.8 m | | |
| 42. | 45. Find the perimeter of the rectangle | 46. | Find the area of the rectangle in |
| 43. | below. | | Exercise 45 . |
| 44. | 5 in. | | |
| 45. | 9 in. | | |
| 46. | 47. Find $\sqrt{\frac{4}{25}}$. | 48. | Find $\sqrt{\frac{9}{16}}$. |
| 47. | V 25 | 50 | V 10 |
| 48. | 49. Find the ratio of corresponding sides for triangles <i>ABC</i> and <i>DEF</i> . | 50. | Use the figures in Exercise 49 and find the value of <i>x</i> . |
| 49. | | | |
| 50. | 10 ft | | |
| | $B \xrightarrow{12 \text{ ft}} C = E \xrightarrow{19 \text{ ft}} F$ | | |

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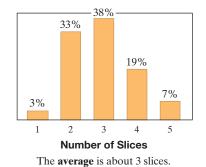
Reading Graphs and Introduction to Statistics and Probability

How Many Times per Month Do You Usually Eat Pizza?



The average is 4 times a month.

How Many Slices Do You Usually Eat When Eating Pizza?



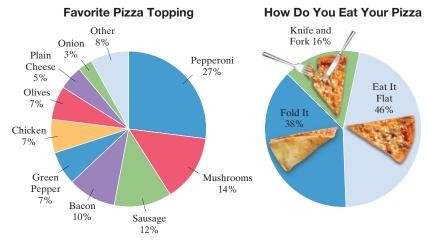
All About Pizza!

he word *pizza* was first documented in AD 997 in Italy, and it literally means "pie." Foods similar to pizza can be traced back to ancient Greece, Persia, and other countries, although modern-day pizza is believed to have been invented in Naples, Italy. Pizza was mainly eaten in Italy until immigrants brought the idea of pizza to the United States.

Surveys show that pizza is ranked number 1 among comfort foods. In this chapter, we study all types of graphs as well as measures of central tendency, such as average. For example,

- the average price of a slice of pizza is \$3.26, and
- the average cost of a pie (or whole pizza) is \$16.73.
- Depending on the survey, New York City is usually ranked first as the city with the best pizza, followed by Chicago.

Throughout this chapter, we study all types of graphs as well as average, shown on the graphs above and below.



9

We often need to make decisions based on known statistics or the probability of an event occurring. For example, we decide whether or not to bring an umbrella to work based on the probability of rain. We choose an investment based on its mean, or average, return. We can predict which football team will win based on the trend in its previous wins and losses. This chapter reviews presenting data in a usable form on a graph and the basic ideas of statistics and probability.

Sections

- 9.1 Pictographs, Bar Graphs, Histograms, and Line Graphs
- 9.2 Circle Graphs

Integrated Review— Reading Graphs

- 9.3 Mean, Median, Mode, and Range
- 9.4 Counting and Introduction to Probability

Check Your Progress

Vocabulary Check Chapter Highlights Chapter Review Getting Ready for the Test Chapter Test Cumulative Review

9.1 Pictographs, Bar Graphs, Histograms, and Line Graphs

Objectives

- 🗛 Read Pictographs. 🜔
- B Read and Construct Bar Graphs.
- C Read and Construct Histograms (or Frequency Distribution Graphs).

D Read Line Graphs. 🜔

Practice 1

Use the pictograph shown in Example 1 to answer the following questions:

- **a.** Approximate the number of people who primarily speak Spanish.
- **b.** Approximate how many more people primarily speak Spanish than Arabic.

Often data are presented visually in a graph. In this section, we practice reading several kinds of graphs including pictographs, bar graphs, and line graphs.

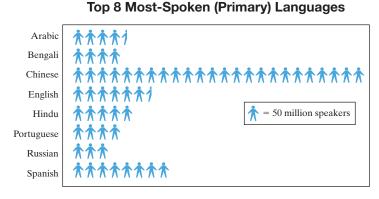
Objective 🗛 Reading Pictographs 💽

A **pictograph** such as the one below is a graph in which pictures or symbols are used. This type of graph contains a key that explains the meaning of the symbol used. An advantage of using a pictograph to display information is that comparisons can easily be made. A disadvantage of using a pictograph is that it is often hard to tell what fractional part of a symbol is shown. For example, in the pictograph below, Arabic shows a part of a symbol, but it's hard to read with any accuracy what fractional part of a symbol is shown.

Example 1

Calculating Languages Spoken

The following pictograph shows the top eight most-spoken (primary) languages. Use this pictograph to answer the questions.



Source: www.ethnologue.com

- a. Approximate the number of people who primarily speak Russian.
- **b.** Approximate how many more people primarily speak English than Russian.

Solution:

- **a.** Russian corresponds to 3 symbols, and each symbol represents 50 million speakers. This means that the number of people who primarily speak Russian is approximately 3 · (50 million) or 150 million people.
- **b.** English shows $3\frac{1}{2}$ more symbols than Russian. This means that $3\frac{1}{2} \cdot (50 \text{ million})$ or 175 million more people primarily speak English than Russian.

Work Practice 1

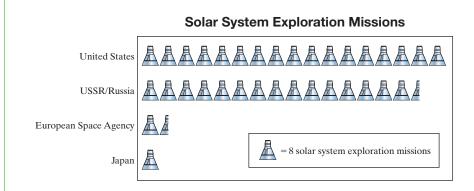
Answers

a. 400 million people
 b. 175 million people

Example 2

Calculating Solar System Exploration

The following pictograph shows the approximate number of solar system exploration missions by various countries or space consortia from 1957 to the present day. Use this pictograph to answer the questions.



- a. Approximate the number of solar system exploration missions undertaken by the United States.
- **b.** Approximate how many more solar system exploration missions have been undertaken by the United States than by the USSR/Russia.

Solution:

- **a.** The United States corresponds to 17 symbols, and each symbol represents 8 solar system exploration missions. This means that the United States has undertaken approximately $17 \cdot 8 = 136$ missions for solar system exploration.
- **b.** The USSR/Russia shows $15\frac{1}{2}$ symbols, or $1\frac{1}{2}$ fewer than the United States. This

means that the United States has undertaken $1\frac{1}{2} \cdot 8 = 12$ more solar system exploration missions than the USSR/Russia.

Work Practice 2

Objective **B** Reading and Constructing Bar Graphs ()

Another way to visually present data is with a **bar graph.** Bar graphs can appear with vertical bars or horizontal bars. Although we have studied bar graphs in previous sections, we now practice reading the height or length of the bars contained in a bar graph. An advantage to using bar graphs is that a scale is usually included for greater accuracy. Care must be taken when reading bar graphs, as well as other types of graphs—they may be misleading, as shown later in this section.

Practice 2

Use the pictograph shown in Example 2 to answer the following questions:

- **a.** Approximate the number of solar system exploration missions undertaken by the European Space Agency.
- **b.** Approximate the total number of solar system exploration missions undertaken by the European Space Agency and Japan.

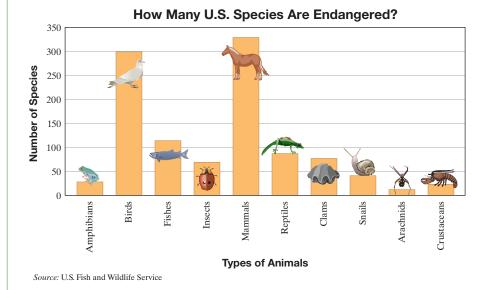
Practice 3

Use the bar graph in Example 3 to answer the following questions:

- **a.** Approximate the number of endangered species that are fishes.
- **b.** Which category shows the fewest endangered species?

Example 3 Finding the Number of Endangered Species

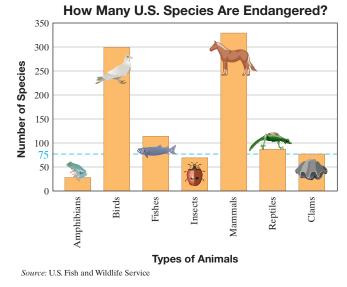
The following bar graph shows the number of endangered species in the United States in 2016. Use this graph to answer the questions.

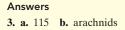


- a. Approximate the number of endangered species that are clams.
- **b.** Which category has the most endangered species?

Solution:

- **a.** To approximate the number of endangered species that are clams, we go to the top of the bar that represents clams. From the top of this bar, we move horizon-tally to the left until the scale is reached. We read the height of the bar on the scale as approximately 75. There are approximately 75 clam species that are endangered, as shown. (See the graph below.)
- **b.** The most endangered species is represented by the tallest (longest) bar. The tallest bar corresponds to mammals.





Work Practice 3

Next, we practice constructing a bar graph.

Example 4

Draw a vertical bar graph using the information in the table below, which gives the caffeine content of selected foods.

| Average Caffeine Content of Selected Foods | | | |
|---|------------|---------------------------------------|------------|
| Food | Milligrams | Food | Milligrams |
| Brewed coffee
(percolator, 8 ounces) | 124 | Instant coffee
(8 ounces) | 104 |
| Brewed decaffeinated coffee (8 ounces) | 3 | Brewed tea (U.S.
brands, 8 ounces) | 64 |
| Coca-Cola Classic
(8 ounces) | 31 | Mr. Pibb (8 ounces) | 27 |
| Dark chocolate
(semisweet, $1\frac{1}{2}$ ounces)30Milk chocolate
(8 ounces)9 | | | |
| (Sources: International Food Information Council and the Coca-Cola Company) | | | |

Practice 4

60

50

40

30

20

10

Texas

Florida

State

Kansas Indiana

California

Georgia

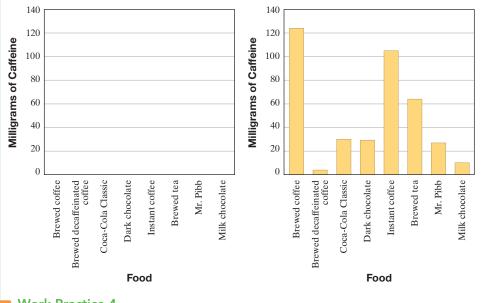
Electoral Votes for President

Draw a vertical bar graph using the information in the table about electoral votes for selected states.

| Total Electoral Votes
by Selected States | | |
|---|----|--|
| State Electoral Votes | | |
| Texas | 38 | |
| California | 55 | |
| Florida 29 | | |
| Kansas 6 | | |
| Indiana | 20 | |
| Georgia 15 | | |
| (Source: World Almanac) | | |

Solution: We draw and label a vertical line and a horizontal line as shown below on the left. These lines are also called axes. We place the different food categories along the horizontal axis. Along the vertical axis, we place a scale.

There are many choices of scales that would be appropriate. Notice that the milligrams range from a low of 3 to a high of 124. From this information, we use a scale that starts at 0 and then shows multiples of 20 so that the scale is not too cluttered. The scale stops at 140, the smallest multiple of 20 that will allow all milligrams to be graphed. It may also be helpful to draw horizontal lines along the scale markings to help draw the vertical bars at the correct height. The finished bar graph is shown below on the right.



Answer 4 60 Electoral Votes for President 50 40 30 20

Florida

State

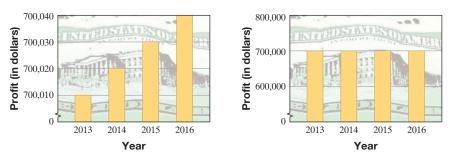
10

Texas Californi

Work Practice 4

As mentioned previously, graphs can be misleading. Both graphs on the next page show the same information but with different scales. Special care should be taken when forming conclusions from the appearance of a graph.

Notice the 4 symbol on each vertical scale on the graphs below. This symbol alerts us that numbers are missing from that scale



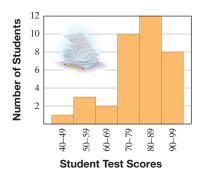
Are profits shown in the graphs above greatly increasing, or are they remaining about the same?

Objective C Reading and Constructing Histograms ()

Suppose that the test scores of 36 students are summarized in the table below. We call this table a **frequency distribution table** since one column gives the frequency or number of times the event in the other column occurred.

| Student Scores | Frequency
(Number of Students) |
|----------------|-----------------------------------|
| 40–49 | 1 |
| 50–59 | 3 |
| 60–69 | 2 |
| 70–79 | 10 |
| 80–89 | 12 |
| 90–99 | 8 |

The results in this frequency distribution table can be displayed in a histogram. A **histogram** is a special bar graph. The width of each bar represents a range of numbers called a **class interval**. The height of each bar corresponds to how many times a number in the class interval occurs and is called the **class frequency**. The bars in a histogram lie side by side with no space between them. Note: Another name for this histogram is a **frequency distribution graph**.



Example 5

Use the preceding histogram to determine how many students scored 50–59 on the test.

Reading a Histogram on Student Test Scores

Solution: We find the bar representing 50–59. The height of this bar is 3, which means 3 students scored 50–59 on the test.

Work Practice 5

Practice 5

Use the histogram above Example 4 to determine how many students scored 80–89 on the test.

Answer

5. 12

Example 6 Reading a Histogram on Student Test Scores

Use the histogram above Example 4 to determine how many students scored 80 or above on the test.

Solution: We see that two different bars fit this description. There are 12 students who scored 80–89 and 8 students who scored 90–99. The sum of these two categories is 12 + 8 or 20 students. Thus, 20 students scored 80 or above on the test.

Work Practice 6

Now we will look at a way to construct histograms.

The daily high temperatures for 1 month in New Orleans, Louisiana, are recorded in the following list:

| 85° | 90° | 95° | 89° | 88° | 94° |
|-----|-----|-----|-----|-----|-----|
| 87° | 90° | 95° | 92° | 95° | 94° |
| 82° | 92° | 96° | 91° | 94° | 92° |
| 89° | 89° | 90° | 93° | 95° | 91° |
| 88° | 90° | 88° | 86° | 93° | 89° |

The data in this list have not been organized and can be hard to interpret. One way to organize the data is to place them in a **frequency distribution table.** We will do this in Example 7.

Example 7

Completing a Frequency Distribution on Temperature

Complete the frequency distribution table for the preceding temperature data.

Solution: Go through the data and place a tally mark in the second column of the table next to the class interval. Then count the tally marks and write each total in the third column of the table.

| Class Intervals
(Temperatures) | Tally | Class Frequency
(Number of Days) |
|-----------------------------------|-------|-------------------------------------|
| 82°-84° | | 1 |
| 85°-87° | | 3 |
| 88°–90° | 11111 | 11 |
| 91°–93° | 1 | 7 |
| 94°–96° | 1 | 8 |

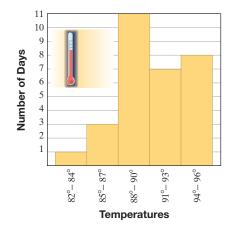
Work Practice 7

Example 8

Construct a histogram from the frequency distribution table in Example 7.

Constructing a Histogram





Practice 6

Use the histogram above Example 4 to determine how many students scored less than 80 on the test.

Practice 7

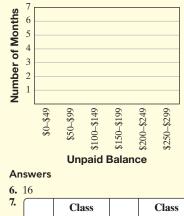
Complete the frequency distribution table for the data below. Each number represents a credit card owner's unpaid balance for one month.

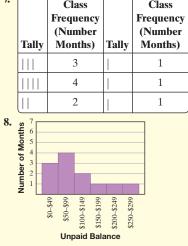
| 0 | 53 | 89 | 125 |
|-----|-----|-----|-----|
| 265 | 161 | 37 | 76 |
| 62 | 201 | 136 | 42 |

| Class
Intervals
(Credit Card
Balances) | Tally | Class
Frequency
(Number of
Months) |
|---|-------|---|
| \$0-\$49 | | |
| \$50-\$99 | | |
| \$100-\$149 | | |
| \$150-\$199 | | |
| \$200-\$249 | | |
| \$250-\$299 | | |

Practice 8

Construct a histogram from the frequency distribution table for Practice 7.





Concept Check Which of the following sets of data is better suited to representation by a histogram? Explain.

| Set 1 | | Set 2 | |
|-------------------|------------------|-------------------|------------------------|
| Grade on
Final | # of
Students | Section
Number | Avg. Grade
on Final |
| 51-60 | 12 | 150 | 78 |
| 61–70 | 18 | 151 | 83 |
| 71-80 | 29 | 152 | 87 |
| 81–90 | 23 | 153 | 73 |
| 91–100 | 25 | | |

Objective D Reading Line Graphs 💽

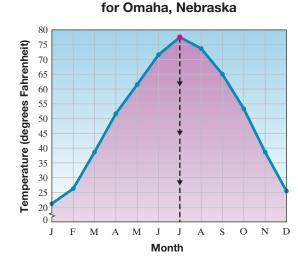
Another common way to display information with a graph is by using a **line graph**. An advantage of a line graph is that it can be used to visualize relationships between two quantities. A line graph can also be very useful in showing changes over time.

Example 9

Reading Temperatures from a Line Graph

The following line graph shows the average daily temperature for each month in Omaha, Nebraska. Use this graph to answer the questions below.

Average Daily Temperature





- a. During what month is the average daily temperature the highest?
- **b.** During what month, from July through December, is the average daily temperature 65°F?
- c. During what months is the average daily temperature less than 30°F?

Solution:

a. The month with the highest temperature corresponds to the highest point. This is the red point shown on the graph above. We follow this highest point downward to the horizontal month scale and see that this point corresponds to July.

Practice 9

Use the temperature graph in Example 8 to answer the following questions:

- **a.** During what month is the average daily temperature the lowest?
- **b.** During what month is the average daily temperature 25°F?
- **c.** During what months is the average daily temperature greater than 70°F?

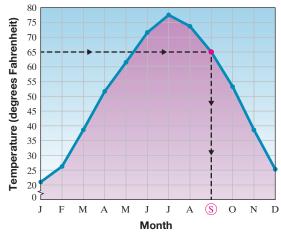
Answers

9. a. January **b.** December **c.** June, July, and August

Concept Check Answer

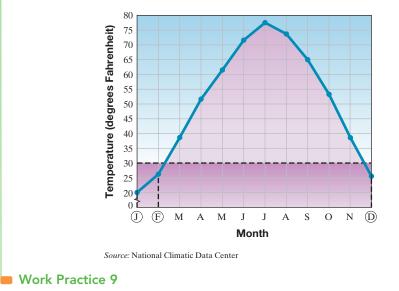
Set 1; the grades are arranged in ranges of scores.

b. The months July through December correspond to the right side of the graph. We find the 65°F mark on the vertical temperature scale and move to the right until a point on the right side of the graph is reached. From that point, we move downward to the horizontal month scale and read the corresponding month. During the month of September, the average daily temperature is 65°F.



Source: National Climatic Data Center

c. To see what months the temperature is less than 30°F, we find what months correspond to points that fall below the 30°F mark on the vertical scale. These months are January, February, and December.



Vocabulary, Readiness & Video Check

Fill in each blank with one of the choices below.

| pictograph | bar | class frequency |
|------------|------|-----------------|
| histogram | line | class interval |

- **1.** A(n) ______ graph presents data using vertical or horizontal bars.
- 2. A(n) ______ is a graph in which pictures or symbols are used to visually present data.
- 3. A(n) ______ graph displays information with a line that connects data points.
- 4. A(n) ______ is a special bar graph in which the width of each bar represents a(n) ______ and

the height of each bar represents the _____

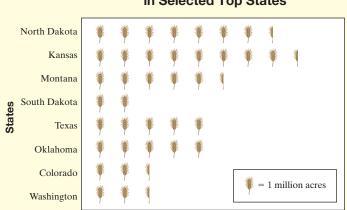
| Martin-Gay Interactive Videos | Watch the section lecture video and answer the following questions. | |
|-------------------------------|---|---|
| | Objective A 5. | From the pictograph in 🖪 Example 1, how would you |
| | Objective B 6. | approximate the number of wildfires for any given year?
From Example 5, what is one advantage of displaying data |
| A S K | Objective C 7. | in a bar graph?
Complete this statement based on the lecture before |
| See Video 9.1 | Objective D 8. | Example 6: A histogram is a special kind of
From the line graph in Examples 10–13, what year aver- |
| | | aged the greatest number of goals per game average and what was this average? |

9.1 Exercise Set MyLab Math

Objective A The following pictograph shows the number of acres devoted to wheat production in 2016 in selected states. Use this graph to answer Exercises 1 through 8. See Examples 1 and 2. (Source: U.S. Department of Agriculture)

- **1.** Which state plants the greatest acreage in wheat?
- **2.** Which of the states shown plant the least amount of wheat acreage?
- **3.** Approximate the number of acres of wheat planted in Montana.
- **4.** Approximate the number of acres of wheat planted in Kansas.
- **5.** Which state(s) plant less than 3,000,000 acres of wheat?
- **6.** Which state(s) plant more than 7,000,000 acres of wheat?
- **7.** Which state plants more wheat: Montana or Oklahoma?



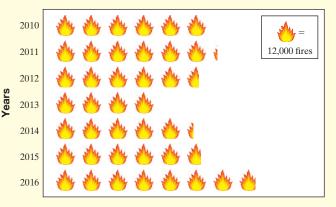


8. Which states plant about the same amount of acreage?

The following pictograph shows the average number of wildfires in the United States between 2010 and 2016. Use this graph to answer Exercises 9 through 16. See Examples 1 and 2. (Source: National Interagency Fire Center)

- 9. Approximate the number of wildfires in 2013.
- **10.** Approximately how many wildfires were there in 2012?
- 11. Which year, of the years shown, had the most wildfires?
 - **12.** In what years were the number of wildfires greater than 72,000?

Wildfires in the United States

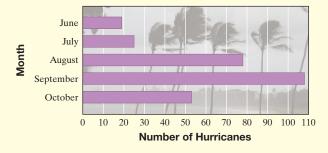


- **13.** What was the amount of decrease in wildfires from 2012 to 2013?
- 15. What was the average annual number of wildfires from 2013 to 2015? (*Hint:* How do you calculate the average?)
- **14.** What was the amount of increase in wildfires from 2015 to 2016?
- **16.** Give a possible explanation for the sharp increase in the number of wildfires in 2016.

Objective B The National Weather Service has exacting definitions for hurricanes; they are tropical storms with winds in excess of 74 mph. The following bar graph shows the number of hurricanes, by month, that have made landfall on the mainland United States between 1851 and 2016. Use this graph to answer Exercises 17 through 22. See Example 3. (Source: National Weather Service: National Hurricane Center)

- **17.** In which month did the most hurricanes make landfall in the United States?
- **18.** In which month did the fewest hurricanes make landfall in the United States?
- **19.** Approximate the number of hurricanes that made landfall in the United States during the month of August.
- **20.** Approximate the number of hurricanes that made landfall in the United States in September.
- **21.** In 2008 alone, two hurricanes made landfall during the month of August. What fraction of all the 78 hurricanes that made landfall during August is this?

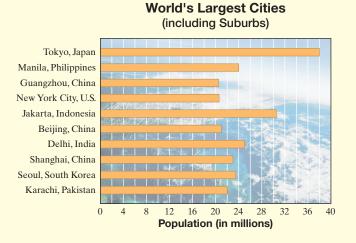
Hurricanes Making Landfall in the United States, by Month, 1851–2016



22. In 2007, only one hurricane made landfall on the United States during the entire season, in the month of September. If there have been 108 hurricanes to make landfall in the month of September since 1851, approximately what percent of these arrived in 2007?

The following horizontal bar graph shows the approximate 2016 population of the world's largest cities (including their suburbs). Use this graph to answer Exercises 23 through 28. See Example 3. (Source: CityPopulation)

- **23.** Name the city with the largest population, and estimate its population.
- **24.** Name the city whose population is between 23 million and 24 million.
- **25.** Name the city in the United States with the largest population, and estimate its population.
- **26.** Name the two cities that have approximately the same population.
- **27.** How much larger (in terms of population) is Manila, Philippines, than Beijing, China?



28. How much larger (in terms of population) is Jakarta, Indonesia, than Seoul, South Korea?

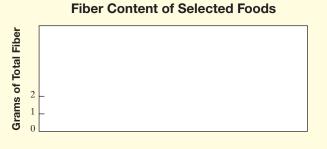
Use the information given to draw a vertical bar graph. Clearly label the bars. See Example 4.

| Fiber Content of Selected Foods | | |
|---|----------------------|--|
| Food | Grams of Total Fiber | |
| Kidney beans $\left(\frac{1}{2}c\right)$ | 4.5 | |
| Oatmeal, cooked $\left(\frac{3}{4}c\right)$ | 3.0 | |
| Peanut butter, chunky (2 tbsp) | 1.5 | |
| Popcorn (1 c) | 1.0 | |
| Potato, baked with skin (1 med) | 4.0 | |
| Whole wheat bread (1 slice) | 2.5 | |

| 30. | U.S. Annual Food Sales | | | |
|-----|------------------------|------------------------------|--|--|
| | Year | Sales in Billions of Dollars | | |
| | 2013 | 1410 | | |
| | 2014 | 1462 | | |
| | 2015 | 1512 | | |
| | 2016 | 1584 | | |
| | - | | | |

(Source: U.S. Department of Agriculture)

| 1. Best | Best-Selling Albums of All Time (U.S. Sales) | | |
|-------------|--|----------------------------------|--|
| Album | | Estimated Sales
(in millions) | |
| Pink Floyd | l: The Wall (1979) | 23 | |
| Michael Ja | ckson: Thriller (1982) | 29 | |
| Billy Joel: | Greatest Hits Volumes I&II (1985) | 23 | |
| Eagles: Th | eir Greatest Hits (1976) | 29 | |
| Led Zeppe | elin: Led Zeppelin IV (1971) | 23 | |
| (Source: Re | cording Industry Association of America |) | |



Food



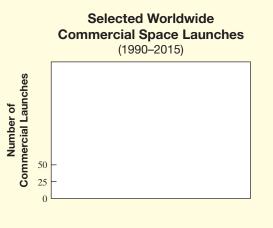
Year





Album

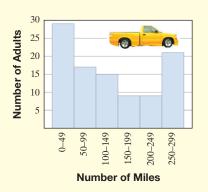
| 32. | Selected Worldwide Commercial Space Launches | | | |
|-----|--|--|--|--|
| | Location or Name | Total Commercial Space Launches
1990–2015 | | |
| | United States | 181 | | |
| | Europe | 169 | | |
| | Russia | 162 | | |
| | China | 23 | | |
| | Sea Launch [*] | 41 | | |
| | *Sea Launch is an international venture involving four countries that uses
its own launch facility outside national borders.
(<i>Source:</i> Bureau of Transportation Statistics) | | | |



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Objective C The following histogram shows the number of miles that each adult, from a survey of 100 adults, drives per week. Use this histogram to answer Exercises 33 through 42. See Examples 5 and 6.

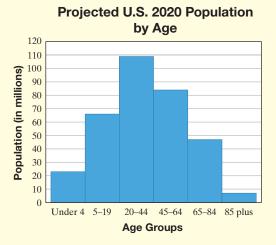
- **33.** How many adults drive 100–149 miles per week?
- **34.** How many adults drive 200–249 miles per week?
- **35.** How many adults drive fewer than 150 miles per week?
 - **36.** How many adults drive 200 miles or more per week?
 - **37.** How many adults drive 100–199 miles per week?
- **39.** How many more adults drive 250–299 miles per week than 200–249 miles per week?
 - **41.** What is the ratio of adults who drive 150–199 miles per week to the total number of adults surveyed?



- **38.** How many adults drive 150–249 miles per week?
- **40.** How many more adults drive 0–49 miles per week than 50–99 miles per week?
- **42.** What is the ratio of adults who drive 50–99 miles per week to the total number of adults surveyed?

The following histogram shows the projected population (in millions), by age groups, for the United States for the year 2020. Use this histogram to answer Exercises 43 through 50. For Exercises 45 through 48, estimate to the nearest whole million. See Examples 5 and 6.

- **43.** What age range will be the largest population group in 2020?
- **44.** What age range will be the smallest population group in 2020?
- **45.** How large is the population of 20- to 44-year-olds expected to be in 2020?
- **46.** How large is the population of 45- to 64-year-olds expected to be in 2020?
- **47.** How large is the population of those less than 4 years old expected to be in 2020?
- **49.** Which bar represents the age range you expect to be in during 2020?



- **48.** How large is the population of 5- to 19-year-olds expected to be in 2020?
- **50.** How many more 20- to 44-year-olds are there expected to be than 45- to 64-year-olds in 2020?

| e rigni. See I | Example 7. | | | | | | | |
|----------------|------------|----|----|-----|--------------|-----------------|-------|-------------------|
| 78 | 84 | 91 | 93 | 97 | | Class Intervals | | Class Frequency |
| 97 | 95 | 85 | 95 | 96 | | (Scores) | Tally | (Number of Games) |
| 101 | 89 | 92 | 89 | 100 | 0 51. | 70–79 | | |
| | | | | | ● 52. | 80–89 | | |
| | | | | | 0 53. | 90–99 | | |
| | | | | | ● 54. | 100–109 | | |

The following list shows the golf scores for an amateur golfer. Use this list to complete the frequency distribution table to the right. See Example 7.

Twenty-five people in a survey were asked to give their current checking account balances. Use the balances shown in the following list to complete the frequency distribution table to the right. See Example 7.

| \$53 | \$105 | \$162 | \$443 | \$109 |
|-------|-------|-------|-------|-------|
| \$468 | \$47 | \$259 | \$316 | \$228 |
| \$207 | \$357 | \$15 | \$301 | \$75 |
| \$86 | \$77 | \$512 | \$219 | \$100 |
| \$192 | \$288 | \$352 | \$166 | \$292 |
| | | | | |

| | Class Intervals
(Account Balances) | Tally | Class Frequency
(Number of People) |
|-------------|---------------------------------------|-------|---------------------------------------|
| 55. | \$0-\$99 | | |
| 56 . | \$100-\$199 | | |
| 57. | \$200-\$299 | | |
| 58. | \$300-\$399 | | |
| 59. | \$400–\$499 | | |
| 60. | \$500–\$599 | | |

61. Use the frequency distribution table from Exercises 51 through 54 to construct a histogram. See Example 8.



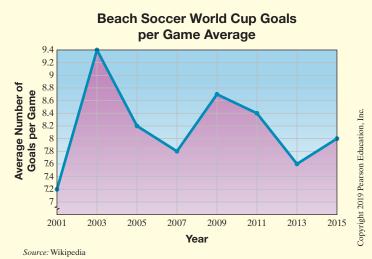
62. Use the frequency distribution table from Exercises **55** through **60** to construct a histogram. See Example 8.



Account Balances

Objective D Beach Soccer World Cup is now held every two years. The following line graph shows the World Cup goals per game average for beach soccer during the years shown. Use this graph to answer Exercises 63 through 70. See Example 9.

- **63.** Find the average number of goals per game in 2015.
 - **64.** Find the average number of goals per game in 2013.
- **65.** During what year shown was the average number of goals per game the highest?
 - **66.** During what year shown was the average number of goals per game the lowest?



- 67. From 2013 to 2015, did the average number of goals per game increase or decrease?
- 69. During what year(s) shown were the average goals per game less than 8?

Review

Find each percent. See Section 6.3 or 6.4.

71. 30% of 12 **72.** 45% of 120

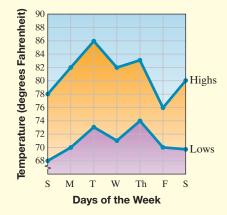
Write each fraction as a percent. See Section 6.2.

| 75. $\frac{1}{4}$ | 76. $\frac{2}{5}$ | 77. $\frac{17}{50}$ | 78. $\frac{9}{10}$ |
|--------------------------|--------------------------|----------------------------|---------------------------|
| | | | |

Concept Extensions

The following double line graph shows temperature highs and lows for a week. Use this graph to answer Exercises 79 through 84.

- **79.** What was the high temperature reading on Thursday?
- **80.** What was the low temperature reading on Thursday?
- **81.** What day was the temperature the lowest? What was this low temperature?
- **82.** What day of the week was the temperature the highest? What was this high temperature?
- **83.** On what day of the week was the difference between the high temperature and the low temperature the greatest? What was this difference in temperature?
- **85.** True or false? With a bar graph, the width of the bar is just as important as the height of the bar. Explain your answer.



68. From 2011 to 2013, did the average number of goals

70. During what year(s) shown were the average goals

74. 95% of 50

per game increase or decrease?

per game greater than 8?

73. 10% of 62

- **84.** On what day of the week was the difference between the high temperature and the low temperature the least? What was this difference in temperature?
- **86.** Kansas plants about 17% of the wheat acreage in the United States. About how many acres of wheat are planted in the United States, according to the pictograph for Exercises **1** through **8**? Round to the nearest million acres.

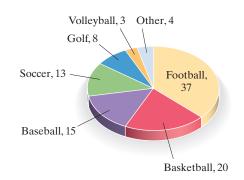
9.2 Circle Graphs 🔘

Objectives

| Α | Read Circle Graphs. > |
|---|-----------------------|
| В | Draw Circle Graphs. > |

Objective A Reading Circle Graphs 🔘

In Exercise Set 6.1, the following **circle graph** was shown. This particular graph shows the favorite sport for 100 adults.



Each sector of the graph (shaped like a piece of pie) shows a category and the relative size of the category. In other words, the most popular sport is football, and it is represented by the largest sector.



Find the ratio of adults preferring basketball to total adults. Write the ratio as a fraction in simplest form.

Solution: The ratio is

$$\frac{\text{people preferring basketball}}{\text{total adults}} = \frac{20}{100} = \frac{1}{5}$$

Work Practice 1

A circle graph is often used to show percents in different categories, with the whole circle representing 100%.

Example 2

Using a Circle Graph

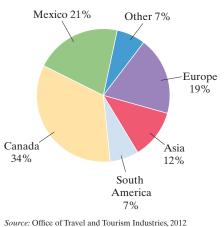
The following graph shows the percent of visitors to the United States in a recent year by various regions. Using the circle graph shown, determine the percent of visitors who came to the United States from Mexico or Canada.

Solution: To find this percent, we add the percents corresponding to Mexico and Canada. The percent of visitors to the United States that came from Mexico or Canada is

34% + 21% = 55%

Work Practice 2





Practice 1

Find the ratio of adults preferring golf to total adults. Write the ratio as a fraction in simplest form.

Practice 2

Using the circle graph shown in Example 2, determine the percent of visitors to the United States that came from Europe, Asia, or South America.

Answers



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Helpful Hint

Since a circle graph represents a whole, the percents should add to 100% or 1. Notice this is true for Example 2.

Example 3 Finding Percent of Population

The U.S. Department of Commerce forecasts 81 million international visitors to the United States in 2017. Use the circle graph from Example 2 and predict the number of tourists that might be from Europe.

Solution: We use the percent equation.

amount = percent \cdot base amount = 0.19 · 81,000,000 = 0.19(81,000,000)= 15,390,000

Thus, 15,390,000 tourists might come from Europe in 2017.

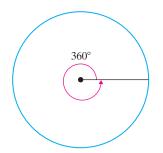
Work Practice 3

Concept Check Can the following data be represented by a circle graph? Why or why not?

| Responses to the Question "In Which Activities Are You Involved?" | | | |
|---|-----|--|--|
| Intramural sports | 60% | | |
| On-campus job | 42% | | |
| Fraternity/sorority | 27% | | |
| Academic clubs | 21% | | |
| Music programs | 14% | | |

Objective **B** Drawing Circle Graphs 🕗

To draw a circle graph, we use the fact that a whole circle contains 360° (degrees).



Practice 3

Use the information in Example 3 and the circle graph from Example 2 to predict the number of tourists from Mexico in 2017.

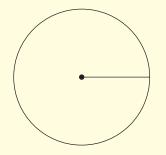
Answer 3. 17,010,000 tourists from Mexico

Concept Check Answer no; the percents add up to more than 100%

Practice 4

Use the data shown to draw a circle graph.

| | 0 1 | |
|----|-----------|-----|
| Fr | reshmen | 30% |
| So | ophomores | 27% |
| Ju | niors | 25% |
| Se | eniors | 18% |
| | | |





Drawing a Circle Graph for U.S. Armed Forces Personnel

The following table shows the percent of U.S. armed forces personnel that were in each branch of service in 2016. (*Source:* U.S. Department of Defense)

| Branch of Service | Percent | |
|--|---------|--|
| Army | 37 | |
| Navy | 25 | |
| Marine Corps | 14 | |
| Air Force | 24 | |
| (Note: The Coast Guard is now under the
Department of Homeland Security.) | | |

Draw a circle graph showing this data.

Solution: First we find the number of degrees in each sector representing each branch of service. Remember that the whole circle contains 360°. (We will round degrees to the nearest whole degree.)

| Sector | Degrees in Each Sector |
|--------------|---|
| Army | $37\% \times 360^\circ = 0.37 \times 360^\circ = 133.2^\circ \approx 133^\circ$ |
| Navy | $25\% \times 360^\circ = 0.25 \times 360^\circ = 90^\circ$ |
| Marine Corps | $14\% \times 360^\circ = 0.14 \times 360^\circ = 50.4^\circ \approx 50^\circ$ |
| Air Force | $24\% \times 360^\circ = 0.24 \times 360^\circ = 86.4^\circ \approx 86^\circ$ |

Helpful Hint

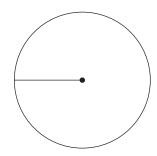
Check your calculations by finding the sum of the degrees.

 $133^{\circ} + 90^{\circ} + 50^{\circ} + 86^{\circ} = 359^{\circ}$

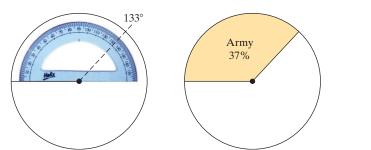
The sum should be 360°. (Our sum varies slightly because of rounding.)

Next we draw a circle and mark its center. Then we draw a line from the center of the circle to the circle itself.

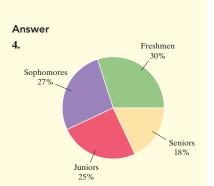
To construct the sectors, we will use a **protractor**. A protractor measures the number of degrees in an angle. We place the hole in the protractor over the center of the circle. Then we adjust the protractor so that 0° on the protractor is aligned with the line that we drew.



It makes no difference which sector we draw first. To construct the "Army" sector, we find 133° on the protractor and mark our circle. Then we remove the protractor and use this mark to draw a second line from the center to the circle itself.



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To construct the "Navy" sector, we follow the same procedure as above, except that we line up 0° with the second line we drew and mark the protractor at 90° . Army Army 37% 37% Navy We continue in this manner until the circle graph is complete. Army 37% Navy 25% Air Force 24% Marine Corps 14% Work Practice 4 **Concept Check** True or false? The larger a sector in a circle graph, the larger

the percent of the total it represents. Explain your answer.

Concept Check Answer true

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank.

100 sector circle 360

1. In a ____ _____ graph, each section (shaped like a piece of pie) shows a category and the relative size of the category.

- 2. A circle graph contains pie-shaped sections, each called a _____
- 3. The number of degrees in a whole circle is _
- 4. If a circle graph has percent labels, the percents should add up to _

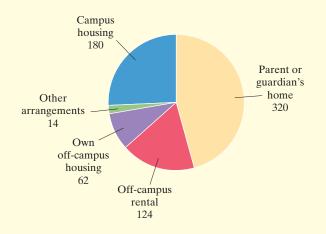
Martin-Gay Interactive Videos Watch the section lecture video and answer the following questions.

Objective A 5. From Example 3, when a circle graph shows different parts or percents of some whole category, what is the sum of the percents in the whole circle graph? **Objective B** 6. From Example 6, when looking at the sector degree measures of a circle graph, the whole circle graph corresponds to what degree measure? see Video 9.2 🛑

9.2 Exercise Set MyLab Math

Objective A The following circle graph is a result of surveying 700 college students. They were asked where they live while attending college. Use this graph to answer Exercises 1 through 6. Write all ratios as fractions in simplest form. See *Example 1.*

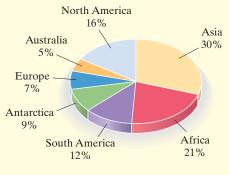
- **•1.** Where do most of these college students live?
 - **2.** Besides the category "Other arrangements," where do the fewest of these college students live?
- 3. Find the ratio of students living in campus housing to total students.
 - **4.** Find the ratio of students living in off-campus rentals to total students.
 - **5.** Find the ratio of students living in campus housing to students living in a parent or guardian's home.



6. Find the ratio of students living in off-campus rentals to students living in a parent or guardian's home.

The following circle graph shows the percent of the land area of the continents of Earth. Use this graph for Exercises 7 through 14. See Example 2.

- **7.** Which continent is the largest?
- **8.** Which continent is the smallest?
- **9.** What percent of the land on Earth is accounted for by Asia and Europe together?
- **10.** What percent of the land on Earth is accounted for by North and South America?



Source: National Geographic Society

The total amount of land from the continents is approximately 57,000,000 square miles. Use the graph to find the area of the continents given in Exercises 11 through 14. See Example 3.

11. Asia

12. South America

13. Australia

14. Europe

Nonfiction

25%

Children's fiction

22%

The following circle graph shows the percent of the types of books available at Midway Memorial Library. Use this graph for Exercises 15 through 24. See Example 2.

- **15.** What percent of books are classified as some type of fiction?
 - **16.** What percent of books are nonfiction or reference?
- **17.** What is the second-largest category of books?
 - **18.** What is the third-largest category of books?

If this library has 125,600 books, find how many books are in each category given in Exercises 19 through 24. See *Example 3*.

| • 19. Nonfiction | 20. Reference | 21. Children's fiction |
|----------------------------|-------------------------------|--------------------------------|
| 22. Adult's fiction | 23. Reference or other | 24. Nonfiction or other |

Objective B Fill in each table. Round to the nearest degree. Then draw a circle graph to represent the information given in each table. (Remember: The total of "Degrees in Sector" column should equal 360° or very close to 360° because of rounding.) See Example 4.

| 25. | Types of Apples Grown in Washington State | | | | | |
|-----|---|---------|-------------------|--|--|--|
| | Type of Apple | Percent | Degrees in Sector | | | |
| | Red Delicious | 37% | | | | |
| | Golden Delicious | 13% | | | | |
| | Fuji | 14% | | | | |
| | Gala | 15% | | | | |
| | Granny Smith | 12% | | | | |
| | Other varieties | 6% | | | | |
| | Braeburn | 3% | | | | |
| | (Source: U.S. Apple Association) | | | | | |

(

| 26. | Color Distribution of M&M's Milk Chocolate | | | | | |
|-----|--|---------|-------------------|--|--|--|
| | Color | Percent | Degrees in Sector | | | |
| | Blue | 24% | | | | |
| | Orange | 20% | | | | |
| | Green | 16% | | | | |
| | Yellow | 14% | | | | |
| | Red | 13% | | | | |
| | Brown | 13% | | | | |
| | (Source: M&M N | Mars) | | | | |

Adult's fiction 33%

Reference

17%

Other

3%

| Distribution of Large Dams by Continent | | | | | | |
|--|-----|--|--|--|--|--|
| Continent Percent Degrees in Sector | | | | | | |
| Europe | 19% | | | | | |
| North America | 32% | | | | | |
| South America | 3% | | | | | |
| Asia | 39% | | | | | |
| Africa | 5% | | | | | |
| Australia | 2% | | | | | |
| (Source: International Commission on Large Dams) | | | | | | |

| 28. | Distribution of Department of the
Interior Public Lands by Management | | | | | | | |
|-----|--|-----------------------------|--|--|--|--|--|--|
| | Bureau of Management Percent Degrees in Sector | | | | | | | |
| | Bureau of Indian Affairs | Bureau of Indian Affairs 9% | | | | | | |
| | National Park Service | 11% | | | | | | |
| | Fish and Wildlife | 20% | | | | | | |
| | U.S. Forest Service 31% | | | | | | | |
| | Bureau of Land Management 29% | | | | | | | |
| | (Source: Department of the Interior: National Park Service) | | | | | | | |

Review

Write the prime factorization of each number. See Section 2.2.

| 29. 20 | 30. 25 | 31. 40 |
|---------------|---------------|----------------|
| 32. 16 | 33. 85 | 34. 105 |

Concept Extensions

The following circle graph shows the relative sizes of the great oceans. Use this graph for Exercises 35 through 40.

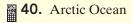
35. Without calculating, determine which ocean is the largest. How can you answer this question by looking at the circle graph?
36. Without calculating, determine which ocean is the smallest. How can you answer this question by looking at the circle graph?
36. Without calculating, determine which ocean is the smallest. How can you answer this question by looking at the circle graph?

These oceans together make up 264,489,800 square kilometers of Earth's surface. Find the square kilometers for each ocean.

37. Pacific Ocean

38. Atlantic Ocean

39. Indian Ocean



1

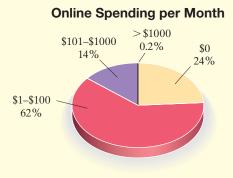
The following circle graph summarizes the results of online spending in America. Let's use these results to make predictions about the online spending behavior of a community of 2800 Internet users age 18 and over. Use this graph for Exercises 41 through 46. Round to the nearest whole. (Note: Because of rounding, these percents do not have a sum of 100%.)

- **41.** How many of the survey respondents said that they spend \$0 online each month?
- **42.** How many of the survey repondents said that they spend \$1-\$100 online each month?
- **43.** How many of the survey respondents said that they spend \$0 to \$100 online each month?
- **44.** How many of the survey respondents said that they spend \$1 to \$1000 online each month?
 - **45.** Find the ratio of *number* of respondents who spend \$0 online to *number* of respondents who spend \$1–\$100 online. Write the ratio as a fraction. Simplify the fraction if possible.

See the Concept Checks in this section.

47. Can the data below be represented by a circle graph? Why or why not?

| Responses to the Question "What Classes Are You Taking?" | | | |
|--|-----|--|--|
| Math | 80% | | |
| English | 72% | | |
| History | 37% | | |
| Biology | 21% | | |
| Chemistry | 14% | | |

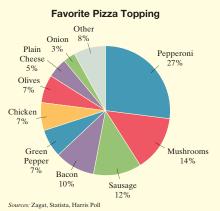


Source: The Digital Future Report, 2013

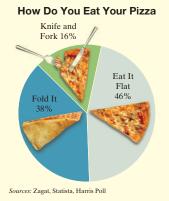
- **46.** Find the ratio of *percent* of respondents who spend \$101-\$1000 online to *percent* of those who spend \$1-\$100. Write the ratio as a fraction with integers in the numerator and denominator. Simplify the fraction if possible.
- **48.** True or false? The smaller a sector in a circle graph, the smaller the percent of the total it represents. Explain why.

Study the Chapter Opener circle graphs below and conduct surveys with at least 30 people.

49. Using the "Favorite Pizza Topping" circle graph as a guide, ask each person in your survey to choose his or her favorite pizza topping. Tally the results, draw a circle graph and compare your circle graph to the one shown.



50. Using the "How Do You Eat Your Pizza?" circle graph as a guide, ask each person in your survey to choose how he or she eats pizza. Then follow the directions in Exercise **49**.



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Integrated Review

Sections 9.1–9.2

Answers

Reading Graphs

1.

2.

3.

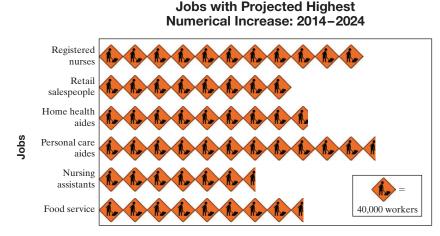
4.

5.

6.

7.

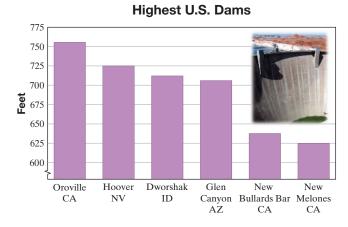
The following pictograph shows the six occupations with the largest estimated numerical increase in employment in the United States between 2014 and 2024. Use this graph to answer Exercises 1 through 4.



Source: Bureau of Labor Statistics

- **1.** Approximate the increase in the number of retail salespeople from 2014 to 2024.
- 2. Approximate the increase in the number of registered nurses from 2014 to 2024.
- **3.** Which occupation is expected to show the greatest increase in number of employees between the years shown?
- **4.** Which of the listed occupations is expected to show the least increase in number of employees between the years shown?

The following bar graph shows the highest U.S. dams. Use this graph to answer Exercises 5 through 8.



- **5.** Name the U.S. dam with the greatest height and estimate its height.
- **6.** Name the U.S. dam whose height is between 625 and 650 feet and estimate its height.
- **7.** Estimate how much higher the Hoover Dam is than the Glen Canyon Dam.
- **8.** How many U.S. dams have heights over 700 feet?

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8.

Integrated Review

The following line graph shows the daily high temperatures for 1 week in Annapolis, Maryland. Use this graph to answer Exercises 9 through 12.

- **9.** Name the day(s) of the week with the highest temperature and give that high temperature.
- **10.** Name the day(s) of the week with the lowest temperature and give that low temperature.
- **11.** On what days of the week was the temperature less than 90° Fahrenheit?
- **12.** On what days of the week was the temperature greater than 90° Fahrenheit?

The following circle graph shows the types of milk beverages consumed in the United States. Use this graph for Exercises 13 through 16.

If a store in Kerrville, Texas, sells 200 quart containers of milk per week, estimate how many quart containers are sold in each category below.

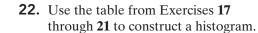
13. Whole milk Types of Beverage Milk Consumed Skim 26% Whole **14.** Skim milk 35% **15.** Buttermilk Flavored whole 1% Flavored reduced **16.** Flavored reduced fat and skim milk Buttermilk 2% Reduced fat and skim 1% fat 34% 3%

Source: U.S. Department of Agriculture

The following list shows weekly quiz scores for a student in basic college mathematics. Use this list to complete the frequency distribution table.

| 50 | 80 | 71 | 83 | 86 |
|----|----|----|----|----|
| 67 | 89 | 93 | 88 | 97 |
| 75 | 80 | 78 | 93 | 99 |
| | 53 | 90 | | |

| | Class Intervals
(Scores) | Tally | Class Frequency
(Number of Quizzes) |
|-----|-----------------------------|-------|--|
| 17. | 50–59 | | |
| 18. | 60–69 | | |
| 19. | 70–79 | | |
| 20. | 80–89 | | |
| 21. | 90–99 | | |





| Quiz | Scores |
|------|--------|
|------|--------|

9. 10. 11. 12. 13. 14. 15. 16. 17. 18. 19. 20. 21. 22.

100 98 degrees Fahrenheit) 96 Temperature 94 92 90 88 86 84 82 S Т W Th F Μ S Days of the Week

Objectives

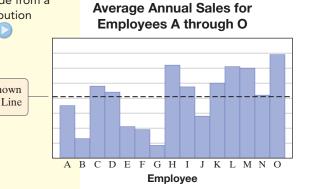
- A Find the Mean (or Average) of a List of Numbers. 🜔
- **B** Find the Median of a List of Numbers. 🕟
- **C** Find the Mode of a List of Numbers. 🕟
- D Calculate Range, Mean, Median, and Mode from a **Frequency Distribution** Table or Graph. 🌔

Average Shown on Dashed Line

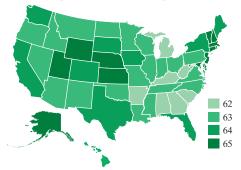
9.3 Mean, Median, Mode, and Range

We are certainly familiar with the word "average." The next examples show real-life averages. For example,

- The average cost of a pie (or whole pizza) is \$16.73.
- Adults employed in the United States report working an average of 47 hours per week, according to a Gallup poll.
- The U.S. miles per gallon average for light vehicles is 25.5, according to autonews. com (Automotive News).



The Average Retirement Age in the U.S.



Based on U.S. Census Bureau labor force participation data.

As our accumulation of data increases, our ability to gather, store, and present these tremendous amounts of data increases. Sometimes it is desirable to be able to describe a set of data by a single "middle" number or a measure of central tendency. Three of the most common **measures of central tendency** are the **mean** (or average), the median, and the mode.

Objective 🗛 Finding the Mean 🕑

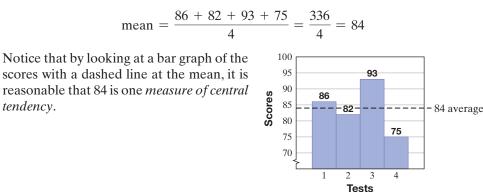
The most common measure of central tendency is the mean (sometimes called the "arithmetic mean" or the "average"). Recall that we first introduced finding the average of a list of numbers in Section 1.7.

The mean (average) of a set of number items is the sum of the items divided by the number of items.

mean = _____ sum of items number of items

tendency.

For example: To find the mean of four test scores -86, 82, 93, and 75 – we find the sum of the scores and then divide by the number of scores, 4.



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Example 1

Finding the Mean Time in an Experiment

Seven students in a psychology class conducted an experiment on mazes. Each student was given a pencil and asked to successfully complete the same maze. The timed results are below:

| Student | Ann | Thanh | Carlos | Jesse | Melinda | Ramzi | Dayni |
|----------------|------|-------|--------|-------|---------|-------|-------|
| Time (Seconds) | 13.2 | 11.8 | 10.7 | 16.2 | 15.9 | 13.8 | 18.5 |

- **a.** Who completed the maze in the shortest time? Who completed the maze in the longest time?
- **b.** Find the mean time.
- **c.** How many students took longer than the mean time? How many students took shorter than the mean time?

Solution:

- **a.** Carlos completed the maze in 10.7 seconds, the shortest time. Dayni completed the maze in 18.5 seconds, the longest time.
- **b.** To find the mean (or average), we find the sum of the items and divide by 7, the number of items.

mean = $\frac{\text{sum of items}}{\text{number of items}} = \frac{13.2 + 11.8 + 10.7 + 16.2 + 15.9 + 13.8 + 18.5}{7}$ = $\frac{100.1}{7} = 14.3$

c. Three students, Jesse, Melinda, and Dayni, had times longer than the mean time. Four students, Ann, Thanh, Carlos, and Ramzi, had times shorter than the mean time.

Work Practice 1

Concept Check Estimate the mean of the following set of data:

5, 10, 10, 10, 10, 15

The mean has one main disadvantage. This measure of central tendency can be greatly affected by *outliers*. (Outliers are values that are especially large or small when compared with the rest of the data set.) Let's see an example of this next.

Example 2

The table lists the rounded salary of 10 staff numbers.

| Staff | Α | В | С | D | Е | F | G | Н | Ι | J |
|----------------|------|------|------|------|------|------|-------|------|------|------|
| Salary | \$32 | \$34 | \$46 | \$38 | \$42 | \$95 | \$102 | \$50 | \$42 | \$41 |
| (in thousands) | | | | | | | | | | |

a. Find the mean of all 10 staff members.

b. Find the mean of all staff members except F and G.

Solution

a. mean =
$$\frac{32 + 34 + 46 + 38 + 42 + 95 + 102 + 50 + 42 + 41}{10} = \frac{522}{10}$$

The mean salary is \$52.2 thousand or \$52,200.

(Continued on next page)

Practice 1

Find the mean of the following test scores: 87, 75, 96, 91, and 78.

Practice 2

Use the table in Example 2 and find the mean salary of all staff members except G. Round thousands of dollars to 2 decimal places.

Answers 1. 85.4 2. \$46.67 thousand or \$46,670

Concept Check Answer

Chapter 9 | Reading Graphs and Introduction to Statistics and Probability

b. mean =
$$\frac{32 + 34 + 46 + 38 + 42 + 50 + 42 + 41}{8} = \frac{325}{8}$$

= 40.625

Now, the mean salary is \$40.625 thousand or \$40,625.

Work Practice 2

The mean in part **a**. does not appear to be a measure of central tendency because this mean, \$52.2 thousand, is greater than all salaries except 2 of the 10. Also, notice the difference in the means for parts **a**. and **b**. By removing the 2 outliers, the mean was greatly reduced.

Although the mean was calculated correctly each time, parts **a**. and **b**. of Example 2 show one disadvantage of the mean. That is, a few numerical outliers can greatly affect the mean.

Later in this section, we will discuss the range of a data set as well as calculate measures of central tendency from frequency distribution tables and graphs.

Helpful Hint

Remember an important disadvantage of the mean: If our data set has a few outliers, the mean may not be the best measure of central tendency.

Often in college, the calculation of a **grade point average** (GPA) is a **weighted mean** and is calculated as shown in Example 3.

Example 3 Calculating Grade Point Average (GPA)

The following grades were earned by a student during one semester. Find the student's grade point average.

| Course | Grade | Credit Hours |
|---------------------|-------|--------------|
| College mathematics | A | 3 |
| Biology | В | 3 |
| English | A | 3 |
| PE | C | 1 |
| Social studies | D | 2 |

Solution: To calculate the grade point average, we need to know the point values for the different possible grades. The point values of grades commonly used in colleges and universities are given below:

A: 4, B: 3, C: 2, D: 1, F: 0

Now, to find the grade point average, we multiply the number of credit hours for each course by the point value of each grade. The grade point average is the sum of these products divided by the sum of the credit hours.

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| Course | Grade | Point Value
of Grade | Credit
Hours | Point Value of
Credit Hours |
|---------------------|-------|-------------------------|-----------------|--------------------------------|
| College mathematics | A | 4 | 3 | 12 |
| Biology | В | 3 | 3 | 9 |
| English | А | 4 | 3 | 12 |
| PE | C | 2 | 1 | 2 |
| Social studies | D | 1 | 2 | 2 |
| < | | Totals: | 12 | 37 |

Practice 3

Find the grade point average if the following grades were earned in one semester. Round to 2 decimal places.

| Grade | Credit Hours |
|-------|--------------|
| А | 2 |
| В | 4 |
| С | 5 |
| D | 2 |
| A | 2 |

grade point average = $\frac{37}{12} \approx 3.08$ rounded to two decimal places

The student earned a grade point average of 3.08.

Work Practice 3

Objective **B** Finding the Median 🕑

You may have noticed that a very low number or a very high number can affect the mean of a list of numbers. Because of this, you may sometimes want to use another measure of central tendency. A second measure of central tendency is called the **median**. The median of a list of numbers is not affected by a low or high number in the list.

The **median** of a set of numbers in numerical order is the middle number. If the number of items is odd, the median is the middle number. If the number of items is even, the median is the mean of the two middle numbers.

Example 4

Find the median of the following list of numbers:

25, 54, 56, 57, 60, 71, 98

Solution: Because this list is in numerical order, the median is the middle number, 57.

Work Practice 4

Example 5 Find the median of the following list of scores: 67,91,75,86,55,91

Solution: First we list the scores in numerical order and then we find the middle number.

55, 67, 75, 86, 91, 91

Since there is an even number of scores, there are two middle numbers, 75 and 86. The median is the mean of the two middle numbers.

median = $\frac{75 + 86}{2} = 80.5$

The median is 80.5.

Work Practice 5

Helpful Don't forget to write the numbers in order from smallest to largest before finding the median.

Objective C Finding the Mode 🜔

The last common measure of central tendency is called the mode.

The **mode** of a set of numbers is the number that occurs most often. (It is possible for a set of numbers to have more than one mode or to have no mode.)

Example 6

Find the mode of the list of numbers:

11, 14, 14, 16, 31, 56, 65, 77, 77, 78, 79

Solution: There are two numbers that occur the most often. They are 14 and 77. This list of numbers has two modes, 14 and 77.

Work Practice 6

Practice 4

Find the median of the list of numbers: 5, 11, 14, 23, 24, 35, 38, 41, 43

Practice 5

Find the median of the list of scores: 36, 91, 78, 65, 95, 95, 88, 71

Practice 6

Find the mode of the list of numbers: 14, 10, 10, 13, 15, 15, 15, 17, 18, 18, 20

Answers 4. 24 5. 83 6. 15 a city in Montana.

76, 80, 85, 86, 89, 87, 82, 77, 76, 79, 82, 89, 89, 92

Solution: First we write the numbers in numerical order. 76, 76, 77, 79, 80, 82, 82, 85, 86, 87, 89, 89, 89, 92

Practice 7

Find the median and the mode of the list of numbers: 26, 31, 15, 15, 26, 30, 16, 18, 15, 35

Work Practice 7

numbers, 82 and 85.

median = $\frac{82 + 85}{2}$ = 83.5

The mode is 89, since 89 occurs most often.

Example 7

Concept Check True or false? Every set of numbers *must* have a mean, median, and mode. Explain your answer.

Since there is an even number of items, the median is the mean of the two middle

Find the median and the mode of the following set of numbers. These numbers were high temperatures for 14 consecutive days in

Helpful Hint

Don't forget that it is possible for a list of numbers to have no mode. For example, the list

2, 4, 5, 6, 8, 9

has no mode. There is no number or numbers that occur more often than the others.

Objective **D** Finding the Range of a Data Set and Reviewing Mean, Median, and Mode 💟

In this objective, we study one way to describe the dispersion of a data set, and we review mean, median, and mode. What is dispersion? In statistics, dispersion is a way to describe the degree to which the data values are scattered.

Range

The range of a data set is the difference between the largest data value and the smallest data value.

range = largest data value - smallest data value

Example 8

The following pulse rates (for 1 minute) were recorded for a group of 15 students. Find the range.

78, 80, 66, 68, 71, 64, 82, 71, 70, 65, 70, 75, 77, 86, 72.

Solution: range = largest data value – smallest data value

$$= 86 - 64$$

= 22

The range of this data set is 22.

Work Practice 8

Practice 8

The table lists the rounded salary of 10 staff members. Find the range.

| Staff | Salary
(in thousands) |
|-------|--------------------------|
| А | \$32 |
| В | \$34 |
| С | \$46 |
| D | \$38 |
| Е | \$42 |
| F | \$95 |
| G | \$102 |
| Н | \$50 |
| Ú J | \$42 |

Answers

7. median: 22; mode: 15 8. \$70 thousand

Concept Check Answer

false; a set of numbers may have no mode

Let's recall a few facts about the median, and then we will introduce a formula for finding the position of the median.

- The median of a set of numbers in numerical order is the middle number.
- If the number of items is odd, the median is the middle number.
- If the number of items is even, the median is the *mean* (average) of the two middle numbers.

For a long list of data items, this formula gives us the **position** of the median.

Position of the Median

For *n* data items in order from smallest to largest, the median is the item in the

 $\frac{n+1}{2}$ position.

Note:

If *n* is an even number, then the position formula, $\frac{n+1}{2}$, will not be a whole number.

In this case, simply find the average of the two data items whose positions are closest to, but before and after $\frac{n+1}{2}$.

Helpful Hint

The formula above, $\frac{n+1}{2}$ does not give the *value* of the median, just the **position** of the median.

Example 9

Find the (a) range, (b) mean, (c) median, and (d) mode from this frequency distribution table of retirement ages. If needed, round answers to 1 decimal place.

| Age | Frequency |
|-----|-----------|
| 60 | 3 |
| 61 | 1 |
| 62 | 1 |
| 63 | 2 |
| 64 | 2 |
| 65 | 2 |

Solution: Study the table for a moment. From the frequency column, we see that there are 11 data items (3 + 1 + 1 + 2 + 2 + 2).

a. range = largest data value - smallest data value

$$= 65 - 60$$

= 5

The range of this data set is 5.

(Continued on next page)

Practice 9

One state with a young retirement age is Michigan. The table below is from a poll of retirement ages from that state.

| Age | Frequency |
|-----|-----------|
| 50 | 1 |
| 59 | 3 |
| 60 | 3 |
| 62 | 5 |
| 63 | 2 |
| 67 | 1) |

Find the (a) range, (b) mean, (c) median, and (d) mode of these data. If needed, round answers to 1 decimal place.

Answers

9. a. range: 17 b. mean: 60.7,c. median: 62, d. mode: 62

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Helpful Hint Since there are three 60's, for example, we can either use: 60 + 60 + 60 or $3 \cdot 60$.

b. To find the mean, we use our mean formula:

mean =
$$\frac{\text{sum of items}}{\text{number of items}} = \frac{3 \cdot 60 + 61 + 62 + 2 \cdot 63 + 2 \cdot 64 + 2 \cdot 65}{11}$$

= $\frac{687}{11} \approx 62.5$

The mean of the data set is approximately 62.5.

c. Since there are 11 data items and the items are arranged in numerical order in the table, we find $\frac{n+1}{2}$ to locate the middle item. This is $\frac{11+1}{2} = \frac{12}{2} = 6$, or the sixth item.

The median is the sixth number, or 63.

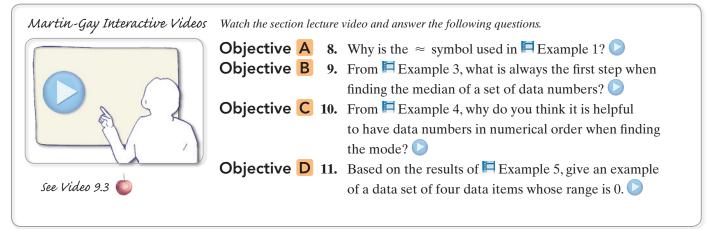
d. The mode has the greatest frequency, so the mode is 60.

Work Practice 9

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Some choices may be used more than once.

| | mean
median | mode
range | grade point average
average |
|----|-----------------------------|---------------------------|--|
| 1. | Another word | for "mean" is _ | · |
| 2. | The number th | at occurs most | often in a set of numbers is called the |
| 3. | The | of a | set of number items is $\frac{\text{sum of items}}{\text{number of items}}$. |
| 4. | The | of a | set of numbers is the middle number. If the number of numbers is even, it is the |
| | | of the tw | vo middle numbers. |
| 5. | An example of | weighted mea | n is a calculation of |
| 6. | | = grea | test data value – smallest data value |
| 7. | The formula <u><i>n</i></u> | $\frac{+1}{2}$ can be use | ed to find the position of the |



9.3 Exercise Set MyLab Math 🚺

Objectives A B C Mixed Practice For each set of numbers, find the mean, median, and mode. If necessary, round the mean to one decimal place. See Examples 1, 2, and 4 through 6.

| 1. 15, 2 | 3, 24, 18, 25 | 2. | 45, 36, 28, 46, 52 |
|------------------|--|----|---|
| 3. 7.6, 8 | 8.2, 8.2, 9.6, 5.7, 9.1 | 4. | 4.9, 7.1, 6.8, 6.8, 5.3, 4.9 |
| 5. 0.5, 0 | 0.2, 0.2, 0.6, 0.3, 1.3, 0.8, 0.1, 0.5 | 6. | 0.6, 0.6, 0.8, 0.4, 0.5, 0.3, 0.7, 0.8, 0.1 |
| 7. 231, | 543, 601, 293, 588, 109, 334, 268 | 8. | 451, 356, 478, 776, 892, 500, 467, 780 |

The 10 tallest buildings in the world, completed as of the end of 2016, are listed in the following table. Use this table to answer Exercises 9 through 14. If necessary, round results to one decimal place. See Examples 1, 2, and 4 through 6.

- **9.** Find the mean height of the five tallest buildings.
- **10.** Find the median height of the five tallest buildings.
- **11.** Find the median height of the six tallest buildings.
- **12.** Find the mean height of the six tallest buildings.
- 13. Given the building heights, explain how you know, without calculating, that the answer to Exercise 10 is greater than the answer to Exercise 11.

| Building | Height in Feet |
|---|----------------|
| Burj Khalifa, Dubai | 2717 |
| Shanghai Tower, Shanghai | 2073 |
| Makkah Royal Clock Tower, Mecca | 1972 |
| Ping An Finance Center | 1965 |
| Lotte World Tower | 1819 |
| One World Trade Center, New York City | 1776 |
| Guangzhou CTF Finance Center, Guangzhou | 1739 |
| Taipei 101, Taipei | 1667 |
| Shanghai World Financial Center, Shanghai | 1614 |
| International Commerce Center, Hong Kong | 1588 |
| (Source: Council on Tall Buildings and Urban Habitat) | • |

14. Given the building heights, explain how you know, without calculating, that the answer to Exercise **12** is less than the answer to Exercise **9**.

For Exercises 15 through 18, the grades are given for a student for a particular semester. Find the grade point average. If necessary, round the grade point average to the nearest hundredth. See Example 3.

1

15. Grade Credit Hours

| Graue | Cicult Hours |
|-------|--------------|
| В | 3 |
| С | 3 |
| А | 4 |
| С | 4 |

| 17. | Grade | Credit Hours |
|-----|-------|--------------|
| | А | 3 |
| | A | 3 |
| | А | 4 |
| | В | 3 |
| | С | 1 |

| 16. | Grade | Credit Hours |
|-----|-------|--------------|
| | D | 1 |
| | F | 1 |
| | С | 4 |
| | В | 5 |

| 8. | Grade | Credit Hours |
|----|-------|--------------|
| | В | 2 |
| | В | 2 |
| | С | 3 |
| | А | 3 |
| | В | 3 |

| - | g an experiment, the following time
8, 6.9, 7.5, 4.7, 6.9, 7.0. | es (in seconds) we | re recorded: | |
|---------------|---|-----------------------|----------------------------|------------------------------------|
| 19. Fi | ind the mean. | 20. Find the m | edian. | 21. Find the mode. |
| | athematics class, the following test
3, 85, 89, 79, 88, 91. | scores were recoi | ded for a student: | |
| 22. Fi | nd the mean. | 23. Find the m | edian. | 24. Find the mode. |
| - | llowing pulse rates were recorded j
3, 80, 66, 68, 71, 64, 82, 71, 70, 65, 7 | | students: | |
| 25. Fi | ind the mean. | | 26. Find the median | 1. |
| 27. Fi | nd the mode. | | 28. How many puls | e rates were higher than the mean? |
| 29. H | ow many pulse rates were lower t | than the mean? | 30. Explain how to | find the position of the median. |

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| Name | Length (miles) |
|----------------------|----------------|
| Nile | 4160 |
| Amazon | 4000 |
| Yangtze | 3915 |
| Mississippi-Missouri | 3709 |
| Ob-Irtysh | 3459 |
| Huang Ho | 3395 |

Below are lengths for the six longest rivers in the world.

Find the mean and the median for each of the following.

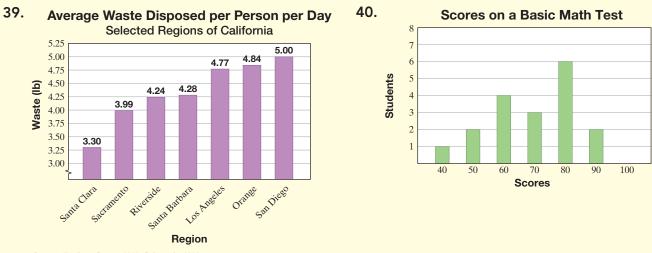
 4160
 31. the six longest rivers
 32. the three longest rivers

 3915
 3709

 3459
 3395

Objective D *Find the range for each data set. See Example 8.*

33. 14, 16, 8, 10, 20
34. 25, 15, 11, 40, 37
36. 129, 188, 188, 276
37. 9, 9, 9, 9, 11



Sources: Equinox Center, 2013; Calrecycle, 2013

Use each frequency distribution table to find the a. mean, b. median, and c. mode. If needed, round the mean to 1 decimal place. See Example 9.

| 41. | Data Item | Frequency |
|-----|-------------|------------------|
| | 5 | 1 |
| | 6 | 1 |
| | 7 | 2 |
| | 8 | 5 |
| | 9 | 6 |
| | 10 | 2 |
| 43. | Data Item | Frequency |
| | 2 | 5 |
| | | |
| | 3 | 7 |
| | 3 4 | |
| | | 7 |
| | 4 | 7
4 |
| | 4 5 | 7
4
7 |
| | 4
5
6 | 7
4
7
8 |

10

5

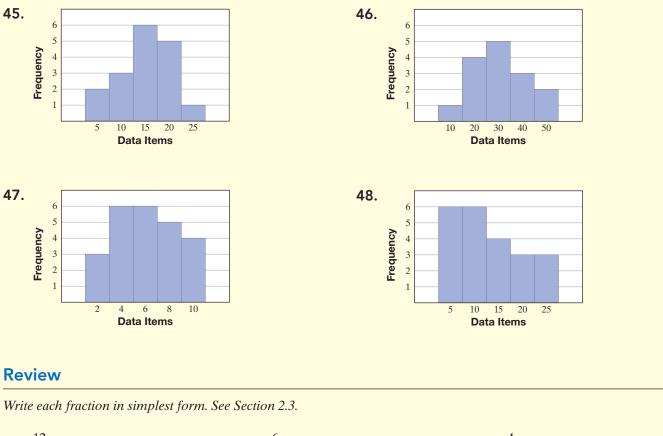
(

| 42 . (| Data Item | Frequency |
|---------------|-----------|-----------|
| | 3 | 2 |
| | 4 | 1 |
| | 5 | 4 |
| | 6 | 7 |
| | 7 | 2 |
| ĺ | 8 | 1 |
| | | - |

35. 206, 206, 555, 556

38. 7, 7, 7, 7, 10

| 44. | Data Item | Frequency |
|-----|-----------|-----------|
| | 4 | 3 |
| | 5 | 8 |
| | 6 | 5 |
| | 7 | 8 |
| | 8 | 2 |



Use each graph of data items to find the **a**. mean, **b**. median, and **c**. mode. If needed round the mean to one decimal place.

49. $\frac{12}{20}$ 50. $\frac{6}{18}$ 51. $\frac{4}{36}$ 52. $\frac{18}{30}$ 53. $\frac{35}{100}$ 54. $\frac{55}{75}$

Concept Extensions

Find the missing numbers in each set of numbers.

- **55.** ____, ___, 40, ____. The mode is 35. The median is 37. The mean is 38.
- 57. Without making any computations, decide whether the median of the following list of numbers will be a whole number. Explain your reasoning. 36, 77, 29, 58, 43
- **56.** 16, 18, ____, ____, ____. The mode is 21. The median is 20.
- **58.** Write a list of numbers for which you feel the median would be a better measure of central tendency than the mean.

9.4 Counting and Introduction to Probability

Objective 🗛 Using a Tree Diagram 🕑

In our daily conversations, we often talk about the likelihood or **probability** of a given result occurring. For example:

The chance of thundershowers is 70 percent.

What are the *odds* that the New Orleans Saints will go to the Super Bowl? What is the *probability* that you will finish cleaning your room today?

Each of these chance happenings—thundershowers, the New Orleans Saints playing in the Super Bowl, and finishing cleaning your room today—is called an **experiment**. The possible results of an experiment are called **outcomes**. For example, flipping a coin is an experiment, and the possible outcomes are heads (H) or tails (T).

One way to picture the outcomes of an experiment is to draw a **tree diagram**. Each outcome is shown on a separate branch. For example, the outcomes of flipping a coin are



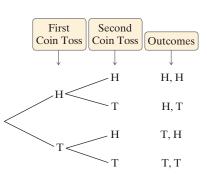




Example 1

Draw a tree diagram for tossing a coin twice. Then use the diagram to find the number of possible outcomes.

Solution:



There are 4 possible outcomes when tossing a coin twice.

Work Practice 1

Example 2

Draw a tree diagram for an experiment consisting of rolling a die and then tossing a coin. Then use the diagram to find the number of possible outcomes.



Objectives



B Find the Probability of an Event.

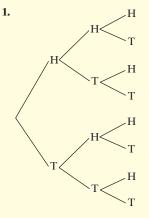
Practice 1

Draw a tree diagram for tossing a coin three times. Then use the diagram to find the number of possible outcomes.

Practice 2

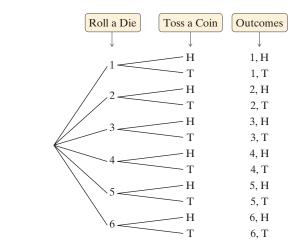
Draw a tree diagram for an experiment consisting of tossing a coin and then rolling a die. Then use the diagram to find the number of possible outcomes. (Answer appears on the next page.)

Answer



(Continued on next page)

Solution: Recall that a die has six sides and that each side represents a number, 1 through 6.



There are 12 possible outcomes for rolling a die and then tossing a coin.

Work Practice 2

Any number of outcomes considered together is called an **event.** For example, when tossing a coin twice, H, H is an event. The event is tossing heads first and tossing heads second. Another event would be tossing tails first and then heads (T, H), and so on.

Objective **B** Finding the Probability of an Event 💟

As we mentioned earlier, the **probability of an event is a measure of the chance or likelihood of it occurring.** For example, if a coin is tossed, what is the probability that heads occurs? Since one of two equally likely possible outcomes is heads, the probability is $\frac{1}{2}$.

The Probability of an Event

| probability of an event = | number of ways that
the event can occur | |
|---------------------------|--|--|
| | number of possible | |
| | outcomes | |

Note from the definition of probability that the probability of an event is always between 0 and 1, inclusive (i.e., including 0 and 1). A probability of 0 means that an event won't occur, and a probability of 1 means that an event is certain to occur.

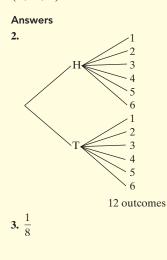


If a coin is tossed twice, find the probability of tossing heads on the first toss and then heads again on the second toss (H, H).

Solution: 1 way the event can occur H,T, H,H, T,H, T,T4 possible outcomes

Practice 3

If a coin is tossed three times, find the probability of tossing tails, then heads, then tails (T, H, T).



probability $= \frac{1}{4}$ Number of ways the event can occur Number of possible outcomes The probability of tossing heads and then heads is $\frac{1}{4}$. Work Practice 3 <u>Example</u> 4 If a die is rolled one time, find the probability of rolling a 3 or a 4. **Solution:** Recall that there are 6 possible outcomes when rolling a die. 2 ways that the event can occur possible outcomes: 1, 2, 3, 4, 5, 6 6 possible outcomes probability of a 3 or a 4 = $\frac{2}{6}$ Number of ways the event can occur Number of possible outcomes $=\frac{1}{3}$ Simplest form Work Practice 4 **Concept Check** Suppose you have calculated a probability of $\frac{11}{9}$. How do you know that you have made an error in your calculation? Example 5 Find the probability of choosing a red marble from a box containing 1 red, 1 yellow, and 2 blue marbles. Solution: 1 way that event can occur

Practice 4

If a die is rolled one time, find the probability of rolling a 2 or a 5.

Practice 5

Use the diagram and information in Example 5 and find the probability of choosing a blue marble from the box.

Answers

4. $\frac{1}{3}$ **5.** $\frac{1}{2}$

Concept Check Answer

The number of ways an event can occur can't be larger than the number of possible outcomes.

Vocabulary, Readiness & Video Check

yellow

4 possible outcomes

blue

blue

Use the choices below to fill in each blank. Choices may be used more than once.

| 0 | probability | tree diagram |
|---|-------------|--------------|
|---|-------------|--------------|

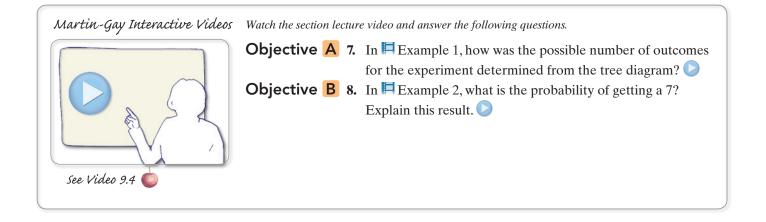
1 outcome

probability = $\frac{1}{4}$

Work Practice 5

- 1. A possible result of an experiment is called a(n)
- **2.** A(n) ______ shows each outcome of an experiment as a separate branch.
- 3. The ______ of an event is a measure of the likelihood of it occurring.

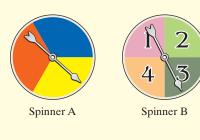
- 4. ______ is calculated by the number of ways that an event can occur divided by the number of possible outcomes.
- 5. A probability of _____ means that an event won't occur.
- 6. A probability of ______ means that an event is certain to occur.



9.4 Exercise Set MyLab Math

Objective A *Draw a tree diagram for each experiment. Then use the diagram to find the number of possible outcomes. See Examples 1 and 2.*

- 1. Choosing a letter in the word MATH and then a number (1, 2, or 3)
- **2.** Choosing a number (1 or 2) and then a vowel (a, e, i, o, or u)



- **3.** Spinning Spinner A once
- 4. Spinning Spinner B once

5. Spinning Spinner B twice

6. Spinning Spinner A twice

- **7.** Spinning Spinner A and then Spinner B
- 8. Spinning Spinner B and then Spinner A

- **9.** Tossing a coin and then spinning Spinner B
- **10.** Spinning Spinner A and then tossing a coin

Objective B If a single die is tossed once, find the probability of each event. See Examples 3 through 5.

D11. A 5 **12.** A 9 **13.** A 1 or a 6 **14.** A 2 or a 3

| 1 5 | . An | even | number | |
|------------|------|------|--------|--|
|------------|------|------|--------|--|

16. An odd number

17. A number greater **18.** A num than 2

18. A number less than 6

Suppose the spinner shown is spun once. Find the probability of each event. See Examples 3 through 5.



- **21.** The result of the spin is 1, 2, or 3.
- **23.** The result of the spin is an odd number.

- **19.** The result of the spin is 2.
 - **20.** The result of the spin is 3.
 - **22.** The result of the spin is not 3.
 - **24.** The result of the spin is an even number.

If a single choice is made from the bag of marbles shown, find the probability of each event. See Examples 3 through 5.

29. A green or red marble is chosen.

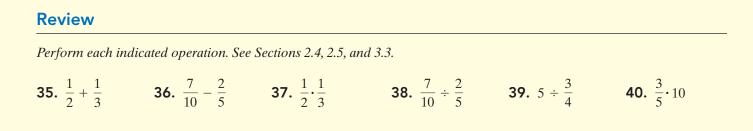
- **25.** A red marble is chosen.
- **26.** A blue marble is chosen.
- **27.** A yellow marble is chosen.
- **28.** A green marble is chosen.
- **30.** A blue or yellow marble is chosen.

A new drug is being tested that is supposed to lower blood pressure. This drug was given to 200 people, and the results are shown below.

| Lower | Higher | Blood Pressure |
|----------------|----------------|----------------|
| Blood Pressure | Blood Pressure | Not Changed |
| 152 | 38 | 10 |

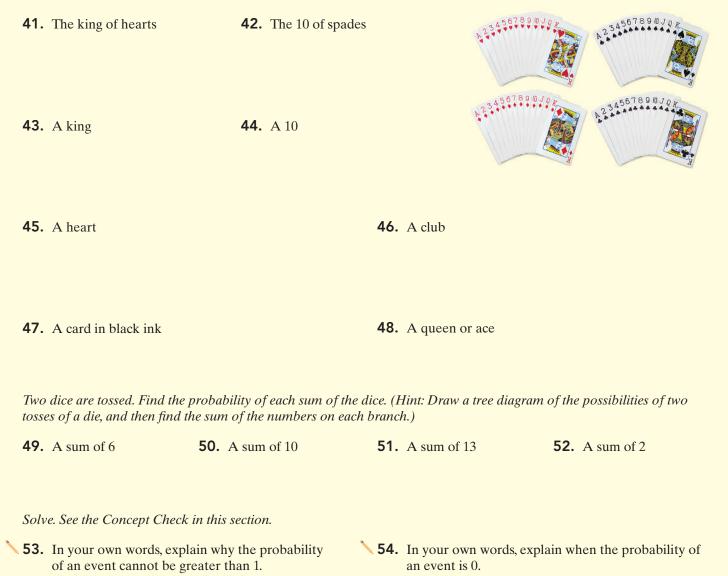
- **31.** If a person is testing this drug, what is the probability that his or her blood pressure will be higher?
- **33.** If a person is testing this drug, what is the probability that his or her blood pressure will not change?
- **32.** If a person is testing this drug, what is the probability that his or her blood pressure will be lower?
- **34.** What is the sum of the answers to Exercises **31**, **32**, and 33? In your own words, explain why.





Concept Extensions

Recall that a deck of cards contains 52 cards. These cards consist of four suits (hearts, spades, clubs, and diamonds) of each of the following: 2, 3, 4, 5, 6, 7, 8, 9, 10, jack, queen, king, and ace. If a card is chosen from a deck of cards, find the probability of each event.



Chapter 9 Group Activity

Sections 9.1, 9.2, 9.3

This activity may be completed by working in groups or individually.

How often have you read an article in a newspaper or in a magazine that included results from a survey or poll? Surveys seem to have become very popular ways of getting feedback on anything from a political candidate, to a new product, to services offered by a health club. In this activity, you will conduct a survey and analyze the results.

- **1.** Conduct a survey of 30 students in one of your classes. Ask each student to report his or her age.
- **2.** Classify each age according to the following categories: under 20, 20 to 24, 25 to 29, 30 to 39, 40 to 49, and 50 or over. Tally the number of your survey respondents that fall into each category. Make a histogram

of your results. What does this graph tell you about the ages of your survey respondents?

- 3. Find the average age of your survey respondents.
- 4. Find the median age of your survey respondents.
- 5. Find the mode of the ages of your survey respondents.
- 6. Compare the mean, median, and mode of your age data. Are these measures similar? Which is largest? Which is smallest? If there is a noticeable difference between any of these measures, can you explain why?
- **7.** Conduct another survey with at least 30 people. Follow the directions of Exercises 49 and 50 of Section 9.2.

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Chapter 9 Vocabulary Check

Fill in each blank with one of the words or phrases listed below. Some choices may be used more than once.

| | | 5 | 1 | | |
|-----|--|----------------|------------------------------|--------------------------------|----------------------------------|
| | outcomes | bar | experiment | mean | tree diagram |
| | pictograph | line | class interval | median | probability |
| | histogram | circle | class frequency | range | mode |
| 1. | A(n) | gra | ph presents data using | vertical or ho | rizontal bars. |
| 2. | The | of a s | et of number items is -
r | sum of items
number of item |
18 |
| 3. | The possible resu | ults of an exp | periment are the | | |
| 4. | A(n) | is a g | raph in which pictures | or symbols ar | e used to visually present data. |
| 5. | The | of a s | et of numbers is the nu | umber that occ | eurs most often. |
| 6. | A(n) | graph | displays information | with a line that | t connects data points. |
| 7. | The of an ordered set of numbers is the middle number. | | | | |
| 8. | • A(n) is one way to picture and count outcomes. | | | | |
| 9. | 0. A(n) is an activity being considered, such as tossing a coin or rolling a die. | | | | |
| 10. | 0. In a(n) graph, each section (shaped like a piece of pie) shows a category and the relative size of | | | | |
| | the category. | | | | |
| 11. | 11. The of an event is the event can occur | | | | |
| 12. | 12. A(n) is a special bar graph in which the width of each bar represents a(n) and the height of each bar represents the | | | | |
| 13. | 13. = greatest data value – smallest data value | | | | |
| 14. | 14. The formula $\frac{n+1}{2}$ can be used to find the position of the | | | | |

Helpful Hint

• Are you preparing for your test? To help, don't forget to take these:

- Chapter 9 Getting Ready for the Test on page 639
- Chapter 9 Test on page 641

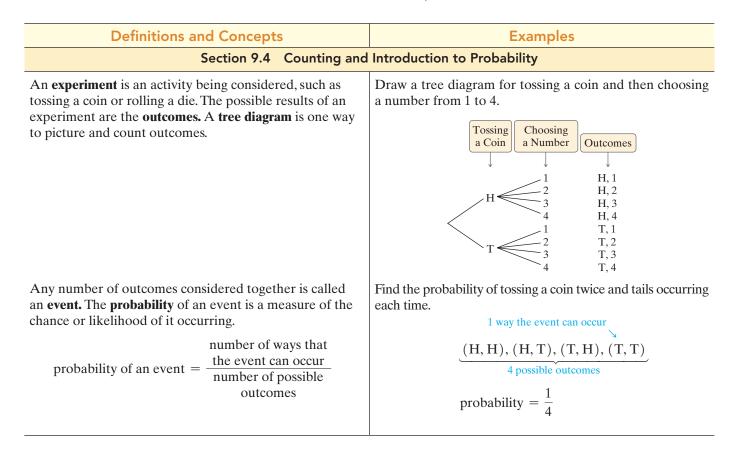
Then check all of your answers at the back of the text. For further review, the step-by-step video solutions to any of these exercises are located in MyLab Math.

9 Chapter Highlights

| Definitions and Concepts | Examples | |
|--|---|--|
| Section 9.1 Pictographs, Bar Gra | aphs, Histograms, and Line Graphs | |
| A pictograph is a graph in which pictures or symbols are used to visually present data. | Corn Production, Selected States | |
| A line graph displays information with a line that connects data points. | | |
| A bar graph presents data using vertical or horizontal bars. | Acres Harvested | |
| The bar graph on the right shows the number of acres of corn harvested in a recent year for selected states. | | |
| | IA KS TX IL MN NE | |
| | States Source: U.S. Department of Agriculture | |
| A histogram is a special bar graph in which the width of
each bar represents a class interval and the height of each
bar represents the class frequency. The histogram on the
right shows student quiz scores. | Approximately how many acres of corn were harvested in Iowa?
12,800,000 acres About how many more acres of corn were harvested in Illinois than Nebraska?
12 million
<u>- 8.5 million</u>
3.5 million or 3,500,000 acres subsect of 3,500,000 acres add the section of 3,500,000 acres add the section of 3,500,000 acres add the section of 3,500,000 acres begin add the section of 3,500,000 acres add the section of 3,500,000 acres begin add the section of 3,500,000 acres < | |
| | 4 students | |
| | 2. How many students received a score of 11–20? | |

9 + 13 = 22 students

| Definitions and Concepts | Examples | |
|--|--|--|
| Section 9.2 | Circle Graphs | |
| In a circle graph , each section (shaped like a piece of pie) shows a category and the relative size of the category. | Tornado Wind Speeds | |
| The circle graph on the right classifies tornadoes by wind speed. | 110-205 mph
28%Greater than
205 mph
2%Less than
110 mph
70% | |
| | Source: National Oceanic and Atmospheric Administration | |
| | 1. What percent of tornadoes have wind speeds of 110 mph or greater? | |
| | 28% + 2% = 30% | |
| | 2. If there were 1059 tornadoes in the United States in 2016, how many of these might we expect to have had wind speeds less than 110 mph? Find 70% of 1059. | |
| | $70\%(1059) = 0.70(1059) = 741.3 \approx 741$ | |
| | Around 741 tornadoes would be expected to have had wind speeds of less than 110 mph. | |
| Section 9.3 Mean, Me | dian, Mode, and Range | |
| The mean (or average) of a set of number items is | Find the mean, median, and mode of the following set of numbers: 33, 35, 35, 43, 68, 68 | |
| $mean = \frac{sum of items}{number of items}$ | mean = $\frac{33 + 35 + 35 + 43 + 68 + 68}{6} = 47$ | |
| The median of a set of numbers in numerical order is
the middle number. If the number of items is even, the
median is the mean of the two middle numbers. | The median is the mean of the two middle numbers,
35 and 43
median $= \frac{35 + 43}{2} = 39$ | |
| The mode of a set of numbers is the number that occurs most often. (A set of numbers may have no mode or more than one mode.) | There are two modes because there are two numbers that occur twice:
35 and 68 | |
| Range | | |
| The range of a data set is the difference between the largest data value and the smallest data value. | The range of data set 5, 7, 9, 11, 21, 21 is:
range = $21 - 5 = 16$ | |
| range = largest data value – smallest data value | | |



Chapter 9

Review

(9.1) The following pictograph shows the number of new homes constructed from October 2015 to October 2016, by region. Use this graph to answer Exercises 1 through 6.

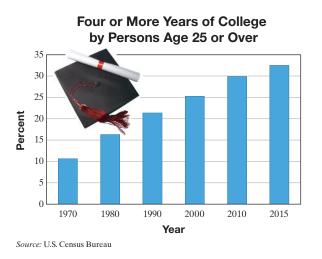


New Home Construction

Source: U.S. Census Bureau

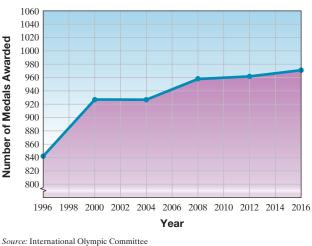
- **1.** How many new homes were constructed in the Midwest during the given year?
- **3.** Which region had the most new homes constructed?
- **5.** Which region(s) had 3,000,000 or more new homes constructed?
- **2.** How many new homes were constructed in the South during the given year?
- **4.** Which region had the fewest new homes constructed?
- **6.** Which region(s) had fewer than 3,000,000 new homes constructed?

The following bar graph shows the percent of persons age 25 or over who completed four or more years of college. Use this graph to answer Exercises 7 through 10.



- **7.** Approximate the percent of persons who had completed four or more years of college by 2010.
- **8.** What year shown had the greatest percent of persons completing four or more years of college?
- **9.** What years shown had 20% or more of persons completing four or more years of college?
- **10.** Describe any patterns you notice in this graph.

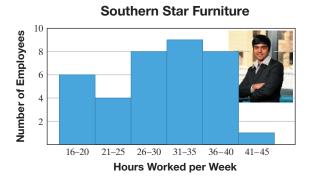
The following line graph shows the total number of Olympic medals awarded during the Summer Olympics since 1996. Use this graph to answer Exercises 11 through 16.



Number of Medals Awarded During Summer Olympics: 1996–2016

- **11.** Approximate the number of medals awarded during the Summer Olympics of 2012.
- **12.** Approximate the number of medals awarded during the Summer Olympics of 2000.
- **13.** Approximate the number of medals awarded during the Summer Olympics of 2016.
- **14.** Approximate the number of medals awarded during the Summer Olympics of 1996.
- **15.** How many more medals were awarded at the Summer Olympics of 2008 than at the Summer Olympics of 2004?
- **16.** The number of medals awarded at the Summer Olympics of 2016 is the greatest number of medals awarded at previous Summer Olympics. Why do you think this is so? Give your explanation in complete sentences.

The following histogram shows the hours worked per week by the employees of Southern Star Furniture. Use this histogram to answer Exercises 17 through 20.



- **17.** How many employees work 41–45 hours per week?
- **18.** How many employees work 21–25 hours per week?
- **19.** How many employees work 30 hours or less per week?
- **20.** How many employees work 36 hours or more per week?

Following is a list of monthly record high temperatures for New Orleans, Louisiana. Use this list to complete the frequency distribution table below.

| 83 | 96 | 101 | 92 |
|----|-----|-----|-----|
| 85 | 100 | 92 | 102 |
| 89 | 101 | 87 | 84 |

| | Class Intervals
(Temperatures) | Tally | Class Frequency
(Number of Months) |
|-----|-----------------------------------|-------|---------------------------------------|
| 21. | 80°-89° | | |
| 22. | 90°-99° | | |
| 23. | 100°-109° | | |

24. Use the table from Exercises **21** through **23** to draw a histogram.



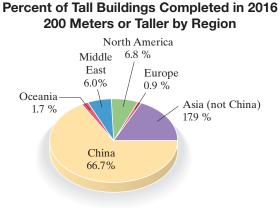
Temperatures

(9.2) The following circle graph shows a family's \$4000 monthly budget. Use this graph to answer Exercises 25 through 30. Write all ratios as fractions in simplest form.

- **25.** What is the largest budget item?
- **26.** What is the smallest budget item?
- **27.** How much money is budgeted for the mortgage payment and utilities?
- **28.** How much money is budgeted for savings and contributions?
- **29.** Find the ratio of the mortage payment to the total monthly budget.
- **30.** Find the ratio of food to the total monthly budget.

Food Car expenses \$700 \$500 Utilities \$250 Contributions \$300 Mortgage payment Miscellaneous \$975 bills \$475 Credit card bills Savings \$400 \$400

In 2016, there were approximately 117 buildings 200 meters or taller completed in the world. The following circle graph shows the percent of these buildings by region. Use this graph to answer Exercises 31 through 34. Round each answer to the nearest whole.



- **31.** How many completed tall buildings were located in China?
- **32.** How many completed tall buildings were located in the rest of Asia?
- **33.** How many completed tall buildings were located in Oceania?
- **34.** How many completed tall buildings were located in the Middle East?

Source: Council on Tall Buildings and Urban Habitats

(9.3) Find the mean, median, and any mode(s) for each list of numbers. If necessary, round to the nearest tenth.

35. 13, 23, 33, 14, 6

36. 45, 86, 21, 60, 86, 64, 45

37. 14,000, 20,000, 12,000, 20,000, 36,000, 45,000

38. 560, 620, 123, 400, 410, 300, 400, 780, 430, 450

For Exercises 39 and 40, the grades are given for a student for a particular semester. Find each grade point average. If necessary, round the grade point average to the nearest hundredth.

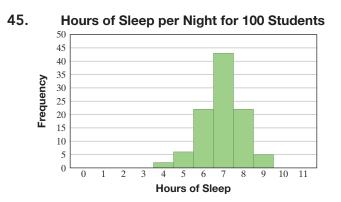
| 39. | Grade | Credit Hours |
|-----|-------|--------------|
| | А | 3 |
| | А | 3 |
| | С | 2 |
| | В | 3 |
| | С | 1 |

| 40. | Grade | Credit Hours |
|-----|-------|--------------|
| | В | 3 |
| | В | 4 |
| | С | 2 |
| | D | 2 |
| | В | 3 |

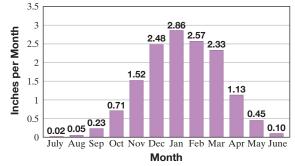
Find the range for each data set.

41. 4, 4, 4, 3, 3, 5, 6 **42.** 1, 1, 1, 8, 8





46. Monthly Average Precipitation for a City in California



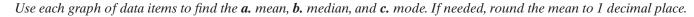
Use each frequency distribution table to find the **a**. mean, **b**. median, and **c**. mode. If needed, round the mean to 1 decimal place.

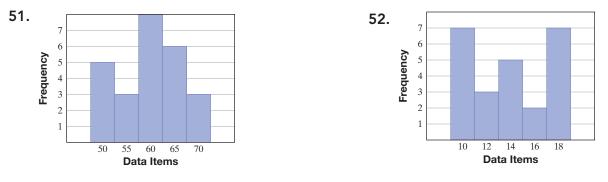
| Data Item | Frequency |
|-----------|----------------------|
| 60 | 2 |
| 61 | 10 |
| 62 | 5 |
| 63 | 11 |
| 64 | 3 |
| | 60
61
62
63 |

| Data Item | Frequency | |
|-----------|----------------------------|--|
| 11 | 5 | |
| 12 | 5 | |
| 13 | 3 | |
| 14 | 1 | |
| 16 | 3 | |
| 17 | 1 | |
| | 11
12
13
14
16 | |

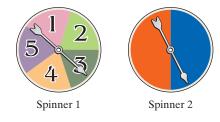
| 48. | Data Item | Frequency |
|-----|-----------|-----------|
| | 60 | 5 |
| | 61 | 7 |
| | 62 | 8 |
| | 63 | 10 |
| | 64 | 15 |
| | | |

| 50. | Data Item | Frequency | |
|-----|-----------|-----------|--|
| | 15 | 3 | |
| | 16 | 2 | |
| | 17 | 1 | |
| | 18 | 6 | |
| | 19 | 4 | |
| | 20 | 6 | |





(9.4) Draw a tree diagram for each experiment. Then use the diagram to determine the number of outcomes.



53. Tossing a coin and then spinning Spinner 1

54. Spinning Spinner 2 and then tossing a coin

55. Spinning Spinner 1 twice

56. Spinning Spinner 2 twice

57. Spinning Spinner 1 and then Spinner 2

Find the probability of each event.

| | 58. Rolling a 4 on a die | 59. Rolling a 3 on a die |
|-----|--|---|
| ••• | 60. Spinning a 4 on Spinner 1 | 61. Spinning a 3 on Spinner 1 |
| vie | 62. Spinning either a 1, 3, or 5 on Spinner 1 | 63. Spinning either a 2 or a 4 on Spinner 1 |
| | 64. Rolling an even number on a die | 65. Rolling a number greater than 3 on a die |

Mixed Review

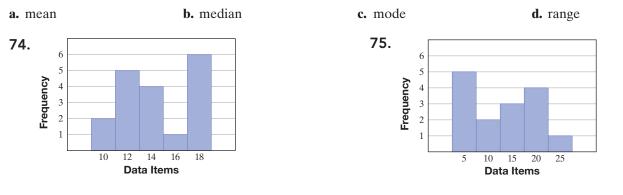
Find the mean, median, and any mode(s) for each list of numbers. If needed, round answers to two decimal places.

66. 73, 82, 95, 68, 54 **67.** 25, 27, 32, 98, 62 **68.** 750, 500, 427, 322, 500, 225 **69.** 952, 327, 566, 814, 327, 729

Given a bag containing 2 red marbles, 2 blue marbles, 3 yellow marbles, and 1 green marble, find the following:

- **70.** The probability of choosing a blue marble from the bag
- **71.** The probability of choosing a yellow marble from the bag
- **72.** The probability of choosing a red marble from the bag
- **73.** The probability of choosing a green marble from the bag

For each graph, calculate parts a.-d. Round the mean to two decimal places.



Getting Ready for the Test

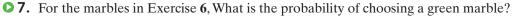
MULTIPLE CHOICE Exercises 1–13 are **Multiple Choice.** Choose the correct letter.

For Exercises 1 through 4, use the graph below.

Chapter 9

| | Bushels of O | ranges Picked | | |
|---|-------------------------------|--------------------------|---|--|
| Orchard 5 | | | | |
| Orchard 4 | | | | |
| Orchard 3 | | | | |
| Orchard 2 | | | | |
| Orchard 1 | | 4 thousand
bushels | | |
| ● 1. How many bushels of oranges di | d Orahard 1 produce? | | | |
| | 28 bushels | C. 28,000 bushels | | |
| 2. Which orchard above produced t | | | | |
| A. Orchard 1 B. | Orchard 2 | C. Orchard 5 | D. Orchards 2 and 5 produced the same. | |
| 03. How many bushels of oranges di | * | | | |
| A. 3 bushels B. | $2\frac{1}{2}$ bushels | C. 10 bushels | D. 10 thousand bushels | |
| • 4. How many more bushels did Ore | | ard 4? | | |
| A. 24 bushels B. | $6\frac{1}{2}$ bushels | C. 24,000 bushels | D. 6000 bushels | |
| For Exercises 5 through 7, choose the correct letter. | | | | |
| 5. Choose the degrees in the unknown | own sector of this circle gra | ph. | | |
| ?
90°
100°
100°
100° | | | | |
| A. 60° B. | 50° | C. 40° | D. 80° | |
| • 6. The five colored marbles are place a red marble? | ced in a bag. What is the pr | obability of choosing |) 🌑 🔮 🌑 🌑 | |
| A. $\frac{1}{5}$ B. | $\frac{2}{5}$ | C. $\frac{3}{5}$ | D. $\frac{4}{5}$ | |
| 0 7. For the marbles in Exercise 6. W | hat is the probability of cho | oosing a green marble? | | |

Bushels of Oranges Picked



For Exercises 8 through 10, choose the correct directions that lead to the given correct answer for the data set: 7, 9, 10, 13, 13

| A. Find the mean. | B. Find the median. | C. Find the mode. |
|--------------------------------------|--|---------------------------|
| 8 . answer: 10 | 9 . answer: 13 | ● 10. answer: 10.4 |
| For Exercises 11 through 13, use | e the data sets and choices below to answe | er. |
| A. data set: 10, 10, 10, 10, | 10 B. dat | a set: 6, 8, 10, 12, 14 |
| C. data set: 8, 9, 10, 11, 12 | D. the | y are the same |

● **11.** Which data set has the greatest range?

12. Which data set has the greatest median?

● **13.** Which data set has the greatest mean?

MATCHING Exercises 14 through 17 are Matching exercises.

Choose two data sets (*two letters*) *from the right column that make each statement in the left column true. Data sets may be used more than once or not at all.*

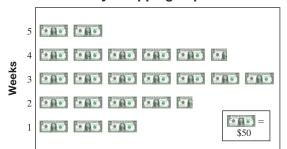
| 0 14. | equal means | А. | 10, 20, 30, 30, 40, 50 |
|--------------|-----------------------|----|------------------------|
| 0 15. | equal number of modes | B. | 9, 11, 11, 30, 48 |
| 0 16. | equal ranges | C. | 20, 25, 30, 35, 40 |
| 0 17. | equal medians | D. | 50, 55, 60, 65, 70 |

For additional practice go to your study plan in MyLab Math.

The following pictograph shows the money collected each week from a wrapping paper fundraiser. Use this graph to answer Exercises 1 through 3.

Weekly Wrapping Paper Sales

MyLab Math or You Tube



- 1. How much money was collected during the second week?
- During which week was the most money collected? How much money was collected during that week?

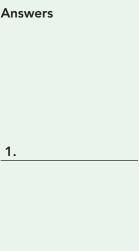
3. What was the total money collected for the fundraiser?

The bar graph shows the normal monthly precipitation in centimeters for Chicago, Illinois. Use this graph to answer Exercises 4 through 6.

Chicago Precipitation 11 10 9 8 7 Centimeters 6 5 4 3 2 1 0 D Ν S Ο J А T А Μ F Μ J Month

Source: U.S. National Oceanic and Atmospheric Administration, Climatography of the United States, No. 81

- 4. During which month(s) does Chicago normally have more than 9 centimeters of precipitation?
- **5.** During which month does Chicago normally have the least amount of precipitation? How much precipitation occurs during that month?



Chapter 9

Test

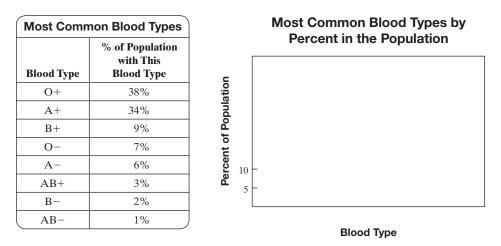
2.

3.

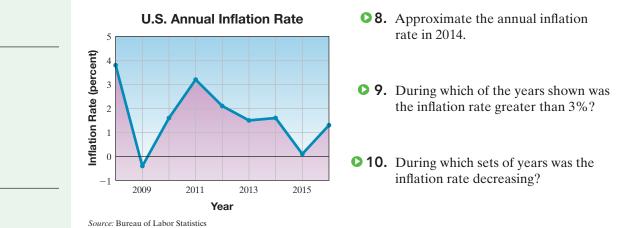
4.

6. During which month(s) does 7 centimeters of precipitation normally occur?

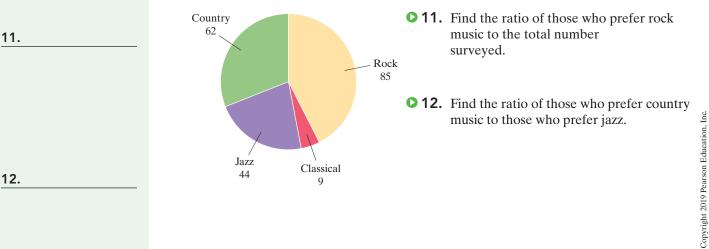
•7. Use the information in the table to draw a bar graph. Clearly label each bar.



The following line graph shows the annual inflation rate in the United States for the years 2008–2016. Use this graph to answer Exercises 8 through 10.



The result of a survey of 200 people is shown in the following circle graph. Each person was asked to tell his or her favorite type of music. Use this graph to answer Exercises 11 and 12.



642

6.

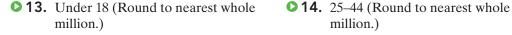
7.

8.

9.

The following circle graph shows the projected age distribution of the population of the United States in 2020. There are projected to be 335 million people in the United States in 2020. Use the graph to find how many people are expected to be in the age groups given.

> U.S. Population in 2020 by Age Groups 25-44 45-64 27% 25% 85 and over 2% 18–24 Under 18 9% 22% 65-84 15% Source: U.S. Census Bureau



A professor measures the heights of the students in her class. The results are shown in the following histogram. Use this histogram to answer Exercises 15 and 16.

Student Heights

5'8"-5'11"

Number of Students 4 2 5'0"-5'3" 5'4"-5'7" Heights ● **15.** How many students are 5'8''-5'11''

10

8

6

● **16.** How many students are 5'7" or shorter?

6'0"-6'3"

0 17. The history test scores of 25 students are shown below. Use these scores to complete the frequency distribution table.

| 70 | 86 | 81 | 65 | 92 | |
|----|----|----|----|----|--|
| 43 | 72 | 85 | 69 | 97 | |
| 82 | 51 | 75 | 50 | 68 | |
| 88 | 83 | 85 | 77 | 99 | |
| 77 | 63 | 59 | 84 | 90 | |
| | | | | | |

tall?

| Class Intervals
(Scores) | Tally | Class Frequency
(Number of Students) |
|-----------------------------|-------|---|
| 40–49 | | |
| 50–59 | | |
| 60–69 | | |
| 70–79 | | |
| 80–89 | | |
| 90–99 | | |

13.

14.

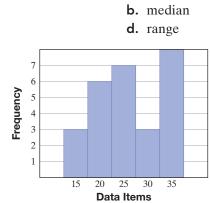
15.

16.

| 644 | Chapter 9 Reading Graphs and Introduction to Statistics and Probability |
|---------------|---|
| 18. | ● 18. Use the results of Exercise 17 to draw a histogram. |
| 19. | Number of Students |
| 20. | Scores |
| 20. | Find the mean, median, and mode of each list of numbers. 19. 26, 32, 42, 43, 49 20. 8, 10, 16, 16, 14, 12, 12, 13 |
| | Find the grade point average. If necessary, round to the nearest hundredth. |
| 22. | Carde Credit Hours |
| | A 3 B 3 C 3 B 4 |
| 23. | |
| <u>24. a.</u> | O 22. Given the data items:
10, 18, 13, 16, 13. Find the range. O 23. Use the data for Exercise 17 and find the range. |
| b | • 24. Use the frequency distribution table to find the following: Round the mean to |
| C | 1 decimal place. a. mean b. median c. mode d. range |
| | Data Item Frequency 90 3 91 1 92 2 |
| d | 92 2 93 8 94 8 |



- a. mean
- **c.** mode



26. Draw a tree diagram for the experiment of spinning the spinner twice. State the number of outcomes.



○27. Draw a tree diagram for the experiment of tossing a coin twice. State the number of outcomes.

- Suppose that the numbers 1 to 10 are each written on same-size pieces of paper and placed in a bag. You then select one piece of paper from the bag.
- **28.** What is the probability of choosing a **29.** What is the probability of choosing a 6 from the bag?
 - 3 or a 4 from the bag?

| 25. a.
b.
c. |
|--------------------|
| |
| |
| |
| |
| c. |
| c |
| c |
| <u>с.</u> |
| |
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| |
| d. |
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| |
| 26. |
| |
| |
| |
| 27. |
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| |
| 28. |
| |
| |
| |
| |
| 29. |
| |

| Chapters 1–9 | Cumulative Review | |
|-------------------------|---|---|
| Answers
1. | 1. Simplify: $(8-6)^2 + 2^3 \cdot 3$ | 2. Simplify: 48 ÷ 8 • 2 |
| 2.
3. | 3. Write in simplest form: $\frac{30}{108}$ | 4. Subtract: $\frac{19}{40} - \frac{3}{10}$ |
| <u>4.</u>
<u>5.</u> | 5. Add: $1\frac{4}{5} + 4 + 2\frac{1}{2}$ | 6. Multiply: $5\frac{1}{3} \cdot 2\frac{1}{8}$ |
| 6.
7.
8. | \triangle 7. The formula for finding the area of a triangle is Area = $\frac{1}{2} \cdot \text{base} \cdot \text{height}$.
Find the area of a triangle with height 3 feet and base length 5.6 feet. | 8. Find the perimeter of a rectangle with length $3\frac{1}{2}$ meters and width $1\frac{1}{2}$ meters. |
| <u>9.</u>
10.
11. | 9. Write the ratio of \$15 to \$10 as a fraction in simplest form. | 10. Write the ratio 14 inches to 3 feet as a fraction in simplest form. |
| 12.

13. | Write each rate as a fraction in simplest form.
11. \$2160 for 12 weeks | 12. 340 miles every 5 hours |
| <u>14.</u>
646 | 13. 360 miles on 16 gallons of gasoline | 14. 78 files every 4 hours |

| | Cumulative Review | 647 |
|----------------------|---|------------|
| | | 15. |
| 16. | Is $\frac{7.8}{3} = \frac{5.2}{2}$ a true proportion? | 16 |
| 18. | On a certain map, 2 inches represents | <u>17.</u> |
| | 75 miles. How many miles are repre-
sented by 7 inches? | <u>18.</u> |
| | | <u>19.</u> |
| | | 20. |
| 20. | 0.29% | 21. |
| 22. | 452% | 22. |
| | | 23. |
| ^{ı.}
24. | 27% | 24 |
| | | 25 |
| 26. | $61\frac{1}{7}\%$ | 26 |
| 28. | Translate to a proportion. | 27 |
| | 5 is what percent of 20? | 28 |
| 30. | A salesperson makes a 7% commission rate on her total sales. If her total sales | 29. |
| | are \$23,000, what is her commission? | 30 |
| 22 | | 31. |

31. An accountant invested \$2000 at a simple interest rate of 10% for 2 years. What total amount of money will she have from her investment in 2 years?

15. Is $\frac{1\frac{1}{6}}{10\frac{1}{2}} = \frac{\frac{1}{2}}{4\frac{1}{2}}$ a true proportion?

17. The standard dose of an antibiotic

is 4 cc (cubic centimeters) for every

rate, find the standard dose for a

140-lb woman.

19. 4.6%

21. 190%

23. 40%

25. $33\frac{1}{3}\%$

27. Translate to an equation.

5 is what percent of 20?

29. Find the sales tax and the total price

on the purchase of an \$85.50 atlas in a

city where the sales tax rate is 7.5%.

Write each percent as a decimal.

25 pounds (lb) of body weight. At this

Write each percent as a fraction in simplest form.

40, and 32.

32. Find the mean (or average) of 28, 35,

| 648 | Chapter 9 Reading Graphs and Introdu | ction to Statistics and Probability |
|---------------------------------|--|--|
| 33 | 33. Convert 7 feet to yards. | 34. Convert 2.5 tons to pounds. |
| <u>34.</u>
<u>35.</u> | 35. Divide 9 lb 6 oz by 2. | 36. Find: 1 + 3(10 - 8) |
| <u>36.</u>
<u>37.</u> | 37. Convert 2.35 cg to grams. | 38. Convert 106 cm to millimeters. |
| <u>38.</u>
<u>39.</u> | 39. Convert 3210 ml to liters. | 40. Convert 5 m to centimeters. |
| <u>40.</u>
<u>41.</u> | 41. Convert 15°C to degrees Fahrenheit. | 42. Convert 41°F to degrees Celsius. |
| <u>42.</u>
<u>43.</u> | 43. Find the complement of a 48° angle. | 44. Find the supplement of a 48° angle. |
| <u>44.</u>
<u>45.</u> | 45. Find: $\sqrt{\frac{1}{36}}$ | 46. Find: $\sqrt{\frac{1}{25}}$ |
| <u>46.</u>
<u>47.</u>
48. | 47. Find the mode of the list of numbers: 11, 14, 14, 16, 31, 56, 65, 77, 77, 78, 79 | 48. Find the median of the numbers in Exercise 47 . |
| 49.
50. | 49. If a coin is tossed twice, find the probability of tossing heads on the first toss and then heads again on the second toss. | 50. A bag contains 3 red marbles and 2 blue marbles. Find the probability of choosing a red marble. |

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Signed Numbers

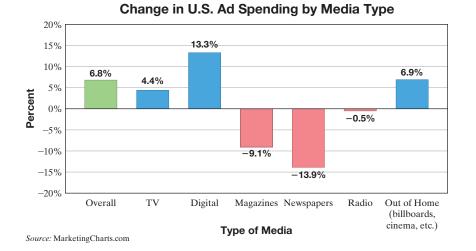


Where Do You See or Hear the Most Advertising?

o understand where the most money is spent in advertising, let's study the meaning of the bar graph below. The first bar shows the overall percent increase (6.8%) in money spent in the United States for advertising. If a bar drawn above the zero (0) horizontal axis is for percent increase, how do we denote a percent decrease? We do so by drawing a bar below the zero (0) axis.

Notice the different ad categories and think about how you personally see ads. Does it make sense that the amount of money companies spend on types of print ads is decreasing (bars below 0) while the amount of money spent on digital and TV and out-of-home ads is increasing.

Throughout this chapter, we study numbers less than zero, such as percent decrease, temperatures below zero, and altitudes below sea level. Thus, notice bar graphs will contain bars "below" zero.



10

Thus far, we have studied whole numbers, fractions, and decimals. However, these numbers are not sufficient for representing many situations in real life. For example, to express 5 degrees below zero or \$100 in debt, numbers less than 0 are needed. This chapter is devoted to signed numbers, which include numbers less than 0, and to operations on these numbers.

Sections

- **10.1** Signed Numbers
- **10.2** Adding Signed Numbers
- **10.3** Subtracting Signed Numbers

Integrated Review— Signed Numbers

- **10.4** Multiplying and Dividing Signed Numbers
- 10.5 Order of Operations

Check Your Progress

Vocabulary Check Chapter Highlights Chapter Review Getting Ready for the Test Chapter Test Cumulative Review

10.1 Signed Numbers

Objectives

- A Represent Real-Life Situations with Signed Numbers.
- B Graph Signed Numbers on a Number Line.
- C Compare Signed Numbers.
- D Find the Absolute Value of a Number.
- E Find the Opposite of a Number.
- F Read Bar Graphs Containing Signed Numbers.

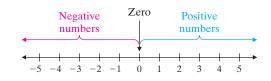
Objective 🗛 Representing Real-Life Situations 🜔

Thus far in this text, all numbers have been 0 or greater than 0. Numbers greater than 0 are called **positive numbers.** However, sometimes situations exist that cannot be represented by a number greater than 0. For example,



To represent these situations, we need numbers less than 0.

Extending the number line to the left of 0 allows us to picture negative numbers, which are numbers that are less than 0.



When a single + sign or no sign is in front of a number, the number is a positive number. When a single - sign is in front of a number, the number is a negative number. Together, we call positive numbers, negative numbers, and zero the **signed numbers**.

-5 indicates "negative five."

5 and +5 both indicate "positive five."

The number 0 is neither positive nor negative.

Now we have numbers to represent the situations previously mentioned.

5 degrees below $0-5^{\circ}$

20 feet below sea level -20 feet

Helpful Hint

A - sign, such as the one in -1, tells us that the number is to the left of 0 on a number line.

-1 is read "negative one."

A + sign or no sign tells us that a number lies to the right of 0 on a number line. For example, 3 and +3 both mean positive three.

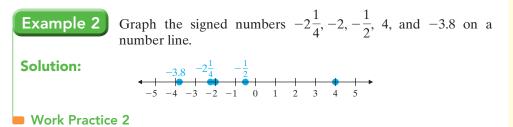
Example 1 Representing Depth with an Integer

The world's deepest cave is Krubera (or Voronja), in the country of Georgia, located by the Black Sea in Asia. It has been explored to a depth of 7208 feet below the surface of the Earth. Represent this position using a signed number. (*Source:* Speleogenesis.info)

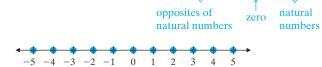
Solution: If 0 represents the surface of the Earth, then 7208 feet below the surface can be represented by -7208.

Work Practice 1

Objective **B** Graphing Signed Numbers 🕑



Some signed numbers are integers. The **integers** consist of 0, the natural numbers, and the opposites of the natural numbers. (A formal definition of opposites is given later in this section.) The integers are $\ldots, -3, -2, -1, 0, 1, 2, 3, \ldots$ and are graphed below.



In Example 2 above we graphed the signed numbers $-2\frac{1}{4}$, -2, $-\frac{1}{2}$, 4, -3.8. Of these signed numbers, -2 and 4 are integers; the rest are not integers.

Objective C Comparing Signed Numbers 🕗

For any two numbers graphed on a number line, recall that the number to the **right** is the **greater number**, and the number to the **left** is the **smaller number**. Also, recall that the symbol > means "is greater than" and the symbol < means "is less than."

To illustrate, both -5 and -2 are graphed on the number line shown:

-5 -4 -3 -2 -1 0 1 2 3 4 5

The graph of -5 is to the left of -2, so -5 is less than -2. We can write this as

-5 < -2

We can also write

-2 > -5

since -2 is to the right of -5, so -2 is greater than -5.

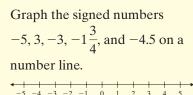
Concept Check Is there a smallest negative number? Is there a largest positive number? Explain.

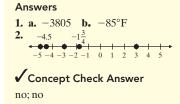
Practice 1

- a. The world's deepest bat colony spends each winter in a New York zinc mine at a depth of 3805 feet. Represent this position with a signed number. (Source: Guinness Book of World Records)
- **b.** The tamarack tree, a kind of larch, commonly grows at the edge of the arctic tundra and survives winter temperatures of 85 degrees below zero Fahrenheit. Represent this temperature with a signed number in degrees Fahrenheit.



Practice 2







Chapter 10 | Signed Numbers

Practice 3–9

Insert < or > between each pair of numbers to make a true statement.

3. 8 -8 **4.** -11 0 **5.** -15 -14 **6.** 3 -4.6 **7.** 0 -2 **8.** -7.9 7.9 **9.** $-\frac{3}{8}$ -1 $\frac{1}{7}$



Insert < or > between each pair of numbers to make a true statement.

| 3. -7 7 | -7 is to the left of 7, so $-7 < 7$. |
|---|---|
| 4. 0 -4 | 0 is to the right of -4 , so $0 > -4$. |
| 5. -9 -11 | -9 is to the right of -11 , so $-9 > -11$. |
| 6. −2.9 −1 | -2.9 is to the left of -1 , so $-2.9 < -1$. |
| 7. -6 0 | -6 is to the left of 0, so $-6 < 0$. |
| 8. 8.6 -8.6 | 8.6 is to the right of -8.6 , so $8.6 > -8.6$. |
| 9. $-1\frac{1}{4}$ $-2\frac{1}{2}$ | $-1\frac{1}{4}$ is to the right of $-2\frac{1}{2}$, so $-1\frac{1}{4} > -2\frac{1}{2}$. |
| Work Practice | 3–9 |

Helpful Hint

If you think of < and > as arrowheads, notice that in a true statement the arrow always points to the smaller number.

5 > -4 -3 < -1smaller smaller number number

Objective D Finding the Absolute Value of a Number 🕑

The **absolute value** of a number is the number's distance from 0 on a number line. The symbol for absolute value is $| \cdot |$. For example, |3| is read as "the absolute value of 3."

$$|3| = 3 \text{ because } 3 \text{ is } 3 \text{ units from } 0.$$

$$3 \text{ units}$$

$$-2 -1 \quad 0 \quad 1 \quad 2 \quad 3 \quad 4$$

$$|-3| = 3 \text{ because } -3 \text{ is } 3 \text{ units from } 0.$$

$$4 \text{ units}$$

$$-4 \text{ units}$$

Find each absolute value.

- **10.** |-2| = 2 because -2 is 2 units from 0. **11.** |5| = 5 because 5 is 5 units from 0. **12.** |0| = 0 because 0 is 0 units from 0. **13.** $\left|-\frac{3}{4}\right| = \frac{3}{4}$ because $-\frac{3}{4}$ is $\frac{3}{4}$ unit from 0.
- **14.** |1.2| = 1.2 because 1.2 is 1.2 units from 0.

Work Practice 10–14

Helpful Hint

Since the absolute value of a number is that number's *distance* from 0, the absolute value of a number is always 0 or positive. It is never negative.

$$|0| = 0$$
 $|-6| = 6$
zero a positive number

Practice 10–14 Find each absolute value.

10. |6| **11.** |-4| **12.** |0|**13.** $\left|\frac{7}{8}\right|$

14. |-3.4|

Answers 3. > 4. < 5. < 6. > 7. > 8. < 9. > 10. 6 11. 4 12. 0 13. $\frac{7}{8}$ 14. 3.4

Objective E Finding the Opposite of a Number 🕗

Two numbers that are the same distance from 0 on a number line but are on opposite sides of 0 are called **opposites.**

4 and -4 are opposites.
4 units 4 units

$$-5 - 4 -3 -2 -1 0 1 2 3 4 5$$

When two numbers are opposites, we say that each is the opposite of the other. Thus, **4** is the opposite of -4 and -4 is the opposite of 4.

The phrase "the opposite of" is written in symbols as "-". For example,

| the opposite of | 9 | is | -9 |
|-----------------|--------------|--------------|--------------|
| \downarrow | \downarrow | \downarrow | \downarrow |
| — | (9) | = | -9 |
| the opposite of | -3 | is | 3 |
| \downarrow | \downarrow | \downarrow | \downarrow |
| — | (-3) | = | 3 |

Notice we just stated that

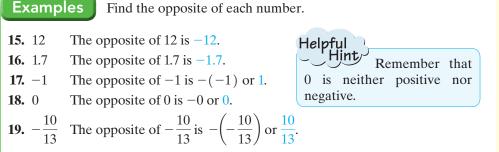
$$-(-3) = 3$$

In general, we have the following:

Opposites

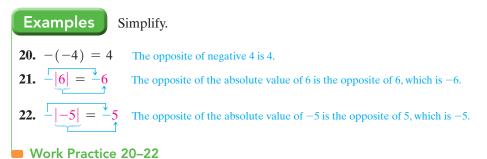
If *a* is a number, then -(-a) = a.

Notice that because "the opposite of" is written as "-", to find the opposite of a number we place a "-" sign in front of the number.



Work Practice 15–19

Concept Check True or false? The number 0 is the only number that is its own opposite.



Practice 15–19

Find the opposite of each number.

15.
$$-7$$
 16. 0
17. $\frac{11}{15}$ **18.** -9.6
19. 4

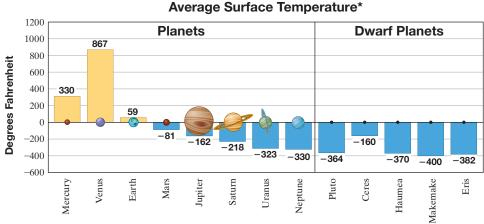
Practice 20–22 Simplify. **20.** −(−11) **21.** −|7| **22.** −|−2|

Answers 15. 7 16. 0 17. $-\frac{11}{15}$ 18. 9.6 19. -4 20. 11 21. -7 22. -2

Concept Check Answer true

Objective F Reading Bar Graphs Containing Signed Numbers >

The bar graph below shows the average temperature (in degrees Fahrenheit) of the eight planets and five dwarf planets. Notice that a negative temperature is illustrated by a bar below the horizontal line representing 0° F, and a positive temperature is illustrated by a bar above the horizontal line representing 0° F.



Source: The World Almanac and Internet research

* For some planets, the temperature given is the temperature where the atmospheric pressure equals 1 Earth atmosphere.



Which planet or dwarf planet has the lowest average temperature?

Solution: The planet with the lowest average temperature is the one that corresponds to the bar that extends the farthest in the negative direction (downward). The dwarf planet Makemake has the lowest average temperature of -400° F.

Work Practice 23

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Not all choices will be used.

| | opposites
inequality symbols
signed | absolute value
negative
integers | right
positive
is greater than | is less than
left | | |
|----|--|--|--------------------------------------|-----------------------|--|--|
| 1. | The numbers $\ldots -3, -2, -1, 0, 1, 2, 3, \ldots$ are called | | | | | |
| 2. | Positive numbers, negative numbers, and zero, together, are called numbers. | | | | | |
| 3. | The symbols "<" and ">" are called | | | | | |
| 4. | Numbers greater than 0 are called numbers while numbers less than 0 are called | | | | | |
| | numbers. | | | | | |
| 5. | The sign "<" means | | | | | |
| 6. | On a number line, the gre | eater number is to the | e0 | of the lesser number. | | |
| 7. | A number's distance from 0 on a number line is the number's | | | | | |

8. The numbers -5 and 5 are called _____

Practice 23

Which planet has the highest average temperature?

Answer 23. Venus

| Martin-Gay Interactive Videos | Watch the section lecture video and answer the following questions. | | | |
|-------------------------------|---|---|--|--|
| | - | In 🗏 Example 1, what application is used to represent a | | |
| | | negative number? | | |
| | - | In Example 2, the tick marks are labeled with what numbers on the number line? | | |
| | | From 🗏 Example 4 and our knowledge of a number line, | | |
| | | complete this statement: 0 will always be greater than any of | | |
| see Video 10.1 🍅 | | the numbers. | | |
| • | Objective D 12. | The absolute value of what other number has the same answer as that of \bowtie Example 6? | | |
| | Objective E 13. | Complete this statement based on the lecture after | | |
| | | Example 11: The of a positive number is a | | |
| | | negative number; the of a negative number is a positive number. | | |
| | | Complete this statement based on the lecture after | | |
| | | Example 11: The phrase "the opposite of" can be | | |
| | _ | represented by a(n) symbol. > | | |
| | - | In 🗮 Examples 14 and 15, what other lake has an elevation below sea level? | | |
| | | | | |

10.1 Exercise Set MyLab Math 🕗

Objective A *Represent each quantity by a signed number. See Example 1.*

- 1. A worker in a silver mine in Nevada works 1235 feet underground.
 - **3.** The peak of Mount Elbert in Colorado is 14,433 feet above sea level. (*Source:* U.S. Geological Survey)



- **5.** The record high temperature in Nevada is 125 degrees above zero Fahrenheit. (*Source:* National Climatic Data Center)
- **7.** The average depth of the Pacific Ocean is 13,215 feet below the surface of the ocean. (*Source:* Information Please Database)

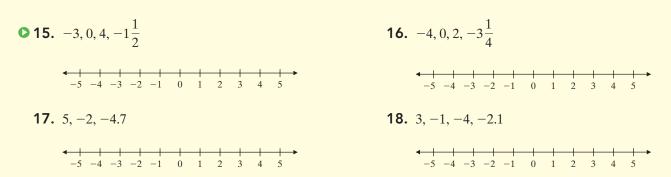
- **2.** A scuba diver is swimming 25 feet below the surface of the water in the Gulf of Mexico.
- **4.** The lowest elevation in the United States is found at Death Valley, California, at an elevation of 282 feet below sea level. (*Source:* U.S. Geological Survey)



- **6.** The record high temperature in Seattle, Washington, is 103 degrees above zero Fahrenheit. (*Source:* National Climatic Data Center)
- **8.** The average depth of the Atlantic Ocean is 12,880 feet below the surface of the ocean. (*Source:* Information Please Database)

- **9.** Uber lost \$1270 million in the first half of 2016. (*Source:* Bloomberg)
- **11.** The Moscow Subway system is well known for its ornate and fanciful underground stations. The average depth of the Moscow subway relative to the surface of the Earth is 276 feet. (*Source:* Moscow Metro)
- **13.** In 2015, the amount of money spent on print advertising decreased by 8 percent. (*Source:* Strategy Analytics)

- **10.** Yahoo reported a loss of \$4.4 billion in 2015. (*Source: USA Today*)
- **12.** Two divers are exploring the wreck of the *Andrea Doria*, south of Nantucket Island, Massachusetts. Guillermo is 160 feet below the surface of the ocean and Luigi is 147 feet below the surface. Represent each quantity by a signed number and determine who is deeper.
- **14.** In 2020, the amount of money spent on television advertising is predicted to decrease by 1 percent. (*Source:* Statista)



Objective B Graph the signed numbers in each list on a number line. See Example 2.

| Objective C <i>Insert</i> < <i>or</i> | > between each pair of nur | ibers to make a true statement. See | e Examples 3 through 9. |
|--|-----------------------------|--|--|
| 19. 5 7 | 20. 16 10 | 21. 4 0 | 22. 8 0 |
| ● 23. -5 -7 | 24. -12 -10 | ▶25. 0 -3 | 26. 0 -7 |
| 27. -4.6 -2.7 | 28. -8.4 -1.6 | 29. $-1\frac{3}{4}$ 0 | 30. 0 $-\frac{7}{8}$ |
| 31. $\frac{1}{4}$ $-\frac{8}{11}$ | 32. $-\frac{1}{5}$ 6 | 33. $-2\frac{1}{2}$ $-\frac{9}{10}$ | 34. $-1\frac{1}{5}$ $-3\frac{1}{9}$ |

Objective D *Find each absolute value. See Examples 10 through 14.*

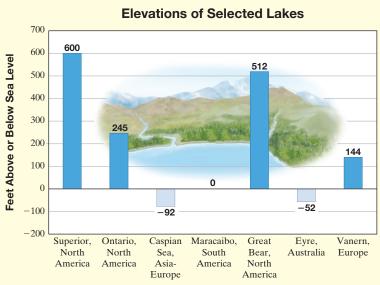
| 35. 9 | 36. 7 | ○ 37. -8 | 38. -19 | ○ 39. 0 | 40. 100 |
|--|---|-------------------|-------------------|--|--|
| 41. -5 | 42. -10 | ●43. -8.1 | 44. -31.6 | 45. $\left -\frac{1}{2}\right $ | 46. $\left \frac{9}{10}\right $ |
| 47. $\left -\frac{3}{8}\right $ | 48. $\left \frac{20}{23}\right $ | 49. 7.6 | 50. -0.6 | | |

| Objective E Find the opposite of each number. See Examples 15 through 19. | | | | | | | | | | | | |
|--|---------------------------|-----------------|-------------------|----------------------------|--------------------------|--|--|--|--|--|--|--|
| © 51. 5 | 52. 8 | ○53. -4 | 54. -6 | 55. 23.6 | 56. 123.9 | | | | | | | |
| ● 57. $-\frac{9}{16}$ | 58. $-\frac{4}{9}$ | 59. -0.7 | 60. -4.4 | 61. $\frac{17}{18}$ | 62. $\frac{2}{3}$ | | | | | | | |
| Simplify. See Ex | amples 20 through 22 | 2. | | | | | | | | | | |
| 63. -7 | 64. -11 | 65. - 20 | 66. - 43 | ○67. - -3 | 68. - -18 | | | | | | | |
| ○69. -(-8) | 70. -(-7) | 71. -14 | 72. -(-14) | 73. -(-29) | 74. - -29 | | | | | | | |

Objectives D E Mixed Practice *Fill in the charts. See Examples 10 through 19.*

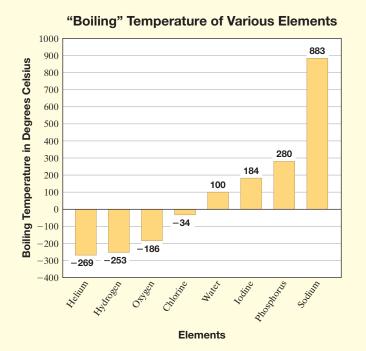
| | Number | Absolute Value
of Number | Opposite of
Number | | Number | Absolute Value
of Number | Opposite of
Number |
|-----|--------|-----------------------------|-----------------------|-----|--------|-----------------------------|-----------------------|
| 75. | 31 | | | 76. | -13 | | |
| 77. | | | 8.4 | 78. | | | $-\frac{11}{18}$ |

Objective F *The bar graph shows the elevations of selected lakes. Use this graph for Exercises 79 through 82 (Source: U.S. Geological Survey). See Example 23.*



- **○79.** Which lake shown has the lowest elevation?
 - **80.** Which lake has an elevation at sea level?
- 81. Which lake shown has the highest elevation?
 - **82.** Which lake shown has the second lowest elevation?

The following bar graph represents the boiling temperature, the temperature at which a substance changes from liquid to gas at standard atmospheric pressure. Use this graph to answer Exercises 83 through 86.



- **83.** Which element has a positive boiling temperature closest to that of water?
- **84.** Which element has the lowest boiling temperature?
- **85.** Which element has a boiling temperature closest to -200° C?
- **86.** Which element has an average boiling temperature closest to +300°C?

Review

Add. See Section 1.3.

| 87. 0 + 13 | 88. 9 + 0 | 89. 15 + 20 |
|--------------------|--------------------------|--------------------------|
| 90. 20 + 15 | 91. 47 + 236 + 77 | 92. 362 + 37 + 90 |

Concept Extensions

Write the given numbers in order from least to greatest.

93. 2^2 , -|3|, -(-5), -|-8|**94.** |10|, 2^3 , -|-5|, -(-4)**95.** |-1|, -|-6|, -(-6), -|1|**96.** 1^4 , -(-3), -|7|, |-20|**97.** -(-2), 5^2 , -10, -|-9|, |-12|**98.** 3^3 , -|-11|, -(-10), -4, -|2|

For Exercises 99 and 100, choose all numbers for x from each given list that make each statement true.

 99. |x| > 8 100. |x| > 4

 a. 0
 b. -5
 c. 8
 d. -12

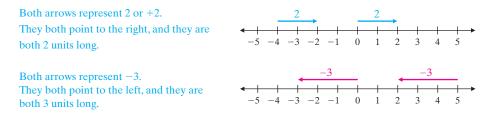
 101. Evaluate: -(-|-5|) 102. Evaluate: -(-|-(-7)|)

Answer true or false for Exercises 103 through 107.

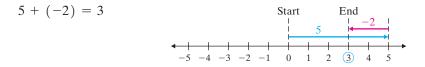
- **103.** If a > b, then a must be a positive number.
- **105.** A positive number is always greater than a negative number.
- **107.** The number -a is always a negative number. (*Hint:* Read "–" as "the opposite of.")
- **109.** Write in your own words how to find the absolute **110.** Explain how to determine which of two signed value of a signed number.
 - For Exercises 111 and 112, see the first Concept Check in this section.
 - **111.** Is there a largest negative number? If so, what is it?
 - **10.2** Adding Signed Numbers

Objective A Adding Signed Numbers 🕑

Adding signed numbers can be visualized by using a number line. A positive number can be represented on the number line by an arrow of appropriate length pointing to the right, and a negative number by an arrow of appropriate length pointing to the left.



To add signed numbers such as 5 + (-2) on a number line, we start at 0 on the number line and draw an arrow representing 5. From the tip of this arrow, we draw another arrow representing -2. The tip of the second arrow ends at their sum, 3.



To add -1 + (-4) on the number line, we start at 0 and draw an arrow representing -1. From the tip of this arrow, we draw another arrow representing -4. The tip of the second arrow ends at their sum, -5.

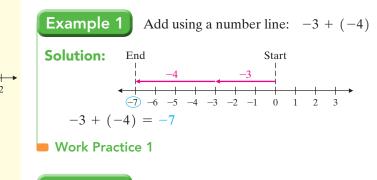
-1 + (-4) = -5End Start -4 -1 -1 -4 -1 -1 -4 -1

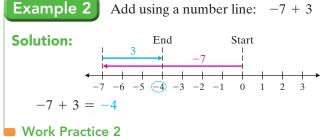
- **104.** The absolute value of a number is *always* a positive number.
- **106.** Zero is always less than a positive number.
- **108.** Given the number line, is it true that b < a?
- $\begin{array}{c|c} \bullet & \bullet & \bullet \\ a & b & -1 & 0 & 1 \end{array}$
- numbers is larger.
- **112.** Is there a smallest positive number? If so, what is it?

Objectives

- 🗛 Add Signed Numbers. >
- **B** Solve Problems by Adding Signed Numbers. D

Chapter 10 | Signed Numbers





Using a number line each time we add two numbers can be time consuming. Instead, we can notice patterns in the previous examples and write rules for adding signed numbers.

Rules for adding signed numbers depend on whether we are adding numbers with the same sign or different signs. When adding two numbers with the same sign, notice that the sign of the sum is the same as the sign of the addends.

Adding Two Numbers with the Same Sign

Step 1: Add their absolute values.

Step 2: Use their common sign as the sign of the sum.

-21)

Solution:

Practice 4–7

Add: (-3) + (-9)

Practice 3

Add.

4.
$$-12 + (-3)$$
 5. $9 +$
6. $-\frac{4}{15} + \left(-\frac{1}{15}\right)$
7. $-8.3 + (-5.7)$

5

Answers

1. End -5 + (-3) = -82. 3 (4) 5 + (-1) = 4**3.** -12 **4.** -15 **5.** 14 **6.** $-\frac{1}{3}$ **7.** -14

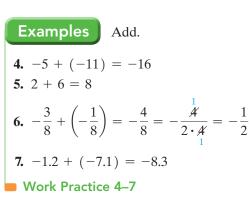
Example 3 Add:
$$-2 + (-1)$$

Step 1: |-2| = 2, |-21| = 21, and 2 + 21 = 23.

Step 2: Their common sign is negative, so the sum is negative:

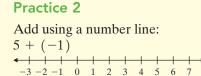
$$-2 + (-21) = -23$$

Work Practice 3



Practice 1

Add using a number line:



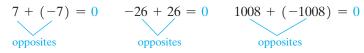
The rule for adding two numbers with different signs follows:

Adding Two Numbers with Different Signs **Step 1:** Find the larger absolute value minus the smaller absolute value. Step 2: Use the sign of the number with the larger absolute value as the sign of the sum. **Example 8** Add: -2 + 20Practice 8 Add: -3 + 9Solution: **Step 1:** |-2| = 2, |20| = 20, and 20 - 2 = 18. Step 2: 20 has the larger absolute value and its sign is an understood + so the sum is positive. -2 + 20 = +18 or 18 Work Practice 8 **Example 9** Add: 3 + (-7)Practice 9 Add: 2 + (-8)Solution: **Step 1:** |3| = 3, |-7| = 7, and 7 - 3 = 4. **Step 2:** -7 has the larger absolute value and its sign is - so the sum is negative. 3 + (-7) = -4Work Practice 9 Examples Add. Practice 10–13 Add. **10.** -18 + 10 = -8**10.** -46 + 20 **11.** 8.6 + (-6.2)**11.** 12.9 + (-8.6) = 4.3**12.** $-\frac{3}{4} + \frac{1}{8}$ **13.** -2 + 0

12. $-\frac{1}{2} + \frac{1}{6} = -\frac{3}{6} + \frac{1}{6} = -\frac{2}{6} = -\frac{1}{3}$ **13.** 0 + (-5) = -5 The sum of 0 and any number is the number.

Work Practice 10–13

Recall that numbers such as 7 and -7 are called opposites. In general, the sum of a number and its opposite is always 0.



If *a* is a number, then -a is its opposite. Also, a + (-a) = 0

$$\begin{array}{c} a + (-a) = 0 \\ -a + a = 0 \end{array}$$
 The sum of a number and its opposite is 0.

Answers 8. 6 9. -6 10. -26 11. 2.4 12. $-\frac{5}{8}$ 13. -2 Chapter 10 | Signed Numbers

Practice 14–15 Add. **14.** 18 + (-18) **15.** -64 + 64 **Examples** Add. **14.** -21 + 21 = 0 **15.** 36 + (-36) = 0**Work Practice 14–15**

Concept Check What is wrong with the following calculation?

5 + (-22) = 17

In the following examples, we add three or more signed numbers. Remember that by the associative and commutative properties for addition, we may add numbers in any order that we wish. In Examples 16 and 17, let's add the numbers from left to right.

Practice 16 Add: 6 + (-2) + (-15) Example 16 Add: (-3) + 4 + (-11)Solution: (-3) + 4 + (-11) = 1 + (-11)= -10Work Practice 16

Practice 17 Add: 5 + (-3) + 12 + (-14)

Helpful Hint Don't forget that addition is commutative and associative. In other words, numbers may be added in any order. Example 17 Add: 1 + (-10) + (-8) + 9Solution: 1 + (-10) + (-8) + 9 = -9 + (-8) + 9= -17 + 9= -8

The sum will be the same if we add the numbers in any order. To see this, let's add the positive numbers together and then the negative numbers together first.

1 + 9 = 10 Add the positive numbers. (-10) + (-8) = -18 Add the negative numbers. 10 + (-18) = -8 Add these results.

The sum is -8.

Work Practice 17

Objective B Solving Problems by Adding Signed Numbers

Next, we practice solving problems that require adding signed numbers.

Concept Check Answer 5 + (-22) = -17

14. 0 **15.** 0 **16.** -11 **17.** 0

Answers

Example 18 Calculating Temperature

In Philadelphia, Pennsylvania, the record extreme high temperature is 104°F. Decrease this temperature by 111 degrees, and the result is the record extreme low temperature. Find this temperature. (*Source:* National Climatic Data Center)

Solution:

In words: $\begin{array}{c} \text{extreme low} \\ \text{temperature} \end{array} = \begin{array}{c} \text{extreme high} \\ \text{temperature} \end{array} + \begin{array}{c} \text{decrease} \\ \text{of } 111^{\circ} \end{array}$ $\begin{array}{c} \downarrow \\ \text{temperature} \end{array} = \begin{array}{c} 104 \\ \text{temperature} \end{array} + \begin{array}{c} (-111) \\ \text{temperature} \end{array}$

The record extreme low temperature in Philadelphia, Pennsylvania, is -7°F.



Practice 18

If the temperature was -7° Fahrenheit at 6 a.m., and it rose 4 degrees by 7 a.m. and then rose another 7 degrees in the hour from 7 a.m. to 8 a.m., what was the temperature at 8 a.m.?



Answer 18. 4°F

Calculator Explorations Entering Negative Numbers

To enter a negative number on a calculator, find the key marked $\pm/-$. (Some calculators have a key marked <u>CHS</u> and some calculators have a special key (-) for entering a negative sign.) To enter the number -2, for example, press the keys $2 \pm/-$. The display will read <u>-2</u>. To find -32 + (-131), press the keys <u>32</u> \pm/ \pm <u>131</u> \pm/ \equiv or (-) <u>32</u> \pm (-) <u>131</u> <u>ENTER</u> The display will read <u>-163</u>. Thus -32 + (-131) = -163.

Use a calculator to perform each indicated operation.

1. -256 + 97 **2.** 811 + (-1058) **3.** 6(15) + (-46) **4.** -129 + 10(48) **5.** -108,650 + (-786,205)**6.** -196,662 + (-129,856)

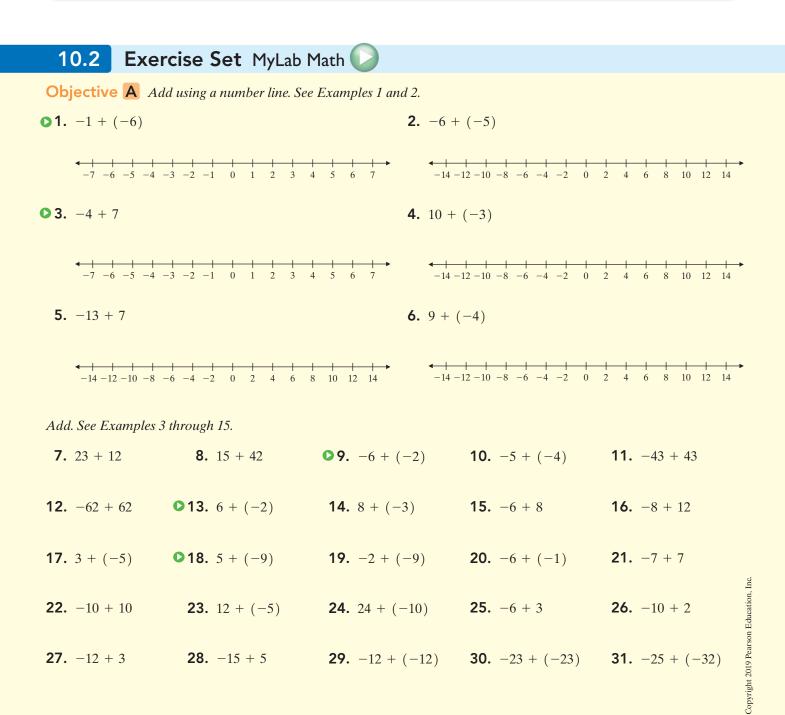
Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Not all choices will be used.

-a a 0 commutative associative

- **1.** If *n* is a number, then -n + n = _____.
- 2. Since x + n = n + x, we say that addition is _____.
- **3.** If *a* is a number, then -(-a) = _____.
- 4. Since n + (x + a) = (n + x) + a, we say that addition is _____.

| Martin-Gay Interactive Videos | Watch the section lecture video and answer the following questions. |
|-------------------------------|--|
| | Objective A 5. What is the sign of the sum in E Example 5 and why? |
| See Video 10.2 | Objective B 6. What does the answer to ⊨ Example 9, -231, mean in the context of the application? |



| 32. -45 + (-90) | 33. 56 + (-26) | 34. 89 + (-37) | 35. -37 + 57 | 36. -25 + 65 |
|---|--|---|-------------------------------|---|
| 37. -123 + (-100) | 38. -500 + (-230) | 39. -42 + 193 | 40. -64 + 164 | 41. -6.3 + (-2.2) |
| 42. -9.1 + (-4.6) | ● 43. -10.7 + 1 | 5.3 44. -19 | 0.6 + 23.1 | 45. $-\frac{7}{11} + \left(-\frac{1}{11}\right)$ |
| 46. $-\frac{9}{13} + \left(-\frac{1}{13}\right)$ | •47. $-\frac{2}{3} + \left(-\frac{2}{3} + \frac{2}{3}\right)$ | $(\frac{1}{6})$ 48. $-\frac{3}{8}$ | $+\left(-\frac{1}{4}\right)$ | 49. $-\frac{4}{5} + \frac{1}{10}$ |
| 50. $-\frac{9}{16} + \frac{3}{8}$ | 51. $-2\frac{1}{4} + 7\frac{7}{8}$ | 52. –4 | $\frac{1}{5} + 6\frac{9}{10}$ | |
| Add. See Examples 16 | and 17. | | | |
| ○53. -4 + 2 + (-5) | 54. | -1 + 5 + (-8) | 55. -5.2 | 2 + (-7.7) + (-11.7) |
| 56. -10.3 + (-3.2) | + (-2.7) 57. | 12 + (-4) + (-4) + 1 | 12 58. 18 + | (-9) + 5 + (-2) |
| 59. (-10) + 14 + 25 | 5 + (-16) | 60. 34 | + (-12) + (-11) + | - 213 |
| Objective B Tran | slating Solve. See Ex | ample 18. | | |
| 61. Find the sum of – | 8 and 25. | 62. Find | d the sum of -30 and | 10. |

- **63.** Find the sum of -31, -9, and 30.
- **65.** Suppose a deep-sea diver dives from the surface to 215 feet below the surface. He then dives down 16 more feet. Use positive and negative numbers (or 0) to represent this situation. Then find the diver's present depth.
- **62.** Find the sum of -30 and 10.
- **64.** Find the sum of -49, -2, and 40.
- **66.** Suppose a diver dives from the surface to 248 meters below the surface and then swims up 6 meters, down 17 meters, down another 24 meters, and then up 23 meters. Use positive and negative numbers (or 0) to represent this situation. Then find the diver's depth after these movements.

In some card games, it is possible to have positive and negative scores. The table shows the scores for two teams playing a series of four games. Use this table to answer Exercises 67 and 68.

| | Game 1 | Game 2 | Game 3 | Game 4 |
|--------|--------|--------|--------|--------|
| Team 1 | -2 | -13 | 20 | 2 |
| Team 2 | 5 | 11 | -7 | -3 |

- **67.** Find each team's total score after four games. If the winner is the team with the greater score, find the winning team.
- **68.** Find each team's total score after three games. If the winner is the team with the greater score, which team was winning after three games?

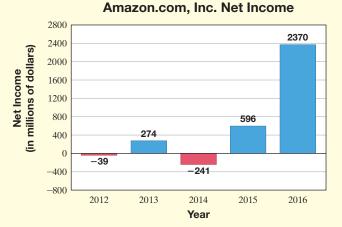
In golf, it is possible to have positive and negative scores. The following table shows the results of the eighteen-hole Round 4 for Jason Day and Daniel Summerhays at the 2016 PGA Championship at Baltusrol Golf Club in Springfield, New Jersey. Use the table to answer Exercises 69 through 72.

| Player/Hole | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
|-------------|----|---|----|----|----|---|---|---|----|----|----|----|----|----|----|----|----|----|
| Day | +1 | 0 | +1 | 0 | -1 | 0 | 0 | 0 | -1 | 0 | -1 | 0 | 0 | 0 | 0 | 0 | 0 | -2 |
| Summerhays | 0 | 0 | 0 | +1 | 0 | 0 | 0 | 0 | -1 | 0 | 0 | -1 | -1 | +1 | -1 | -1 | 0 | -1 |

- **69.** Find the total score for each of the athletes after playing the first 9 holes.
- **70.** Find the total score for each of the athletes over the last 9 holes.
- **71.** Find the total score for each of the athletes shown in Round 4.
- **72.** In golf, the lower score is the winner. Use the result of Exercise **71** to determine who won Round 4.

The following bar graph shows the yearly net income for Amazon.com, Inc. Net income is one indication of a company's health. It measures revenue (money taken in) minus cost (money spent). Use this graph to answer Exercises 73 through 76. (Source: Amazon.com, Inc.)

- **73.** What was the net income (in dollars) for Amazon.com, Inc. in 2012?
- **74.** What was the net income (in dollars) for Amazon.com, Inc. in 2014?
- **75.** Find the total net income for the years 2014 and 2015.
- **76.** Find the total net income for all the years shown.
- **77.** The temperature at 4 p.m. on February 2 was -10° Celsius. By 11 p.m. the temperature had risen 12 degrees. Find the temperature at 11 p.m.



78. In some card games, it is possible to have both positive and negative scores. After four rounds of play, Michelle had scores of 14, -5, -8, and 7. What was her total score for the game?

A small business company reports the following net incomes. Use this table to answer Exercises 79 and 80.

| Year | Net Income (in dollars) |
|------|-------------------------|
| 2013 | -\$10,412 |
| 2014 | -\$1786 |
| 2015 | \$15,395 |
| 2016 | \$31,418 |

- **79.** Find the sum of the net incomes for 2014 and 2015.
- **80.** Find the sum of the net incomes for all four years shown.

- **81.** The all-time record low temperature for Wisconsin is -55°F. West Virginia's all-time record low temperature is 8°F higher than Wisconsin's record low. What is West Virginia's record low temperature? (*Source:* National Climatic Data Center)
- **82.** The all-time record low temperature for Oklahoma is -27°F. In Georgia, the lowest temperature ever recorded is 10°F higher than Oklahoma's all-time low temperature. What is the all-time record low temperature for Georgia? (*Source:* National Climatic Data Center)
- **83.** The deepest spot in the Pacific Ocean is the Mariana Trench, which has an elevation of 10,924 meters below sea level. The bottom of the Pacific's Aleutian Trench has an elevation 3245 meters higher than that of the Mariana Trench. Use a negative number to represent the depth of the Aleutian Trench. (*Source:* Defense Mapping Agency)

Review

Subtract. See Sections 1.4 and 4.3.

85. 44 - 0 **86.** 91 - 0 **87.** 76.1 - 4.09 **88.** 93.7 - 10.08 **89.** 200 - 59 **90.** 400 - 18

Concept Extensions

Solve.

- **91.** Name two numbers whose sum is -17.
- **92.** Name two numbers whose sum is -30.

Each calculation below is incorrect. Find the error and correct it. See the Concept Check in this section.

| 93. 7 | $+(-10) \stackrel{?}{=} 17$ | 94. | $-4 + 14 \stackrel{?}{=} -18$ |
|--------------|------------------------------------|-----|----------------------------------|
| 95. – | $-10 + (-12) \stackrel{?}{=} -120$ | 96. | $-15 + (-17) \stackrel{?}{=} 32$ |

For Exercises 97 through 100, determine whether each statement is true or false.

- **97.** The sum of two negative numbers is always a negative number.
- **99.** The sum of a positive number and a negative number is always a negative number.
- **101.** In your own words, explain how to add two negative numbers.
- **98.** The sum of two positive numbers is always a positive number.
- **100.** The sum of zero and a negative number is always a negative number.
- **102.** In your own words, explain how to add a positive number and a negative number.



84. The deepest spot in the Atlantic Ocean is the Puerto Rico Trench, which has an elevation of 8605 meters below sea level. The bottom of the Atlantic's Cayman Trench has an elevation 1070 meters above the level of the Puerto Rico Trench. Use a negative number to represent the depth of the Cayman Trench. (*Source:* Defense Mapping Agency)

10.3 Subtracting Signed Numbers

In Section 10.1 we discussed the opposite of a number.

The opposite of 3 is -3. The opposite of -6.7 is 6.7.

Notice the pattern when we find the sum of these opposites.

3 + (-3) = 0 and -6.7 + 6.7 = 0

This pattern is always true. That is, the sum of a number and its opposite is always 0. Because of this, the opposite of a number is also called the **additive inverse** of a number. In this section, we use opposites (or additive inverses) to subtract signed numbers.

Objective A Subtracting Signed Numbers 💽

To subtract signed numbers, we write the subtraction problem as an addition problem. To see how we do this, study the examples below:

10 - 4 = 610 + (-4) = 6

Since both expressions simplify to 6, this means that

10 - 4 = 10 + (-4) = 6

Also,

3-2 = 3 + (-2) = 115-1 = 15 + (-1) = 14

Thus, to subtract two numbers, we add the first number to the opposite (also called the **additive inverse**) of the second number.

Subtracting Two Numbers

Examples Subtract

If a and b are numbers, then a - b = a + (-b).

| | | kampies | Subtr | act. | | | |
|------|----|--------------|--------------|-----------------|--------------|-------------------------------|---|
| 1 | | subtraction | = | first
number | + | opposite of the second number | |
| (-1) | | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | |
| | 1. | 8 - 5 | = | 8 | + | (-5) | = |
| | 2. | -4 - 10 | = | -4 | + | (-10) | = |
| | 3. | 6 - (-5) | = | 6 | + | 5 | = |
| | 4. | -11 - (-7) | = | -11 | + | 7 | = |
| | | | | | | | |

Work Practice 1–4

Answers 1. 5 2. -10 3. 25 4. -8

3. 11 - (-14) **4.** -9 - (

Practice 1–4 Subtract. **1.** 12 – 7

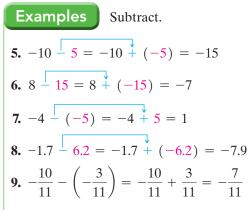
2. -6 - 4

Objectives

- A Subtract Signed Numbers.
- B Add and Subtract Signed Numbers.
- C Solve Problems by Subtracting Signed Numbers.

3 -14

> 11 -4



Work Practice 5–9

Helpful Hint

To visualize subtraction, try the following: The difference between 5°F and -2°F can be found by subtracting. That is, 5 - (-2) = 5 + 2 = 7

Can you visually see from the thermometer on the right that there are actually 7 degrees between $5^{\circ}F$ and $-2^{\circ}F$?



Concept Check What is wrong with the following calculation?

$$-7 - (-3) = -10$$

Example 10 Subtract 7 from –3.

Solution: To subtract 7 *from* -3, we find

$$-3 - 7 = -3 + (-7) = -10$$

Work Practice 10

Objective **B** Adding and Subtracting Signed Numbers 🕗

If a problem involves adding or subtracting more than two signed numbers, we rewrite differences as sums and add. Recall that by associative and commutative properties, we may add numbers in any order. In Examples 11 and 12, we will add from left to right.

Example 11 Simplify: 7 - 8 - (-5) - 1Solution: 7 - 8 - (-5) - 1 = 7 + (-8) + 5 + (-1)= -1 + 5 + (-1)= 4 + (-1)= 3

Work Practice 11

Practice 10 Subtract 5 from -10.

Practice 11 Simplify: -4 - 3 - 7 - (-5)

Answers 5. -4 6. -16 7. 5 8. -24.8 9. $-\frac{7}{13}$ 10. -15 11. -9 \checkmark Concept Check Answer -7 - (-3) = -4

Practice 5–9
Subtract.
5.
$$5 - 9$$
 6. $-12 - 4$
7. $-2 - (-7)$ 8. $-10.5 - 14.3$
9. $\frac{5}{13} - \frac{12}{13}$

Practice 12 Simplify: 3 + (-5) - 6 - (-4)

Practice 13

The highest point in Asia is the top of Mount Everest, at a height of 29,028 feet above sea level. The lowest point is the Dead Sea, which is 1312 feet below sea level. How much higher is Mount Everest than the Dead Sea? (*Source:* National Geographic Society) Chapter 10 | Signed Numbers

Example 12 Simplify:
$$7 + (-12) - 3 - (-8)$$

Solution:
 $7 + (-12) - 3 - (-8) = 7 + (-12) + (-3) + 8$
 $= -5 + (-3) + 8$
 $= -8 + 8$
 $= 0$

Work Practice 12

Objective C Solving Problems by Subtracting Signed Numbers (>>

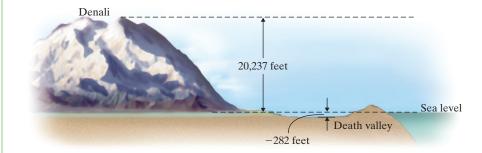
Solving problems often requires subtraction of signed numbers.

Example 13 Finding a Change in Elevation

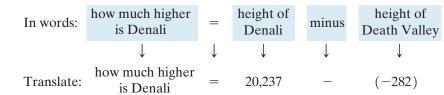
The highest point in the United States is the top of Denali, at a height of 20,237 feet above sea level. The lowest point is Death Valley, California, which is 282 feet below sea level. How much higher is Denali than Death Valley? (*Source:* U.S. Geological Survey)

Solution:

1. UNDERSTAND. Read and reread the problem. To find "how much higher," we subtract. Don't forget that since Death Valley is 282 feet *below* sea level, we represent its height by -282. Draw a diagram to help visualize the problem.



2. TRANSLATE.



3. SOLVE:

20,237 - (-282) = 20,237 + 282 = 20,519

4. INTERPRET. Check and state your conclusion: Denali is 20,519 feet higher than Death Valley.

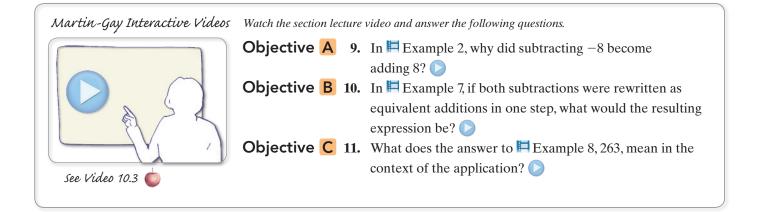
(Note: A new digital survey measured the elevation as 20,237 feet, somewhat lower than the 20,320 feet surveyed in 1952.)

Work Practice 13

Vocabulary, Readiness & Video Check

Multiple choice: Select the correct lettered response following each exercise.

| 1. It is true that <i>a</i> | -b = | | |
|------------------------------------|--------------------------|------------------------|---------------------|
| a. <i>b</i> – <i>a</i> | b. $a + (-b)$ | c. $a + b$ | |
| 2. The opposite o | of <i>n</i> is | | |
| a. - <i>n</i> | b. −(− <i>n</i>) | c. <i>n</i> | |
| 3. The expression | 1 - 10 - (-14) equals | ı | |
| a. 10 - 14 | b. −10 − 14 | c. $-14 - 10$ | d. −10 + 14 |
| 4. The expression | n -5 - 10 equals | | |
| a. 5 - 10 | b. 5 + 10 | c. $-5 + (-10)$ | d. 10 - 5 |
| Subtract. | | | |
| 5. 5 – 5 | 6. 7 – 7 | 7. 6.2 – 6.2 | 8. 1.9 – 1.9 |



10.3 Exercise Set MyLab Math 💭

Objective A Subtract. See Examples 1 through 9.

1. -5 - (-5) **2.** -6 - (-6) **3.** 8 - 3 **4.** 5 - 2 **5.** 3 - 8 **6.** 2 - 5 **7.** 7 - (-7) **8.** 12 - (-12) **9.** -5 - (-8) **10.** -25 - (-28) **9.** 11. -14 - 4 **12.** -2 - 42 **13.** 2 - 16 **14.** 8 - 9 **15.** 2.2 - 5.5 **16.** 1.7 - 6.3 **17.** 3.62 - (-0.4) **18.** 8.44 - (-0.2) **19.** $-\frac{3}{10} - \left(-\frac{7}{10}\right)$ **20.** $-\frac{2}{11} - \left(-\frac{5}{11}\right)$ **9.** $21. \frac{2}{5} - \frac{7}{10}$ **22.** $\frac{3}{16} - \frac{7}{8}$ **23.** $\frac{1}{2} - \left(-\frac{1}{3}\right)$ **24.** $\frac{1}{7} - \left(-\frac{1}{4}\right)$

| Translating Translate each phras | e, then simplify. See Example 10. | |
|--|-----------------------------------|--|
| 25. Subtract 18 from -20. | 26. Subtract 10 from -22. | 27. Find the difference of -20 and -3 . |
| 28. Find the difference of -8 and -13 . | ● 29. Subtract −11 from 2. | 30. Subtract -50 from -50. |

Mixed Practice (Sections 10.2 and 10.3) Add or subtract as indicated.

31. -21 + (-17) **32.** -35 + (-11) **33.** 9 - 20 **34.** 7 - 30 **35.** -4.9 - 7.8 **36.** -10.5 - 6.8 **37.** $\frac{4}{7} + \left(-\frac{1}{7}\right)$ **38.** $\frac{9}{13} + \left(-\frac{5}{13}\right)$

Objective B *Simplify. See Examples 11 and 12.*

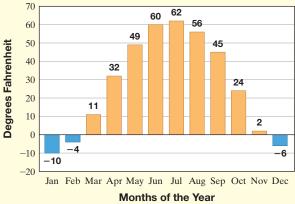
39. 7 - 3 - 2**40.** 8 - 4 - 1**41.** 12 - 5 - 7**42.** 30 - 7 - 12**43.** -5 - 8 - (-12)**44.** -10 - 6 - (-9)**45.** -10 + (-5) - 12**46.** -15 + (-8) - 4**47.** 12 - (-34) + (-6)**48.** 23 - (-17) + (-9)**49.** 19 - 14 + (-6) + (-50)**50.** 28 - 16 + (-14) + (-1)

Objective C *Solve. See Example 13.*

The bar graph below shows the monthly average temperature in Fairbanks, Alaska. Notice that a negative temperature is illustrated by a bar below the horizontal line representing 0°F. Use this graph to answer Exercises 51 through 54.

- **51.** Find the difference in temperature between the months of March and February.
- **52.** Find the difference in temperature between the months of November and December.
- **53.** Find the difference in temperature between the two months with the lowest temperatures.
- **54.** Find the difference in temperature between the month with the warmest temperature and the month with the coldest temperature.





● 55. The coldest temperature ever recorded on Earth was -129°F in Antarctica. The warmest temperature ever recorded was 134°F in Death Valley. How many degrees warmer is 134°F than -129°F? (Source: World Meteorological Organization) (Note: The former record of 136°F in the Sahara Desert has been disqualified.)

Solve.

- **57.** Aaron Aiken has \$125 in his checking account. He writes a check for \$117, makes a deposit of \$45, and then writes another check for \$69. Find the balance in his account. (Write the amount as a signed number.)
- 59. The temperature one morning is -4° Celsius at 6 a.m. If the temperature drops 3 degrees by 7 a.m., rises 4 degrees between 7 a.m. and 8 a.m., and then drops 7 degrees between 8 a.m. and 9 a.m., find the temperature at 9 a.m.

- **56.** The coldest temperature ever recorded in the United States was -80° F in Alaska. The warmest temperature ever recorded was 134°F in California. How many degrees warmer is 134°F than -80° F? (*Source: The World Almanac*)
- **58.** A woman received a statement of her charge account at Old Navy. She spent \$93 on purchases last month. She returned an \$18 top because she didn't like the color. She also returned a \$26 nightshirt because it was damaged. What does she actually owe on her account?
- **60.** Mauna Kea in Hawaii has an elevation of 13,796 feet above sea level. The Mid-America Trench in the Pacific Ocean has an elevation of 21,857 feet below sea level. Find the difference in elevation between those two points. (*Source:* National Geographic Society and Defense Mapping Agency)

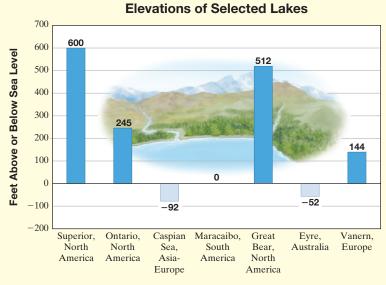
Some places on Earth lie below sea level, which is the average level of the surface of the oceans. Use this diagram to answer *Exercises 61 through 64. (Source:* Fantastic Book of Comparisons, *Russell Ash)*

- **61.** Find the difference in elevation between Death Valley and Qattâra Depression.
- **62.** Find the difference in elevation between the Danakil and Turfan Depressions.
- **63.** Find the difference in elevation between the two lowest elevations shown.
- **64.** Find the difference in elevation between the highest elevation shown and the lowest elevation shown.

Turfan Depression, Xinjiang, China: -505 ft Qattâra Depression, Egypt: -436 ft Poluostrov Mangyshlak, Kazakhstan: -433 ft Danakil Depression, Ethiopia: -384 ft Death Valley, US: -282 ft Salton Sea, US: -236 ft

The bar graph from Section 10.1 shows elevations of selected lakes. For Exercises 65 through 68, find the difference in elevation for the lakes listed. (Source: U.S. Geological Survey)

- **65.** Lake Superior and Lake Eyre
- 66. Great Bear Lake and Caspian Sea
- **67.** Lake Maracaibo and Lake Vanern
- **68.** Lake Eyre and Caspian Sea



Solve.

- **69.** The average surface temperature of the hottest planet, Venus, is 867° F, while the average surface temperature of the coldest planet, Neptune, is -330° F. Find the difference in temperatures.
- **70.** The average surface temperature of Mercury is 330° F, while the average surface temperature of Jupiter is -162° F. Find the difference in temperatures.

The difference between a country's exports and imports is called the country's trade balance.

- **71.** In March, 2017 the United States had \$191 billion in exports and \$235 billion in imports. What was the U.S. trade balance in March, 2017? (*Source:* U.S. Census Bureau)
- **72.** In 2016, the United States exported an average of 5190 thousand barrels of petroleum products per day and imported an average of 10,060 thousand barrels of petroleum products per day. What was the average U.S. trade balance for petroleum products per day in 2016? (*Source:* U.S. Energy Information Administration)

Review

Multiply. See Section 1.6.

| 73. 8.0 | 74. 0.8 | 75. 1 • 8 |
|----------------|-----------------------------------|--|
| 76. 8·1 | 77. $\frac{23}{\times 46}$ | 78. 51 <u>× 89</u> [−] |

Concept Extensions

Solve.

- **79.** Name two numbers whose difference is -3.
- **80.** Name two numbers whose difference is -10.

Each calculation below is incorrect. Find the error and correct it. See the Concept Check in this section.

81. $9 - (-7) \stackrel{?}{=} 2$ **82.** $-4 - 8 \stackrel{?}{=} 4$ **83.** $10 - 30 \stackrel{?}{=} 20$ **84.** $-3 - (-10) \stackrel{?}{=} -13$

Simplify. (Hint: Find the absolute values first.)

▶ 85. |-3| - |-7|
▶ 86. |-12| - |-5|
▶ 87. |-5| - |5|
▶ 88. |-8| - |8|
▶ 89. |-15| - |-29|
▶ 90. |-23| - |-42|

For Exercises 91 and 92, determine whether each statement is true or false.

- **91.** |-8-3| = 8-3
- **93.** In your own words, explain how to subtract one signed number from another.

92.
$$|-2 - (-6)| = |-2| - |-6|$$

94. A student explains to you that the first step to simplify $8 + 12 \cdot 5 - 100$ is to add 8 and 12. Is the student correct? Explain why or why not.

| | | Sections 10.1 | –10.3 | Integra | ated Review |
|----------------------|---|---|---------------------------|------------------------------|-------------|
| Signed Nu | mbers | | | | Answers |
| Represent each quan | tity by a signed number. | | | | |
| | lount Everest in Asia is ove sea level. (Source: | 2. The Mariana Tr
Ocean is estima | | | 2. |
| U.S. Geological | | below sea level
Almanac) | | | 3. |
| | | , | | | 4. |
| | le ever drilled in the in Russia and its depth | Surface of the earth | - | | 5. |
| | below sea level. | | an astronomity there a | | |
| Comparisons) | | | | | 6. |
| | | | Ove | r 7 miles | 7. |
| | | | | | 8. |
| | | | | | 9. |
| above sea level | 2 in Asia is 28,250 feet
. (<i>Source:</i> National | 5. Graph the signed given number li | | | 10. |
| Geographic So | ciety) | | | | |
| | | -5 -4 -3 -2 -1 | 0 1 2 3 | 4 5 | <u>11.</u> |
| | | | | | 12. |
| Insert < or > betwee | en each pair of numbers t | o make a true statemen | t. | | <u>13.</u> |
| 6. 0 -3 | 7. 7 0 | 8. $-1\frac{1}{2}$ $1\frac{1}{4}$ | 9. -2 | -7.6 | 14. |
| | | 2 4 | | | 15. |
| | | | 1 | 1 | |
| 10. -15 -5 | 11. -4 -40 | 12. 3.9 -3.9 | 13. $-\frac{1}{2}$ | $\frac{1}{2}$ $-\frac{1}{3}$ | <u>16.</u> |
| | | | | | 17. |
| Simplify. | | | | | 18. |
| 14. -1 | 15. 1 | 16. 0 | 17. – | -4 | <u>19.</u> |
| | | | | | 20. |
| 10 02 | 10 100.2 | 20. $-\left(-\frac{3}{4}\right)$ | 21 | 3 | 21. |
| 18. -8.6 | 19. 100.3 | 20. $-(-\frac{1}{4})$ | 21 | $-\frac{1}{4}$ | |

101

10.0

Intograted Poviow

| 676 | Chapter 10 Sig | gned Numbers | | |
|------------|--|--|-------------------|--|
| 22. | Find the opposite of ea | ch number. | | |
| 23. | 22. 6 | 23. -13 | 24. 89.1 | 25. $-\frac{2}{9}$ |
| | | | | |
| 25. | Add or subtract as indi | cated. | | |
| <u>26.</u> | 26. -7 + 12 | 27. -9.2 + | (-11.6) | 28. $\frac{5}{9} + \left(-\frac{1}{3}\right)$ |
| 27. | | | | 9 (3/ |
| 28. | | 3 (| 3) | |
| 29. | 29. 1 – 3 | 30. $\frac{3}{8} - \left(-\frac{3}{8}\right)^{\frac{3}{8}}$ | 8) | 31. -2.6 - 1.4 |
| 30. | | | | |
| 31. | 32. -7 + (-2.6) | 33. -14 + 8 | | 34. -8 - (-20) |
| 32. | 35. 18 - (-102) | | 36. 8.65 – | 12.00 |
| 33. | 33. 18 - (-102) | | 30. 8.03 - | 12.09 |
| 34. | 37. $-\frac{4}{5} - \frac{3}{10}$ | | 20 0 1 | (() + 20 |
| 35. | 37. $-\frac{1}{5} - \frac{1}{10}$ | | 38. -8 + | (-6) + 20 |
| 36. | 20 11 7 (10 | ~ | 10 | |
| 37. | 39. -11 - 7 - (-19 | ') | 40. –4 + | (-8) - 16 - (-9) |
| 38. | Translate each phrase, i | then simplify | | |
| 39. | 41. Subtract 26 from | | 42. Subtra | ct −8 from −12. |
| 40. | | | | |
| 41. | 43. Find the sum of – | -17 and -27. | 44. Add – | 3.6 and 2.1 |
| 42. | | | | |
| 43. | Solve. | | | |
| 44. | | 73°F in Ust'Shchugor, | in Asia | ildest temperature ever recorded \sim a was -90° F in Oimekon, Russia. |
| 45. | | Europe was 118°F in | cordec | armest temperature ever re-
l in Asia was 129°F in Tirat Tsvi, |
| 46. | warmer is 118°F t | How many degrees
han -73°F? (<i>Source:</i>
gical Organization) | 129°F | How many degrees warmer is
than -90°F? (<i>Source</i> : World
rological Organization) |
| | | 0 0) | | |

10.4 Multiplying and Dividing Signed Numbers

Multiplying and dividing signed numbers is similar to multiplying and dividing whole numbers. One difference is that we need to determine whether the result is a positive number or a negative number.

Objective A Multiplying Signed Numbers 🜔

Consider the following pattern of products:

First factor $3 \cdot 2 = 6$ decreases by 1 $2 \cdot 2 = 4$ each time. $1 \cdot 2 = 2$ $0 \cdot 2 = 0$ \checkmark Product decreases by 2 each time.

This pattern can be continued, as follows:

$$-1 \cdot 2 = -2$$
$$-2 \cdot 2 = -4$$
$$-3 \cdot 2 = -6$$

This suggests that the product of a negative number and a positive number is a negative number.

What is the sign of the product of two negative numbers? To find out, we form another pattern of products. Again, we decrease the first factor by 1 each time, but this time the second factor is negative.

$$2 \cdot (-3) = -6$$

$$1 \cdot (-3) = -3$$

$$0 \cdot (-3) = 0$$
Product increases by 3 each time.

This pattern continues as

 $-1 \cdot (-3) = 3$ $-2 \cdot (-3) = 6$ $-3 \cdot (-3) = 9$

This suggests that the product of two negative numbers is a positive number. Thus, we can determine the sign of a product when we know the signs of the factors.

Multiplying Numbers

The product of two numbers having the same sign is a positive number.

The product of two numbers having different signs is a negative number.

Product of Different Signs

(-)(+) = -(+)(-) = -

Product of Like Signs

$$(+)(+) = +$$

 $(-)(-) = +$

Multiply.

1.
$$-7 \cdot 3 = -21$$

2. $-2(-5) = 10$
3. $0 \cdot (-4) = 0$
4. $\left(-\frac{1}{2}\right)\left(-\frac{2}{3}\right) = \frac{1 \cdot \frac{1}{2}}{\frac{2}{3} \cdot 3} = \frac{1}{3}$
5. $-3(1.2) = -3.6$
Work Practice 1–5

Objectives

- A Multiply Signed Numbers.
- B Divide Signed Numbers. 🜔
- C Solve Problems by Multiplying and Dividing Signed Numbers.

Practice 1–5 Multiply. 1. $-2 \cdot 6$ 2. -4(-3)3. $0 \cdot (-10)$ 4. $\left(\frac{3}{7}\right)\left(-\frac{1}{3}\right)$ 5. -4(-3.2)Answers 1. -12 2. 12 3. 0 4. $-\frac{1}{7}$ 5. 12.8

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Recall that by the associative and commutative properties for multiplication, we may multiply numbers in any order that we wish. In Examples 6 and 7, we multiply from left to right.

Examples Multiply.
6.
$$7(-6)(-2) = -42(-2)$$

 $= 84$
7. $(-2)(-3)(-4) = 6(-4)$
 $= -24$
8. $(-1)(-2)(-3)(-4) = -1(-24)$ We have -24 from Example 7.
 $= 24$

Work Practice 6–8

Concept Check What is the sign of the product of five negative numbers? Explain.

Helpful Hint

| Have you noticed a pattern when multiplying signed numbers? |
|--|
| If we let $(-)$ represent a negative number and $(+)$ represent a positive |
| number, then |
| The product of an even number of negative numbers is a positive result.
(-)(-)(-) = (+) $(-)(-)(-)(-) = (+)$ $(-)(-)(-)(-)(-) = (+)$ $(-)(-)(-)(-)(-) = (-)$ The product of an odd number of negative numbers is a negative result. |

Recall from our study of exponents that $2^3 = 2 \cdot 2 \cdot 2 = 8$. We can now work with bases that are negative numbers. For example,

$$(-2)^3 = (-2)(-2)(-2) = -8$$

3 factors of -2

Example 9 Evaluate: $(-5)^2$

Solution: Remember that $(-5)^2$ means 2 factors of -5.

$$(-5)^2 = (-5)(-5) = 25$$

Work Practice 9

Notice in Example 9 the parentheses around -5 in $(-5)^2$. With these parentheses, -5 is the base that is squared. Without parentheses, such as -7^2 , only the 7 is squared, as shown next.

Example 10 Evaluate: -7^2

Solution: Remember that without parentheses, only the 7 is squared.

$$-7^2 = -(7 \cdot 7) = -49$$

Practice 6–8

Multiply. 6. 7(-2)(-4)7. (-5)(-6)(-1)8. (-2)(-5)(-6)(-1)

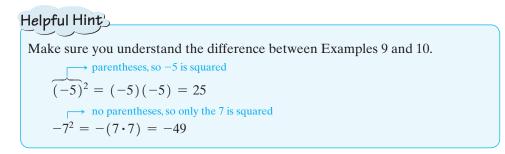
Practice 9 Evaluate: $(-3)^4$

Practice 10

Evaluate: -9^2

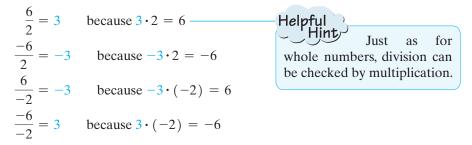
Answers **6.** 56 **7.** -30 **8.** 60 **9.** 81 **10.** -81

Concept Check Answer negative



Objective B Dividing Signed Numbers 🜔

Division of signed numbers is related to multiplication of signed numbers. The sign rules for division can be discovered by writing a related multiplication problem. For example,



Dividing Numbers

The quotient of two numbers having the same sign is a positive number.

The quotient of two numbers having different signs is a negative number.

Quotient of Like Signs

- $\frac{(+)}{(+)} = + \qquad \frac{(-)}{(-)} = +$
- Quotient of Different Signs

$$\frac{(+)}{(-)} = - \qquad \frac{(+)}{(+)} =$$

Divide.
11.
$$\frac{-12}{6} = -2$$

12. $-20 \div (-4) = 5$
13. $\frac{1.2}{-0.6} = -2$ 0.6) $\frac{2}{1.2}$
14. $\frac{7}{9} \div \left(-\frac{2}{5}\right) = \frac{7}{9} \cdot \left(-\frac{5}{2}\right) = -\frac{7 \cdot 5}{9 \cdot 2} = -\frac{35}{18} \text{ or } -1\frac{17}{18}$

Concept Check Find the error in the following computation:

$$\frac{1}{2} \div (-3) = \frac{1}{2} \cdot \frac{1}{3} = \frac{1}{6}$$

Practice 11–14 Divide. 11. $\frac{28}{-7}$ 12. -18 ÷ (-2) 13. $\frac{-4.6}{0.2}$ 14. $\frac{3}{5} \div \left(-\frac{2}{7}\right)$

Answers
11. -4 12. 9 13. -23
14.
$$-\frac{21}{10}$$
 or $-2\frac{1}{10}$
Concept Check Answer
 $\frac{1}{2} \div (-3) = \frac{1}{2} \cdot \left(-\frac{1}{3}\right) = -\frac{1}{6}$

Examples

Practice 15–16 Divide, if possible.

15.
$$\frac{-1}{0}$$
 16. $\frac{0}{-2}$

15. ⁰/₋₅ = 0 because 0 · -5 = 0
16. ⁻⁷/₀ is undefined because there is no number that gives a product of -7 when multiplied by 0

Work Practice 15–16

Let's take a moment and notice a pattern from earlier work in this section.

$$\frac{-6}{2} = -3$$
, $\frac{6}{-2} = -3$, and $-\frac{6}{2} = -3$

Divide, if possible.

Since $\frac{-6}{2}$, $\frac{6}{-2}$, and $-\frac{6}{2}$ all equal -3, then they must equal each other. Thus,

$$\frac{-6}{2} = \frac{6}{-2} = -\frac{6}{2}.$$

In general, this shows us three equivalent ways to write a negative fraction.

The fraction
$$-\frac{a}{b} = \frac{-a}{b} = \frac{a}{-b}$$

Concept Check Write $-\frac{4}{7}$ in two other equivalent ways.

Objective C Solving Problems by Multiplying and Dividing Signed Numbers >

Many real-life problems involve multiplication and division of signed numbers.

Example 17 Calculating a Total Golf Score

A professional golfer finished seven strokes under par (-7) for each of three days of a tournament. What was her total score for the tournament?

Solution:

- **1.** UNDERSTAND. Read and reread the problem. Although the key word is "total," since this is repeated addition of the same number, we multiply.
- 2. TRANSLATE.

| In words: | golfer's total score | = | number of days | • | score
each day |
|------------|----------------------|--------------|----------------|--------------|-------------------|
| | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| Translate: | golfer's
total | = | 3 | • | (-7) |

- **3.** SOLVE: $3 \cdot (-7) = -21$
- **4.** INTERPRET. Check and state your conclusion: The golfer's total score was -21, or 21 strokes under par.

Work Practice 17

Practice 17

A card player had a score of -13 for each of four games. Find the total score.



Answers 15. undefined 16. 0 17. -52

Concept Check Answer

 $\frac{-4}{7}, \frac{4}{-7}$

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Choices may be used more than once.

| negative | 0 |
|----------|-----------|
| positive | undefined |

- **1.** The product of a negative number and a positive number is a(n) _____ number.
- **2.** The product of two negative numbers is a(n) _____ number.
- **3.** The quotient of two negative numbers is a(n) _____ number.
- **4.** The quotient of a negative number and a positive number is a(n) _____ number.
- 5. The product of a negative number and zero is ______.
- **6.** The quotient of 0 and a negative number is _____.
- 7. The quotient of a negative number and 0 is _____.

Martin-Gay Interactive Videos
Watch the section lecture video and answer the following questions.
Objective A 8. When multiplying two signed numbers in Examples 1–5, what was done first?
Objective B 9. Complete this statement based on the lecture before Example 6: We can find out about sign rules for division because we know sign rules for ______.
Objective C 10. In Example 11, what phrase told us that the example will involve a negative number?

10.4 Exercise Set MyLab Math

Objective A *Multiply. See Examples 1 through 5.*

| 1. -2(-3) | 2. 5(-3) | ○3. -4(9) | 4. -7(-2) | 5. (2.6)(-1.2) |
|---------------------|------------------|------------------|---|--|
| 6. -0.3(5.6) | 7. 0(-14) | 8. -6(0) | 9. $-\frac{3}{5}\left(-\frac{2}{7}\right)$ | 10. $-\frac{3}{4}\left(\frac{9}{10}\right)$ |

Multiply. See Examples 6 through 8.

- **11.** 6(-4)(2) **12.** 8(-3)(3) **13.** -1(-2)(-4) **14.** -2(-5)(-4)
- **15.** -4(4)(-5) **16.** -2(3)(-7) **17.** 10(-5)(-1)(-3) **18.** 2(-1)(3)(-2)

| Evaluate. See Examples 9 and | <i>l 10</i> . | | |
|-------------------------------|------------------------------|---|--|
| ○19. (−2) ² | 20. (-2) ⁴ | 21. -5^2 | 22. -3^2 |
| ▶23. (-3) ³ | 24. (-1) ⁴ | 25. -2^3 | 26. -1^3 |
| 27. (-9) ² | 28. (-4) ³ | 29. $\left(-\frac{5}{11}\right)^2$ | 30. $\left(-\frac{3}{7}\right)^2$ |

Objective B Divide. See Examples 11 through 16.

9 31. $-24 \div 6$ **32.** $90 \div (-9)$ **33.** $\frac{-30}{6}$ **34.** $\frac{56}{-8}$ **935.** $\frac{-88}{-11}$ **36.** $\frac{-32}{4}$ **937.** $\frac{0}{14}$ **938.** $\frac{-13}{0}$ **39.** $\frac{39}{-3}$ **40.** $\frac{-24}{-12}$ **41.** $\frac{7.8}{-0.3}$ **42.** $\frac{1.21}{-1.1}$ **43.** $-\frac{5}{12} \div \left(-\frac{1}{5}\right)$ **44.** $-\frac{3}{8} \div \left(-\frac{2}{7}\right)$ **45.** $\frac{100}{-20}$ **46.** $\frac{240}{-40}$ **47.** $450 \div (-9)$ **48.** $480 \div (-8)$ **49.** $\frac{-12}{-4}$ **50.** $\frac{-36}{-3}$ **951.** $\frac{-120}{0.4}$ **52.** $\frac{-200}{2.5}$ **53.** $-\frac{8}{15} \div \frac{2}{3}$ **54.** $-\frac{1}{6} \div \frac{7}{18}$

Objectives A B Mixed Practice Perform the indicated operation. See Examples 1 through 16.

55. -12(0)**56.** 0(-100)**57.** (-5)^3**58.** (-3)^2**59.** $\frac{430}{-8.6}$ **60.** $\frac{-423}{4.7}$ **61.** -1(2)(7)(-3.1)**62.** -2(3)(5)(-6.2)**63.** $\frac{4}{3} \left(-\frac{8}{9}\right)$ **64.** $-\frac{1}{9}\left(-\frac{1}{3}\right)$ **65.** $\frac{4}{3} \div \left(-\frac{8}{9}\right)$ **66.** $-\frac{1}{9} \div \left(-\frac{1}{3}\right)$

Objective C Translating Translate each phrase, then simplify. See Example 17.

- **67.** Find the quotient of -54 and 9. **68.** Find the quotient of -63 and -3.
- **69.** Find the product of -42 and -6.

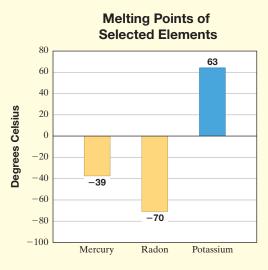
70. Find the product of -49 and 5.

Solve. See Example 17.

- 71. A football team lost four yards on each of three consecutive plays. Represent the total loss as a product of signed numbers and find the total loss.
 - **73.** A deep-sea diver must move up or down in the water in short steps in order to keep from getting a physical condition called the "bends." Suppose a diver moves down from the surface in five steps of 20 feet each. Represent his total movement as a product of signed numbers and find the product.
- **72.** Joe Norstrom lost \$400 on each of seven consecutive days in the stock market. Represent his total loss as a product of signed numbers and find his total loss.
- **74.** A weather forecaster predicts that the temperature will drop five degrees each hour for the next six hours. Represent this drop as a product of signed numbers and find the total drop in temperature.

The graph shows melting points in degrees Celsius of selected elements. Use this graph to answer Exercises 75 through 78.

- **75.** The melting point of nitrogen is 3 times the melting point of radon. Find the melting point of nitrogen.
- **76.** The melting point of rubidium is -1 times the melting point of mercury. Find the melting point of rubidium.
- **77.** The melting point of argon is -3 times the melting point of potassium. Find the melting point of argon.
- **78.** The melting point of strontium is -11 times the melting point of radon. Find the melting point of strontium.
- **79.** For the second quarter of 2016, Sears Holding Corporation posted a loss of \$396 million due to a decline in sales. If this trend were consistent for each month of the quarter, how much would you expect this loss to have been for each month? (*Source:* Sears Holdings Corporation)
- **81.** In 2012 there were 6533 analog (non-digital) U.S. movie screens. In 2016, this number of screens dropped to 869 (*Source:* Motion Picture Association of America)
 - **a.** Find the change in the number of U.S. analog screens from 2012 to 2016.
 - **b.** Find the average change per year in the number of analog movie screens over this period.



- **80.** From 2003 through 2015, the estimated population of mourning doves in the United States dropped by 73,023,000 birds. If the loss in birds were evenly spaced over these years, by how many birds would you expect the population to drop each year? (*Source:* U.S. Fish and Wildlife Service)
- **82.** In 1987, the California condor was all but extinct in the wild, with about 30 condors in the world. The U.S. Fish and Wildlife Service captured the condors in the wild in an aggressive move to rebuild the population by breeding them in captivity and releasing the chicks into the wild. The condor population increased to approximately 436 by 2016. (*Source:* U.S. Fish and Wildlife Service)
 - **a.** Find the change in the number of California condors from 1987 to 2016.
 - **b.** Find the average change per year in the California condor population over the period in part **a**.

Review

Perform each indicated operation. See Section 1.9.

| 83. (11 - 8) · (200 - 100) | 84. (2·3) ² | 85. (3·5) ² |
|-----------------------------------|-------------------------------|--|
| 86. (12 − 3) • (18 − 10) | 87. 90 + $12^2 - 5^3$ | 88. $3 \cdot (7 - 4) + 2 \cdot 5^2$ |
| 89. 12 ÷ 4 – 2 + 7 | 90. 12 ÷ (4 − 2) + 7 | |

Concept Extensions

| Mixed Practice (Sections 10.2, 10.3, and 10.4) Perform the indicated of |
|---|
|---|

| 91. -87 ÷ 3 | 92. -9(-10) | 93. -9 - 10 |
|---------------------------|----------------------------|-----------------------|
| 94. -4 + (-3) + 21 | 95. -4 - 15 - (-11) | 96. -16 - (-2) |

In Exercises 97 through 100, determine whether each statement is true or false.

97. The product of two negative numbers is always a negative number.
98. The product of a positive number and a negative number is always a negative number.
99. The quotient of two negative numbers is always a positive number.
100. The quotient of zero and a negative number is always zero.

Solve. See the first Concept Check in this section.

- **101.** What is the sign of the product of seven negative numbers?
- **102.** What is the sign of the product of ten negative numbers?

For Exercises 103 and 104, write the fractions in two other equivalent ways by different placements of the negative sign. See the third Concept Check in this section.

103.
$$-\frac{20}{41}$$
 104. $-\frac{8}{17}$

Without actually finding the product, write the list of numbers in Exercises 105 and 106 in order from least to greatest. For help, see a Helpful Hint box in this section.

105.
$$(-2)^{12}$$
, $(-2)^{17}$, $(-5)^{12}$, $(-5)^{17}$

- **107.** In your own words, explain how to divide two signed numbers.
- **106.** $(-1)^{50}$, $(-1)^{55}$, 0^{15} , $(-7)^{20}$, $(-7)^{23}$
- **108.** In your own words, explain how to multiply two signed numbers.

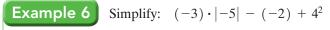
10.5 Order of Operations Objective A Simplifying Expressions 🕗 **Objectives** We first discussed the order of operations in Chapter 1. In this section, you are given an A Simplify Expressions by Using opportunity to practice using the order of operations when expressions contain signed the Order of Operations. 🕟 numbers. The rules for the order of operations from Section 1.9 are repeated here. **B** Find the Average of a List of Numbers. > **Order of Operations** 1. Perform all operations within parentheses (), brackets [], or other grouping symbols such as square roots or fraction bars. 2. Evaluate any expressions with exponents. 3. Multiply or divide in order from left to right. 4. Add or subtract in order from left to right. **Example 1** Simplify: $60 + 30 + (-2)^3$ Practice 1 **Solution:** $60 + 30 + (-2)^3 = 60 + 30 + (-8)$ Write $(-2)^3$ as -8. Simplify: $20 + 50 + (-4)^3$ = 90 + (-8)Add from left to right. = 82Work Practice 1 **Example 2** Simplify: $\frac{-6(2)}{-3}$ Practice 2 Simplify: $\frac{25}{5(-1)}$ **Solution:** First we multiply –6 and 2. Then we divide. $\frac{-6(2)}{-3} = \frac{-12}{-3}$ = 4Work Practice 2 **Example 3** Simplify: $\frac{12 - 16}{-1 + 3}$ Practice 3 Simplify: $\frac{-18 + 6}{-3 - 1}$ **Solution:** We simplify above and below the fraction bar separately. Then we divide. $\frac{12-16}{-1+3} = \frac{-4}{2}$ = -2Work Practice 3 **Example 4** Simplify: $-4^2 + (-3)^2 - 1^3$ Practice 4 Simplify: $-2^3 + (-4)^2 + 1^5$ Solution: $-4^{2} + (-3)^{2} - 1^{3} = -16 + 9 - 1$ Simplify expressions with exponents. = -7 - 1 Add or subtract from left to right. = -8Answers **1.** 6 **2.** -5 **3.** 3 **4.** 9 Work Practice 4

Chapter 10 | Signed Numbers

Practice 5 Simplify: $2(2-8) + (-12) - \sqrt{9}$

Solution: $3(4-7) + (-2) - \sqrt{25} = 3(-3) + (-2) - 5$ Simplify inside parentheses and replace $\sqrt{25}$ with 5. = -9 + (-2) - 5Multiply. = -11 - 5Add or subtract from left to right. = -16

Work Practice 5



Example 5 Simplify: $3(4-7) + (-2) - \sqrt{25}$

Solution:

$$(-3) \cdot |-5| - (-2) + 4^2 = (-3) \cdot 5 - (-2) + 4^2 \quad \text{Write } |-5| \text{ as } 5.$$

= (-3) \cdot 5 - (-2) + 16 Write 4² as 16.
= -15 - (-2) + 16 Multiply.
= -13 + 16 Add or subtract from left to right.
= 3

Work Practice 6

Example 7

le 7 Simplify: -2[-3 + 2(-1 + 6)] - 5.3

Solution: Here we begin with the innermost set of parentheses.

$$-2[-3 + 2(-1 + 6)] - 5.3 = -2[-3 + 2(5)] - 5.3 \quad \text{Write } -1 + 6 \text{ as } 5.$$

$$= -2[-3 + 10] - 5.3 \qquad \text{Multiply.}$$

$$= -2(7) - 5.3 \qquad \text{Add.}$$

$$= -14 - 5.3 \qquad \text{Multiply.}$$

$$= -19.3 \qquad \text{Subtract.}$$

Work Practice 7

Concept Check True or false? Explain your answer. The result of -4(3-7) - 8(9-6)

is positive because there are four negative signs.

Example 8 Simplify: $\left(\frac{1}{6} - \frac{5}{6}\right) \cdot \frac{3}{7}$ Solution: $\left(\frac{1}{6} - \frac{5}{6}\right) \cdot \frac{3}{7} = -\frac{2}{3} \cdot \frac{3}{7} \quad \frac{1}{6} - \frac{5}{6} = -\frac{4}{6} = -\frac{2}{3}$ $= -\frac{2 \cdot \frac{3}{7}}{\frac{3}{7} \cdot 7}$ Multiply. $= -\frac{2}{7}$ Simplify.

Practice 8 Simplify: $\frac{5}{8} \div \left(\frac{1}{4} - \frac{3}{4}\right)$

Answers 5. -27 **6.** -15 **7.** -39.9 **8.** $-\frac{5}{4}$

Concept Check Answer false; -4(3-7) - 8(9-6) = -8

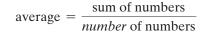
Work Practice 8

Practice 6 Simplify: $(-5) \cdot |-4| + (-3) + 2^3$

Practice 7 Simplify: -4[-2 + 5(-3 + 5)] - 7.9

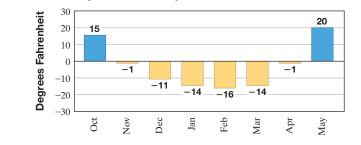
Objective **B** Review Finding Averages 🕑

Recall from Chapter 1 that the average of a list of numbers is



Example 9 The graph shows some monthly normal temperatures for Barrow, Alaska. Use this graph to find the average of the temperatures for the months January through May.

Monthly Normal Temperatures for Barrow, Alaska



Practice 9

Find the average of the temperatures for the months October through April.



| average = | $\frac{-14 + (-16) + (-14) + (-1) + 20}{5}$ | There are 5 months from January through May. |
|----------------|---|--|
| = | $\frac{-25}{5}$ | |
| = | -5 | |
| The average of | the temperatures is -5° F. | |
| Work Practic | e 9 | |



Calculator Explorations Simplifying an Expression Containing a Fraction Bar

Recall that even though most calculators follow the order of operations, parentheses must sometimes be inserted. For example, to simplify $\frac{-8+6}{-2}$ on a calculator, enter parentheses about the expression above the fraction bar so that it is simplified separately.

To simplify
$$\frac{-8+6}{-2}$$
, press the keys

$$(8 + / - + 6) \div 2 + / - = or$$

$$((-) 8 + 6) \div (-) 2 ENTER.$$

The display will read $\boxed{1}$.

Thus,
$$\frac{-8+6}{-2} = 1$$

Use a calculator to simplify.

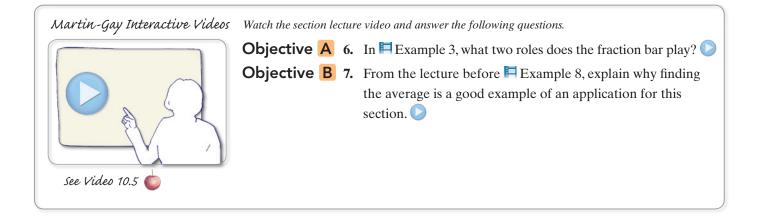
1.
$$\frac{-120 - 360}{-10}$$

2. $\frac{4750}{-2 + (-17)}$
3. $\frac{-316 + (-458)}{28 + (-25)}$
4. $\frac{-234 + 86}{-18 + 16}$

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank.

| | average addition | subtraction
multiplication | division |
|----|------------------|--|--|
| 1. | To simplify -2 | $2 \div 2 \cdot (3)$, which op | eration should be performed first? |
| 2. | To simplify –9 | $\theta - 3 \cdot 4$, which operation | ation should be performed first? |
| 3. | The | of a list of nu | mbers is $\frac{\text{sum of numbers}}{number \text{ of numbers}}$. |
| 4. | To simplify 5[- | $-9 + (-3)] \div 4$, wh | ich operation should be performed first? |
| 5. | To simplify -2 | $2 + 3(10 - 12) \cdot (-3)$ | 8), which operation should be performed first? |
| | ~ - | | |



10.5 Exercise Set MyLab Math 💽

Objective A *Simplify. See Examples 1 through 8.*

| ○1. -1(-2) + 1 | 2. $3 + (-8) \div 2$ | 3. $\frac{-8(-5)}{10}$ | 4. $\frac{-9(-6)}{18}$ |
|---|--|-------------------------------------|-------------------------------------|
| 5. 9 - 12 - 4 | 6. 10 - 23 - 12 | 7. 4 + 3(-6) | 8. 8 + 4(-3) |
| 9. $\frac{4}{9}\left(\frac{2}{10}-\frac{7}{10}\right)$ | 10. $\frac{2}{5}\left(\frac{3}{8}-\frac{4}{8}\right)$ | 11. -10 + 4 ÷ 2 | 12. -12 + 6 ÷ 3 |
| 13. $25 \div (-5) + \sqrt{81}$ | 14. $28 \div (-7) + \sqrt{25}$ | 15. $\frac{- -5 +3}{7-9}$ | 16. $\frac{- -11 +7}{7-9}$ |
| • 17. $\frac{24}{10 + (-4)}$ | 18. $\frac{88}{-8-3}$ | 19. 5(-3) - (-12) | 20. 7(-4) - (-6) |
| 21. -19 - 12(3) | 22. -24 - 14(2) | 23. $\frac{-23+7}{14+(-10)}$ | 24. $\frac{-27+6}{13+(-10)}$ |

25.
$$[8 + (-4)]^2$$
 26. $[9 + (-2)]^3$ 027. $3^3 - 12$ 28. $5^2 - 100$
29. $(3 - 12) + 3$ 30. $(12 - 19) + 7$ 31. $5 + 2^3 - 4^3$ 32. $12 + 5^3 - 2^4$
33. $(5 - 9)^2 + (4 - 2)^2$ 34. $(2 - 7)^2 + (4 - 3)^4$ 035. $[8 - 24] \cdot (-2) + (-2)$
36. $[3 - 15] \cdot (-4) + (-16)$ 37. $(-12 - 20) + 16 - 25$ 38. $(-20 - 5) + 5 - 15$
39. $5(5 - 2) + (-5)^2 - \sqrt{36}$ 40. $3(8 - 3) + (-4)^2 - \sqrt{100}$ 41. $(02 - 0.7)(0.6 - 1.9)$
42. $(0.4 - 1.2)(0.8 - 1.7)$ 043. $2 - 7 \cdot 6 - 19$ 44. $4 - 12 \cdot 8 - 17$
45. $(-36 + 6) - (4 + 4)$ 46. $(-4 + 4) - (8 + 8)$ 47. $(\frac{1}{2})^2 - (\frac{1}{3})^2$
48. $(\frac{1}{4})^2 - (\frac{1}{2})^2$ 49. $(-5)^2 - 6^3$ 50. $(-4)^4 - 5^4$
51. $(10 - 4^2)^2$ 52. $(11 - 3^2)^3$ 53. $2(8 - 10)^2 - 5(1 - 6)^2$
54. $-3(4 - 8)^2 + 5(14 - 16)^3$ 55. $3(-10) + [5(-3) - 7(-2)]$ 56. $12 - [7 - (3 - 6)] + (2 - 3)^5$
60. $(1.3)^2 - (22)^2$ 61. $-3^2 + (-2)^3 - 4^2$ 62. $-4^2 + (-3)^2 - 2^2$
 $[8 - 13] + \sqrt{81}$ $[10 - 6] + \sqrt{36}$

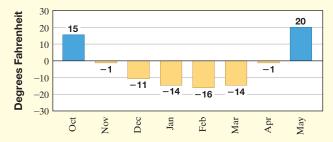
63.
$$\frac{|0|}{-5(3)-(-5)}$$
 64. $\frac{|10|}{-4(5)-(-12)}$

Objective B Find the average of each list of numbers. See Example 9.

▶ 65. -10, 8, -4, 2, 7, -5, -12
▶ 66. -18, -8, -1, -1, 0, 4
▶ 67. -17, -26, -20, -13
▶ 68. -40, -20, -10, -15, -5

Let's use the graph from Example 9, which shows some monthly normal temperatures for Barrow, Alaska. Use this for Exercises 69 through 72.

Monthly Normal Temperatures for Barrow, Alaska



71. Can the average of all these temperatures be greater than the highest temperature, 20? Explain why or why not.

- **69.** Find the average of the temperatures for the months December through March.
- **70.** Find the average of the temperatures for the months October through January.
- **72.** Can the average of all these temperatures be less than the lowest temperature, −16? Explain why or why not.

Review

Perform each indicated operation. See Sections 1.3, 1.4, 1.6, and 1.7.

73. 45 · 90 **74.** 90 ÷ 45 **75.** 90 - 45 **76.** 45 + 90

Find the perimeter of each figure. See Section 8.3.



Concept Extensions

Insert parentheses where needed so that each expression evaluates to the given number.

81. $2 \cdot 7 - 5 \cdot 3$; evaluates to 12

82. $7 \cdot 3 - 4 \cdot 2$; evaluates to 34

83. $-6 \cdot 10 - 4$; evaluates to -36

84. $2 \cdot 8 \div 4 - 20$; evaluates to -36

- **85.** Are parentheses necessary in the expression $3 + (4 \cdot 5)$? Explain your answer.
- **87.** Discuss the effect parentheses have in an exponential expression. For example, what is the difference between $(-6)^2$ and -6^2 ?

Evaluate.

89. (-12)⁴

- **86.** Are parentheses necessary in the expression $(3 + 4) \cdot 5$? Explain your answer.
- **88.** Discuss the effect parentheses have in an exponential expression. For example, what is the difference between $(2 \cdot 4)^2$ and $2 \cdot 4^2$?

90. (-17)⁶

Chapter 10 Group Activity

Magic Squares

Sections 10.1-10.3

A magic square is a set of numbers arranged in a square table so that the sum of the numbers in each column, row, and diagonal is the same. For instance, in the magic square below, the sum of each column, row, and diagonal is 15. Notice that no number is used more than once in the magic square.

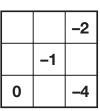
| 2 | 9 | 4 |
|---|---|---|
| 7 | 5 | 3 |
| 6 | 1 | 8 |

The properties of magic squares have been known for a very long time and once were thought to be good luck charms. The ancient Egyptians and Greeks understood their patterns. A magic square even made it into a famous work of art. The engraving titled *Melencolia I*, created by German artist Albrecht Dürer in 1514, features the following four-by-four magic square on the building behind the central figure.

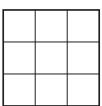
| 16 | 3 | 2 | 13 |
|----|----|----|----|
| 5 | 10 | 11 | 8 |
| 9 | 6 | 7 | 12 |
| 4 | 15 | 14 | 1 |

Exercises

- 1. Verify that what is shown in the Dürer engraving is, in fact, a magic square. What is the common sum of the columns, rows, and diagonals?
- **2.** Negative numbers can also be used in magic squares. Complete the following magic square:



3. Use the numbers -16, -12, -8, -4, 0, 4, 8, 12, and 16 to form a magic square:



Chapter 10 Vocabulary Check

Fill in each blank with one of the words or phrases listed below.

| | signed | positive | opposites | n | egative | absolute value | additive inverse |
|-----|--|-----------------------------|--------------------|-------------------|--|---|---|
| | integers | inequality symbols | average | is | less than | is greater than | |
| 1. | | rs that are the same distar | ice from 0 on a r | numt | per line but are | on opposite sides of | 0 are |
| 2. | Together, po | sitive numbers, negative | numbers, and 0 a | are ca | alled | numbers | š. |
| 3. | The | of a number | r is that number | 's dis | stance from 0 or | n a number line. | |
| 4. | The | are, -3 | , -2, -1, 0, 1, 2, | 3, | •• | | |
| 5. | The opposite | e of a number is also calle | d its | | · | | |
| 6. | The | numbers ar | e numbers less t | han z | zero. | | |
| 7. | The | numbers ar | e numbers great | er th | an zero. | | |
| 8. | . The symbols "<" and ">" are called | | | | | | |
| 9. | • The of a list of numbers is $\frac{\text{sum of numbers}}{number \text{ of numbers}}$. | | | | | | |
| 10. | The sign " </th <th>" means</th> <th> and ">" me</th> <th>eans ₋</th> <th></th> <th>·</th> <th></th> | " means | and ">" me | eans ₋ | | · | |
| | | | | / | Chapter 10 Chapter 10 Then check a
For further red |) Test on page 698
ll of your answers at | the Test on page 697
the back of this text.
ep video solutions to |

| | U | |
|--|---|--|

Chapter Highlights

| Definitions and Concepts | Examples |
|---|--|
| Section 10.1 S | igned Numbers |
| Together, positive numbers, negative numbers, and 0 are called signed numbers. | -432, -10, 0, 15 |
| The integers are, $-3, -2, -1, 0, 1, 2, 3,$ | 2 units |
| The absolute value of a number is that number's distance from 0 on a number line. The symbol for absolute value is $ $. | -2 = 2 $ 2 = 2$ $2 units$ $ 2 = 2$ $2 units$ $2 units$ |
| | -3 - 2 - 1 0 1 2 3 |
| Two numbers that are the same distance from 0 on a | 5 and -5 are opposites. |
| number line but are on opposite sides of 0 are called opposites. | 5 units 5 units
-5 -4 -3 -2 -1 0 1 2 3 4 5 |
| If <i>a</i> is a number, then $-(-a) = a$. | -(-11) = 11. Do not confuse with $- -3 = -3$ |

| | Definitions and Concepts | Examples |
|---|---|--|
| | Section 10.2 Addi | |
| Adding | Two Numbers with the Same Sign | Add: |
| Step 1: Add their absolute values. | | -2 + (-3) = -5 |
| Step 2: | Use their common sign as the sign of the sum. | -7 + (-15) = -22 |
| Adding | Two Numbers with Different Signs | -1.2 + (-5.7) = -6.9 |
| Step 1: | Find the larger absolute value minus the smaller | -6 + 4 = -2 |
| | absolute value. | 17 + (-12) = 5 |
| Step 2: | Use the sign of the number with the larger abso- | $-\frac{4}{11} + \frac{1}{11} = -\frac{3}{11}$ |
| | lute value as the sign of the sum. | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ |
| | | -32 + (-2) + 1434 + 14
= -20 |
| | Casting 10.2 Culture | |
| | | cting Signed Numbers |
| | cting Two Numbers | Subtract: |
| 11 <i>a</i> and | b are numbers, then $a - b = a + (-b)$. | -35 - 4 = -35 + (-4) = -39 |
| | | 3 - 8 = 3 + (-8) = -5
-7.8 - (-10.2) = -7.8 + 10.2 = 2.4 |
| | | 7 - 20 - 18 - (-3) = 7 + (-20) + (-18) + 3 |
| | | = -13 + (-18) + 3 |
| | | = -31 + 3 |
| | | = -28 |
| | Section 10.4 Multiplying ar | nd Dividing Signed Numbers |
| Multipl | ying Signed Numbers | Multiply: |
| 1 | oduct of two numbers having the same sign is a | (-7)(-6) = 42 |
| • | number. | 9(-4) = -36 |
| | oduct of two numbers having different signs is a e number. | -3(0.7) = -2.1 |
| | | Evaluate: |
| | | $(-3)^2 = (-3)(-3) = 9$ |
| | | $\left(-\frac{2}{3}\right)^2 = \left(-\frac{2}{3}\right)\left(-\frac{2}{3}\right) = \frac{4}{9}$ |
| | | $-3^2 = -(3 \cdot 3) = -9$ |
| Dividin | g Signed Numbers | Divide: |
| - | otient of two numbers having the same sign is a number. | $-100 \div (-10) = 10$ |
| The que | otient of two numbers having different signs is a e number. | $\frac{14}{-2} = -7, \frac{-3.6}{-0.3} = 12, \frac{0}{-3} = 0, \frac{22}{0}$ is undefined. |

| Definitions and Concepts | Examples | | | | |
|--|---|--|--|--|--|
| Section 10.5 Order of Operations | | | | | |
| Order of Operations | Simplify: | | | | |
| Perform all operations within parentheses (),
brackets [], or other grouping symbols such as square
roots or fraction bars. Evaluate any expressions with exponents. Multiply or divide in order from left to right. Add or subtract in order from left to right. | $3 + 2 \cdot (-5) = 3 + (-10)$
= -7
$\frac{-2(5-7)}{-7+ -3 } = \frac{-2(-2)}{-7+3}$
= $\frac{4}{-4}$
= -1 | | | | |

Chapter 10

Review

- (10.1) *Represent each quantity by a signed number.*
- **1.** A gold miner is working 1435 feet below the surface of Earth.

Graph each number on a number line.

3.
$$-2, 4, -3.5, 0$$

4. $-7, -1.6, 3, -4\frac{1}{3}$
5. $-7, -6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7$
4. $-7, -1.6, 3, -4\frac{1}{3}$
5. $-7, -6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7$
5. Insert < or > between each pair of numbers to form a true statement.

6. $-5\frac{1}{3}$ $-4\frac{7}{8}$ **7.** -12.3 **5.** –18 -20

Find each absolute value.

8. |-12| **9.** |0|

Find the opposite of each number.

12. $\frac{1}{2}$ **11.** –12

Simplify.

13. -(-3.9)

Determine whether each statement is true or false.

15. A negative number is always less than a positive number.

(10.2) Add.

18. 18 + (-4) **17.** 5 + (-3)

2. A mountain peak is 7562 meters above sea level.

10. $\left|-\frac{7}{8}\right|$

16. The absolute value of a number is always 0 or a

19. -12 + 16

positive number.

14. -|-7|

20. -23 + 40

-19.8

Chapter 10 Review

21. -8 + (-15) **22.** -5 + (-17)

25.
$$\frac{2}{3} + \left(-\frac{2}{5}\right)$$
 26. $-\frac{8}{9} + \frac{1}{3}$

- **29.** The temperature at 5 a.m. on a day in January was -15° Celsius. By 6 a.m. the temperature had fallen 5 degrees. Use a signed number to represent the temperature at 6 a.m.
- **31.** During the 2017 LPGA ANA Inspiration golf tournament in Rancho Mirage, California, the winner So Yeon Ryu had scores of -4, -3, -3, and -4 over four rounds of golf. What was her total score for the tournament? (*Source:* Ladies Professional Golf Association)

23.
$$-2.4 + 0.3$$
 24. $-8.9 + 1.9$

27. -43 + (-108) **28.** -100 + (-506)

- **30.** A diver starts out at 127 feet below the surface and then swims downward another 23 feet. Use a signed number to represent the diver's current depth.
- **32.** The Ryder Cup, a biennial (every two years) pro men golfers' tournament between an American team and a European team, scores holes won. During the 2016 Ryder Cup, the winners, the American team, had a score of 17. The losing team, the Europeans, had a score 6 less than the Americans' score. What was the European team's score? (*Source:* Ryder Cup 2016)

33. 4 - 12 **34.** -12 - 14 **35.**
$$-\frac{3}{4} - \frac{1}{2}$$
 36. $-\frac{2}{5} - \frac{7}{10}$

41. -1.7 - (-2.9) **42.** -0.5 - (-1.2) **43.**
$$\frac{4}{9} - \frac{7}{9} - \left(-\frac{1}{18}\right)$$
 44. $\frac{3}{7} - \frac{5}{7} - \left(-\frac{1}{14}\right)$

45. Josh Weidner has \$142 in his checking account. He writes a check for \$125, makes a deposit for \$43, and then writes another check for \$85. Represent the balance in his account by a signed number.

48. (-3)⁴

46. If the elevation of Lake Superior is 600 feet above sea level and the elevation of the Caspian Sea is 92 feet below sea level, find the difference in elevation. Represent the difference by a signed number.

39. -(-5) - 12 - (-3) **40.** -16 - 16 - (-4) - (-12)

- (10.4) Perform the indicated operations.
- **47.** $(-11)^2$
- **51.** $\left(-\frac{4}{5}\right)^3$ **52.** $\left(-\frac{2}{3}\right)^3$
- **55.** $\frac{-78}{3}$ **56.** $\frac{38}{-2}$
- **59.** $-\frac{2}{3} \cdot \frac{7}{8}$ **60.** -0.5(-12)

- **49.** -3^4 **50.** -11^2
- **53.** (-3)(-7) **54.** -6·3
- **57.** (-4)(-1)(-9) **58.** (-2)(-2)(-10)

61. -2 ÷ 0 **62.** 0 ÷ (-61)

63. $\frac{-0.072}{-0.06}$ **64.** $-\frac{8}{25} \div \left(-\frac{2}{5}\right)$

Simplify.

67.
$$-10 + 3(-2)$$
 68. $3(-12) - \sqrt{64}$ **69.** $5 \cdot 2 + \sqrt{36} \div (-0.3)$ **70.** $-6 + (-10) \div (-0.2)$

71. $|-16| + (-3) \cdot 12 \div 4$ **72.** $-(-4) \cdot |-3| - 5$ **73.** $4^3 - (8 - 3)^2$ **74.** $2^3 - (9 - 2)^2$

75.
$$\left(-\frac{1}{3}\right)^2 - \frac{8}{3}$$
 76. $\left(-\frac{1}{10}\right)^2 - \frac{9}{10}$

Perform the indicated operations.

- **79.** $(-4)^2$ **80.** -4^2
- **84.** $\frac{84}{-4}$ **83.** -4(-12)
- **87.** $-\frac{15}{14} \div \left(-\frac{25}{28}\right)$ **88.** $\frac{3}{11} \cdot \left(-\frac{22}{4}\right)$
- **91.** Joe owed his mother \$32. He gave her \$23. Write his financial situation as a signed number.
- **93.** The top of the mountain has an altitude of 12,923 feet. The bottom of the valley is 195 feet below sea level. Find the difference between these two elevations.

Simplify.

95. $(3-7)^2 \div (6-4)^3$

97.
$$3(4+2) + (-6) - 3^2$$

100. $4 - 6 \cdot 5 + \sqrt{1}$

| 81. -6 + (-9) | 82. -16 - 3 |
|--------------------------|---|
| 85. -7.6 - (-9.7) | 86. $-\frac{9}{20} + \frac{4}{20}$ |

77. $\frac{(-4)(-3) - (-2)(-1)}{-10 + 5}$ **78.** $\frac{4(12 - 18)}{-10 \div (-2 - 3)}$

89.
$$\frac{7}{8} - \frac{9}{10}$$
 90. 5(-0.27)

- 92. The temperature at noon on a Monday in December was -11° C. By noon on Tuesday, it had warmed by 17°C. What was the temperature at noon on Tuesday?
- **94.** Wednesday's lowest temperature was -18° C. The cold weather continued and by Friday it had dropped another 9°C. What was the low temperature on Friday?

102. $5(7-6)^3 - 4(2-3)^2 + 2^4$

96.
$$(4+6)^2 \div (2-7)^2$$

101. $\frac{-|-14|-6}{7+2(-3)}$

9

98.
$$4(5-3) - (-2) + 3^3$$
 99. $2 - 4 \cdot 3 + \sqrt{25}$

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Chapter 10 Getting Ready for the Test

MULTIPLE CHOICE. All the exercises below are **Multiple Choice**. Choose the correct letter. Not all letters may be used and some may be used more than once.

For Exercises 1 through 4, identify each answer as **A.** 2 **B.** −2 **C.** 0 $\mathbf{O1.}$ -2; choose the opposite $\bigcirc 2$. -2; choose the absolute value **03.** 2; choose the absolute value **4**. 2; choose the opposite For Exercises 5 through 10, identify each answer as **A.** addition **B.** subtraction **C.** multiplication **D.** division \bigcirc 5. For 5(6), the operation is . **6.** For -12(+3), the operation is _____. **Q7.** For -12 + 3, the operation is **O8.** For $\frac{-12}{+3}$, the operation is _____. **Q**9. For $4 + 6 \cdot 2$, which operation is performed first? **10.** For $4 + 6 \div 2$, which operation is performed first? For Exercises 11 through 24, fill in the blank with the correct choice. **A.** 0 **B.** a positive number **C.** a negative number **D.** cannot be determined **• 11.** (a negative number) \cdot (a negative number) = _____. **\bigcirc 12.** (a negative number) + (a negative number) = ____. **013.** (a negative number) \div (a negative number) = ____. **• 14.** (a negative number) - (a negative number) = _____. **15.** $0 \cdot (a \text{ negative number}) = _____.$ \mathbf{O} **16.**0 + (a negative number) = ____. \mathbf{O} **17.**0 - (a negative number) = ____. **18.** $0 \div$ (a negative number) = ____. **0 19.** (a positive number) \cdot (a negative number) = ____. **20.** (a negative number) \cdot (a positive number) = _____. **Q 21.** (a positive number) + (a negative number) = ____. **Q 22.** (a positive number) - (a negative number) = _____. **Q 23.** (a negative number) - (a positive number) = _____. **24.** (a positive number) - (a positive number) = .

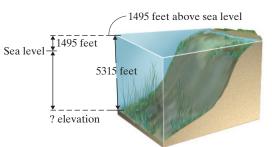
| Chapter 10 | Test MyLab Mat | | for additional practice go to your study plan
n MyLab Math. |
|---|---|----------------------------------|--|
| Answers | ● 1. Graph each number of $-5, 0, 2, -6.5, -1\frac{2}{3}$ | n a number line. | |
| | ←
-7 -6 · | -5 -4 -3 -2 -1 0 | 1 2 3 4 5 6 7 |
| <u> 1. </u> | 2. Find the opposite of | $\frac{2}{3}$. | |
| 3.
 | <i>Simplify</i> .
▶ 3. −2.9 | ●4. -(-98) | ○5. - -98 |
| 6.
7. | Insert $< or >$ between each 6. -17 -19 | | orm a true statement. |
| 8.
9.
10. | Simplify each expression. | | |
| <u>11.</u>
<u>12.</u> | 8. −5 + 8 | 9. 18 – 24 | 5) 10. 0.5(-20) |
| <u>13.</u>
<u>14.</u>
15. | ○ 11. -16 ÷ (-4) | 012. $-\frac{3}{11} + (-$ | 13. $-7 - (-19)$ |
| <u>16.</u>
17. | ○ 14. -5(-13) | 015. $\frac{-2.5}{-0.5}$ | ●16. -25 + (-13) |
| <u>18.</u>
<u>19.</u> | ● 17. -8 + 9 ÷ (-3) | | 18. $-7 + (-32) - 12 + \sqrt{25}$ |
| <u>20.</u>
698 | • 19. $(-5)^3 - 24 \div (-3)$ | 0 | 20. $(5-9)^2 \cdot (8-6)^3$ |

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• 21.
$$\frac{-3(-2) + 12}{-1(-4 - 5)}$$
 • 22. $\frac{|25 - 30|^2}{2(-6) + 7}$ • 23. $\left(\frac{5}{9} - \frac{7}{9}\right)^2 + \left(-\frac{2}{9}\right)^2$
• 24. Find the sum of -7, -9, and 35. • 25. Subtract 43 from 40.
• 26. Find the product of $-\frac{1}{10}$ and $\frac{2}{9}$. • 27. Find the quotient of $-\frac{1}{10}$ and $\frac{2}{9}$.

- **28.** A diver starts at sea level and then makes 4 successive descents of 22 feet. After the descents, what is her elevation (with respect to sea level)?
- **29.** Aaron Hawn has \$129 in his checking account. He writes a check for \$79, withdraws \$40 from an ATM, and then deposits \$35. Represent the new balance in his account by an integer.
- **30.** Mt. Washington in New Hampshire has an elevation of 6288 feet above sea level. The Romanche Gap in the Atlantic Ocean has an elevation of 25,354 feet below sea level. Represent the difference in elevation between these two points by an integer. (Source: National Geographic Society and Defense Mapping Agency)
- **31.** Lake Baykal in Siberian Russia is the deepest lake in the world, with a maximum depth of 5315 feet. The elevation of the lake's surface is 1495 feet above sea level. What is the elevation (with respect to sea level) of the deepest point in the lake? (Source: U.S. Geological Survey)



| 21. | |
|------------|--|
| 22. | |
| 23. | |
| | |
| 24. | |
| <u>25.</u> | |
| 26. | |
| 27. | |
| 28. | |
| 29. | |
| <u></u> | |
| 30. | |
| 31. | |
| 32. | |
| | |

| Chapters 1–1 | 0 Cumulative Review | , |
|-------------------------------|--|--|
| Answers
1. | 1. Multiply: 631×125 | 2. Multiply: $\frac{5}{8} \cdot \frac{10}{11}$ |
| 2.
 | 3. Divide: $\frac{2}{5} \div \frac{1}{2}$ | 4. Divide: 2124 ÷ 9 |
| <u>4.</u>
<u>5.</u> | 5. Add: $\frac{2}{3} + \frac{1}{7}$ | 6. Subtract: $9\frac{2}{7} - 7\frac{1}{2}$ |
| <u>6.</u>
<u>7.</u> | For Exercises 7 through 9, write each decimal7. Forty-eight and twenty-six hundredths | <i>in standard form.</i>
8. Eight hundredths |
| <u>8.</u>
<u>9.</u>
10. | 9. Six and ninety-five thousandths | 10. Multiply: 563.21 × 100 |
| <u>11.</u> | 11. Subtract: 3.5 – 0.068 | 12. Divide: 0.27 ÷ 0.02 |
| <u>12.</u>
<u>13.</u> | 13. Simplify: $\frac{5.68 + (0.9)^2 \div 100}{0.2}$ | 14. Simplify: $50 \div 5 \cdot 2$ |
| <u>14.</u>
<u>15.</u> | 15. Write "\$31,500 every 7 months" as a unit rate. | 16. Write "300 miles every 5 hours" as a unit rate. |
| <u>16.</u> | Find the value of the unknown number n. | |
| <u>17.</u>
18. | 17. $\frac{51}{34} = \frac{3}{n}$ | 18. $\frac{7}{8} = \frac{6}{n}$ |
| <u>19.</u>
20.
700 | 19. 46 out of every 100 college students live at home. What percent of students live at home? (<i>Source:</i> Independent Insurance Agents of America) | 20. A basketball player made 4 out of 5 free throws. What percent of free throws were made? |

Cumulative Review

Write each fraction, mixed, or whole number as a percent.

- **21.** $\frac{9}{20}$ **22.** $\frac{53}{50}$
- **23.** $1\frac{1}{2}$ **24.** 5
- Solve.
- **25.** 13 is $6\frac{1}{2}$ % of what number?
- **27.** Translate to a proportion. 101 is what percent of 200?
- **29.** Ivan Borski borrowed \$2400 at 10% simple interest for 8 months to help him buy a used Toyota Corolla. Find the simple interest he paid.
- **31.** Add 3 ft 2 in. and 5 ft 11 in.
- **32.** Find the perimeter of the square.

28. Translate to an equation. 101 is what

30. C. J. Dufour wants to buy a digital

camera. She has \$762 in her savings

account. If the camera costs \$237, how

17 meters

much money will she have in her account after buying the camera?

26. What is 110% of 220?

percent of 200?

33. Normal body temperature is 98.6°F. What is this temperature in degrees Celsius?

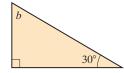
35. Find the supplement of a 107° angle.

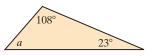
- - **36.** Find the complement of a 34° angle.

 \triangle **38.** Find the measure of $\angle a$.

34. Convert 7.2 meters to centimeters.

37. Find the measure of $\angle b$.





| 21. |
|------------|
| |
| 22. |
| 2 2 |
| 23. |
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| 26. |
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| 27. |
| 28. |
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| 29. |
| 20 |
| 30. |
| 31. |
| |
| 32. |
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| 33. |
| |
| 34. |
| 35. |
| |
| 36. |
| |
| 37. |
| |
| 38. |

701

| 702 | Chapter 10 Signed Numbers |
|-------------------|---|
| <u>39.</u>
40. | \triangle 39. Find the area of the parallelogram.
1.5 miles
3.4 miles
\triangle 40. Find the area of the circle. Give the exact area, then use 3.14 for π to approximate the area. |
| <u>41.</u> | \triangle 41. Calculate the volume of a ball of radius 2 inches. Give the exact answer and an approximate answer. Use the |
| 42. | approximation $\frac{22}{7}$ for π .
2 cm $4 cm$ $3 cm$ |
| <u>43.</u> | |
| 44. | |
| 45. | 43. Find the median of the list of numbers: 25, 54, 56, 57, 60, 71, 98
44. Find the mean or average of 36, 25, 18, and 19. |
| <u>46.</u> | 45. If a die is rolled one time, find the probability of rolling a 3 or a 4.
46. Subtract: $-9 - (-4.1)$ |
| <u>47.</u> | |
| <u>48. a.</u> | 47. Add: $-2 + (-21)$
48. Simplify:
a. $(-10)^3$
b. -10^3 |
| b | 49. Simplify: $60 + 30 + (-2)^3$ 50. Simplify: $\frac{\sqrt{16} - (-8)}{9 - 12}$ |
| <u>49.</u> | |
| 50. | |

Introduction to Algebra



A Canopy of Trees

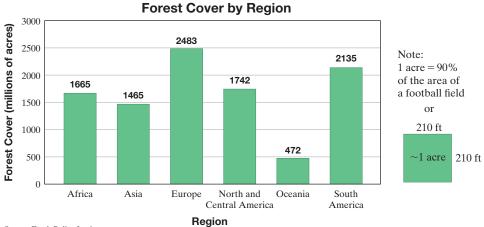


The Rings of a Tree

What Are the Largest and Longest-Living Plants on Our Planet?

rees are not only the largest plants on our planet, but they are the longest-living species. They absorb carbon dioxide, store the carbon, and release oxygen back into the air. Trees also prevent soil erosion and flooding as well as offer food and shelter to birds, insects, fungi, and other living plants and animals. Thousands of things are made from trees—from medicines to toothpaste to furniture. Since some trees live thousands of years, they also give us a glimpse into the past through the study of their rings. (See the photo above to the right.)

The photo above to the left shows a canopy of trees, which act as a filter. This filter provides shade, reduces noise, traps dust, and absorbs pollutants that are present in the air. The graph below shows the forest cover in regions of the world. In Section 11.1, Exercises 117 and 118, we examine the size of some giant trees.



Source: Earth Policy Institute

11

In this chapter we make the transition from arithmetic to algebra. In algebra, letters are used to stand for unknown quantities. Using variables is a very powerful tool for solving problems that cannot be solved with arithmetic alone. This chapter introduces variables, algebraic expressions, and solving variable equations.

Sections

- **11.1** Introduction to Variables
- **11.2** Solving Equations: The Addition Property
- **11.3** Solving Equations: The Multiplication Property

Integrated Review— Expressions and Equations

- **11.4** Solving Equations Using Addition and Multiplication Properties
- **11.5** Equations and Problem Solving

Check Your Progress

Vocabulary Check

- **Chapter Highlights**
- Chapter Review

Getting Ready for the Test

Chapter Test

Cumulative Review

11.1 Introduction to Variables

Objectives

A Evaluate Algebraic Expressions for Given Replacement Values for the Variables.

B Use Properties of Numbers to Combine Like Terms.

C Use Properties of Numbers to Multiply Expressions.

D Simplify Expressions by Multiplying and Then Combining Like Terms.

E Find the Perimeter and Area of Figures.

Objective A Evaluating Algebraic Expressions 🕑

Perhaps the most important quality of mathematics is that it is a science of pattern. Communicating about patterns is made possible by using a letter to represent all the numbers fitting a pattern. We call such a letter a **variable**. For example, in Section 1.3 we presented the addition property of 0, which states that the sum of 0 and any whole number is that number. We might write

0 + 1 = 10 + 2 = 20 + 3 = 30 + 4 = 40 + 5 = 50 + 6 = 6:

continuing indefinitely. This is a pattern, and all whole numbers fit the pattern. We can communicate this pattern for all whole numbers by letting a letter, such as *a*, represent all whole numbers. We can then write

$$0 + \mathbf{a} = \mathbf{a}$$

Helpful Hint

Variables have been used in previous chapters, although we have not called them that. For example, in the ratio and proportion chapter, we wrote equations such as

$$\frac{4}{n} = \frac{6}{12}$$

Here, the letter *n* is a variable.

Learning to use variable notation is a primary goal of learning **algebra**. We now take some important beginning steps in learning to use variable notation.

A combination of numbers, letters (variables), and operation symbols is called an **algebraic expression** or simply an **expression.** For example,

3 + x, $5 \cdot y$, and $2 \cdot z - 1 + x$

are expressions.

If two variables or a number and a variable are next to each other, with no operation sign between them, the indicated operation is multiplication. For example,

2x means $2 \cdot x$

and

xy or x(y) means $x \cdot y$

Also, the meaning of an exponent remains the same when the base is a variable. For example,

$$x^2 = \underbrace{x \cdot x}_{2 \text{ factors of } x}$$
 and $y^5 = \underbrace{y \cdot y \cdot y \cdot y \cdot y}_{5 \text{ factors of } y}$

Algebraic expressions have different values depending on the replacement values for the variable(s). Replacing a variable in an expression by a number and then finding the value of the expression is called **evaluating the expression**. When finding the value of an expression, remember to follow the order of operations.

Example 1 Evaluate: 3x - 7 when x = 2Practice 1 Evaluate: 5x - 12 when Solution: x = 2 $3x - 7 = 3 \cdot 2 - 7$ Replace x with 2. = 6 - 7 Multiply. = -1Subtract. Work Practice 1 **Example 2** Evaluate: 2x + y when x = 8 and y = -7Practice 2 Evaluate: 5x - y when x = 2**Solution:** Replace *x* with 8 and *y* with -7 in 2x + y. and v = -3 $2x + y = 2 \cdot 8 + (-7)$ Replace x with 8 and y with -7. = 16 + (-7) Multiply first because of the order of operations. = 9Add. Work Practice 2 **Example 3** Evaluate: $\frac{3m-2n}{-2q}$ when m = 8, n = 4, and q = 1Practice 3 Evaluate: $\frac{5r-2s}{-3q}$ when Solution: $\frac{3m-2n}{-2q} = \frac{3\cdot 8 - 2\cdot 4}{-2\cdot 1}$ Replace *m* with 8, *n* with 4, and *q* with 1. r = 3, s = 3, and q = 1 $=\frac{24-8}{-2}$ Multiply. $=\frac{16}{-2}$ Subtract in the numerator. = -8Divide. Work Practice 3 **Example 4** Evaluate: 8 - (6a - 5) when a = -3Practice 4 Evaluate: 13 - (3a + 8)Solution: when a = -2 $8 - (6a - 5) = 8 - (6 \cdot (-3) - 5)$ Replace *a* with -3. = 8 - (-18 - 5)Multiply. = 8 - (-23) Simplify inside the parentheses. = 8 + 23= 31Add. Work Practice 4 **Example 5** Evaluate: $x^3 - 1.1y$ when x = 4 and y = -1Practice 5 Evaluate: $a^2 - 0.7b$ when Solution: a = 6 and b = -2 $x^{3} - 1.1y = 4^{3} - 1.1(-1)$ Replace x with 4 and y with -1. = 64 - 1.1(-1) Evaluate 4³. = 64 - (-1.1) Multiply. = 64 + 1.1= 65.1Add. Answers **1.** -2 **2.** 13 **3.** -3 **4.** 11 **5.** 37.4 Work Practice 5

Practice 6

The formula for finding the perimeter of a rectangle is $P = 2 \cdot l + 2 \cdot w$ (which we now know can be written as P = 2l + 2w). Find the perimeter of a rectangular garden that is 25 meters wide and 40 meters long.



Example 6 Finding the Area of a Rectangle

The formula for finding the area of a rectangle is $A = l \cdot w$ (which we now know can be written as A = lw), where *l* is the length of the rectangle and *w* is the width. Find the area of a rectangular floor that is 45 feet long and 30 feet wide.



Solution:

$$A = \begin{matrix} l & \cdot & w \\ \downarrow & \downarrow \end{matrix}$$

= (45 feet) \cdot (30 feet) Replace *l* with 45 feet and *w* with 30 feet.
= 1350 square feet

The area of the floor is 1350 square feet.

Work Practice 6

Objective **B** Combining Like Terms 🕑

The addends of an algebraic expression are called the terms of the expression.

$$x + 3$$

$$1 1 2 \text{ terms}$$

$$3y^2 + (-6y) + 4$$

$$1 1 3 \text{ terms}$$

A term that is only a number has a special name. It is called a **constant term**, or simply a **constant**. A term that contains a variable is called a **variable term**.

| $x \uparrow$ | + 3
↑ | $3y^2 + (-6y) + \uparrow$ | 4
↑ |
|--------------|----------|---------------------------|----------|
| variable | constant | variable | constant |
| term | term | terms | term |

The number factor of a variable term is called the **numerical coefficient.** A numerical coefficient of 1 is usually not written.

| 5x | $x \text{ or } 1x$ \uparrow | $3y^2$ \uparrow | -6y |
|-----------------------------|--|-----------------------------|---------------------------------|
| Numerical coefficient is 5. | Understood
numerical
coefficient is 1. | Numerical coefficient is 3. | Numerical coefficient is -6 . |

Terms with the same variable factors, except that they may have different numerical coefficients, are called **like terms**.

| Like Terms | Unlike Terms |
|--------------------|-------------------------|
| $3x, \frac{1}{2}x$ | $5x, x^2$ |
| -6y, 2y, y | 7 <i>x</i> , 7 <i>y</i> |

Concept Check True or false? The terms -7xy and -7yx are like terms. Explain.

A sum or difference of like terms can be simplified using the **distributive property.** Recall from Section 1.6 that the distributive property says that multiplication distributes over addition (and subtraction). Using variables, we can write the distributive property as follows:

$$(a+b)c = ac + bc$$

Hint Recall that $1 \cdot any$ number = that number. This means that

Helpfi

```
1 \cdot x = x or that 1x = x.
```

Thus *x* can always be replaced by 1x or $1 \cdot x$.

Answer

6. 130 m

✓ Concept Check Answer

true; the order of the variable factors does not make a difference

If we write the right side of the equation first, then the left side, we have the following:

Distributive Property If a, b, and c are numbers, then ac + bc = (a + b)cAlso, ac - bc = (a - b)c

The distributive property guarantees that, no matter what number x is, 7x + 5x (for example) has the same value as (7 + 5)x, or 12x. We then have that

7x + 5x = (7 + 5)x = 12x

This is an example of **combining like terms.** An algebraic expression is **simplified** when all like terms have been combined.

Example 7 Simplify each expression by combining like terms.

a. 3x + 2xb. y - 7ySolution: We add or subtract like terms. a. 3x + 2x = (3 + 2)x = 5xUnderstood 1 b. y - 7y = 1y - 7y = (1 - 7)y = -6yWork Practice 7

The commutative and associative properties of addition and multiplication can also help us simplify expressions. We presented these properties in Sections 1.3 and 1.6 and state them again using variables.

Properties of Addition and Multiplication

If a, b, and c are numbers, then

a + b = b + a Commutative property of addition $a \cdot b = b \cdot a$ Commutative property of multiplication

That is, the **order** of adding or multiplying two numbers can be changed without changing their sum or product.

(a + b) + c = a + (b + c) Associative property of addition $(a \cdot b) \cdot c = a \cdot (b \cdot c)$ Associative property of multiplication

That is, the **grouping** of numbers in addition or multiplication can be changed without changing their sum or product.

Practice 7

Simplify each expression by combining like terms. **a.** 8m - 11m

b. 5a + a

Helpful Hint

• Examples of these properties are

2 + 3 = 3 + 2 $7 \cdot 9 = 9 \cdot 7$ (1+8) + 10 = 1 + (8+10) Associative property of addition $(4 \cdot 2) \cdot 3 = 4 \cdot (2 \cdot 3)$

Commutative property of addition Commutative property of multiplication Associative property of multiplication

• These properties are not true for subtraction or division.

Practice 8

Simplify: 8m + 5 + m - 4

Practice 9–12

Simplify each expression by combining like terms. 9. 7y + 11y - 8**10.** 2y - 6 + y + 7y**11.** 3.7x + 5 - 4.2x + 1512. -9v + 2 - 4v - 8x

+ 12 - x

Practice 13–14 Multiply. **13.** 7(8*a*) 14. -5(9x)

Answers **8.** 9m + 1 **9.** 18y - 8 **10.** 10y - 6

11. -0.5x + 20 **12.** -13y - 9x + 14**13.** 56*a* **14.** -45*x*

Example 8 Simplify: 2y - 6 + 4y + 8

Solution: We begin by writing subtraction as the addition of opposites.

2y - 6 + 4y + 8 = 2y + (-6) + 4y + 8= 2v + 4v + (-6) + 8Apply the commutative property of addition. = (2+4)y + (-6) + 8 Apply the distributive property. = 6v + 2Simplify.

Work Practice 8

Examples Simplify each expression by combining like terms. 9. 6x + 2x - 5 = 8x - 5**10.** 4x + 3 - 5x + 2x = 4x - 5x + 2x + 3= 1x + 3 or x + 3

11. 1.2y + 10 - 5.7y - 9 = 1.2y - 5.7y + 10 - 9= -4.5v + 1

12. 2x - 5 + 3y + 4x - 10y + 11 = 6x - 7y + 6

Work Practice 9–12

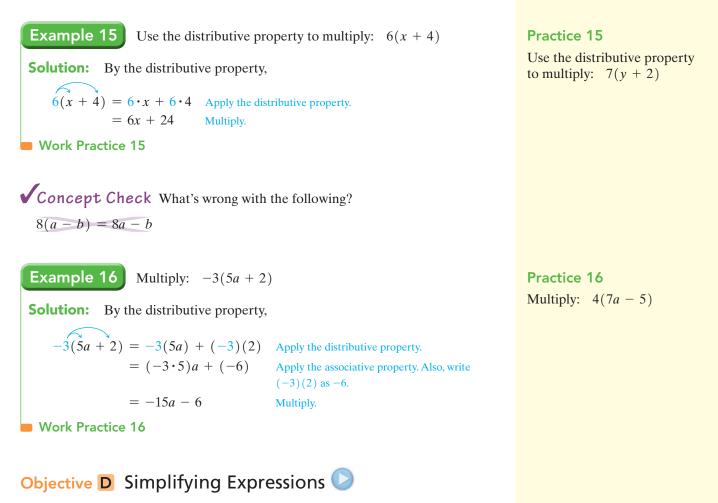
Objective C Multiplying Expressions 🕑

We can also use properties of numbers to multiply expressions such as 3(2x). By the associative property of multiplication, we can write the product 3(2x) as $(3 \cdot 2)x$, which simplifies to 6x.

| Examples Multiply. | |
|-------------------------------------|---|
| 13. $5(3y) = (5 \cdot 3)y$ | Apply the associative property of multiplication. |
| = $15y$ | Multiply. |
| 14. $-2(4x) = (-2 \cdot 4)x$ | Apply the associative property of multiplication. |
| = $-8x$ | Multiply. |
| Work Practice 13–14 | |

We can use the distributive property to combine like terms, which we have done, and also to multiply expressions such as 2(3 + x). By the distributive property, we have that

 $2(3 + x) = 2 \cdot 3 + 2 \cdot x$ Apply the distributive property. = 6 + 2x Multiply.



Next, we will simplify expressions containing parentheses by first using the distributive property to multiply and then **combining** any like terms.

Example 17 Simplify: 2(3 + 7x) - 15

Solution: First we use the distributive property to remove parentheses.

2(3 + 7x) - 15 = 2(3) + 2(7x) - 15 = 6 + 14x - 15Apply the distributive property.
Multiply. = 14x + (-9) or 14x - 9 Combine like terms.

Work Practice 17

Example 18 Simplify: -2(x-5) + 4(2x+2)**Solution:** First we use the distributive property to remove parentheses. -2(x-5) + 4(2x+2) = -2(x) - (-2)(5) + 4(2x) + 4(2) Apply the distribution utive property. = -2x + 10 + 8x + 8Multiply. = 6x + 18Combine like

Practice 17 Simplify: 5(2y - 3) - 8

| Helpful |
|--|
| Helpful
Hint 2 is <i>not</i> distrib- |
| uted to the -15 since it is not |
| within the parentheses. |

Practice 18 Simplify:

-7(x-1) + 5(2x+3)

Answers

terms.

15. 7y + 14 **16.** 28a - 20**17.** 10y - 23 **18.** 3x + 22

Concept Check Answer did not distribute the 8

Work Practice 18

Objective E Finding Perimeter and Area 💟



Find the perimeter of the triangle.

2z feet 3z feet

Solution: Recall that the perimeter of a figure is the distance around the figure. To find the perimeter, then, we find the sum of the lengths of the sides. We use the letter P to represent perimeter.

P = 2z + 3z + 5z= 10z





The perimeter is 10z feet.

Work Practice 19

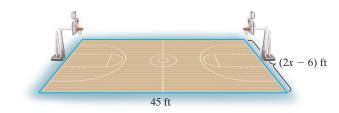
Practice 20

Find the area of the rectangular garden.



Example 20 Finding the Area of a Basketball Court

Find the area of this YMCA basketball court.



Solution: Recall how to find the area of a rectangle. Area = Length · Width, or if *A* represents area, *l* represents length, and *w* represents width, we have $A = l \cdot w$.

$$A = l \cdot w$$

= 45(2x - 6) Let l = 45 and w = (2x - 6).
= 90x - 270 Multiply.

The area is (90x - 270) square feet.

Work Practice 20





• measured in square un



- distance around
- measured in units

Practice 19

square.

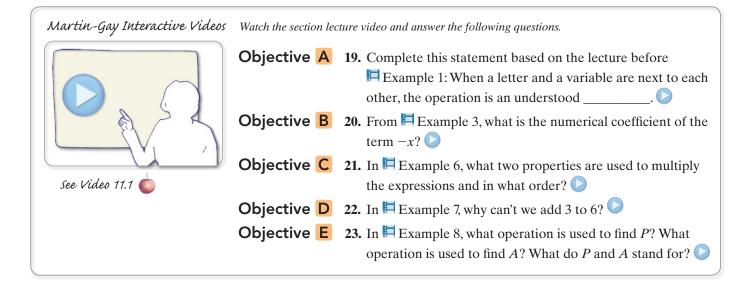
Find the perimeter of the

2x centimeters

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Some choices may be used more than once.

| | numerical coefficient | combine like terms | like | term | variable | associative |
|-----|--|--|--------------|--------------------------------------|-------------------------|------------------------------|
| | constant | expression | unlike | distributive | commutative | |
| 1. | $14y^2 + 2x - 23$ is called | a(n) | _while 14 | y^2 , 2x, and -23 a | re each called a(n |) |
| 2. | To multiply $3(-7x + 1)$. | , we use the | pı | operty. | | |
| 3. | To simplify an expression | n like $y + 7y$, we | | · | | |
| 4. | By the | _ properties, the <i>order</i> | of adding of | or multiplying tw | o numbers can be | e changed without |
| | changing their sum or pr | oduct. | | | | |
| 5. | The term $5x$ is called a(n |) te | rm while t | he term 7 is calle | ed a(n) | term. |
| 6. | The term z has an unders | stood | of 1. | | | |
| 7. | By the | _ properties, the group | ing of num | bers in addition | or multiplication | can be changed |
| | without changing their su | um or product. | | | | |
| 8. | The terms $-x$ and $5x$ are | ter | ms. | | | |
| 9. | For the term $-3x^2y$, -3 is | s called the | · | | | |
| 10. | The terms $5x$ and $5y$ are | terr | ns. | | | |
| Ide | Identify each pair of terms as like terms or unlike terms. | | | | | |
| 11. | 5 <i>x</i> and 5 <i>y</i> | 12. -3 <i>a</i> and -3 <i>b</i> | 1 | 3. <i>x</i> and $-2x$ | 14. ⁷ | 7 <i>y</i> and <i>y</i> |
| 15. | $-5n$ and $6n^2$ | 16. $4m^2$ and $2m$ | 1 | 7. 8 <i>b</i> and −6 <i>b</i> | 18. | 12 <i>a</i> and -11 <i>a</i> |



11.1 Exercise Set MyLab Math 🕗

Objective A *Evaluate each expression when* x = -2, y = 5, *and* z = -3. *See Examples 1 through 6.*

| 1. $3 + 2z$ | 2. $7 + 3z$ | 3. $-y - z$ | 4. $-y - x$ |
|--|---|--------------------------------|-------------------------------|
| 5. $z - x + y$ | 6. $x + y - z$ | 7. $3x - z$ | 8. $y + 5z$ |
| 9. 8 - (5 <i>y</i> - 7) | 10. $5 + (2x - 1)$ | 11. $y^3 - 4x$ | 12. $y^2 - 2z$ |
| 13. $\frac{6xy}{4}$ | 14. $\frac{8yz}{15}$ | 15. $\frac{2y-2}{x}$ | 16. $\frac{6+3x}{z}$ |
| 017. $\frac{x+2y}{2z}$ | 18. $\frac{2z-y}{3x}$ | 19. $\frac{5x}{y} - 10$ | 20. $7 - \frac{3y}{z}$ |
| 21. $\frac{xz}{y} + \frac{3}{10}$ | 22. $\frac{x}{yz} + \frac{31}{30}$ | 23. $ x - y - 7.6$ | 24. $ z - y - 1$ |

Objective B *Simplify each expression by combining like terms. See Examples 7 through 12.*

| 25. $3x + 5x$ | 26. $8y + 3y$ | 27. 5 <i>n</i> - 9 <i>n</i> |
|---|--|--|
| 28. 7z - 10z | 29. $4c + c - 7c$ | 30. 5b - 8b - b |
| 31. $5x - 7x + x - 3x$ | 32. $8y + y - 2y - y$ | 33. 4 <i>a</i> + 3 <i>a</i> + 6 <i>a</i> - 8 |
| 34. 5b - 4b + b - 15 | 35. 1.7 <i>x</i> + 3.4 - 2.6 <i>x</i> + 7.8 | 36. -8.6 <i>y</i> + 1.3 - 2.9 <i>y</i> - 14.7 |
| ○ 37. 3 <i>x</i> + 7 − <i>x</i> − 14 | 38. $9x - 6 + x - 10$ | 39. $4x + 5y + 2 - y - 9x - 7$ |
| 40. <i>a</i> + 4 <i>b</i> + 3 - 7 <i>a</i> - 5 <i>b</i> - 10 | 41. $\frac{5}{6} - \frac{7}{12}x - \frac{1}{3} - \frac{3}{10}x$ | 42. $-\frac{2}{5} + \frac{4}{9}y - \frac{4}{15} + \frac{1}{6}y$ |

43. -5m - 2.3m + 11 + 2.5m - 15.1 **44.** -13n - 4.8n + 13 + 6.9n - 13.6

| Objective C Multiply. See Examples 13 through 16. | | | | |
|---|-------------------------------|-------------------------------|-----------------------------|------------------------------|
| 45. 6(5 <i>x</i>) | 46. 4(4 <i>x</i>) | ○ 47. -2(11y) | 48. -3(21 <i>z</i>) | 49. -0.6(7 <i>a</i>) |
| 50. -0.4(9 <i>a</i>) | 51. $\frac{2}{3}(-6a)$ | 52. $\frac{3}{4}(-8a)$ | 53. 2(<i>y</i> + 2) | 54. 3(<i>x</i> + 1) |

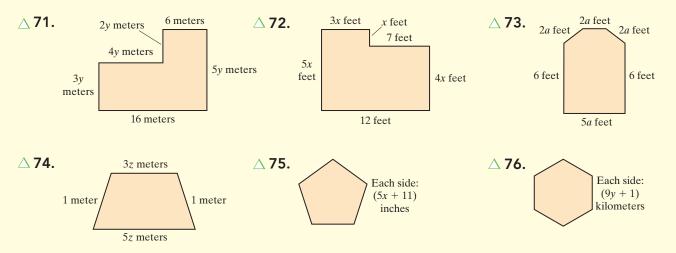
12.7

55.
$$5(3a-8)$$
56. $4(5y-6)$ **57.** $-4(3x+7)$ **58.** $-8(8y+10)$ **59.** $1.2(5x-0.1)$ **60.** $3.1(7x-0.3)$ **61.** $\frac{1}{2}(-8x-3)$ **62.** $\frac{1}{5}(-20x-7)$

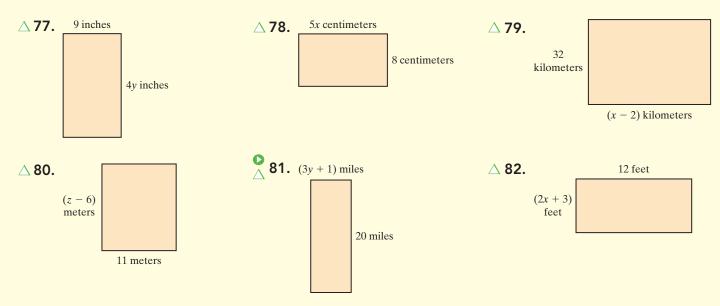
Objective D *Simplify each expression. Use the distributive property to remove parentheses first. See Examples 17 and 18.*

63. 2(x + 4) - 17**64.** 5(6 + y) - 2**65.** 4(6n - 5) + 3n**66.** 3(5 - 2b) - 4b**67.** 3 + 6(w + 2) + w**68.** 8z + 5(6 + z) + 20**69.** -2(3x + 1) - 5(x - 2)**70.** -3(5x - 2) - 2(3x + 1)

Objective E *Find the perimeter of each figure. See Example 19.*



Find the area of each rectangle. See Example 20.

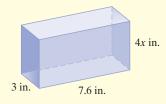


Objectives A B C D E Mixed Practice Solve. See Examples 1 through 20.

- **83.** Find the area of a regulation NCAA basketball court that is 94 feet long and 50 feet wide.
- **85.** A decorator wishes to put a wallpaper border around a rectangular room that measures 14 feet by 18 feet. Find the room's perimeter.
- **87.** Find the perimeter of a triangular garden that measures 5 feet by x feet by (2x + 1) feet.
- **89.** How much interest will \$3000 in a passbook savings account earn in 2 years at Money Bank, which pays 6% simple interest? Use I = PRT.
- **91.** Find the area of a circular braided rug with a radius of 5 feet. Use $A = \pi r^2$ and $\pi \approx 3.14$.



- **93.** Convert Paris, France's, low temperature of -5° C to Fahrenheit. Use F = $\frac{9}{5}$ C + 32.
- **95.** Find the volume of a box that measures 12 inches by 6 inches by 4 inches. Use V = lwh.
- **97.** Find the volume. Use V = lwh.



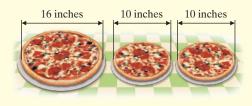
Review

Perform each indicated operation. See Sections 10.2 and 10.3.

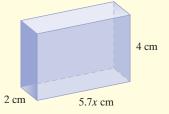
103. -4 + 4

- **99.** -13 + 10 **100.** -15 + 23
- **102.** -7 (-4)

- **84.** Find the area of a rectangular movie screen that is 50 feet long and 40 feet high.
- **86.** How much fencing will a rancher need for a rectangular cattle lot that measures 80 feet by 120 feet?
- **88.** Find the perimeter of a triangular picture frame that measures x inches by x inches by (x 14) inches.
- **90.** How much interest will a \$12,000 certificate of deposit earn in 1 year at a rate of 8% simple interest? Use *I* = *PRT*.
- **92.** Mario's Pizza sells one 16" cheese pizza or two 10" cheese pizzas for \$9.99. Which deal gives you more pizza? Use $A = \pi r^2$ with $\pi \approx 3.14$.



- **94.** Convert Nome, Alaska's, 18°F high temperature to Celsius. Use $C = \frac{5}{9}(F - 32)$.
- **96.** How many cubic meters does a space shuttle cargo compartment have if its dimensions are 8 meters long by 4 meters wide by 3 meters high? Use V = lwh.
- **98.** Find the volume. Use V = lwh.



101. -4 - (-12)

104. 8 + (-8)

Concept Extensions

If the expression on the left side of the equal sign is equivalent to the right, write "correct." If not, write "incorrect" and then write an expression that is equivalent to the left side. See the second Concept Check in this section.

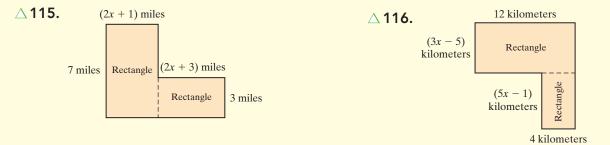
105. $5(3x-2) \stackrel{?}{=} 15x-2$ **106.** $2(xy) \stackrel{?}{=} 2x \cdot$ **107.** $7x - (x+2) \stackrel{?}{=} 7x - x + 2$ **108.** 4(y-3) + 2

Review the commutative, associative, and distributive properties. Then identify which property allows us to write the equivalent expression on the right side of the equal sign.

- **109.** 6(2x 3) + 5 = 12x 18 + 5
- **111.** -7 + (4 + y) = (-7 + 4) + y

113. If *x* is a whole number, which expression is the largest: 2x, 5x, or $\frac{1}{3}x$? Explain your answer.

Find the area of each figure.



To appraise the value of a large tree in landscaping, the trunk area is used. The trunk area A is calculated with the formula $A = 0.7854d^2$, where d is the diameter of the tree.

117. *Tane Mahuta* is the name of New Zealand's largest known living Kauri tree. Its trunk has a diameter of 173 inches. Use the formula to find the trunk area of this tree. Round your result to the nearest tenth. (*Source*: New Zealand Parks)



Simplify.

118. Lost Monarch, which was only discovered in 1998, is a coast redwood tree in northern California. It is located among other giant redwoods in "The Grove of Titans," in Jedediah Smith Redwoods State Park. This mammoth tree has confirmed diameter of 312 inches. Use the formula to find the trunk area of this tree. Round your result to the nearest tenth. (*Source:* Sierra Club)



110. 9 + 7x + (-2) = 7x + 9 + (-2)

114. If x is a whole number, which expression is the

smallest: 2x, 5x, or $\frac{1}{3}x$? Explain your answer.

112. (x + y) + 11 = 11 + (x + y)

119. 9684q - 686 - 4860q + 12,960

11.2 Solving Equations: The Addition Property

Objectives

- A Determine Whether a Given Number Is a Solution of an Equation.
- B Use the Addition Property of Equality to Solve Equations.

Frequently in this book we have written statements like 7 + 4 = 11 or Area = length · width. Each of these statements is called an **equation.** An equation is of the form

expression = expression

An equation can be labeled as

equal sign $x + 7 \stackrel{\downarrow}{=} 10$ $\uparrow \uparrow \uparrow$ left side right side

It is very important to know the difference between an **expression** and an **equation**. An equation contains an equal sign and an expression does not.

| | Equations | Expressions | |
|-------|---------------|------------------|----------------|
| equal | 7x = 6x + 4 | 7x - 6x + 4 | no equal signs |
| signs | 3(3y-5) = 10y | y - 1 + 11y - 21 |) |

Objective A Determining Whether a Number Is a Solution

When an equation contains a variable, finding which values of the variable make an equation a true statement is called **solving** the equation for the variable. A **solution** of an equation is a value for the variable that makes the equation a true statement. For example, 2 is a solution of the equation x + 5 = 7 since replacing x with 2 results in the *true* statement 2 + 5 = 7. Similarly, 3 is not a solution of x + 5 = 7 since replacing x with 3 results in the *false* statement 3 + 5 = 7.

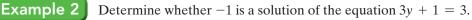
Example 1 Determine whether 6 is a solution of the equation 4(x - 3) = 12.

Solution: We replace *x* with 6 in the equation.

4(x - 3) = 12 \downarrow $4(6 - 3) \stackrel{?}{=} 12 \quad \text{Replace } x \text{ with } 6.$ $4(3) \stackrel{?}{=} 12 \quad \text{True}$

Since 12 = 12 is a true statement, 6 *is* a solution of the equation.

Work Practice 1



Solution:

3y + 1 = 3 $3(-1) + 1 \stackrel{?}{=} 3$ $-3 + 1 \stackrel{?}{=} 3$ $-2 \stackrel{?}{=} 3$ False

Since -2 = 3 is false, -1 is *not* a solution of the equation.

Work Practice 2

Practice 2

Practice 1

3(y-6) = 6.

Determine whether 4 is a

solution of the equation

Determine whether -2 is a solution of the equation -4x - 3 = 5.

Answers 1. no 2. yes

Objective **B** Using the Addition Property to Solve Equations

To solve an equation, we use properties of equality to write simpler equations, all equivalent to the original equation, until the final equation has the form

x = **number** or **number** = x

Equivalent equations have the same solution, so the word "number" above represents the solution of the original equation. The first property of equality to help us write simpler, equivalent, equations is the **addition property of equality**.

Addition Property of Equality

Let a, b, and c represent numbers. Then

a = band a + c = b + care equivalent equations. Also, a = band a - c = b - care equivalent equations.

In other words, the **same number** may be **added to or subtracted from both sides** of an equation without changing the solution of the equation.

A good way to visualize a true equation is to picture a balanced scale. Since it is balanced, each side of the scale weighs the same amount. Similarly, in a true equation the expressions on each side have the same value. Picturing our balanced scale, if we add the same weight to each side, the scale remains balanced.



Example 3 Solve: x - 2 = 1 for x.

Solution: To solve the equation for x, we need to rewrite the equation in the form x = number. In other words, our goal is to get x alone on one side of the equation. To do so, we add 2 to both sides of the equation.

x - 2 = 1 x - 2 + 2 = 1 + 2 Add 2 to both sides of the equation. x + 0 = 3 Replace -2 + 2 with 0. x = 3 Simplify by replacing x + 0 with x.

Check: To check, we replace *x* with 3 in the *original* equation.

x - 2 = 1 Original equation $3 - 2 \stackrel{?}{=} 1$ Replace x with 3. $1 \stackrel{?}{=} 1$ True

Since 1 = 1 is a true statement, 3 is the solution of the equation.

Work Practice 3

Helpful Hint

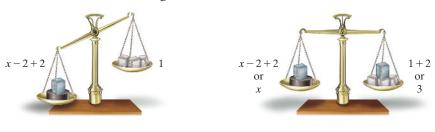
Note that it is always a good idea to check the solution in the *original* equation to see that it makes the equation a true statement.

Practice 3

Solve the equation for *y*: y - 5 = -3 Let's visualize how we used the addition property of equality to solve the equation in Example 3. Picture the original equation, x - 2 = 1, as a balanced scale. The left side of the equation has the same value as the right side.



If the same weight is added to each side of a scale, the scale remains balanced. Likewise, if the same number is added to each side of an equation, the left side continues to have the same value as the right side.



Solution: To get x alone on one side of the equation, we subtract 1 from both

Helpful

Remember that

we can get the variable alone

on either side of the equa-

tion. For example, the equations x = 2 and 2 = x both

have the solution of 2.

Replace 1 - 1 with 0.

Simplify.



Solve: -1 = z + 9



Example 5 Solve: y - 1.2 = -3.2 - 6.6

Example 4

Check:

sides of the equation.

-8 = x + 1

-9 = x + 0

 $-8 \stackrel{?}{=} -9 + 1$ Replace x with -9.

True

-9 = x

-8 = x + 1

 $-8 \stackrel{?}{=} -8$

The solution is -9.

Work Practice 4

Solution: First we simplify the right side of the equation.

Solve: -8 = x + 1

-8 - 1 = x + 1 - 1 Subtract 1 from both sides.

y - 1.2 = -3.2 - 6.6y - 1.2 = -9.8

Next, we get *y* alone on the left side by adding 1.2 to both sides of the equation.

y - 1.2 + 1.2 = -9.8 + 1.2 Add 1.2 to both sides. y = -8.6 Simplify.

Check to see that -8.6 is the solution.

Work Practice 5

Concept Check What number should be added to or subtracted from both sides of the equation in order to solve the equation -3.75 = y + 2.1?

Practice 5

Solve: x - 2.6 = -1.8 - 5.9

Answers 4. -10 5. -5.1

Concept Check Answer subtract 2.1 from both sides

Example 6 Solve: 5x + 2 - 4x = 7 - 9

Solution: First we simplify each side of the equation separately.

$$5x + 2 - 4x = 7 - 9$$

$$5x - 4x + 2 = 7 - 9$$

$$1x + 2 = -2$$

To get *x* alone on the left side, we subtract 2 from both sides.

1x + 2 - 2 = -2 - 21x = -4 or x = -4

Check to verify that -4 is the solution.

Work Practice 6

Example 7 Solve: $\frac{7}{8} = y - \frac{1}{2}$

Solution: We use the addition property of equality to add
$$\frac{1}{2}$$
 to both sides.

 $\frac{7}{8} = y - \frac{1}{2}$ $\frac{7}{8} + \frac{1}{2} = y - \frac{1}{2} + \frac{1}{2}$ Add $\frac{1}{2}$ to both sides. $\frac{7}{8} + \frac{4}{8} = y$ Simplify. $\frac{11}{8} = y$ Simplify.

Check to see that $\frac{11}{8}$ is the solution. (Although $\frac{11}{8} = 1\frac{3}{8}$, we will leave solutions as improper fractions.)

Work Practice 7

Example 8 Solve: 3(3x - 5) = 10x

Solution: First we multiply on the left side to remove the parentheses.

3(3x - 5) = 10x $3 \cdot 3x - 3 \cdot 5 = 10x$ Use the distributive property. 9x - 15 = 10x

Now we subtract 9x from both sides.

9x - 15 - 9x = 10x - 9x Subtract 9x from both sides. -15 = 1x or x = -15 Simplify.

Work Practice 8

Recall that the addition property of equality allows us to add or subtract the same number to or from both sides of an equation. Let's see how adding the same number to both sides of an equation also allows us to subtract the same number from both sides. To do so, let's add (-c) to both sides of a = b. Then we have

a + (-c) = b + (-c)

which is the same as a - c = b - c, and there we have it.

Practice 6 Solve: -6y + 1 + 7y = 6 - 11

Practice 7 Solve: $\frac{2}{3} = x - \frac{4}{9}$

Practice 8 Solve: 13x = 4(3x - 1)

Answers 6. -6 7. $\frac{10}{9}$ 8. -4

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank.

| equation | addition | simplifying |
|----------|------------|-------------|
| solving | equivalent | expression |

- 1. The equations x + 6 = 10 and x + 6 6 = 10 6 are called ______ equations.
- The difference between an equation and an expression is that a(n) ______ contains an equal sign, while a(n) ______ does not.
- 3. The process of writing -3x + 10x as 7x is called ______ the expression.
- 4. For the equation x 1 = -21, the process of finding that -20 is the solution is called ______ the equation.
- 5. By the _____ property of equality, x = -2 and x + 7 = -2 + 7 are equivalent equations.

Martin-Gay Interactive Videos
Watch the section lecture video and answer the following questions.
Objective A 6. From the lecture before Example 1, what does an equation have that an expression does not?
Objective B 7. In the lecture before Example 2, what does the addition property of equality mean in words?
8. When solving Example 7, what must be done before applying the addition property of equality?

11.2 Exercise Set MyLab Math

Objective A Decide whether the given number is a solution of the given equation. See Examples 1 and 2.

Is 10 a solution of x - 8 = 2?
 Is 9 a solution of y - 2 = 7?
 Is -5 a solution of x + 12 = 17?
 Is -7 a solution of a + 23 = -16?
 Is -8 a solution of -9f = 64 - f?
 Is -6 a solution of -3k = 12 - k?
 Is 3 a solution of 5(c - 5) = -10?
 Is 1 a solution of 2(b - 3) = 10?

Objective B Solve. Check each solution. See Examples 3 through 7.

| 9. $a + 5 = 23$ | 10. $f + 4 = -6$ | 11. $d - 9 = -17$ |
|------------------------------|---------------------------|--|
| 12. <i>s</i> - 7 = 15 | • 13. $7 = y - 2$ | 14. $1 = y + 7$ |
| 15. $-12 = x + 4$ | 16. $-10 = z - 15$ | 17. $x + \frac{1}{2} = \frac{7}{2}$ |

| 18. $x + \frac{1}{3} = \frac{4}{3}$ | 19. $y - \frac{3}{4} = -\frac{5}{8}$ | 20. $y - \frac{5}{6} = -\frac{11}{12}$ |
|--|---|---|
| 21. $x - 3 = -1 + 4$ | 22. $y - 8 = -5 - 1$ | 23. $-7 + 10 = m - 5$ |
| 24. 1 - 8 = <i>n</i> + 2 | 25. $x - 0.6 = 4.7$ | 26. <i>y</i> - 1.2 = 7.5 |
| 27. $-2 - 3 = -4 + x$ | 28. 7 - (-10 | (0) = x - 5 |
| 29. $y + 2.3 = -9.2 - 8.6$ | 30. <i>x</i> + 4.7 = | = -7.5 - 3.4 |
| 31. $-8x + 4 + 9x = -1 + 7$ | 32. $3x - 2x$ | +5 = 5 - 2 |
| 33. $5 + (-12) = 5x - 7 - 4x$ | 34. 11 + (-) | 15) = 6x - 4 - 5x |
| 35. $7x + 14 - 6x = -4 + (-10)$ | 36. $-10x + 10x$ | 11x + 5 = -9 + (-5) |

Solve. First multiply to remove parentheses. See Example 8.

| 37. $2(5x - 3) = 11x$ | 38. $6(3x + 1) = 19x$ | 39. $3y = 2(y + 12)$ |
|------------------------------|-------------------------------|------------------------------|
| 40. $17x = 4(4x - 6)$ | 41. $21y = 5(4y - 6)$ | 42. $28z = 9(3z - 2)$ |
| 43. $-3(-4-2z) = 7z$ | 44. $-2(-1 - 3y) = 7y$ | |

Review

Perform each indicated operation. See Section 10.4.

| 45. $\frac{-7}{-7}$ | 46. $\frac{4.2}{4.2}$ | 47. $\frac{1}{3} \cdot 3$ |
|----------------------------------|--|--|
| 48. $\frac{1}{5} \cdot 5$ | 49. $-\frac{2}{3} \cdot -\frac{3}{2}$ | 50. $-\frac{7}{2} \cdot -\frac{2}{7}$ |

Concept Extensions

What number should be added to or subtracted from both sides of each equation in order to solve the equation?

51. $\frac{2}{3} + x = \frac{1}{12}$ **52.** 12.5 = -3.75 + x

53.
$$-\frac{1}{7} = -\frac{4}{5} + x$$
 54. $9.1 = 5.9 + x$

55. In your own words, explain what is meant by the phrase "a number is a solution of an equation."

56. In your own words, explain how to check a possible solution of an equation.

Solve.

57. x - 76,862 = 86,102

58. -968 + 432 = 86y - 508 - 85y

A football team's total offense T is found by adding the total passing yardage P to the total rushing yardage R: T = P + R.

- **59.** During the 2016 regular football season, the Super Bowl Champion New England Patriots' total offense was 6180 yards. The Patriots' passing yardage for the season was 4308 yards. How many yards did the Patriots gain by rushing during the regular season? (*Source:* National Football League)
- **60.** During the 2016 regular football season, the Houston Texans' total offense was 5035 yards. The Texans' rushing yardage for the season was 1859 yards. How many yards did the Texans gain by passing during the regular season? (*Source:* National Football League)

In accounting, a company's annual net income I can be computed using the relation I = R - E, where R is the company's total revenues for the year and E is the company's total expenses for the year.

- **61.** At the end of fiscal year 2017, Kohl's has a net income of \$556,000,000. During the year, Kohl's has total expenses of \$18,130,000,000. What were Kohl's total revenues for the year? (*Source:* Kohl's Corporation)
- **62.** At the end of fiscal year 2017, Target had a net income of \$2,670,000,000. During the year, Target had total expenses of \$66,825,000,000. What were Target's total revenues for the year? (*Source:* Target Corporation)

11.3 Solving Equations: The Multiplication Property C **Objective A** Using the Multiplication Property to Solve **Objective** Equations 🜔 A Use the Multiplication Property to Solve Although the addition property of equality is a powerful tool for helping us solve Equations. D equations, it cannot help us solve all types of equations. For example, it cannot help us solve an equation such as 2x = 6. To solve this equation, we use a second property of equality called the multiplication property of equality. **Multiplication Property of Equality** Let a, b, and c represent numbers and let $c \neq 0$. Then Also, a = ba = band $\frac{a}{c} = \frac{b}{c}$ and $a \cdot c = b \cdot c$ are equivalent equations. are equivalent equations.

In other words, both sides of an equation may be multiplied or divided by the same nonzero number without changing the solution of the equation.

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Picturing again our balanced scale, if we multiply or divide the weight on each side by the same nonzero number, the scale (or equation) remains balanced.



To solve 2x = 6 for x, we use the multiplication property of equality to divide both sides of the equation by 2, and simplify as follows:

$$2x = 6$$

$$\frac{2x}{2} = \frac{6}{2}$$
Divide both sides by 2.

$$\frac{2}{2} \cdot x = 3$$
1 · x = 3
x = 3
Example 1 Solve: $-5x = 15$
Solution: To get x by itself, we divide both sides by -5 .
 $-5x = 15$ Original equation
 $\frac{-5x}{-5} = \frac{15}{-5}$
 $\frac{-5}{-5} \cdot x = \frac{15}{-5}$ Divide both sides by -5
1 · x = -3 Simplify.
x = -3
Check: To check, we replace x with -3 in the original equation.
 $-5x = 15$ Original equation
 $-5(-3) \stackrel{?}{=} 15$ Let $x = -3$.
 $15 \stackrel{?}{=} 15$ True
The solution: To get y alone, we divide both sides of the equation by 2.
 $-8 = 2y$
 $\frac{-8}{2} = \frac{2y}{2}$ Divide both sides by 2.
 $-4 = 1 \cdot y$ or $y = -4$
Check to see that -4 is the solution.
• Work Practice 2
Names
 $1 - 6 \stackrel{?}{=} 2 - 2$

Practice 3 Solve: -0.3y = -27 **Example 3** Solve: -1.2x = -36

Solution: We divide both sides of the equation by the numerical coefficient of x, which is -1.2.

$$-1.2x = -36$$
$$\frac{-1.2x}{-1.2} = \frac{-36}{-1.2}$$
$$1 \cdot x = 30$$
$$x = 30$$

Check to see that 30 is the solution.

Work Practice 3

Example 4 Solve: $\frac{3}{5}a = 9$

Solution: Recall that the product of a number and its reciprocal is 1. To get *a* alone then, we multiply both sides by $\frac{5}{3}$, the reciprocal of $\frac{3}{5}$.

$$\frac{3}{5}a = 9$$

$$\frac{5}{3} \cdot \frac{3}{5}a = \frac{5}{3} \cdot 9$$
Multiply both sides by $\frac{5}{3}$.
$$1 \cdot a = \frac{5 \cdot \frac{9}{3}}{\frac{3}{5} \cdot 1}$$
Multiply.
$$a = 15$$
Simplify.

Check: To check, we replace *a* with 15 in the original equation.

$$\frac{3}{5}a = 9 \quad \text{Original equation}$$
$$\frac{3}{5} \cdot 15 \stackrel{?}{=} 9 \quad \text{Replace } a \text{ with } 15.$$
$$\frac{3}{5} \cdot \frac{15}{1} \stackrel{?}{=} 9 \quad \text{Multiply.}$$
$$9 \stackrel{?}{=} 9 \quad \text{True}$$
Since 9 = 9 is true, 15 is the solution of $\frac{3}{5}a = 9$.

Work Practice 4

Practice 4 Solve: $\frac{5}{7}b = 25$

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Example 5 Solve: $-\frac{1}{4}x = \frac{1}{8}$ **Solution:** We multiply both sides of the equation by $-\frac{4}{1}$, the reciprocal of $-\frac{1}{4}$. $-\frac{1}{4}x = \frac{1}{8}$ $-\frac{4}{1} \cdot -\frac{1}{4}x = -\frac{4}{1} \cdot \frac{1}{8}$ Multiply both sides by $-\frac{4}{1}$. $1 \cdot x = -\frac{\frac{1}{4} \cdot 1}{1 \cdot \frac{8}{2}}$ Multiply. $x = -\frac{1}{2}$ Simplify. Check to see that $-\frac{1}{2}$ is the solution. **Work Practice 5**

Concept Check Which operation is appropriate for solving each of the following equations, addition or division?

a. 6 = -4x **b.** 6 = x - 4

We often need to simplify one or both sides of an equation before applying the properties of equality to get the variable alone.

Example 6 Solve: 3y - 7y = 12 **Solution:** First we combine like terms. 3y - 7y = 12 -4y = 12 Combine like terms. $\frac{-4y}{-4} = \frac{12}{-4}$ Divide both sides by -4. y = -3 Simplify. **Check:** We replace y with -3. 3y - 7y = 12 $3(-3) - 7(-3) \stackrel{?}{=} 12$ $-9 + 21 \stackrel{?}{=} 12$ $12 \stackrel{?}{=} 12$ True The solution is -3. **Work Practice 6** Practice 6 Solve: 2m - 4m = 10

Answers

5.
$$-\frac{4}{7}$$
 6. -5

Concept Check Answers a. division b. addition

Chapter 11 | Introduction to Algebra

Practice 7

Solve: -3a + 2a = -8 + 6

Solve: -2z + z = 11 - 5Example 7

Solution: We simplify both sides of the equation first.

$$-2z + z = 11 - 5$$

$$-1z = 6$$
 Combine like terms.

$$\frac{-1z}{-1} = \frac{6}{-1}$$
 Divide both sides by -1.

$$z = -6$$
 Simplify.

Check to see that -6 is the solution.

Example 8 Solve: $\frac{z}{-4} = 11 - 5$

Work Practice 7

Practice 8

Solve: $-8 + 6 = \frac{a}{3}$

Solution: Simplify the right side of the equation first.

$$\frac{z}{-4} = 11 - 5$$
$$\frac{z}{-4} = 6$$

Next, to get z alone, multiply both sides by -4.

$$-4 \cdot \frac{z}{-4} = -4 \cdot 6$$

Multiply both sides by -4.
$$\frac{-4}{-4} \cdot z = -4 \cdot 6$$

$$1z = -24 \text{ or } z = -24$$

Check to see that -24 is the solution.
Work Practice 8

Answers **7.** 2 **8.** −6

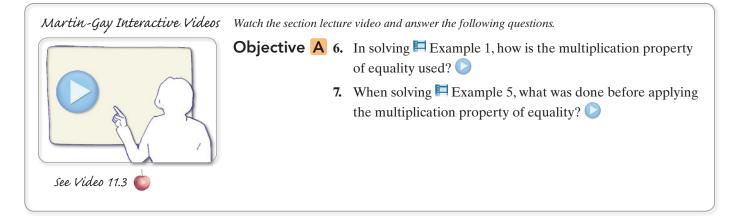
Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank.

| equation | multiplication | simplifying |
|----------|----------------|-------------|
| solving | equivalent | expression |

1. The equations -3x = 51 and $\frac{-3x}{-3} = \frac{51}{-3}$ are called ______ equations.

- 2. The difference between an equation and an expression is that a(n) ______ contains an equal sign, while a(n) _____ does not.
- 3. The process of writing -3x + x as 2x is called ______ the expression.
- 4. For the equation -5x = -20, the process of finding that 4 is the solution is called ______ the equation.
- 5. By the _____ property of equality, y = 8 and $3 \cdot y = 3 \cdot 8$ are equivalent equations.



6. 0.8x = -8

11.3 Exercise Set MyLab Math 🕗

Objective A Solve. See Examples 1 through 5.

- **1.** 5x = 20 **2.** 6y = 48 **3.** -3z = 12
- **4.** -2x = 26 **5.** 0.4y = -12
- **7.** 2z = -34 **8.** 7y = -21 **9.** -0.3x = -15
- **10.** -0.4z = -16 **11.** $10 = \frac{2}{5}x$ **12.** $27 = \frac{3}{7}x$
- **13.** $\frac{1}{6}y = -5$ **14.** $\frac{1}{8}y = -3$ **15.** $\frac{5}{6}x = \frac{5}{18}$
- **16.** $\frac{4}{7}y = \frac{8}{21}$ **17.** $-\frac{2}{9}z = \frac{4}{27}$ **18.** $-\frac{3}{4}v = \frac{9}{14}$

Solve. First combine any like terms on each side of the equation. See Examples 6 and 7.

19. 2w - 12w = 40**20.** -8y + y = 35**21.** 16 = 10t - 8t**22.** 100 = 15y - 5y**23.** 2z = 1.2 + 1.4**24.** 3x = 1.1 + 0.7**25.** 4 - 10 = -3z**26.** 12 - 20 = -4x

Mixed Practice Solve. See Examples 1 through 8.

27. -7x = 0 **28.** -20y = 0 **29.** 0.4 = -8z **30.** 0.5 = -20x **31.** $\frac{8}{5}t = -\frac{3}{8}$ **32.** $\frac{7}{4}r = -\frac{2}{7}$ **33.** $-\frac{3}{5}x = -\frac{6}{15}$ **34.** $-\frac{6}{7}y = -\frac{1}{14}$

35.
$$-3.6 = -0.9u + 0.3u$$

36. $-5.4 = -1.4y + 1.3y$
37. $5 - 5 = 2x + 7x$
38. $12 + (-12) = 7x + 8x$
39. $-42 + 20 = -2x + 13x$
40. $-4y + 9y = -20 + 15$
41. $-3x - 3x = 50 - 2$
42. $5y - 9y = -14 + (-14)$
43. $23x - 25x = 7 - 9$
44. $6x - 8x = 12 - 22$
45. $\frac{1}{4}x - \frac{5}{8}x = 20 - 47$
46. $\frac{1}{2}x - \frac{4}{5}x = 10 - 19$
47. $18 - 11 = \frac{x}{5}$
48. $14 - 9 = \frac{x}{12}$
49. $\frac{x}{-4} = 1 - (-6)$
50. $\frac{y}{-6} = 6 - (-1)$

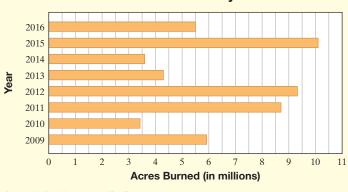
Review

C

Evaluate each expression when x = 5*. See Section 11.1.*

51. 3x + 10 **52.** 40x **53.** $\frac{x-3}{2}$ **54.** 7x - 20 **55.** $\frac{3x+5}{x-7}$ **56.** $\frac{2x-1}{x-8}$

The bar graph shows the number of acres burned by wildfires in the United States in recent years. Use the bar graph to answer Exercises 57 through 60. See Section 9.1.





Source: National Interagency Fire Center

- **57.** During which year shown is the number of acres burned by wildfires the greatest?
- **58.** During which year shown is the number of acres burned by wildfires the least?
- **59.** Use the length of the bar to estimate the number of acres burned by wildfires in 2012.
- **60.** Describe any trends shown in this graph.

)

| What operation is appropriate for solving each equation: addition or division? See the Concept Check in this section. | | | | |
|---|-----------------------|-----------------------|--------------------------|--|
| 61. 12 = <i>x</i> - 5 | 62. $12 = -5x$ | 63. $-7x = 21$ | 64. $-7 + x = 21$ | |

65. Why does the multiplication property of equality not allow us to divide both sides of an equation by zero?

Concept Extensions

66. Is the equation -x = 6 solved for the variable? Explain why or why not.

The equation $d = r \cdot t$ describes the relationship between distance d in miles, rate r in miles per hour, and time t in hours. If necessary, round answers to the nearest tenth.

- **67.** The distance between New Orleans, Louisiana, and Memphis, Tennessee, by road is 390 miles. How long will it take to drive from New Orleans to Memphis if the driver maintains a speed of 60 miles per hour? (*Source: World Almanac*)
- **69.** The distance between Cleveland, Ohio, and Indianapolis, Indiana, by road is 294 miles. At what speed should a driver drive if he or she would like to make the trip in 5 hours? (*Source: World Almanac*)
- **68.** The distance between Boston, Massachusetts, and Milwaukee, Wisconsin, by road is 1050 miles. How long will it take to drive from Boston to Milwaukee if the driver maintains a speed of 55 miles per hour? (*Source: World Almanac*)
- **70.** The distance between St. Louis, Missouri, and Minneapolis, Minnesota, by road is 552 miles. If it took 9 hours to drive from St. Louis to Minneapolis, what was the driver's average speed? (*Source: World Almanac*)

Solve.

71. -0.025x = 91.2

72. 3.6y = -1.259 - 3.277

Solve.

73.
$$\frac{y}{72} = -86 - (-1029)$$

75. $\frac{x}{-2} = 5^2 - |-10| - (-9)$

74.
$$\frac{x}{-13} = 4^6 - 5^7$$

76.
$$\frac{y}{10} = (-8)^2 - |20| + (-2)^2$$

Sections 11.1–11.3

Expressions and Equations

| Answers | For the table below, identify each as an expression | on or an equation. |
|------------|---|---|
| 1. | Expression or Equation | |
| | 1. $7x - 5y + 14$ | |
| 2. | 2. $7x = 35 + 14$ | |
| | 3. $3(x-2) = 5(x+1) - 17$ | |
| 3 | 4. $-9(2x+1) - 4(x-2) + 14$ | |
| | Fill in each blank with "simplify" or "solve." | |
| 5. | 5. To an expression, we combine any | y like terms. |
| 6. | | |
| _7 | 6. To an equation, we use the proper variable that makes the equation a true state | |
| 8. | | |
| 9. | Evaluate each expression when $x = -1$ and $y =$ | |
| 10. | 7. $y - x$ 8. $\frac{8y}{4x}$ | 9. $5x + 2y$ 10. $\frac{y^2 + x}{2x}$ |
| <u>11.</u> | Simplify each expression by combining like term | 15. |
| 12. | 11. $7x + x$ | 12. 6 <i>y</i> - 10 <i>y</i> |
| 13. | | |
| 14. | 13. $2a + 5a - 9a - 2$ | 14. $3x - y + 4 - 5x + 4y - 11$ |
| 15. | | |
| | Multiply and simplify if possible. | |
| 16. | 15. $-2(4x + 7)$ | 16. $-3(2x - 10)$ |
| 730 | | |

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|---|--|------------|
| 17. $5(y + 2) - 20$ | 18. $12x + 3(x - 6) - 13$ | _17 |
| | | <u>18.</u> |
| \triangle 19. Find the area. | \triangle 20. Find the perimeter. | <u> </u> |
| Rectangle 3 meters $(4x-2)$ meters | Square
5 <i>y</i> inches | 20. |
| | | <u>21.</u> |
| <i>Solve and check.</i> 21. $x + 7 = 20$ | 22. $-11 = x - 2$ | 22. |
| | | 23. |
| 23. $n - \frac{2}{5} = \frac{3}{10}$ | 24. $-7y = 0$ | <u>24.</u> |
| | | <u>25.</u> |
| 25. $12 = 11x - 14x$ | 26. $\frac{3}{5}x = 15$ | <u>26.</u> |
| | 5 | 27. |
| 27. $x - 1.2 = -4.5 + 2.3$ | 28. $8y + 7y = -45$ | <u>28.</u> |
| | | 29. |
| 29. $6 - (-5) = x + 5$ | 30. $-0.2m = -1.6$ | <u>30.</u> |
| | | <u>31.</u> |
| 31. $-\frac{2}{3}n = \frac{6}{11}$ | 32. 11 <i>x</i> = 55 | <u>32.</u> |

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11.4 Solving Equations Using Addition and Multiplication Properties

Objectives

A Solve Equations Using Addition and Multiplication Properties.

B Solve Equations Containing Parentheses.

C Write Numerical Sentences as Equations.

Practice 1

Solve: 5y - 8 = 17

Objective A Solving Equations Using Addition and Multiplication Properties 🜔

We will now solve equations using more than one property of equality. To solve an equation such as 2x - 6 = 18, we will first get the variable term 2x alone on one side of the equation.

Example 1 Solve: 2x - 6 = 18

Solution: We start by adding 6 to both sides to get the variable term 2x alone.

2x - 6 = 18 2x - 6 + 6 = 18 + 6 Add 6 to both sides. 2x = 24 Simplify.

To finish solving, we divide both sides by 2.

 $\frac{2x}{2} = \frac{24}{2}$ Divide both sides by 2. $1 \cdot x = 12$ Simplify. x = 12

Check:

2x - 6 = 18 $2(12) - 6 \stackrel{?}{=} 18$ Replace x with 12 and simplify. $24 - 6 \stackrel{?}{=} 18$ $18 \stackrel{?}{=} 18$ True

The solution is 12.

Work Practice 1

Helpful Hint

Make sure you understand which property to use to solve an equation.

| Addition | | Understood multiplicat | lon |
|--------------------------------------|--------------------------|---------------------------------------|--|
| x + 2 = 10 | | 2x = 10 |) |
| To undo addition of 2, we subtract 2 | 2 from both sides. | To undo multiplication | of 2, we divide both |
| x + 2 - 2 = 10 - 2 | Use addition | sides by 2. | |
| x = 8 | property of
equality. | $\frac{2x}{2} = \frac{10}{2}$ $x = 5$ | Use multiplication property of equality. |
| Check: $x + 2 = 10$ | | | |
| $8 + 2 \stackrel{?}{=} 10$ | | Check: $2x = 10$ | |
| 10 [?] = 10 | True | $2 \cdot 5 \stackrel{?}{=} 10$ | |
| | | 10 ° 210 | True |

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Answer 1. 5 732 **Example 2** Solve: 17 - x + 3 = 15 - (-6)**Solution:** First we simplify each side of the equation.

$$17 - x + 3 = 15 - (-6)$$

$$20 - x = 21$$

Combine like terms on each side of the equation.

Next, we get the variable term alone on one side of the equation.

20 - x - 20 = 21 - 20Subtract 20 from both sides. -1x = 1Simplify. Recall that -x means -1x. $\frac{-1x}{-1} = \frac{1}{-1}$ Divide both sides by -1. $1 \cdot x = -1$ Simplify. x = -1

Check:

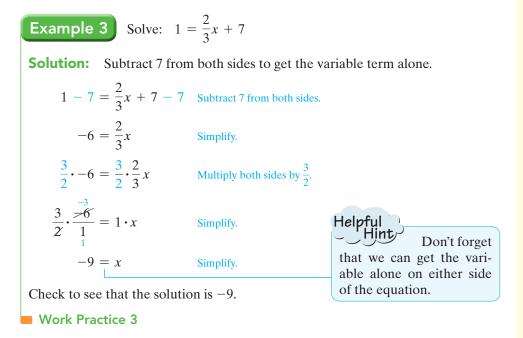
$$20 - x = 21$$

$$20 - (-1) \stackrel{?}{=} 21$$

$$21 \stackrel{?}{=} 21 \text{ True}$$

The solution is -1.

```
Work Practice 2
```

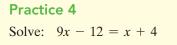


If an equation contains variable terms on both sides, we use the addition property of equality to get all the variable terms on one side and all the constants, or numbers, on the other side. **Practice 2** Solve: 7 - y + 3 = 20 - (-25)

Solve: $11 = \frac{3}{4}y + 20$

Practice 3

Chapter 11 | Introduction to Algebra



Example 4 Solution: 3a - 6 = a + 43a - 6 + 6 = a + 4 + 6Add 6 to both sides. 3a = a + 10Simplify. 3a - a = a + 10 - aSubtract *a* from both sides. 2a = 10Simplify. $\frac{2a}{2} = \frac{10}{2}$ Divide both sides by 2. a = 5Simplify.

Check to see that the solution is 5.

Work Practice 4

| Example 5 | Solve: | 7x + 3.2 | = 4x - 1.6 |
|-----------|--------|----------|------------|
| | | | |

Solution:

7x + 3.2 = 4x - 1.6 7x + 3.2 - 3.2 = 4x - 1.6 - 3.2Subtract 3.2 from both sides. 7x = 4x - 4.8Simplify. 7x - 4x = 4x - 4.8 - 4xSubtract 4x from both sides. 3x = -4.8Simplify. $\frac{3x}{3} = \frac{-4.8}{3}$ Divide both sides by 3. x = -1.6Simplify.

Check to see that -1.6 is the solution.

Example 6 Solve: 7(x - 2) = 9x - 6

7(x-2) = 9x - 6

other side.

Solution: First we apply the distributive property.

7x - 14 = 9x - 6 Apply the distributive property.

Work Practice 5

Objective B Solving Equations Containing Parentheses

If an equation contains parentheses, we must first use the distributive property to remove them.

Next, we move variable terms to one side of the equation and constants to the

| Practice 6 | |
|------------|--|
|------------|--|

Solve: 6(a - 5) = 8a - 12

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Practice 5

Solve: 8x + 4.2 = 10x - 11.6

7x - 14 - 9x = 9x - 6 - 9xSubtract 9x from both sides. -2x - 14 = -6Simplify. -2x - 14 + 14 = -6 + 14Add 14 to both sides. -2x = 8Simplify. $\frac{-2x}{-2} = \frac{8}{-2}$ Divide both sides by -2. x = -4Simplify.

Check to see that -4 is the solution.

Work Practice 6

You may want to use the steps shown below to solve equations.

Steps for Solving an Equation

- Step 1: If parentheses are present, use the distributive property.
- Step 2: Combine any like terms on each side of the equation.
- **Step 3:** Use the addition property of equality to rewrite the equation so that variable terms are on one side of the equation and constant terms are on the other side.
- **Step 4:** Use the multiplication property of equality to divide both sides by the numerical coefficient of the variable to solve.
- **Step 5:** Check the solution in the *original equation*.

Example 7 Solve: 3(2x - 6) + 6 = 0

Solution:

| | 3(2x-6) + 6 = 0 | |
|----------|--|--|
| Step 1: | 6x - 18 + 6 = 0 | Apply the distributive property. |
| Step 2: | 6x - 12 = 0 | Combine like terms on the left side of the equation. |
| Step 3: | 6x - 12 + 12 = 0 + 12 | Add 12 to both sides. |
| | 6x = 12 | Simplify. |
| Step 4: | $\frac{6x}{6} = \frac{12}{6}$ | Divide both sides by 6. |
| | x = 2 | Simplify. |
| Step 5: | | |
| Check: | 3(2x-6)+6=0 | |
| | $3(2 \cdot 2 - 6) + 6 \stackrel{?}{=} 0$ | |
| | $3(4-6) + 6 \stackrel{?}{=} 0$ | |
| | $3(-2) + 6 \stackrel{?}{=} 0$ | |
| | $-6 + 6 \stackrel{?}{=} 0$ | |
| | $0 \stackrel{?}{=} 0$ | True |
| The solu | tion is 2. | |

Work Practice 7

Practice 7 Solve: 4(2x - 3) + 4 = 0

Answer 7. 1 Example 8

Solution:

a. The product of 7 and 6 is 42.

b. Twice the sum of 3 and 5 is equal to 16.

c. The quotient of -45 and 5 yields -9.

Objective C Writing Sentences as Equations 🕑

Next, we practice translating sentences into equations. Below are key words and phrases that translate to an equal sign:

| Key Words or Phrases | Examples | Symbols |
|----------------------|--|----------------------|
| equals | 3 equals 2 plus 1 | 3 = 2 + 1 |
| gives | the quotient of 10 and -5 gives -2 | $\frac{10}{-5} = -2$ |
| is/was | 17 minus 12 is 5 | 17 - 12 = 5 |
| yields | 11 plus 2 yields 13 | 11 + 2 = 13 |
| amounts to | twice -15 amounts to -30 | 2(-15) = -30 |
| is equal to | -24 is equal to 2 times -12 | -24 = 2(-12) |

Translate each sentence into an equation.

Practice 8

Translate each sentence into an equation.

- **a.** The difference of 110 and 80 is 30.
- **b.** The product of 3 and the sum of -9 and 11 amounts to 6.
- **c.** The quotient of 24 and -6 yields -4.

the product a. In words: 42 is of 7 and 6 Ţ Ţ Translate: $7 \cdot 6$ = 42 the sum of **b.** In words: twice is equal to 16 3 and 5 ↓ Ţ Ţ 2 (3 + 5)Translate: 16 the quotient **c.** In words: vields of -45 and 5 Ţ -45-9 Translate: _ Work Practice 8

8. a. 110 - 80 = 30b. 3(-9 + 11) = 6 c. $\frac{24}{-6} = -4$

Answers

<u>د</u>

Calculator Explorations Checking Possible Solutions

A calculator can be used to check possible solutions of equations. To do this, replace the variable by the possible solution and evaluate each side of the equation separately. For example, to see whether 7 is a solution of the equation 52x = 15x + 259, replace x with 7 and use your calculator to evaluate each side separately.

| Equation: $52x = 15x + 259$ |
|--|
| $52 \cdot 7 \stackrel{?}{=} 15 \cdot 7 + 259$ |
| Evaluate left side: 52×7 then = or ENTER. |
| Display: 364. |
| Evaluate right side: $15 \times 7 + 259$ then = |
| or ENTER. Display: 364. |

Since the left side equals the right side, 7 is a solution of the equation 52x = 15x + 259.

Use a calculator to determine whether the numbers given are solutions of each equation.

1. 76(x - 25) = -988; 12 **2.** -47x + 862 = -783; 35 **3.** x + 562 = 3x + 900; -170 **4.** 55(x + 10) = 75x + 910; -18 **5.** 29x - 1034 = 61x - 362; -21 **6.** -38x + 205 = 25x + 120; 25

Vocabulary, Readiness & Video Check

Use the choices below to fill in each blank. Some choices may be used more than once.

additionmultiplicationcombine like terms5(2x + 6) - 1 = 393x - 9 + x - 16distributive**1.** An example of an expression iswhile an example of an equation is.**2.** To solve $\frac{x}{-7} = -10$, we use the ______ property of equality.**3.** To solve x - 7 = -10, we use the ______ property of equality.**4.** To solve 9x - 6x = 10 + 6, first ______.**5.** To solve 5(x - 1) = 25, first use the _______ property.**6.** To solve 4x + 3 = 19, first use the _______ property of equality.

Martin-Gay Interactive Videos
 Watch the section lecture video and answer the following questions.
 Objective ▲ 7. In ■ Example 1, the number 1 is subtracted from the left side of the equation. What property tells us we must also subtract 1 from the right side? Why is it important to do the same thing to both sides?
 Objective B 8. From ■ Example 3, what is the first step when solving an equation that contains parentheses? What property do we use to perform this step?
 Objective C 9. What word or phrase translates to "equals" in ■ Example 5? In ■ Example 6?

11.4 Exercise Set MyLab Math

Objective A Solve each equation. See Examples 1 through 5.

1. 2x - 6 = 02. 3y - 12 = 03. 3n + 3.6 = 9.34. 4z + 0.8 = 5.25. 6 - n = 106. 7 - y = 97. $-\frac{2}{5}x + 19 = -21$ 8. $-\frac{3}{7}y - 14 = 7$ 9. 1.7 = 2y + 9.510. -5.1 = 3x + 2.411. 2n + 8 = 012. 8w + 40 = 013. 3x - 7 = 4x + 514. 7x - 1 = 8x + 4**0** 15. 10x + 15 = 6x + 316. 5x - 3 = 2x - 1817. 9 - 3x = 14 + 2x18. 4 - 7m = -3m + 419. -1.4x - 2 = -1.2x + 720. 5.7y + 14 = 5.4y - 1021. x + 20 + 2x = -10 - 2x - 1522. 2x + 10 + 3x = -12 - x - 2023. 40 + 4y - 16 = 13y - 12 - 3y24. 19x - 2 - 7x = 31 + 6x - 15

| Objective B Solve each equation. See Examples 6 and 7. | | | |
|---|---------------------------------------|--------------------------------------|--|
| 25. $-2(y+4) = 2$ | 26. $-1(y+3) = 10$ | 27. $3(x-1) - 12 = 0$ | |
| 28. $2(x+5) + 8 = 0$ | 29. $35 - 17 = 3(x - 2)$ | 30. $22 - 42 = 4(x - 1)$ | |
| 31. $2(y-3) = y - 6$ | 32. $3(z+2) = 5z + 6$ | 33. $2t - 1 = 3(t + 7)$ | |
| 34. $-4 + 3c = 4(c + 2)$ | 35. $3(5c + 1) - 12 = 13c + 3$ | 36. $4(3t + 4) - 20 = 3 + 5t$ | |

Mixed Practice (Sections 11.1, 11.2, 11.3, and 11.4) Solve each equation. See Examples 1 through 7.

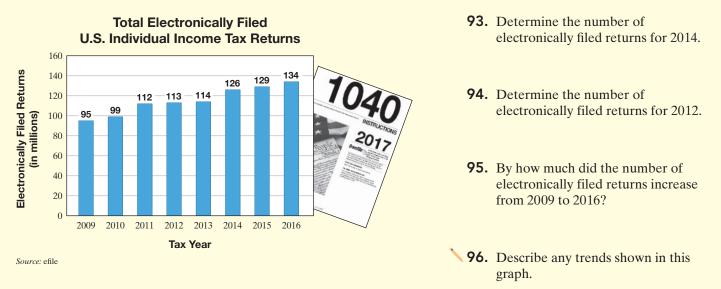
| 37. $-4x = 44$ | 38. $-3x = 51$ | 39. $x + 9 = 2$ |
|--|---|--|
| 40. $y - 6 = -11$ | 41. 8 - b = 13 | 42. 7 - z = 15 |
| 43. 3 <i>r</i> + 4 = 19 | 44. 5 <i>m</i> + 1 = 46 | 45. $2x - 1 = -7$ |
| 46. 3 <i>t</i> − 2 = −11 | 47. $7 = 4c - 1$ | 48. $9 = 2b - 5$ |
| 49. $9a + 29 = -7$ | 50. $10 + 4\nu = -6$ | 51. $0 = 4x + 4$ |
| 52. $0 = 5y + 5$ | 53. $11(x-2) = 22$ | 54. $5(a-4) = 20$ |
| 55. $-7c + 1 = -20$ | 56. $-2b + 5 = -7$ | 57. $3(x-5) = -7 - 11$ |
| 58. $4(x-2) = -20 - 4$ | 59. $-5 + 7k = -13 + 8k$ | 60. $-7 + 9d = -17 + 10d$ |
| 61. $4x + 3 = 2x + 11$ | 62. $6y - 8 = 3y + 7$ | 63. $-8(n+2) + 17 = -6n - 5$ |
| 64. $-10(x+1) + 2 = -x + 10$ | 65. $\frac{3}{8}x + 14 = \frac{5}{8}x - 2$ | 66. $\frac{2}{7}x - 9 = \frac{5}{7}x - 15$ |
| 67. $10 + 5(z - 2) = -4z + 1$ | 68. $20 + 4(w - 5) = 5 - 2w$ | 69. $\frac{5}{8}a = \frac{1}{8}a + \frac{3}{4}$ |
| 70. $\frac{4}{9}a = \frac{1}{9}a + \frac{5}{6}$ | 71. $7(6 + w) = 6(w - 2)$ | 72. $6(5+c) = 5(c-4)$ |
| 73. $3 + 2(2n - 5) = 1$ | 74. $5 + 4(3x - 2) = 21$ | 75. $2(3z-2) - 2(5-2z) = 4$ |
| 76. $2(3w + 7) - 4(5 - 2w) = 6$ | 77. $-20 - (-50) = \frac{x}{9}$ | 78. $-2 - 10 = \frac{z}{10}$ |

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| 79. $12 + 5t = 6(t + 2)$ | 80. $4 + 3c = 2(c$ | + 2) | •81. $3(5c - 1) - 2 = 13c + 3$ |
|---|----------------------------|-------------------------|--|
| 82. $4(2t+5) - 21 = 7t - 6$ | 83. $10 + 5(z - 2)$ |) = 4z + 1 | 84. $14 + 4(w - 5) = 6 - 2w$ |
| Objective C Write each sentence as | s an equation. See Exa | mple 8. | |
| 85. The sum of -42 and 16 is -26. | | 86. The differen | ace of -30 and 10 equals -40 . |
| • 87. The product of -5 and -29 gives 2 | 145. | 88. The quotien | t of -16 and 2 yields -8 . |
| ● 89. Three times the difference of -14 to -48. | and 2 amounts | 90. The product | t of -2 and the sum of 3 and 12 is -30 . |
| 91. The quotient of 100 and twice 50 i | s equal to 1. | 92. Seventeen s | ubtracted from -12 equals -29 . |

Review

The following bar graph shows the number of U.S. federal individual income tax returns that are filed electronically during the years shown using efile. Use this graph to answer Exercises 93 through 96. Write number answers in millions and in standard form. See Section 9.1.



Concept Extensions

Using the steps for solving an equation, choose the next operation for solving the given equation.

97. 2x - 5 = -7

- **a.** Add 7 to both sides.
- **b.** Add 5 to both sides.
- **c.** Divide both sides by 2.

98. 3x + 2x = -x - 4

- a. Add 4 to both sides.
- **b.** Subtract 2*x* from both sides.
- **c.** Add 3*x* and 2*x*.

99. -3x = -12

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a. Divide both sides by -3.

b. Add 12 to both sides.

c. Add 3x to both sides.

100. 9 - 5x = 15

104. $3^2 \cdot x = (-9)^3$

106. $x + 45^2 = 54^2$

- **a.** Divide both sides by -5.
- **b.** Subtract 15 from both sides.
- **c.** Subtract 9 from both sides.

102. 37x + 1 = 9(4x - 7)

37x + 1 = 36x - 7

37x + 1 - 1 = 36x - 7 - 1

37x = 36x - 8

37x - 36x = 36x - 8 - 36xx = -8

- A classmate shows you steps for solving an equation. The solution does not check, but the classmate is unable to find the error. For each set of steps, check the solution, find the error, and correct it.
- **101.** 2(3x-5) = 5x 76x - 5 = 5x - 76x - 5 + 5 = 5x - 7 + 56x = 5x - 26x - 5x = 5x - 2 - 5xx = -2

Solve.

- **103.** $(-8)^2 + 3x = 5x + 4^3$
- **105.** $2^{3}(x + 4) = 3^{2}(x + 4)$
- **107.** A classmate tries to solve 3x = 39 by subtracting 3 from both sides of the equation. Will this step solve the equation for x? Why or why not?

108. A classmate tries to solve 2 + x = 20 by dividing both sides by 2. Will this step solve the equation for x? Why or why not?

The equation $C = \frac{5}{9}(F - 32)$ gives the relationship between Celsius temperatures C and Fahrenheit temperatures F.

- **109.** The highest recorded temperature in Australia occurred in January 1960 at Oodnadatta, South Australia. The temperature reached 50.7°C. Use the given equation to convert this temperature to degrees Fahrenheit. (Source: World Weather Centre at Perth)
- **111.** The lowest recorded temperature in Australia occurred in June 1994 at Charlotte Pass, New South Wales. The temperature plummeted to -23.0° C. Use the given equation to convert this temperature to degrees Fahrenheit. (Source: World Weather Centre at Perth)
- **110.** The highest recorded temperature in Africa occurred in July 1931 at Kebili, Tunisia. The temperature reached 55.0°C. Use the given equation to convert this temperature to degrees Fahrenheit. (Source: World Meteorological Organization)
- **112.** The lowest recorded temperature in North America occurred in February 1947 at Snag, Canada. The temperature plummeted to -63.0° C. Use the given equation to convert this temperature to degrees Fahrenheit. (Source: World Weather Centre at Perth)

11.5 Equations and Problem Solving

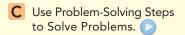
Objective A Writing Phrases as Algebraic Expressions 🕗

Now that we have practiced solving equations for a variable, we can extend considerably our problem-solving skills. We begin by writing phrases as algebraic expressions using the following key words and phrases as a guide:

| Addition | Subtraction | Multiplication | Division | Equal Sign |
|--------------|-----------------|----------------|------------|-------------|
| sum | difference | product | quotient | equals |
| plus | minus | times | divided by | gives |
| added to | subtracted from | multiply | into | is/was |
| more than | less than | twice | per | yields |
| increased by | decreased by | of | | amounts to |
| total | less | double | | is equal to |

Objectives

- A Write Phrases as Algebraic Expressions.
- B Write Sentences as Equations.

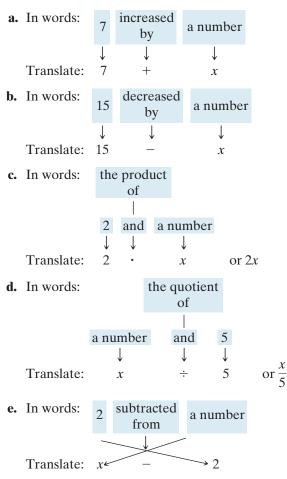


Example 1

Write each phrase as an algebraic expression. Use *x* to represent "a number."

- **a.** 7 increased by a number
- **c.** the product of 2 and a number
- **e.** 2 subtracted from a number

Solution:



- **b.** 15 decreased by a number
- **d.** the quotient of a number and 5
- **f.** the sum of 9 and twice a number

Practice 1

Write each phrase as an algebraic expression. Use *x* to represent "a number."

- **a.** twice a number
- **b.** 8 increased by a number
- **c.** 10 minus a number
- **d.** 10 subtracted from a number
- e. the quotient of 6 and a number
- **f.** the sum of 14 and triple a number

(Continued on next page)

Answers 1. a. 2x b. 8 + x c. 10 - xd. x - 10 e. $\frac{6}{x}$ f. 14 + 3x

| f. | In words: | th | the sum of | | | |
|-----------------|------------|--------------|--------------|--------------|--|--|
| | | | | | | |
| | | 9 | and | twice a | | |
| | | 9 | anu | number | | |
| | | \downarrow | \downarrow | \downarrow | | |
| | Translate: | 9 | + | 2x | | |
| Work Practice 1 | | | | | | |

Objective **B** Writing Sentences as Equations

Now that we have practiced writing phrases as algebraic expressions, let's write sentences as equations. You may want to first study the key words and phrases chart to review some key words and phrases that translate to an equal sign.

Example 2

Write each sentence as an equation. Use x to represent "a number."

and 5 is -30.

- **a.** Nine increased by a number is 5.
- **b.** Twice a number equals -10. c. A number minus 6 amounts to 168. **d.** Three times the sum of a number
- e. The quotient of twice a number and 8 is equal to 2.

Solution:

| a. | In words: | nine | | rease
by | ed | a nu | ımbe | r is | 5 |
|------------|-----------------|-------------------|------|------------------------|-----------|----------------|----------------------------|----------------------------|----------|
| | Translate: | ↓
9 | | \downarrow + | | | $\downarrow x$ | $\stackrel{\downarrow}{=}$ | ↓
5 |
| b. | In words: | twice
numbe | | equa | ls | -10 |) | | |
| | Translate: | \downarrow $2x$ | | ↓
= | | ↓
-10 |) | | |
| c. | In words: | a num | ber | miı | nus | 6 | amo
te | | 168 |
| | Translate: | $\downarrow x$ | | - | - | \downarrow 6 | = | = | ↓
168 |
| d. | In words: | three
times | | ne sui
mbe | | | is | -30 | |
| | Translate: | \downarrow
3 | | (x + | ,
- 5) |) | $\stackrel{\downarrow}{=}$ | ↓
-30 | |
| e. | In words: | t | he c | quoti
of | ent | | | | |
| | | | | | | | 1 | | |
| | | twice
numbe | | and | 8 | | qual
o | 2 | |
| | Translate: | \downarrow $2x$ | | \downarrow
\div | - | - | ↓
 | \downarrow 2 | |
| | | or $\frac{2x}{8}$ | = 2 | | | | | | |
| – v | Work Practice 2 | | | | | | | | |

Practice 2

Write each sentence as an equation. Use x to represent "a number."

- **a.** Five times a number is 20.
- **b.** The sum of a number and -5 yields 14.
- c. Ten subtracted from a number amounts to -23.
- **d.** Five times the difference of a number and 7 is equal to -8.
- e. The quotient of triple a number and 5 gives 1.

2. a. 5x = 20 b. x + (-5) = 14**c.** x - 10 = -23 **d.** 5(x - 7) = -8**e.** $\frac{3x}{5}$ $= 1 \text{ or } 3x \div 5 = 1$

Answers

Objective C Using Problem-Solving Steps to Solve Problems

Our main purpose for studying arithmetic and algebra is to solve problems. The same problem-solving steps that have been used throughout this text are used in this section also. Those steps are next.

Problem-Solving Steps

- **1.** UNDERSTAND the problem. During this step, become comfortable with the problem. Some ways of doing this are as follows:
 - Read and reread the problem.
 - Construct a drawing.
 - Propose a solution and check. Pay careful attention to how you check your proposed solution. This will help when writing an equation to model the problem.
 - Choose a variable to represent an unknown. Use this variable to represent any other unknowns.
- 2. TRANSLATE the problem into an equation.
- 3. SOLVE the equation.
- **4.** INTERPRET the results: *Check* the proposed solution in the stated problem and *state* your conclusion.

The first problem that we solve consists of finding an unknown number.

Example 3 Finding an Unknown Number

Twice a number plus 3 is the same as the number minus 6. Find the unknown number.

Solution:

 UNDERSTAND the problem. To do so, we read and reread the problem. Let's propose a solution to help us understand. Suppose the unknown number is 5. Twice this number plus 3 is 2 • 5 + 3 or 13. Is this the same as the number minus 6, or 5 - 6, or -1? Since 13 is not the same as -1, we know that 5 is not the solution. However, remember that the purpose of proposing a solution is not to guess correctly, but to better understand the problem.

Now let's choose a variable to represent the unknown. Let's let

x = unknown number

2. TRANSLATE the problem into an equation.

| In words: | | plus 3 | is the | the number |
|------------|--------------|--------------|--------------|--------------|
| | number | pius 5 | same as | minus 6 |
| | \downarrow | \downarrow | \downarrow | \downarrow |
| Translate: | 2x | + 3 | = | x - 6 |

3. SOLVE the equation. To solve the equation, we first subtract x from both sides.

2x + 3 = x - 6 2x + 3 - x = x - 6 - x x + 3 = -6Simplify. x + 3 - 3 = -6 - 3Subtract 3 from both sides. x = -9Simplify. Practice 3

Translate "The difference of a number and 2 equals 6 added to three times the number" into an equation and solve.

(Continued on next page)

Answer 3. x - 2 = 6 + 3x; -4 **4.** INTERPRET the results. First, *check* the proposed solution in the stated problem. Twice "-9" is -18 and -18 + 3 is -15. This is equal to the number minus 6, or "-9" -6, or -15. Then *state* your conclusion: The unknown number is -9.

Work Practice 3

✓ Concept Check Suppose you have solved an equation involving perimeter to find the length of a rectangular table. Explain why you would want to recheck your math if you obtain the result of −5.

Example 4 Determining Distances

The distance by road from Chicago, Illinois, to Los Angeles, California, is 1091 miles *more* than the distance from Chicago to Boston, Massachusetts. If the total of these two distances is 3017 miles, find the distance from Chicago to Boston. (*Source: World Almanac*)

Solution:

1. UNDERSTAND the problem. We read and reread the problem.

Let's propose and check a solution to help us better understand the problem. Suppose the distance from Chicago to Boston is 600 miles. Since the distance from Chicago to Los Angeles is 1091 *more* miles, then this distance is 600 + 1091 = 1691 miles. With these numbers, the total of the distances is 600 + 1691 = 2291 miles. This is less than the given total of 3017 miles, so we are incorrect. But not only do we have a better understanding of this exercise, we also know that the distance from Boston to Chicago is greater than 600 miles since this proposed solution led to a total too small. Now let's choose a variable to represent an unknown. Then we'll use this variable to represent any other unknown quantities. Let

x = distance from Chicago to Boston

Then

3.

x + 1091 = distance from Chicago to Los Angeles

since that distance is 1091 more miles.

2. TRANSLATE the problem into an equation.

| In words: | Chicago to
Boston distance | + | Chicago to Los
Angeles distance | = | total miles |
|-------------|-------------------------------|-------|------------------------------------|---------|--------------|
| | \downarrow | | ¥ | | \downarrow |
| Translate: | x | + | x + 1091 | = | 3017 |
| • SOLVE the | equation: | | | | |
| x | + x + 1091 = 30 | 017 | | | |
| | 2x + 1091 = 30 |)17 | Combine like | terms. | |
| 2x + 2 | 1091 - 1091 = 30 |)17 – | 1091 Subtract 1091 | from bo | th sides. |
| | 2 10 | 006 | 0. 1.0 | | |

| 2x + 1091 = 3017 | Combine like terms. |
|---------------------------------|------------------------------|
| 2x + 1091 - 1091 = 3017 - 1091 | Subtract 1091 from both side |
| 2x = 1926 | Simplify. |
| $\frac{2x}{2} = \frac{1926}{2}$ | Divide both sides by 2. |
| x = 963 | Simplify. |

4. INTERPRET the results. First *check* the proposed solution in the stated problem. Since *x* represents the distance from Chicago to Boston, this is 963 miles. The distance from Chicago to Los Angeles is x + 1091 = 963 + 1091 = 2054 miles.

The distance by road from Cincinnati, Ohio, to Denver, Colorado, is 71 miles *less* than the distance from Denver to San Francisco, California. If the total of these two distances is 2399 miles, find the distance from Denver to San Francisco.



Answer 4. 1235 miles

Concept Check Answer Length cannot be negative. To check, notice that the total number of miles is 963 + 2054 = 3017 miles, the given total of miles. Also, 2054 is 1091 more miles than 963, so the solution checks. Then, *state* your conclusion: The distance from Chicago to Boston is 963 miles.

Work Practice 4

Example 5

Calculating Separate Costs

A salesperson at an electronics store sold a computer system and software for \$2100, receiving four times as much money for the computer system as for the software. Find the price of each.

Solution:

- **1.** UNDERSTAND the problem. We read and reread the problem. Then we choose a variable to represent an unknown. We use this variable to represent any other unknown quantities. We let
 - x = the software price
 - 4x = the computer system price
- **2.** TRANSLATE the problem into an equation.

| In words: | software
price | and | computer
price | is | 2100 |
|------------|-------------------|----------------|-------------------|----------------------------|-----------|
| Translate: | $\downarrow x$ | \downarrow + | \downarrow 4x | $\stackrel{\downarrow}{=}$ | ↓
2100 |

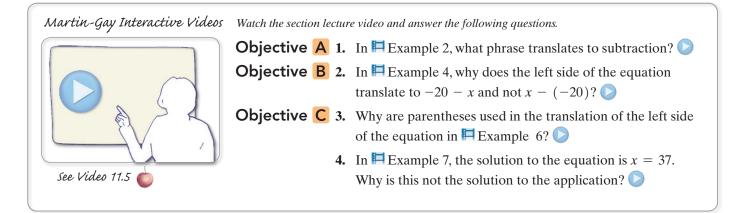
3. SOLVE the equation:

x + 4x = 2100 5x = 2100 Combine like terms. $\frac{5x}{5} = \frac{2100}{5}$ Divide both sides by 5. x = 420 Simplify.

4. INTERPRET the results. *Check* the proposed solution in the stated problem. The software sold for \$420. The computer system sold for 4x = 4(\$420) = \$1680. Since \$420 + \$1680 = \$2100, the total price, and \$1680 is four times \$420, the solution checks. *State* your conclusion: The software sold for \$420, and the computer system sold for \$1680.

Work Practice 5

Vocabulary, Readiness & Video Check



Practice 5

Answer

5. husband: \$38,000; son: \$19,000

A woman's \$57,000 estate is to be divided so that her husband receives twice as much as her son. How much will each receive?

11.5 Exercise Set MyLab Math

Objective A Translating Write each phrase as a variable expression. Use x to represent "a number." See Example 1.

- ▶1. The sum of a number and five **2.** Ten plus a number
 - **3.** The total of a number and eight
- **5**. Twenty decreased by a number
 - **7.** The product of 512 and a number
 - **9.** A number divided by 2
- **11.** The sum of seventeen, a number, and the product of five and the number

- **4.** The difference of a number and five hundred
- **6.** A number less thirty
- **8.** A number times twenty
- **10.** The quotient of six and a number
- **12.** The difference of twice a number, and four

Objective B Translating Write each sentence as an equation. Use x to represent "a number." See Example 2.

13. A number added to -5 is -7. **14.** Five subtracted from a number equals 10. **16.** The quotient of 8 and a number is -2. **15.** Three times a number yields 27. ● 17. A number subtracted from -20 amounts to 104. **18.** Two added to twice a number gives -14.

Objectives A B Mixed Practice Translating Write each phrase as a variable expression or each sentence as an equation. Use x to represent "a number." See Examples 1 and 2.

19. The product of five and a number **20.** The quotient of twenty and a number, decreased by three **21.** A number subtracted from 11 **22.** Twelve subtracted from a number **23.** Twice a number gives 108. **24.** Five times a number is equal to -75. **25.** Fifty decreased by eight times a number **26.** Twenty decreased by twice a number **27.** The product of 5 and the sum of -3 and a number **28.** Twice the sum of -17 and a number is -14. is -20.

Objective C *Translate each to an equation. Then solve the equation. See Example 3.*

- **29.** Three times a number, added to 9, is 33. Find the number.
- **30.** Twice a number, subtracted from 60, is 20. Find the number.

- **31.** The sum of 3, 4, and a number amounts to 16. Find the number.
- **33.** The difference of a number and 3 is equal to the quotient of 10 and 5. Find the number.
- **35.** Thirty less a number is equal to the product of 3 and the sum of the number and 6. Find the number.
- **37.** 40 subtracted from five times a number is 8 more than the number. Find the number.
- **39.** Three times the difference of a number and 5 amounts to the quotient of 108 and 12. Find the number.
 - **41.** The product of 4 and a number is the same as 30 less twice that same number. Find the number.

- **32.** The sum of 7, 9, and a number is 40. Find the number.
- **34.** Eight decreased by a number equals the quotient of 15 and 5. Find the number.
- **36.** The product of a number and 3 is twice the sum of that number and 5. Find the number.
- **38.** Five times the sum of a number and 2 is 11 less than the number times 8. Find the number.
- **40.** Seven times the difference of a number and 1 gives the quotient of 70 and 10. Find the number.
- **42.** Twice a number equals 25 less triple that same number. Find the number.

Solve. For Exercises 43 and 44, the solutions have been started for you. See Examples 4 and 5.

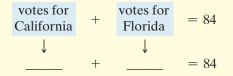
43. Florida has 26 fewer electoral votes for president than California. If the total number of electoral votes for these two states is 84, find the number for each state. (*Source:* U.S. Electoral College)

Start the solution:

1. UNDERSTAND the problem. Reread it as many times as needed. Let's let

x = number of electoral votes for California Then

- x 26 = number of electoral votes for Florida
- **2.** TRANSLATE into an equation. (Fill in the blanks below.)



Now, you finish with

- **3.** SOLVE the equation.
- 4. INTERPRET the results.

44. Ohio has twice the number of electoral votes for president as Alabama. If the total number of electoral votes for these two states is 27, find the number for each state. (*Source:* U.S. Electoral College)

Start the solution:

1. UNDERSTAND the problem. Reread it as many times as needed. Let's let

x = number of electoral votes for Alabama Then

2x = number of electoral votes for Ohio

2. TRANSLATE into an equation. (Fill in the blanks below.)

votes for
Alabama + votes for
$$\downarrow$$
 = 27
 \downarrow = 27
+ = 27

Now, you finish with

- **3.** SOLVE the equation.
- 4. INTERPRET the results.

◆ 45. A falcon, when diving, can travel five times as fast as a pheasant's top speed. If the total speed for these two birds is 222 miles per hour, find the fastest speed of the falcon and the fastest speed of the pheasant. (Source: Fantastic Book of Comparisons)



- **47.** The largest university (by enrollment) is Indira Gandhi National Open University in India, followed by Anadolu University in Turkey. If the enrollment in the Indian university is 1.5 million more students than the Turkish university and their combined enrollment is 5.5 million students, find the enrollment for each university. (*Source:* Wikipedia.org)
- **49.** The two top-selling Xbox 360 games are *Kinect Adventures* and *Grand Theft Auto V*. A price for *Grand Theft Auto V* is \$24 more than a price for *Kinect Adventures*. If the total of these two prices is \$36, find the price of each game. (*Source:* Gamestop.com)



46. Norway has had three times as many rulers as Liechtenstein. If the total number of rulers for both countries is 56, find the number of rulers for Norway and the number for Liechtenstein.



- **48.** The average life expectancy for an elephant is 24 years longer than the life expectancy for a chimpanzee. If the total of these life expectancies is 130 years, find the life expectancy of each.
- **50.** The U.S. newspaper with the greatest circulation is USA Today, followed by The Wall Street Journal. If the average daily circulation for USA Today is 226 thousand more than the average daily circulation of The Wall Street Journal and their combined circulation is 4340 thousand, find the circulation for each paper. (Source: USA Today)



- **51.** By air, the distance from New York City to London is 2001 miles *less* than the distance from Los Angeles to Tokyo. If the total of these two distances is 8939 miles, find the distance from Los Angeles to Tokyo.
- **52.** By air, the distance from Melbourne, Australia, to Cairo, Egypt, is 2338 miles *more* than the distance from Madrid, Spain, to Bangkok, Thailand. If the total of these distances is 15,012 miles, find the distance from Madrid to Bangkok.



53. The two NCAA stadiums with the largest capacities are Michigan Stadium (Univ. of Michigan) and Beaver Stadium (Penn State). Michigan Stadium has a capacity of 3329 more than Beaver Stadium. If the combined capacity for the two stadiums is 216,473, find the capacity for each stadium. (*Source:* Wikipedia.org)



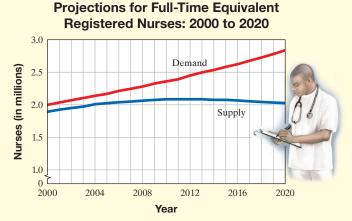
- **55.** California contains the largest state population of native Americans. This population is five times the native American population of Washington state. If the total of these two populations is 792 thousand, find the native American population in each of these two states. (*Source:* U.S. Census Bureau)
- **57.** During the 2017 Men's NCAA Division 1 basketball championship game, the North Carolina Tar Heels scored 6 points more than the Gonzaga Bulldogs. Together, both teams scored 136 points. How many points did the 2017 Champion North Carolina Tar Heels score during the game? (*Source:* National Collegiate Athletic Association)
- **59.** In 2020, the shortage of nurses is projected to be 533,201 more nurses than the shortage in 2010. If the total number of nurse shortages for these two years is 1,083,631, find the nurse shortage for each year.
- **60.** The percent shortage of nurses in 2019 is predicted to be three times the percent shortage in 2007. If the total percent shortages for these two years is 36%, find the percent shortage in 2007 and the percent shortage in 2019.

54. In 2020, China is projected to be the country with the greatest number of visiting tourists. This number is twice the number of tourists projected for Spain. If the total number of tourists for these two countries is projected to be 210 million, find the number projected for each. (*Source: The State of the World Atlas* by Dan Smith)



- **56.** During 2015, twice as many motor vehicles were manufactured in the United States than in Germany. If the total number of vehicles manufactured in these two countries was approximately 18,300,000, find the number manufactured in the United States and the number manufactured in Germany. (*Source:* Organization of Motor Vehicle Manufacturers)
- **58.** During the 2017 Women's NCAA Division 1 basketball championship game, the Mississippi State Bulldogs scored 12 points fewer than the South Carolina Gamecocks. Together, both teams scored a total of 122 points. How many points did the 2017 Champion South Carolina Gamecocks score during this game?

National Supply and Demand



Source: Bureau of Health Professions, RN Supply and Demand Projections

- **61.** The Pittsburgh Steelers hold the record for the most Super Bowl wins. The Miami Dolphins have 4 fewer Super Bowl wins than the Steelers. If the total number of Super Bowl wins for these two teams is 8, find the number of wins for each team. (*Source:* National Football League)
- **63.** A biker sold his used mountain bike and accessories for \$270. If he received five times as much money for the bike as he did for the accessories, find how much money he received for the bike.
- **65.** In 2017, Asia had the highest number of Internet users, followed by Europe. If Asia had 1250 million more Internet users than Europe and the total number of Internet users for both continents was 2550 million, find the number of Internet users for each continent. (*Source:* internetworldstats.com)

- **62.** The New York Yankees hold the record for the most World Series titles. The St. Louis Cardinals have won 16 fewer World Series titles than the Yankees. If the total number of World Series titles for these two teams is 38, find the number of World Series titles for each team.
- **64.** A tractor and a plow attachment are worth \$1200. The tractor is worth seven times as much money as the plow. Find the value of the tractor and the value of the plow.
- **66.** Based on 2017 data, North America had 174 million more Internet users than the Middle East. If these two regions together had 466 million Internet users, how many Internet users did each region have? (*Source:* internetworldstats.com)

Review

Round each number to the given place value. See Section 1.5.

| 67. 586 to the nearest ten | 68. 82 to the nearest ten |
|---|---|
| 69. 1026 to the nearest hundred | 70. 52,333 to the nearest thousand |
| 71. 2986 to the nearest thousand | 72. 101,552 to the nearest hundred |

Concept Extensions

- **73.** Solve Example 4 again, but this time let *x* be the distance from Chicago to Los Angeles. Did you get the same results? Explain why or why not.
- **74.** Solve Exercise **43** again, but this time let *x* be the number of electoral votes for Florida. Did you get the same results? Explain why or why not.

In real estate, a house's selling price P is found by adding the real estate agent's commission C to the amount A that the seller of the house receives: P = A + C.

- **75.** A house sold for \$230,000. The owner's real estate agent received a commission of \$13,800. How much did the seller receive? (*Hint:* Substitute the known values into the equation, then solve the equation for the remaining unknown.)
- **76.** A homeowner plans to use a real estate agent to sell his house. He hopes to sell the house for \$165,000 and keep \$156,750 of that. If everything goes as he has planned, how much will his real estate agent receive as a commission?

In retailing, the retail price P of an item can be computed using the equation P = C + M, where C is the wholesale cost of the item and M is the amount of markup.

- **77.** The retail price of a computer system is \$999 after a markup of \$450. What is the wholesale cost of the computer system? (*Hint:* Substitute the known values into the equation, then solve the equation for the remaining unknown.)
- **78.** Slidell Feed and Seed sells a bag of cat food for \$12. If the store paid \$7 for the cat food, what is the markup on the cat food?

Chapter 11 Group Activity

Modeling Equation Solving with Addition and Subtraction

Sections 11.1-11.4

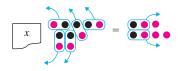
We can use positive counters • and negative counters • to help us model the equation-solving process. We also need to use an object that represents a variable. We use small slips of paper with the variable name written on them.

Recall that taking a • and • together creates a neutral or zero pair. After a neutral pair has been formed, it can be removed from or added to an equation model without changing the overall value. We also need to remember that we can add or remove the same number of positive or negative counters from both sides of an equation without changing the overall value.

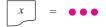
We can represent the equation x + 5 = 2 as follows:



To get the variable by itself, we must remove 5 black counters from the left side of the model. To do so, we must add 5 negative counters to both sides of the model. Then we can remove neutral pairs: 5 from the left side and 2 from the right side (since there are only 2 black counters on the right side).



We are left with the following model, which represents the solution, x = -3.



Similarly, we can represent the equation x - 4 = -6 as follows:



To get the variable by itself, we must remove 4 red counters from both sides of the model



We are left with the following model, which represents the solution, x = -2.



Use the counter model to solve each equation.

| 1. $x - 3 = -7$ | 2. $x - 1 = -9$ |
|------------------------|-------------------------|
| 3. $x + 2 = 8$ | 4. $x + 4 = 5$ |
| 5. $x + 8 = 3$ | 6. $x - 5 = -1$ |
| 7. $x - 2 = 1$ | 8. $x - 5 = 10$ |
| 9. $x + 3 = -7$ | 10. $x + 8 = -2$ |
| | |

Chapter 11 Vocabulary Check

Fill in each blank with one of the words or phrases listed below.

| | variable
terms
like | addition
simplified
combined | constant
multiplication
numerical coefficient | algebraic expression
evaluating the expression
distributive | equation solution | | |
|-----|--|------------------------------------|---|---|-------------------------|--|--|
| 1. | An algebraic | expression is | when | all like terms have been | | | |
| 2. | Terms that are exactly the same, except that they may have different numerical coefficients, are called terms. | | | | | | |
| 3. | A letter used | to represent a nu | umber is called a(n) | | | | |
| 4. | A combinatio | n of operations of | on variables and numbers is | called a(n) | · | | |
| 5. | The addends | of an algebraic ex | xpression are called the | of the expr | ession. | | |
| 6. | The number f | actor of a variable | le term is called the | | | | |
| 7. | | | ression by a number and the _ for the variable. | en finding the value of the expres | sion is | | |
| 8. | A term that is | a number only i | s called a(n) | | | | |
| 9. | A(n) | | is of the form expression = | expression. | | | |
| 10. | A(n) | | of an equation is a value for | or the variable that makes the equ | ation a true statement. | | |
| 11. | • To multiply $-3(2x + 1)$, we use the property. | | | | | | |
| 12. | By the property of equality, we may multiply or divide both sides of an equation by any nonzero number without changing the solution of the equation. | | | | | | |
| 13. | 3. By the property of equality, the same number may be added to or subtracted from both sides of an equation without changing the solution of the equation. | | | | | | |
| | Helpful | | | | | | |

Hint Are you preparing for your test?

To help, don't forget to take these:

- Chapter 11 Getting Ready for the Test on page 760
- Chapter 11 Test on page 761

Then check all of your answers at the back of this text. For further review, the step-by-step video solutions to any of these exercises are located in MyLab Math.

Chapter Highlights

| Definitions and Concepts | Examples |
|---|--|
| Section 11.1 Intro | duction to Variables |
| A letter used to represent a number is called a variable .
A combination of numbers, letters (variables), and
operation symbols is called an algebraic expression , or
expression . | x, y, z, a, b3 + x, 7y, x3 + y - 10 |
| Replacing a variable in an expression by a number
and then finding the value of the expression is called
evaluating the expression. | Evaluate: $2x + y$ when $x = 22$ and $y = 4$
$2x + y = 2 \cdot 22 + 4$ Replace x with 22 and y with 4.
= 44 + 4 Multiply.
= 48 Add. |
| The addends of an algebraic expression are called the terms of the expression. | $5x^2 + (-4x) + (-2)$ $\uparrow \qquad \uparrow \qquad 3 \text{ terms}$ |

| Definitions and Concepts | Examples | |
|---|--|--|
| Section 11.1 Introduction | to Variables (continued) | |
| The number factor of a variable term is called the numerical coefficient. | TermNumerical Coefficient $7x$ 7 $-6y$ -6 x or $1x$ 1 | |
| Terms that are exactly the same, except that they may have different numerical coefficients, are called like terms. | 5x + 11x = (5 + 11)x = 16x
like terms
y - 6y = (1 - 6)y = -5y | |
| An algebraic expression is simplified when all like terms have been combined. | Simplify:
-4(x + 2) + 3(5x - 7) | |
| Use the distributive property to multiply an algebraic
expression within parentheses by a term. Once any like
terms are then combined, the algebraic expression is
simplified. | = -4(x) + (-4)(2) + 3(5x) - 3(7)
= -4x + (-8) + 15x - (21)
= -4x + 15x + (-8) + (-21)
= 11x + (-29) or 11x - 29 | |
| Section 11.2 Solving Equat | tions: The Addition Property | |
| Addition Property of Equality | Solve for <i>x</i> : | |
| Let <i>a</i> , <i>b</i> , and <i>c</i> represent numbers. Then | x + 8 = 2 + (-1) | |
| a = b Also, $a = b$ | x + 8 = 1 | |
| and $a+c = b+c$ and $a-c = b-c$ | x + 8 - 8 = 1 - 8 Subtract 8 from both sides. | |
| are equivalent equations. are equivalent equations. | x = -7 Simplify. | |
| In other words, the same number may be added to or
subtracted from both sides of an equation without
changing the solution of the equation. | The solution is -7 . | |
| Section 11.3 Solving Equations: The Multiplication Property | | |
| Multiplication Property of Equality | Solve: $-7x = 42$ | |
| Let <i>a</i> , <i>b</i> , and <i>c</i> represent numbers and let $c \neq 0$. then | $\frac{-7x}{7} = \frac{42}{7}$ Divide both sides by -7. | |
| a = b Also, $a = b$ | -/ -/ | |
| and $a \cdot c = b \cdot c$ and $\frac{a}{c} = \frac{b}{c}$ | x = -6 Simplify.
Solve: $\frac{2}{3}x = -10$ | |
| are equivalent equations. are equivalent equations. | | |
| In other words, both sides of an equation may be mul-
tiplied or divided by the same nonzero number without
changing the solution of the equation. | $\frac{\cancel{2}}{\cancel{2}} \cdot \frac{\cancel{2}}{\cancel{3}} x = \frac{3}{2} \cdot -10 \text{Multiply both sides by } \frac{3}{2}.$ $x = -15 \qquad \text{Simplify.}$ | |

| | Definitions and Concepts | | Examples |
|---|---|---|--|
| | Section 11.4 Solving Equations Using | Addition a | and Multiplication Properties |
| | r Solving an Equation | Solve for | f(x) = 5(3x - 1) + 15 = -5 |
| - | If parentheses are present, use the distributive property. | Step 1: | 15x - 5 + 15 = -5 Apply the distributive property. |
| Step 2: | Combine any like terms on each side of the equation. | - | 15x + 10 = -5 Combine like terms. |
| Step 3: | Use the addition property of equality to rewrite
the equation so that variable terms are on one
side of the equation and constant terms are on
the other side. | Step 3: | 15x + 10 - 10 = -5 - 10 Subtract 10 from both
sides.
15x = -15 $15x - 15$ Divide both sides |
| Step 4: | Use the multiplication property of equality to
divide both sides by the numerical coefficient
of the variable to solve. | Step 4: | $\frac{15x}{15} = \frac{-15}{15}$ $x = -1$ Divide both sides
by 15. |
| Step 5: | Check the solution in the <i>original equation</i> . | Step 5: (| Check to see that -1 is the solution. |
| | Section 11.5 Equation | ns and Pro | blem Solving |
| 1. UND this a Read Con Cho | d and reread the problem.
struct a drawing.
ose a variable to represent an unknown in the | the incub
their incu
period fo
Internati
1. UND | bation period for a golden eagle is three times
bation period for a hummingbird. If the total of
ubation periods is 60 days, find the incubation
or each bird. (<i>Source: Wildlife Fact File</i> ,
tional Masters Publishers)
ERSTAND the problem. Then choose a
ble to represent an unknown. Let |
| - | olem. | د
3ء
2. TRAN | $x = \text{incubation period of a hummingbird}$ $x = \text{incubation period of a golden eagle}$ $NSLATE.$ $x = \text{incubation}$ $x = \text{incubation}$ $x = \text{incubation}$ $x = \text{incubation}$ $y = \frac{1}{2} \text{ of } \text{ is } 60$ $y = \frac{1}{2} \text{ of } \frac{1}$ |
| 3. SOLV | /E the equation. | 3. SOLV | VE:
$x + 3x = 60$ $4x = 60$ $\frac{\cancel{4}x}{\cancel{4}x} = \frac{60}{4}$ $x = 15$ |
| 4. INTERPRET the results. <i>Check</i> the proposed solution in the stated problem and <i>state</i> your conclusion. | | The in
15 day
3x =
Since
the so
<i>State</i> y
humm | ERPRET the solution in the stated problem.
An experimental energy of the solution period for a hummingbird is
ys. The incubation period for a golden eagle is
$3 \cdot 15 = 45$ days.
15 days + 45 days = 60 days and 45 is 3(15),
plution checks.
your conclusion: The incubation period for a
ningbird is 15 days. The incubation period for a
n eagle is 45 days. |

Chapter 11 Review

- (11.1) Evaluate each expression when x = 5, y = 0, and z = -2.
- **1.** $\frac{2x}{z}$ **2.** 4x 3 **3.** $\frac{x+7}{y}$
- **4.** $\frac{y}{5x}$ **5.** $x^3 2z$

6. $\frac{7+x}{3z}$

 \triangle **7.** Find the volume of a storage cube whose sides measure 2 feet. Use $V = s^3$.



9. Lamar deposited his \$5000 bonus into an account paying 6% annual interest. How much interest will he earn in 6 years? Use I = PRT.

Simplify each expression by combining like terms.

11. -6x - 9x **12.** $\frac{2}{3}x - \frac{9}{10}x$ **13.** 2y - 10 - 8y

 14. 8a + a - 7 - 15a **15.** y + 3 - 9y - 1 **16.** 1.7x - 3.2 + 2.9x - 8.7

Multiply.

- **17.** -2(4y) **18.** 3(5y 8)
- Simplify.
- **19.** 7x + 3(x 4) + x **20.** 4(x 7) + 21
- **21.** 3(5a-2) + 10(-2a+1) **22.** 6y + 3 + 2(3y-6)

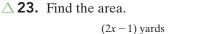
 \triangle **8.** Find the volume of a wooden crate in the shape of a cube 4 feet on each side. Use $V = s^3$.



10. Jennifer Lewis borrowed \$2000 from her grandmother and agreed to pay her 5% simple interest. How much interest will she owe after 3 years? Use I = PRT. \triangle **24.** Find the perimeter.

7y meters

Square



| _ | (); |
|------------|-----------|
| 3
yards | Rectangle |

(11.2)

Solve.

| 27. $z - 5 = -7$ | 28. <i>x</i> + 1 = 8 | 29. $x + \frac{7}{8} = \frac{3}{8}$ | 30. | $y + \frac{4}{11} = \frac{1}{2}$ | $-\frac{2}{11}$ |
|-------------------------|-----------------------------|--|-----|----------------------------------|-----------------|
| | | 0 0 | | 11 | 11 |

31. n + 18 = 10 - (-2) **32.** 15 = 8x + 35 - 7x **33.** m - 3.9 = -2.6 **34.** z - 4.6 = -2.2

- (11.3) Solve.
- **35.** -3y = -21 **36.** -8x = 72
- **37.** -5n = -5 **38.** -3a = 15
- **39.** $\frac{2}{3}x = -\frac{8}{15}$ **40.** $-\frac{7}{8}y = 21$
- **41.** -1.2x = 144 **42.** -0.8y = -10.4

43. -5x = 100 - 120 **44.** 18 - 30 = -4x

(11.4) Solve.

45. 3x - 4 = 11 **46.** 6y + 1 = 73

47.
$$-\frac{5}{9}x + 23 = -12$$
 48. $-\frac{2}{3}x - 11 = \frac{2}{3}x - 55$

49. 6.8 + 4y = -2.2 **50.** -9.6 + 5y = -3.1

Chapter 11 Review

51. 2x + 7 = 6x - 1 **52.** 5x - 18 = -4x + 36

53.
$$5(n-3) = 7 + 3n$$
 54. $7(2 + x) = 4x - 1$

55.
$$2(4n - 11) + 8 = 5n + 4$$

56. $3(5x - 6) + 9 = 13x + 7$

Write each sentence as an equation.

- **57.** The difference of 20 and -8 is 28.
- **59.** The quotient of -75 and the sum of 5 and 20 is equal to -3.
- **58.** Nineteen subtracted from -2 amounts to -21.
- **60.** The product of -5 and the sum of -2 and 6 yields -20.

(11.5) Write each phrase as an algebraic expression. Use x to represent "a number."

- **61.** The quotient of 70 and a number
- **63.** A number subtracted from 85.

- **62.** The difference of a number and 13
- **64.** Eleven added to twice a number

Write each sentence as an equation. Use x to represent "a number."

65. A number increased by 8 is 40.

66. Twelve subtracted from twice a number is 10.

Solve.

- **67.** Five times a number subtracted from 40 is the same as three times the number. Find the number.
- **68.** The product of a number and 3 is twice the difference of that number and 8. Find the number.

- 69. Bamboo and Pacific Kelp, a kind of seaweed, are two fast-growing plants. Bamboo grows twice as fast as kelp. If in one day both can grow a total of 54 inches, find how many inches each plant can grow in one day.
- 70. In an election between the incumbent and a challenger, the incumbent received 11,206 more votes than the challenger. If a total of 18,298 votes were cast, find the number of votes for each candidate.



Mixed Review

Evaluate each expression when x = 4, y = -3, and z = 5.

71.
$$18 - (9 - 5x)$$
 72. $\frac{z}{100} + \frac{y}{10}$

Simplify.

73. 9*x* - 20*x* **74.** -5(7*x*)

75.
$$12x + 5(2x - 3) - 4$$
 76. $-7(x + 6) - 2(x - 5)$

Write each phrase as an algebraic expression. Use x to represent "a number."

77. Seventeen less than a number **78.** Three times the sum of a number and five

Write each sentence as an equation using x to represent "a number."

- **79.** The difference of a number and 3 is the quotient of the number and 4.
- **80.** The product of a number and 6 is equal to the sum of the number and 2.
- **81.** Is 3 a solution of 4y + 2 6y = 5 + 7? **82.** Is 7 a solution of 4(z - 8) + 12 = 8?

72.
$$\frac{z}{100} + \frac{y}{10}$$

Solve.

83.
$$c - 5 = -13 + 7$$
84. $7x + 5 - 6x = -20$
85. $-7x + 3x = -50 - 2$
86. $-x + 8x = -38 - 4$

87.
$$14 - y = -3$$
 88. $7 - z = 0$

89.
$$9x + 12 - 8x = -6 + (-4)$$

90. $-17x + 14 + 20x - 2x = 5 - (-3)$

91.
$$\frac{4}{9}x = -\frac{1}{3}$$
 92. $-\frac{5}{24}x = \frac{5}{6}$

93.
$$2y + 6y = 24 - 8$$
 94. $13x - 7x = -4 - 12$

95.
$$\frac{2}{3}x - 12 = -4$$
 96. $\frac{7}{8}x + 5 = -2$

- **97.** -5z + 3z 7 = 8z 7
- **99.** Three times a number added to twelve is 27. Find the number.

98. 4x - 3 + 6x = 5x - 3

100. Twice the sum of a number and four is ten. Find the number.

Getting Ready for the Test

MULTIPLE CHOICE Exercises 1 through 16 are Multiple Choice. Choose the correct letter.

For Exercises 1 through 4, let a = 35 and b = 5. Choose the expression that gives each answer.

A.
$$a - b$$
 B. $a \div b$ **C.** $a + b$ **D.** ab

Chapter 11

2. answer: 175

- **3**. answer: 30
- **4**. answer: 40

Simplify each expression in Exercises 5 through 10. Then choose the simplified form: A, B, C, D, or E. Choices may be used more than once or not at all. **E** Ax + 6

| | A. $-6x$ | B. 6 <i>x</i> | C. $4x + 2$ | D. $4x +$ | 1 E. $4x + 6$ |
|-------------|-----------|----------------------|--------------------|------------------|----------------------|
| • 5. | x - 7x | | | 06. | -2x + 3 + 8x - 3 |
| ○ 7. | -3(2x) | | | 08. | 2(2x + 1) |
| 0 9. | -(x+2)+5x | + 4 | | 0 10. | 3(1+2x) - 3 |

For Exercises 11 through 14, choose the solution of each equation as

A. 2 **B.** -2 **C.** 18 **D.** -18 **D.** 11. -3x = 6 **D.** 2 **C.** 18 **D.** -18 **D.** 13. $\frac{x}{-3} = 6$ **D.** 14. x + 2 = 4

For Exercises 15 and 16, choose the correct letter.

- ▶ 15. To solve 5x 10 = 0, we will first add 10 to each side of the equation. Once this is done, the equivalent equation is A. 5x = 0 B. 5x = 10 C. 5x = -10
- ▶ 16. To solve 4(2x + 1) 8 = 14x 10, we will first simplify the left side of the equation. Once this is done, the equivalent equation is

A. 8x - 4 = 14x - 10 **B.** 8x - 7 = 14x - 10 **C.** 2x - 7 = 14x - 10

MATCHING Let x represent "a number." Match each phrase in the first column with its translated variable expression in the second column.

| \bigcirc 17. the sum of -3 and a number | A. $-3x$ |
|---|----------------------|
| ● 18. the product of -3 and a number | B. $3 + x$ |
| ● 19. 5 subtracted from a number | C. $-3 + x$ |
| ▶ 20. 5 minus a number | D. $x - 5$ |
| | E. $5 - x$ |
| | F. 5 <i>x</i> |

MATCHING Let x represent "a number." Match each sentence in the first column with its translated equation in the second or third column.

| 21. Twice a number gives 14. | A. $6x = 14$ | E. $x - 2 = 14$ |
|---|------------------------------|---------------------------|
| 22. A number divided by 6 yields 14. | B. $2x = 14$ | F. $2 + 6x = 14$ |
| ● 23. Two subtracted from a number equals 14. | C. $\frac{x}{6} = 14$ | G. $6(2 + x) = 14$ |
| • 24. Six times a number, added to 2 is 14. | D. $2 - x = 14$ | |

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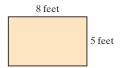
| Chapter 11 Te | st MyLab Math or You Tube | For additional practice g
in MyLab Math. | o to your study plan |
|--|---|---|------------------------|
| •1. Evaluate $\frac{3x-5}{2y}$ when $x = y = -8$. | • 7 and • 2. Simplify $7x - 5 - 1$ combining like term | 2x + 10 by | Answers |
| •3. Multiply: $-2(3y + 7)$ | • 4. Simplify: $5(3z + 2)$ |) — z — 18 | <u>1.</u>
2. |
| 5. Write a product that repres | Sents the area of the rectangle. Then mult
4 meters
Rectangle $(3x - 1)$
meters | iply. | <u>3.</u>
<u>4.</u> |
| | | | 5. |
| <i>Solve.</i> 6. $x - 17 = -10$ | • 7. $y + \frac{3}{4} = \frac{1}{4}$ | | 6.
7. |
| 8. $-4x = 48$ | 9. $-\frac{5}{8}x = -25$ | | <u>8.</u>
9. |
| | 8 ^x - 25 | | 10. |
| • 10. $5x + 12 - 4x - 14 = 22$ | • 11. $2 - c + 2c = 5$ | | <u>11.</u>
12. |
| • 12. $3x - 5 = -11$ | 13. $-4x + 7 = 15$ | | <u>13.</u>
761 |

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|------------|--|
| 14. | • 14. $3.6 - 2x = -5.4$ • 15. $12 = 3(4 + 2y)$ |
| 15. | • 16. $5x - 2 = x - 10$ • 17. $10y - 1 = 7y + 21$ |
| <u>16.</u> | |
| 17. | • 18. $6 + 2(3n - 1) = 28$
• 19. $4(5x + 3) = 2(7x + 6)$ |
| <u>18.</u> | Solve. |
| <u>19.</u> | A lawn is in the shape of a trapezoid with a height of 60 feet and bases of 70 feet and 130 feet. Find the area of A lawn is in the shape of a trapezoid with a height of 60 feet and bases of 70 feet and 130 feet. Find the area of A lawn is in the shape of a trapezoid with a height of 60 feet and bases of 70 feet and 130 feet. Find the area of |
| 20. | the lawn. Use
$A = \frac{1}{2}h(B + b).$ $A = \frac{1}{2}bh.$ |
| 21. | |
| 22. a. | 22. Translate the following phrases into mathematical expressions. Use <i>x</i> to represent "a number."23. The difference of three times a number and five times the same number is 4. Find the number. |
| b | a. The product of a number and 17b. Twice a number subtracted from 20 |
| 23. | |
| 24. | O 24. In a championship basketball game,
Paula Zimmerman scored twice as
many points as Maria Kaminsky. If the
total number of points made by both O 25. In a 10-kilometer race, there are 112
more men entered than women. Find
the number of women runners if the
total number of runners in the race |
| 25. | women was 51, find how many points is 600.
Paula scored. |

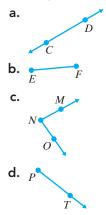
Cumulative Review

Chapters 1–11

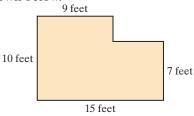
- **1.** Multiply: 0.0531×16
- **3.** Given the rectangle shown:



- **a.** Find the ratio of its width to its length.
- **b.** Find the ratio of its length to its perimeter.
- **7.** What percent of 12 is 9?
- **9.** Convert 3 pounds to ounces.
- **11.** Add 2400 ml to 8.9 L.
- **13.** Identify each figure as a line, a ray, a line segment, or an angle.



 \triangle **17.** Find the perimeter of the room shown below.



| 2. Multiply: | 0.0531×1000 |
|---------------------|----------------------|
|---------------------|----------------------|

4. Add:
$$\frac{5}{12} + \frac{2}{9}$$

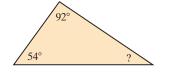
- **5.** 12% of what number is 0.6?
- **6.** Multiply: $\frac{7}{8} \cdot \frac{2}{3}$

8. Divide: $1\frac{4}{5} \div 2\frac{3}{10}$

- **10.** Round 23,781 to the nearest thousand.
- **12.** Round 0.02351 to the nearest thousandth.
- **14.** Find the supplement of a 12° angle.
- \triangle **15.** Find the diameter of the circle.



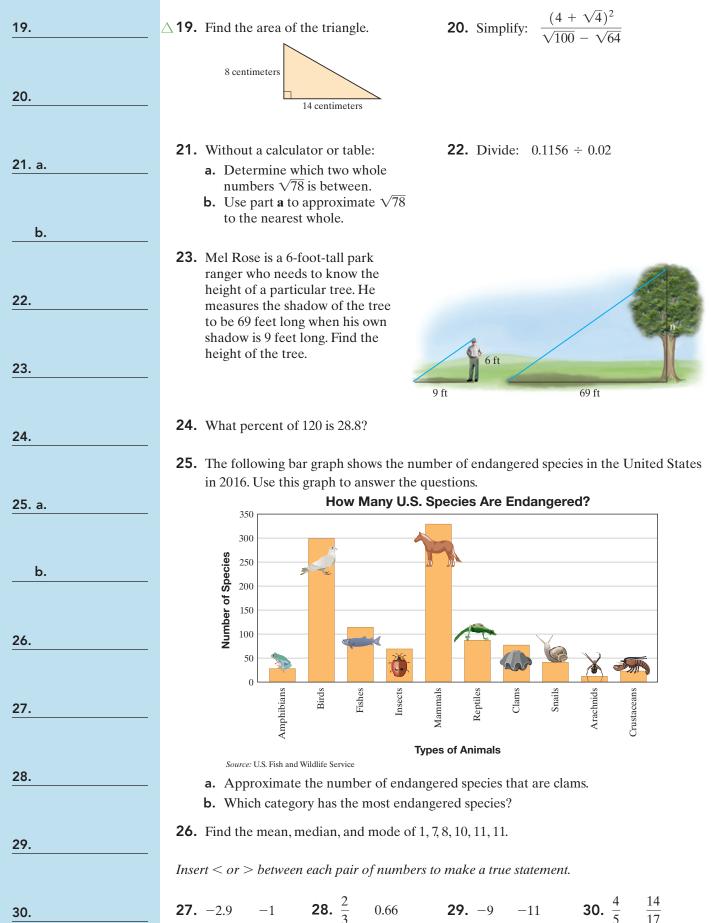
16. Find the measure of the unknown angle.



 \triangle **18.** Find the area of the room in Exercise **17**.

| Answers | |
|---------|--|
| 1. | |
| | |
| 2. | |
| 3 3 | |
| J. d. | |
| b. | |
| | |
| 4. | |
| | |
| 5. | |
| , | |
| 6. | |
| 7. | |
| | |
| 8. | |
| | |
| 9. | |
| 10. | |
| | |
| 11. | |
| | |
| 12. | |
| 13. a. | |
| 10. 4. | |
| b. | |
| | |
| с. | |
| d. | |
| | |
| 14. | |
| | |
| 15. | |
| 16. | |
| | |
| 17. | |
| | |
| 18. | |

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Cumulative Review

Find each absolute value.

31.
$$|-2|$$
 32. $\left|\frac{5}{6}\right|$ **33.** $|1.2|$ **34.** $|0|$
Add.
35. $-5 + (-11)$ **36.** $-8.2 + 4.6$
37. $-\frac{3}{8} + \left(-\frac{1}{8}\right)$ **38.** $\frac{2}{5} + \left(-\frac{3}{10}\right)$
Subtract.
39. $8 - 15$ **40.** $4.6 - (-1.2)$
41. $-4 - (-5)$ **42.** $\frac{7}{10} - \frac{23}{24}$
Multiply.
43. $-2(-5)$ **44.** $-8(1.2)$
45. $\left(-\frac{1}{2}\right)\left(-\frac{2}{3}\right)$ **46.** $-2\frac{2}{9}\left(1\frac{4}{5}\right)$
47. Simplify: $(-3) \cdot |-5| - (-2) + 4^2$ **48.** Solve: $4x - 7.1 = 3x + 2.6$
49. Solve: $3(2x - 6) + 6 = 0$ **50.** Solve: $6(x - 5) = 4(x + 4) - 6$

765

31.

32.

33.

34.

35.

36.

37.

38.

39.

40.

41.

42.

43.

44.

45.

46.

47.

48.

49.

50.

Tables

Appendix

A.1 Addition Table and One Hundred Addition Facts

| + | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|---|---|----|----|----|----|----|----|----|----|----|
| 0 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| 2 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| 3 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 4 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| 5 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| 6 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| 7 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| 8 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| 9 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |

One Hundred Addition Facts

Knowledge of the basic addition facts found above is an important prerequisite for a course in basic college mathematics. Study the table above and then perform the additions. Check your answers either by comparing them with those found in the back-of-the-book answer section or by using the table. Review any facts that you missed.

| 1. 1
<u>+4</u> | | 3. 2
+3 | | | 6. 6 <u>+1</u> |
|--------------------------|-----------------------|--------------------------|------------------------|------------------------|------------------------|
| 7. 4 <u>+4</u> | 8. 0 <u>+6</u> | 9. 9
<u>+5</u> | 10. 8 <u>+2</u> | 11. 5 <u>+7</u> | 12. 3 <u>+2</u> |
| 13. 5 <u>+5</u> | | 15. 8 <u>+1</u> | | | 18. 3 <u>+5</u> |
| 19. 9
+9 | | 21. 6 <u>+4</u> | | | 24. 3 <u>+7</u> |
| 25. 9
+8 | 26. 0
+8 | 27. 4
+9 | 28. 3
+0 | 29. 7
+5 | 30. 8 + 9 |

| | 33. 4 <u>+3</u> | | |
|--|---------------------------|--|--|
| | 39. 8
+0 | | |
| | 45. 3
<u>+6</u> | | |
| | 51. 2
+0 | | |
| | 57. 0 <u>+5</u> | | |
| | 63. 1
<u>+6</u> | | |
| | 69. 4
+1 | | |
| | 75. 7
+7 | | |
| | 81. 2
+8 | | |
| | 87. 7 <u>+3</u> | | |
| | 93. 2
+7 | | |
| | 99. 9
<u>+0</u> | | |

767

| × | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|---|---|----|----|----|----|----|----|----|----|
| 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 2 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 |
| 3 | 3 | 6 | 9 | 12 | 15 | 18 | 21 | 24 | 27 |
| 4 | 4 | 8 | 12 | 16 | 20 | 24 | 28 | 32 | 36 |
| 5 | 5 | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45 |
| 6 | 6 | 12 | 18 | 24 | 30 | 36 | 42 | 48 | 54 |
| 7 | 7 | 14 | 21 | 28 | 35 | 42 | 49 | 56 | 63 |
| 8 | 8 | 16 | 24 | 32 | 40 | 48 | 56 | 64 | 72 |
| 9 | 9 | 18 | 27 | 36 | 45 | 54 | 63 | 72 | 81 |

A.2 Multiplication Table and One Hundred Multiplication Facts

One Hundred Multiplication Facts

Knowledge of the basic multiplication facts found above is an important prerequisite for a course in basic college mathematics. Study the table above and then perform the multiplications. Check your answers either by comparing them with those found in the back-of-the-book answer section or by using the table. Review any facts that you missed.

| | | 5. 8
<u>×4</u> | |
|---------------------------|-------------------------|---------------------------|---------------------------|
| 8. 7
<u>×1</u> | | 11. 9
<u>×7</u> | 12. 8 <u>×8</u> |
| | | 17. 4
<u>×6</u> | |
| 20. 8
<u>×9</u> | | 23. 4
<u>×8</u> | 24. 1 × 2 |
| | | 29. 6
<u>×9</u> | |
| | 33. 4 <u>× 9</u> | 35. 6
<u>×2</u> | 36. 4
<u>×5</u> |

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| | 40. 1
<u>×6</u> | |
|------------------------|---------------------------|------------------------|
| | 46. 7
<u>×4</u> | |
| | 52. 2
× 6 | |
| | 58. 1
<u>×9</u> | 60. 6 <u>×1</u> |
| | 64. 7
<u>×3</u> | |
| | 70. 2
<u>×0</u> | |
| | 76. 3
<u>×8</u> | |
| | 82. 6
<u>×5</u> | |
| | 88. 7
<u>×7</u> | |
| | 94. 0
<u>×4</u> | |
| 98. 5 <u>×2</u> | | |



A.3 Table of Geometric Figures

| Plane Fig | ures Have Length and Width but No Thickr | ness or Depth |
|----------------------|---|---|
| Name | Description | Figure |
| Polygon | Union of three or more coplanar line seg-
ments that intersect with each other only at
each endpoint, with each endpoint shared by
two segments. | |
| Triangle | Polygon with three sides (sum of measures of three angles is 180°). | |
| Scalene Triangle | Triangle with no sides of equal length. | |
| Isosceles Triangle | Triangle with two sides of equal length. | |
| Equilateral Triangle | Triangle with all sides of equal length. | |
| Right Triangle | Triangle that contains a right angle. | leg hypotenuse
leg |
| Quadrilateral | Polygon with four sides (sum of measures of four angles is 360°). | |
| Trapezoid | Quadrilateral with exactly one pair of oppo-
site sides parallel. | base
leg parallel leg
sides
base |
| Isosceles Trapezoid | Trapezoid with legs of equal length. | |
| Parallelogram | Quadrilateral with both pairs of opposite sides parallel. | |
| Rhombus | Parallelogram with all sides of equal length. | |
| Rectangle | Parallelogram with four right angles. | |

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| Plan | Plane Figures Have Length and Width but No Thickness or Depth | | | | | | |
|--------|---|------------------------------|--|--|--|--|--|
| Name | Description | Figure | | | | | |
| Square | Rectangle with all sides of equal length. | | | | | | |
| Circle | All points in a plane the same distance
from a fixed point called the center. | radius
center
diameter | | | | | |

| Solid F | Solid Figures Have Length, Width, and Height or Depth | | | | | | |
|-------------------------|--|------------------|--|--|--|--|--|
| Name | Description | Figure | | | | | |
| Rectangular Solid | A solid with six sides, all of which are rectangles. | | | | | | |
| Cube | A rectangular solid whose six sides are squares. | | | | | | |
| Sphere | All points the same distance from a fixed point, called the center. | radius
center | | | | | |
| Right Circular Cylinder | A cylinder having two circular bases that are perpendicular to its altitude. | | | | | | |
| Right Circular Cone | A cone with a circular base that is perpendicular to its altitude. | | | | | | |



A.4 Table of Percents, Decimals, and Fraction Equivalents 🔘

| Percent | Decimal | Fraction |
|---|-------------------|-------------------------------|
| 1% | 0.01 | $\frac{1}{100}$ |
| 5% | 0.05 | $\frac{1}{20}$ |
| 10% | 0.1 | $\frac{1}{10}$ |
| 12.5% or $12\frac{1}{2}$ % | 0.125 | $\frac{1}{8}$ |
| $16.\overline{6}\%$ or $16\frac{2}{3}\%$ | $0.1\overline{6}$ | $\frac{1}{6}$ |
| 20% | 0.2 | $\frac{1}{5}$ |
| 25% | 0.25 | $\frac{1}{4}$ |
| 30% | 0.3 | $\frac{3}{10}$ |
| $33.\overline{3}\%$ or $33\frac{1}{3}\%$ | 0.3 | $\frac{1}{3}$ |
| 37.5% or $37\frac{1}{2}\%$ | 0.375 | <u>3</u>
8 |
| 40% | 0.4 | $\frac{2}{5}$ |
| 50% | 0.5 | $\frac{1}{2}$ |
| 60% | 0.6 | $\frac{3}{5}$ |
| 62.5% or $62\frac{1}{2}\%$ | 0.625 | <u>5</u>
8 |
| $66.\overline{6}\%$ or $66\frac{2}{3}\%$ | $0.\overline{6}$ | $\frac{2}{3}$ |
| 70% | 0.7 | $\frac{7}{10}$ |
| 75% | 0.75 | $\frac{3}{4}$ |
| 80% | 0.8 | $\frac{4}{5}$ |
| $83.\overline{3}\%$ or $83\frac{1}{3}\%$ | $0.8\overline{3}$ | $\frac{5}{6}$ |
| 87.5% or $87\frac{1}{2}\%$ | 0.875 | $\frac{7}{8}$ |
| 90% | 0.9 | $\frac{9}{10}$ |
| 100% | 1.0 | 1 |
| 110% | 1.1 | $1\frac{1}{10}$ |
| 125% | 1.25 | $1\frac{1}{4}$ |
| $133.\overline{3}\%$ or $133\frac{1}{3}\%$ | 1.3 | 1 <u>1</u> |
| 150% | 1.5 | 11/2 |
| $166.\overline{6}\% \text{ or } 166\frac{2}{3}\%$ | 1.6 | 1 ² / ₃ |
| 175% | 1.75 | 13/4 |
| 200% | 2.0 | 2 |

A.5 Table on Finding Common Percents of a Number

| Common Percent
Equivalences* | Shortcut Method
for Finding Percent | Example |
|---|--|--|
| $1\% = 0.01 \left(\text{ or } \frac{1}{100} \right)$ | To find 1% of a number, multiply by 0.01.
To do so, move the decimal point 2 places
to the left. | 1% of 210 is 2.10 or 2.1.
1% of 1500 is 15.
1% of 8.6 is 0.086. |
| $10\% = 0.1 \left(\text{ or } \frac{1}{10} \right)$ | To find 10% of a number, multiply by 0.1,
or move the decimal point of the number
one place to the left. | 10% of 140 is 14.
10% of 30 is 3.
10% of 17.6 is 1.76. |
| $25\% = \frac{1}{4}$ | To find 25% of a number, find $\frac{1}{4}$ of the number, or divide the number by 4. | 25% of 20 is $\frac{20}{4}$ or 5.
25% of 8 is 2.
25% of 10 is $\frac{10}{4}$ or $2\frac{1}{2}$. |
| $50\% = \frac{1}{2}$ | To find 50% of a number, find $\frac{1}{2}$ of the number, or divide the number by 2. | 50% of 64 is $\frac{64}{2}$ or 32.
50% of 1000 is 500.
50% of 9 is $\frac{9}{2}$ or $4\frac{1}{2}$. |
| 100% = 1 | To find 100% of a number, multiply the
number by 1. In other words, 100% of a
number is the number. | 100% of 98 is 98.
100% of 1407 is 1407.
100% of 18.4 is 18.4. |
| 200% = 2 | To find 200% of a number, multiply the number by 2. | 200% of 31 is 31 · 2 or 62.
200% of 750 is 1500.
200% of 6.5 is 13. |

*See Appendix A.4.

A.6 Table of Squares and Square Roots

| n | n ² | \sqrt{n} | n | n ² | \sqrt{n} |
|----|----------------|------------|-----|----------------|------------|
| 1 | 1 | 1.000 | 51 | 2601 | 7.141 |
| 2 | 4 | 1.414 | 52 | 2704 | 7.211 |
| 3 | 9 | 1.732 | 53 | 2809 | 7.280 |
| 4 | 16 | 2.000 | 54 | 2916 | 7.348 |
| 5 | 25 | 2.236 | 55 | 3025 | 7.416 |
| 6 | 36 | 2.449 | 56 | 3136 | 7.483 |
| 7 | 49 | 2.646 | 57 | 3249 | 7.550 |
| 8 | 64 | 2.828 | 58 | 3364 | 7.616 |
| 9 | 81 | 3.000 | 59 | 3481 | 7.681 |
| 10 | 100 | 3.162 | 60 | 3600 | 7.746 |
| 11 | 121 | 3.317 | 61 | 3721 | 7.810 |
| 12 | 144 | 3.464 | 62 | 3844 | 7.874 |
| 13 | 169 | 3.606 | 63 | 3969 | 7.937 |
| 14 | 196 | 3.742 | 64 | 4096 | 8.000 |
| 15 | 225 | 3.873 | 65 | 4225 | 8.062 |
| 16 | 256 | 4.000 | 66 | 4356 | 8.124 |
| 17 | 289 | 4.123 | 67 | 4489 | 8.185 |
| 18 | 324 | 4.243 | 68 | 4624 | 8.246 |
| 19 | 361 | 4.359 | 69 | 4761 | 8.307 |
| 20 | 400 | 4.472 | 70 | 4900 | 8.367 |
| 21 | 441 | 4.583 | 71 | 5041 | 8.426 |
| 22 | 484 | 4.690 | 72 | 5184 | 8.485 |
| 23 | 529 | 4.796 | 73 | 5329 | 8.544 |
| 24 | 576 | 4.899 | 74 | 5476 | 8.602 |
| 25 | 625 | 5.000 | 75 | 5625 | 8.660 |
| 26 | 676 | 5.099 | 76 | 5776 | 8.718 |
| 27 | 729 | 5.196 | 77 | 5929 | 8.775 |
| 28 | 784 | 5.292 | 78 | 6084 | 8.832 |
| 29 | 841 | 5.385 | 79 | 6241 | 8.888 |
| 30 | 900 | 5.477 | 80 | 6400 | 8.944 |
| 31 | 961 | 5.568 | 81 | 6561 | 9.000 |
| 32 | 1024 | 5.657 | 82 | 6724 | 9.055 |
| 33 | 1089 | 5.745 | 83 | 6889 | 9.110 |
| 34 | 1156 | 5.831 | 84 | 7056 | 9.165 |
| 35 | 1225 | 5.916 | 85 | 7225 | 9.220 |
| 36 | 1296 | 6.000 | 86 | 7396 | 9.274 |
| 37 | 1369 | 6.083 | 87 | 7569 | 9.327 |
| 38 | 1444 | 6.164 | 88 | 7744 | 9.381 |
| 39 | 1521 | 6.245 | 89 | 7921 | 9.434 |
| 40 | 1600 | 6.325 | 90 | 8100 | 9.487 |
| 41 | 1681 | 6.403 | 91 | 8281 | 9.539 |
| 42 | 1764 | 6.481 | 92 | 8464 | 9.592 |
| 43 | 1849 | 6.557 | 93 | 8649 | 9.644 |
| 44 | 1936 | 6.633 | 94 | 8836 | 9.695 |
| 45 | 2025 | 6.708 | 95 | 9025 | 9.747 |
| 46 | 2116 | 6.782 | 96 | 9216 | 9.798 |
| 47 | 2209 | 6.856 | 97 | 9409 | 9.849 |
| 48 | 2304 | 6.928 | 98 | 9604 | 9.899 |
| 49 | 2401 | 7.000 | 99 | 9801 | 9.950 |
| 50 | 2500 | 7.071 | 100 | 10,000 | 10.000 |

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| | | | | | | Comp | Compounded Annually | nually | | | | | | |
|----------|---------|---------|---------|---------|---------|---------|-------------------------|----------|----------|----------|----------|----------|----------|----------|
| | 5% | 6% | 7% | 8% | 6% | 10% | 11% | 12% | 13% | 14% | 15% | 16% | 17% | 18% |
| 1 year | 1.05000 | 1.06000 | 1.07000 | 1.08000 | 1.09000 | 1.10000 | 1.11000 | 1.12000 | 1.13000 | 1.14000 | 1.15000 | 1.16000 | 1.17000 | 1.18000 |
| 5 years | 1.27628 | 1.33823 | 1.40255 | 1.46933 | 1.53862 | 1.61051 | 1.68506 | 1.76234 | 1.84244 | 1.92541 | 2.01136 | 2.10034 | 2.19245 | 2.28776 |
| 10 years | 1.62889 | 1.79085 | 1.96715 | 2.15892 | 2.36736 | 2.59374 | 2.83942 | 3.10585 | 3.39457 | 3.70722 | 4.04556 | 4.41144 | 4.80683 | 5.23384 |
| 15 years | 2.07893 | 2.39656 | 2.75903 | 3.17217 | 3.64248 | 4.17725 | 4.78459 | 5.47357 | 6.25427 | 7.13794 | 8.13706 | 9.26552 | 10.53872 | 11.97375 |
| 20 years | 2.65330 | 3.20714 | 3.86968 | 4.66096 | 5.60441 | 6.72750 | 8.06231 | 9.64629 | 11.52309 | 13.74349 | 16.36654 | 19.46076 | 23.10560 | 27.39303 |
| | | | | | | Compou | Compounded Semiannually | annually | | | | | | |
| | 5% | 6% | 7% | 8% | %6 | 10% | 11% | 12% | 13% | 14% | 15% | 16% | 17% | 18% |
| 1 year | 1.05063 | 1.06090 | 1.07123 | 1.08160 | 1.09203 | 1.10250 | 1.11303 | 1.12360 | 1.13423 | 1.14490 | 1.15563 | 1.16640 | 1.17723 | 1.18810 |
| 5 years | 1.28008 | 1.34392 | 1.41060 | 1.48024 | 1.55297 | 1.62889 | 1.70814 | 1.79085 | 1.87714 | 1.96715 | 2.06103 | 2.15892 | 2.26098 | 2.36736 |
| 10 years | 1.63862 | 1.80611 | 1.98979 | 2.19112 | 2.41171 | 2.65330 | 2.91776 | 3.20714 | 3.52365 | 3.86968 | 4.24785 | 4.66096 | 5.11205 | 5.60441 |
| 15 years | 2.09757 | 2.42726 | 2.80679 | 3.24340 | 3.74532 | 4.32194 | 4.98395 | 5.74349 | 6.61437 | 7.61226 | 8.75496 | 10.06266 | 11.55825 | 13.26768 |
| 20 years | 2.68506 | 3.26204 | 3.95926 | 4.80102 | 5.81636 | 7.03999 | 8.51331 | 10.28572 | 12.41607 | 14.97446 | 18.04424 | 21.72452 | 26.13302 | 31.40942 |
| | | | | | | Compo | Compounded Quarterly | arterly | | | | | | |
| | 5% | 6% | %2 | 8% | %6 | 10% | 11% | 12% | 13% | 14% | 15% | 16% | 17% | 18% |
| 1 year | 1.05095 | 1.06136 | 1.07186 | 1.08243 | 1.09308 | 1.10381 | 1.11462 | 1.12551 | 1.13648 | 1.14752 | 1.15865 | 1.16986 | 1.18115 | 1.19252 |
| 5 years | 1.28204 | 1.34686 | 1.41478 | 1.48595 | 1.56051 | 1.63862 | 1.72043 | 1.80611 | 1.89584 | 1.98979 | 2.08815 | 2.19112 | 2.29891 | 2.41171 |
| 10 years | 1.64362 | 1.81402 | 2.00160 | 2.20804 | 2.43519 | 2.68506 | 2.95987 | 3.26204 | 3.59420 | 3.95926 | 4.36038 | 4.80102 | 5.28497 | 5.81636 |
| 15 years | 2.10718 | 2.44322 | 2.83182 | 3.28103 | 3.80013 | 4.39979 | 5.09225 | 5.89160 | 6.81402 | 7.87809 | 9.10513 | 10.51963 | 12.14965 | 14.02741 |
| 20 years | 2.70148 | 3.29066 | 4.00639 | 4.87544 | 5.93015 | 7.20957 | 8.76085 | 10.64089 | 12.91828 | 15.67574 | 19.01290 | 23.04980 | 27.93091 | 33.83010 |
| | | | | | | Con | Compounded Daily | Jaily | | | | | | |
| | 5% | 6% | %2 | 8% | %6 | 10% | 11% | 12% | 13% | 14% | 15% | 16% | 17% | 18% |
| 1 year | 1.05127 | 1.06183 | 1.07250 | 1.08328 | 1.09416 | 1.10516 | 1.11626 | 1.12747 | 1.13880 | 1.15024 | 1.16180 | 1.17347 | 1.18526 | 1.19716 |
| 5 years | 1.28400 | 1.34983 | 1.41902 | 1.49176 | 1.56823 | 1.64861 | 1.73311 | 1.82194 | 1.91532 | 2.01348 | 2.11667 | 2.22515 | 2.33918 | 2.45906 |
| 10 years | 1.64866 | 1.82203 | 2.01362 | 2.22535 | 2.45933 | 2.71791 | 3.00367 | 3.31946 | 3.66845 | 4.05411 | 4.48031 | 4.95130 | 5.47178 | 6.04696 |
| 15 years | 2.11689 | 2.45942 | 2.85736 | 3.31968 | 3.85678 | 4.48077 | 5.20569 | 6.04786 | 7.02625 | 8.16288 | 9.48335 | 11.01738 | 12.79950 | 14.86983 |
| 20 years | 2.71810 | 3.31979 | 4.05466 | 4.95216 | 6.04831 | 7.38703 | 9.02202 | 11.01883 | 13.45751 | 16.43582 | 20.07316 | 24.51533 | 29.94039 | 36.56577 |

Appendix

Unit Analysis

Let's suppose that you are traveling at a rate of 60 miles per hour. This means that

in 1 hour, your distance traveled is 60 miles;

in 2 hours, your distance traveled is $2 \cdot 60$ or 120 miles.

The rate 60 miles per hour can also be written as

| 60 mph, 60 miles per 1 hour, or $\frac{60 \text{ mil}}{1 \text{ hour}}$ | |
|---|--|
|---|--|

We can use rates such as $\frac{60 \text{ miles}}{1 \text{ hour}}$ to help us solve problems. Before we do this, notice that if 60 miles are traveled in 1 hour, then in 1 hour a distance of 60 miles is traveled and we also have the rate $\frac{1 \text{ hour}}{60 \text{ miles}}$, if needed.

Let's practice writing the fraction form of rates once again. The rate of 30 drops of medicine per liter of saline solution can be written as:

 $\frac{30 \text{ drops}}{1 \text{ liter}}$. If needed, we also have the rate $\frac{1 \text{ liter}}{30 \text{ drops}}$.

How do we know which version to use when solving a problem? As you will see in the examples, we use the rate that has *units to be divided out* in the *denominator* and *units asked to find* in the *numerator*.

Example 1

If you are traveling in a car at a rate of 60 miles per hour, how many miles do you travel in 21 hours?

Solution: Let's use a form of the given rate to help us answer this question. Since we are asked to find miles, we will multiply 21 hours by a version of the rate that has units to be divided out (hours) in the denominator and units asked to find (miles) in the numerator.

miles traveled in 21 hours = $\frac{21 \text{ hours}}{1} \cdot \frac{60 \text{ miles}}{1 \text{ hour}}$ = $\frac{21 \cdot 60}{1 \cdot 1}$ miles = 1260 miles

You travel 1260 miles in 21 hours.

Helpful Hint

Pay careful attention to units and how they divide out.

Example 2

If you are traveling at the rate of 60 miles per hour, how many hours does it take to travel 900 miles in the car?

Solution: Let's use a form of the given rate again. For this example, we are asked to find hours, so we will write a rate so that units to be divided out (miles) are in the denominator and units needed in the answer (hours) are in the numerator.

hours to travel 900 miles = $\frac{900 \text{ miles}}{1} \cdot \frac{1 \text{ hour}}{60 \text{ miles}}$ = $\frac{900 \cdot 1}{1 \cdot 60}$ hours = 15 hours

It takes 15 hours to travel 900 miles.

Helpful Hint

Remember: The rate you use depends on the exercise. A general rule is to use a factor that has units needed to divide out in the denominator and units asked to find in the numerator.

To solve some unit applications, it may be necessary to multiply by 2 or more rates. (More exercises involving unit conversions on length, weight, or mass can be found in the chapter on measurement, Chapter 7.)

Example 3 A telemarketer makes an average of 24 calls per hour. He is paid \$0.50 per call. If he worked 25 hours last week, calculate his earnings (before deductions).

Solution: To calculate his earnings, notice we multiply by two different rates.

earnings for 25 hours = $\frac{25 \text{ hours}}{1} \cdot \frac{24 \text{ calls}}{1 \text{ hour}} \cdot \frac{\$0.50}{1 \text{ call}}$ = $\frac{25 \cdot 24 \cdot \$0.50}{1 \cdot 1 \cdot 1}$ = \$300

He made \$300 last week.

B Exercise Set MyLab Math

- **1.** Suppose you make \$16 per hour.
 - **a.** Calculate your earnings (before deductions) for 40 hours.
 - **b.** How many hours of work are required to earn \$240 (before deductions)?
- **2.** A lab technician needs a solution containing 20 drops of concentrated medicine per liter of saline solution.
 - **a.** How many drops are needed for 17 liters of solution?
 - **b.** How many drops are needed for 280 liters of saline solution?
 - **c.** If you are told to make a solution using an entire container of 520 drops of medicine, how many liters of saline solution are needed?
- **3.** A hummingbird's wings beat an average of 90 beats per second.
 - **a.** How many beats occur during 14 seconds?
 - **b.** How much time (in seconds) has elapsed after 5400 wing beats? How much time is your answer in minutes?
 - **c.** How much time (in seconds) has elapsed after 8100 wing beats? How much time is your answer in minutes?
- **5.** Switzerland has an average of one hospital bed per 155 people (in population).
 - **a.** Suppose there is a city in Switzerland with a population of 31,000. At this rate, how many hospital beds are there in this city?
 - **b.** Suppose the only hospital in a city in Switzerland has 73 beds. Using the given rate, estimate the population of the city.
- **7.** A recipe calls for 3 cups of water for every 2 cups of flour.
 - **a.** If 9 cups of water are added, how many cups of flour are needed?
 - **b.** If 20 cups of water are added, how many cups of flour are needed?
 - **c.** If 15 cups of flour are added, how many cups of water are needed?
- **9.** A computer technician on an assembly line makes \$0.75 for her completion of each computer component. She can complete 26 components in an hour. If she worked 33 hours last week, what was her pay before deductions?

- **4.** Noah Wyle (of *ER*) was once the highest paid TV drama actor per episode. He earned \$400,000 per episode.
 - **a.** How much money did he make for 12 episodes?
 - **b.** How many episodes did he need to tape in order to earn \$6,800,000?
- **6.** Niger has an average of one hospital bed per 2000 people (in population).
 - **a.** Suppose there is a city in Niger with a population of 16,000. At this rate, how many hospital beds are there in this city?
 - **b.** Suppose the only hospital in a city in Niger has 21 beds. Using the given rate, estimate the population of the city.
- **8.** A recipe calls for 4 cups of sugar for every 3 cups of water.
 - **a.** If 12 cups of sugar are added, how many cups of water are needed?
 - **b.** If 14 cups of sugar are added, how many cups of water are needed?
 - **c.** If 20 cups of water are added, how many cups of sugar are needed?
- **10.** A cockroach is traveling at a rate of 3 miles per hour. Convert this speed to feet per second.

- **11.** A lab technician needs a solution containing 15 drops of concentrated medicine per liter of saline solution.
 - **a.** How many drops will be needed for 17.5 liters of solution?
 - **b.** How many liters will be needed for 300 drops of concentrated medicine?
- **13.** A tortilla-making machine makes 16 tortillas per minute.
 - a. How many tortillas can be made in 7.5 hours?
 - **b.** How long will it take to make 200 tortillas?
- **15.** Ray Romano (of *Everybody Loves Raymond*) was once the world's highest paid TV actor. He earned \$1.8 million per episode.
 - **a.** At this rate, how much money did he earn for 6 episodes?
 - **b.** How many episodes did he tape to earn \$8.1 million?
- **17.** A cheetah is the fastest known land animal and has been recorded traveling at speeds of 65 miles per hour. Suppose a particular cheetah is traveling at a speed of 45 miles per hour.
 - **a.** How far has the cheetah traveled in $\frac{1}{4}$ hour?
 - **b.** How long does it take the cheetah to travel 5 miles? Give your answer in hours and then in minutes.

- 12. A car travels at a rate of 57 miles per hour.a. How many miles does the car travel
 - in $5\frac{1}{2}$ hours?
 - **b.** At this rate, how many hours does it take to travel 627 miles in the car?
- 14. During a flood watch in New Orleans, Louisiana, an average of 0.5 inch of rain fell per hour for 48 hours.a. How much water fell during the first 21 hours?
 - **b.** At this given rate, how long did it take for 15.5 inches of rain to fall?
- **16.** Suppose a supporting actor in a television series makes \$18,000 per episode.
 - **a.** How much money does she make for 8 episodes?
 - **b.** How many episodes did she perform in to earn \$486,000?
 - **c.** According to this actor's contract, it is possible to pay her for fractional portions of episodes. How much money does she make for 12.5 episodes?
- **18.** The Gentoo penguin has a maximum speed of 27 kilometers per hour.
 - a. Convert this to miles per hour. (Round to the nearest tenth.) (*Hint*: 1 mile ≈ 1.61 km)
 - **b.** How far can the penguin travel in 10 minutes? Give your answer in miles.

Contents of Student Resources

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Attitude and Study Tips

Study Skills Builder 1

Have You Decided to Complete This Course Successfully?

Ask yourself if one of your current goals is to complete this course successfully.

If it is not a goal of yours, ask yourself why. One common reason is fear of failure. Amazingly enough, fear of failure alone can be strong enough to keep many of us from doing our best in any endeavor.

Another common reason is that you simply haven't taken the time to think about or write down your goals for this course. To help accomplish this, answer the questions below.

Exercises

1. Write down your goal(s) for this course.

- 2. Now list steps you will take to make sure your goal(s) in Exercise 1 are accomplished.
- **3.** Rate your commitment to this course with a number between 1 and 5. Use the diagram below to help.

| Η | ligh | Average No | | ot Committed | |
|------|---------|------------|---|--------------|--|
| Comr | nitment | Commitment | | at All | |
| 5 | 4 | 3 | 2 | 1 | |

4. If you have rated your personal commitment level (from the exercise above) as a 1, 2, or 3, list the reasons why this is so. Then determine whether it is possible to increase your commitment level to a 4 or 5.

Good luck, and don't forget that a positive attitude will make a big difference.

Tips for Studying for an Exam To prepare for an exam, try the following study techniques:

- Start the study process days before your exam.
- Make sure that you are up to date on your assignments.
- If there is a topic that you are unsure of, use one of the many resources that are available to you. For example,

See your instructor. View a lecture video on the topic. Visit a learning resource center on campus. Read the textbook material and examples on the topic.

- Reread your notes and carefully review the Chapter Highlights at the end of any chapter.
- Work the review exercises at the end of the chapter.
- Find a quiet place to take the Chapter Test found at the end of the chapter. Do not use any resources when taking this sample test. This way, you will have a clear indication of how prepared you are for your exam. Check your answers and use the Chapter Test Prep Videos to make sure that you correct any missed exercises.

Good luck, and keep a positive attitude.

Exercises

Let's see how you did on your last exam.

- **1.** How many days before your last exam did you start studying for that exam?
- 2. Were you up to date on your assignments at that time or did you need to catch up on assignments?
- 3. List the most helpful text supplement (if you used one).
- **4.** List the most helpful campus supplement (if you used one).
- 5. List your process for preparing for a mathematics test.
- **6.** Was this process helpful? In other words, were you satisfied with your performance on your exam?
- **7.** If not, what changes can you make in your process that will make it more helpful to you?

Study Skills Builder 3

What to Do the Day of an Exam

Your first exam may be soon. On the day of an exam, don't forget to try the following:

- Allow yourself plenty of time to arrive.
- Read the directions on the test carefully.
- Read each problem carefully as you take your test. Make sure that you answer the question asked.
- Watch your time and pace yourself so that you may attempt each problem on your test.
- Check your work and answers.
- *Do not turn your test in early.* If you have extra time, spend it double-checking your work.

Good luck!

Exercises

Answer the following questions based on your most recent mathematics exam, whenever that was.

- 1. How soon before class did you arrive?
- **2.** Did you read the directions on the test carefully?
- **3.** Did you make sure you answered the question asked for each problem on the exam?
- 4. Were you able to attempt each problem on your exam?
- 5. If your answer to Exercise 4 is no, list reasons why.
- 6. Did you have extra time on your exam?
- 7. If your answer to Exercise 6 is yes, describe how you spent that extra time.

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Are You Satisfied with Your Performance on a Particular Quiz or Exam?

If not, don't forget to analyze your quiz or exam and look for common errors. Were most of your errors a result of:

- *Carelessness*? Did you turn in your quiz or exam before the allotted time expired? If so, resolve to use any extra time to check your work.
- *Running out of time?* Answer the questions you are sure of first. Then attempt the questions you are unsure of, and delay checking your work until all questions have been answered.
- *Not understanding a concept?* If so, review that concept and correct your work so that you make sure you understand it before the next quiz or the final exam.
- *Test conditions?* When studying for a quiz or exam, make sure you place yourself in conditions similar to test conditions. For example, before your next quiz or exam, take a sample test without the aid of your notes or text.

(For a sample test, see your instructor or use the Chapter Test at the end of each chapter.)

Exercises

- 1. Have you corrected all your previous quizzes and exams?
- **2.** List any errors you have found common to two or more of your graded papers.
- **3.** Is one of your common errors not understanding a concept? If so, are you making sure you understand all the concepts for the next quiz or exam?
- **4.** Is one of your common errors making careless mistakes? If so, are you now taking all the time allotted to check over your work so that you can minimize the number of careless mistakes?
- **5.** Are you satisfied with your grades thus far on quizzes and tests?
- 6. If your answer to Exercise 5 is no, are there any more suggestions you can make to your instructor or yourself to help? If so, list them here and share these with your instructor.

Study Skills Builder 5

How Are You Doing?

If you haven't done so yet, take a few moments and think about how you are doing in this course. Are you working toward your goal of successfully completing this course? Is your performance on homework, quizzes, and tests satisfactory? If not, you might want to see your instructor to see if he/she has any suggestions on how you can improve your performance. Reread Section 1.1 for ideas on places to get help with your mathematics course.

Exercises

Answer the following.

- **1.** List any textbook supplements you are using to help you through this course.
- **2.** List any campus resources you are using to help you through this course.
- **3.** Write a short paragraph describing how you are doing in your mathematics course.
- **4.** If improvement is needed, list ways that you can work toward improving your situation as described in Exercise **3**.

Are You Preparing for Your Final Exam?

To prepare for your final exam, try the following study techniques:

- Review the material that you will be responsible for on your exam. This includes material from your textbook, your notebook, and any handouts from your instructor.
- Review any formulas that you may need to memorize.
- Check to see if your instructor or mathematics department will be conducting a final exam review.
- Check with your instructor to see whether final exams from previous semesters/quarters are available to students for review.
- Use your previously taken exams as a practice final exam. To do so, rewrite the test questions in mixed order on blank sheets of paper. This will help you prepare for exam conditions.
- If you are unsure of a few concepts, see your instructor or visit a learning lab for assistance. Also, view the video segment of any troublesome sections.
- If you need further exercises to work, try the Cumulative Reviews at the end of the chapters.

Once again, good luck! I hope you are enjoying this textbook and your mathematics course.

Organizing Your Work

Study Skills Builder 7

Learning New Terms

Many of the terms used in this text may be new to you. It will be helpful to make a list of new mathematical terms and symbols as you encounter them and to review them frequently. Placing these new terms (including page references) on 3×5 index cards might help you later when you're preparing for a quiz.

Exercises

- 1. Name one way you might place a word and its definition on a 3 \times 5 card.
- **2.** How do new terms stand out in this text so that they can be found?

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Are You Organized?

Have you ever had trouble finding a completed assignment? When it's time to study for a test, are your notes neat and organized? Have you ever had trouble reading your own mathematics handwriting? (Be honest—I have.)

When any of these things happens, it's time to get organized. Here are a few suggestions:

- Write your notes and complete your homework assignments in a notebook with pockets (spiral or ring binder).
- Take class notes in this notebook, and then follow the notes with your completed homework assignment.
- When you receive graded papers or handouts, place them in the notebook pocket so that you will not lose them.
- Mark (possibly with an exclamation point) any note(s) that seem extra important to you.
- Mark (possibly with a question mark) any notes or homework that you are having trouble with.
- See your instructor or a math tutor to help you with the concepts or exercises that you are having trouble understanding.

• If you are having trouble reading your own handwriting, *slow down* and write your mathematics work clearly!

Exercises

- 1. Have you been completing your assignments on time?
- **2.** Have you been correcting any exercises you may be having difficulty with?
- **3.** If you are having trouble with a mathematical concept or correcting any homework exercises, have you visited your instructor, a tutor, or your campus math lab?
- **4.** Are you taking lecture notes in your mathematics course? (By the way, these notes should include worked-out examples solved by your instructor.)
- **5.** Is your mathematics course material (handouts, graded papers, lecture notes) organized?
- 6. If your answer to Exercise 5 is no, take a moment and review your course material. List at least two ways that you might better organize it.

Organizing a Notebook

It's never too late to get organized. If you need ideas about organizing a notebook for your mathematics course, try some of these:

- Use a spiral or ring binder notebook with pockets and use it for mathematics only.
- Start each page by writing the book's section number you are working on at the top.
- When your instructor is lecturing, take notes. *Always* include any examples your instructor works for you.
- Place your worked-out homework exercises in your notebook immediately after the lecture notes from that section. This way, a section's worth of material is together.
- Homework exercises: Attempt and check all assigned homework.
- Place graded quizzes in the pockets of your notebook or a special section of your binder.

Exercises

Check your notebook organization by answering the following questions.

- **1.** Do you have a spiral or ring binder notebook for your mathematics course only?
- **2.** Have you ever had to flip through several sheets of notes and work in your mathematics notebook to determine what section's work you are in?
- **3.** Are you now writing the textbook's section number at the top of each notebook page?
- **4.** Have you ever lost or had trouble finding a graded quiz or test?
- **5.** Are you now placing all your graded work in a dedicated place in your notebook?
- **6.** Are you attempting all of your homework and placing all of your work in your notebook?
- **7.** Are you checking and correcting your homework in your notebook? If not, why not?
- **8.** Are you writing in your notebook the examples your instructor works for you in class?

Study Skills Builder 10

How Are Your Homework Assignments Going?

It is very important in mathematics to keep up with homework. Why? Many concepts build on each other. Often your understanding of a day's concepts depends on an understanding of the previous day's material.

Remember that completing your homework assignment involves a lot more than attempting a few of the problems assigned.

To complete a homework assignment, remember these four things:

- Attempt all of it.
- Check it.
- Correct it.
- If needed, ask questions about it.

Exercises

Take a moment and review your completed homework assignments. Answer the questions below based on this review.

- **1.** Approximate the fraction of your homework you have attempted.
- **2.** Approximate the fraction of your homework you have checked (if possible).
- **3.** If you are able to check your homework, have you corrected it when errors have been found?
- **4.** When working homework, if you do not understand a concept, what do you do?

MyLab Math and MathXL

Study Skills Builder 11

Tips for Turning In Your Homework on Time

It is very important to keep up with your mathematics homework assignments. Why? Many concepts in mathematics build upon each other.

Remember these 4 tips to help ensure your work is completed on time:

- Know the assignments and due dates set by your instructor.
- Do not wait until the last minute to submit your homework.
- Set a goal to submit your homework 6–8 hours before the scheduled due date in case you have unexpected technology trouble.
- Schedule enough time to complete each assignment.

Following the tips above will also help you avoid potentially losing points for late or missed assignments.

Exercises

Take a moment to consider your work on your homework assignments to date and answer the following questions:

- **1.** What percentage of your assignments have you turned in on time?
- **2.** Why might it be a good idea to submit your homework 6–8 hours before the scheduled deadline?
- **3.** If you have missed submitting any homework by the due date, list some of the reasons why this occurred.
- **4.** What steps do you plan to take in the future to ensure your homework is submitted on time?

Study Skills Builder 12

Tips for Doing Your Homework Online

Practice is one of the main keys to success in any mathematics course. Did you know that MyLab Math/MathXL provides you with **immediate feedback** for each exercise? If you are incorrect, you are given hints to work the exercise correctly. You have **unlimited practice opportunities** and can rework any exercises you have trouble with until you master them, and submit homework assignments unlimited times before the deadline.

Remember these success tips when doing your homework online:

- Attempt all assigned exercises.
- Write down (neatly) your step-by-step work for each exercise before entering your answer.
- Use the immediate feedback provided by the program to help you check and correct your work for each exercise.
- Rework any exercises you have trouble with until you master them.
- Work through your homework assignment as many times as necessary until you are satisfied.

Exercises

Take a moment to think about your homework assignments to date and answer the following:

- **1.** Have you attempted all assigned exercises?
- 2. Of the exercises attempted, have you also written out your work before entering your answer—so that you can check it?
- **3.** Are you familiar with how to enter answers using the MathXL player so that you avoid answer entry type errors?
- **4.** List some ways the immediate feedback and practice supports have helped you with your homework. If you have not used these supports, how do you plan to use them with the success tips above on your next assignment?

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Organizing Your Work

Have you ever used any readily available paper (such as the back of a flyer, another course assignment, postits, etc.) to work out homework exercises before entering the answer in MathXL? To save time, have you ever entered answers directly into MathXL without working the exercises on paper? When it's time to study, have you ever been unable to find your completed work or read and follow your own mathematics handwriting?

When any of these things happen, it's time to get organized. Here are some suggestions:

- Write your step-by-step work for each homework exercise, (neatly) on lined, loose-leaf paper and keep this in a 3-ring binder.
- Refer to your step-by-step work when you receive feedback that your answer is incorrect in MathXL. Double-check against the steps and hints provided by the program and correct your work accordingly.
- Keep your written homework with your class notes for that section.

- Identify any exercises you are having trouble with and ask questions about them.
- Keep all graded quizzes and tests in this binder as well to study later.

If you follow the suggestions above, you and your instructor or tutor will be able to follow your steps and correct any mistakes. You will also have a written copy of your work to refer to later to ask questions and study for tests.

Exercises

- **1.** Why is it important that you write out your step-by-step work on homework exercises and keep a hard copy of all work submitted online?
- **2.** If you have gotten an incorrect answer, are you able to follow your steps and find your error?
- **3.** If you were asked today to review your previous homework assignments and first test, could you find them? If not, list some ways you might better organize your work.

Study Skills Builder 14

Getting Help with Your Homework Assignments

There are many helpful resources available to you through MathXL to help you work through any homework exercises you may have trouble with. It is important that you know what these resources are and know when and how to use them.

Let's review these features found in the homework exercises:

- Help Me Solve This—provides step-by-step help for the exercise you are working. You must work an additional exercise of the same type (without this help) before you can get credit for having worked it correctly.
- View an Example—allows you to view a correctly worked exercise similar to the one you are having trouble with. You can go back to your original exercise and work it on your own.
- **E-Book**—allows you to read examples from your text and find similar exercises.

- **Video**—your text author, Elayn Martin-Gay, works an exercise similar to the one you need help with. **Not all exercises have an accompanying video clip.
- Ask My Instructor allows you to e-mail your instructor for help with an exercise.

Exercises

- 1. How does the "Help Me Solve This" feature work?
- **2.** If the "View an Example" feature is used, is it necessary to work an additional problem before continuing the assignment?
- **3.** When might be a good time to use the "Video" feature? Do all exercises have an accompanying video clip?
- **4.** Which of the features above have you used? List those you found the most helpful to you.
- **5.** If you haven't used the features discussed, list those you plan to try on your next homework assignment.

Student Resources

Tips for Preparing for an Exam

Did you know that you can rework your previous homework assignments in MyLab Math and MathXL? This is a great way to prepare for tests. To do this, open a previous homework assignment and click "similar exercise." This will generate new exercises similar to the homework you have submitted. You can then rework the exercises and assignments until you feel confident that you understand them.

To prepare for an exam, follow these tips:

- Review your written work for your previous homework assignments along with your class notes.
- Identify any exercises or topics that you have questions on or have difficulty understanding.
- Rework your previous assignments in MyLab Math and MathXL until you fully understand them and can do them without help.
- Get help for any topics you feel unsure of or for which you have questions.

Exercises

- 1. Are your current homework assignments up to date and is your written work for them organized in a binder or notebook? If the answer is no, it's time to get organized. For tips on this, see Study Skills Builder 13—Organizing Your Work.
- **2.** How many days in advance of an exam do you usually start studying?
- **3.** List some ways you think that practicing previous homework assignments can help you prepare for your test.
- **4.** List two or three resources you can use to get help for any topics you are unsure of or have questions on.

Good luck!

Study Skills Builder 16

How Well Do You Know the Resources Available to You in MyLab Math?

There are many helpful resources available to you in MyLab Math. Let's take a moment to locate and explore a few of them now. Go into your MyLab Math course, and visit the multimedia library, tools for success, and E-book. Let's see what you found.

Exercises

1. List the resources available to you in the Multimedia Library.

- **2.** List the resources available to you in the Tools for Success folder.
- **3.** Where did you find the English/Spanish Audio Glossary?
- 4. Can you view videos from the E-Book?
- **5.** Did you find any resources you did not know about? If so, which ones?
- **6.** Which resources have you used most often or found most helpful?

Additional Help Inside and Outside Your Textbook

Study Skills Builder 17

How Well Do You Know Your Textbook?

The questions below will help determine whether you are familiar with your textbook. For additional information, see Section 1.1 in this text.

Exercises

- **1.** What does the **>** icon mean?
- **2.** What does the \leftharpoonup icon mean?
- **3.** What does the \triangle icon mean?
- **4.** Where can you find a review for each chapter? What answers to this review can be found in the back of your text?

- **5.** Each chapter contains an overview of the chapter along with examples. What is this feature called?
- **6.** Each chapter contains a review of vocabulary. What is this feature called?
- **7.** There are practice exercises that are contained in this text. What are they and how can they be used?
- **8.** This text contains a student section in the back entitled Student Resources. List the contents of this section and how they might be helpful.
- **9.** What exercise answers are available in this text? Where are they located?

Study Skills Builder 18

Are You Familiar with Your Textbook Supplements?

Below is a review of some of the student supplements available for additional study. Check to see if you are using the ones most helpful to you.

- Chapter Test Prep Videos. These videos provide video clip solutions to the Chapter Test exercises in this text. You will find this extremely useful when studying for tests or exams.
- Interactive DVD Lecture Series. These are keyed to each section of the text. The material is presented by me, Elayn Martin-Gay, and I have placed a O by the exercises in the text that I have worked on the video.
- The *Student Solutions Manual*. This contains workedout solutions to odd-numbered exercises as well as every exercise in the Integrated Reviews, Chapter Reviews, Chapter Tests, and Cumulative Reviews.
- Pearson Tutor Center. Mathematics questions may be phoned, faxed, or e-mailed to this center.
- MyLab Math is a text-specific online course. MathXL is an online homework, tutorial, and assessment system.

Take a moment and determine whether these are available to you.

As usual, your instructor is your best source of information.

Exercises

Let's see how you are doing with textbook supplements.

- 1. Name one way the Lecture Videos can be helpful to you.
- **2.** Name one way the Chapter Test Prep Video can help you prepare for a chapter test.
- **3.** List any textbook supplements that you have found useful.
- **4.** Have you located and visited a learning resource lab located on your campus?
- **5.** List the textbook supplements that are currently housed in your campus's learning resource lab.

Are You Getting All the Mathematics Help That You Need?

Remember that, in addition to your instructor, there are many places to get help with your mathematics course. For example:

- This text has an accompanying video lesson for every section and the CD in this text contains worked-out solutions to every Chapter Test exercise.
- The back of the book contains answers to oddnumbered exercises and selected solutions.
- A *Student Solutions Manual* is available that contains worked-out solutions to odd-numbered exercises as well as solutions to every exercise in the Integrated Reviews, Chapter Reviews, Chapter Tests, and Cumulative Reviews.
- Don't forget to check with your instructor for other local resources available to you, such as a tutoring center.

Exercises

- **1.** List items you find helpful in the text and all student supplements to this text.
- **2.** List all the campus help that is available to you for this course.
- 3. List any help (besides the textbook) from Exercises 1 and 2 above that you are using.
- **4.** List any help (besides the textbook) that you feel you should try.
- **5.** Write a goal for yourself that includes trying everything you listed in Exercise **4** during the next week.

Bigger Picture— Study Guide Outline

- I. Some Operations on Sets of Numbers
 - A. Whole Numbers

| 1. Add or Subtract: (Sec. 1.3, 1.4) 14 | 300 |
|---|------------------------|
| + 39 _ | 27 |
| 53 | 273 |
| 2. Multiply or Divide: (Sec. 1.6, 1.7) 238 | <u>127</u> R2
7)891 |
| $\frac{\times 47}{1666}$ | <u> </u> |
| 9520 | 19 |
| <u> </u> | $\frac{-14}{-14}$ |
| 11,100 | 51 |
| | -49 |
| | 2 |

3. Exponent: (Sec. 1.9) 4 factors of 3

$$3^4 = 3 \cdot 3 \cdot 3 \cdot 3 = 81$$

4. Square Root: (Sec. 1.9)

 $\sqrt{25} = 5$ because $5 \cdot 5 = 25$ and 5 is a positive number.

5. Order of Operations: (Sec. 1.9)

| $24 \div 3 \cdot 2 - (2 + 8) = 24 \div 3 \cdot 2 - (10)$ | Parentheses. |
|--|--|
| $= 8 \cdot 2 - 10$ | Multiply or divide from left to right. |
| = 16 - 10 | Multiply or divide from left to right. |
| = 6 | Add or subtract from left to right. |

B. Fractions

1. Simplify: Factor the numerator and denominator. Then divide out factors of 1 by dividing out common factors in the numerator and denominator. (Sec. 2.3)

Simplify: $\frac{20}{28} = \frac{4 \cdot 5}{4 \cdot 7} = \frac{5}{7}$

- **2. Multiply:** Numerator times numerator over denominator times denominator. (Sec. 2.4)
 - $\frac{5}{9} \cdot \frac{2}{7} = \frac{10}{63}$
- **3.** Divide: First fraction times the reciprocal of the second fraction. (Sec. 2.5)

$$\frac{2}{11} \div \frac{3}{4} = \frac{2}{11} \cdot \frac{4}{3} = \frac{8}{33}$$

4. Add or Subtract: Must have same denominators. If not, find the LCD, and write each fraction as an equivalent fraction with the LCD as denominator. (Sec. 3.3)

$$\frac{2}{5} + \frac{1}{15} = \frac{2}{5} \cdot \frac{3}{3} + \frac{1}{15} = \frac{6}{15} + \frac{1}{15} = \frac{7}{15}$$

C. Decimals

1. Add or Subtract: Line up decimal points. (Sec. 4.3) 1.27

D. Signed Numbers

1. Add: (Sec. 10.2) -5 + (-2) = -7 Adding like signs. Add absolute value

Add absolute value. Attach the common sign. -5 + 2 = -3 Adding unlike signs. Subtract absolute values. Attach the sign of

- the number with the larger absolute value.
- **2.** Subtract: Add the first number to the opposite of the second number. (Sec. 10.3)

7 - 10 = 7 + (-10) = -3

3. Multiply or Divide: Multiply or divide as usual. If the signs of the two numbers are the same, the answer is positive. If the signs of the two numbers are different, the answer is negative. (Sec. 10.4)

$$-5 \cdot 5 = -25$$
 $\frac{-32}{-8} = 4$

II. Solving Equations

A. Proportions: Set cross products equal to each other. Then solve. (Sec. 5.3) 14 2 6 3

 $\frac{14}{3} = \frac{2}{n}, \text{ or } 14 \cdot n = 3 \cdot 2, \text{ or } 14 \cdot n = 6, \text{ or } n = \frac{6}{14} = \frac{3}{7}$

B. Percent Problems

1. Solved by Equations: Remember that "of" means multiplication and "is" means equals. (Sec. 6.3)

"12% of some number is 6" translates to

 $12\% \cdot n = 6 \text{ or } 0.12 \cdot n = 6 \text{ or } n = \frac{6}{0.12} \text{ or } n = 50$

2. Solved by Proportions: Remember that percent, *p*, is identified by % or percent; base, *b*, usually appears after "of"; and amount, *a*, is the part compared to the whole. (Sec. 6.4)

"12% of some number is 6" translates to

$$\frac{6}{b} = \frac{12}{100} \text{ or } 6 \cdot 100 = b \cdot 12 \text{ or } 600 = b \cdot 12 \text{ or } \frac{600}{12} = b \text{ or } 50 = b$$

C. Equations in General: Simplify both sides of the equation by removing parentheses and combining any like terms. Then use the Addition Property to write variable terms on one side, constants (or numbers) on the other side. Then use the Multiplication Property to solve for the variable by dividing both sides of the equation by the coefficient of the variable. (Sec. 11.4)

Solve: 2(x - 5) = 80 2x - 10 = 80 Use the distributive property. 2x - 10 + 10 = 80 + 10 Add 10 to both sides. 2x = 90 Simplify. $\frac{2x}{2} = \frac{90}{2}$ Divide both sides by 2. x = 45 Simplify.

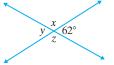
Practice Final Exam

| 1. | Note: Exercises 1–41 review operativ
For exercises 1–11, simplify by perfo
For exercises 12–19, solve. | | |
|-------------------|--|--------------------|--|
| 2. | 1. 600 – 487 | 2. | $(2^4 - 5) \cdot 3$ |
| 3.
4. | 3. $\frac{16}{3} \div \frac{3}{12}$ | 4. | $\frac{11}{12} + \frac{3}{8} + \frac{5}{24}$ |
| <u>5.</u>
6. | 5. $\frac{64 \div 8 \cdot 2}{(\sqrt{9} - \sqrt{4})^2 + 1}$ | 6. | $\frac{10.2}{\times 4.3}$ |
| 7. 8. | 7. $\frac{0.23 + 1.63}{0.3}$ | 8. | $5\frac{1}{6}$ $-3\frac{7}{8}$ |
| <u>9.</u>
10. | 9. $3\frac{1}{3} \cdot 6\frac{3}{4}$ | 10. | 126.9 × 100 |
| 11. | 11. $\left(\frac{3}{4}\right)^2 \div \left(\frac{2}{3} + \frac{5}{6}\right)$ | 12. | Round 52,369 to the nearest thousand. |
| 12.
13. | 13. Round 34.8923 to the nearest | tenth. 14. | Write $\frac{16}{17}$ as a decimal. Round to the nearest thousandth. |
| <u>14.</u>
15. | 15. Write 85% as a decimal. | 16. | Write 6.1 as a percent. |
| 16. | 17. Write $\frac{3}{8}$ as a percent. | 18. | Write 0.2% as a fraction in simplest form. |
| 17 | 19. Find the perimeter and the ar | ea of the rectang | le below. |
| 18. | | Rectangle | $\frac{2}{3}$ foot |
| <u>19.</u> | | 1 foot | |
| 20. | Write each ratio or rate as a fraction | n in simplest form | - · |
| 21. | 20. 4500 trees to 6500 trees | 21. | 9 inches of rain in 30 days |
| 22. | 22. Find the unit rate: 650 kilometers in 8 hours | | |

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| 23. | Find each unit price and decide which
is the better buy.
Jelly:
\$1.49 for 16 ounces | 24. | Find the unknown number, <i>n</i> , in the proportion:
$\frac{8}{n} = \frac{11}{6}$ | <u>23.</u> |
|------|---|----------|--|------------|
| | \$2.39 for 24 ounces | | | 24. |
| Solv | Ре. | | | 25. |
| 25. | Subtract 8.6 from 20. | 26. | A small airplane used $58\frac{3}{4}$ gallons of | |
| | | | fuel on a $7\frac{1}{2}$ -hour trip. How many gal- | 26. |
| | | | lons of fuel were used for each hour? | |
| 27. | Jerome Grant worked 6 hours and | 28. | Twenty-nine cans of Sherwin-Williams | 27. |
| | packed 86 cartons of books. At this
rate, how many cartons can he pack in
8 hours? | | paint cost \$493. How much was each can? | 28. |
| | | | | |
| 29. | 0.6% of what number is 7.5? | 30. | 567 is what percent of 756? | 29. |
| 31. | An alloy is 12% copper. How much copper is contained in 320 pounds of | 32. | A \$120 framed picture is on sale for 15% off. Find the discount and the | 30. |
| | this alloy? | | sale price. | 31. |
| Con | wert. | | | <u>51.</u> |
| | 2.4 kg to grams | 34 | $2\frac{1}{2}$ gal to quarts | 32. |
| | 2.1 kg to grains | 04. | 2^{2} gar to quarts | |
| 35. | If 2 ft 9 in. of material is used to manu- | 36. | Find the complement of a 78° angle. | 33. |
| | facture one scarf, how much material is needed for 6 scarves? | | 1 0 | |
| | needed for 0 scarves: | | | 34. |
| 37. | Find the measures of angles x , y , and z . | 38. | Find the measure of $\angle x$. | |
| | x | | 92° | 35. |
| | y x 62° | | 62° x | 36. |
| | | | | <u> </u> |
| 39. | Given that the following triangles are sin | nilar, i | find the missing length <i>n</i> . | 37. |
| | |) | | |
| | ° | , | 5 | 38. |
| | 12 | | n | |
| | | | | 39. |
| 40. | Find the mean, median, and mode of the | list of | f numbers. 26, 32, 42, 43, 49 | |
| | | | | 40. |

- **25.** Subtract 8.6 from 2
- **27.** Jerome Grant work packed 86 cartons rate, how many car 8 hours?
- **29.** 0.6% of what number 0.6%
- **31.** An alloy is 12% cop copper is contained this alloy?
- Convert.
- **33.** 2.4 kg to grams
- **35.** If 2 ft 9 in. of mater facture one scarf, h needed for 6 scarve
- **37.** Find the measures



| 796 | Practice Final Exam |
|--------------------------|--|
| <u>41.</u> | A professor measures the heights of the students in her class. The results are shown in the following histogram. Use this histogram to answer Exercise 41. |
| <u>42.</u>
<u>43.</u> | Student Heights |
| <u>44.</u> | 41. How many students are $5'7''$ or shorter? |
| 45 | Note: Exercises 42–51 may contain signed numbers.
Simplify by performing the indicated operations.
42. $(-5)^3 - 24 \div (-3)$
43. $-7 - (-19)$ |
| <u>46.</u> | |
| 47 | 44. $\frac{-3(-2) + 12}{-1(-4-5)}$ 45. $\left(\frac{5}{9} - \frac{7}{9}\right)^2 + \left(-\frac{2}{9}\right)$ |
| 48 | 46. Evaluate: $\frac{3x-5}{2y}$ when $x = 7$ and $y = -8$
47. Multiply, then simplify: $5(3z+2) - z - 18$ |
| <u>49.</u> | Solve.
48. $-\frac{5}{8}x = -25$ 49. $5x + 12 - 4x - 14 = 22$ |
| 50. | 50. $3x - 5 = -11$
51. In a 10-kilometer race, there are 112 more men entered than women. Find the number of women runners if the total number of runners in the race is 600. |
| 51. | race is 600. |

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Answers to Selected Exercises

Chapter 1 The Whole Numbers

Section 1.2

Vocabulary, Readiness & Video Check 1. whole 3. words 5. period 7. hundreds 9. 80,000

Exercise Set 1.2 1. tens **3.** thousands **5.** hundred-thousands **7.** millions **9.** three hundred fifty-four **11.** eight thousand, two hundred seventy-nine **13.** twenty-six thousand, nine hundred ninety **15.** two million, three hundred eighty-eight thousand **17.** twenty-four million, three hundred fifty thousand, one hundred eighty-five **19.** three hundred twenty-two thousand, six hundred fifty-three **21.** two thousand, seven hundred seventeen **23.** one hundred one million, five hundred thousand **25.** fourteen thousand, four hundred thirty-three **27.** twenty-two million, three hundred thirty-eight thousand, six hundred eighteen **29.** 6587 **31.** 59,800 **33.** 13,601,011 **35.** 7,000,017 **37.** 260,997 **39.** 418 **41.** 16,732 **43.** \$119,119,000 **45.** 108,000 **47.** 400 + 6 **49.** 3000 + 400 + 70 **51.** 80,000 + 700 + 70 + 4 **53.** 60,000 + 6000 + 40 + 9 **55.** 30,000,000 + 9,000,000 + 600,000 + 80,000 **57.** 5532; five thousand, five hundred thirty-two **59.** 5000 + 400 + 90 + 2 **61.** Mt. Washington **63.** National Gallery **65.** six million, two thousand **67.** 3 **69.** 9861 **71.** no; one hundred five **73.** answers may vary **75.** 93,000,000,000,000,000,000 **77.** Canton

Section 1.3

Calculator Explorations 1. 134 3. 340 5. 2834

Vocabulary, Readiness & Video Check 1. number 3. sum; addend 5. grouping; associative 7. place; right; left 9. increased by

Exercise Set 1.3 1. 36 3. 292 5. 49 7. 5399 9. 117 11. 512 13. 209,078 15. 25 17. 62 19. 212 21. 94 23. 910 25. 8273 27. 11,926 29. 1884 31. 16,717 33. 1110 35. 8999 37. 35,901 39. 632,389 41. 42 in. 43. 25 ft 45. 24 in. 47. 8 yd 49. 29 in. 51. 44 m 53. 2093 55. 266 57. 544 59. 3452 61. 22,434 thousand 63. 6684 ft 65. 340 ft 67. 2425 ft 69. 262,191 71. 115,310 F-Series trucks and Silverados 73. 124 ft 75. 3275 77. California 79. 2282 81. Florida and Georgia 83. 6358 mi 85. answers may vary 87. answers may vary 89. 1,044,473,765 91. correct 93. incorrect: 530

Section 1.4

Calculator Explorations 1. 770 3. 109 5. 8978

Vocabulary, Readiness & Video Check 1. 0 **3.** minuend; subtrahend **5.** 0 **7.** 600 **9.** We cannot take 7 from 2 in the ones place, so we borrow one ten from the tens place and move it over to the ones place to give us 10 + 2 or 12.

Exercise Set 1.4 1. 44 3. 265 5. 135 7. 2254 9. 5545 11. 600 13. 25 15. 45 17. 146 19. 288 21. 168 23. 106 25. 447 27. 5723 29. 504 31. 89 33. 79 35. 39,914 37. 32,711 39. 5041 41. 31,213 43. 4 45. 20 47. 7 49. 72 51. 88 53. 264 pages 55. 5 million sq km 57. 264,000 sq mi 59. 283,000 sq mi 61. 6065 ft 63. 28 ft 65. 358 mi 67. \$619 69. 1609 thousand 71. 100 dB 73. 58 dB 75. 30 77. 5920 sq ft 79. Hartsfield-Jackson Atlanta International 81. 12 million 83. Jo; by 271 votes 85. 1034 87. 9 89. 8518 91. 22,876 93. minuend: 48; subtrahend: 1 95. minuend: 70; subtrahend: 7 97. incorrect: 685 99. correct 101. 5269 - 2385 = 2884 103. no; answers may vary 105. no: 1089 more pages

Section 1.5

Vocabulary, Readiness & Video Check 1. graph **3.** 70;60 **5.** 3 is in the place value we're rounding to (tens), and the digit to the right of this place value is 5 or greater, so we need to add 1 to the 3. **7.** Each circled digit is to the right of the place value being rounded to and is used to determine whether or not we add 1 to the digit in the place value being rounded to.

Exercise Set 1.5 1. 420 3. 640 5. 2800 7. 500 9. 21,000 11. 34,000 13. 328,500 15. 36,000 17. 39,990 19. 30,000,000 21. 5280; 5300; 5000 23. 9440; 9400; 9000 25. 14,880; 14,900; 15,000 27. 27,000 students 29. 38,000 points 31. \$150,000,000,000 33. \$4,200,000 35. 220,000,000 smart phone users 37. 130 39. 80 41. 5700 43. 300 45. 11,400 47. incorrect 49. correct 51. correct 53. \$3400 55. 900 mi 57. 6000 ft 59. 1,000,000,000 pieces 61. 182,000 children 63. \$12,140,000,000; \$12,100,000,000 65. \$2,110,000,000; \$2,100,000,000 67. 5723, for example 69. 1000 71. 0 73. 8550 75. answers may vary 77. 140 m

Section 1.6

Calculator Explorations 1. 3456 3. 15,322 5. 272,291

Vocabulary, Readiness & Video Check 1. 0 **3.** product; factor **5.** grouping; associative **7.** length **9.** distributive property **11.** Think of the problem as 50 times 9 and then attach the two zeros from 900, or think of the problem as 5 times 9 and then attach the three zeros at the end of 50 and 900. Both approaches give us 45,000. **13.** Multiplication is also an application of addition since it is addition of the same addend.

A2

 Exercise Set 1.6
 1. 24
 3. 0
 5. 0
 7. 87
 9. $6 \cdot 3 + 6 \cdot 8$ 11. $4 \cdot 3 + 4 \cdot 9$ 13. $20 \cdot 14 + 20 \cdot 6$ 15. 512
 17. 3678

 19. 1662
 21. 6444
 23. 1157
 25. 24,418
 27. 24,786
 29. 15,600
 31. 0
 33. 6400
 35. 48,126
 37. 142,506
 39. 2,369,826

 41. 64,790
 43. 3,949,935
 45. 800
 47. 11,000
 49. 74,060
 51. 24,000
 53. 45,000
 55. 3,280,000
 57. area: 63 sq m;

 perimeter: 32 m
 59. area: 680 sq ft; perimeter: 114 ft
 61. 240,000
 63. 300,000
 65. c
 67. c
 69. 880
 71. 4200
 73. 4480

 75. 375 cal
 77. \$3290
 79. a. 20 boxes
 b. 100 boxes
 c. 2000 lb
 81. 8800 sq ft
 83. 56,000 sq ft
 85. 5828 pixels

 87. 2100 characters
 89. 1360 cal
 91. \$10, \$60; \$10, \$200; \$12, \$36, \$12, \$36; total cost: \$372
 93. 1,440,000 tea bags
 95. 135

 97. 2144
 99. 23
 101. 15
 103. $4 \cdot 7$ or $7 \cdot 4$ 105. a. 5 + 5 + 5 or 3 + 3 + 3 + 3 + 3 b. answers may vary
 107. 203

 $\times 93$ 293
 203
 203
 203
 203
 203
 203
 203

Section 1.7

ers to Selected Exercis

Calculator Explorations 1. 53 3. 62 5. 261 7. 0

Vocabulary, Readiness & Video Check 1. quotient; dividend; divisor 3. 1 5. undefined 7. 0 9. $202 \cdot 102 + 15 = 20,619$ 11. addition and division

Exercise Set 1.7 1. 6 **3.** 12 **5.** 0 **7.** 31 **9.** 1 **11.** 8 **13.** undefined **15.** 1 **17.** 0 **19.** 9 **21.** 29 **23.** 74 **25.** 338 **27.** undefined **29.** 9 **31.** 25 **33.** 68 R 3 **35.** 236 R 5 **37.** 38 R 1 **39.** 326 R 4 **41.** 13 **43.** 49 **45.** 97 R 8 **47.** 209 R 11 **49.** 506 **51.** 202 R 7 **53.** 54 **55.** 99 R 100 **57.** 202 R 15 **59.** 579 R 72 **61.** 17 **63.** 511 R 3 **65.** 2132 R 32 **67.** 6080 **69.** 23 R 2 **71.** 5 R 25 **73.** 20 R 2 **75.** 33 students **77.** 165 lb **79.** 310 yd **81.** 89 bridges **83.** 11 light poles **85.** 5 mi **87.** 1760 yd **89.** 20 **91.** 387 **93.** 79 **95.** 74° **97.** 9278 **99.** 15,288 **101.** 679 **103.** undefined **105.** 9 R 12 **107.** c **109. b 111.** 77 **113.** increase; answers may vary **115.** no; answers may vary **117.** 12 ft **119.** answers may vary **121.** 5 R 1

Integrated Review 1. 148 2. 6555 3. 1620 4. 562 5. 79 6. undefined 7. 9 8. 1 9. 0 10. 0 11. 0 12. 3 13. 2433 14. 9826 15. 213 R 3 16. 79,317 17. 27 18. 9 19. 138 20. 276 21. 1099 R 2 22. 111 R 1 23. 663 R 6 24. 1076 R 60 25. 1024 26. 9899 27. 30,603 28. 47,500 29. 65 30. 456 31. 6 R 8 32. 53 33. 183 34. 231 35. 9740; 9700; 10,000 36. 1430; 1400; 1000 37. 20,800; 20,800; 21,000 38. 432,200; 432,200; 432,000 39. perimeter: 24 ft; area: 36 sq ft 40. perimeter: 42 in.; area: 98 sq in. 41. 28 mi 42. 26 m 43. 24 44. 124 45. Lake Pontchartrain Bridge; 2175 ft 46. 730 qt

Section 1.8

Vocabulary, Readiness & Video Check 1. The George Washington Bridge has a length of 3500 feet.

Exercise Set 1.8 1. 49 **3.** 237 **5.** 42 **7.** 600 **9. a.** 400 ft **b.** 9600 sq ft **11.** \$15,500 **13.** 168 hr **15.** 3500 ft **17.** 141 yr **19.** 372 billion bricks **21.** 719 towns **23.** \$26 **25.** 55 cal **27.** 21 hot dogs **29.** 3,219,600 visitors **31.** 694,000 people **33.** 3987 mi **35.** 13 paychecks **37.** \$239 **39.** \$1045 **41. b** will be cheaper by \$3 **43.** Asia **45.** 1846 million **47.** 66 million **49.** 951 million **51.** \$14,754 **53.** 16,800 mg **55. a.** 3750 sq ft **b.** 375 sq ft **c.** 3375 sq ft **57.** \$10 **59.** answers may vary

Section 1.9

Calculator Explorations 1. 4096 3. 3125 5. 2048 7. 2526 9. 4295 11. 8

Vocabulary, Readiness & Video Check 1. base; exponent 3. addition 5. division 7. exponent; base 9. Because $8 \cdot 8 = 64$. 11. The area of a rectangle is length \cdot width. A square is a special rectangle where length = width. Thus, the area of a square is side \cdot side \cdot side or (side)².

Exercise Set 1.9 1. 4^3 **3.** 7^6 **5.** 12^3 **7.** $6^2 \cdot 5^3$ **9.** $9 \cdot 8^2$ **11.** $3 \cdot 2^4$ **13.** $3 \cdot 2^4 \cdot 5^5$ **15.** 64 **17.** 125 **19.** 32 **21.** 1 **23.** 7 **25.** 128 **27.** 256 **29.** 256 **31.** 729 **33.** 144 **35.** 100 **37.** 20 **39.** 729 **41.** 192 **43.** 162 **45.** 3 **47.** 8 **49.** 12 **51.** 4 **53.** 21 **55.** 7 **57.** 5 **59.** 16 **61.** 46 **63.** 8 **65.** 64 **67.** 83 **69.** 2 **71.** 48 **73.** 4 **75.** undefined **77.** 59 **79.** 52 **81.** 44 **83.** 12 **85.** 21 **87.** 24 **89.** 28 **91.** 3 **93.** 25 **95.** 23 **97.** 13 **99.** area: $49 \, \text{sq}$ m; perimeter: $28 \, \text{m}$ **101.** area: $529 \, \text{sq}$ m; perimeter: $92 \, \text{mi}$ **103.** true **105.** false **107.** $(2 + 3) \cdot 6 - 2$ **109.** $24 \div (3 \cdot 2) + 2 \cdot 5$ **111.** $1260 \, \text{ft}$ **113.** 6,384,814 **115.** answers may vary; sample answer: $(20 - 10) \cdot 5 \div 25 + 3$

Chapter 1 Vocabulary Check 1. whole numbers 2. perimeter 3. place value 4. exponent 5. area 6. square root 7. digits 8. average 9. divisor 10. dividend 11. quotient 12. factor 13. product 14. minuend 15. subtrahend 16. difference 17. addend 18. sum

Chapter 1 Review 1. tens 2. ten-millions 3. seven thousand, six hundred forty 4. forty-six million, two hundred thousand, one hundred twenty 5. 3000 + 100 + 50 + 8 6. 400,000,000 + 3,000,000 + 200,000 + 20,000 + 5000 7. 81,900 8. 6,304,000,000 9. 636,831,820 10. 326,975,340 11. Asia 12. Oceania/Australia 13. 63 14. 67 15. 48 16. 77 17. 956 18. 840 19. 7950 20. 7250 21. 4211 22. 1967 23. 1326 24. 886 25. 27,346 26. 39,300 27. 8032 mi 28. \$197,699 29. 276 ft 30. 66 km

31. 14 **32.** 34 **33.** 65 **34.** 304 **35.** 3914 **36.** 7908 **37.** 17,897 **38.** 34,658 **39.** 141,934 **40.** 36,746 **41.** 397 pages **42.** \$25,626 **43.** May **44.** August **45.** \$110 **46.** \$240 **47.** 90 **48.** 50 **49.** 470 **50.** 500 **51.** 4800 **52.** 58,000 **53.** 50,000,000 **54.** 800,000 **55.** 264,000,000 **56.** 98,000 **57.** 7400 **58.** 4100 **59.** 2500 mi **60.** 800,000 **61.** 1911 **62.** 1396 **63.** 1410 **64.** 2898 **65.** 800 **66.** 900 **67.** 3696 **68.** 1694 **69.** 0 **70.** 0 **71.** 16,994 **72.** 8954 **73.** 113,634 **74.** 44,763 **75.** 411,426 **76.** 636,314 **77.** 375,000 **78.** 108,000 **79.** 12,000 **80.** 35,000 **81.** 5,100,000 **82.** 7,600,000 **83.** 1150 **84.** 4920 **85.** 108 **86.** 112 **87.** 24 g **88.** \$158,980 **89.** 60 sq mi **90.** 500 sq cm **91.** 3 **92.** 4 **93.** 6 **94.** 7 **95.** 5 R 2 **96.** 4 R 2 **97.** undefined **98.** 0 **99.** 1 **100.** 10 **101.** 0 **102.** undefined **103.** 33 R 2 **104.** 19 R 7 **105.** 24 R 2 **106.** 35 R 15 **107.** 506 R 10 **108.** 907 R 40 **109.** 2793 R 140 **110.** 2012 R 60 **111.** 18 R 2 **112.** 21 R 2 **113.** 458 ft **114.** 13 mi **115.** 51 **116.** 59 **117.** 27 boxes **118.** \$192 **119.** \$1,700,000,000 **120.** 75¢ **121.** \$898 **122.** 23,150 sq ft **123.** 49 **124.** 125 **125.** 45 **126.** 400 **127.** 13 **128.** 10 **129.** 15 **130.** 7 **131.** 12 **132.** 9 **133.** 42 **134.** 33 **135.** 9 **136.** 2 **137.** 1 **138.** 0 **139.** 6 **140.** 29 **141.** 40 **142.** 72 **143.** 5 **144.** 7 **145.** 49 sq m **146.** 9 sq in. **147.** 307 **148.** 682 **149.** 2169 **150.** 2516 **151.** 901 **152.** 1411 **153.** 458 R 8 **154.** 237 R 1 **155.** 70,848 **156.** 95,832 **157.** 1644 **158.** 8481 **159.** 740 **160.** 258,000 **161.** 2000 **162.** 40,000 **163.** thirty-six thousand, nine hundred eleven **164.** one hundred fifty-four thousand, eight hundred sixty-three **165.** 70,943 **166.** 43,401 **167.** 64 **168.** 125 **169.** 12 **170.** 10 **171.** 12 **172.** 1 **173.** 2 **174.** 6 **175.** 4 **176.** 24 **177.** 24 **178.** 14 **179.** \$190,000 **180.** \$1,289,000 **181.** 53 full boxes with 18 left over **182.** \$86

Chapter 1 Getting Ready for the Test 1. D 2. C 3. B 4. E 5. C 6. A 7. B, E 8. D 9. B 10. C 11. A 12. D 13. B 14. A 15. E 16. C 17. C 18. A 19. B 20. A

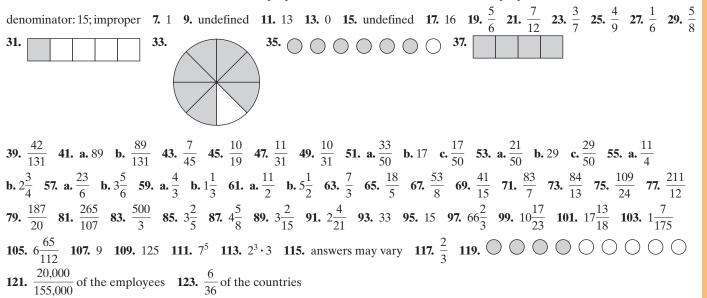
Chapter 1 Test 1. eighty-two thousand, four hundred twenty-six 2. 402,550 3. 141 4. 113 5. 14,880 6. 766 R 42 7. 200 8. 10 9. 0 10. undefined 11. 33 12. 21 13. 8 14. 36 15. 5,698,000 16. 11,200,000 17. 52,000 18. 13,700 19. 1600 20. 92 21. 122 22. 1605 23. 7 R 2 24. \$17 25. \$126 26. 360 cal 27. \$7905 28. 20 cm; 25 sq cm 29. 60 yd; 200 sq yd

Chapter 2 Multiplying and Dividing Fractions

Section 2.1

Vocabulary, Readiness & Video Check 1. fraction; denominator; numerator **3.** improper; proper; mixed number **5.** The fraction is equal to 1. **7.** Each shape is divided into 3 equal parts. **9.** division

Exercise Set 2.1 1. numerator: 1; denominator: 2; proper 3. numerator: 10; denominator: 3; improper 5. numerator: 15;



Section 2.2

Vocabulary, Readiness & Video Check 1. prime factorization **3.** prime **5.** factors **7.** Because order doesn't matter when we multiply, so switching the order doesn't give us any new factors of 12. **9.** order; one

Exercise Set 2.2 1. 1,2,4,8 **3.** 1,5,25 **5.** 1,2,4 **7.** 1,2,3,6,9,18 **9.** 1,29 **11.** 1,2,4,5,8,10,16,20,40,80 **13.** 1,2,3,4,6,12 **15.** 1,2,17,34 **17.** prime **19.** composite **21.** prime **23.** composite **25.** prime **27.** composite **29.** prime **31.** composite **33.** composite **35.** 2^5 **37.** $3 \cdot 5$ **39.** $2^3 \cdot 5$ **41.** $2^2 \cdot 3^2$ **43.** $3 \cdot 13$ **45.** $2^2 \cdot 3 \cdot 5$ **47.** $2 \cdot 5 \cdot 11$ **49.** $5 \cdot 17$ **51.** 2^7 **53.** $2 \cdot 7 \cdot 11$ **55.** $2^2 \cdot 3 \cdot 5^2$ **57.** $2^4 \cdot 3 \cdot 5$ **59.** $2^2 \cdot 3^2 \cdot 23$ **61.** $2 \cdot 3^2 \cdot 7^2$ **63.** $7^2 \cdot 13$ **65.** $3 \cdot 11$ **67.** $2 \cdot 7^2$ **69.** prime **71.** $3^3 \cdot 17$ **73.** prime **75.** $2^2 \cdot 5^2 \cdot 7$ **77.** 4300 **79.** 7,660,000 **81.** 20,000 **83.** 6043 **85.** $\frac{2003}{6043}$ **87.** $2^2 \cdot 3^5 \cdot 5 \cdot 7$ **89.** answers may vary **91.** answers may vary

Section 2.3

Calculator Explorations 1. $\frac{4}{7}$ 3. $\frac{20}{27}$ 5. $\frac{15}{8}$ 7. $\frac{9}{2}$

Vocabulary, Readiness & Video Check 1. simplest form 3. cross products 5. 0 7. equivalent 9. $\frac{10}{24}$ is not in simplest form; $\frac{5}{12}$ Exercise Set 2.3 1. $\frac{1}{4}$ 3. $\frac{2}{21}$ 5. $\frac{7}{8}$ 7. $\frac{2}{3}$ 9. $\frac{7}{10}$ 11. $\frac{7}{9}$ 13. $\frac{3}{5}$ 15. $\frac{27}{64}$ 17. $\frac{5}{8}$ 19. $\frac{5}{8}$ 21. $\frac{14}{17}$ 23. $\frac{3}{2}$ or $1\frac{1}{2}$ 25. $\frac{3}{4}$ 27. $\frac{5}{14}$ 29. $\frac{3}{14}$ 31. $\frac{11}{17}$ 33. $\frac{3}{14}$ 35. $\frac{7}{8}$ 37. $\frac{3}{5}$ 39. 14 41. equivalent 43. not equivalent 45. equivalent 47. equivalent 49. not equivalent 51. not equivalent 53. $\frac{1}{4}$ of a shift 55. $\frac{1}{2}$ mi 57. a. $\frac{5}{39}$ b. 68 monuments c. $\frac{34}{39}$ 59. $\frac{5}{12}$ of the wall 61. a. 17 states b. $\frac{17}{50}$ 63. $\frac{9}{32}$ of full-time employees 65. 364 67. 2322 69. 2520 71. answers may vary 73. $\frac{3}{5}$ 75. $\frac{9}{25}$ 77. $\frac{1}{25}$ 79. $\frac{1}{10}$ 81. answers may vary 83. $\frac{3}{50}$ 85. answers may vary 87. 786, 222, 900, 1470 89. 6; answers may vary Integrated Review 1. $\frac{3}{6}$ (or $\frac{1}{2}$ simplified) 2. $\frac{7}{4}$ or $1\frac{3}{4}$ 3. $\frac{73}{85}$ 4.

Integrated Review 1.
$$\frac{3}{6}$$
 (or $\frac{1}{2}$ simplified) 2. $\frac{7}{4}$ or $1\frac{3}{4}$ 3. $\frac{73}{85}$ 4.
5. 1 6. 17 7. 0 8. undefined 9. $\frac{25}{8}$ 10. $\frac{28}{5}$ 11. $\frac{69}{7}$ 12. $\frac{141}{7}$ 13. $2\frac{6}{7}$ 14. 5 15. $4\frac{7}{8}$ 16. $8\frac{10}{11}$ 17. 1, 5, 7, 35 18. 1, 2, 4, 5, 8, 10, 20, 40 19. composite 20. prime 21. 5 · 13 22. 2 · 5 · 7 23. $2^5 \cdot 3$ 24. $2^2 \cdot 3 \cdot 11$ 25. $2^2 \cdot 3^2 \cdot 7$ 26. prime 27. $3^2 \cdot 5 \cdot 7$ 28. $3^2 \cdot 7^2$ 29. $2 \cdot 11 \cdot 13$ 30. prime 31. $\frac{1}{7}$ 32. $\frac{6}{5}$ or $1\frac{1}{5}$ 33. $\frac{9}{19}$ 34. $\frac{21}{55}$ 35. $\frac{14}{15}$ 36. $\frac{9}{10}$ 37. $\frac{2}{5}$ 38. $\frac{3}{8}$ 39. $\frac{11}{14}$ 40. $\frac{7}{11}$ 41. not equivalent 43. a. $\frac{1}{25}$ b. 48 c. $\frac{24}{25}$ 44. a. $\frac{11}{21}$ b. 20 c. $\frac{10}{21}$

Section 2.4

Vocabulary, Readiness & Video Check 1. $\frac{a \cdot c}{b \cdot d}$ 3. multiplication 5. There's a common factor of 2 in the numerator and denominator that can be divided out first. 7. radius is $\frac{1}{2}$ of diameter

Exercise Set 2.4 1. $\frac{2}{15}$ 3. $\frac{6}{35}$ 5. $\frac{9}{80}$ 7. $\frac{5}{28}$ 9. $\frac{12}{5}$ or $2\frac{2}{5}$ 11. $\frac{1}{70}$ 13. 0 15. $\frac{1}{110}$ 17. $\frac{18}{55}$ 19. $\frac{27}{80}$ 21. $\frac{1}{56}$ 23. $\frac{2}{105}$ 25. 0 **27.** $\frac{1}{90}$ **29.** 8 **31.** 6 **33.** 20 **35.** 3 **37.** $\frac{5}{2}$ or $2\frac{1}{2}$ **39.** $\frac{1}{5}$ **41.** $\frac{5}{3}$ or $1\frac{2}{3}$ **43.** $\frac{2}{3}$ **45.** Exact: $\frac{77}{10}$ or $7\frac{7}{10}$; Estimate: 8 **47.** Exact: $\frac{836}{35}$ or $23\frac{31}{35}$; Estimate: 24 **49.** $\frac{25}{2}$ or $12\frac{1}{2}$ **51.** 15 **53.** 6 **55.** $\frac{45}{4}$ or $11\frac{1}{4}$ **57.** $\frac{49}{3}$ or $16\frac{1}{3}$ **59.** $\frac{1}{30}$ **61.** 0 **63.** $\frac{16}{5}$ or $3\frac{1}{5}$ **65.** $\frac{7}{2}$ or $3\frac{1}{2}$ 67. $\frac{1}{8}$ 69. $\frac{1}{56}$ 71. $\frac{55}{3}$ or $18\frac{1}{3}$ 73. 0 75. $\frac{208}{7}$ or $29\frac{5}{7}$ 77. 50 79. 20 81. 128 freshmen 83. 120 million 85. 868 mi **87.** $\frac{3}{16}$ in. **89.** 30 gal **91.** $\frac{17}{2}$ in. or $8\frac{1}{2}$ in. **93.** $\frac{39}{2}$ in. or $19\frac{1}{2}$ in. **95.** $\frac{2242}{625}$ sq in. or $3\frac{367}{625}$ sq in. **97.** $\frac{1}{14}$ sq ft **99.** $\frac{7}{2}$ sq yd or $3\frac{1}{2}$ sq yd **101.** 3840 mi **103.** 2400 mi **105.** 206 **107.** 56 R 12 **109.** answers may vary **111.** $3\frac{2}{3} \cdot 1\frac{1}{7} = \frac{11}{3} \cdot \frac{8}{7} = \frac{11 \cdot 8}{3 \cdot 7} = \frac{88}{21}$ or $4\frac{4}{21}$ 113. b 115. a 117. 37 students 119. 684,750 Māori

Section 2.5

Vocabulary, Readiness & Video Check 1. reciprocals 3. $\frac{a \cdot d}{b \cdot c}$ 5. $\frac{1}{n}$ 7. Because we still have a division problem and we can't divide out common factors until we rewrite the division as a multiplication.

Exercise Set 2.5 1. $\frac{7}{4}$ 3. 11 5. $\frac{1}{15}$ 7. $\frac{7}{12}$ 9. $\frac{4}{5}$ 11. $\frac{16}{9}$ or $1\frac{7}{9}$ 13. $\frac{18}{35}$ 15. $\frac{3}{4}$ 17. $\frac{1}{100}$ 19. $\frac{1}{3}$ 21. $\frac{5}{3}$ or $1\frac{2}{3}$ 23. $\frac{35}{36}$ 25. $\frac{14}{37}$ **27.** $\frac{8}{45}$ **29.** 1 **31.** undefined **33.** 0 **35.** $\frac{7}{10}$ **37.** $\frac{1}{6}$ **39.** $\frac{40}{3}$ or $13\frac{1}{3}$ **41.** 5 **43.** $\frac{5}{28}$ **45.** $\frac{36}{35}$ or $1\frac{1}{35}$ **47.** $\frac{26}{51}$ **49.** 0

51. $\frac{17}{13}$ or $1\frac{4}{13}$ **53.** $\frac{35}{18}$ or $1\frac{17}{18}$ **55.** $\frac{19}{30}$ **57.** $\frac{1}{6}$ **59.** $\frac{121}{60}$ or $2\frac{1}{60}$ **61.** 96 **63.** $\frac{3}{4}$ **65.** undefined **67.** $\frac{11}{119}$ **69.** $\frac{35}{11}$ or $3\frac{2}{11}$ **71.** $\frac{9}{5}$ or $1\frac{4}{5}$ **73.** $3\frac{3}{16}$ miles **75.** $\frac{5}{6}$ Tbsp **77.** $\frac{19}{30}$ in. **79.** 20 lb **81.** $4\frac{2}{3}$ m **83.** $\frac{8}{35}$ **85.** $\frac{128}{51}$ or $2\frac{26}{51}$ **87.** $\frac{16}{15}$ or $1\frac{1}{15}$ **89.** $\frac{121}{400}$ **91.** 201 **93.** 196 **95.** 1569 **97.** $20\frac{2}{3} \div 10\frac{1}{2} = \frac{62}{3} \div \frac{21}{2} = \frac{62}{3} \cdot \frac{2}{21} = \frac{124}{63}$ or $1\frac{61}{63}$ **99. c 101. d 103.** 5 **105.** 650 aircraft **107.** answers may vary

Chapter 2 Vocabulary Check 1. reciprocals 2. composite number 3. equivalent 4. improper fraction 5. prime number 6. simplest form 7. proper fraction 8. mixed number 9. numerator; denominator 10. prime factorization 11. undefined 12. 0 13. cross products

Chapter 2 Review 1. proper 2. improper 3. proper 4. mixed number 5. $\frac{2}{6}$ 6. $\frac{4}{7}$ 7. $\frac{7}{3}$ 8. $\frac{13}{4}$ 9. $\frac{11}{12}$ 10. a. 108 b. $\frac{108}{131}$ 11. $3\frac{3}{4}$ 12. $45\frac{5}{6}$ 13. 3 14. 5 15. $\frac{6}{5}$ 16. $\frac{22}{21}$ 17. $\frac{26}{9}$ 18. $\frac{47}{12}$ 19. composite 20. prime 21. 1, 2, 3, 6, 7, 14, 21, 42 22. 1, 2, 4, 5, 10, 20 23. $2^{2} \cdot 17$ 24. $2 \cdot 3^{2} \cdot 5$ 25. $5 \cdot 157$ 26. $3 \cdot 5 \cdot 17$ 27. $\frac{3}{7}$ 28. $\frac{5}{9}$ 29. $\frac{1}{3}$ 30. $\frac{1}{2}$ 31. $\frac{29}{32}$ 32. $\frac{18}{23}$ 33. 8 34. 6 35. $\frac{2}{3}$ of a foot 36. $\frac{3}{5}$ of the cars 37. no 38. yes 39. $\frac{3}{10}$ 40. $\frac{5}{14}$ 41. 9 42. $\frac{1}{2}$ 43. $\frac{35}{8}$ or $4\frac{3}{8}$ 44. $\frac{5}{2}$ or $2\frac{1}{2}$ 45. $\frac{5}{3}$ or $1\frac{2}{3}$ 46. $\frac{49}{3}$ or $16\frac{1}{3}$ 47. Exact: $\frac{26}{5}$ or $5\frac{1}{5}$; Estimate: 6 48. Exact: $\frac{60}{11}$ or $5\frac{5}{11}$; Estimate: 8 49. $\frac{99}{4}$ or $24\frac{3}{4}$ 50. $\frac{1}{6}$ 51. $\frac{110}{3}$ g or $36\frac{2}{3}$ g 52. $\frac{135}{4}$ in or $33\frac{3}{4}$ in. 53. $\frac{119}{80}$ sq in or $1\frac{39}{80}$ sq in. 54. $\frac{275}{8}$ sq m or $34\frac{3}{8}$ sq m 55. $\frac{1}{7}$ 56. 8 57. $\frac{23}{14}$ 58. $\frac{5}{17}$ 59. 2 60. $\frac{15}{4}$ or $3\frac{3}{4}$ 61. $\frac{5}{6}$ 62. $\frac{8}{3}$ or $2\frac{2}{3}$ 63. $\frac{21}{4}$ or $5\frac{1}{4}$ 64. $\frac{121}{46}$ or $2\frac{29}{46}$ 65. 22 mi 66. $\frac{21}{20}$ mi or $1\frac{1}{20}$ mi 67. proper 68. improper 69. mixed number 70. improper 71. $31\frac{1}{4}$ 72. 6 73. $\frac{95}{17}$ 74. $\frac{47}{6}$ 75. composite 76. prime 77. $2^{2} \cdot 3^{2} \cdot 5$ 78. $2 \cdot 7^{2}$ 79. $\frac{9}{10}$ 80. $\frac{5}{7}$ 81. $\frac{14}{15}$ 82. $\frac{3}{5}$ 83. $\frac{7}{12}$ 84. $\frac{1}{4}$ 85. 9 86. $\frac{27}{2}$ or $13\frac{1}{2}$ 87. Exact: 10; Estimate: 8 88. Exact: $\frac{51}{4}$ or $12\frac{3}{4}$; Estimate: 12 89. $\frac{7}{3}$ or $2\frac{1}{3}$ 90. $\frac{32}{5}$ or $6\frac{2}{5}$ 91. $\frac{81}{2}$ sq ft or $40\frac{1}{2}$ sq ft 92. $\frac{47}{61}$ in.

Chapter 2 Getting Ready for the Test 1. B 2. C 3. A 4. D 5. C 6. A 7. B 8. A 9. B 10. B 11. A Chapter 2 Test 1. $\frac{7}{16}$ 2. $\frac{13}{5}$ 3. $\frac{23}{3}$ 4. $\frac{39}{11}$ 5. $4\frac{3}{5}$ 6. $18\frac{3}{4}$ 7. $\frac{4}{35}$ 8. $\frac{3}{5}$ 9. not equivalent 10. equivalent 11. $2^2 \cdot 3 \cdot 7$ 12. $3^2 \cdot 5 \cdot 11$ 13. $\frac{4}{3}$ or $1\frac{1}{3}$ 14. $\frac{4}{3}$ or $1\frac{1}{3}$ 15. $\frac{1}{4}$ 16. $\frac{16}{45}$ 17. 16 18. $\frac{9}{2}$ or $4\frac{1}{2}$ 19. $\frac{4}{11}$ 20. 9 21. $\frac{64}{3}$ or $21\frac{1}{3}$ 22. $\frac{45}{2}$ or $22\frac{1}{2}$ 23. $\frac{18}{5}$ or $3\frac{3}{5}$ 24. $\frac{20}{3}$ or $6\frac{2}{3}$ 25. $\frac{34}{27}$ sq mi or $1\frac{7}{27}$ sq mi 26. 24 mi 27. $\frac{16,000}{3}$ sq yd or $5333\frac{1}{3}$ sq yd 28. \$90 per share

Cumulative Review 1. hundred-thousands; Sec. 1.2, Ex. 1 **2.** two thousand, thirty-six; Sec. 1.2 **3.** 805; Sec. 1.2, Ex. 9 **4.** 31; Sec. 1.3 **5.** 184,046; Sec. 1.3, Ex. 2 **6.** 39; Sec. 1.7 **7.** 13 in.; Sec. 1.3, Ex. 5 **8.** 17; Sec. 1.4 **9.** 10,591,862; Sec. 1.3, Ex. 7 **10.** 5; Sec. 1.9 **11.** 7321; Sec. 1.4, Ex. 2 **12.** 64; Sec. 1.9 **13. a.** Indonesia **b.** 333; Sec. 1.3, Ex. 8 **14.** 25 R 5; Sec. 1.7 **15.** 570; Sec. 1.5, Ex. 1 **16.** 2400; Sec. 1.5 **17.** 1800; Sec. 1.5, Ex. 5 **18.** 300; Sec. 1.5 **19. a.** 6 **b.** 0 **c.** 45 **d.** 0; Sec. 1.6, Ex. 1 **20.** 20; Sec. 1.9 **21. a.** $3 \cdot 4 + 3 \cdot 5$ **b.** 10 $\cdot 6 + 10 \cdot 8$ **c.** $2 \cdot 7 + 2 \cdot 3$; Sec. 1.6, Ex. 2 **22.** 180; Sec. 1.6 **23. a.** 0 **b.** 0 **c.** 0 **d.** undefined; Sec. 1.7, Ex. 3 **24.** 154 sq mi; Sec. 1.6 **25.** 208; Sec. 1.7, Ex. 5 **26.** 4014; Sec. 1.4 **27.** 12 cards; 10 cards left over; Sec. 1.7, Ex. 11 **28.** 63; Sec. 1.6 **29.** 40 ft; Sec. 1.8, Ex. 5 **30.** 16; Sec. 1.3 **31.** 7³; Sec. 1.9, Ex. 1 **32.** 7⁴; Sec. 1.9 **33.** 3⁴ $\cdot 17^3$; Sec. 1.9, Ex. 4 **34.** 2² $\cdot 3 \cdot 13$; Sec. 2.2 **39. a.** $\frac{38}{9}$ **b.** $\frac{19}{11}$; Sec. 2.1, Ex. 17 **40.** $\frac{39}{5}$; Sec. 2.1 **41.** 1, 2, 4, 5, 10, 20; Sec. 2.2, Ex. 1 **42.** equivalent; Sec. 2.3 **43.** $\frac{7}{11}$; Sec. 2.3, Ex. 2 **44.** $\frac{2}{3}$; Sec. 2.3 **45.** $\frac{35}{12}$ or $2\frac{11}{12}$; Sec. 2.4, Ex. 8 **46.** $\frac{8}{3}$ or $2\frac{2}{3}$; Sec. 2.4 **47.** $\frac{3}{1}$ or 3; Sec. 2.5, Ex. 3 **48.** $\frac{1}{9}$; Sec. 2.5, Ex. 6 **50.** $\frac{11}{56}$; Sec. 2.5

Chapter 3 Adding and Subtracting Fractions

Section 3.1

Vocabulary, Readiness & Video Check 1. like; unlike 3. $\frac{a-c}{b}$ 5. unlike 7. like 9. like 11. unlike 13. We can simplify by dividing out a common factor of 3 from the numerator and denominator to get $\frac{2}{3}$. 15. $P = \frac{4}{20} + \frac{9}{20} + \frac{7}{20}$; 1 in.

Exercise Set 3.1 1. $\frac{3}{7}$ 3. $\frac{1}{5}$ 5. $\frac{2}{3}$ 7. $\frac{7}{20}$ 9. $\frac{1}{2}$ 11. $\frac{13}{11}$ or $1\frac{2}{11}$ 13. $\frac{7}{13}$ 15. $\frac{2}{3}$ 17. $\frac{6}{11}$ 19. $\frac{3}{5}$ 21. 1 23. $\frac{3}{4}$ 25. $\frac{5}{6}$ 27. $\frac{4}{5}$ 29. $\frac{1}{90}$ 31. $\frac{19}{33}$ 33. $\frac{13}{21}$ 35. $\frac{9}{10}$ 37. 0 39. $\frac{3}{4}$ 41. 1 in. 43. 2 m 45. $\frac{7}{10}$ mi 47. $\frac{3}{2}$ hr or $1\frac{1}{2}$ hr 49. $\frac{43}{100}$ 51. $\frac{1}{10}$ 53. $\frac{2}{5}$ 55. $\frac{13}{50}$ 57. $\frac{7}{25}$ 59. $\frac{1}{50}$ 61. $\frac{2}{5}$ 63. 2.5 65. 2³ 67. 5.11 69. $\frac{5}{8}$ 71. $\frac{8}{11}$ 73. $\frac{2}{7} + \frac{9}{7} = \frac{11}{7}$ or $1\frac{4}{7}$ 75. answers may vary 77. 1; answers may vary 79. $\frac{1}{4}$ mi

Section 3.2

A6

Vocabulary, Readiness & Video Check 1. equivalent 3. multiple 5. Because 24 is a multiple of 8.

Exercise Set 3.2 1. 12 3. 45 5. 36 7. 72 9. 126 11. 75 13. 24 15. 42 17. 216 19. 150 21. 68 23. 588 25. 900 27. 1800 29. 363 31. 60 33. $\frac{20}{35}$ 35. $\frac{14}{21}$ 37. $\frac{15}{3}$ 39. $\frac{15}{30}$ 41. $\frac{30}{21}$ 43. $\frac{21}{28}$ 45. $\frac{30}{45}$ 47. $\frac{36}{81}$ 49. $\frac{90}{78}$ 51. $\frac{56}{68}$ 53. $\frac{86}{100}$; $\frac{58}{100}$; $\frac{68}{100}$; $\frac{12}{100}$; $\frac{84}{100}$; $\frac{68}{100}$; $\frac{90}{100}$; $\frac{79}{100}$; $\frac{74}{100}$; $\frac{78}{100}$ 55. drugs, health and beauty aids 57. $\frac{1}{2}$ 59. $\frac{2}{5}$ 61. $\frac{4}{9}$ 63. 1 65. $\frac{814}{3630}$ 67. answers may vary 69. a, b, and d

Section 3.3

Calculator Explorations 1. $\frac{37}{80}$ 3. $\frac{95}{72}$ 5. $\frac{394}{323}$

Vocabulary, Readiness & Video Check 1. equivalent; least common denominator 3. $\frac{15}{24}$; $\frac{4}{24}$; $\frac{19}{24}$ 5. Multiplying by $\frac{3}{3}$ is multiplying by a form of 1. Thus, the result is an equivalent fraction. 7. $\frac{34}{15}$ cm and $2\frac{4}{15}$ cm

Exercise Set 3.3 1. $\frac{5}{6}$ 3. $\frac{5}{6}$ 5. $\frac{8}{33}$ 7. $\frac{9}{14}$ 9. $\frac{3}{5}$ 11. $\frac{5}{12}$ 13. $\frac{53}{60}$ 15. $\frac{13}{42}$ 17. $\frac{67}{99}$ 19. $\frac{98}{143}$ 21. $\frac{13}{27}$ 23. $\frac{75}{56}$ or $1\frac{19}{56}$ 25. $\frac{19}{18}$ or $1\frac{1}{18}$ 27. $\frac{19}{12}$ or $1\frac{7}{12}$ 29. $\frac{11}{16}$ 31. $\frac{17}{42}$ 33. $\frac{33}{56}$ 35. $\frac{37}{99}$ 37. $\frac{1}{35}$ 39. $\frac{11}{36}$ 41. $\frac{1}{20}$ 43. $\frac{1}{84}$ 45. $\frac{9}{1000}$ 47. $\frac{17}{99}$ 49. $\frac{19}{36}$ 51. $\frac{1}{5}$ 53. $\frac{69}{280}$ 55. $\frac{14}{9}$ or $1\frac{5}{9}$ 57. $\frac{34}{15}$ cm or $2\frac{4}{15}$ cm 59. $\frac{17}{10}$ m or $1\frac{7}{10}$ m 61. $\frac{7}{100}$ mph 63. $\frac{5}{8}$ in. 65. $\frac{31}{32}$ in. 67. $\frac{19}{100}$ of Girl Scout cookies 69. $\frac{19}{25}$ 71. $\frac{17}{50}$ 73. $\frac{81}{100}$ 75. 5 77. $\frac{16}{29}$ 79. $\frac{19}{3}$ or $6\frac{1}{3}$ 81. $\frac{3}{5} + \frac{4}{5} = \frac{7}{5}$ or $1\frac{2}{5}$ 83. $\frac{223}{540}$ 85. $\frac{49}{44}$ or $1\frac{5}{44}$ 87. answers may vary

Integrated Review 1. 30 2. 21 3. 14 4. 25 5. 100 6. 90 7. $\frac{9}{24}$ 8. $\frac{28}{36}$ 9. $\frac{10}{40}$ 10. $\frac{12}{30}$ 11. $\frac{55}{75}$ 12. $\frac{40}{48}$ 13. $\frac{1}{2}$ 14. $\frac{2}{5}$ 15. $\frac{7}{12}$ 16. $\frac{13}{15}$ 17. $\frac{3}{4}$ 18. $\frac{2}{15}$ 19. $\frac{17}{45}$ 20. $\frac{19}{50}$ 21. $\frac{37}{40}$ 22. $\frac{11}{36}$ 23. 0 24. $\frac{1}{17}$ 25. $\frac{5}{33}$ 26. $\frac{1}{42}$ 27. $\frac{5}{18}$ 28. $\frac{1}{2}$ 29. $\frac{11}{18}$ 30. $\frac{37}{50}$ 31. $\frac{47}{30}$ or $1\frac{17}{30}$ 32. $\frac{7}{30}$ 33. $\frac{3}{5}$ 34. $\frac{27}{20}$ or $1\frac{7}{20}$ 35. $\frac{279}{350}$ 36. $\frac{309}{350}$ 37. $\frac{98}{5}$ or $19\frac{3}{5}$ 38. $\frac{9}{250}$ 39. $\frac{31}{3}$ or $10\frac{1}{3}$ 40. $\frac{93}{64}$ or $1\frac{29}{64}$ 41. $\frac{49}{54}$ 42. $\frac{83}{48}$ or $1\frac{35}{48}$ 43. $\frac{390}{101}$ or $3\frac{87}{101}$ 44. $\frac{116}{5}$ or $23\frac{1}{5}$ 45. $\frac{106}{135}$ 46. $\frac{67}{224}$

Section 3.4

Vocabulary, Readiness & Video Check 1. mixed number 3. round 5. a 7. c 9. The fractional part of a mixed number should not be an improper fraction. 11. Because we need to borrow first.

Exercise Set 3.4 1. Exact: $6\frac{4}{5}$; Estimate: 7 3. Exact: $13\frac{11}{14}$; Estimate: 14 5. $17\frac{7}{25}$ 7. $7\frac{5}{8}$ 9. $7\frac{5}{24}$ 11. $20\frac{1}{15}$ 13. 19 15. $56\frac{53}{270}$ 17. $13\frac{13}{24}$ 19. $47\frac{53}{84}$ 21. Exact: $2\frac{3}{5}$; Estimate: 3 23. Exact: $7\frac{5}{14}$; Estimate: 7 25. $\frac{24}{25}$ 27. $2\frac{7}{15}$ 29. $5\frac{11}{14}$ 31. $23\frac{31}{72}$ 33. $1\frac{4}{5}$

35.
$$1\frac{13}{15}$$
 37. $3\frac{5}{9}$ **39.** $15\frac{3}{4}$ **41.** $28\frac{7}{12}$ **43.** $15\frac{7}{8}$ **45.** 8 **47.** $17\frac{11}{12}$ **49.** $\frac{1}{16}$ in. **51.** no; she will be $\frac{1}{12}$ of a foot short **53.** $7\frac{13}{20}$ in. **55.** $10\frac{1}{4}$ hr **57.** $2\frac{3}{8}$ hr **59.** $5\frac{15}{16}$ lb **61.** $319\frac{1}{3}$ yd **63.** $9\frac{3}{4}$ min **65.** $1\frac{4}{5}$ min **67.** 7 mi **69.** $21\frac{5}{24}$ m **71.** 8 **73.** 25 **75.** 4 **77.** 167 **79.** 4 **81.** $9\frac{5}{8}$ **83.** a, b, c **85.** answers may vary **87.** Supreme is heavier by $\frac{1}{8}$ lb

Section 3.5

Vocabulary, Readiness & Video Check 1. multiplication **3.** subtraction **5.** denominators; numerators **7.** We need to make sure we have the same denominator when adding and subtracting fractions; this is not necessary when multiplying and dividing fractions.

Exercise Set 3.5 1. > 3. < 5. < 7. > 9. > 11. < 13. > 15. < 17. $\frac{1}{16}$ 19. $\frac{8}{125}$ 21. $\frac{64}{343}$ 23. $\frac{4}{81}$ 25. $\frac{1}{6}$ 27. $\frac{18}{125}$ 29. $\frac{11}{15}$ 31. $\frac{3}{35}$ 33. $\frac{5}{9}$ 35. $10\frac{4}{99}$ 37. $\frac{1}{12}$ 39. $\frac{9}{11}$ 41. 0 43. 0 45. $\frac{2}{5}$ 47. $\frac{2}{77}$ 49. $\frac{17}{60}$ 51. $\frac{5}{8}$ 53. $\frac{1}{2}$ 55. $\frac{29}{10}$ or $2\frac{9}{10}$ 57. $\frac{27}{32}$ 59. $\frac{1}{81}$ 61. $\frac{5}{6}$ 63. $\frac{3}{5}$ 65. $\frac{1}{2}$ 67. $\frac{19}{7}$ or $2\frac{5}{7}$ 69. $\frac{9}{64}$ 71. $\frac{3}{4}$ 73. $\frac{13}{60}$ 75. $\frac{13}{25}$ 77. A 79. M 81. S 83. D 85. M 87. A 89. no; answers may vary 91. subtraction, multiplication, addition, division 93. division, multiplication, subtraction, addition, division 95. first-class mail 97. discretionary purchases

Section 3.6

Vocabulary, Readiness & Video Check 1. To make sure we answer the question asked in the original problem.

Exercise Set 3.6 1. $\frac{1}{2} + \frac{1}{3}$ 3. $20 \div 6\frac{2}{5}$ 5. $\frac{15}{16} - \frac{5}{8}$ 7. $\frac{21}{68} + \frac{7}{34}$ 9. $8\frac{1}{3} \cdot \frac{7}{9}$ 11. $3\frac{1}{3}c$ 13. $12\frac{1}{2}in$ 15. $21\frac{1}{2}mi$ per gal 17. $1\frac{1}{2}$ yr 19. $9\frac{2}{5}in$ 21. no; $\frac{1}{4}$ yd 23. 5 pieces 25. $\frac{9}{8}$ or $1\frac{1}{8}in$ 27. $3\frac{3}{4}c$ 29. $11\frac{1}{4}$ sq in. 31. $3\frac{1}{3}min$ 33. $1\frac{1}{20}cu$ in. 35. 67 sheets 37. a. yes b. 1 ft left over 39. $2\frac{15}{16}$ lb 41. area: $\frac{9}{128}$ sq in.; perimeter: $1\frac{1}{8}in$. 43. area: $\frac{25}{81}$ sq m; perimeter: $2\frac{2}{9}m$ 45. $4\frac{3}{4}$ ft 47. $\frac{5}{26}$ ft 49. 3 51. 81 53. 4 55. 30 57. 35 59. no; no; answers may vary 61. $36\frac{44}{81}$ sq ft 63. 68 customers 65. 22 hr

Chapter 3 Vocabulary Check 1. like 2. least common multiple 3. Equivalent 4. mixed number 5. > 6. <
7. least common denominator 8. unlike 9. exponent

Chapter 3 Review 1. $\frac{10}{11}$ 2. $\frac{3}{25}$ 3. $\frac{2}{3}$ 4. $\frac{1}{7}$ 5. $\frac{3}{5}$ 6. $\frac{3}{5}$ 7. 1 8. 1 9. $\frac{19}{25}$ 10. $\frac{16}{21}$ 11. $\frac{3}{4}$ of his homework 12. $\frac{3}{2}$ mi or $1\frac{1}{2}$ mi 13. 55 14. 60 15. 120 16. 80 17. 252 18. 72 19. $\frac{56}{64}$ 20. $\frac{20}{30}$ 21. $\frac{21}{33}$ 22. $\frac{20}{26}$ 23. $\frac{16}{60}$ 24. $\frac{25}{60}$ 25. $\frac{11}{18}$ 26. $\frac{7}{15}$ 27. $\frac{7}{26}$ 28. $\frac{17}{36}$ 29. $\frac{41}{42}$ 30. $\frac{43}{72}$ 31. $\frac{13}{45}$ 32. $\frac{39}{70}$ 33. $\frac{19}{9}$ m or $2\frac{1}{9}$ m 34. $\frac{3}{2}$ ft or $1\frac{1}{2}$ ft 35. $\frac{1}{4}$ of a yd 36. $\frac{7}{10}$ has been cleaned 37. $45\frac{16}{21}$ 38. 60 39. $32\frac{13}{22}$ 40. $3\frac{19}{60}$ 41. $111\frac{5}{18}$ 42. $20\frac{7}{24}$ 43. $5\frac{16}{35}$ 44. $3\frac{4}{55}$ 45. $7\frac{4}{5}$ in. 46. $\frac{1}{40}$ oz 47. 5 ft 48. $11\frac{1}{6}$ ft 49. < 50. > 51. < 52. > 53. > 54. > 55. \frac{9}{49} 56. $\frac{64}{125}$ 57. $\frac{9}{400}$ 58. $\frac{9}{100}$ 59. $\frac{8}{13}$ 60. 2 61. $\frac{81}{196}$ 62. $\frac{1}{27}$ 63. $\frac{13}{18}$ 64. $\frac{11}{15}$ 65. $\frac{1}{7}$ 66. $\frac{18}{5}$ or $3\frac{3}{5}$ 67. $\frac{45}{28}$ or $1\frac{17}{28}$ 68. $\frac{5}{6}$ 69. $\frac{99}{56}$ or $1\frac{43}{56}$ 70. $\frac{29}{110}$ 71. $\frac{29}{54}$ 72. $\frac{37}{60}$ 73. 50 moons 74. $15\frac{5}{8}$ acres 75. each measurement is $4\frac{1}{4}$ in. 76. $\frac{7}{10}$ yd 77. perimeter: $\frac{17}{11}$ mi or $1\frac{6}{11}$ mi; area: $\frac{3}{22}$ sq mi 78. perimeter: $\frac{7}{3}$ m or $2\frac{1}{3}$ m; area: $\frac{5}{16}$ sq m 79. 90 80. 60 81. $\frac{40}{48}$ 82. $\frac{63}{72}$ 83. $\frac{1}{6}$ 84. $\frac{1}{5}$ 85. $\frac{11}{12}$ 86. $\frac{27}{55}$ 87. $13\frac{5}{12}$ 88. $12\frac{3}{8}$ 89. $3\frac{16}{35}$ 90. $8\frac{1}{21}$ 91. $\frac{11}{15}$ 92. $\frac{1}{8}$ 93. $\frac{1}{144}$ 94. $\frac{64}{27}$ or $2\frac{10}{127}$ 95. $\frac{5}{17}$ 96. $\frac{1}{12}$ 97. < 98. > 99. $\frac{1}{2}$ hr 100. $6\frac{7}{20}$ lb 101. $44\frac{1}{2}$ yd 102. $2\frac{2}{15}$ ft 103. $7\frac{1}{2}$ tablespoons 104. $\frac{3}{8}$ gal

Chapter 3 Getting Ready for the Test 1. A, C 2. C, D 3. B 4. C 5. D 6. C 7. B 8. C 9. D 10. A, B 11. C 12. B

Chapter 3 Test 1. 60 2. 72 3. < 4. < 5.
$$\frac{8}{9}$$
 6. $\frac{2}{5}$ 7. $\frac{13}{10}$ or $1\frac{3}{10}$ 8. $\frac{8}{21}$ 9. $\frac{13}{24}$ 10. $\frac{2}{3}$ 11. $\frac{67}{60}$ or $1\frac{7}{60}$ 12. $\frac{7}{50}$
13. $\frac{3}{2}$ or $1\frac{1}{2}$ 14. $14\frac{1}{40}$ 15. $30\frac{13}{45}$ 16. $1\frac{7}{24}$ 17. $16\frac{8}{11}$ 18. $\frac{5}{3}$ or $1\frac{2}{3}$ 19. $\frac{16}{81}$ 20. $\frac{9}{16}$ 21. $\frac{153}{200}$ 22. $\frac{3}{8}$ 23. $\frac{11}{12}$ 24. $3\frac{3}{4}$ ft
25. $7\frac{5}{6}$ gal 26. $\frac{23}{50}$ 27. $\frac{13}{50}$ 28. \$2820 29. perimeter: $\frac{10}{3}$ ft or $3\frac{1}{3}$ ft; area: $\frac{2}{3}$ sq ft 30. $\frac{5}{3}$ in. or $1\frac{2}{3}$ in.

13. $\frac{3}{2}$ or $1\frac{1}{2}$ **14.** $14\frac{4}{40}$ **15.** $30\frac{13}{45}$ **16.** $1\frac{7}{24}$ **17.** $16\frac{3}{11}$ **18.** $\frac{3}{3}$ or $1\frac{5}{4}$ **19.** $\frac{10}{81}$ **20.** $\frac{7}{16}$ **21.** $\frac{135}{200}$ **22.** $\frac{3}{8}$ **23.** $\frac{11}{12}$ **24.** $3\frac{3}{4}$ ft **25.** $7\frac{5}{6}$ gal **26.** $\frac{23}{50}$ **27.** $\frac{13}{50}$ **28.** \$2820 **29.** perimeter: $\frac{10}{3}$ ft or $3\frac{1}{3}$ ft; area: $\frac{2}{3}$ sq ft **30.** $\frac{5}{3}$ in or $1\frac{2}{3}$ in. **Cumulative Review 1.** eighty-five; Sec. 1.2, Ex. 4 **2.** one hundred seven; Sec. 1.2 **3.** one hundred twenty-six; Sec. 1.2, Ex. 5 **4.** five thousand, twenty-six; Sec. 1.2 **5.** 159; Sec. 1.3, Ex. 1 **6.** 19 in.; Sec. 1.2 **3.** one hundred twenty-six; Sec. 1.2, Ex. 5 **4.** five thousand, twenty-six; Sec. 1.2 **5.** 159; Sec. 1.3, Ex. 1 **6.** 19 in.; Sec. 1.3 **7.** 514; Sec. 1.4, Ex. 3 **8.** 121 R1; Sec. 1.7 **9.** 278,000; Sec. 1.5, Ex. 2 **10.** 1, 2, 3, 5, 6, 10, 15, 30; Sec. 2.2 **11.** 20,296; Sec. 1.6, Ex. 4 **12.** 0; Sec. 1.6 **13. a.** 7 **b.** 12 **c.** 1 **d.** 1 **e.** 20 **f.** 1; Sec. 1.7, Ex. 2 **14.** 25; Sec. 1.7 **15.** 1038 mi; Sec. 1.8, Ex. 1 **16.** 11; Sec. 1.9 **17.** 81; Sec. 1.9, Ex. 5 **18.** 125; Sec. 19 **19.** 81; Sec. 1.9, Ex. 7 **20.** 1000; Sec. 1.9 **21.** $\frac{4}{3}$ or $1\frac{1}{3}$; Sec. 2.1, Ex. 15 **22.** $\frac{11}{4}$ or $2\frac{3}{4}$; Sec. 2.1 **23.** $\frac{5}{2}$ or $2\frac{1}{2}$; Sec. 2.1, Ex. 16 **24.** $\frac{14}{3}$ or $4\frac{2}{3}$; Sec. 2.1 **25.** 3, 11, 17 are prime; 9, 26 are composite; Sec. 2.2, Ex. 2 **26.** 5; Sec. 1.9 **27.** $2^2 \cdot 3^2 \cdot 5$; Sec. 2.2, Ex. 4 **28.** 62; Sec. 1.4 **29.** $\frac{36}{13}$ or $2\frac{10}{13}$; Sec. 2.3, Ex. 5 **30.** $\frac{79}{8}$; Sec. 2.1 **31.** equivalent; Sec. 2.3, Ex. 8 **32.** >; Sec. 3.5 **33.** $\frac{10}{33}$; Sec. 2.4, Ex. 1 **34.** $\frac{3}{2}$ or $1\frac{1}{2}$; Sec. 2.4 **35.** $\frac{1}{8}$; Sec. 3.1, Ex. 2 **42.** $\frac{1}{5}$; Sec. 3.1 **43.** 24; Sec. 3.2, Ex. 1 **44.** 35; Sec. 3.2 **45.** 2; Sec. 3.3, Ex. 4 **46.** $\frac{25}{81}$; Sec. 3.5 **47.** $4\frac{1}{3}$; Sec. 3.4, Ex. 4 **48.** $\frac{11}{100}$; Sec. 3.4 **49.** $\frac{6}{13}$; Sec. 3.5, Ex. 11 **50.** $\frac{8}{175}$; Sec. 3.5

Chapter 4 Decimals

Section 4.1

Vocabulary, Readiness & Video Check 1. words; standard form 3. and 5. tens 7. tenths 9. as "and" 11. Reading a decimal correctly gives us the correct place value, which tells us the denominator of our equivalent fraction.

Exercise Set 4.1 1. six and fifty-two hundredths 3. sixteen and twenty-three hundredths 5. two hundred five thousandths 7. one hundred sixty-seven and nine thousandths 9. two hundred and five thousandths 11. one hundred five and six tenths 13. two and forty-three hundredths 15. eighty-seven and ninety-seven hundredths 17. one hundred eighteen and four tenths

19. R. W. Financial; 321.42; Three hundred twenty-one and 42/100 **21.** Bell South; 59.68; Fifty-nine and 68/100 **23.** 6.5 **25.** 9.08 **27.** 705.625 **29.** 0.0046 **31.** 32.52 **33.** 1.3 **35.** $\frac{3}{10}$ **37.** $\frac{27}{100}$ **39.** $\frac{4}{5}$ **41.** $\frac{3}{20}$ **43.** $5\frac{47}{100}$ **45.** $\frac{6}{125}$ **47.** $7\frac{1}{125}$ **49.** $15\frac{401}{500}$ **51.** $\frac{601}{2000}$ **53.** $487\frac{8}{25}$ **55.** 0.6 **57.** 0.45 **59.** 3.7 **61.** 0.268 **63.** 0.09 **65.** 4.026 **67.** 0.028 **69.** 56.3 **71.** 0.43; forty-three hundred the start of th

six million, eight hundred forty-nine thousand, five hundred seventy-six hundred-billionths 85. 17.268

Section 4.2

Vocabulary, Readiness & Video Check 1. circumference 3. after 5. left to right

Exercise Set 4.2 1. < 3. > 5. < 7. = 9. < 11. > 13. 0.006, 0.0061, 0.06 15. 0.03, 0.042, 0.36 17. 1.01, 1.09, 1.1, 1.16**19.** 20.905, 21.001, 21.03, 21.12 **21.** 0.6 **23.** 0.23 **25.** 0.594 **27.** 98,210 **29.** 12.3 **31.** 17.67 **33.** 0.5 **35.** 0.130 **37.** 3830 **39.** \$0.07 **41.** \$42,650 **43.** \$27 **45.** \$0.20 **47.** 0.3 cm **49.** 1.73 hr **51.** \$48 **53.** 89.4 people per sq mi **55.** 24.623 hr **57.** 0.5 min **59.** 5766 **61.** 71 **63.** 243 **65.** b **67.** a **69.** 225.228; 225 $\frac{57}{250}$; Audi Sport North America **71.** 224.200, 214.927, 214.500, 197.400 73. answers may vary 75. answers may vary 77. 0.26499, 0.25786 79. 0.10299, 0.1037, 0.1038, 0.9 81. \$11,800 million Section 4.3

Calculator Explorations 1. 328.742 3. 5.2414 5. 865.392

Vocabulary, Readiness & Video Check 1. 37.0 3. difference; minuend; subtrahend 5. false 7. Lining up the decimal points also lines up place values; to make sure we only add digits in the same place. 9. Check subtraction by addition.

| Exercise Set 4.3 1. | 3.5 3. 6.83 5. 0.094 | 7. 622.012 9. 583.09 11. Exact: 465.56; Estimate: 230 13. Exact: 115.123; $\frac{+230}{150}$ | | | | |
|--|------------------------------------|--|--|--|--|--|
| Estimate: 100 15. 27.0578 17. 56.432 19. 6.5 21. 15.3 23. 598.23 25. Exact: 1.83; Estimate: $6 - 4 = 2$ 27. 861.6
$\frac{+9}{-115}$ | | | | | | |
| 115 29. 376.89 31. Exact: 876.6; Estimate: 1000 33. 194.4 35. 2.9988 37. 16.3 39. 88.028 41. 84.072 43. 243.17 45. 56.83 $-\frac{100}{900}$ $-\frac{100}{900}$ $-\frac{100}{900}$ 47. 3.16 49. \$7.52 51. \$454.71 53. \$0.14 55. 28.56 m 57. 4.76 in. 59. 196.3 mph 61. 33.9° F 63. 763.035 mph 65. 16.16 in. 67. \$0.22 69. 29.4 billion (29,400,000,000) 71. 326.0 in. 73. 67.44 ft 75. \$1.552 77. 715.05 hr 79. Switzerland 81. 5.2 lb | | | | | | |
| 83. | Pounds of Chocolate | 85. 46 87. 3870 89. $\frac{4}{9}$ 91. incorrect; 9.200 93. 6.08 in. 95. \$1.20 | | | | |
| Country | per Person | 8.630 | | | | |
| Switzerland | 19.8 | + 4.005 | | | | |
| Germany 17.4 21.835 | | | | | | |
| Ireland | 16.3 | | | | | |
| United Kingdom | 16.3 | | | | | |
| Norway | 14.6 | | | | | |

97. 1 dime, 1 nickel, and 2 pennies; 3 nickels and 2 pennies; 1 dime and 7 pennies; 2 nickels and 7 pennies **99.** answers may vary **101.** answers may vary

Section 4.4

Vocabulary, Readiness & Video Check 1. sum 3. right; zeros 5. circumference 7. 3 9. 4 11. 8 13. Whether we placed the decimal point correctly in our product. 15. We used an approximation for π . The exact answer is 8π meters.

Exercise Set 4.4 1. 0.12 3. 0.6 5. 1.3 7. Exact: 22.26; Estimate: $5 \times 4 = 20$ 9. 0.4032 11. Exact: 8.23854; Estimate: 1 $\times 8$

13. 11.2746 **15.** 84.97593 **17.** 65 **19.** 0.65 **21.** 0.072 **23.** 709.3 **25.** 6046 **27.** 0.03762 **29.** 0.0492 **31.** 12.3 **33.** 1.29 **35.** 0.096 **37.** 0.5623 **39.** 43.274 **41.** 5,500,000,000 **43.** 97,800,000 **45.** 292,300 **47.** $8\pi \text{ m} \approx 25.12 \text{ m}$ **49.** $10\pi \text{ cm} \approx 31.4 \text{ cm}$ **51.** $18.2\pi \text{ yd} \approx 57.148 \text{ yd}$ **53.** \$715.20 **55.** \$8850 **57.** 24.8 g **59.** 14.36 sq in **61.** $250\pi \text{ ft} \approx 785 \text{ ft}$ **63.** $135\pi \text{ m} \approx 423.9 \text{ m}$ **65.** 64.9605 in. **67. a.** 62.8 m and 125.6 m **b.** yes **69.** 42.4 sq in. **71.** 26 **73.** 36 **75.** 8 **77.** 9 **79.** 3.64 **81.** 3.56 **83.** 0.1105 **85.** 3,831,600 mi **87.** answers may vary

Integrated Review 1. 2.57 2. 4.05 3. 8.9 4. 3.5 5. 0.16 6. 0.24 7. 11.06 8. 9.72 9. 4.8 10. 6.09 11. 75.56 12. 289.12 13. 25.026 14. 44.125 15. 82.7 16. 273.9 17. 280 18. 1600 19. 224.938 20. 145.079 21. 6 22. 6.2 23. 27.6092 24. 145.6312 25. 5.4 26. 17.74 27. 414.44 28. 1295.03 29. 116.81 30. 18.79 31. 156.2 32. 25.62 33. 5.62 34. 304.876 35. 114.66 36. 119.86 37. 0.000432 38. 0.00075 39. 0.0672 40. 0.0275 41. 862 42. 0.0293 43. 200 mi

Section 4.5

Calculator Explorations 1. not reasonable 3. reasonable

Vocabulary, Readiness & Video Check 1. quotient; divisor; dividend **3.** left; zeros **5.** 5.9 **7.** 0 **9.** 1 **11.** undefined **13.** a whole number **15.** When dividing by powers of 10, only the decimal point is moved. 1000 has three zeros, so we move the decimal point in the decimal number three places to the left. **17.** The fraction bar serves as a grouping symbol.

Exercise Set 4.5 1. 4.6 3. 0.094 5. 300 7. 5.8 9. Exact: 6.6; Estimate: $\frac{6}{6)36}$ 11. 0.413 13. 0.045 15. 7 17. 4.8 19. 2100

21. 30 **23.** 7000 **25.** Exact: 9.8; Estimate: $\frac{10}{7/70}$ **27.** 9.6 **29.** 45 **31.** 54.592 **33.** 0.0055 **35.** 179 **37.** 23.87 **39.** 113.1 **41.** 0.54982 **43.** 2.687 **45.** 0.0129 **47.** 12.6 **49.** 1.31 **51.** 12.225 **53.** 0.045625 **55.** 11 qt **57.** 202.1 lb **59.** 5.1 m **61.** 11.4 boxes **63.** 24 tsp **65.** 8 days **67.** 290.3 mi **69.** 217.5 kph **71.** 18.3 points per game **73.** 2.45 **75.** 0.66 **77.** 80.52 **79.** 14.7 **81.** 930.7 **83.** 571 **85.** 92.06 **87.** 144.4 **89.** $\frac{9}{10}$ **91.** $\frac{1}{20}$ **93.** 4.26 **95.** 1.578 **97.** 26.66 **99.** 904.29 **101.** c **103.** b **105.** 85.5 **107.** 8.6 ft **109.** answers may vary **111.** 65.2-82.6 knots **113.** 319.64 m

Section 4.6

Vocabulary, Readiness & Video Check 1. false 3. true 5. We place a bar over just the repeating digits and only 6 repeats in our decimal answer. 7. $A = l \cdot w$; 0.248 sq yd

8

Exercise Set 4.6 1. 0.2 3. 0.68 5. 0.75 7. 0.08 9. 1.2 11. 0.916 13. 0.425 15. 0.45 17. 0.3 19. 0.4375 21. 0.63 23. 5.85 **25.** 0.624 **27.** 0.33 **29.** 0.44 **31.** 0.6 **33.** 0.62 **35.** 0.485 **37.** 0.02 **39.** < **41.** = **43.** < **45.** < **47.** < **49.** > **51.** < **53.** < **55.** 0.32, 0.34, 0.35 **57.** 0.49, 0.491, 0.498 **59.** 0.73, $\frac{3}{4}$, 0.78 **61.** 0.412, 0.453, $\frac{4}{7}$ **63.** 5.23, $\frac{42}{8}$, 5.34 **65.** $\frac{17}{8}$, 2.37, $\frac{12}{5}$ **67.** 25.65 sq in. **69.** 9.36 sq cm **71.** 0.248 sq yd **73.** 8 **75.** 72 **77.** $\frac{1}{81}$ **79.** $\frac{9}{25}$ **81.** $\frac{5}{2}$ **83.** = 1 **85.** > 1 **87.** < 1 **89.** 0.057 91. 8200 stations 93. answers may vary 95. answers may vary 97. 47.25 99. 3.37 101. 0.45 Chapter 4 Vocabulary Check 1. decimal 2. numerator; denominator 3. vertically 4. and 5. sum 6. circumference 7. standard form 8. circumference; diameter 9. difference 10. quotient 11. product 12. sum Chapter 4 Review 1. tenths 2. hundred-thousandths 3. forty-five hundredths 4. three hundred forty-five hundred-thousandths 5. one hundred nine and twenty-three hundredths 6. forty-six and seven thousandths 7. 2.15 8. 503.102 9. $\frac{4}{25}$ 10. $12\frac{23}{1000}$ **11.** $1\frac{9}{2000}$ **12.** $25\frac{1}{4}$ **13.** 0.9 **14.** 0.25 **15.** 0.045 **16.** 26.1 **17.** > **18.** = **19.** 0.92, 8.09, 8.6 **20.** 0.09, 0.091, 0.1 **21.** 0.6 **22.** 0.94 **23.** \$0.26 **24.** \$12.46 **25.** \$31,304 **26.** 10.8 **27.** 9.52 **28.** 2.7 **29.** 7.28 **30.** 26.007 **31.** 459.7 **32.** 100.278 33. 65.02 34. 189.98 35. 52.6 mi 36. \$4.83 37. 22.2 in. 38. 38.9 ft 39. 18.5 40. 54.6 41. 72 42. 9345 43. 9.246 **44.** 3406.446 **45.** 14π m; 43.96 m **46.** 63.8 mi **47.** 887,000,000 **48.** 600,000 **49.** 0.087 **50.** 15.825 **51.** 70 **52.** 0.21 **53.** 8.059 **54.** 30.4 **55.** 0.0267 **56.** 9.3 **57.** 7.3 m **58.** 45 mo **59.** 16.94 **60.** 3.89 **61.** 129 **62.** 55 **63.** 0.81 **64.** 7.26 **65.** 0.8 **66.** 0.923 **67.** 2.3 or 2.333 **68.** 0.21 $\overline{6}$ or 0.217 **69.** = **70.** = **71.** < **72.** < **73.** 0.837, 0.839, $\frac{17}{20}$ **74.** $\frac{19}{12}$, 1.63, $\frac{18}{11}$ **75.** 6.9 sq ft **76.** 5.46 sq in. **77.** two hundred and thirty-two ten-thousandths **78.** 16,025.014 **79.** $\frac{231}{100,000}$ **80.** 0.75, $\frac{6}{7}$, $\frac{8}{9}$ 81. 0.07 82. 0.1125 83. 51.057 84. > 85. < 86. < 87. 42.90 88. 16.349 89. \$123 90. \$3646 91. 1.7 92. 2.49 93. 320.312 94. 148.74236 95. 8.128 96. 7.245 97. 4900 98. 23.904 99. 9600 sq ft 100. yes 101. 0.1024 102. 3.6 Chapter 4 Getting Ready for the Test 1. C 2. B 3. E 4. D 5. B 6. D 7. C 8. A 9. C 10. B 11. D 12. A 13. D 14. A 15. B 16. C 17. C Chapter 4 Test 1. forty-five and ninety-two thousandths 2. 3000.059 3. 34.9 4. 0.862 5. < 6. $\frac{4}{9}$, 0.445, 0.454 7. $\frac{69}{200}$ **8.** $24\frac{73}{100}$ **9.** 0.65 **10.** 5.8 or 5.889 **11.** 0.941 **12.** 17.583 **13.** 11.4 **14.** 43.86 **15.** 56 **16.** 0.07755 **17.** 6.673 **18.** 12,690 **19.** 4.73 **20.** 0.363 **21.** 6.2 **22.** 4,583,000,000 **23.** 2.31 sq mi **24.** 18π mi, 56.52 mi **25.** a. 9904 sq ft b. 198.08 oz **26.** 54 mi Cumulative Review 1. one hundred six million, fifty-two thousand, four hundred forty-seven; Sec. 1.2, Ex. 7 2. 276,004; Sec. 1.2 **3.** 10,591,862; Sec 1.3, Ex. 7 **4.** 288; Sec. 1.6 **5.** 726; Sec. 1.4, Ex. 4 **6.** 200; Sec. 1.9 **7.** 2300; Sec. 1.5, Ex. 4 **8.** 84; Sec. 1.9 **9.** 57,600 megabytes; Sec. 1.6, Ex. 11 **10.** perimeter: 28 ft; area: 49 sq ft; Sec. 1.6 **11.** 401 R 2; Sec. 1.7, Ex. 8 **12.** $\frac{21}{9}$; Sec. 2.1 **13.** 47; Sec. 1.9, Ex. 15 **14.** $12\frac{4}{5}$; Sec. 2.1 **15.** numerator: 3; denominator: 7; Sec. 2.1, Ex. 1 **16.** 9; Sec. 1.9 **17.** $\frac{1}{10}$; Sec. 2.3, Ex. 6

18. 17; Sec. 1.9 **19.** $\frac{15}{1}$ or 15; Sec. 2.4, Ex. 9 **20.** 13; Sec. 1.9 **21.** $\frac{63}{16}$; Sec. 2.5, Ex. 5 **22.** 128; Sec. 1.7 **23.** $\frac{15}{4}$ or $3\frac{3}{4}$; Sec. 2.4, Ex. 10 **24.** \$9; Sec. 1.7 **25.** $\frac{3}{20}$; Sec. 2.5, Ex. 8 **26.** $\frac{27}{20}$ or $1\frac{7}{20}$; Sec. 2.5 **27.** $\frac{7}{9}$; Sec. 3.1, Ex. 4 **28.** $\frac{2}{5}$; Sec. 3.1 **29.** $\frac{1}{4}$; Sec. 3.1, Ex. 5 **30.** $\frac{2}{5}$; Sec. 3.1 **31.** $\frac{15}{20}$; Sec. 3.2, Ex. 8 **32.** $\frac{35}{45}$; Sec. 3.2 **33.** $\frac{31}{30}$ or $1\frac{1}{30}$; Sec. 3.3, Ex. 2 **34.** $\frac{1}{90}$; Sec. 3.3 **35.** $4\frac{7}{40}$ lb; Sec. 3.4, Ex. 7 **36.** $27\frac{3}{4}$ lb; Sec. 3.4 **37.** $\frac{1}{16}$; Sec. 3.5, Ex. 3 **38.** $\frac{49}{121}$; Sec. 3.5 **39.** $\frac{3}{256}$; Sec. 3.5, Ex. 5 **40.** $\frac{2}{81}$; Sec. 3.5 **41.** $\frac{43}{100}$; Sec. 4.1, Ex. 8 **42.** 0.75; Sec. 4.1 **43.** >; Sec. 4.2, Ex. 1 **44.** 5.06; Sec. 4.1 **45.** 11.568; Sec. 4.3, Ex. 4 **46.** 75.329; Sec. 4.3 **47.** 2370.2; Sec. 4.4, Ex. 6 **48.** 0.119; Sec. 4.4 **49.** 768.05; Sec. 4.4, Ex. 9 **50.** 8.9; Sec. 4.5

Chapter 5 Ratio and Proportion

Section 5.1

Vocabulary, Readiness & Video Check 1. true 3. false 5. true 7. true 9. We can use "to" as in 1 to 2, a colon as in 1 : 2, or a fraction as in $\frac{1}{2}$.

Exercise Set 5.1 1. $\frac{11}{4}$ 3. $\frac{23}{10}$ 5. $\frac{151}{201}$ 7. $\frac{2.8}{7.6}$ 9. $\frac{5}{7\frac{1}{2}}$ 11. $\frac{3\frac{3}{4}}{1\frac{2}{3}}$ 13. $\frac{2}{3}$ 15. $\frac{77}{100}$ 17. $\frac{463}{821}$ 19. $\frac{3}{4}$ 21. $\frac{5}{12}$ 23. $\frac{8}{25}$ 25. $\frac{12}{7}$ 27. $\frac{16}{23}$ 29. $\frac{2}{5}$ 31. $\frac{2}{7}$ 33. $\frac{4}{1}$ 35. $\frac{10}{29}$ 37. $\frac{16}{51}$ 39. $\frac{25}{144}$ 41. $\frac{5}{4}$ 43. $\frac{15}{1}$ 45. $\frac{17}{40}$ 47. $\frac{52}{718} = \frac{26}{359}$ 49. $\frac{1}{3}$ 51. $\frac{27}{1118}$ 53. $\frac{1}{49}$ 55. 2.3 57. 0.15 59. the ratio of seven to nine 61. the ratio of thirty to one 63. no; answers may vary 65. no; $\frac{3}{2}$ 67. no; $\frac{2}{5}$ 69. no; $\frac{9}{2}$ 71. No, the shipment should not be refused. 73. a. $\frac{14}{50}$ or $\frac{7}{25}$ b. 36 states c. $\frac{14}{36}$ or $\frac{7}{18}$

Section 5.2

Vocabulary, Readiness & Video Check 1. unit **3.** division **5.** numerator; denominator **7.** We want a unit rate, which is a rate with a denominator of 1. A unit rate tells us how much of the first quantity (\$) will occur in 1 of the second quantity (years).

Exercise Set 5.2 1. $\frac{1 \text{ shrub}}{3 \text{ ft}}$ 3. $\frac{3 \text{ returns}}{20 \text{ sales}}$ 5. $\frac{3 \text{ laser printers}}{14 \text{ computers}}$ 7. $\frac{9 \text{ gal}}{2 \text{ acres}}$ 9. $\frac{3 \text{ flight attendants}}{100 \text{ passengers}}$ 11. $\frac{71 \text{ cal}}{2 \text{ fl oz}}$ 13. 110 cal/oz 15. 75 riders/car 17. 90 wingbeats/sec 19. \$50,000/yr 21. 74,355 residents/parish 23. 300 good/defective 25. \$8,200,350/player 27. 66 crayons/day 29. \$65,000/species 31. \$90,000/house 33. 8.7 tornadoes/hr 35. a. 31.25 computer boards/hr b. 33.5 computer boards/hr c. Suellen 37. a. 27.6 miles/gal b. 29.2 miles/gal c. the truck 39. \$11.50 per DVD 41. \$0.17 per banana 43. 8 oz: \$0.149 per oz; 12 oz: \$0.133 per oz; 12 oz 45. 16 oz: \$0.106 per oz; 6 oz: \$0.115 per oz; 16 oz 47. 12 oz: \$0.191 per oz; 8 oz: \$0.186 per oz; 8 oz 49. 100: \$0.006 per napkin; 180: \$0.005 per napkin; 180 napkins 51. 10.2 53. 4.44 55. 1.9 57. 257; 19.2 59. 347; 21.6 61. 1.5 steps/ft 63. answers may vary 65. no; answers may vary

| Integrated Review | 1. $\frac{9}{10}$ 2. $\frac{9}{25}$ 3. $\frac{4}{5}$ | $\frac{43}{50}$ 4. $\frac{8}{23}$ 5. | • $\frac{173}{139}$ 6. $\frac{6}{7}$ 7. $\frac{7}{26}$ | 8. $\frac{20}{33}$ 9. $\frac{2}{3}$ 10 | 0. $\frac{1}{8}$ 11. $\frac{1859}{1237}$ | 12. $\frac{9}{37}$ 13. a. 3 |
|---|---|--|--|--|--|---|
| b. $\frac{4}{7}$ 14. $\frac{2}{3}$ 15. $\frac{1}{4}$ | 1 office
graduate assistants | $16. \ \frac{2 \text{ lights}}{5 \text{ ft}}$ | 17. $\frac{2 \text{ senators}}{1 \text{ state}}$ 18. | $\frac{1 \text{ teacher}}{28 \text{ students}} 19.$ | $\frac{16 \text{ computers}}{25 \text{ households}}$ | 20. $\frac{9 \text{ students}}{2 \text{ computers}}$ |

21. 55 mi/hr **22.** 140 ft/sec **23.** 21 employees/fax line **24.** 17 phone calls/teenager **25.** 23 mi/gal **26.** 16 teachers/computer **27.** 6 books/student **28.** 154 lb/adult **29.** 8 lb: \$0.27 per lb; 18 lb: \$0.28 per lb; 8 lb **30.** 100: \$0.020 per plate; 500: \$0.018 per plate; 500 paper plates **31.** 3 packs: \$0.80 per pack; 8 packs: \$0.75 per pack; 8 packs **32.** 4: \$0.92 per battery; 10: \$0.99 per battery; 4 batteries

Section 5.3

Vocabulary, Readiness & Video Check 1. proportion; ratio 3. true 5. true 7. false 9. true 11. equals or = 13. a variable

| Exercise Set 5.3 | 1. $\frac{10 \text{ diamonds}}{6 \text{ opals}}$ | = <u>- 3.</u> - | $\frac{3 \text{ printers}}{2 \text{ computers}} =$ | $= \frac{1 \text{ printer}}{4 \text{ computers}}$ | 5. $\frac{6 \text{ eagl}}{58 \text{ sparr}}$ | = | eagles
sparrows | |
|--|---|--|--|---|--|------------------|--|-------------------------------|
| 7. $\frac{2\frac{1}{4} \text{cups flour}}{24 \text{ cookies}}$ | $= \frac{6\frac{3}{4} \text{cups flour}}{72 \text{ cookies}}$ | 9. $\frac{22 \text{ vanilla wafers}}{1 \text{ cup cookie crum}}$ | | anilla wafers
s cookie crumbs | 11. true | 13. false | 15. true 1 $\frac{2}{2}$ | 17. true $\frac{2}{3}$ |

19. false **21.** false **23.** true **25.** false **27.** true **29.**
$$\frac{8}{12} = \frac{4}{6}$$
; true **31.** $\frac{5}{2} = \frac{13}{5}$; false **33.** $\frac{1.8}{2} = \frac{4.5}{5}$; true **35.** $\frac{3}{\frac{1}{5}} = \frac{5}{\frac{1}{9}}$; false **37.** 3 **39.** 9 **41.** 4 **43.** 3.2 **45.** 38.4 **47.** 25 **49.** 0.0025 **51.** 1 **53.** $\frac{9}{20}$ **55.** 12 **57.** $\frac{3}{4}$ **59.** $\frac{35}{18}$ **61.** < **63.** > **65.** < **67.** $\frac{9}{3} = \frac{15}{5}$; $\frac{5}{15} = \frac{3}{9}$; $\frac{15}{9} = \frac{5}{3}$ **69.** $\frac{6}{1} = \frac{18}{3}$; $\frac{3}{18} = \frac{1}{6}$; $\frac{18}{6} = \frac{3}{1}$ **71.** possible answers: $\frac{d}{b} = \frac{c}{a}$; $\frac{a}{c} = \frac{b}{d}$; $\frac{b}{a} = \frac{d}{c}$ **73.** answers may vary

75. 14.9 **77.** 0.07 **79.** 3.163 **81.** 0 **83.** 1400 **85.** 252.5

Section 5.4

Vocabulary, Readiness & Video Check 1. There are approximately 102.9 mg of cholesterol in a 5-ounce serving of lobster. Exercise Set 5.4 1. 360 baskets 3. 165 min 5. 630 applications 7. 23 ft 9. 270 sq ft 11. 25 gal 13. 450 km 15. 16 bags 17. 15 hits 19. 27 people 21. 18 applications 23. 5 weeks 25. $10\frac{2}{3}$ servings 27. 37.5 sec 29. a. 18 tsp b. 6 tbsp 31. 6 people 33. 112 ft; 11-in. difference 35. 102.9 mg 37. 1257 ft; the actual height of the Empire State Building is 1248 feet. 39. 434 emergency room visits 41. 2 million SUV crossovers 43. 2.4 c 45. a. 0.1 gal b. 13 fl oz 47. a. 2062.5 mg b. no 49. $3 \cdot 5$ 51. $2^2 \cdot 5$ 53. $2^3 \cdot 5^2$ 55. 2^5 57. 0.8 ml 59. 1.25 ml 61. $11 \approx 12$ or 1 dozen; $1.5 \times 8 = 12$; 12 cups of milk 63. $4\frac{2}{3}$ ft 65. answers may vary Chapter 5 Vocabulary Check 1. ratio 2. proportion 3. unit rate 4. unit price 5. rate 6. cross products 7. equal 8. not equal Answers to Selected Exercises

Chapter 5 Review 1. $\frac{23}{37}$ 2. $\frac{14}{51}$ 3. $\frac{5}{4}$ 4. $\frac{11}{13}$ 5. $\frac{7}{15}$ 6. $\frac{17}{35}$ 7. $\frac{18}{35}$ 8. $\frac{35}{27}$ 9. a. 3 b. $\frac{3}{25}$ 10. a. 14 b. $\frac{14}{25}$ 11. $\frac{1 \text{ stillborn birth}}{125 \text{ live births}}$ 12. $\frac{3 \text{ professors}}{10 \text{ assistants}}$ 13. $\frac{5 \text{ pages}}{2 \text{ min}}$ 14. $\frac{4 \text{ computers}}{3 \text{ hr}}$ 15. 52 mi/hr 16. 15 ft/sec 17. \$6.96/CD **18.** $1\frac{1}{2}$ gal/acre **19.** \$46.80/course **20.** 13 bushels/tree **21.** 8 oz: \$0.124 per oz; **22.** 18 oz: \$0.083 per oz; 28 oz: \$0.085 per oz; 12 oz: \$0.141 per oz; 8-oz size 18-oz size **24.** 12 oz: \$0.049 per oz; **25.** $\frac{20 \text{ men}}{14 \text{ women}} = \frac{10 \text{ men}}{7 \text{ women}}$ **26.** $\frac{50 \text{ tries}}{4 \text{ successes}} = \frac{25 \text{ tries}}{2 \text{ successes}}$ **23.** 16 oz: \$0.037 per oz; 64 oz: \$0.026 per oz; 16 oz: \$0.049 per oz; 32 oz: \$0.037 per oz; 128 oz: \$0.018 per oz; 1-gal size 32-oz size 27. $\frac{16 \text{ sandwiches}}{8 \text{ players}} = \frac{2 \text{ sandwiches}}{1 \text{ player}}$ 28. $\frac{12 \text{ tires}}{3 \text{ cars}} = \frac{4 \text{ tires}}{1 \text{ car}}$ 29. no 30. yes 31. yes 32. no 33. 5 34. 15 35. 32.5 36. 5.625 **37.** 32 **38.** $6\frac{3}{4}$ **39.** 60 **40.** $7\frac{1}{5}$ **41.** 0.94 **42.** 0.36 **43.** $1\frac{1}{8}$ **44.** $1\frac{3}{7}$ **45.** 14 passes **46.** 35 passes **47.** 8 bags **48.** 16 bags **49.** no **50.** 79 gal **51.** \$54,600 **52.** \$1023.50 **53.** $40\frac{1}{2}$ ft **54.** $8\frac{1}{4}$ in. **55.** $\frac{3}{5}$ **56.** $\frac{4}{9}$ **57.** $\frac{1}{2}$ **58.** $\frac{5}{12}$ **59.** $\frac{1}{27}$ **60.** $\frac{1}{8}$ **61.** $\frac{1 \text{ teacher}}{9 \text{ students}}$ 62. $\frac{1 \text{ nurse}}{4 \text{ patients}}$ 63. 4 cups/person 64. 6 toys/child 65. 34 mi/hr 66. 2 gal/cow 67. 4 oz: \$1.235 per oz; 8 oz: \$1.248 per oz; 4-oz size 68. 12 oz: \$0.054 per oz; 64 oz: \$0.047 per oz; 64-oz size 69. $\frac{2 \text{ cups cookie dough}}{30 \text{ cookies}} = \frac{4 \text{ cups cookie dough}}{60 \text{ cookies}}$ 70. $\frac{5 \text{ nickels}}{3 \text{ dollars}} = \frac{20 \text{ nickels}}{12 \text{ dollars}}$ 71. yes 72. no 73. 1.6 74. 4.8 75. 84 76. 25 77. \$609.50 78. \$477 79. \$171 80. \$95 Chapter 5 Getting Ready for the Test 1. B 2. C 3. A 4. B 5. A 6. A 7. A 8. A Chapter 5 Test 1. $\frac{15}{2}$ 2. $\frac{9}{13}$ 3. $\frac{7 \text{ men}}{1 \text{ woman}}$ 4. $\frac{13 \text{ in.}}{10 \text{ days}}$ 5. $\frac{43}{50}$ 6. $\frac{47}{78}$ 7. $\frac{197}{62}$ 8. 81.25 km/hr 9. $\frac{2}{3}$ in./hr 10. 28 students/teacher 11. 9 in/sec 12. 8-oz size 13. 16-oz size 14. true 15. false 16. $\frac{25 \text{ computers}}{600 \text{ students}} = \frac{1 \text{ computer}}{24 \text{ students}}$ **17.** 5 **18.** $4\frac{4}{11}$ **19.** $\frac{7}{2}$ **20.** 8 **21.** $\frac{7}{8}$ **22.** $49\frac{1}{2}$ ft **23.** $3\frac{3}{4}$ hr **24.** $53\frac{1}{3}$ g **25.** $114\frac{2}{3}$ cartons **26.** 5925 adults Cumulative Review 1. a. 3 b. 15 c. 0 d. 70; Sec. 1.4, Ex. 1 2. a. 0 b. 20 c. 0 d. 20; Sec. 1.6 3. 249,000; Sec. 1.5, Ex. 3 **4.** 249,000; Sec. 1.5 **5. a.** 200 **b.** 1230; Sec. 1.6, Ex. 3 **6.** 373 R 24; Sec. 1.7 **7.** \$16,071; Sec. 1.8, Ex. 3 **8.** 16,591 ft; Sec. 1.8 **9.** $3 \cdot 3 \cdot 5$ or $3^2 \cdot 5$; Sec. 2.2, Ex. 3 **10.** 8; Sec. 1.9 **11.** $\frac{3}{5}$; Sec. 2.3, Ex. 1 **12.** 243; Sec. 1.9 **13.** $\frac{6}{5}$; Sec. 2.4, Ex. 5 **14.** $15\frac{3}{8}$; Sec. 2.4 **15.** $\frac{2}{5}$; Sec. 2.4, Ex. 6 **16.** $\frac{5}{54}$; Sec. 2.4 **17.** $\frac{5}{7}$; Sec. 3.1, Ex. 1 **18.** $\frac{19}{30}$; Sec. 3.1 **19.** $\frac{16}{13}$ or $1\frac{3}{13}$; Sec. 3.1, Ex. 3 **20.** $\frac{13}{10}$ or $1\frac{3}{10}$; Sec. 3.1 **21.** 36; Sec. 3.2, Ex. 2 **22.** $\frac{49}{50}$; Sec. 3.3 **23.** $\frac{12}{24}$; Sec. 3.2, Ex. 9 **24.** yes; Sec. 2.3 **25.** $\frac{8}{33}$; Sec. 3.3, Ex. 6 **26.** $7\frac{47}{72}$; Sec. 3.4 **27.** $\frac{1}{6}$ of an hour; Sec. 3.3, Ex. 9 **28.** 27; Sec. 1.9 **29.** $7\frac{17}{24}$; Sec. 3.4, Ex. 1 **30.** $\frac{16}{27}$; Sec. 2.5 **31.** >; Sec. 3.5, Ex. 1 32. 14,000,000; Sec. 1.6 33. one and three tenths; Sec. 4.1, Ex. 1 34. 0.075; Sec. 4.1 35. 736.2; Sec. 4.2, Ex. 5 36. 736.236; Sec. 4.2 37. 25.454; Sec. 4.3, Ex. 1 38. 681.24; Sec. 4.3 39. 0.0849; Sec. 4.4, Ex. 2 40. 0.375; Sec. 4.6 **41.** 0.125; Sec. 4.5, Ex. 3 **42.** $\frac{79}{10}$; Sec. 4.1 **43.** 3.7; Sec. 4.5, Ex. 12 **44.** 3; Sec. 5.3 **45.** $\frac{4}{9}$, $\frac{9}{20}$, 0.456; Sec. 4.6, Ex. 9 **46.** 140 m/sec; Sec. 5.2 **47.** $\frac{2.6}{3.1}$; Sec. 5.1, Ex. 2 **48.** $\frac{1}{3}$; Sec. 5.1 **49.** $\frac{1\frac{1}{2}}{7\frac{3}{2}}$; Sec. 5.1, Ex. 3 **50.** $\frac{1}{10}$; Sec. 5.1

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Chapter 6 Percent

Section 6.1

Vocabulary, Readiness & Video Check 1. Percent 3. percent 5. 0.01 7. $\frac{1}{100}$; 0.01

Exercise Set 6.1 1. 96% 3. a. 75% b. 25% 5. football; 37% 7. 50% 9. 0.41 11. 0.06 13. 1.00 or 1 15. 0.736 17. 0.028 19. 0.006 21. 3.00 or 3 23. 0.3258 25. 0.38 27. 0.493 29. 0.45 31. 98% 33. 310% 35. 2900% 37. 0.3% 39. 22% 41. 530% 43. 5.6% 45. 33.28% 47. 300% 49. 70% 51. 77% 53. 10.9% 55. 4.9% 57. 0.25 59. 0.65 61. 0.9 63. b, d 65. 4% 67. occupational therapy assistant 69. 0.30 71. answers may vary

Section 6.2

Vocabulary, Readiness & Video Check 1. Percent 3. 100% 5. 13% 7. 87% 9. 1% 11. The fraction of $\frac{4}{100}$ can be simplified to $\frac{1}{25}$. 13. The difference is in how the percent symbol is replaced—for a decimal, replace % with the equivalent decimal form 0.01, and for a fraction, replace % with the equivalent fraction form $\frac{1}{100}$.

Exercise Set 6.2 1. $\frac{3}{25}$ 3. $\frac{1}{25}$ 5. $\frac{9}{200}$ 7. $\frac{7}{4}$ or $1\frac{3}{4}$ 9. $\frac{73}{100}$ 11. $\frac{1}{8}$ 13. $\frac{1}{16}$ 15. $\frac{3}{50}$ 17. $\frac{31}{300}$ 19. $\frac{179}{800}$ 21. 75% 23. 70% 25. 40% 27. 59% 29. 34% 31. $37\frac{1}{2}$ % 33. $31\frac{1}{4}$ % 35. 160% 37. $77\frac{7}{9}$ % 39. 65% 41. 250% 43. 190% 45. 63.64% 47. 26.67% 49. 14.29% 51. 91.67% 53. $0.35, \frac{7}{20}$; 20%, 0.2; 50%, $\frac{1}{2}$; $0.7, \frac{7}{10}$; 375%, 0.375 55. $0.4, \frac{2}{5}$; $23\frac{1}{2}$ %, $\frac{47}{200}$; 80%, 0.8; $0.333\overline{3}$, $\frac{1}{3}$; 875%, 0.875; $0.075, \frac{3}{40}$ 57. 2, 2; 280%, $2\frac{4}{5}$; 705, $7\frac{1}{20}$; 454%, 4.54 59. $0.66; \frac{33}{50}$ 61. $0.592; \frac{74}{125}$ 63. 48% 65. 0.0975 67. 18% 69. $0.005; \frac{1}{200}$ 71. $0.162; \frac{81}{500}$ 73. $0.049; \frac{49}{1000}$ 75. 15 77. 10 79. 12 81. a. 52.9% b. 52.86% 83. 107.8% 85. 65.79% 87. 77% 89. 75% 91. 80% 93. greater 95. answers may vary 97. 0.266; 26.6% 99. 1.155; 115.5% Section 6.3

Vocabulary, Readiness & Video Check 1. is **3.** amount; base; percent **5.** greater **7.** percent: 42%; base: 50; amount: 21 **9.** percent: 125%; base: 86; amount: 107.5 **11.** "of" means multiplication; "is" means equal; "what" (or some equivalent) means the unknown number

Exercise Set 6.3 1. $18\% \cdot 81 = n$ **3.** $20\% \cdot n = 105$ **5.** $0.6 = 40\% \cdot n$ **7.** $n \cdot 80 = 3.8$ **9.** $n = 9\% \cdot 43$ **11.** $n \cdot 250 = 150$ **13.** 3.5 **15.** 28.7 **17.** 10 **19.** 600 **21.** 110% **23.** 34% **25.** 1 **27.** 645 **29.** 500 **31.** 5.16% **33.** 25.2 **35.** 35% **37.** 35 **39.** 0.624 **41.** 0.5% **43.** 145 **45.** 63% **47.** 4% **49.** n = 30 **51.** $n = 3\frac{7}{11}$ **53.** $\frac{17}{12} = \frac{n}{20}$ **55.** $\frac{8}{9} = \frac{14}{n}$ **57.** c **59.** b **61.** Twenty percent of some number is eighteen and six tenths. **63.** b **65.** c **67.** c **69.** a **71.** a **73.** answers may vary **75.** 686.625 **77.** 12,285

Section 6.4

Vocabulary, Readiness & Video Check 1. amount; base; percent 3. amount 5. amount: 12.6; base: 42; percent: 30 7. amount: 102; base: 510; percent: 20 9. 45 follows the word "of," so it is the base

Exercise Set 6.4 1. $\frac{a}{45} = \frac{98}{100}$ 3. $\frac{a}{150} = \frac{4}{100}$ 5. $\frac{14.3}{b} = \frac{26}{100}$ 7. $\frac{84}{b} = \frac{35}{100}$ 9. $\frac{70}{400} = \frac{p}{100}$ 11. $\frac{8.2}{82} = \frac{p}{100}$ 13. 26 15. 18.9 17. 600 19. 10 21. 120% 23. 28% 25. 37 27. 1.68 29. 1000 31. 210% 33. 55.18 33. 45% 37. 75 39. 0.864 41. 0.5% 43. 140 45. 9.6 47. 113% 49. $\frac{7}{8}$ 51. $3\frac{2}{15}$ 53. 0.7 55. 2.19 57. answers may vary 59. no; a = 16 61. yes 63. answers may vary 65. 12,011.2 67. 7270.6

Integrated Review 1. 12% 2. 68% 3. 12.5% 4. 250% 5. 520% 6. 800% 7. 6% 8. 44% 9. 750% 10. 325% 11. 3% 12. 5% 13. 0.65 14. 0.31 15. 0.08 16. 0.07 17. 1.42 18. 4 19. 0.029 20. 0.066 21. 0.03; $\frac{3}{100}$ 22. 0.05; $\frac{1}{20}$ 23. 0.0525; $\frac{21}{400}$ 24. 0.1275; $\frac{51}{400}$ 25. 0.38; $\frac{19}{50}$ 26. 0.45; $\frac{9}{20}$ 27. 0.123; $\frac{37}{300}$ 28. 0.167; $\frac{1}{6}$ 29. 8.4 30. 100 31. 250 32. 120% 33. 28% 34. 76 35. 11 36. 130% 37. 86% 38. 378 39. 150 40. 62

Section 6.5

Vocabulary, Readiness & Video Check 1. The price of the home was \$175,000.

Exercise Set 6.51. 1600 bolts3. 8.8 lb5. 14%7. 91,800 businesses9. 38.6%11. 496 chairs; 5704 chairs13. 59,917occupational therapy assistants15. 1835 thousand17. 29%19. 50%21. 12.5%23. 29.2%25. \$175,00027. 31.2 hr

29. increase: \$867.87; new price: \$20,153.87**31.** 40 ft**33.** increase: \$1043; tuition in 2016–2017: \$10,037**35.** increase: 1,494,100enrolled in associate degree programs; projected enrollment in 2024–2025: 8,194,100**37.** 30; 60%**39.** 52; 80%**41.** 2; 25%**43.** 120; 75%**45.** 44%**47.** 1.3%**49.** 142.0%**51.** 374.6%**53.** 9.8%**55.** 51.4%**57.** 28.9%**59.** 21.5%**61.** 4.56**63.** 11.18

65. 58.54 **67.** The increased number is double the original number. **69.** percent of increase $=\frac{30}{150}=20\%$ **71.** False; the percents are different.

Section 6.6

Vocabulary, Readiness & Video Check 1. sales tax **3.** commission **5.** sale price **7.** We rewrite the percent as an equivalent decimal. **9.** Replace "amount of discount" in the second equation with "discount rate \cdot original price": sale price = original price – (discount rate \cdot original price).

Exercise Set 6.61. \$7.503. \$858.935. 7%7. a. \$270b. \$292.959. \$117; \$191711. \$48513. 6%15. \$16.10; \$246.1017. \$53,176.0419. 14%21. \$4888.5023. \$185,50025. \$8.90; \$80.1027. \$98.25; \$98.2529. \$143.50; \$266.5031. \$3255;\$18,44533. \$45; \$25535. \$27.45; \$332.4537. \$3.08; \$59.0839. \$707441. 8%43. 120045. 13247. 1649. d51. \$4.00;\$6.00; \$8.0053. \$720; \$10.80; \$14.4055. a discount of 60% is better; answers may vary57. \$26,838.45

Section 6.7

Calculator Explorations 1. 1.56051 3. 8.06231 5. \$634.49

Vocabulary, Readiness & Video Check 1. simple **3.** Compound **5.** Total amount **7.** principal **9.** The denominator is the total number of payments. We are asked to find the monthly payment for a 4-year loan, and since there are 48 months in 4 years, there are 48 total payments.

Exercise Set 6.7 1. \$32 3. \$73.60 5. \$750 7. \$33.75 9. \$700 11. \$101,562.50; \$264,062.50 13. \$5562.50 15. \$5400 17. \$46,815.37 19. \$2327.14 21. \$58,163.65 23. 2915.75 25. \$2938.66 27. \$2971.89 29. \$260.31 31. \$637.26 33. 32 yd 35. 35 m 37. answers may vary 39. answers may vary

Chapter 6 Vocabulary Check 1. of 2. is 3. Percent 4. Compound interest 5. $\frac{\text{amount}}{\text{base}}$ 6. 100% 7. 0.01 8. $\frac{1}{100}$ 9. base; amount 10. Percent of decrease 11. Percent of increase 12. Sales tax 13. Total price 14. Commission 15. Amount of discount 16. Sale price

Chapter 6 Review 1. 37% 2. 77% 3. 0.83 4. 0.75 5. 0.035 6. 0.015 7. 1.25 8. 1.45 9. 0.005 10. 0.007 11. 2.00 or 2 12. 4.00 or 4 13. 0.2625 14. 0.8534 15. 260% 16. 102% 17. 35% 18. 5.5% 19. 72.5% 20. 25.2% 21. 76% 22. 8.5% 23. 71% 24. 65% 25. 400% 26. 900% 27. $\frac{1}{100}$ 28. $\frac{1}{10}$ 29. $\frac{1}{4}$ 30. $\frac{17}{200}$ 31. $\frac{51}{500}$ 32. $\frac{1}{6}$ 33. $\frac{1}{3}$ 34. $1\frac{1}{10}$ 35. 20% 36. 70% 37. $83\frac{1}{3}$ % 38. 60% 39. 125% 40. $166\frac{2}{3}$ % 41. 6.25% 42. 62.5% 43. 100,000 44. 8000 45. 23% 46. 114.5 47. 3000 48. 150% 49. 418 50. 300 51. 64.8 52. 180% 53. 110% 54. 165 55. 66% 56. 16% 57. 20.9% 58. 106.25% 59. \$206,400 60. \$13.23 61. \$273.75 62. \$3.36 63. \$5000 64. \$300.38 65. discount: \$900; sale price: \$2100 66. discount: \$9; sale price: \$81 67. \$160 68. \$325 69. \$30,104.61 70. \$17,506.54 71. \$180.61 72. \$33,830.10 73. 0.038 74. 0.245 75. 0.009 76. 54% 77. 9520% 78. 30% 79. $\frac{47}{100}$ 80. $\frac{8}{125}$ 81. $\frac{7}{125}$ 82. $37\frac{1}{2}$ % 83. $15\frac{5}{13}$ % 84. 120% 85. 268.75 86. 110% 87. 708.48 88. 134% 89. 300% 90. 38.4 91. 560 92. 325% 93. 26% 94. \$6786.50 95. \$617.70 96. \$9.45 97. 12.5% 98. \$1491 99. \$17,951.01 100. \$11,687.50

Chapter 6 Getting Ready for the Test 1. D 2. A 3. B 4. C 5. B 6. D 7. A 8. C 9. C 10. A 11. D 12. C Chapter 6 Test 1. 0.85 2. 5 3. 0.008 4. 5.6% 5. 610% 6. 39% 7. $\frac{6}{5}$ or $1\frac{1}{5}$ 8. $\frac{77}{200}$ 9. $\frac{1}{500}$ 10. 55% 11. 37.5% 12. $155\frac{5}{9}\%$ 13. 33.6 14. 1250 15. 75% 16. 38.4 lb 17. \$56,750 18. \$358.43 19. 5% 20. discount: \$18; sale price: \$102 21. \$395 22. 1% 23. \$647.50 24. \$2005.63 25. \$427

Cumulative Review 1. 206 cases; 12 cans; yes; Sec. 1.8, Ex. 2 2. 31,084; Sec. 1.6 3. a. $4\frac{2}{7}$ b. $1\frac{1}{15}$ c. 14; Sec. 2.1, Ex. 18 4. a. $\frac{19}{7}$ b. $\frac{101}{10}$ c. $\frac{43}{8}$; sec. 2.1 5. $2 \cdot 2 \cdot 2 \cdot 2 \cdot 5$ or $2^4 \cdot 5$; Sec. 2.2, Ex. 7 6. 119 sq mi; Sec. 1.6 7. $\frac{10}{27}$; Sec. 2.3, Ex. 3 8. 44; Sec. 1.7 9. $\frac{23}{56}$; Sec. 2.4, Ex. 4 10. 76,500; Sec. 1.5 11. $\frac{8}{11}$; Sec. 2.5, Ex. 2 12. $\frac{15}{4}$; $3\frac{3}{4}$; Sec. 2.1 13. $\frac{4}{5}$ in.; Sec. 3.1, Ex. 6 14. 50; Sec. 1.9 15. 60; Sec. 3.2, Ex. 4 16. $\frac{1}{3}$; Sec. 3.1 17. $\frac{2}{3}$; Sec. 3.3, Ex. 1 18. 340; Sec. 2.4 19. $3\frac{5}{14}$; Sec. 3.4, Ex. 5 20. 33; Sec. 1.9 21. $\frac{7}{16}$; Sec. 3.5, Ex. 6 22. $33\frac{27}{40}$; Sec. 3.4 23. $\frac{2}{33}$; Sec. 3.5, Ex. 8 24. $6\frac{3}{8}$; Sec. 2.4 25. 0.8; Sec. 4.1, Ex. 13 26. 0.09; Sec. 4.1 **27.** 8.7; Sec. 4.1, Ex. 14 **28.** 0.0048; Sec. 4.1 **29.** \$3.18; Sec. 4.2, Ex. 7 **30.** 27.94; Sec. 4.3 **31.** 829.6561; Sec. 4.3, Ex. 2 **32.** 1248.3; Sec. 4.4 **33.** 18.408; Sec. 4.4, Ex. 1 **34.** 76,300; Sec. 4.4 **35.** 0.7861; Sec. 4.5, Ex. 8 **36.** 1.276; Sec. 4.5 **37.** 0.012; Sec. 4.5, Ex. 9 **38.** 50.65; Sec. 4.5 **39.** 7236; Sec. 4.5, Ex. 11 **40.** 0.191; Sec. 4.5 **41.** 0.25; Sec. 4.6, Ex. 1 **42.** $0.\overline{5} \approx 0.556$; Sec. 4.6 **43.** $\frac{5 \text{ nails}}{3 \text{ ft}}$; Sec. 5.2, Ex. 1 **44.** 23 miles/gal; Sec. 5.2 **45.** no; Sec. 5.3, Ex. 3 **46.** 18: \$0.052 per tortilla; 24: \$0.058 per tortilla; 18 tortillas is better buy; Sec. 5.2 **47.** $17\frac{1}{2}$ mi; Sec. 5.4, Ex. 1 **48. a.** 0.07; Sec. 6.1 **b.** 2 **c.** 0.005 **49.** $n = 25\% \cdot 0.008$; Sec. 6.3, Ex. 3 **50.** 37.5% or $37\frac{1}{2}\%$; Sec. 6.2

Chapter 7 Measurement

Section 7.1

Vocabulary, Readiness & Video Check 1. meter 3. yard 5. feet 7. feet 9. feet; Feet are the original units and we want them to divide out. 11. The sum of 21 yd 4 ft is correct, but is not in a good format since there is a yard in 4 feet. Convert 4 feet = 1 yd 1 ft and add again: 21 yd + 1 yd + 1 ft = 22 yd 1 ft. 13. 1.29 cm and 12.9 mm; These two different-unit lengths are equal.

Exercise Set 7.1 1. 5 ft **3.** 36 ft **5.** 8 mi **7.** 102 in. **9.** $3\frac{1}{3}$ yd **11.** 33,792 ft **13.** 4.5 yd **15.** 0.25 ft **17.** 13 yd 1 ft

19. 7 ft 1 in. **21.** 1 mi 4720 ft **23.** 62 in. **25.** 26 ft **27.** 84 in. **29.** 11 ft 2 in. **31.** 22 yd 1 ft **33.** 6 ft 5 in. **35.** 7 ft 6 in. **37.** 14 ft 4 in. **39.** 83 yd 1 ft **41.** 6000 cm **43.** 4 cm **45.** 0.5 km **47.** 1.7 m **49.** 15 m **51.** 42,000 cm **53.** 7000 m **55.** 83 mm **57.** 0.201 dm **59.** 40 mm **61.** 8.94 m **63.** 2.94 m or 2940 mm **65.** 1.29 cm or 12.9 mm **67.** 12.64 km or 12,640 m **69.** 54.9 m **71.** 1.55 km **73.** $348\frac{2}{3}$; 12,552 **75.** $11\frac{2}{3}$; 420 **77.** 5000; 0.005; 500 **79.** 0.065; 65; 0.000065 **81.** 342,000; 342,000,000; 34,200,000 **83. a.** $213\frac{2}{3}$ yd **b.** 7692 in. **85.** 10 ft 6 in. **87.** 5100 ft **89.** 5.0 times **91.** 13 ft 11 in. **93.** 26.7 mm **95.** 15 ft 9 in. **97.** 96 ft **99.** 41.25 m or 4125 cm **101.** 3.35 m **103.** 2.13 m **105.** $72\frac{2}{3}$ yd **107.** 15 tiles **109.** $\frac{21}{100}$ **111.** 0.13 **113.** 0.25 **115.** no **117.** yes **119.** no **121.** Estimate: 13 yd **123.** answers may vary; for example, $1\frac{1}{3}$ yd or 48 in. **125.** answers may vary **127.** 334.89 sq m

Section 7.2

Vocabulary, Readiness & Video Check 1. Mass 3. gram 5. 2000 7. 2 lb 9. 2 tons 11. pounds; Pounds are the units we're converting to. 13. 3 places to the right; 4 g = 4000 mg

Exercise Set 7.2 1. 32 oz **3.** 10,000 lb **5.** 9 tons **7.** $3\frac{3}{4}$ lb **9.** $1\frac{3}{4}$ tons **11.** 204 oz **13.** 9800 lb **15.** 76 oz **17.** 1.5 tons **19.** $\frac{1}{20}$ lb **21.** 92 oz **23.** 161 oz **25.** 5 lb 9 oz **27.** 53 lb 10 oz **29.** 8 tons 750 lb **31.** 3 tons 175 lb **33.** 8 lb 11 oz **35.** 31 lb 2 oz **37.** 1 ton 700 lb **39.** 0.5 kg **41.** 4000 mg **43.** 25,000 g **45.** 0.048 g **47.** 0.0063 kg **49.** 15,140 mg **51.** 6250 g **53.** 350,000 cg **55.** 13.5 mg **57.** 5.815 g or 5815 mg **59.** 1850 mg or 1.85 g **61.** 1360 g or 1.36 kg **63.** 13.52 kg **65.** 2.125 kg **67.** 200,000; 3,200,000 **69.** $\frac{269}{400}$ or 0.6725; 21,520 **71.** 0.5; 0.0005; 50 **73.** 21,000; 21,000,000; 2,100,000 **75.** 8.064 kg **77.** 35 lb 14 oz **79.** 112.5 g **81.** 5 lb 8 oz **83.** 6 lb 15.5 oz **85.** 144 mg **87.** 6.12 kg **89.** 130 lb **91.** 211 lb **93.** 0.16 **95.** 0.875 **97.** no **99.** yes **101.** no **103.** answers may vary; for example, 250 mg or 0.25 g **105.** true **107.** answers may vary

Section 7.3

Vocabulary, Readiness & Video Check 1. capacity 3. fluid ounces 5. cups 7. quarts 9. 2 pt 11. 2 gal 13. 3 qt 15. 3 c 17. amount; unit 19. 3 places to the left; 5600 ml = 5.6 L

Exercise Set 7.3 1. 4 c **3.** 16 pt **5.** $3\frac{1}{2}$ gal **7.** 5 pt **9.** 8 c **11.** $3\frac{3}{4}$ qt **13.** $10\frac{1}{2}$ qt **15.** 9 c **17.** 23 qt **19.** $\frac{1}{4}$ pt **21.** 14 gal 2 qt **23.** 4 gal 3 qt 1 pt **25.** 22 pt **27.** 13 gal 2 qt **29.** 4 c 4 fl oz (or 2 pt 4 fl oz or 1 qt 4 fl oz) **31.** 1 gal 1 qt **33.** 2 gal 3 qt 1 pt **35.** 17 gal **37.** 4 gal 3 qt **39.** 5000 ml **41.** 0.00016 kl **43.** 5.6 L **45.** 320 cl **47.** 0.41 kl **49.** 0.064 L **51.** 160 L **53.** 3600 ml **55.** 19.3 L **57.** 4.5 L or 4500 ml **59.** 8410 ml or 8.41 L **61.** 16,600 ml or 16.6 L **63.** 3840 ml **65.** 162.4 L **67.** 336; 84; 168

69. $\frac{1}{4}$; 1; 2 **71.** 1.59 L **73.** 18.954 L **75.** 4.3 fl oz **77.** yes **79.** \$0.632 **81.** $\frac{4}{5}$ **83.** $\frac{3}{5}$ **85.** $\frac{9}{10}$ **87.** no **89.** no **91.** less than; answers may vary **93.** answers may vary **95.** 128 fl oz **97.** 1.5 cc **99.** 2.7 cc **101.** 54 u or 0.54 cc **103.** 86 u or 0.86 cc

Integrated Review 1. 3 ft 2. 2 mi 3. $6\frac{2}{3}$ yd 4. 19 ft 5. 11,088 ft 6. 38.4 in. 7. 3000 cm 8. 2.4 cm 9. 2 m 10. 18 m 11. 72 mm 12. 0.6 km 13. 15,000 lb 14. 5.5 tons 15. 136 oz 16. 4.5 lb 17. 6.5 lb 18. 80 oz 19. 28,000 g 20. 1.4 g 21. 0.0056 kg 22. 6000 g 23. 0.67 g 24. 0.0036 kg 25. 12 pt 26. 2.5 qt 27. 3.5 gal 28. 8.5 pt 29. 7 c 30. 6.5 gal 31. 7000 ml 32. 0.35 kl 33. 0.047 L 34. 970 L 35. 126 L 36. 0.075 L 37. 4 fl oz 38. 12 c

Section 7.4

Vocabulary, Readiness & Video Check 1. $1 L \approx 0.26$ gal or $3.79 L \approx 1$ gal

Exercise Set 7.4 1. 25.57 fl oz **3.** 218.44 cm **5.** 40 oz **7.** 57.66 mi **9.** 3.77 gal **11.** 13.5 kg **13.** $1.5; 1\frac{2}{3}; 150; 60$ **15.** 55; 5500; 180; 2160 **17.** 3.94 in. **19.** 80.5 kph **21.** 0.008 oz **23.** 229.6 ft **25.** 9.92 billion mi **27.** yes **29.** 2790 mi **31.** 90 mm **33.** 112.5 g **35.** 104 mph **37.** 26.24 ft **39.** 3 mi **41.** 8 fl oz **43. b 45. b 47. c 49. d 51. d 53.** 29 **55.** 9 **57.** 5 **59.** 36 **61.** 2.13 sq m **63.** 1.19 sq m **65.** 1.69 sq m **67.** 21.3 mg–25.56 mg **69.** 800 sq m or 8606.72 sq ft

Section 7.5

Vocabulary, Readiness & Video Check 1. F = 1.8C + 32;27

Exercise Set 7.5 1. 5° C **3.** 40° C **5.** 140° F **7.** 239° F **9.** 16.7° C **11.** 61.2° C **13.** 197.6° F **15.** 61.3° F **17.** 50° C **19.** 80.6° F **21.** 100° C **23.** 37.9° C **25.** 244.4° F **27.** 462.2° C **29.** 21.1° C **31.** 12 in. **33.** 12 cm **35.** 8 ft 4 in. **37.** false **39.** true **41.** $\approx 5,000,000,000,000^{\circ}$ C **43.** yes **45.** no **47.** no **49.** yes **51.** answers may vary

Section 7.6

Vocabulary, Readiness & Video Check 1. Energy 3. British Thermal Unit 5. 30 ft-lb 7. 60 ft-lb 9. 90 cal 11. 5 cal 13. U.S.; British; pound; Fahrenheit

Exercise Set 7.6 1. 1140 ft-lb **3.** 3696 ft-lb **5.** 425,000 ft-lb **7.** 23,340 ft-lb **9.** 778,000 ft-lb **11.** 15,560,000 ft-lb **13.** 26,553,140 ft-lb **15.** 10,283 BTU **17.** 805 cal **19.** 750 cal **21.** 1440 cal **23.** 2.6 hr **25.** 175 mi **27.** 73 **29.** 163 **31.** 19 **33.** 92.925 ft-lb **35.** 256 lb **37.** answers may vary

Chapter 7 Vocabulary Check 1. Weight 2. Mass 3. meter 4. unit fractions 5. gram 6. Energy 7. British Thermal Unit 8. liter 9. calorie

Chapter 7 Review 1. 9 ft 2. 24 yd 3. 7920 ft 4. 18 in. 5. 17 yd 1 ft 6. 3 ft 10 in. 7. 4200 cm 8. 820 mm 9. 0.01218 m 10. 0.00231 km 11. 21 yd 1 ft 12. 7 ft 5 in. 13. 41 ft 3 in. 14. 3 ft 8 in. 15. 9.5 cm or 95 mm 16. 2.74 m or 274 cm 17. 34.48 m 18. 2.45 km 19. 169 yd 2 ft 20. 126 ft 8 in. 21. 108.5 km 22. 0.24 sq m 23. 4.125 lb 24. 4600 lb 25. 3 lb 4 oz 26. 5 tons 300 lb 27. 0.027 g 28. 40,000 g 29. 21 dag 30. 0.0003 dg 31. 3 lb 9 oz 32. 10 tons 800 lb 33. 2 tons 750 lb 34. 33 lb 8 oz 35. 21.5 mg 36. 0.6 kg or 600 g 37. 4 lb 4 oz 38. 9 tons 1075 lb 39. 785 kg 40. 1.1625 kg 41. 8 qt 42. 5 c 43. 7 pt 44. 72 c 45. 4 qt 1 pt 46. 3 gal 3 qt 47. 3800 ml 48. 0.042 dl 49. 1.4 kl 50. 3060 cl 51. 1 gal 1 qt 52. 7 gal 53. 736 ml or 0.736 L 54. 15.5 L or 15,500 ml 55. 2 gal 3 qt 56. 6 fl oz 57. 10.88 L 58. yes 59. 22.96 ft 60. 10.55 m 61. 4.55 gal 62. 8.27 qt 63. 425.25 g 64. 10.35 kg 65. 109 yd 66. 180.4 lb 67. 3.18 qt 68. 2.36 in. 69. 473°F 70. 320°F 71. 1076°F 72. 34°C 73. 5.2°C 74. 26.7°C 75. 1.7°C 76. 329°F 77. 672 ft-lb 78. 136.5 ft-lb 79. 108,000 ft-lb 80. 9,336,000 ft-lb 81. 2600 BTU 82. 1125 cal 83. 15,120 cal 84. $2\frac{1}{3}$ hr 85. 13,200 ft 86. 75 in. 87. 4.5 mi 88. 10.75 ft

89. 4 tons 200 lb **90.** 2 tons 300 lb **91.** 500 cm **92.** 0.000286 km **93.** 1.4 g **94.** 0.24 g **95.** 27 qt **96.** 21 qt **97.** 17 c **98.** 12.5 c **99.** 186.8°F **100.** 59°F **101.** 11°C **102.** 28°C **103.** 9117 m or 9.117 km **104.** 8.353 km or 8353 m **105.** 13.9 L or 13,900 ml **106.** 35.7 L or 35,700 ml **107.** 8.1 g or 8100 mg **108.** 1.6 g or 1600 mg **109.** 50.4 kg **110.** 12.8 kg **111.** 7 gal 3 qt **112.** 8 gal 2 qt **113.** 38 dm or 3800 mm **114.** 58 dm or 5800 mm **115.** 2.25 tons **116.** 2.25 tons

Chapter 7 Getting Ready for the Test 1. C 2. D 3. D 4. A 5. B 6. A 7. A, C 8. B, D 9. D 10. A 11. C 12. B 13. A

18. 54.7°F **19.** 5.6 m **20.** 4 gal 3 qt **21.** 91.4 m **22.** 16 ft 6 in. **23.** 493 ft 6 in. **24.** 150.368 m **25.** 56.7°C **26.** 105.8°F **27.** 37,336 pt **28.** 0.2 oz **29.** 3.1 mi **30.** 18.95 L **31.** 679 ft-lb **32.** 20,228,000 ft-lb **33.** 900 cal **Cumulative Review 1.** 2010; Sec. 1.3, Ex.4 **2.** 1531; Sec. 1.4 **3.** $3 \cdot 3 \cdot 3 \cdot 5 \cdot 7$ or $3^3 \cdot 5 \cdot 7$; Sec. 2.2, Ex.5 **4.** 153 sq in.; Sec. 1.6 **5.** 33; Sec. 3.2, Ex.7 **6.** $\frac{10}{63}$; Sec. 3.3 **7.** $5\frac{1}{15}$; Sec. 3.4, Ex.2 **8.** $10\frac{1}{3}$; Sec. 2.4 **9.** $\frac{1}{8}$; Sec. 4.1, Ex.10 **10.** $1\frac{1}{5}$; Sec. 4.1 **11.** $105\frac{83}{1000}$; Sec. 4.1, Ex.12 **12.** $\frac{8}{27}$; Sec. 3.5 **13.** <; Sec. 4.2, Ex.2 **14.** 25; Sec. 1.9 **15.** 6769; Sec. 4.3, Ex.6 **16.** 139.231; Sec. 4.3 **17.** 4.21; Sec. 4.4, Ex.8 **18.** 186,040; Sec. 4.4 **19.** 0.0092; Sec. 4.4, Ex. 10 **20.** 5.8; Sec. 4.5 **21.** 0.26; Sec. 4.5, Ex.2 **22.** $\frac{21}{20}$ or $1\frac{1}{20}$; Sec. 3.3 **23.** 2.1875; Sec. 4.6, Ex.4 **24.** 73; Sec. 4.2 **25.** $0.\overline{6}$; Sec. 4.6, Ex.2 **26.** 2.16; Sec. 4.5 **27.** $\frac{12}{17}$; Sec. 5.1, Ex.1 **28.** $\frac{12}{23}$; Sec. 5.1 **29.** 22.5 mi/gal; Sec. 5.2, Ex.5 **30.** $\frac{1}{4}$; Sec. 5.1 **31.** $n = \frac{35}{6}$ or $5\frac{5}{6}$; Sec. 5.3, Ex.6 **32.** 75 cups; Sec. 5.3 **33.** 7 bags; Sec. 5.4, Ex.3 **34.** $\frac{23}{100}$; Sec. 6.2 **35.** 0.23; Sec. 6.1, Ex.3 **36.** 875% or $87\frac{1}{2}\%$; Sec. 6.2 **37.** 8.33%; Sec. 6.2, Ex.9 **38.** 24%; Sec. 6.3 or 6.4 **39.** 14; Sec. 6.3, Ex.7 **40.** 32 pints; Sec. 73 **41.** $\frac{75}{30} = \frac{p}{100}$; Sec. 6.4, Ex.5 **42.** 860 cm; Sec. 71 **43.** 18%; Sec. 6.5, Ex.6 **44.** 6.5 tons; Sec. 72 **45.** discount: \$16.25; sale price: \$48.75; Sec. 6.6, Ex.5 **46.** 52 oz; Sec. 72 **47.** $\frac{1}{2}$ tons; Sec. 72, Ex.1 **50.** 77°F; Sec. 75

Chapter 7 Test 1. 23 ft 4 in. **2.** 10 qt **3.** 1.875 lb **4.** 5600 lb **5.** $4\frac{3}{4}$ gal **6.** 0.04 g **7.** 2400 g **8.** 36 mm **9.** 0.43 g

10. 830 ml **11.** 1 gal 2 qt **12.** 3 lb 13 oz **13.** 8 ft 3 in. **14.** 2 gal 3 qt **15.** 66 mm or 6.6 cm **16.** 2.256 km or 2256 m **17.** 28.9°C

Chapter 8 Geometry

Section 8.1

Vocabulary, Readiness & Video Check 1. plane 3. Space 5. ray 7. straight 9. acute 11. Parallel; intersecting 13. degrees 15. vertical 17. $\angle WUV$, $\angle VUW$, $\angle U$, $\angle x$ 19. $180^{\circ} - 17^{\circ} = 163^{\circ}$

Exercise Set 8.1 1. line; line *CD* or line *l* or \overrightarrow{CD} **3.** line segment; line segment *MN* or \overline{MN} **5.** angle; $\angle GHI$ or $\angle IHG$ or $\angle H$ **7.** ray; ray *UW* or \overrightarrow{UW} **9.** $\angle CPR$, $\angle RPC$ **11.** $\angle TPM$, $\angle MPT$ **13.** straight **15.** right **17.** obtuse **19.** acute **21.** 67° **23.** 163° **25.** 32° **27.** 30° **29.** $\angle MNP$ and $\angle RNO$; $\angle PNQ$ and $\angle QNR$ **31.** $\angle SPT$ and $\angle TPQ$; $\angle SPR$ and $\angle RPQ$; $\angle SPT$ and $\angle SPR$; $\angle TPQ$ and $\angle QPR$ **33.** 27° **35.** 132° **37.** $m \angle x = 30^\circ$; $m \angle y = 150^\circ$; $m \angle z = 30^\circ$ **39.** $m \angle x = 77^\circ$; $m \angle y = 103^\circ$; $m \angle z = 77^\circ$ **41.** $m \angle x = 100^\circ$; $m \angle y = 80^\circ$; $m \angle z = 100^\circ$ **43.** $m \angle x = 134^\circ$; $m \angle y = 46^\circ$; $m \angle z = 134^\circ$ **45.** $\angle ABC$ or $\angle CBA$ **47.** $\angle DBE$ or $\angle EBD$ **49.** 15° **51.** 50° **53.** 65° **55.** 95° **57.** $\frac{9}{8}$ or $1\frac{1}{8}$ **59.** $\frac{7}{32}$ **61.** $\frac{5}{6}$ **63.** $\frac{4}{3}$ or $1\frac{1}{3}$ **65.** 360° **67.** 54.8° **69.** 45° **71.** false; answers may vary **73.** true **75.** $m \angle a = 60^\circ$; $m \angle b = 50^\circ$; $m \angle c = 110^\circ$; $m \angle d = 70^\circ$; $m \angle e = 120^\circ$ **77.** no; answers may vary **79.** 45° ; 45°

Section 8.2

Vocabulary, Readiness & Video Check 1. Because the sum of the measures of the angles of a triangle equals 180°, each angle in an equilateral triangle must measure 60°.

Exercise Set 8.2 1. pentagon 3. hexagon 5. quadrilateral 7. pentagon 9. equilateral 11. scalene; right 13. isosceles 15. 25° 17. 13° 19. 40° 21. diameter 23. rectangle 25. parallelogram 27. hypotenuse 29. 14 m 31. 14.5 cm 33. 40.6 cm 35. r = 2.3 mm 37. cylinder 39. rectangular solid 41. cone 43. cube 45. rectangular solid 47. sphere 49. pyramid 51. 14.8 in. 53. 13 mi 55. 72,368 mi 57. 108 59. 12.56 61. true 63. true 65. false 67. yes; answers may vary 69. answers may vary

Section 8.3

Vocabulary, Readiness & Video Check 1. perimeter 3. π 5. $\frac{22}{7}$ (or 3.14); 3.14 $\left(\text{or } \frac{22}{7} \right)$ 7. Opposite sides of a rectangle have the same length, so we can just find the sum of the lengths of all four sides.

Exercise Set 8.3 1. 64 ft **3.** 120 cm **5.** 21 in. **7.** 48 ft **9.** 42 in. **11.** 155 cm **13.** 21 ft **15.** 624 ft **17.** 346 yd **19.** 22 ft **21.** \$55 **23.** 72 in. **25.** 28 in. **27.** \$36.12 **29.** 96 m **31.** 66 ft **33.** 74 cm **35.** 17π cm; 53.38 cm **37.** 16π mi; 50.24 mi **39.** 26π m; 81.64 m **41.** 150π ft; 471 ft **43.** 12,560 ft **45.** 30.7 mi **47.** 14π cm \approx 43.96 cm **49.** 40 mm **51.** 84 ft **53.** 23 **55.** 1 **57.** 6 **59.** 10 **61. a.** width: 30 yd; length: 40 yd **b.** 140 yd **63. b 65. a.** 62.8 m; 125.6 m **b.** yes **67.** answers may vary **69.** 27.4 m **71.** 75.4 m **73.** 6.5 ft

Section 8.4

Vocabulary, Readiness & Video Check 1. The formula for the area of a rectangle; We split the L-shaped figure into two rectangles, used the area formula twice to find the area of each, and then added these two areas.

Answers to Selected Exercises

Exercise Set 8.4 1. 7 sq m **3.** $9\frac{3}{4}$ sq yd **5.** 15 sq yd **7.** 2.25π sq in. \approx 7.065 sq in. **9.** 17.64 sq ft **11.** 28 sq m **13.** 22 sq yd **15.** $36\frac{3}{4}$ sq ft **17.** $22\frac{1}{2}$ sq in. **19.** 25 sq cm **21.** 86 sq mi **23.** 24 sq cm **25.** 36π sq in. \approx 113 $\frac{1}{7}$ sq in. **27.** 168 sq ft **29.** 128,775 sq ft **31.** 1π sq cm \approx 3.14 sq cm **33.** 128 sq in.; $\frac{8}{9}$ sq ft **35.** 510 sq in. **37.** 168 sq ft **39.** 9200 sq ft **41. a.** 381 sq ft **b.** 4 squares **43.** 14π in. \approx 43.96 in. **45.** 25 ft **47.** $12\frac{3}{4}$ ft **49.** perimeter **51.** area **53.** area **55.** perimeter **57.** 12-in. pizza **59.** $1\frac{1}{3}$ sq ft; 192 sq in. **61.** 7.74 sq in. **63.** 5.29π sq mm; 16.6106 sq mm **65.** 298.5 sq m **67. a.** width: 40 yd; length: 60 yd **b.** 2400 sq yd **69.** no; answers may vary

Section 8.5

nswers to Selected Exercises

Vocabulary, Readiness & Video Check 1. volume 3. cubic 5. perimeter 7. Exact answers are in terms of π , and approximate answers use an approximation for π .

Exercise Set 8.5 1. 72 cu in. 3. 512 cu cm 5. 4π cu yd $\approx 12\frac{4}{7}$ cu yd 7. $\frac{500}{3}\pi$ cu in. $\approx 523\frac{17}{21}$ cu in. 9. 9π cu in. $\approx 28\frac{2}{7}$ cu in. 11. 75 cu cm 13. $2\frac{10}{27}$ cu in. 15. 8.4 cu ft 17. $10\frac{5}{6}$ cu in. 19. 960 cu cm 21. $\frac{1372}{3}\pi$ cu in. or $457\frac{1}{3}\pi$ cu in. 23. $7\frac{1}{2}$ cu ft 25. 288π cu ft 27. 5.25π cu in. 29. 4.5π cu m; 14.13 cu m 31. $12\frac{4}{7}$ cu cm 33. 8.8 cu in. 35. 10.648 cu in. 37. 25 39. 9 41. 5 43. 20 45. 2093.33 cu m 47. no; answers may vary 49. 5.5 cu ft; 5.8 cu ft; (b) is larger 51. $6\frac{2}{3}\pi$ cu in. ≈ 21 cu in. Integrated Review 1. 153° ; 63° 2. $m \angle x = 75^{\circ}$; $m \angle y = 105^{\circ}$; $m \angle z = 75^{\circ}$ 3. $m \angle x = 128^{\circ}$; $m \angle y = 52^{\circ}$; $m \angle z = 128^{\circ}$ 4. $m \angle x = 52^{\circ}$ 5. 4.6 in. 6. $4\frac{1}{4}$ in. 7. 20 m; 25 sq m 8. 12 ft; 6 sq ft 9. 10π cm ≈ 31.4 cm; 25π sq cm ≈ 78.5 sq cm 10. 32 m; 44 sq mi 11. 54 cm; 143 sq cm 12. 62 ft; 238 sq ft 13. 64 cu in. 14. 30.6 cu ft 15. 400 cu cm 16. $4\frac{1}{2}\pi$ cu mi $\approx 14\frac{1}{7}$ cu mi

Section 8.6

Calculator Explorations 1. 32 3. 5.568 5. 9.849

Vocabulary, Readiness & Video Check 1. 10 3. squaring 5. 9. The Pythagorean theorem works only for right triangles. $\log \int_{\log \frac{1}{\log 2}} \frac{1}{\log 2} \sqrt{49} = 7$ because 7^2 or $7 \cdot 7 = 49$.

Exercise Set 8.6 1. 2 3. 11 5. $\frac{1}{9}$ 7. $\frac{4}{8} = \frac{1}{2}$ 9. 1.732 11. 3.873 13. 6.856 15. 5.099 17. 6,7 19. 10,11 21. 16 23. 9.592 25. $\frac{7}{12}$ 27. 8.426 29. 13 in. 31. 6.633 cm 33. 52.802 m 35. 117 mm 37. 5 39. 12 41. 17.205 43. 44.822 45. 42.426 47. 1.732 49. 8.5 51. 141.42 yd 53. 25.0 ft 55. 340 ft 57. n = 4 59. n = 45 61. n = 6 63. 6 65. 10 67. answers may vary 69. yes 71. $(\sqrt{80} - 6)$ in. ≈ 2.94 in.

Section 8.7

Vocabulary, Readiness & Video Check 1. false 3. true 5. false 7. $\angle M$ and $\angle Y$, $\angle N$ and $\angle X$, $\angle P$ and $\angle Z$, $\frac{p}{z} = \frac{m}{y} = \frac{n}{x}$ 9. The ratios of corresponding sides are the same.

Exercise Set 8.7 1. congruent; SSS **3.** not congruent **5.** congruent; ASA **7.** congruent; SAS **9.** $\frac{2}{1}$ **11.** $\frac{3}{2}$ **13.** 4.5 **15.** 6 **17.** 5 **19.** 13.5 **21.** 17.5 **23.** 10 **25.** 28.125 **27.** 10 **29.** 520 ft **31.** 500 ft **33.** 60 ft **35.** 14.4 ft **37.** 52 neon tetras **39.** 381 ft **41.** 4.01 **43.** 1.23 **45.** $3\frac{8}{9}$ in.; no **47.** 8.4 **49.** answers may vary **51.** 200 ft, 300 ft, 425 ft

Chapter 8 Vocabulary Check 1. right triangle; hypotenuse; legs 2. line segment 3. complementary 4. line 5. perimeter
6. angle; vertex 7. Congruent 8. Area 9. ray 10. square root 11. transversal 12. straight 13. volume 14. vertical
15. adjacent 16. obtuse 17. right 18. acute 19. supplementary 20. Similar

Chapter 8 Review 1. right 2. straight 3. acute 4. obtuse 5. 65° 6. 75° 7. 58° 8. 98° 9. 90° 10. 25° 11. $\angle a$ and $\angle b; \angle b$ and $\angle c; \angle c$ and $\angle d; \angle d$ and $\angle a$ 12. $\angle x$ and $\angle w; \angle y$ and $\angle z$ 13. $m \angle x = 100^{\circ}; m \angle y = 80^{\circ}; m \angle z = 80^{\circ}$ 14. $m \angle x = 155^{\circ}; m \angle y = 155^{\circ}; m \angle z = 25^{\circ}$ 15. $m \angle x = 53^{\circ}; m \angle y = 53^{\circ}; m \angle z = 127^{\circ}$ 16. $m \angle x = 42^{\circ}; m \angle y = 42^{\circ}; m \angle z = 138^{\circ}$ 17. 103° 18. 60° 19. 60° 20. 65° 21. $4\frac{1}{5}$ m 22. 7 ft 23. 9.5 m 24. $15\frac{1}{5}$ cm 25. cube 26. cylinder 27. pyramid 28. rectangular solid 29. 18 in. 30. 2.35 m 31. pentagon 32. hexagon 33. equilateral 34. isosceles, right 35. 89 m 36. 30.6 cm 37. 36 m 38. 90 ft 39. 32 ft 40. 440 ft 41. 5.338 in. 42. 31.4 yd 43. 240 sq ft 44. 140 sq m 45. 600 sq cm 46. 189 sq yd 47. 49π sq ft ≈ 153.86 sq ft 48. 82.81 sq m 49. 119 sq in. 50. 1248 sq cm 51. 144 sq m 52. 432 sq ft 53. 130 sq ft 54. $15\frac{5}{8}$ cu in. 55. 84 cu ft 56. $20,000\pi$ cu cm $\approx 62,800$ cu cm 57. $\frac{1}{6}\pi$ cu km $\approx \frac{11}{21}$ cu km 58. $2\frac{2}{3}$ cu ft 59. 307.72 cu in. 60. $7\frac{1}{2}$ cu ft 61. 0.5π cu ft or $\frac{1}{2}\pi$ cu ft 62. 8 63. 12 64. $\frac{2}{5}$ 65. $\frac{1}{10}$ 66. 13 67. 29 68. 10.7 69. 93 70. 127.3 ft 71. 88.2 ft 72. $37\frac{1}{2}$ 73. $13\frac{1}{3}$ 74. 174 75. 33 ft 76. $x = \frac{5}{6}$ in; $y = 2\frac{1}{6}$ in. 77. 108° 78. 89° 79. 82° 80. 78° 81. 95° 82. 57° 83. 13 m 84. 12.6 cm 85. 22 dm 86. 273 in. 87. 194 ft 88. 1624 sq m 89. 9π sq m ≈ 28.26 sq m 90. $346\frac{1}{2}$ cu in. 91. 140 cu in. 92. 1260 cu ft 93. 28.728 cu ft 94. 1 95. 6 96. $\frac{4}{9}$ 97. 86.6 98. 20.8 99. 48.1 100. 19.7101. $6\frac{1}{2}$ 102. 12

Chapter 8 Getting Ready for the Test 1. D 2. B 3. E 4. A 5. F 6. C 7. B 8. C 9. A 10. B 11. B 12. C 13. A and D 14. B 15. A or D 16. C 17. D 18. D 19. A 20. B 21. B 22. A

Chapter 8 Test 1. 12° **2.** 56° **3.** 57° **4.** $m \angle x = 118^{\circ}$; $m \angle y = 62^{\circ}$; $m \angle z = 118^{\circ}$ **5.** $m \angle x = 73^{\circ}$; $m \angle y = 73^{\circ}$; $m \angle z = 73^{\circ}$ **6.** 6.2m **7.** $10\frac{1}{4}$ in. **8.** 26° **9.** circumference $= 18\pi$ in. ≈ 56.52 in.; area $= 81\pi$ sq in. ≈ 254.34 sq in. **10.** perimeter = 24.6 yd; area = 37.1 sq yd **11.** perimeter = 68 in.; area = 185 sq in. **12.** $62\frac{6}{7}$ cu in. **13.** 30 cu ft **14.** 7 **15.** 8.888 **16.** $\frac{8}{10} = \frac{4}{5}$ **17.** 16 in. **18.** 18 cu ft **19.** 62 ft; \$115.94 **20.** 5.66 cm **21.** 198.08 oz **22.** 75 **23.** approximately 69 ft

Cumulative Review 1. nineteen and five thousand twenty-three ten-thousandths; Sec. 4.1, Ex. 3 **2.** $\frac{53}{66}$; Sec. 3.3 **3.** 736.2; Sec. 4.2, Ex. 5 **4.** 700; Sec. 1.5 **5.** 47.06; Sec. 4.3, Ex. 3 **6.** $\frac{20}{11}$ or $1\frac{9}{11}$; Sec. 2.5 **7.** 76.8; Sec. 4.4, Ex. 5 **8.** $\frac{7}{66}$; Sec. 2.4 **9.** 76,300; Sec. 4.4, Ex. 7 **10.** $\frac{23}{2}$ or $11\frac{1}{2}$; Sec. 2.4 **11.** 38.6; Sec. 4.5, Ex. 1 **12.** 0.567; Sec. 4.5 **13.** 3.7; Sec. 4.5, Ex. 12 **14.** $\frac{3}{5}$ or 0.6; Sec. 3.5 **15.** >; Sec. 4.6, Ex. 7 **16.** <; Sec. 3.5 **17.** $\frac{26}{31}$; Sec. 5.1, Ex. 5 **18.** $\frac{16}{45}$; Sec. 3.3 **19.** yes; Sec. 5.3, Ex. 2 **20.** $\frac{35}{2}$ or $17\frac{1}{2}$; Sec. 5.3 **21.** 25%; Sec. 6.1, Ex. 1 **22.** 68%; Sec. 6.2 **23.** $\frac{19}{1000}$; Sec. 6.2, Ex. 2 **24.** $\frac{13}{50}$; Sec. 6.2 **25.** $\frac{5}{4}$ or $1\frac{1}{4}$; Sec. 6.2, Ex. 3 **26.** $\frac{28}{5}$ or $5\frac{3}{5}$; Sec. 6.2 **27.** 255; Sec. 6.3, Ex. 8 **28.** 15%; Sec. 6.3, or 6.4 **29.** 52; Sec. 6.4, Ex. 9 **30.** 9; Sec. 1.9 **31.** 775 freshmen; Sec. 6.5, Ex. 3 **32.** \$2.25/sq ft; Sec. 5.2 **33.** \$3210; Sec. 6.6, Ex. 3 **34.** 35 exercises; Sec. 5.3 **35.** 96 in; Sec. 7.1, Ex. 1 **36.** 2 yd 2 ft 4 in; Sec. 7.1 **37.** 3200 g; Sec. 7.2, Ex. 7 **38.** 0.07 m; Sec. 7.1 **39.** 3 gal 3 qt; Sec. 7.3, Ex. 3 **40.** 70,052; Sec. 1.2 **41.** 84.2°F; Sec. 7.5, Ex. 2 **42.** 12.5%; Sec. 6.2 **43.** 50°; Sec. 8.2, Ex. 1 **44.** 33 m; Sec. 8.3 **45.** 28 in; Sec. 8.3, Ex. 1 **46.** 45 sq in; Sec. 8.4

47. $\frac{2}{5}$; Sec. 8.6, Ex. 3 **48.** $\frac{3}{4}$; Sec. 8.6 **49.** $\frac{12}{19}$; Sec. 8.7, Ex. 2 **50.** $15\frac{5}{6}$; Sec. 8.7

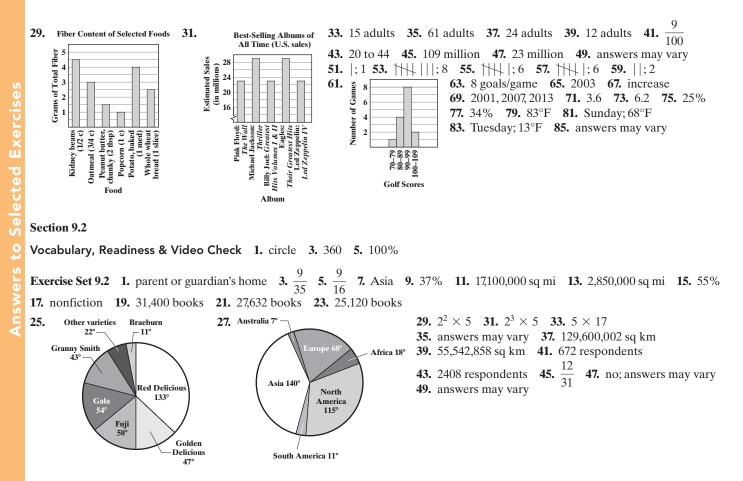
Chapter 9 Reading Graphs and Introduction to Statistics and Probability

Section 9.1

Vocabulary, Readiness & Video Check 1. bar 3. line 5. Count the number of symbols and multiply this number by how much each symbol stands for (from the key). 7. bar graph

Exercise Set 9.1 1. Kansas 3. 5.5 million or 5,500,000 acres 5. South Dakota, Colorado, and Washington 7. Montana

9. 48,000 **11.** 2016 **13.** 18,000 **15.** 60,000 wildfires/year **17.** September **19.** 78 **21.** $\frac{1}{39}$ **23.** Tokyo, Japan; about 38 million or 38,000,000 **25.** New York; 20.6 million or 20,600,000 **27.** approximately 3 million



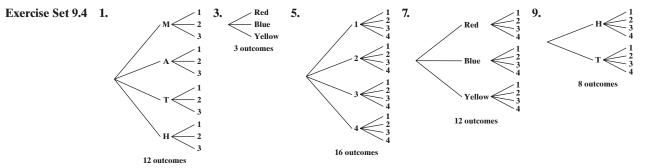
Integrated Review 1. 320,000 **2.** 440,000 **3.** personal care aides **4.** nursing assistants **5.** Oroville Dam; 755 ft 6. New Bullards Bar Dam; 635 ft 7. 15 ft 6. 5 caunt 11. Sunday, Monday, and Tuesday 12. Wednesday, Thursday, Friday, and Saturday 13. 70 qt containers 15. 2 qt containers 16. 6 qt containers 17. ||; 2 18. |; 1 19. || |; 3 20. $\uparrow \downarrow \downarrow \downarrow |; 6$ 21. $\uparrow \downarrow \downarrow \downarrow ; 5$ 22. $\downarrow 6$ $\downarrow 9$ \downarrow 11. Sunday, Monday, and Tuesday 12. Wednesday, Thursday, Friday, and Saturday 13. 70 qt containers 14. 52 qt containers Vocabulary, Readiness & Video Check 1. average 3. mean (or average) 5. grade point average 666686 82525

7. median 9. Place the data numbers in numerical order (or verify that they already are). **11.** answers may vary; For example: 6, 6, 6, 6

Exercise Set 9.3 1. mean: 21; median: 23; no mode 3. mean: 8.1; median: 8.2; mode: 8.2 5. mean: 0.5; median: 0.5; mode: 0.2 and 0.5 7. mean: 370.9; median: 313.5: no mode 9. 2109.2 ft 11. 1968.5 ft 13. answers may vary 15. 2.79 17. 3.64 19. 6.8 21. 6.9 23. 88.5 25. 73 27. 70 and 71 29. 9 rates 31. mean: 3773 mi; median: 3812 mi 33. 12 35. 350 37. 2 39. 1.7 41. a. 8.2 b. 8 c. 9 43. a. 6.1 b. 6 c. 6, 7, 8 45. a. 15 b. 15 c. 15 **47. a.** 6.1 **b.** 6 **c.** 4, 6 **49.** $\frac{3}{5}$ **51.** $\frac{1}{9}$ **53.** $\frac{7}{20}$ **55.** 35, 35, 37, 43 **57.** yes; answers may vary

Section 9.4

Vocabulary, Readiness & Video Check 1. outcome 3. probability 5. 0 7. The number of outcomes equals the ending number of branches drawn.



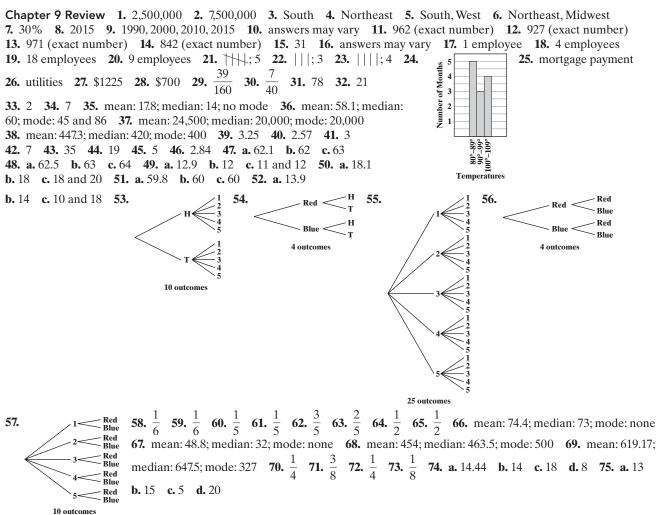
Quiz Scores

19.
$$\frac{1}{3}$$
 21. 1 **23.** $\frac{2}{3}$ **25.** $\frac{1}{7}$ **27.** $\frac{2}{7}$ **29.** $\frac{4}{7}$ **31.** $\frac{19}{100}$ **33.** $\frac{1}{20}$ **35.** $\frac{5}{6}$ **37.** $\frac{1}{6}$ **39.** $6\frac{2}{3}$ **41.** $\frac{1}{52}$

43. $\frac{1}{13}$ **45.** $\frac{1}{4}$ **47.** $\frac{1}{2}$ **49.** $\frac{5}{36}$ **51.** 0 **53.** answers may vary

11. $\frac{1}{6}$ **13.** $\frac{1}{3}$ **15.** $\frac{1}{2}$ **17.** $\frac{2}{3}$

Chapter 9 Vocabulary Check 1. bar 2. mean 3. outcomes 4. pictograph 5. mode 6. line 7. median 8. tree diagram 9. experiment 10. circle 11. probability 12. histogram; class interval; class frequency 13. range 14. median



Chapter 9 Getting Ready for the Test 1. C 2. C 3. D 4. C 5. C 6. C 7. A 8. B 9. C 10. A 11. B 12. D 13. D 14. A and C 15. A and B 16. C and D 17. A and C

Chapter 9 Test 1. \$225 2. 3rd week; \$350 3. \$1100 4. June, August, September 5. February; 3 cm 6. March and November



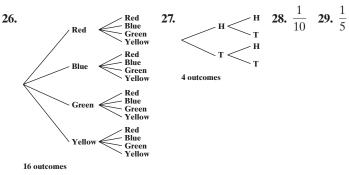
Lecter and the second s

8. 1.6% **9.** 2008, 2011 **10.** 2008–2009, 2011–2012, 2012–2013, 2014–2015 **11.** $\frac{17}{40}$ **12.** $\frac{31}{22}$ **13.** 74 million **14.** 90 million **15.** 9 students **16.** 11 students

| Class Intervals
(Scores) | Tally | Class Frequency
(Number of Students) | 18. | er of
ents | 8 |
|-----------------------------|---------|---|-----|-----------------------|-------|
| 40–49 | | 1 | | Number of
Students | 4 |
| 50–59 | | 3 | | 2 | 2 |
| 60–69 | | 4 | | | 40-49 |
| 70–79 | 1 | 5 | | | |
| 80–89 | 1+++111 | 8 | | | |
| 90–99 | | 4 | | | |

A21

19. mean: 38.4; median: 42; no mode **20.** mean: 12.625; median: 12.5; mode: 12 and 16 **21.** 3.07 **22.** 8 **23.** 56 **24. a.** 92.8 **b.** 93 **c.** 93 and 94 **d.** 4 **25. a.** 26.3 **b.** 25 **c.** 35 **d.** 20



Cumulative Review 1. 28; Sec. 1.9, Ex. 14 **2.** 12; Sec. 1.9 **3.** $\frac{5}{18}$; Sec. 2.3, Ex. 4 **4.** $\frac{7}{40}$; Sec. 3.3 **5.** $8\frac{3}{10}$; Sec. 3.4, Ex. 3 **6.** $\frac{34}{3}$ or $11\frac{1}{3}$; Sec. 2.4 **7.** 8.4 sq ft; Sec. 4.6, Ex. 10 **8.** 10 m; Sec. 3.6 **9.** $\frac{3}{2}$; Sec. 5.1, Ex. 4 **10.** $\frac{7}{18}$; Sec. 5.1 **11.** $\frac{\$180}{1 \text{ week}}$; Sec. 5.2, Ex. 2 **12.** $\frac{68 \text{ mi}}{1 \text{ hr}}$ or 68 mi/hr; Sec. 5.2 **13.** $\frac{45 \text{ mi}}{2 \text{ gal}}$; Sec. 5.2, Ex. 3 **14.** $\frac{39 \text{ files}}{2 \text{ hr}}$; Sec. 5.2 **15.** yes; Sec. 5.3, Ex. 4 **16.** yes; Sec. 5.3 **17.** 22.4 cc; Sec. 5.4, Ex. 2 **18.** 262.5 m; Sec. 5.4 **19.** 0.046; Sec. 6.1, Ex. 4 **20.** 0.0029; Sec. 6.1 **21.** 1.9; Sec. 6.1, Ex. 5 **22.** 4.52; Sec. 6.1 **23.** $\frac{2}{5}$; Sec. 6.2, Ex. 1 **24.** $\frac{27}{100}$; Sec. 6.2 **25.** $\frac{1}{3}$; Sec. 6.2, Ex. 4 **26.** $\frac{107}{175}$; Sec. 6.2 **27.** $5 = n \cdot 20$; Sec. 6.3, Ex. 1 **28.** $\frac{5}{20} = \frac{p}{100}$; Sec. 6.4 **29.** sales tax: \$6.41; total price: \$91.91; Sec. 6.6, Ex. 1 **30.** \$1610; Sec. 6.6 **31.** \$2400; Sec. 6.7, Ex. 3 **32.** 33.75; Sec. 9.3 **33.** $2\frac{1}{3}$ yd; Sec. 71, Ex. 2 **34.** 5000 pounds; Sec. 72 **35.** 4 lb 11 oz; Sec. 72, Ex. 5 **36.** 7; Sec. 1.9 **37.** 0.0235 g; Sec. 72, Ex. 8 **38.** 1060 mm; Sec. 71 **39.** 3.21 L; Sec. 73, Ex. 6 **40.** 500 cm; Sec. 71 **41.** 59°F; Sec. 75, Ex. 1 **42.** 5° C; Sec. 75 **43.** 42° ; Sec. 8.1, Ex. 4 **44.** 132°; Sec. 8.1 **45.** $\frac{1}{6}$; Sec. 8.6, Ex. 2 **46.** $\frac{1}{5}$; Sec. 8.6 **47.** 14 and 77; Sec. 9.3, Ex. 6 **48.** 56; Sec. 9.3 **49.** $\frac{1}{4}$; Sec. 9.4, Ex. 3 **50.** $\frac{3}{5}$; Sec. 9.4

Chapter 10 Signed Numbers

Section 10.1

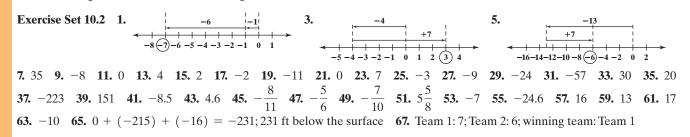
Vocabulary, Readiness & Video Check 1. integers 3. inequality symbols 5. is less than; is greater than 7. absolute value 9. number of feet a miner works underground 11. negative 13. opposite; opposite 15. Eyre

Exercise Set 10.1 1. -1235 3. +14,433 5. +125 7. -13,215 9. -1270 million 11. -276 13. -8

Section 10.2

Calculator Explorations 1. -159 3. 44 5. -894,855

Vocabulary, Readiness & Video Check 1. 0 **3.** a **5.** Negative; the numbers have different signs, so the sign of the sum is the same as the sign of the number with the larger absolute value, -9.



69. Day: 0; Summerhays: 0 **71.** Day: -3; Summerhays: -4 **73.** -\$39,000,000 **75.** \$355,000,000 **77.** 2°C **79.** \$13,609 **81.** -47°F **83.** -7679 m **85.** 44 **87.** 72.01 **89.** 141 **91.** answers may vary **93.** -3 **95.** -22 **97.** true **99.** false **101.** answers may vary

Section 10.3

Vocabulary, Readiness & Video Check 1. b **3.** d **5.** 0 **7.** 0 **9.** When subtracting, change the operation to addition and write down the opposite of the second number. The second number is -8, therefore its opposite is 8. **11.** The warmest temperature is 263° F warmer than the coldest temperature.

Exercise Set 10.3 1. 0 3. 5 5. -5 7. 14 9. 3 11. -18 13. -14 15. -3.3 17. 4.02 19. $\frac{2}{5}$ 21. $-\frac{3}{10}$ 23. $\frac{5}{6}$ 25. -38 27. -17 29. 13 31. -38 33. -11 35. -12.7 37. $\frac{3}{7}$ 39. 2 41. 0 43. -1 45. -27 47. 40 49. -51 51. 15°F 53. 4°F 55. 263°F 57. -\$16 59. -10°C 61. 154 ft 63. 69 ft 65. 652 ft 67. 144 ft 69. 1197°F 71. -\$44 billion 73. 0 75. 8 77. 1058 79. answers may vary 81. 16 83. -20 85. -4 87. 0 89. -14 91. false 93. answers may vary

Integrated Review 1. +29,028 2. -35,814 3. -7 4. +28,250 5.
-1.5
$$3\frac{1}{4}$$
 6. > 7. > 8. <

9. > 10. < 11. > 12. > 13. < 14. 1 15. 1 16. 0 17. -4 18. 8.6 19. 100.3 20. $\frac{3}{4}$ 21. $-\frac{3}{4}$ 22. -6 23. 13 24. -89.1 25. $\frac{2}{9}$ 26. 5 27. -20.8 28. $\frac{2}{9}$ 29. -2 30. $\frac{3}{4}$ 31. -4 32. -9.6 33. -6 34. 12 35. 120 36. -3.44 37. $-\frac{11}{10}$ or $-1\frac{1}{10}$ 38. 6 39. 1 40. -19 41. -12 42. -4 43. -44 44. -1.5 45. 191°F 46. 219°F

Section 10.4

Vocabulary, Readiness & Video Check 1. negative 3. positive 5. 0 7. undefined 9. multiplication

Exercise Set 10.4 1. 6 3. -36 5. -3.12 7. 0 9. $\frac{6}{35}$ 11. -48 13. -8 15. 80 17. -150 19. 4 21. -25 23. -27 25. -8 27. 81 29. $\frac{25}{121}$ 31. -4 33. -5 35. 8 37. 0 39. -13 41. -26 43. $\frac{25}{12}$ or $2\frac{1}{12}$ 45. -5 47. -50 49. 3 51. -300 53. $-\frac{4}{5}$ 55. 0 57. -125 59. -50 61. 43.4 63. $-\frac{32}{27}$ or $-1\frac{5}{27}$ 65. $-\frac{3}{2}$ or $-1\frac{1}{2}$ 67. -6 69. 252 71. $3 \cdot (-4) = -12$: a loss of 12 yd 73. $5 \cdot (-20) = -100$: a depth of 100 feet 75. -210°C 77. -189°C 79. -\$132 million per month 81. a. -5664 screens b. -1416 screens per year 83. 300 85. 225 87. 109 89. 8 91. -29 93. -19 95. -8 97. false 99. true 101. negative 103. $\frac{-20}{41}, \frac{20}{-41}$ 105. $(-5)^{17}, (-2)^{17}, (-2)^{12}, (-5)^{12}$ 107. answers may vary Section 10.5

Calculator Explorations 1. 48 3. -258

Vocabulary, Readiness & Video Check 1. division **3.** average **5.** subtraction **7.** Finding the average is a good application of both the order of operations and adding and dividing signed numbers.

Exercise Set 10.5 1. 3 3. 4 5. -7 7. -14 9. $-\frac{2}{9}$ 11. -8 13. 4 15. 1 17. 4 19. -3 21. -55 23. -4 25. 16 27. 15 29. -3 31. -3 33. 4 35. 16 37. -27 39. 34 41. 0.65 43. -59 45. -7 47. $\frac{5}{36}$ 49. -11 51. 36 53. -117 55. 30 57. -3 59. -2.21 61. -33 63. $-\frac{7}{5}$ 65. -2 67. -19 69. -13.75°F 71. no; answers may vary 73. 4050 75. 45 77. 32 in. 79. 30 ft 81. $2 \cdot (7-5) \cdot 3$ 83. -6 $\cdot (10-4)$ 85. answers may vary 87. answers may vary 89. 20,736

Chapter 10 Vocabulary Check 1. opposites 2. signed 3. absolute value 4. integers 5. additive inverse 6. negative 7. positive 8. inequality symbols 9. average 10. is less than; is greater than

34. -26 **35.** $-\frac{5}{4}$ or $-1\frac{1}{4}$ **36.** $-\frac{11}{10}$ or $-1\frac{1}{10}$ **37.** 20 **38.** 8 **39.** -4 **40.** -16 **41.** 1.2 **42.** 0.7 **43.** $-\frac{5}{18}$ **44.** $-\frac{3}{14}$ **45.** -\$25 **46.** +692 ft **47.** 121 **48.** 81 **49.** -81 **50.** -121 **51.** $-\frac{64}{125}$ **52.** $-\frac{8}{27}$ **53.** 21 **54.** -18 **55.** -26 **56.** -19 **57.** -36 **58.** -40 **59.** $-\frac{7}{12}$ **60.** 6 **61.** undefined **62.** 0 **63.** 1.2 **64.** $\frac{4}{5}$ **65.** 15 **66.** -7 **67.** -16 **68.** -44 **69.** -14.8 **70.** 44 **71.** 7 **72.** 7 **73.** 39 **74.** -41 **75.** $-\frac{23}{9}$ **76.** $-\frac{89}{100}$ **77.** -2 **78.** -12 **79.** 16 **80.** -16 **81.** -15 **82.** -19 **83.** 48 **84.** -21 **85.** 2.1 **86.** $-\frac{1}{4}$ **87.** $\frac{6}{5}$ **88.** $-\frac{3}{2}$ **89.** $-\frac{1}{40}$ **90.** -1.35 **91.** -\$9 **92.** 6°C **93.** 13,118 ft **94.** -27°C **95.** 2 **96.** 4 **97.** 3 **98.** 37 **99.** -5 **100.** -25 **101.** -20 **102.** 17

Chapter 10 Getting Ready for the Test 1. A 2. A 3. A 4. B 5. C 6. C 7. A 8. D 9. C 10. D 11. B 12. C 13. B 14. D 15. A 16. C 17. B 18. A 19. C 20. C 21. D 22. B 23. C 24. D

Cumulative Review 1. 78,875; Sec. 1.6, Ex. 5 **2.** $\frac{25}{44}$; Sec. 2.4 **3.** $\frac{4}{5}$; Sec. 2.5, Ex. 7 **4.** 236; Sec. 1.7 **5.** $\frac{17}{21}$; Sec. 3.3, Ex. 3 **6.** $1\frac{11}{14}$; Sec. 3.4 **7.** 48.26; Sec. 4.1, Ex. 6 **8.** 0.08; Sec. 4.1 **9.** 6.095; Sec. 4.1, Ex. 7 **10.** 56,321; Sec. 4.4 **11.** 3.432; Sec. 4.3, Ex. 5 **12.** 13.5; Sec. 4.5 **13.** 28.4405; Sec. 4.5, Ex. 13 **14.** 20; Sec. 19 **15.** $\frac{4500 \text{ dollars}}{1 \text{ month}}$ or 4500 dollars/month; Sec. 5.2, Ex. **16.** $\frac{60 \text{ miles}}{1 \text{ hour}}$ or 60 miles/hour; Sec. 5.2 **17.** n = 2; Sec. 5.3, Ex. 5 **18.** $n = \frac{48}{7}$; Sec. 5.3 **19.** 46%; Sec. 6.1, Ex. 2 **20.** 80%; Sec. 6.2 **21.** 45%; Sec. 6.2, Ex. 6 **22.** 106%; Sec. 6.2 **23.** 150%; Sec. 6.2, Ex. 8 **24.** 500%; Sec. 6.2 **25.** 200; Sec. 6.3, Ex. 10 **26.** 242; Sec. 6.3 or 6.4 **27.** $\frac{101}{200} = \frac{p}{100}$; Sec. 6.4, Ex. 2 **28.** 101 = $n \cdot 200$; Sec. 6.3 **29.** \$160; Sec. 6.7, Ex. 2 **30.** \$525; Sec. 1.4 **31.** 9 ft 1 in; Sec. 71, Ex. 6 **32.** 68 m; Sec. 8.3 **33.** 37°C; Sec. 75, Ex. 5 **34.** 720 cm; Sec. 71 **35.** 73°; Sec. 8.1, Ex. 5 **36.** 56°; Sec. 8.1 **37.** 60°; Sec. 8.2, Ex. 2 **38.** 49°; Sec. 8.2 **39.** 5.1 sq mi; Sec. 8.4, Ex. 2 **40.** 25π sq m ≈ 78.5 sq m; Sec. 8.4 **41.** $\frac{32}{3}\pi$ cu in. $\approx 33\frac{11}{21}$ cu in.; Sec. 8.5, Ex. 2 **42.** 24 cu cm; Sec. 8.5 **43.** 57; Sec. 9.3, Ex. 4 **44.** 24.5; Sec. 9.3 **45.** $\frac{1}{3}$; Sec. 9.4, Ex. 4 **46.** -4.9; Sec. 10.3 **47.** -23; Sec. 10.2, Ex. 3 **48. a.** -1000 **b.** -1000; Sec. 10.4 **49.** 82; Sec. 10.5, Ex. 1 **50.** -4; Sec. 10.5

Chapter 11 Introduction to Algebra

Section 11.1

Vocabulary, Readiness & Video Check 1. expression; term 3. combine like terms 5. variable; constant 7. associative 9. numerical coefficient 11. unlike 13. like 15. unlike 17. like 19. multiplication 21. the distributive property first, then the associative property of multiplication 23. addition; multiplication; P = perimeter, A = area

Exercise Set 11.1 1. -3 **3.** -2 **5.** 4 **7.** -3 **9.** -10 **11.** 133 **13.** -15 **15.** -4 **17.** $-\frac{4}{3}$ or $-1\frac{1}{3}$ **19.** -12 **21.** $\frac{3}{2}$ or $1\frac{1}{2}$ **23.** -10.6 **25.** 8x **27.** -4n **29.** -2c **31.** -4x **33.** 13a - 8 **35.** -0.9x + 11.2 **37.** 2x - 7 **39.** -5x + 4y - 5 **41.** $\frac{1}{2} - \frac{53}{60}x$ **43.** -4.8m - 4.1 **45.** 30x **47.** -22y **49.** -4.2a **51.** -4a **53.** 2y + 4 **55.** 15a - 40 **57.** -12x - 28 **59.** 6x - 0.12 **61.** $-4x - \frac{3}{2}$ **63.** 2x - 9 **65.** 27n - 20 **67.** 15 + 7w **69.** -11x + 8 **71.** (14y + 22) m **73.** (11a + 12) ft **75.** (25x + 55) in. **77.** 36y sq in. **79.** (32x - 64) sq km **81.** (60y + 20) sq mi **83.** 4700 sq ft **85.** 64 ft **87.** (3x + 6) ft **89.** \$360 **91.** 78.5 sq ft **93.** 23°F **95.** 288 cu in. **97.** 91.2x cu in. **99.** -3 **101.** 8 **103.** 0 **105.** incorrect; 15x - 10

107. incorrect; 7x - x - 2 or 6x - 2 **109.** distributive **111.** associative **113.** answers may vary **115.** (20x + 16) sq mi **117.** 23,506.2 sq in. **119.** 4824q + 12,274

Section 11.2

Vocabulary, Readiness & Video Check 1. equivalent **3.** simplifying **5.** addition **7.** We can add the same number to both sides of an equation or subtract the same number from both sides of an equation and we'll have an equivalent equation.

Exercise Set 11.2 1. yes 3. no 5. yes 7. yes 9. 18 11. -8 13. 9 15. -16 17. 3 19. $\frac{1}{8}$ 21. 6 23. 8 25. 5.3 27. -1 29. -20.1 31. 2 33. 0 35. -28 37. -6 39. 24 41. -30 43. 12 45. 1 47. 1 49. 1 51. subtract $\frac{2}{3}$ from both sides 53. add $\frac{4}{5}$ to both sides 55. answers may vary 57. 162,964 59. 1872 yards 61. \$18,686,000,000

Section 11.3

Vocabulary, Readiness & Video Check 1. equivalent 3. simplifying 5. multiplication 7. Simplified each side of the equation by combining like terms.

Exercise Set 11.3 1. 4 3. -4 5. -30 7. -17 9. 50 11. 25 13. -30 15. $\frac{1}{3}$ 17. $-\frac{2}{3}$ 19. -4 21. 8 23. 1.3 25. 2 27. 0 29. -0.05 31. $-\frac{15}{64}$ 33. $\frac{2}{3}$ 35. 6 37. 0 39. -2 41. -8 43. 1 45. 72 47. 35 49. -28 51. 25 53. 1 55. -10 57. 2015 59. 9.3 million acres or 9,300,000 acres 61. addition 63. division 65. answers may vary 67. 6.5 hr 69. 58.8 mph 71. -3648 73. 67,896 75. -48

Integrated Review 1. expression 2. equation 3. equation 4. expression 5. simplify 6. solve 7. 4 8. -6 9. 1 10. -4 11. 8x 12. -4y 13. -2a - 2 14. -2x + 3y - 7 15. -8x - 14 16. -6x + 30 17. 5y - 10 18. 15x - 31 19. (12x - 6) sq m 20. 20y in. 21. 13 22. -9 23. $\frac{7}{10}$ 24. 0 25. -4 26. 25 27. -1 28. -3 29. 6 30. 8 31. $-\frac{9}{11}$ 32. 5

Section 11.4

Calculator Explorations 1. yes 3. no 5. yes

Vocabulary, Readiness & Video Check 1. 3x - 9 + x - 16; 5(2x + 6) - 1 = 39 3. addition 5. distributive 7. the addition property of equality; to make sure we get an equivalent equation 9. gives; amounts to

Exercise Set 11.4 1. 3 3. 1.9 5. -4 7. 100 9. -3.9 11. -4 13. -12 15. -3 17. -1 19. -45 21. -9 23. 6 25. -5 27. 5 29. 8 31. 0 33. -22 35. 6 37. -11 39. -7 41. -5 43. 5 45. -3 47. 2 49. -4 51. -1 53. 4 55. 3 57. -1 59. 8 61. 4 63. 3 65. 64 67. $\frac{1}{9}$ 69. $\frac{3}{2}$ 71. -54 73. 2 75. $\frac{9}{5}$ 77. 270 79. 0 81. 4 83. 1 85. -42 + 16 = -26 87. -5(-29) = 145 89. 3(-14-2) = -48 91. $\frac{100}{2(50)} = 1$ 93. 126 million or 126,000,000 95. 39 million or 39,000,000 97. b 99. a 101. 6x - 10 = 5x - 7 103. 0 105. -4 107. no; answers may vary 109. 123.26°F 111. -9.4°F

Section 11.5

Vocabulary, Readiness & Video Check 1. decreased by 3. The phrase is "three times the difference of a number and 5." The "difference of a number and 5" translates to the expression x - 5, and in order to multiply 3 times this expression, we insert parentheses around the expression.

Exercise Set 11.5 1. x + 5 3. x + 8 5. 20 - x 7. 512x 9. $\frac{x}{2}$ 11. 17 + x + 5x 13. -5 + x = -7 15. 3x = 2717. -20 - x = 104 19. 5x 21. 11 - x 23. 2x = 108 25. 50 - 8x 27. 5(-3 + x) = -20 29. 9 + 3x = 33; 8 31. 3 + 4 + x = 16; 9 33. $x - 3 = \frac{10}{5}$; 5 35. 30 - x = 3(x + 6); 3 37. 5x - 40 = x + 8; 12 39. $3(x - 5) = \frac{108}{12}$; 8

41. 4x = 30 - 2x; **5 43.** California: 55 votes; Florida: 29 votes **45.** falcon: 185 mph; pheasant: 37 mph **47.** India: 3.5 million students; Turkey: 2.0 million students **49.** *Grand Theft Auto V*: \$30; *Kinect Adventures*: \$6 **51.** 5470 miles **53.** Michigan Stadium: 109,901; Beaver Stadium: 106,572 **55.** California: 660 thousand; Washington: 132 thousand **57.** 71 points **59.** 2010: 275,215; 2020: 808,416 **61.** Steelers: 6; Dolphins: 2 **63.** \$225 **65.** Asia: 1900 million; Europe: 650 million **67.** 590 **69.** 1000 **71.** 3000 **73.** yes; answers may vary **75.** \$216,200 **77.** \$549

Chapter 11 Vocabulary Check 1. simplified; combined 2. like 3. variable 4. algebraic expression 5. terms 6. numerical coefficient 7. evaluating the expression 8. constant 9. equation 10. solution 11. distributive 12. multiplication 13. addition

Chapter 11 Review 1. -5 2. 17 3. undefined 4. 0 5. 129 6. -2 7. 8 cu ft 8. 64 cu ft 9. \$1800 10. \$300 11. -15x 12. $-\frac{7}{30}x$ 13. -6y - 10 14. -6a - 7 15. -8y + 2 16. 4.6x - 11.9 17. -8y 18. 15y - 24 19. 11x - 12 20. 4x - 7 21. -5a + 4 22. 12y - 9 23. (6x - 3) sq yd 24. 28y m 25. yes 26. no 27. -2 28. 7 29. $-\frac{1}{2}$ 30. $-\frac{6}{11}$ 31. -6 32. -20 33. 1.3 34. 2.4 35. 7 36. -9 37. 1 38. -5 39. $-\frac{4}{5}$ 40. -24 41. -120 42. 13 43. 4 44. 3 45. 5 46. 12 47. 63 48. 33 49. -2.25 50. 1.3 51. 2 52. 6 53. 11 54. -5 55. 6 56. 8 57. 20 - (-8) = 28 58. -2 - 19 = -21

59. $\frac{-75}{5+20} = -3$ **60.** -5(-2+6) = -20 **61.** $\frac{70}{x}$ **62.** x - 13 **63.** 85 - x **64.** 2x + 11 **65.** x + 8 = 40 **66.** 2x - 12 = 1067. 5 68. -16 69. bamboo: 36 inches; kelp: 18 inches 70. incumbent: 14,752 votes; challenger: 3546 votes 71. 29 72. $-\frac{1}{4}$ **73.** -11x **74.** -35x **75.** 22x - 19 **76.** -9x - 32 **77.** x - 17 **78.** 3(x + 5) **79.** $x - 3 = \frac{x}{4}$ **80.** 6x = x + 2 **81.** no 82. yes 83. -1 84. -25 85. 13 86. -6 87. 17 88. 7 89. -22 90. -6 91. $-\frac{3}{4}$ 92. -4 93. 2 94. $-\frac{8}{3}$ 95. 12 **96.** -8 **97.** 0 **98.** 0 **99.** 5 **100.** 1 Chapter 11 Getting Ready for the Test 1. B 2. D 3. A 4. C 5. A 6. B 7. A 8. C 9. C 10. B 11. B 12. B 13. D 14. A 15. B 16. A 17. C 18. A 19. D 20. E 21. B 22. C 23. E 24. F Chapter 11 Test 1. -1 2. -5x + 5 3. -6y - 14 4. 14z - 8 5. 4(3x - 1) sq m = (12x - 4) sq m 6. 7 7. $-\frac{1}{2}$ 8. -129. 40 10. 24 11. 3 12. -2 13. -2 14. 4.5 15. 0 16. -2 17. $\frac{22}{3}$ 18. 4 19. 0 20. 6000 sq ft 21. 30 sq ft 22. a. 17x **b.** 20 - 2x **23.** -2 **24.** 34 points **25.** 244 women Cumulative Review 1. 0.8496; Sec. 4.4, Ex. 3 2. 53.1; Sec. 4.4 3. a. $\frac{5}{8}$ b. $\frac{4}{13}$; Sec. 5.1, Ex. 8 4. $\frac{23}{36}$; Sec. 3.3 **5.** 5; Sec. 6.3, Ex. 9 **6.** $\frac{7}{12}$; Sec. 2.4 **7.** 75%; Sec. 6.3, Ex. 11 **8.** $\frac{18}{23}$; Sec. 2.5 **9.** 48 oz; Sec. 7.2, Ex. 2 **10.** 24,000; Sec. 1.5 11. 11.3 L or 11,300 ml; Sec. 7.3, Ex. 8 12. 0.024; Sec. 4.2 13. a. line b. line segment c. angle d. ray; Sec. 8.1, Ex. 1 14. 168°; Sec. 8.1 15. 10 cm; Sec. 8.2, Ex.3 16. 34°; Sec. 8.2 17. 50 ft; Sec. 8.3, Ex.6 18. 132 sq ft; Sec. 8.4 19. 56 sq cm; Sec. 8.4, Ex. 1 20. 18; Sec. 1.9 21. a. 8 and 9 b. 9; Sec. 8.6, Ex. 5 22. 5.78; Sec. 4.5 23. 46 ft; Sec. 8.7, Ex. 4 24. 24%; Sec. 6.3 or 6.4 **25.** a. 75 clam species b. mammals; Sec. 9.1, Ex. 3 **26.** mean: 8; median: 9; mode: 11; Sec. 9.3 **27.** <; Sec. 10.1, Ex. 6 **28.** >; Sec. 4.6 **29.** >; Sec. 10.1, Ex. 5 **30.** < ; Sec. 3.5 **31.** 2; Sec. 10.1, Ex. 10 **32.** $\frac{5}{6}$; Sec. 10.1 **33.** 1.2; Sec. 10.1, Ex. 14 **34.** 0; Sec. 10.1 **35.** -16; Sec. 10.2, Ex. 4 **36.** -3.6; Sec. 10.2 **37.** $-\frac{1}{2}$; Sec. 10.2, Ex. 6 **38.** $\frac{1}{10}$; Sec. 10.2 **39.** -7; Sec. 10.3, Ex. 6 **40.** 5.8; Sec. 10.3 **41.** 1; Sec. 10.3, Ex. 7 **42.** $-\frac{31}{120}$; Sec. 10.3 **43.** 10; Sec. 10.4, Ex. 2 **44.** -9.6; Sec. 10.4 **45.** $\frac{1}{3}$; Sec. 10.4, Ex. 4 **46.** -4; Sec. 10.4 **47.** 3 Sec. 10.5, Ex. 6 **48.** 9.7; Sec. 11.2 **49.** 2; Sec. 11.4, Ex. 7 **50.** 20; Sec. 11.4

Appendices

 A1: One Hundred Addition Facts
 1. 5
 3. 5
 5. 12
 7. 8
 9. 14
 11. 12
 13. 10
 15. 9
 17. 11
 19. 18
 21. 10
 23. 10

 25. 17
 27. 13
 29. 12
 31. 16
 33. 7
 35. 4
 37. 8
 39. 8
 41. 6
 43. 16
 45. 9
 47. 12
 49. 7
 51. 2
 53. 11
 55. 8
 57. 5

 59. 14
 61. 13
 63. 7
 65. 7
 67. 13
 69. 5
 71. 4
 73. 16
 75. 14
 77. 1
 79. 4
 81. 10
 83. 8
 85. 5
 87. 10
 89. 11

 91. 12
 93. 9
 95. 9
 97. 14
 99. 9
 9
 95. 9
 97. 14
 99. 9

A2: One Hundred Multiplication Facts 1. 1 3. 56 5. 32 7. 28 9. 4 11. 63 13. 6 15. 30 17. 24 19. 18 21. 40 23. 32 25. 54 27. 56 29. 54 31. 2 33. 36 35. 12 37. 36 39. 12 41. 48 43. 8 45. 0 47. 27 49. 15 51. 45 53. 0 55. 81 57. 0 59. 0 61. 18 63. 3 65. 36 67. 63 69. 35 71. 42 73. 40 75. 0 77. 9 79. 15 81. 5 83. 0 85. 21 87. 0 89. 16 91. 0 93. 4 95. 6 97. 18 99. 0

Exercise Set B

1. a. \$640 **b.** 15 hr **3. a.** 1260 beats **b.** 60 sec or 1 min **c.** 90 sec or $1\frac{1}{2}$ min **5. a.** 200 beds **b.** 11,315 **7. a.** 6 c **b.** $13\frac{1}{3}$ c **c.** $22\frac{1}{2}$ c **9.** \$643.50 **11. a.** 262.5 drops **b.** 20 liters **13. a.** 7200 tortillas **b.** 12.5 min **15. a.** \$10.8 million **b.** 4.5 episodes **17. a.** $11\frac{1}{4}$ mi **b.** $\frac{1}{9}$ hr or $6\frac{2}{3}$ min

Practice Final Exam 1. 113 2. 33 3. $\frac{64}{3}$ or $21\frac{1}{3}$ 4. $\frac{3}{2}$ or $1\frac{1}{2}$ 5. 8 6. 43.86 7. 6.2 8. $1\frac{7}{24}$ 9. $\frac{45}{2}$ or $22\frac{1}{2}$ 10. 12,690 11. $\frac{3}{8}$ 12. 52,000 13. 34.9 14. 0.941 15. 0.85 16. 610% 17. 37.5% 18. $\frac{1}{500}$ 19. perimeter: $3\frac{1}{3}$ ft; area: $\frac{2}{3}$ sq ft 20. $\frac{9}{13}$

21. $\frac{3 \text{ in.}}{10 \text{ days}}$ **22.** 81.25 km/hr **23.** 16-oz: \$0.0931/oz; 24-oz: \$0.0996/oz; 16-oz size **24.** $\frac{48}{11}$ or $4\frac{4}{11}$ **25.** 11.4 **26.** $7\frac{5}{6}$ gal **27.** $114\frac{2}{3}$ cartons **28.** \$17 **29.** 1250 **30.** 75% **31.** 38.4 lb **32.** discount: \$18; sale price: \$102 **33.** 2400 g **34.** 10 qt **35.** 16 ft 6 in. **36.** 12° **37.** $m \angle x = 118^\circ$; $m \angle y = 62^\circ$; $m \angle z = 118^\circ$ **38.** 26° **39.** 7.5 or $7\frac{1}{2}$ **40.** mean: 38.4; median: 42; no mode **41.** 11 students **42.** -117 **43.** 12 **44.** 2 **45.** $-\frac{14}{81}$ **46.** -1 **47.** 14z - 8 **48.** 40 **49.** 24 **50.** -2 **51.** 244 women

Solutions to Selected Exercises

Chapter 1

| Chapter I | |
|--|--|
| Exercise Set 1.2 | 21. $^{1}_{62}$ |
| 1. The place value of the 5 in 657 is tens. | 18 |
| 5. The place value of the 5 in 43,526,000 is hundred-thousands. | + 14 |
| 9. 354 is written as three hundred fifty-four. | $\frac{+14}{94}$ |
| 13. 26,990 is written as twenty-six thousand, nine hundred ninety. | 25 111 |
| 17. 24,350,185 is written as twenty-four million, three hundred | 23. 7542 |
| fifty thousand, one hundred eighty-five. | 49 |
| 21. 2717 is written as two thousand, seven hundred seventeen. | + 682 |
| 25. 14,433 is written as fourteen thousand, four hundred | 8273 |
| thirty-three. | 29. $^{2}_{627}$ |
| 29. Six thousand, five hundred eighty-seven in standard form | 627
628 |
| is 6587. | + 629 |
| 33. Thirteen million, six hundred one thousand, eleven in | $\frac{+029}{1884}$ |
| standard form is 13,601,011. | 33. 11 |
| 37. Two hundred sixty thousand, nine hundred ninety-seven in | 507 |
| standard form is 260,997. | 593 |
| 41. Sixteen thousand, seven hundred thirty-two in standard | + 10 |
| form is 16,732. | 1110 |
| 45. One hundred eight thousand in standard form is 108,000. | 37. $^{1122}_{49}$ |
| 49. 3470 = 3000 + 400 + 70 | 628 |
| 53. $66,049 = 60,000 + 6000 + 40 + 9$ | 5 762 |
| 57. 5532 is written as five thousand, five hundred thirty-two. | +29,462 |
| 61. The tallest mountain in New England is Mt. Washington. | 35,901 |
| 65. The number of visitors to the Vatican Museums was | |
| 6,002,000, which is written as six million, two thousand. | 41. ² ₉ |
| 69. The largest number is 9861. | 12 |
| 73. answers may vary | 9 |
| 77. The Pro Football Hall of Fame is located in the town of Canton. | + 12 |
| | 42 |
| Exercise Set 1.3 | The perimeter is 42 inches. |
| 1. 14 | 45. Opposite sides of a rectangle have the same length. |
| $\frac{+22}{26}$ | ²
4 |
| 36 | 4 |
| 5. 12 | 8 |
| 13 | <u>+ 8</u> |
| $\frac{+24}{12}$ | $\frac{10}{24}$ |
| 49 | The perimeter is 24 inches. |
| 9. 53 | 49. $8 + 3 + 5 + 7 + 5 + 1 = 8 + 1 + 3 + 7 + 5 + 5$ |
| $\frac{+64}{117}$ | = 9 + 10 + 10 |
| | = 29 |
| 13. $\begin{array}{c} 1 & 1 & 1 \\ 22,781 \end{array}$ | The perimeter is 29 inches. |
| +186,297 | 52 111 |
| 209,078 | 53. ¹¹¹ / ₂₉₇ |
| 17. $^{2}_{6}$ | + 1796 |
| 0 | 2093
57 "Ingrassed by" indicates addition |
| 21 | 57. "Increased by" indicates addition. |
| 14 | 1
452 |
| 9 | +92 |
| $\frac{+12}{62}$ | 544 |
| 62 | 452 increased by 92 is 544. |
| A28 | |

| 61. $\begin{array}{c}1\\20,148\end{array}$ | 9. 6998 Check: 5545 |
|---|--|
| + 2286 | -1453 $+1453$ |
| 22,434 | 5545 6998 |
| | ······································ |
| The population of Florida is projected to be 22,434 thousand in 2025. | 13. 62 <i>Check:</i> 25 |
| | -37 $+37$ |
| 65. $^{21}_{78}$ | 25 62 |
| 90 | |
| 102 | 17. 938 Check: 146 |
| + 70 | -792 $+792$ |
| 340 | 146 938 |
| He needs 340 feet of wiring. | 21. 600 <i>Check:</i> $11 \\ 168$ |
| 1 1 | |
| 69. 161,839 | $\frac{-432}{169}$ $\frac{+432}{600}$ |
| +100,352 | 168 600 |
| 262,191 | 25. 923 Check: $\begin{array}{c} 11\\ 447\end{array}$ |
| 262,191 Harley-Davidson motorcycles were sold in 2016. | - 476 + 476 |
| 73. The sides of a square are all the same length. 1 | 447 923 |
| 31 | |
| 31 | 29. 533 Check: 504^{-1} |
| 31 | - 29 + 29 |
| + 31 | 504 533 |
| 124 | 1 |
| The perimeter of the board is 124 feet. | 33. 1983 Check: 79 |
| 77. California had the most CVS pharmacies. | -1904 + 1904 |
| 81. Pennsylvania and New York: | 79 1983 |
| 408^{-1} | 1111 |
| + 486 | 37. 50,000 <i>Check:</i> $32,711^{11}$ |
| 894 | -17,289 $+17,289$ |
| Florida and Georgia: | 32,711 50,000 |
| 1 | 11 51 111 Charles 21 212 |
| 756 | 41. 51,111 Check: 31,213 |
| $\frac{+313}{1000}$ | - 19,898 + 19,898 - 51,111 |
| 1069
Elevide and Coercie had more CVS pharmagies | 31,213 51,111 |
| Florida and Georgia had more CVS pharmacies.
85. answers may vary | 45. 41 |
| 1111 121 1 | - 21 |
| 89. 56,468,980 | $\overline{20}$ |
| 1,236,785 | The difference of 41 and 21 is 20. |
| + 986,768,000 | 49. 108 |
| 1,044,473,765 | - 36 |
| 93. ²² 14 | 72 |
| 173 | 108 less 36 is 72. |
| 86 | 53. 503 |
| | - 239 |
| $\frac{+257}{530}$ | |
| The given sum is incorrect; the correct sum is 530. | She has 264 more pages to read. |
| The given sum is mediteer, the correct sum is 550. | 57. 189,000 |
| Exercise Set 1.4 | + 75,000 |
| 1. 67 <i>Check:</i> 44 | 264,000 |
| -23 $+23$ | The total land area drained by the Upper Mississippi and |
| 44 67 | Lower Mississippi sub-basins is 264,000 square miles. |
| | 61. 20,320 |
| 5. 167 <i>Check:</i> 135 | - 14,255 |
| $\frac{-32}{125}$ $\frac{+32}{167}$ | 6065 |
| 135 167 | The peak of Denali is 6065 feet higher than the peak of |
| | Long's Peak. |
| | |

Solutions to Selected Exercises

| 65. | 645 | 9 |
|------|--|----|
| | <u>- 287</u> | |
| | 358 | |
| | The distance between Hays, Kansas, and Denver, | 10 |
| | Colorado, is 358 miles. | 13 |
| 69. | | |
| | <u>- 6927</u> | |
| | 1609 | 17 |
| | The projected increase in the population of Arizona is | 10 |
| | 1609 thousand. | |
| 73. | | |
| | <u>- 30</u> | 21 |
| | 58 | |
| | Snoring is 58 dB louder than normal conversation. | |
| 77. | 100,000 | 25 |
| | <u>- 94,080</u> | |
| | 5920 | |
| | The Dole Plantation maze is 5920 square feet larger than | |
| | the Ruurlo maze. | 29 |
| 81. | | |
| | <u>- 66</u> | |
| | 12 | |
| | Chicago O'Hare International Airport had 12 million | 33 |
| | more passengers than Dallas/Ft. Worth International | |
| | Airport in 2016. | |
| 85. | | |
| | + 48 | |
| | 1034 | 37 |
| 89. | 9000 | |
| | <u> </u> | |
| | 8518 | |
| 93. | In $48 - 1, 48$ is the minuend and 1 is the subtrahend. | 41 |
| 97. | 741 | 41 |
| | <u>- 56</u> | |
| | 685 | |
| | The given answer is incorrect; the correct answer is 685. | 45 |
| 101. | 5269_ | 40 |
| | -2385 | |
| | 2884 | |
| 105. | — | 49 |
| | 369,477 | |
| | 218,287 1,000,000 | |
| | +121,685 - 998,911 | 53 |
| | 998,911 1089 | |
| | No, they have not reached their goal. They have 1089 | |
| | more pages to read. | |
| F | | |
| - | rcise Set 1.5 | 57 |
| 1. | To round 423 to the nearest ten, observe that the digit in
the area place is 2. Since this digit is less than 5 we do | |
| | the ones place is 3. Since this digit is less than 5, we do
not add 1 to the digit in the tans place. The number 423 | |
| | not add 1 to the digit in the tens place. The number 423 rounded to the nearest ten is 420. | |
| 5. | To round 2791 to the nearest hundred, observe that the | 61 |
| | digit in the tens place is 9. Since this digit is 5 or greater, | |
| | we add 1 to the digit in the hundreds place. The number | |
| | 2791 rounded to the nearest hundred is 2800. | |

- **9.** To round 21,094 to the nearest thousand, observe that the digit in the hundreds place is 0. Since this digit is less than 5, we do not add 1 to the digit in the thousands place. The number 21,094 rounded to the nearest thousand is 21,000.
- **13.** To round 328,495 to the nearest hundred, observe that the digit in the tens place is 9. Since this digit is 5 or greater, we add 1 to the digit in the hundreds place. The number 328,495 rounded to the nearest hundred is 328,500.
- **17.** To round 39,994 to the nearest ten, observe that the digit in the ones place is 4. Since this digit is less than 5, we do not add 1 to the digit in the tens place. The number 39,994 rounded to the nearest ten is 39,990.
- **21.** Estimate 5281 to a given place value by rounding it to that place value. 5281 rounded to the tens place is 5280, to the hundreds place is 5300, and to the thousands place is 5000.
- **25.** Estimate 14,876 to a given place value by rounding it to that place value. 14,876 rounded to the tens place is 14,880, to the hundreds place is 14,900, and to the thousands place is 15,000.
- **29.** To round 38,387 to the nearest thousand, observe that the digit in the hundreds place is 3. Since this digit is less than 5, we do not add 1 to the digit in the thousands place. Therefore, 38,387 points rounded to the nearest thousand is 38,000 points.
- **33.** To round 4,155,907 to the nearest hundred-thousand, observe that the digit in the ten-thousands place is 5. Since this digit 5 or greater, add 1 to the digit in the hundred-thousands place. Therefore, \$4,155,907 rounded to the nearest hundred-thousand is \$4,200,000.

| nearest nundred-thousand is \$4,200,000. |
|---|
| 37. 39 rounds to 40 |
| 45 rounds to 50 |
| 22 rounds to 20 |
| ± 17 rounds to ± 20 |
| 130 |
| 41. 1913 rounds to 1900 |
| 1886 rounds to 1900 |
| + 1925 rounds to $+ 1900$ |
| 5700 |
| 45. 3995 rounds to 4000 |
| 2549 rounds to 2500 |
| + 4944 rounds to $+ 4900$ |
| 11,400 |
| 49. $229 + 443 + 606$ is approximately |
| 230 + 440 + 610 = 1280. |
| The answer of 1278 is correct. |
| 53. 899 rounds to 900 |
| 1499 rounds to 1500 |
| + 999 rounds to $+ 1000$ |
| 3400 |
| The total cost is approximately \$3400. |
| 57. 20,320 rounds to 20,000 |
| <u>$-14,410$</u> rounds to <u>$-14,000$</u> |
| 6000 |
| The difference in elevation is approximately 6000 feet. |
| 61. 1,128,030 rounds to 1,128,000 |
| -946,357 rounds to $-946,000$ |

The decrease in enrollment was approximately 182,000 children.

65. \$2110 million is \$2,110,000,000 in standard form. \$2,110,000,000 rounded to the nearest hundred-million is \$2.100.000.000. \$2,110,000,000 rounded to the nearest billion is \$2,000,000,000. 69. 999 rounded to the nearest hundred is 1000. 73. The smallest possible number that rounds to 8600 is 8550. **77.** 54 rounds to 50 17 rounds to 20 50 + 20 + 50 + 20 = 140The perimeter is approximately 140 meters. **Exercise Set 1.6** 1. $1 \cdot 24 = 24$ 5. $8 \cdot 0 \cdot 9 = 0$ 9. $6(3+8) = 6 \cdot 3 + 6 \cdot 8$ **13.** $20(14 + 6) = 20 \cdot 14 + 20 \cdot 6$ 17. 613 × 6 3678 21. 42 1074 × 6 6444 25. 421 \times 58 3 3 6 8 21 050 24,418 29. 780 \times 20 15,600 **33.** (640)(1)(10) = (640)(10) = 640037. 609 × 234 2 4 3 6 18 270 121 800 142,506 41. 589 \times 110 5 8 9 0 58 900 64,790 **45.** $8 \times 100 = 800$ **49.** $7406 \cdot 10 = 74.060$ **53.** $50 \cdot 900 = 45,000$ 57. Area = (length)(width)= (9 meters)(7 meters)= 63 square meters Perimeter = (9 + 7 + 9 + 7) meters = 32 meters **61.** 576 rounds to 600 $\times\,354\,$ rounds to $\,\times\,$ 400 240,000

65. 38×42 is approximately 40×40 , which is 1600. The best estimate is **c**. **69.** $80 \times 11 = (8 \times 10) \times 11$ $= 8 \times (10 \times 11)$ $= 8 \times 110$ = 880**73.** 2240 \times 2 4480 77. 94 \times 35 470 2820 3290 The total cost is \$3290. **81.** Area = (length)(width)= (110 feet)(80 feet)= 8800 square feet The area is 8800 square feet. 85. 94 $\times 62$ 188 5640 5828 There are 5828 pixels on the screen. **89.** 170 $\times 8$ 1360 There are 1360 calories in 8 ounces. 93. There are 60 minutes in one hour, so there are 24×60 minutes in one day. $24 \times 60 \times 1000 = 24 \times 6 \times 10 \times 1000$ $= 144 \times 10.000$ = 1,440,000They produce 1,440,000 tea bags in one day. 97. 134 $\times 16$ 804 1340 2144 **101.** 19 - 4 15 The difference of 19 and 4 is 15. **105. a.** $3 \cdot 5 = 5 + 5 + 5 = 3 + 3 + 3 + 3 + 3$ **b.** answers may vary **109.** $42 \times 3 = 126$ $42 \times 90 = 3780$ The problem is 42×93 . **113.** On a side with 7 windows per row, there are $7 \times 23 = 161$ windows. On a side with 4 windows per row, there are $4 \times 23 = 92$ windows. 161 + 161 + 92 + 92 = 506

There are 506 windows on the building.

Exercise Set 1.7

Solutions to Selected Exercises

Solutions to Selected Exercises

| Exercise Set 1.7 |
|--|
| 1. $54 \div 9 = 6$ because $6 \cdot 9 = 54$
5. $0 \div 8 = 0$ because $0 \cdot 8 = 0$ |
| 9. $\frac{18}{18} = 1$ because $1 \cdot 18 = 18$ |
| 13. $26 \div 0$ is undefined. |
| 17. $0 \div 14 = 0$ because $0 \cdot 14 = 0$ |
| |
| 21. $\frac{29}{3)87}$ |
| - 6 |
| $-\frac{0}{27}$ |
| $\frac{-6}{27}$ $\frac{-27}{0}$ |
| $\frac{27}{0}$ |
| Check: $3 \cdot 29 = 87$ |
| |
| 25. <u>338</u>
<u>3)1014</u> |
| |
| $\frac{-9}{11}$ |
| |
| $\frac{-9}{24}$ |
| |
| $\frac{-24}{0}$ |
| Check: $3 \cdot 338 = 1014$ |
| 29. 9 |
| 7)63 |
| |
| $\frac{-63}{0}$ |
| Check: $7 \cdot 9 = 63$ |
| 33. 68 R 3 |
| 7)479 |
| |
| $\frac{-42}{59}$ |
| <u>-56</u> |
| $\frac{3}{3}$ |
| Check: $7 \cdot 68 + 3 = 479$ |
| 37. 38 R 1 |
| 8) <u>305</u> |
| -24 |
| 65 |
| -64 |
| 1 |
| Check: $8 \cdot 38 + 1 = 305$ |
| 41. <u>13</u> <u>55)715</u> |
| -55 |
| <u> 165 </u> |
| -165 |
| $\frac{100}{0}$ |
| Check: $55 \cdot 13 = 715$ |
| 45. 97 R 8 |
| 97)9417 |
| -873 |
| 687 |
| -679 |
| <u></u> |
| Check: $97 \cdot 97 + 8 = 9417$ |
| |

49. 506 13)6578 <u>-65</u> 07 $\underline{-0}$ 78 -780 Check: $13 \cdot 506 = 6578$ 53. 54 236)12744 -1180 944 <u>-94</u>4 0 Check: $236 \cdot 54 = 12,744$ 202 R 15 57. 102)20619 <u>-2</u>04 21 -0219 <u>-2</u>04 15 Check: $102 \cdot 202 + 15 = 20,619$ 17 61. 7)119 __7 49 -49 0 2132 R 32 65. 40)85312 -80 53 -40131 -120112 -8032 23 R 2 5)117 69. -1017 <u>-15</u> 2 The quotient of 117 and 5 is 23 R 2. **73.** 20 R 23)62 -6 02 $\underline{-0}$ 2

The quotient of 62 and 3 is 20 R 2.

| 77. | <u>165</u>
318)52470 |
|-----|-------------------------|
| | -318 |
| | 2067 |
| | -1908 |
| | 1590 |
| | -1590 |
| | 0 |

The person weighs 165 pounds on Earth.

81. $\frac{88}{3)265}$ R 1 $\frac{-24}{25}$

 $\frac{25}{-24}$

There are 88 bridges every 3 miles over the 265 miles, plus the first bridge for a total of 89 bridges.

| 85. | 5 |
|-----|------------|
| | 5280)26400 |
| | -26400 |
| | 0 |

Broad Peak is 5 miles tall.

| | Broad Peak is 5 | miles tall. | |
|------|--------------------------|---------------------------------------|---------------------------|
| 89. | $\frac{2}{10}$ | | $6\overline{)120}$ |
| | | | 6)120 |
| | 24 | | $\frac{-12}{0}$ |
| | 35 | | 0 |
| | 22 | | |
| | 17 | | |
| | + 12 | | |
| | 120 | | |
| | Average $=\frac{120}{6}$ | = 20 | |
| 93. | ²
86 | | 79
5)395 |
| | 79 | | |
| | 81 | | $\frac{-35}{45}$ |
| | 69 | | $\frac{-45}{0}$ |
| | + 80 | | 0 |
| | 395 | | |
| | Average $=\frac{395}{5}$ | = 79 | |
| 97. | ^{1 1 1}
82 | | |
| | 463 | | |
| | 29 | | |
| | +8704 | | |
| | 9278 | | |
| 101. | 722 | | |
| | $\frac{-43}{679}$ | | |
| | | | |
| 105. | 9 R 12
24)228 | | |
| | <u>-216</u> | | |
| | 12 | | |
| 109. | 200 divided by 2 | $0 \text{ is } 200 \div 20, \text{w}$ | hich is choice b . |

113. The average will increase; answers may vary.

```
117. Since Area = length \cdot width, length = \frac{\text{Area}}{\text{width}}.
      length = \frac{60 \text{ square feet}}{5 \text{ feet}} = \frac{60}{5} \text{ feet} = 12 \text{ feet}
      The length is 12 feet.
121. 26
       - 5
         21
       - 5
         16
       - 5
         11
       - 5
          6
       - 5
          1
      Thus 26 \div 5 = 5 \text{ R} 1.
Exercise Set 1.8
   1. 41 increased by 8 is what number
        ↓
                   Ţ
                               ↓
                                   ↓
                                               \downarrow
      41
                   +
                               8 = what number
       41
     + 8
       49
```

41 increased by 8 is 49. 5. The total of 35 and 7 is what number $\downarrow \qquad \downarrow \qquad \downarrow \qquad \downarrow \qquad \downarrow \qquad \downarrow$ 35 + 7 = what number 35 $\frac{+7}{42}$

The total of 35 and 7 is 42.

| 9. a | . Perimeter | is | side | + | side | + | side | + | side |
|------|----------------------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|
| | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| | Perimeter | = | 120 | + | 80 | + | 120 | + | 80 |
| | = 400 | | | | | | | | |
| | The perimeter is 400 feet. | | | | | | | | |
| b | . Area is | leng | gth ti | imes | widt | h | | | |

 $\downarrow \qquad \downarrow \qquad \downarrow \qquad \downarrow \qquad \downarrow \qquad \downarrow$ Area = 120 × 80 120 × 80 9600 The area is 9600 square feet.

13. Hours per week is hours per day times days per week

| | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
|--------------------------------|--------------|--------------|--------------|--------------|--------------|
| Hour | s per we | eek = | 24 | × | 7 |
| 24 | | | | | |
| \times 7 | | | | | |
| 168 | | | | | |
| There are 168 hours in a week. | | | | | |

Solution

Solutions to Selected Exercises

| 17. | Difference \downarrow First State
in years \downarrow National minus
Monument \downarrow \downarrow \downarrow \downarrow \downarrow
Difference = 2013 - | Yellowstone
National Park
↓
1872 |
|--------------------------|--|---|
| 21. | 2013
$\frac{-1872}{141}$ Yellowstone National Park is 141 yea
State National Monument.
Total is number of
Fairview plus number
$\downarrow \qquad \downarrow \qquad \downarrow \qquad \downarrow \qquad \downarrow \qquad \downarrow \qquad \downarrow$ Total = 287 + 252
= 287 + 252 + 180 = 719 | of number of |
| 25. | There are a total of 719 towns named
Riverside.
Calories in 1 ounce is calories produced by $\downarrow \qquad \downarrow \qquad \downarrow$ | l Fairview, Midway, or
er ounces
↓ ↓
÷ 3 |
| 29. | $55 = 3)\overline{165}$ $-15 = 15$ $15 = -15 = 0$ There are 55 calories in 1 ounce of calories in | nned tuna.
1 number of months
↓
12 |
| | $ \begin{array}{r} 268,300 \\ \times 12 \\ \overline{536\ 600} \\ \underline{2683\ 000} \\ 3,219,600 \end{array} $ | |
| 33. | The number of visitors in one year w
Northern length is Southern lengt
$\downarrow \qquad \downarrow \qquad \downarrow$
Length = 1933
= 1933 + 2054 =
The northern boundary of the conter | h plus 2054
$\downarrow \qquad \downarrow$
+ 2054
3987 |
| 37. | is 3987 miles long. | |
| Tot
$\cos \downarrow$ | si sweaters sweater | $\begin{array}{c} \text{imber of} & \text{cost of} \\ \text{shirts} & \text{shirt} \\ \downarrow & \downarrow & \downarrow \\ \hline \end{array}$ |

| cost | | sweaters | | sweater | 1 | shirts | | shirt |
|--------------|--------------|------------------|--------------|--------------|--------------|--------------|--------------|--------------|
| \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| Total | = | 3 | • | 38 | + | 5 | • | 25 |
| | = | $3 \cdot 38 + 5$ | •25 = | 114 + 1 | 25 = | 239 | | |
| т | he | total cost i | is \$230 |) | | | | |

ne total cost is \$239.

- 41. Option a: a hamburger, onion rings, a candy bar, and a soda cost 4 + 3 + 2 + 1 = 10. Option b: a hot dog, an apple, french fries, and a soda cost 3 + 1 + 2 + 1 = 7.Thus option b is cheaper by 10 - 7, or 3.
- 45. The region with the most Internet users (Asia) had 1874 million users. The region with the fewest Internet users (Oceania/Australia) had 28 million users.

```
28
—
 1846
```

49. +

Asia had 1846 million more users than Oceania/Australia.

| 1874 | 951 |
|------|--------|
| + 28 | 2)1902 |
| 1902 | -18 |
| | 10 |
| | -10 |
| | 02 |
| | - 2 |
| | 0 |

The average number of Internet users per region in these two world regions was 951 million.

- **53.** There are 7 days in a week. $7 \cdot 2400 = 16,800$ No more than 16,800 milligrams of sodium should be
- consumed in one week. **57.** 4,893,000,000 rounds to 5,000,000,000.

49,906,000,000 rounds to 50,000,000,000.

The average revenue generated by each package was \$10.

Exercise Set 1.9

1. $4 \cdot 4 \cdot 4 = 4^3$ 5. $12 \cdot 12 \cdot 12 = 12^3$ 9. $9 \cdot 8 \cdot 8 = 9 \cdot 8^2$ **13.** $3 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 5 \cdot 5 \cdot 5 \cdot 5 \cdot 5 = 3 \cdot 2^4 \cdot 5^5$ **17.** $5^3 = 5 \cdot 5 \cdot 5 = 125$ **25.** $2^7 = 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 = 128$ **29.** $4^4 = 4 \cdot 4 \cdot 4 \cdot 4 = 256$ **33.** $12^2 = 12 \cdot 12 = 144$ **37.** $20^1 = 20$ **41.** $3 \cdot 2^6 = 3 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 = 192$ **45.** $\sqrt{9} = 3$ since $3 \cdot 3 = 9$ **49.** $\sqrt{144} = 12$ since $12 \cdot 12 = 144$ **53.** $15 + 3 \cdot 2 = 15 + 6 = 21$

A34

57.
$$32 \div 4 - 3 = 8 - 3 = 5$$

61. $6 \cdot 5 + 8 \cdot 2 = 30 + 16 = 46$
65. $(7 + 5^2) \div 4 \cdot 2^3 = (7 + 25) \div 4 \cdot 2^3$
 $= 32 \div 4 \cdot 8$
 $= 8 \cdot 8$
 $= 64$
69. $\frac{18 + 6}{2^4 - 2^2} = \frac{24}{16 - 4} = \frac{24}{12} = 2$
73. $\frac{7(9 - 6) + 3}{3^2 - 3} = \frac{7(3) + 3}{9 - 3} = \frac{21 + 3}{6} = \frac{24}{6} = 4$
77. $2^4 \cdot 4 - (25 \div 5) = 2^4 \cdot 4 - 5$
 $= 16 \cdot 4 - 5$
 $= 64 - 5$
 $= 59$
81. $(7 \cdot 5) + [9 \div (3 \div 3)] = (7 \cdot 5) + [9 \div (1)]$
 $= 35 + 9$
 $= 44$
85. $\frac{9^2 + 2^2 - 1^2}{8 \div 2 \cdot 3 \cdot 1 \div 3} = \frac{81 + 4 - 1}{4 \cdot 3 \cdot 1 \div 3}$
 $= \frac{85 - 1}{12 \cdot 1 \div 3}$
 $= \frac{84}{4}$
89. $4 \cdot \sqrt{49} - 0 \div \sqrt{100} = 4 \cdot 7 - 0 \div 10$
 $= 28 - 0$
 $= 28$
93. $\sqrt{81} \div \sqrt{9} + 4^2 \cdot 2 - 10 = 9 \div 3 + 16 \cdot 2 - 10$
 $= 35 - 10$
 $= 25$
97. $7^2 - \{18 - [40 \div (4 \cdot 2) + \sqrt{4}] + 5^2\}$
 $= 7^2 - \{18 - [40 \div 8 + \sqrt{4}] + 5^2\}$
 $= 7^2 - \{18 - [40 \div 8 + \sqrt{4}] + 5^2\}$
 $= 7^2 - \{18 - [40 \div 8 + \sqrt{4}] + 5^2\}$
 $= 7^2 - \{18 - [40 \div 8 + \sqrt{4}] + 5^2\}$
 $= 7^2 - \{18 - [40 \div 8 + 2] + 5^2\}$
 $= 7^2 - \{18 - [40 \div 8 + 2] + 5^2\}$
 $= 7^2 - \{18 - [40 \div 8 + 2] + 5^2\}$
 $= 7^2 - \{18 - 7 + 25\}$
 $= 7^2 - \{18 - 7 + 25\}$
 $= 7^2 - \{18 - 7 + 25\}$
 $= 7^2 - \{18 - 7 + 25\}$
 $= 7^2 - [11 + 25]$
 $= 7^2 - 36$
 $= 49 - 36$
 $= 13$
101. Area of a square $= (side)^2$
 $= (23 miles)^2$
 $= 529 square miles$
Perimeter $= (23 + 23 + 23 + 23)$ miles
 $= 92$ miles

105.
$$2^5 = 2 \cdot 2 \cdot 2 \cdot 2$$

The statement is false.
109. $24 \div (3 \cdot 2) + 2 \cdot 5 = 24 \div 6 + 2 \cdot 5 = 4 + 10 = 14$
113. $(7 + 2^4)^5 - (3^5 - 2^4)^2 = (7 + 16)^5 - (243 - 16)^2$
 $= 23^5 - 227^2$
 $= 6,436,343 - 51,529$
 $= 6,384,814$

Chapter 1 Test

1. 82,426 is written as eighty-two thousand, four hundred twenty-six.

5. 496

$$\frac{\times 30}{14,880}$$
9. $0 \div 49 = 0$
13. $\frac{64 \div 8 \cdot 2}{(\sqrt{9} - \sqrt{4})^2 + 1} = \frac{8 \cdot 2}{(3 - 2)^2 + 1}$

$$= \frac{16}{1^2 + 1}$$

$$= \frac{16}{1 + 1}$$

$$= \frac{16}{2}$$

$$= 8$$

- **17.** To round 52,369 to the nearest thousand, observe that the digit in the hundreds place is 3. Since this digit is less than 5, we do not add 1 to the digit in the thousands place. The number 52,369 rounded to the nearest thousand is 52,000.
- **21.** ¹₁₅
 - +107
 - 122

The sum of 15 and 107 is 122.

- **25.** 725
 - -599
 - 126

The more expensive refrigerator costs \$126 more than the less expensive one.

- **29.** Perimeter = 20 yards + 20 yards + 10 yards + 10 yards = 60 yards
 - The perimeter is 60 yards.
 - Area = $(length) \cdot (width)$
 - = $(20 \text{ yards}) \cdot (10 \text{ yards})$
 - = 200 square yards
 - The area is 200 square yards.

Chapter 2

| | Chapter 2 | | | | |
|--|--|--|--|--|--|
| | Exercise Set 2.1 | | | | |
| | 1. In the fraction $\frac{1}{2}$, the numerator is 1 and the denominator | | | | |
| ses | is 2. Since 1 is less than 2, the fraction is proper. | | | | |
| Ü | 5. In the fraction $\frac{15}{15}$, the numerator is 15 and the denomina- | | | | |
| Xel | tor is 15. Since 15 is greater than or equal to 15, the frac- | | | | |
| ш | tion is improper. | | | | |
| tte | 9. $\frac{5}{0}$ is undefined. 13. $\frac{0}{20} = 0$ 17. $\frac{16}{1} = 16$ | | | | |
| Solutions to Selected Exercises | 21. | 7 of the 12 equal parts are shaded: $\frac{7}{12}$ | | | |
| to
V | 25. 4 of the 9 equal parts are shaded: $\frac{4}{9}$ | | | | |
| suc | | 5 of the 8 equal parts are shaded: $\frac{5}{8}$ | | | |
| uti | 33. | | | | |
| | | | | | |
| • | | | | | |
| | | × × | | | |
| | 37. | | | | |
| | 41. a. $131 - 42 = 89$ | | | | |
| | 89 students are not freshmen. | | | | |
| | b. $\frac{89}{131}$ of the students are not freshmen. | | | | |
| | 45. $\frac{10}{19}$ of the named tropical storms turned into hurricanes | | | | |
| | 19
2012. | | | | |
| | 10 | | | | |
| | 49. $\frac{10}{31}$ of the class is sophomores. | | | | |
| | 53. a. $\frac{21}{50}$ of the marbles are blue | | | | |
| | b. $50 - 21 = 29$
29 marbles are red. | | | | |
| | | | | | |
| | | c. $\frac{29}{50}$ of the marbles are red. | | | |
| | 57. Each part is $\frac{1}{6}$ of a whole and there are 23 parts shaded, or | | | | |
| | 3 wholes and 5 more parts. | | | | |
| | | a. $\frac{23}{6}$ | | | |
| | | b. $3\frac{5}{6}$ | | | |
| | 6
61. Each part is $\frac{1}{2}$ of a whole and there are 11 parts shaded, o | | | | |
| | | 5 wholes and 1 more part. | | | |
| | | a. $\frac{11}{2}$ | | | |
| | | | | | |
| | | b. $5\frac{1}{2}$ | | | |
| | 65. | $3\frac{3}{5} = \frac{5 \cdot 3 + 3}{5} = \frac{15 + 3}{5} = \frac{18}{5}$ | | | |
| | | $2\frac{11}{15} = \frac{15 \cdot 2 + 11}{15} = \frac{30 + 11}{15} = \frac{41}{15}$ | | | |
| | 07. | 215 15 15 15 15 15 | | | |

| (10 ()) | | | | | |
|--|--|--|--|--|--|
| 73. $6\frac{6}{13} = \frac{13 \cdot 6 + 6}{13}$ | $\frac{7}{2} = \frac{78+6}{12} = \frac{84}{12}$ | | | | |
| 15 15 | 15 15 | | | | |
| 77. $17\frac{7}{12} = \frac{12}{12}$ | $\frac{7}{12} = \frac{204+7}{12} = \frac{211}{12}$ | | | | |
| 51 107·2 + | - 51 214 + 51 265 | | | | |
| 81. $2{107} = {107}$ | $\frac{-51}{-51} = \frac{214 + 51}{107} = \frac{265}{107}$ | | | | |
| 3 R 2 | 3 R 2 | | | | |
| 85. 5)17 | 89. 15)47 | | | | |
| $-\frac{15}{2}$ | $-\frac{45}{2}$ | | | | |
| 17 _ 2 | 47 2 | | | | |
| $\frac{17}{5} = 3\frac{2}{5}$ | $\frac{47}{15} = 3\frac{2}{15}$ | | | | |
| 33 | 66 R 2 | | | | |
| 93. 6)198 | 97. 3)200 | | | | |
| $-\frac{18}{18}$ | $-\frac{18}{20}$ | | | | |
| | 20
-18 | | | | |
| $-\frac{18}{0}$ | $-\frac{18}{2}$ | | | | |
| $\frac{198}{6} = 33$ | $\frac{200}{3} = 66\frac{2}{3}$ | | | | |
| $\frac{-6}{6} = 33$ | $\frac{-3}{3} = \frac{-30}{3}$ | | | | |
| 17 R 13 | 6 R 65 | | | | |
| 101. 18)319 | 105. 112)737 | | | | |
| $-\frac{18}{139}$ | $-\frac{672}{65}$ | | | | |
| -126 | 737 65 | | | | |
| 13 | $\frac{737}{112} = 6\frac{65}{112}$ | | | | |
| $\frac{319}{18} = 17\frac{13}{18}$ | | | | | |
| $18 	 18 	 18 	 109. 	 5^3 = 5 \cdot 5 \cdot 5 = 12$ | 25 113. $2 \cdot 2 \cdot 2 \cdot 3 = 2^3 \cdot 3$ | | | | |
| $109. 5^{\circ} = 5 \cdot 5 \cdot 5 = 125 $ 113. $2 \cdot 2 \cdot 2 \cdot 5 = 2^{\circ} \cdot 5$ | | | | | |
| 11/. | | | | | |
| | | | | | |
| | | | | | |
| $\frac{2}{3}$ is larger than $\frac{1}{2}$. | | | | | |
| $J \qquad \Sigma$ | | | | | |
| 121. $15,200 + 107,400 + 20,000 + 12,400 = 155,000$ | | | | | |
| $\frac{20,000}{155,000}$ of the employees work in the North American | | | | | |
| region. | | | | | |
| Exercise Set 2.2 | | | | | |
| 1. $1 \cdot 8 = 8$ | | | | | |
| $2 \cdot 4 = 8$ | | | | | |
| The factors of 8 are 1, 2, 4, and 8.
5 $1 \cdot 4 = 4$ | | | | | |
| 5. $1 \cdot 4 = 4$
$2 \cdot 2 = 4$ | | | | | |
| The factors of 4 are $1, 2, and 4$. | | | | | |
| 9. $1 \cdot 29 = 29$ | | | | | |
| The factors of 29 are 1 and 29. | | | | | |
| 13. $1 \cdot 12 = 12$ | | | | | |
| $2 \cdot 6 = 12$ | | | | | |
| $3 \cdot 4 = 12$ | | | | | |
| The factors of 12 a
17 7 is prime as its ou | rre 1, 2, 3, 4, 6, and 12. | | | | |

- **17.** 7 is prime, as its only factors are 1 and 7.
- **21.** 23 is prime, since its only factors are 1 and 23.

25

- 29. 31 is prime, since its only factors are 1 and 31. **33.** 119 is composite, since its factors are 1, 7, 17,
- and 119.

| $ \begin{array}{r} 5 \\ 37. \ 3)\overline{15} \\ 15 = 3 \cdot 5 \end{array} $ | 41. $3\overline{)9}$
2)18
2)36
$36 = 2^2 \cdot 3^2$ |
|--|--|
| 45. $3\overline{)15}$
$2\overline{)30}$
$2\overline{)60}$ | 49. $5\overline{)85}$
$85 = 5 \cdot 17$ |
| $60 = 2^{2} \cdot 3 \cdot 5$ 11 53. 7) 77 2)154 154 = 2 \cdot 7 \cdot 11 | 57. $3\overline{)15}$
$2\overline{)30}$
$2\overline{)60}$
$2\overline{)120}$
$2\overline{)240}$
$240 = 2^4 \cdot 3 \cdot 5$ |
| 61. $7)$ $\overline{49}$
$3)\overline{147}$
$3)\overline{441}$
$2)\overline{882}$
$882 = 2 \cdot 3^2 \cdot 7^2$ | 65. $3\overline{)33}$
$33 = 3 \cdot 11$ |

- 69. 67 is prime, since its only factors are 1 and 67.
- 73. 97 is prime, since its only factors are 1 and 97.
- 77. To round 4267 to the nearest hundred, observe that the digit in the tens place is 6. Since this digit is 5 or greater, we add 1 to the digit in the hundreds place. The number 4267 rounded to the nearest hundred is 4300.
- 81. To round 19,764 to the nearest thousand, observe that the digit in the hundreds place is 7. Since this digit is 5 or greater, we add 1 to the digit in the thousands place. The number 19,764 rounded to the nearest thousand is 20,000.
- **85.** 2003 + 1938 + 2102 = 6043

There were a total of 6043 patents granted for the years shown.

 $\frac{2003}{6043}$ of the patents were granted in 2014.

89. answers may vary

Exercise Set 2.3

1.
$$\frac{3}{12} = \frac{3}{3 \cdot 4} = \frac{1 \cdot 3}{4 \cdot 3} = \frac{1}{4}$$

5. $\frac{14}{16} = \frac{2 \cdot 7}{2 \cdot 8} = \frac{7}{8}$
9. $\frac{35}{50} = \frac{5 \cdot 7}{5 \cdot 10} = \frac{7}{10}$
13. $\frac{24}{40} = \frac{8 \cdot 3}{8 \cdot 5} = \frac{3}{5}$

17.
$$\frac{25}{40} = \frac{5 \cdot 5}{5 \cdot 8} = \frac{5}{8}$$

21. $\frac{56}{68} = \frac{4 \cdot 14}{4 \cdot 17} = \frac{14}{17}$
25. $\frac{90}{120} = \frac{30 \cdot 3}{30 \cdot 4} = \frac{3}{4}$
29. $\frac{66}{308} = \frac{22 \cdot 3}{22 \cdot 14} = \frac{3}{14}$
33. $\frac{75}{350} = \frac{25 \cdot 3}{25 \cdot 14} = \frac{3}{14}$
37. $\frac{288}{480} = \frac{96 \cdot 3}{96 \cdot 5} = \frac{3}{5}$
41. Equivalent, since the cross products are equal: $6 \cdot 4 = 24$ and $8 \cdot 3 = 24$
45. Equivalent, since the cross products are equal: $15 \cdot 6 = 90$ and $9 \cdot 10 = 90$
49. Not equivalent, since the cross products are not equal: $13 \cdot 12 = 156$ and $15 \cdot 10 = 150$
53. $\frac{2 \text{ hours}}{8 \text{ hours}} = \frac{2 \cdot 1}{2 \cdot 4} = \frac{1}{4}$
2 hours represents $\frac{1}{4}$ of a work shift.
57. a. $\frac{10 \text{ monuments}}{78 \text{ monuments}} = \frac{2 \cdot 5}{2 \cdot 39} = \frac{5}{39}$
 $\frac{5}{39}$ of the national monuments are in New Mexico.
b. $78 - 10 = 68$
 $68 \text{ of the national monuments are outside New Mexico.}$
61. a. $50 - 33 = 17$
17 states do not have an Albertsons Companies Inc. store
b. $\frac{17 \text{ states}}{50 \text{ states}} = \frac{17}{50}$
 $\frac{17}{50}$ of the states do not have an Albertsons Companies Inc. store
65. 91
 $\frac{91}{364}$
 $\frac{2 \cdot 35}{360}$

store.

Inc.

2160 2520

73. $\frac{3975}{6625} = \frac{3 \cdot 1325}{5 \cdot 1325} = \frac{3}{5}$

77. 3 + 1 = 4 blood donors have an AB blood type.

$$\frac{4 \text{ donors}}{100 \text{ donors}} = \frac{4 \cdot 1}{4 \cdot 25} = \frac{1}{25}$$

 $\frac{1}{25}$ of blood donors have an AB blood type.

- 81. answers may vary
- 85. answers may vary
- 89. The numbers are also divisible by 6; answers may vary

Exercise Set 2.4 1. $\frac{1}{3} \cdot \frac{2}{5} = \frac{1 \cdot 2}{3 \cdot 5} = \frac{2}{15}$ 1. $\frac{1}{3} \cdot \frac{1}{5} = \frac{1}{3 \cdot 5} = \frac{1}{15}$ 5. $\frac{3}{10} \cdot \frac{3}{8} = \frac{3 \cdot 3}{10 \cdot 8} = \frac{9}{80}$ 9. $\frac{16}{5} \cdot \frac{3}{4} = \frac{16 \cdot 3}{5 \cdot 4} = \frac{4 \cdot 4 \cdot 3}{5 \cdot 4} = \frac{4 \cdot 3}{5} = \frac{12}{5} \text{ or } 2\frac{2}{5}$ 13. $0 \cdot \frac{8}{9} = 0$ 17. $\frac{18}{20} \cdot \frac{36}{99} = \frac{18 \cdot 36}{20 \cdot 99} = \frac{9 \cdot 2 \cdot 4 \cdot 9}{4 \cdot 5 \cdot 9 \cdot 11} = \frac{2 \cdot 9}{5 \cdot 11} = \frac{18}{55}$ 21. $\frac{11}{20} \cdot \frac{1}{7} \cdot \frac{5}{22} = \frac{11 \cdot 1 \cdot 5}{20 \cdot 7 \cdot 22}$ $= \frac{11 \cdot 1 \cdot 5}{5 \cdot 4 \cdot 7 \cdot 11 \cdot 2}$ $= \frac{1}{4 \cdot 7 \cdot 2}$ $= \frac{1}{56}$ 25. $\frac{9}{20} \cdot 0 \cdot \frac{4}{19} = 0$ 29. $7\frac{7}{7}$ rounds to 8 **29.** $7\frac{7}{8}$ rounds to 8. **33.** $19\frac{11}{20}$ rounds to 20. **37.** $\frac{5}{8} \cdot 4 = \frac{5}{8} \cdot \frac{4}{1} = \frac{5 \cdot 4}{8 \cdot 1} = \frac{5 \cdot 4}{2 \cdot 4 \cdot 1} = \frac{5}{2} \text{ or } 2\frac{1}{2}$ **41.** $\frac{2}{5} \cdot 4\frac{1}{6} = \frac{2}{5} \cdot \frac{25}{6} = \frac{2 \cdot 25}{5 \cdot 6} = \frac{2 \cdot 5 \cdot 5}{5 \cdot 2 \cdot 3} = \frac{5}{3} \text{ or } 1\frac{2}{3}$ **45.** Exact: $2\frac{1}{5} \cdot 3\frac{1}{2} = \frac{11}{5} \cdot \frac{7}{2} = \frac{11 \cdot 7}{5 \cdot 2} = \frac{77}{10} \text{ or } 7\frac{7}{10}$ Estimate: $2\frac{1}{5}$ rounds to $2, 3\frac{1}{2}$ rounds to $4.2 \cdot 4 = 8$, so the **49.** $5 \cdot 2\frac{1}{2} = \frac{5}{1} \cdot \frac{5}{2} = \frac{5 \cdot 5}{1 \cdot 2} = \frac{25}{2}$ or $12\frac{1}{2}$ **53.** $\frac{3}{4} \cdot 16 \cdot \frac{1}{2} = \frac{3}{4} \cdot \frac{16}{1} \cdot \frac{1}{2}$ $= \frac{3 \cdot 16 \cdot 1}{4 \cdot 1 \cdot 2}$ $= \frac{3 \cdot 2 \cdot 2 \cdot 4 \cdot 1}{4 \cdot 1 \cdot 2}$ $= \frac{3 \cdot 2}{1}$ = 6 **57.** $3\frac{1}{2} \cdot 1\frac{3}{4} \cdot 2\frac{2}{3} = \frac{7}{2} \cdot \frac{7}{4} \cdot \frac{8}{3}$ $= \frac{7 \cdot 7 \cdot 8}{2 \cdot 4 \cdot 3}$ $= \frac{7 \cdot 7 \cdot 2 \cdot 4}{2 \cdot 4 \cdot 3}$ $=\frac{7\cdot7}{3}$ $=\frac{49}{3}$ or $16\frac{1}{3}$ **61.** $\frac{19}{37} \cdot 0 = 0$

65.
$$\frac{3}{2} \cdot \frac{7}{3} = \frac{3 \cdot 7}{2 \cdot 3} = \frac{7}{2} \text{ or } 3\frac{1}{2}$$

69. $\frac{7}{72} \cdot \frac{9}{49} = \frac{7 \cdot 9}{72 \cdot 49} = \frac{7 \cdot 9}{8 \cdot 9 \cdot 7 \cdot 7} = \frac{1}{8 \cdot 7} = \frac{1}{56}$
73. $9\frac{5}{7} \cdot 8\frac{1}{5} \cdot 0 = 0$
77. $\frac{1}{4} \text{ of } 200 = \frac{1}{4} \cdot 200$
 $= \frac{1}{4} \cdot \frac{200}{1}$
 $= \frac{1 \cdot 200}{4 \cdot 1}$
 $= \frac{1 \cdot 4 \cdot 50}{4 \cdot 1}$
 $= \frac{50}{1}$
 $= 50$
81. $\frac{4}{25} \text{ of } 800 = \frac{4}{25} \cdot 800$
 $= \frac{4 \cdot 800}{25 \cdot 1}$
 $= \frac{4 \cdot 25 \cdot 32}{25 \cdot 1}$
 $= \frac{4 \cdot 32}{1}$
 $= 128$

128 of the students would be expected to major in business.

85.
$$\frac{2}{5}$$
 of 2170 = $\frac{2}{5} \cdot 2170$
= $\frac{2}{5} \cdot \frac{2170}{1}$
= $\frac{2 \cdot 2170}{5 \cdot 1}$
= $\frac{2 \cdot 5 \cdot 434}{5 \cdot 1}$
= $\frac{2 \cdot 434}{1}$
= 868

He has hiked 868 miles of the trail.

89.
$$\frac{5}{6}$$
 of $36 = \frac{5}{6} \cdot 36$
 $= \frac{5}{6} \cdot \frac{36}{1}$
 $= \frac{5 \cdot 36}{6 \cdot 1}$
 $= \frac{5 \cdot 6 \cdot 6}{6 \cdot 1}$
 $= \frac{5 \cdot 6}{1}$
 $= 30$

There are normally 30 gallons of solution in the vat.

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93.
$$6 \cdot 3\frac{1}{4} = \frac{6}{1} \cdot \frac{13}{4} = \frac{6 \cdot 13}{1 \cdot 4} = \frac{2 \cdot 3 \cdot 13}{1 \cdot 2 \cdot 2} = \frac{3 \cdot 13}{1 \cdot 2} = \frac{39}{2} \text{ or } 19\frac{1}{2}$$

The sidewalk is $\frac{39}{2}$ inches or $19\frac{1}{2}$ inches wide.
97. Area = length · width $= \frac{5}{14} \cdot \frac{1}{5} = \frac{5 \cdot 1}{14 \cdot 5} = \frac{1}{14}$
The area is $\frac{1}{14}$ square foot.
101. $\frac{8}{25} \cdot 12,000 = \frac{8}{25} \cdot \frac{12,000}{25 \cdot 1}$
 $= \frac{8 \cdot 12,000}{25 \cdot 1}$
 $= \frac{8 \cdot 25 \cdot 480}{25 \cdot 1}$
 $= \frac{8 \cdot 480}{1}$
 $= 3840$
The family drove 3840 miles for work.
206
105. $80\frac{1648}{1648}$
 $\frac{-16}{04}$
 $\frac{-0}{48}$
 $\frac{-48}{0}$
109. answers may vary
113. $3\frac{1}{5}$ rounds to 3
 $4\frac{5}{8}$ rounds to 5
 $3 \cdot 5 = 15$
The best estimate is b.
117. If $\frac{2}{3}$ of the students on the second bus are boys, then $\frac{1}{3}$ of the students on that bus are girls.
 $\frac{3}{4} \text{ of } 36 = \frac{3}{4} \cdot 36$
 $= \frac{3}{4} \cdot \frac{36}{1}$
 $= \frac{3 \cdot 4.9}{4 \cdot 1}$
 $= \frac{3 \cdot 9}{1}$
27 students on the first bus are girls.
 $\frac{1}{3}$ of $30 = \frac{1}{3} \cdot 30 = \frac{1}{3} \cdot \frac{30}{1} = \frac{1 \cdot 3 \cdot 10}{3 \cdot 1} = 10$
10 students on the two buses.
Exercise Set 2.5
1. The reciprocal of $\frac{4}{7}$ is $\frac{7}{4}$.
5. The reciprocal of $15 = \frac{15}{1}$ is $\frac{1}{15}$.

9.
$$\frac{2}{3} \div \frac{5}{6} = \frac{2}{3} \cdot \frac{6}{5} = \frac{2 \cdot 6}{3 \cdot 5} = \frac{2 \cdot 3 \cdot 2}{3 \cdot 5} = \frac{2 \cdot 2}{5} = \frac{4}{5}$$

13. $\frac{7}{7} \div \frac{5}{6} = \frac{3}{7} \cdot \frac{6}{5} = \frac{3 \cdot 6}{7 \cdot 5} = \frac{18}{35}$
17. $\frac{1}{10} \div \frac{10}{11} = \frac{1}{10} \cdot \frac{10}{10} = \frac{1 \cdot 10}{100} = \frac{1}{100}$
21. $\frac{5}{8} \div \frac{3}{8} = \frac{5}{8} \cdot \frac{8}{8} = \frac{5 \cdot 8}{8 \cdot 3} = \frac{5}{3} \text{ or } 1\frac{2}{3}$
25. $\frac{2}{37} \div \frac{1}{7} = \frac{2}{37} \cdot \frac{7}{1} = \frac{2 \cdot 7}{37 \cdot 1} = \frac{14}{37}$
29. $\frac{11}{12} \div \frac{11}{12} = \frac{11}{12} \cdot \frac{12}{12} = \frac{11 \cdot 12}{12 \cdot 11} = 1$
33. $0 \div \frac{7}{8} = 0 \cdot \frac{8}{7} = 0$
37. $\frac{2}{3} \div 4 = \frac{2}{3} \div \frac{4}{1} = \frac{2}{3} \cdot \frac{1}{4} = \frac{2 \cdot 1}{3 \cdot 4} = \frac{2 \cdot 1}{3 \cdot 2 \cdot 2} = \frac{1}{3 \cdot 2} = \frac{1}{6}$
41. $2\frac{1}{2} \div \frac{1}{2} = \frac{5}{2} \div \frac{1}{2} = \frac{5}{2} \cdot \frac{2}{1} = \frac{5 \cdot 2}{2 \cdot 1} = \frac{5}{1} = 5$
45. $3\frac{3}{7} \div 3\frac{1}{3} = \frac{24}{7} \div \frac{10}{3}$
 $= \frac{24 \cdot 3}{7 \cdot 10}$
 $= \frac{24 \cdot 3}{7 \cdot 2 \cdot 5}$
 $= \frac{12 \cdot 3}{135}$
49. $0 \div 15\frac{4}{7} = 0 \div \frac{109}{7} = 0 \cdot \frac{7}{109} = 0$
53. $1 \div \frac{18}{15} = 1 \cdot \frac{31}{18} = \frac{35}{18} \text{ or } 1\frac{17}{18}$
57. $\frac{6}{15} \div \frac{12}{15} = \frac{6}{15} \cdot \frac{5}{12} = \frac{6 \cdot 5}{15 \cdot 12} = \frac{6 \cdot 5}{5 \cdot 3 \cdot 6 \cdot 2} = \frac{1}{3 \cdot 2} = \frac{1}{6}$
61. $12 \div \frac{1}{8} = 12 \cdot \frac{8}{1} = 12 \cdot 8 = 96$
65. $2\frac{3}{8} \div 0$ is undefined.
69. $4\frac{5}{11} \div 1\frac{2}{5} = \frac{49}{11} \div \frac{7}{5}$
 $= \frac{49 \cdot 5}{11 \cdot 7}$
 $= \frac{7 \cdot 7 \cdot 5}{11 \cdot 7}$
 $= \frac{7 \cdot 7 \cdot 5}{11 \cdot 7}$
 $= \frac{35}{11} \text{ or } 3\frac{2}{11}$
73. $12\frac{3}{4} \div 4 = \frac{51}{4} \div \frac{4}{1} = \frac{51}{4} \cdot \frac{1}{4} = \frac{51}{16} \text{ or } 3\frac{3}{16}$
The patient walked $3\frac{3}{16}$ miles per day.

77.
$$15\frac{1}{5} \div 24 = \frac{76}{5} \div \frac{24}{1}$$

 $= \frac{76}{5} \cdot \frac{1}{24}$
 $= \frac{76 \cdot 1}{5 \cdot 24}$
 $= \frac{4 \cdot 19 \cdot 1}{5 \cdot 4 \cdot 6}$
 $= \frac{19 \cdot 1}{5 \cdot 6}$
 $= \frac{19}{30}$
On average, $\frac{19}{30}$ inch of rain

fell per hour.

81. $12 \div 2\frac{4}{7} = \frac{12}{1} \div \frac{10}{7}$ $=\frac{12}{1}\cdot\frac{7}{18}$ $=\frac{12\cdot7}{1\cdot18}$ $=\frac{6\cdot 2\cdot 7}{1\cdot 6\cdot 3}$ $=\frac{2\cdot7}{1\cdot3}$ $=\frac{14}{3}$ or $4\frac{2}{3}$

The length of the rectangle is $4\frac{2}{3}$ meters.

85.
$$2\frac{2}{3} \div 1\frac{1}{16} = \frac{8}{3} \div \frac{17}{16} = \frac{8}{3} \cdot \frac{16}{17} = \frac{8 \cdot 16}{3 \cdot 17} = \frac{128}{51} \text{ or } 2\frac{26}{51}.$$

89. $\frac{11}{20} \div \frac{20}{11} = \frac{11}{20} \cdot \frac{11}{20} = \frac{11 \cdot 11}{20 \cdot 20} = \frac{121}{400}$
93. 968
 $\frac{-772}{196}$

- 97. To divide mixed numbers, first write each mixed number as an improper fraction.
- $20\frac{2}{3} \div 10\frac{1}{2} = \frac{62}{3} \div \frac{21}{2} = \frac{62}{3} \cdot \frac{2}{21} = \frac{62 \cdot 2}{3 \cdot 21} = \frac{124}{3 \cdot 21}$ or $1\frac{61}{63}$ **101.** $12\frac{2}{12}$ rounds to 12. $3\frac{7}{8}$ rounds to 4. $12 \div 4 = 3$ The best estimate is **d**. **105.** $100 \div \frac{2}{13} = \frac{100}{1} \cdot \frac{13}{2} = \frac{2 \cdot 50 \cdot 13}{1 \cdot 2} = \frac{50 \cdot 13}{1} = 650$ The FedEx Express air fleet is 650 aircraft.

Chapter 2 Test

1. 7 of the 16 equal parts are shaded: $\frac{7}{16}$ 4 R 3 5. 5)23 $\frac{23}{5} = 4\frac{3}{5}$

9. Not equivalent, since the cross products are not

equal:
$$7 \cdot 8 = 56 \text{ and } 11 \cdot 5 = 55$$

13. $\frac{4}{4} \div \frac{3}{4} = \frac{4}{4} \cdot \frac{4}{3} = \frac{4 \cdot 4}{4 \cdot 3} = \frac{4}{3} \text{ or } 1\frac{1}{3}$
17. $8 \div \frac{1}{2} = \frac{8}{1} \cdot \frac{2}{1} = \frac{8 \cdot 2}{1 \cdot 1} = 16$
21. $\frac{16}{3} \div \frac{3}{12} = \frac{16}{3} \cdot \frac{12}{3}$
 $= \frac{16 \cdot 12}{3 \cdot 3}$
 $= \frac{16 \cdot 3 \cdot 4}{3 \cdot 3}$
 $= \frac{16 \cdot 4}{3}$
 $= \frac{64}{3} \text{ or } 21\frac{1}{3}$
25. $\frac{2}{3} \cdot 1\frac{8}{9} = \frac{2}{3} \cdot \frac{17}{9} = \frac{2 \cdot 17}{3 \cdot 9} = \frac{34}{27} \text{ or } 1\frac{7}{27}$
The area is $\frac{34}{27}$ square miles or $1\frac{7}{27}$ square miles.

Chapter 3

Exercise Set 3.1 1. $\frac{1}{7} + \frac{2}{7} = \frac{1+2}{7} = \frac{3}{7}$ 5. $\frac{2}{9} + \frac{4}{9} = \frac{2+4}{9} = \frac{6}{9} = \frac{3 \cdot 2}{3 \cdot 3} = \frac{2}{3}$ 9. $\frac{3}{14} + \frac{4}{14} = \frac{3+4}{14} = \frac{7}{14} = \frac{7 \cdot 1}{7 \cdot 2} = \frac{1}{2}$ **13.** $\frac{4}{13} + \frac{2}{13} + \frac{1}{13} = \frac{4+2+1}{13} = \frac{7}{13}$ **17.** $\frac{10}{11} - \frac{4}{11} = \frac{10 - 4}{11} = \frac{6}{11}$ **21.** $\frac{7}{4} - \frac{3}{4} = \frac{7-3}{4} = \frac{4}{4} = 1$ **25.** $\frac{25}{12} - \frac{15}{12} = \frac{25 - 15}{12} = \frac{10}{12} = \frac{2 \cdot 5}{2 \cdot 6} = \frac{5}{6}$ **29.** $\frac{86}{90} - \frac{85}{90} = \frac{86 - 85}{90} = \frac{1}{90}$ **33.** $\frac{8}{21} + \frac{5}{21} = \frac{8+5}{21} = \frac{13}{21}$ **37.** $\frac{13}{28} - \frac{13}{28} = \frac{13 - 13}{28} = \frac{0}{28} = 0$

rimeter =
$$\frac{4}{20} + \frac{7}{20} + \frac{9}{20}$$

= $\frac{4+7+9}{20}$
= $\frac{20}{20}$

The perimeter is 1 inch.

Pe

45. To find the remaining amount of track to be inspected, subtract the $\frac{5}{20}$ mile that has already been inspected from the $\frac{19}{20}$ mile total that must be inspected.

$$\frac{19}{20} - \frac{5}{20} = \frac{19 - 5}{20} = \frac{14}{20} = \frac{2 \cdot 7}{2 \cdot 10} = \frac{7}{10}$$

$$\frac{7}{10}$$
 of a mile of track remains to be inspected.

49. To find the part spent on eating and drinking, grooming, and sleeping, add the part spent eating and drinking

 $\left(\frac{4}{100}\right)$, the part spent grooming $\left(\frac{3}{100}\right)$, and the part spent sleeping $\left(\frac{36}{100}\right)$. $\frac{4}{100} + \frac{3}{100} + \frac{36}{100} = \frac{4+3+36}{100} = \frac{43}{100}$ $\frac{43}{100}$ of a full-time college students' weekday is spent on

eating and drinking, grooming, and sleeping.

53. To find the fraction of U.S. road congestion caused by weather or incidents, add the fraction caused by weather

$$\left(\frac{3}{20}\right) \text{ and the fraction caused by incidents} \left(\frac{5}{20}\right).$$
$$\frac{3}{20} + \frac{5}{20} = \frac{3+5}{20} = \frac{8}{20} = \frac{2 \cdot 4}{5 \cdot 4} = \frac{2}{5}$$

 $\frac{2}{5}$ of U.S. road congestion is caused by weather or incidents.

57. North America takes up $\frac{16}{100}$ of the world's land area,

while South America takes up $\frac{12}{100}$ of the land area. 16 12 16 + 12 28 4.7 7

 $\frac{16}{100} + \frac{12}{100} = \frac{16 + 12}{100} = \frac{28}{100} = \frac{4 \cdot 7}{4 \cdot 25} = \frac{7}{25}$ $\frac{7}{25}$ of the world's land area is within North America

and South America.

61. To find the fraction of U.S. theater screens that were either digital 3-D or analog, add the fraction that were digital

3-D
$$\left(\frac{19}{50}\right)$$
 and the fraction that were analog $\left(\frac{1}{50}\right)$
 $\frac{19}{50} + \frac{1}{50} = \frac{19+1}{50} = \frac{20}{50} = \frac{2 \cdot 10}{5 \cdot 10} = \frac{2}{5}$
 $\frac{2}{5}$ of US theater screens were either digital 3-D or

 $\frac{-}{5}$ of U.S. theater screens were either digital 3-D or analog in 2016.

65.
$$\frac{2}{2)\overline{4}}$$

 $2)\overline{8}$
 $8 = 2 \cdot 2 \cdot 2 = 2^{3}$
69. $\frac{3}{8} + \frac{7}{8} - \frac{5}{8} = \frac{3 + 7 - 5}{8} = \frac{10 - 5}{8} = \frac{5}{8}$
73. $\frac{2}{7} + \frac{9}{7} = \frac{2 + 9}{7} = \frac{11}{7} \text{ or } 1\frac{4}{7}$
77. $\frac{4}{100} + \frac{14}{100} + \frac{3}{100} + \frac{16}{100} + \frac{36}{100} + \frac{6}{100} + \frac{11}{100} + \frac{10}{100}$
 $= \frac{4 + 14 + 3 + 16 + 36 + 6 + 11 + 10}{100}$
 $= \frac{100}{100}$
 $= 1$
answers may vary

Exercise Set 3.2

- Multiples of 3: 3, 6, 9, <u>12</u>, 15, ... Multiples of 4: 4, 8, <u>12</u>, 16, ... LCM: 12
- **5.** Multiples of 12: 12, 24, <u>36</u>, 48, ... Multiples of 18: 18, <u>36</u>, 54, ... LCM: <u>36</u>
- **9.** $18 = 2 \cdot 3 \cdot 3$ $21 = 3 \cdot 7$ LCM: $2 \cdot 3 \cdot 3 \cdot 7 = 126$

13.
$$8 = \boxed{2 \cdot 2 \cdot 2}$$
$$24 = 2 \cdot 2 \cdot 2 \cdot \boxed{3}$$

$$LCM: 2 \cdot 2 \cdot 2 \cdot 3 = 24$$

- **17.** $8 = \boxed{2 \cdot 2 \cdot 2}$ $6 = 2 \cdot 3$ $27 = \boxed{3 \cdot 3 \cdot 3}$
- LCM: $2 \cdot 2 \cdot 2 \cdot 3 \cdot 3 \cdot 3 = 216$ 21. $34 = 2 \cdot 17$ $68 = 2 \cdot 2 \cdot 17$
- $LCM: 2 \cdot 2 \cdot 17 = 68$

25.
$$30 = 2 \cdot 3 \cdot 5$$

 $36 = 2 \cdot 2 \cdot 3 \cdot 3$
 $50 = 2 \cdot 5 \cdot 5$

LCM:
$$2 \cdot 2 \cdot 3 \cdot 3 \cdot 5 \cdot 5 = 900$$

29. 11 = 11

$$33 = \boxed{3} \cdot 11$$
$$121 = \boxed{11 \cdot 11}$$

LCM:
$$3 \cdot 11 \cdot 11 = 363$$

33.
$$\frac{7}{7} = \frac{7 \cdot 5}{7 \cdot 5} = \frac{26}{35}$$

37. $5 = \frac{5}{4} = \frac{5 \cdot 3}{5} = \frac{15}{25}$

41.
$$\frac{10}{7} = \frac{10 \cdot 3}{7 \cdot 3} = \frac{30}{21}$$

45.
$$\frac{2}{3} = \frac{2 \cdot 15}{3 \cdot 15} = \frac{30}{45}$$

49.
$$\frac{13}{13} = \frac{13 \cdot 6}{13 \cdot 6} = \frac{90}{78}$$

53. books and magazines: $\frac{43}{50} = \frac{43 \cdot 2}{50 \cdot 2} = \frac{86}{100}$

clothing and accessories: $\frac{4}{5} = \frac{4 \cdot 20}{5 \cdot 20} = \frac{80}{100}$ computer hardware: $\frac{29}{50} = \frac{29 \cdot 2}{50 \cdot 2} = \frac{58}{100}$ computer software: $\frac{17}{25} = \frac{17 \cdot 4}{25 \cdot 4} = \frac{68}{100}$ drugs, health and beauty aids: $\frac{3}{25} = \frac{3 \cdot 4}{25 \cdot 4} = \frac{12}{100}$ electronics and appliances: $\frac{21}{25} = \frac{21 \cdot 4}{25 \cdot 4} = \frac{84}{100}$ food, beer, and wine: $\frac{17}{25} = \frac{17 \cdot 4}{25 \cdot 4} = \frac{68}{100}$ home furnishings: $\frac{81}{100} = \frac{81}{100}$ **Solutions to Selected Exercises**

78

music and videos:
$$\frac{9}{10} = \frac{9 \cdot 10}{10 \cdot 10} = \frac{90}{100}$$

office equipment and supplies: $\frac{79}{100} = \frac{79}{100}$
sporting goods: $\frac{37}{50} = \frac{37 \cdot 2}{50 \cdot 2} = \frac{74}{100}$
toys, hobbies, and games: $\frac{39}{50} = \frac{39 \cdot 2}{50 \cdot 2} = \frac{78}{100}$
57. $\frac{7}{10} - \frac{2}{10} = \frac{7 - 2}{10} = \frac{5}{10} = \frac{5 \cdot 1}{5 \cdot 2} = \frac{1}{2}$
61. $\frac{23}{18} - \frac{15}{18} = \frac{23 - 15}{18} = \frac{8}{18} = \frac{2 \cdot 4}{2 \cdot 9} = \frac{4}{9}$
65. $\frac{37}{165} = \frac{37 \cdot 22}{165 \cdot 22} = \frac{814}{3630}$
69. a. $\frac{10}{15} = \frac{5 \cdot 2}{5 \cdot 3} = \frac{2}{3}$
b. $\frac{40}{60} = \frac{20 \cdot 2}{20 \cdot 3} = \frac{2}{3}$
c. $\frac{16}{20} = \frac{4 \cdot 4}{4 \cdot 5} = \frac{4}{5}$
d. $\frac{200}{300} = \frac{100 \cdot 2}{100 \cdot 3} = \frac{2}{3}$
a. b, and **d** are equivalent to $\frac{2}{3}$.
Exercise Set 3.3
1. The LCD of 3 and 6 is 6.
 $\frac{2}{3} + \frac{1}{6} = \frac{2}{3} \cdot \frac{2}{2} + \frac{1}{6} = \frac{4}{6} + \frac{1}{6} = \frac{5}{6}$
5. The LCD of 11 and 33 is 33.
 $\frac{2}{11} + \frac{2}{33} = \frac{2}{11} \cdot \frac{3}{3} + \frac{2}{33} = \frac{6}{33} + \frac{2}{33} = \frac{8}{33}$
9. The LCD of 35 and 7 is 35.
 $\frac{11}{35} + \frac{2}{7} = \frac{11}{35} + \frac{2}{7} \cdot \frac{5}{5}$
 $= \frac{11}{35} + \frac{10}{35}$
 $= \frac{21}{35}$

 $=\frac{3}{5}$

13. The LCD of 15 and 12 is 60.

 $\frac{7}{15} + \frac{5}{12} = \frac{7}{15} \cdot \frac{4}{4} + \frac{5}{12} \cdot \frac{5}{5}$

 $=\frac{53}{60}$

 $=\frac{28}{60}+\frac{25}{60}$

 $\frac{9}{44} + \frac{17}{36} = \frac{9}{44} \cdot \frac{9}{9} + \frac{17}{36} \cdot \frac{11}{11}$ $=\frac{81}{396}+\frac{187}{396}$ $=\frac{268}{396}$ $=\frac{4\cdot 67}{4\cdot 99}$ $=\frac{67}{99}$ 21. The LCD of 3, 9, and 27 is 27. $\frac{1}{3} + \frac{1}{9} + \frac{1}{27} = \frac{1}{3} \cdot \frac{9}{9} + \frac{1}{9} \cdot \frac{3}{3} + \frac{1}{27}$ $=\frac{9}{27}+\frac{3}{27}+\frac{1}{27}$ $=\frac{13}{27}$ 25. The LCD of 36, 4, and 6 is 36. $\frac{5}{36} + \frac{3}{4} + \frac{1}{6} = \frac{5}{36} + \frac{3}{4} \cdot \frac{9}{9} + \frac{1}{6} \cdot \frac{6}{6}$ $=\frac{5}{36}+\frac{27}{36}+\frac{6}{36}$ $=\frac{38}{36}$ $=\frac{2\cdot 19}{2\cdot 18}$ $=\frac{19}{18}$ or $1\frac{1}{18}$ 29. The LCD of 8 and 16 is 16. $\frac{7}{8} - \frac{3}{16} = \frac{7}{8} \cdot \frac{2}{2} - \frac{3}{16} = \frac{14}{16} - \frac{3}{16} = \frac{11}{16}$ **33.** The LCD of 7 and 8 is 56. $\frac{5}{7} - \frac{1}{8} = \frac{5}{7} \cdot \frac{8}{8} - \frac{1}{8} \cdot \frac{7}{7} = \frac{40}{56} - \frac{7}{56} = \frac{33}{56}$ **37.** The LCD of 35 and 7 is 35. $\frac{11}{35} - \frac{2}{7} = \frac{11}{35} - \frac{2}{7} \cdot \frac{5}{5} = \frac{11}{35} - \frac{10}{35} = \frac{1}{35}$ **41.** The LCD of 15 and 12 is 60. $\frac{7}{15} - \frac{5}{12} = \frac{7}{15} \cdot \frac{4}{4} - \frac{5}{12} \cdot \frac{5}{5}$ $=\frac{28}{60}-\frac{25}{60}$ $=\frac{3}{60}$ $=\frac{3\cdot 1}{3\cdot 20}$ $=\frac{1}{20}$

17. The LCD of 44 and 36 is 396.

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$$\frac{1}{100} - \frac{1}{1000} = \frac{1}{100} \cdot \frac{10}{10} - \frac{1}{1000}$$
$$= \frac{10}{1000} - \frac{1}{1000}$$
$$= \frac{9}{1000}$$

49. The LCD of 12 and 9 is 36.
$$\frac{5}{12} + \frac{1}{9} = \frac{5}{12} \cdot \frac{3}{3} + \frac{1}{9} \cdot \frac{4}{4} = \frac{15}{36} + \frac{4}{36} = \frac{19}{36}$$

53. The LCD of 28 and 40 is 280.

$$\frac{9}{28} - \frac{3}{40} = \frac{9}{28} \cdot \frac{10}{10} - \frac{3}{40} \cdot \frac{7}{7} = \frac{90}{280} - \frac{21}{280} = \frac{69}{280}$$
57. Add the lengths of the four sides. The LCD of 3 and 5 is 15.

$$\frac{4}{5} + \frac{1}{3} + \frac{4}{5} + \frac{1}{3} = \frac{4}{5} \cdot \frac{3}{3} + \frac{1}{3} \cdot \frac{5}{5} + \frac{4}{5} \cdot \frac{3}{3} + \frac{1}{3} \cdot \frac{5}{5}$$
$$= \frac{12}{15} + \frac{5}{15} + \frac{12}{15} + \frac{5}{15}$$
$$= \frac{34}{15} \text{ or } 2\frac{4}{15}$$
The perimeter is $\frac{34}{15} \text{ cm or } 2\frac{4}{15} \text{ cm.}$

61. Subtract the speed of the three-toed sloth on the ground from its speed in trees. The LCD of 10 and 100 is 100.

 $\frac{17}{100} - \frac{1}{10} = \frac{17}{100} - \frac{1}{10} \cdot \frac{10}{10} = \frac{17}{100} - \frac{10}{100} = \frac{7}{100}$ A sloth can travel $\frac{7}{100}$ mile per hour faster in trees than it can on the ground.

65. Add the lengths shown.

The LCD of 16, 2, and 32 is 32.

$$\frac{5}{16} + \frac{1}{2} + \frac{5}{32} = \frac{5}{16} \cdot \frac{2}{2} + \frac{1}{2} \cdot \frac{16}{16} + \frac{5}{32}$$

$$= \frac{10}{32} + \frac{16}{32} + \frac{5}{32}$$

$$= \frac{31}{32}$$

The total length of the object is $\frac{31}{32}$ inch.

69. The Pacific Ocean takes up $\frac{1}{2}$ of the world's water area, while the Atlantic Ocean takes up $\frac{13}{50}$ of the water area. The LCD of 2 and 50 is 50.

$$\frac{1}{2} + \frac{13}{50} = \frac{1}{2} \cdot \frac{25}{25} + \frac{13}{50}$$
$$= \frac{25}{50} + \frac{13}{50}$$
$$= \frac{38}{50}$$
$$= \frac{2 \cdot 19}{2 \cdot 25}$$
$$= \frac{19}{25}$$

 $\frac{19}{25}$ of the world's water area is accounted for by the Pacific Ocean and the Atlantic Ocean.

73.
$$1 - \frac{19}{100} = \frac{100}{100} - \frac{19}{100} = \frac{81}{100}$$

 $\frac{81}{100}$ of the areas maintained by the National Park Service are not designated as National Monuments.
77. $4 \div 7\frac{1}{4} = \frac{4}{1} \div \frac{29}{4} = \frac{4}{1} \cdot \frac{4}{29} = \frac{4 \cdot 4}{1 \cdot 29} = \frac{16}{29}$
81. a.
b. Yes, there is an error.
c. $\frac{3}{5} + \frac{4}{5} = \frac{3 + 4}{5} = \frac{7}{5}$ or $1\frac{2}{5}$
85. The LCD of 55 and 1760 is 1760.
 $\frac{30}{55} + \frac{1000}{1760} = \frac{30}{55} \cdot \frac{32}{32} + \frac{1000}{1760}$
 $= \frac{960}{1760} + \frac{1000}{1760}$
 $= \frac{1960}{1760}$
 $= \frac{49 \cdot 40}{44 \cdot 40}$
 $= \frac{49}{44}$ or $1\frac{5}{44}$

Exercise Set 3.4

1. Exact:
$$4\frac{7}{10}$$

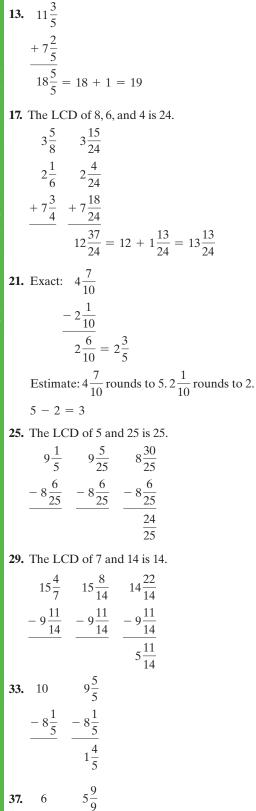
 $\frac{+2\frac{1}{10}}{6\frac{8}{10}} = 6\frac{4}{5}$
Estimate: $4\frac{7}{10}$ rounds to 5. $2\frac{1}{10}$ rounds to 2.
 $5 + 2 = 7$

5. The LCD of 5 and 25 is 25.

$$9\frac{1}{5} \qquad 9\frac{5}{25} \\ + 8\frac{2}{25} \qquad + 8\frac{2}{25} \\ \hline 17\frac{7}{25}$$

9. The LCD of 6 and 8 is 24.

$$\frac{1\frac{5}{6}}{\frac{120}{24}} + \frac{120}{24} + \frac{5\frac{3}{8}}{\frac{120}{624}} + \frac{59}{24} = 6 + 1\frac{5}{24} = 7\frac{5}{24}$$



 $\frac{-2\frac{4}{9}}{-\frac{2}{9}} - \frac{-2\frac{4}{9}}{-\frac{5}{9}}$

41. The LCD of 6 and 12 is 12.

$$\begin{array}{r} 15\frac{1}{6} & 15\frac{2}{12} \\
+13\frac{5}{12} & +13\frac{5}{12} \\
\hline
 & 28\frac{7}{12} \\
\end{array}$$
45. $5\frac{8}{9} \\
+2\frac{1}{9} \\
\hline
 & 7\frac{9}{2} = 7 + 1 = 8 \\
\end{array}$

49. Subtract the diameter for Eastern Bluebirds from the diameter for Mountain Bluebirds.

The LCD of 2 and 16 is 16. 0 0

$$\frac{1\frac{3}{16}}{-1\frac{1}{2}} = \frac{-1\frac{8}{16}}{-\frac{1}{16}}$$

The entrance holes for Mountain Bluebirds should be $\frac{1}{16}$ inch wider.

- 53. Subtract Yuma's average annual rainfall from Tucson's average annual rainfall. The LCD of 4 and 5 is 20.

$$\begin{array}{rcrcrcr}
11\frac{1}{4} & 11\frac{5}{20} & 10\frac{25}{20} \\
\hline
-3\frac{3}{5} & -3\frac{12}{20} & -3\frac{12}{20} \\
\hline
& & & & & \\
\hline
& & & \\$$

On average, Tucson gets $7\frac{13}{20}$ inches more rain annually than Yuma.

57. Subtract the time for a personal return from the time for a small business return. The LCD of 2 and 8 is 8.

It takes him $2\frac{3}{9}$ hours longer to prepare a small business return.

61. Subtract the length of the Lacey V. Murrow Memorial Bridge from the length of the Evergreen Point Bridge.

$$\frac{2526}{-2206\frac{2}{3}} = \frac{2525\frac{3}{3}}{-2206\frac{1}{3}} = \frac{-2206\frac{1}{3}}{-319\frac{1}{3}}$$

The Evergreen Point Bridge is $319\frac{1}{3}$ yards longer than the Lacey V. Murrow Memorial Bridge.

- A45

65. Subtract the length of the August 21, 2017, eclipse from the length of the April 8, 2024, eclipse. The LCD of 3 and 15 is 15.

$$\frac{4\frac{7}{15}}{-\frac{2\frac{2}{3}}{-\frac{2}{3}}} = \frac{4\frac{7}{15}}{-\frac{2\frac{10}{15}}{-\frac{10}{15}}} = \frac{-2\frac{10}{15}}{-\frac{12}{15}} = 1$$

The April 8, 2024, eclipse will be $1\frac{4}{5}$ minutes longer than the August 21, 2017, eclipse.

 $\frac{4}{5}$

69. Add the lengths of the sides. The LCD of 3 and 8 is 24.

The perimeter is $21\frac{5}{24}$ meters.

73. $5^2 = 5 \cdot 5 = 25$ **77.** $2 + 3(8 \cdot 7 - 1) = 2 + 3(56 - 1)$ = 2 + 3(55) = 2 + 165 = 167**81.** $9\frac{10}{16} = 9 + \frac{2 \cdot 5}{2 \cdot 8} = 9\frac{5}{8}$

85. answers may vary

Exercise Set 3.5

1. Since 7 > 6, then $\frac{7}{9} > \frac{6}{9}$. 5. The LCD of 42 and 21 is 42. $\frac{9}{42}$ has a denominator of 42. $\frac{5}{21} = \frac{5}{21} \cdot \frac{2}{2} = \frac{10}{42}$ Since 9 < 10, then $\frac{9}{42} < \frac{10}{42}$, so $\frac{9}{42} < \frac{5}{21}$. 9. The LCD of 4 and 3 is 12. $\frac{3}{4} = \frac{3}{4} \cdot \frac{3}{3} = \frac{9}{12}$ $\frac{2}{3} = \frac{2}{3} \cdot \frac{4}{4} = \frac{8}{12}$ Since 9 > 8, then $\frac{9}{12} > \frac{8}{12}$, so $\frac{3}{4} > \frac{2}{3}$.

13. The LCD of 10 and 11 is 110.

$$\frac{1}{10} = \frac{1}{10} \cdot \frac{11}{11} = \frac{11}{110}$$

$$\frac{1}{11} = \frac{1}{11} \cdot \frac{10}{10} = \frac{10}{110}$$
Since 11 > 10, then $\frac{11}{110} > \frac{10}{110}$, so $\frac{1}{10} > \frac{1}{11}$.
17. $\left(\frac{1}{2}\right)^4 = \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{16}$
21. $\left(\frac{4}{7}\right)^3 = \frac{4}{7} \cdot \frac{4}{7} \cdot \frac{4}{7} = \frac{64}{343}$
25. $\left(\frac{3}{4}\right)^2 \cdot \left(\frac{2}{3}\right)^3 = \left(\frac{3}{4} \cdot \frac{3}{4}\right) \cdot \left(\frac{2}{3} \cdot \frac{2}{3} \cdot \frac{2}{3}\right)$
 $= \frac{3 \cdot 3 \cdot 2 \cdot 2 \cdot 2}{3 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 3 \cdot 3 \cdot 3}$
 $= \frac{1}{2 \cdot 3}$
 $= \frac{1}{6}$
29. The LCD of 15 and 5 is 15.
 $\frac{2}{15} + \frac{3}{5} = \frac{2}{15} + \frac{3}{5} \cdot \frac{3}{3} = \frac{2}{15} + \frac{9}{15} = \frac{11}{15}$
33. $1 - \frac{4}{9} = \frac{9}{9} - \frac{4}{9} = \frac{5}{9}$
37. The LCD of 6 and 4 is 12.
 $\frac{5}{6} - \frac{3}{4} = \frac{5}{6} \cdot \frac{2}{2} - \frac{3}{4} \cdot \frac{3}{3} = \frac{10}{12} - \frac{9}{12} = \frac{1}{12}$
41. $0 \cdot \frac{9}{10} = 0$
45. $\frac{20}{35} \cdot \frac{7}{10} = \frac{20 \cdot 7}{35 \cdot 10} = \frac{10 \cdot 2 \cdot 7}{7 \cdot 5 \cdot 10} = \frac{2}{5}$
49. $\frac{1}{5} + \frac{1}{3} \cdot \frac{1}{4} = \frac{1}{5} + \frac{1 \cdot 1}{3 \cdot 4} = \frac{1}{5} + \frac{1}{12}$
The LCD of 5 and 12 is 60.
 $\frac{1}{5} + \frac{1}{12} = \frac{1}{5} \cdot \frac{12}{12} + \frac{1}{12} \cdot \frac{5}{5} = \frac{12}{60} + \frac{5}{60} = \frac{17}{60}$
53. $\frac{1}{5} \left(2\frac{5}{6} - \frac{1}{3}\right) = \frac{1}{5} \left(\frac{17}{6} - \frac{1}{3} \cdot \frac{2}{2}\right)$
 $= \frac{1}{5} \left(\frac{15}{6}\right)$
 $= \frac{1 \cdot 15}{5 \cdot 6}$
 $= \frac{1 \cdot 5 \cdot 3}{5 \cdot 3 \cdot 2}$
 $= \frac{1}{2}$

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$$57. \left(\frac{3}{4}\right)^{2} \div \left(\frac{3}{4} - \frac{1}{12}\right) = \left(\frac{3}{4}\right)^{2} \div \left(\frac{3}{4} \cdot \frac{3}{3} - \frac{1}{12}\right)$$
$$= \left(\frac{3}{4}\right)^{2} \div \left(\frac{9}{12} - \frac{1}{12}\right)$$
$$= \left(\frac{3}{4}\right)^{2} \div \left(\frac{9}{12} - \frac{1}{12}\right)$$
$$= \left(\frac{3}{4}\right)^{2} \div \left(\frac{8}{12}\right)$$
$$= \left(\frac{3}{4}\right)^{2} \div \left(\frac{2}{4 \cdot 3}\right)$$
$$= \left(\frac{3}{4}\right)^{2} \div \left(\frac{2}{3}\right)$$
$$= \left(\frac{3}{4} \cdot \frac{3}{4}\right) \div \left(\frac{2}{3}\right)$$
$$= \left(\frac{3}{4} \cdot \frac{3}{4}\right) \div \left(\frac{2}{3}\right)$$
$$= \frac{9 \cdot 3}{16 \cdot 2}$$
$$= \frac{9 \cdot 3}{16 \cdot 2}$$
$$= \frac{9 \cdot 3}{16 \cdot 2}$$
$$= \frac{5}{18} + \frac{10}{18}$$
$$= \frac{15}{18}$$
$$= \frac{3 \cdot 5}{3 \cdot 6}$$
$$= \frac{5}{6}$$
$$65. \frac{3}{13} \div \frac{9}{26} - \frac{7}{24} \cdot \frac{8}{14} = \frac{3}{13} \cdot \frac{26}{9} - \frac{7}{24} \cdot \frac{8}{14}$$
$$= \frac{3 \cdot 26}{13 \cdot 9} - \frac{7 \cdot 8}{24 \cdot 14}$$
$$= \frac{3 \cdot 13 \cdot 2}{13 \cdot 3 \cdot 3} - \frac{7 \cdot 8}{8 \cdot 3 \cdot 7 \cdot 2}$$
$$= \frac{2}{3} - \frac{1}{6}$$
$$= \frac{3}{6}$$
$$= \frac{1}{2}$$

$$69. \left(\frac{3}{4} + \frac{1}{8}\right)^2 - \left(\frac{1}{2} + \frac{1}{8}\right) = \left(\frac{3}{4} \cdot \frac{2}{2} + \frac{1}{8}\right)^2 - \left(\frac{1}{2} \cdot \frac{4}{4} + \frac{1}{8}\right)$$
$$= \left(\frac{6}{8} + \frac{1}{8}\right)^2 - \left(\frac{4}{8} + \frac{1}{8}\right)$$
$$= \left(\frac{7}{8}\right)^2 - \left(\frac{5}{8}\right)$$
$$= \left(\frac{7}{8} \cdot \frac{7}{8}\right) - \frac{5}{8}$$
$$= \frac{49}{64} - \frac{5}{8}$$
$$= \frac{49}{64} - \frac{5}{8} \cdot \frac{8}{8}$$
$$= \frac{49}{64} - \frac{40}{64}$$
$$= \frac{9}{64}$$

73. The average is the sum, divided by 3.

$$\left(\frac{1}{5} + \frac{3}{10} + \frac{3}{20}\right) \div 3 = \left(\frac{1}{5} \cdot \frac{4}{4} + \frac{3}{10} \cdot \frac{2}{2} + \frac{3}{20}\right) \div 3$$
$$= \left(\frac{4}{20} + \frac{6}{20} + \frac{3}{20}\right) \div 3$$
$$= \frac{13}{20} \div 3$$
$$= \frac{13}{20} \cdot \frac{1}{3}$$
$$= \frac{13}{60}$$

- 77. "Increased by" is most likely to translate to addition; A.
- **81.** "Subtracted from" is most likely to translate to subtraction; S.
- 85. "Times" is most likely to translate to multiplication; M.

89.
$$\frac{2^3}{3} = \frac{2 \cdot 2 \cdot 2}{3} = \frac{8}{3}$$
$$\left(\frac{2}{3}\right)^3 = \frac{2}{3} \cdot \frac{2}{3} \cdot \frac{2}{3} = \frac{8}{27}$$
$$\frac{2^3}{3} \text{ and } \left(\frac{2}{3}\right)^3 \text{ do not simplify to the same number.}$$
answers may vary

- **93.** The operations should be done in this order: division, multiplication, subtraction, addition
- **97.** The LCD of 5 and 50 is 50.

$$\frac{2}{5} = \frac{2}{5} \cdot \frac{10}{10} = \frac{20}{50}$$
$$\frac{13}{50} = \frac{13}{50}$$

Since 20 > 13, then $\frac{20}{50} > \frac{13}{50}$, so $\frac{2}{5} > \frac{13}{50}$.

The average college student spends more money on discretionary purchases than on room and board.

33. Volume Ţ

Volume

Length 37. a. needed

> ↓ Length

b. 10 - 9

Area =

↓

= -

Ţ

41. Area is Ţ

Perimeter is Ţ

Perimeter =

45. Length i Ţ

29. Area of photograph is length times width

Exercise Set 3.6

- 1. "The sum" translates as addition. $\frac{1}{2}+\frac{1}{3}$
- 5. "Subtract" indicates subtraction.

- 16 8
- 9. "product" indicates multiplication.

$$8\frac{1}{3}\cdot\frac{7}{9}$$

Wall is number of times brick width plus of times mortar width 13. bricks mortar Ţ Ţ Ţ ↓ Ţ Ţ Ţ ↓ $\cdot 2\frac{3}{4} +$ $\frac{1}{2}$ Height = 4 3 . $= 4 \cdot \frac{11}{4} + 3 \cdot \frac{1}{2} = 11 + \frac{3}{2} = 11 + 1 + \frac{1}{2} = 12\frac{1}{2}$ The wall is $12\frac{1}{2}$ inches tall. **17.** Bill is $\frac{1}{1}$ times coin

7. life is
$$\overline{20}$$
 times life
 $\downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow$
Life $= \frac{1}{20} \quad \cdot \quad 30$
 $= \frac{30}{20} = \frac{10 \cdot 3}{10 \cdot 2} = \frac{3}{2} \text{ or } 1\frac{1}{2}$

The life expectancy of circulating paper money is $1\frac{1}{2}$ years.

| 21. | Total
needed | is | amount
for large
shirt | plus | number
of small
shirts | times | amount
for small
shirt |
|-----|-----------------|--------------|--|-----------------|------------------------------|------------------------------|------------------------------|
| | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow |
| | Total | = | $1\frac{1}{2}$ | + | 5 | • | $\frac{3}{4}$ |
| | | = ; | $1\frac{1}{2} + 5 \cdot \frac{3}{4}$ $\frac{21}{4} \text{ or } 5\frac{1}{4}$ | $=\frac{3}{2}+$ | $\frac{15}{4} = \frac{3}{2}$ | $\frac{2}{2} + \frac{15}{4}$ | $=\frac{6}{4}+\frac{15}{4}$ |

The amount of cloth needed is $5\frac{1}{4}$ yards, so the 5-yard remnant is not enough. Another $\frac{1}{4}$ yard of material is required.

25.

| uter
neter | is | left
thickness | plus | inner
diameter | plus | right
thickness | | |
|---------------|--------------|--|------------------------------|--|------------------|--|------------------|-----------------|
| \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | \downarrow | | |
| iter
neter | = | $\frac{3}{16}$ | + | $\frac{3}{4}$ | + | $\frac{3}{16}$ | | |
| | = | $\frac{3}{16} + \frac{3}{4} + \frac{3}{4}$ | $\frac{3}{16} = \frac{1}{2}$ | $\frac{3}{16} + \frac{3}{4} \cdot \frac{4}{4} -$ | $+\frac{3}{16}=$ | $\frac{3}{16} + \frac{12}{16} + \frac{12}$ | $\frac{3}{16} =$ | $\frac{18}{16}$ |
| | = | $\frac{2\cdot 9}{2\cdot 8} = \frac{9}{8} \mathrm{o}$ | or $1\frac{1}{8}$ | | | | | |
| | | | 9 | 1 | | | | |

The outer diameter is $\frac{9}{8}$ inches or $1\frac{1}{8}$ inches.

 $=\frac{19}{4} \text{ or } 4\frac{3}{4}$

Solutions to Selected Exercises

57.
$$5 + 3[14 - (12 \div 3)] = 5 + 3[14 - 4]$$

 $= 5 + 3[10]$
 $= 5 + 30$
 $= 35$
61. The unmarked horizontal edge of the figure has length
 $6\frac{7}{9}$ feet $-3\frac{8}{9}$ feet.
 $6\frac{7}{9} - 3\frac{8}{9} = 5\frac{16}{9} - 3\frac{8}{9} = 2\frac{8}{9}$
The unmarked vertical edge of the figure has length
 $6\frac{2}{3}$ feet $-4\frac{4}{9}$ feet.
 $6\frac{2}{3} - 4\frac{4}{9} = 6\frac{6}{9} - 4\frac{4}{9} = 2\frac{2}{9}$
Area of smaller rectangle $= 2\frac{8}{9} \cdot 2\frac{2}{9}$
 $= \frac{26 \cdot 20}{9 \cdot 9}$
 $= \frac{26 \cdot 20}{9 \cdot 9}$
 $= \frac{520}{81}$
 $= 6\frac{34}{81}$
Area of larger rectangle $= 4\frac{4}{9} \cdot 6\frac{7}{9}$
 $= \frac{40 \cdot 61}{9 \cdot 9}$
 $= \frac{2440}{81}$
 $= 30\frac{10}{81}$
Total area $= 6\frac{34}{81} + 30\frac{10}{81}$
 $= 6 + 30 + \frac{34}{81} + \frac{10}{81}$
 $= 36\frac{44}{81}$

The area of the figure is $36\frac{44}{81}$ square feet.

65. There are 365 days in one year and 24 hours in one day.

$$3 \text{ years} = 3 \text{ years} \cdot \frac{365 \text{ days}}{1 \text{ year}} \cdot \frac{24 \text{ hours}}{1 \text{ day}} = 26,280 \text{ hours}$$
$$26,280 \cdot \frac{11}{13,140} = \frac{26,280}{1} \cdot \frac{11}{13,140} = \frac{2 \cdot 13,140 \cdot 11}{1 \cdot 13,140} = \frac{2 \cdot 11}{1} = 22$$

 $\frac{10}{81}$

Today it takes 22 hours to produce one million coins.

Chapter 3 Test

| - | apter o rest |
|-----|---|
| 1. | $4 = 2 \cdot 2$ |
| | $15 = \boxed{3} \cdot \boxed{5}$ |
| | $15 = \boxed{3} \cdot \boxed{5}$
LCM: 2 \cdot 2 \cdot 3 \cdot 5 = 60 |
| | |
| 5. | $\frac{7}{9} + \frac{1}{9} = \frac{7+1}{9} = \frac{8}{9}$ |
| | , , , , |
| 9. | The LCD of 8 and 3 is 24. $7 - 7 - 2 = 21$ |
| | $\frac{7}{8} = \frac{7}{8} \cdot \frac{3}{3} = \frac{21}{24}$ |
| | 8 8 5 24 |
| | $\frac{1}{3} = \frac{1}{3} \cdot \frac{8}{8} = \frac{8}{24}$ |
| | 5 5 6 24 |
| | $\frac{7}{8} - \frac{1}{3} = \frac{21}{24} - \frac{8}{24} = \frac{13}{24}$ |
| | 8 3 24 24 24 |
| 13. | The LCD of 12, 8, and 24 is 24. |
| | $\frac{11}{12} = \frac{11}{12} \cdot \frac{2}{2} = \frac{22}{24}$ |
| | $\frac{1}{12} = \frac{1}{12} \cdot \frac{1}{2} = \frac{1}{24}$ |
| | $\frac{3}{8} = \frac{3}{8} \cdot \frac{3}{3} = \frac{9}{24}$ |
| | $\frac{1}{8} - \frac{1}{8} \cdot \frac{1}{3} - \frac{1}{24}$ |
| | $\frac{11}{12} + \frac{3}{8} + \frac{5}{24} = \frac{22}{24} + \frac{9}{24} + \frac{5}{24}$ |
| | $\frac{1}{12} + \frac{1}{8} + \frac{1}{24} = \frac{1}{24} + \frac{1}{24} + \frac{1}{24}$ |
| | $=\frac{36}{24}$ |
| | $=\frac{1}{24}$ |
| | 12.3 |
| | $=\frac{12\cdot 3}{12\cdot 2}$ |
| | 3 1 |
| | $=\frac{3}{2} \text{ or } 1\frac{1}{2}$ |
| | 11 |
| 17. | 19 $18\frac{11}{11}$ |
| | 3 3 |
| | $-2\frac{3}{11}$ $-2\frac{3}{11}$ |
| | |
| | $16\frac{8}{11}$ |
| | |
| 21. | $\left(\frac{4}{5}\right)^2 + \left(\frac{1}{2}\right)^3 = \left(\frac{4}{5} \cdot \frac{4}{5}\right) + \left(\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2}\right)$ |
| | |
| | $=\frac{16}{25}+\frac{1}{8}$ |
| | |
| | $=\frac{16}{25}\cdot\frac{8}{8}+\frac{1}{8}\cdot\frac{25}{25}$ |
| | |
| | $=\frac{128}{200}+\frac{25}{200}$ |
| | |
| | $=\frac{153}{200}$ |
| | 200 |
| | |

25. Divide the number of gallons of fuel by the number of hours.

$$58\frac{3}{4} \div 7\frac{1}{2} = \frac{235}{4} \div \frac{15}{2} = \frac{235}{4} \cdot \frac{2}{15} = \frac{235 \cdot 2}{4 \cdot 15} = \frac{5 \cdot 47 \cdot 2}{2 \cdot 2 \cdot 5 \cdot 3}$$
$$= \frac{47}{2 \cdot 3} = \frac{47}{6} \text{ or } 7\frac{5}{6}$$

 $7\frac{5}{6}$ gallons of fuel were used each hour.

A48

49. $\sqrt{9} = 3$, because $3 \cdot 3 = 9$. **53.** $8 \div 4 \cdot 2 = 2 \cdot 2 = 4$

29. Perimeter
$$= 2 \cdot 1 + 2 \cdot \frac{2}{3}$$
$$= 2 + \frac{2}{1} \cdot \frac{2}{3}$$
$$= 2 + \frac{4}{3}$$
$$= 2 + 1 + \frac{1}{3}$$
$$= 3\frac{1}{3}$$
The perimeter is $3\frac{1}{3}$ feet.
Area $= 1 \cdot \frac{2}{3} = \frac{2}{3}$ The area is $\frac{2}{3}$ square foot.

Chapter 4

Exercise Set 4.1

- **1.** 6.52 in words is six and fifty-two hundredths.
- 5. 0.205 in words is two hundred five thousandths.
- 9. 200.005 in words is two hundred and five thousandths.
- 13. 2.43 in words is two and forty-three hundredths.
- **17.** 118.4 in words is one hundred eighteen and four tenths.
- 21. The check should be paid to "Bell South," for the amount of

"59.68," which is written in words as "Fifty-nine and $\frac{68}{100}$."

- 25. Nine and eight hundredths is 9.08.
- **29.** Forty-six ten-thousandths is 0.0046.
- **33.** One and three tenths is 1.3.

37.
$$0.27 = \frac{27}{100}$$

41. $0.15 = \frac{15}{100} = \frac{3}{20}$
45. $0.048 = \frac{48}{1000} = \frac{6}{125}$
49. $15.802 = 15\frac{802}{1000} = 15\frac{401}{500}$
53. $487.32 = 487\frac{32}{100} = 487\frac{8}{25}$
57. $\frac{45}{100} = 0.45$
61. $\frac{268}{1000} = 0.268$
65. $\frac{4026}{1000} = 4.026$
69. $\frac{563}{10} = 56.3$

73. In standard form, eight tenths is 0.8, while as a fraction it is $\frac{8}{1-1}$ or $\frac{4}{1-1}$.

$$s \frac{1}{10} \text{ or } \frac{1}{5}$$
.

- **77.** To round 47,261 to the nearest ten, observe that the digit in the ones place is 1. Since the digit is less than 5, we do not add 1 to the digit in the tens place. The number 47,261 rounded to the nearest ten is 47,260.
- 81. answers may vary

85.
$$17\frac{268}{1000} = 17.268$$

Exercise Set 4.2 1.
$$0.15$$
 0.16
 \uparrow
 \uparrow
 $5 < 6$ so
 $0 < 1$ so

 $0.15 < 0.16$
 $0.098 < 0.1$
9. 167.908
 167.980
 \uparrow
 \uparrow
 $0 < 8$ so

 $167.908 < 167.980$

- 13. Smallest to largest: 0.006, 0.0061, 0.06
- **17.** Smallest to largest: 1.01, 1.09, 1.1, 1.16
- **21.** To round 0.57 to the nearest tenth, observe that the digit in the hundredths place is 7. Since this digit is 5 or greater, we add 1 to the digit in the tenths place. The number 0.57 rounded to the nearest tenth is 0.6.
- **25.** To round 0.5942 to the nearest thousandth, observe that the digit in the ten-thousandths place is 2. Since this digit is less than 5, we do not add 1 to the digit in the thousandths place. The number 0.5942 rounded to the nearest thousandth is 0.594.
- **29.** To round 12.342 to the nearest tenth, observe that the digit in the hundredths place is 4. Since this digit is less than 5, we do not add 1 to the digit in the tenths place. The number 12.342 rounded to the nearest tenth is 12.3.
- **33.** To round 0.501 to the nearest tenth, observe that the digit in the hundredths place is 0. Since this digit is less than 5, we do not add 1 to the digit in the tenths place. The number 0.501 rounded to the nearest tenth is 0.5.
- **37.** To round 3829.34 to the nearest ten, observe that the digit in the ones place is 9. Since this digit is 5 or greater, we add 1 to the digit in the tens place. The number 3829.34 rounded to the nearest ten is 3830.
- **41.** To round 42,650.14 to the nearest one, observe that the digit in the tenths place is 1. Since this digit is less than 5, we do not add 1 to the digit in the ones place. The number 42,650.14 rounded to the nearest one is 42,650. The amount is \$42,650.
- **45.** To round 0.1992 to the nearest hundredth, observe that the digit in the thousandths place is 9. Since this digit is 5 or greater, we add 1 to the digit in the hundredths place. The number 0.1992 rounded to the nearest hundredth is 0.2. The amount is \$0.20.
- **49.** To round 1.725 to the nearest hundredth, observe that the digit in the thousandths place is 5. Since this digit is 5 or greater, we add 1 to the digit in the hundredths place. The number 1.725 rounded to the nearest hundredth is 1.73. The time is 1.73 hours.
- **53.** To round 89.3559 to the nearest tenth, observe that the digit in the hundredths place is 5. Since this digit is 5 or greater, we add 1 to the digit in the tenths place. The number 89.3559 rounded to the nearest tenth is 89.4. The population density is 89.4 people per square mile.
- **57.** To round 0.4667 to the nearest tenth, observe that the digit in the hundredths place is 6. Since this digit is 5 or greater, we add 1 to the digit in the tenths place. The number 0.4667 rounded to the nearest tenth is 0.5. The time is 0.5 minute.

- **61.** 94
 - $\frac{-23}{71}$
- **65.** To round 2849.1738 to the nearest hundred, observe that the digit in the tens place is 4. Since this digit is less than 5, we do not add 1 to the digit in the hundreds place. The number 2849.1738 rounded to the nearest hundred is 2800, which is choice **b**.
- **69.** Comparing each place value, we see that Audi Sport North America's 2010 average speed of 225.228 kilometers per hour is the fastest on the list.

$$225.228 = 225 \frac{228}{1000} = 225 \frac{57}{250}$$

73. answers may vary

- **77.** 0.26499 and 0.25786 rounded to the nearest hundredths are 0.26, 0.26559 rounds to 0.27 and 0.25186 rounds to 0.25.
- **81.** Round to the nearest hundred million and then add.

| 2800 | |
|------|--|
| 2200 | |
| 2100 | |
| 1700 | |
| 1500 | |
| 1500 | |

$$+ 1500 \\ 11.800$$

The total amount of money is estimated as \$11,800 million.

Exercise Set 4.3

| Excicise Set 4.5 | | 1 |
|---------------------------|------------------|-------------------------------|
| 1. 1.3 | 5. 0.003 | 9. ¹ 490.00 |
| +2.2 | + 0.091 | + 93.09 |
| 3.5 | 0.094 | 583.09 |
| | Estimate: 100 | |
| 6.080 | 6 | |
| $\frac{+ 9.034}{115.123}$ | $\frac{+9}{115}$ | |
| 17. 45.023 | | Check: 15.3^{1} |
| 3.006 | $\frac{-2.7}{}$ | |
| $\frac{+ 8.403}{56.432}$ | 15.3 | |
| 25. Exact: 5.90 E | stimate: 6 Check | 1.83 |
| - 4.07 | - 4 | + 4.07 |
| 1.83 | $\frac{-4}{2}$ | 5.90 |
| 29. 500.34 Che | ck: 376.89 | |
| - 123.45 | + 123.45 | |
| 376.89 | 500.34 | |
| 33. 200.0 Chec | ck: 194.4 | |
| <u> </u> | + 5.6 | |
| 194.4 | 200.0 | |
| 37. 23.0 Check | 11.116.3 | |
| - 6.7 | + 6.7 | |
| 16.3 | 23.0 | |
| | | |

- **41.** 86.050 **45.** 150.00

 -1.978 -93.17

 84.072 56.83
- **49.** Two \$20 bills total \$40.

$$40.00$$

 -32.48
 7.52

- Her change was \$7.52.
- **53.** The phrase "By how much did the price change" indicates that we should subtract the lower price from the higher price.
 - 2.979

The price changed by \$0.14.

- **57.** To find the perimeter, we add the lengths of the sides. Opposite sides of a rectangle have the same length.
 - 1.14
 - 1.14
 - 1.24
 - +1.24
 - 4.76

The perimeter is 4.76 inches.

- **61.** Since the February 2017 average temperature is 7.3 degrees Fahrenheit above the 20th-century average for February, we subtract to find the 20th-century average for February.
 - 41.2
 - 7.3
 - 33.9

The 20th-century average temperature for February is 33.9 degrees Fahrenheit.

- **65.** To find perimeter, we add the lengths of the sides. Opposite sides of a rectangle have the same length.
 - 5.44
 - 5.44
 - 2.64 + 2.64
 - $\frac{+2.64}{16.16}$

The perimeter is 16.16 inches.

- **69.** The phrase "Find the decrease" indicates that we should subtract the monthly text messages in 2016 from the monthly text messages in 2010.
 - 187.7
 - -158.3

29.4

The number of text messages decreased by 29.4 billion (29,400,000,000) from 2010 to 2016.

- 73. Add the lengths of the sides to get the perimeter.
 - $11 \\ 12.40$
 - 29.34
 - + 25.70
 - 67.44

67.44 feet of border material is needed.

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77. The phrase "Find the total" indicates that we should add the durations of the flights.

| $\frac{212}{330}$ | | |
|-------------------|----|----|
| 94 | .5 | 67 |

- 147.000
- + 142.900
 - 715.050

James A. Lovell spent 715.05 hours in spaceflight.

- **81.** The greatest chocolate consumption shown in the table is 19.8 pounds per year for Switzerland. The least chocolate consumption shown in the table is 14.6 pounds per year for Norway.
 - 19.8
 - -14.6
 - 5.2

The greatest chocolate consumption shown in the table is 5.2 pounds per person per year more than the least.

- **85.** 23
 - $\times 2$ 46
- **89.** $\left(\frac{2}{3}\right)^2 = \frac{2}{3} \cdot \frac{2}{3} = \frac{2 \cdot 2}{3 \cdot 3} = \frac{4}{9}$
- **93.** 10.68 (2.3 + 2.3) = 10.68 4.60 = 6.08The unknown length is 6.08 inches.
- 97. 1 dime, 1 nickel, and 2 pennies: 0.10 + 0.05 + 0.01 + 0.01 = 0.173 nickels and 2 pennies: 0.05 + 0.05 + 0.05 + 0.01 + 0.01 = 0.171 dime and 7 pennies: 0.10 + 0.01 + 0.01 + 0.01 + 0.01 + 0.01 + 0.01 + 0.01 = 0.172 nickels and 7 pennies: 0.05 + 0.05 + 0.01 + 0.01 + 0.01 + 0.01 + 0.01 + 0.01 + 0.01 = 0.17
- **101.** answers may vary

Exercise Set 4.4

| Exer | cise Set 4 | 1.4 | | | | |
|------|------------------|------------------|------------|----------------|---------|------------|
| 1. | 0.2 | 5. | 0.26 | | 9. | 0.576 |
| | $\times 0.6$ | | \times 5 | | 2 | × 0.7 |
| | 0.12 | | 1.30 0 | or 1.3 | (| 0.4032 |
| 13. | 490.2 | | | 17. 6.5 | × 10 = | = 65 |
| | $\times 0.023$ | | | | | |
| | 14706 | | | | | |
| | 98040 | | | | | |
| | 11.2746 | | | | | |
| 21. | 7.2×0.0 | 01 = 0.072 | 2 | | | |
| 25. | 6.046 \times | 1000 = 60 |)46 | | | |
| 29. | 0.123 | | | 33. | 8.6 | |
| | \times 0.4 | | | \times (|).15 | |
| | 0.0492 | | | | 430 | |
| | | | | | 860 | |
| | | | | 1. | 290 or | 1.29 |
| 37. | 526.3 \times | 0.001 = 0 | .5263 | | | |
| 41. | 5.5 billio | $n = 5.5 \times$ | 1 billi | on | | |
| | | $= 5.5 \times$ | 1,000, | 000,000 | | |
| | | = 5,500 | ,000,00 | 0 | | |
| | The silos | s hold enou | igh to i | make 5,50 | 00,000, | ,000 bars. |

45. 292.3 thousand = 292.3×1 thousand $= 292.3 \times 1000$ = 292.300

292,300 people visited the park each week.

- **49.** Circumference = $\pi \cdot$ diameter
 - $C = \pi \cdot 10 = 10\pi$
 - $C \approx 10(3.14) = 31.4$

The circumference is 10π centimeters, which is approximately 31.4 centimeters.

- 53. Multiply his hourly wage by the number of hours worked. 17.88
 - \times 40
 - 715.20
 - His pay for last week was \$715.20.
- **57.** Multiply the number of ounces by the number of grams of saturated fat in 1 ounce.
 - 6.2
 - \times 4
 - 24.8

There are 24.8 grams of saturated fat in 4 ounces of cream cheese.

Cit 1. 61

| 61. | Circumference = $\pi \cdot \text{diameter}$ |
|-----|--|
| | $C = \pi \cdot 250 = 250\pi$ |
| | 250 |
| | \times 3.14 |
| | 1000 |
| | 2500 |
| | 75000 |
| | 785.00 |
| | The circumference is 250π feet, which is approximately |
| | 785 feet. |
| 65. | Multiply her height in meters by the number of inches in |
| .17 | 1 meter. |
| | 39.37 |
| | \times 1.65 |
| | 19685 |
| | 236220 |
| | 393700 |
| | 64.9605 |
| | She is approximately 64.9605 inches tall. |
| 69. | 5.3 |
| | $\frac{\times 8}{42.4}$ |
| | 42.4 |
| | The area is 42.4 square inches. |
| | |
| 73. | 56)2016 |
| | <u>-168</u> |
| | 336 |
| | <u>-336</u> |
| | 0 |
| 77. | $\frac{24}{7} \div \frac{8}{21} = \frac{24}{7} \cdot \frac{21}{8} = \frac{24 \cdot 21}{7 \cdot 8} = \frac{3 \cdot 8 \cdot 3 \cdot 7}{7 \cdot 8} = \frac{3 \cdot 3}{1} = 9$ |
| | |
| 81. | 3.60 |
| | $\frac{-0.04}{2.56}$ |
| | 3.56 |

| | 85. 20.6 | 0.0055 |
|--------------|--|---|
| | $\times 1.86$ | 33. 3.78)0.02079 becomes 378)2.0790 |
| | 1236 | <u>- 1 890</u> |
| | 16480 | 1890 |
| e S | 20600 | - 1890 |
| N. | 38.316 | 0 |
| L
L | $38.316 \times 100,000 = 3,831,600$ | $23.869 \approx 23.87$ |
| Exercises | Radio waves travel 3,831,600 miles in 20.6 seconds. | 37. $0.023\overline{)0.549}$ becomes $23\overline{)549.000}$ |
| | 89. answers may vary | -46 |
| σ | Exercise Set 4.5 | |
| te - | 4.6 300 | |
| 6 | 1. $3\overline{)13.8}$ 5. $0.06\overline{)18}$ becomes $6\overline{)1800}$ | $\frac{-69}{200}$ |
| Selected | $\frac{-12}{-18}$ | |
| S | $\frac{12}{18}$ $\frac{10}{000}$ | $\frac{-184}{160}$ |
| 2 | | 1 60 |
| S | $\frac{18}{0}$ | $\frac{-138}{222}$ |
| | 0 | 220 |
| Ę | 6.6 | |
| Solutions to | 9. Exact: 5.5)36.3 becomes 55)363.0 | 13 |
| So | - 330 | 41. $\frac{54.982}{100} = 0.54982$ 45. $\frac{12.9}{1000} = 0.0129$ |
| | 33 0 | |
| | <u>- 33 0</u> | 49. $\frac{13.1}{10} = 1.31$ 53. $\frac{456.25}{10,000} = 0.045625$ |
| | 0 | 10 10,000
202.14 \approx 202.1 |
| | 6 | $202.14 \sim 202.1$
57. 39)7883.50 |
| | Estimate: $6\overline{)36}$ | |
| | 0.045 | $\frac{-78}{08}$ |
| | 13. 12)0.540 | |
| | <u>- 48</u> | $\frac{-0}{2}$ |
| | 60 | 83 |
| | -60 | $\frac{-78}{55}$ |
| | 0 | |
| | 4.8 | $\frac{-39}{160}$ |
| | 17. $0.27\overline{)1.296}$ becomes $27\overline{)129.6}$ | |
| | $\frac{-108}{2}$ | $\frac{-156}{4}$ |
| | 21 6 | She needs to buy 202.1 pounds of fertilizer. |
| | $\frac{-216}{2}$ | 61. Divide the number of crayons by 64. |
| | 0 | 11.40 rounded to the nearest tenth is 11.4 boxes. |
| | 30. | 64)730.00 |
| | 21. $0.6\overline{)18}$ becomes $6\overline{)180}$. | -64 |
| | $\frac{-18}{200}$ | 90 |
| | 00 9.8 | <u>-64</u> |
| | 25. Exact: 7.2)70.56 becomes 72)705.6 | $\frac{-01}{260}$ |
| | | -25 6 |
| | $\frac{-648}{576}$ | 40 |
| | | 65. From Exercise 63 , we know that there are 24 teaspoons in |
| | $\frac{-576}{0}$ | 4 fluid ounces. Thus, there are 48 half teaspoons (0.5 tsp) |
| | 0 | or doses in 4 fluid ounces. To see how long the medicine |
| | Estimate: 7)70 | will last if a dose is taken every 4 hours, there are |
| | 45 | $24 \div 4 = 6$ doses taken per day. |
| | 29. $0.027\overline{)1.215}$ becomes $27\overline{)1215}$ | $48 \text{ (doses)} \div 6 \text{ (per day)} = 8 \text{ days.}$ |
| | <u>- 108</u> | The medicine will last 8 days. |
| | | |
| | - 135 | |
| | 0 | |
| | U U | |

| 69. Divide the number of kilometers by the number of hours. $24.06\overline{)5233.5}$ becomes | 113. The rancher will need 4 times the perimeter of th corral. |
|---|--|
| | |
| $217.51 \approx 217.5$ | 24.280 |
| 2406)523350.00 | 24.280 |
| -4812 | 15.675 |
| 4215 | + 15.675 |
| -2406 | 79.910 |
| 18090 | The perimeter is 79.91 meters. |
| | 79.91 |
| -16842 | |
| 12480 | $\frac{\times 4}{2}$ |
| -12030 | 319.64 |
| 4500 | The rancher will need 319.64 meters of wire. |
| -2406 | Exercise Set 4.6 |
| | 0.2 0.75 |
| 2094 | |
| The average speed was 217.5 kilometers per hour. | 1. $5\overline{)1.0}$ $\frac{1}{5} = 0.2$ 5. $4\overline{)3.00}$ $\frac{-10}{0}$ $\frac{-28}{20}$ $\frac{3}{4} = 0.75$ |
| 73. $0.7(6 - 2.5) = 0.7(3.5) = 2.45$ | $\frac{-10}{5}$ 5 $\frac{-28}{3}$ $\frac{3}{-0.75}$ |
| 77. $30.03 + 5.1 \times 9.9 = 30.03 + 50.49 = 80.52$ | $\frac{-10}{0} \frac{-28}{20} \frac{3}{4} = 0.75$ |
| 81. $93.07 \div 10 \times 100 = 9.307 \times 100 = 930.7$ | |
| 85. $5(20.6 - 2.06) - (0.8)^2 = 5(18.54) - (0.8)^2$ | $\frac{-20}{0}$ |
| = 5(18.54) - 0.64 | 1.2 |
| = 92.70 - 0.64 | |
| = 92.06 | 9. 5)6.0 |
| | $\frac{-5}{10}$ $\frac{6}{5} = 1.2$ |
| 89. $0.9 = \frac{9}{10}$ | $\frac{-1}{10}$ $\frac{-5}{5} = 1.2$ |
| | |
| 4.26 | $\frac{-10}{0}$ |
| 93. $0.3\overline{)1.278}$ becomes $3\overline{)12.78}$ | 0 |
| - 12 | |
| $\frac{-12}{07}$ | 0.425 |
| | |
| $\frac{-6}{18}$ | 13. $40\overline{)17.000} = 160 \qquad \frac{17}{40} = 0.425$ |
| 18 | -160 40 0.120 |
| - 18 | 100 |
| $\frac{-18}{0}$ | - 80 |
| $1.278 \div 0.3 = 4.26$ | |
| 97. 8.6 | 200 |
| | 200 |
| \times 3.1 | 0 |
| 86 | |
| 2580 | 0.333 |
| 26.66 | 17. 3) $\overline{1.000}$ 1 $0\overline{2}$ |
| | 17. 3)1.000
-9 $\frac{1}{3} = 0.\overline{3}$ |
| 101. 8.62×41.7 is approximately $9 \times 40 = 360$, which is | |
| choice c. | 10 |
| 105. Add the numbers, then divide by 4. | <u>-9</u> |
| 2
86 | 10 |
| | |
| 78 | $\frac{9}{1}$ |
| 91 | |
| | 0.636363 |
| + 87 | |
| $\frac{+87}{342}$ | 21. 11)7.000000 7 $-0\overline{62}$ |
| 342 | 21. 11)7.000000 $\frac{7}{11} = 0.\overline{63}$ |
| 342
85.5 | |
| 342
85.5
4)342.0 | 40 |
| 342
85.5
4)342.0 | |
| 342
85.5
4)342.0
- 32 | 40 |
| 342 85.5 4)342.0 $ -32 22 $ | $ \begin{array}{r} \underline{} $ |
| $ \begin{array}{r} 342 \\ \underline{85.5} \\ 4)342.0 \\ \underline{-32} \\ 22 \\ \underline{-20} \end{array} $ | $ \begin{array}{r} \underline{-33}\\ \underline{-66} \end{array} $ |
| $ \begin{array}{r} 342 \\ 85.5 \\ 4)\overline{342.0} \\ -32 \\ 22 \\ -20 \\ 20 \end{array} $ | $ \begin{array}{r} -33 \\ -66 \\ 40 \end{array} $ |
| $ \begin{array}{r} 342 \\ 85.5 \\ 4)\overline{342.0} \\ -32 \\ 22 \\ -20 \\ 20 \end{array} $ | $ \begin{array}{r} $ |
| $ \begin{array}{r} 342 \\ 85.5 \\ 4)\overline{342.0} \\ -32 \\ 22 \\ -20 \\ 20 \end{array} $ | $ \begin{array}{r} -33 \\ -66 \\ 40 \end{array} $ |
| $ \begin{array}{r} 342 \\ 85.5 \\ 4)342.0 \\ -32 \\ 22 \\ -20 \\ 2 \\ 0 \\ 0 \end{array} $ | $ \begin{array}{r} -33 \\ -33 \\ 70 \\ -66 \\ 40 \\ -33 \\ 70 \\ \end{array} $ |
| $ \begin{array}{r} 342\\ 85.5\\ 4)342.0\\ -32\\ 22\\ -20\\ 20\\ 20\\ 20\\ 0\\ The average is 85.5. \end{array} $ | $ \begin{array}{r} $ |
| $ \begin{array}{r} 342 \\ 85.5 \\ 4)342.0 \\ -32 \\ 22 \\ -20 \\ 20 \\ 20 \\ 0 \\ \end{array} $ The average is 85.5. | $ \begin{array}{r} -33 \\ -66 \\ 40 \\ -33 \\ 70 \\ -66 \\ 40 \\ -33 \\ 70 \\ -66 \\ 40 \end{array} $ |
| $ \begin{array}{r} 342 \\ 85.5 \\ 4)342.0 \\ -32 \\ 22 \\ -20 \\ 2 \\ 0 \\ 0 \end{array} $ | $ \begin{array}{r} $ |

0.624

| | 25. | $125\overline{)78.000}$ 78 - 0.624 |
|--|-----|---|
| | 201 | $\frac{725}{-750} \frac{76}{125} = 0.624$ |
| | | $\frac{-750}{300}$ 125 |
| S | | - 2 50 |
| š | | 500 |
| U
L | | - 500 |
| Å | | 0 |
| ш | | |
| Solutions to Selected Exercises | 29. | $\frac{7}{16} = 0.4375 \approx 0.44$ |
| ž | | $0.615 \approx 0.62$ |
| ð | 33. | $\begin{array}{r} 91\overline{)56.000} \\ -54.6 \end{array} \qquad \qquad \frac{56}{91} \approx 0.62 \end{array}$ |
| U | | $-546 \qquad \qquad \overline{91} \approx 0.02$ |
| 0 | | 1 40 |
| Ť | | <u>- 91</u> |
| ns | | 490 |
| <u>.</u> | | - 455 |
| Ħ | | 35 |
| 0 | | $\frac{0.02}{50\sqrt{1.00}}$ $\frac{1}{50} = 0.02$ |
| S | 37. | 50/1.00 50 |
| | | -100 |
| | | 0
0.215 |
| | 41 | 200)43.000 |
| | | -400 |
| | | 3 00 |
| | | -200 |
| | | 1 000 |
| | | -1000 |
| | | 0 |
| | | $0.215 = \frac{43}{200}$ |
| | | |
| | 47 | $0.833\ldots$ |
| | 45. | 6)5.000 |
| | | $\frac{-48}{20}$ |
| | | - 18 |
| | | $\frac{10}{20}$ |
| | | |
| | | $\frac{-18}{2}$ |
| | | |
| | | $\frac{5}{6} = 0.8\overline{3}$ and $0.\overline{6} < 0.8\overline{3}$, so $0.\overline{6} < \frac{5}{6}$. |
| | | 0.11 |
| | 49. | 9)1.00 |
| | | $\frac{-9}{10}$ |
| | | |
| | | $\frac{-9}{1}$ |
| | | 1 |
| | | $\frac{1}{9} \approx 0.11 \text{ and } 0.11 > 0.1, \text{ so } \frac{1}{9} > 0.1$ |
| | | |

7.125 **53.** 64)456.000 - 448 80 - 64 1 60 - 1 28 320 <u>- 3</u>20 $\frac{456}{64}$ = 7.125 and 7.123 < 7.125, so 7.123 < $\frac{456}{64}$ **57.** 0.49 = 0.4900.49, 0.491, 0.498 **61.** $\frac{4}{7} \approx 0.571$ $0.412, 0.453, \frac{4}{7}$ **65.** $\frac{12}{5} = 2.400$ 2.37 = 2.370 $\frac{17}{8} = 2.125$ $\frac{17}{8}$, 2.37, $\frac{12}{5}$ **69.** Area = $\frac{1}{2}$ · base · height $=\frac{1}{2}\cdot 5.2\cdot 3.6$ $= 0.5 \cdot 5.2 \cdot 3.6$ = 9.36 The area is 9.36 square centimeters. **73.** $2^3 = 2 \cdot 2 \cdot 2 = 8$ **77.** $\left(\frac{1}{3}\right)^4 = \frac{1}{3} \cdot \frac{1}{3} \cdot \frac{1}{3} \cdot \frac{1}{3} = \frac{1}{81}$ **81.** $\left(\frac{2}{5}\right)\left(\frac{5}{2}\right)^2 = \frac{2}{5} \cdot \frac{5}{2} \cdot \frac{5}{2} = \frac{5}{2}$ **85.** 1.00001 > 1 **89.** The fraction of stations with an all sports format is $\frac{582}{10,181}$. $0.0571 \approx 0.057$ 10181)582.0000 -5090572 950 <u>-71</u>267 16830 -101816649 $\frac{582}{10,181} \approx \ 0.057$ **93.** answers may vary **97.** $(9.6)(5) - \frac{3}{4} = (9.6)(5) - 0.75$ = 48 - 0.75= 47.25 **101.** $\frac{3}{8}(5.9 - 4.7) = 0.375(5.9 - 4.7)$ = 0.375(1.2)= 0.45

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Chapter 4 Test

- 1. 45.092 in words is forty-five and ninety-two thousandths.
- 5. Since 0 < 9 in the tenths place, 25.0909 < 25.9090.
- 0.65 9. 20)13.00 **13.** 20.0 - 8.6 - 12 0 1 00 11.4 -1.000 $\frac{13}{20} = 0.65$ 6.6728 ≈ 6.673 **17.** 7)46.7100 _42 47 -4251 -4920 -1460 <u>-56</u> 4 **21.** $\frac{0.23 + 1.63}{0.3} = \frac{1.86}{0.3}$ 6.2 0.3)1.86 becomes 3)18.6 -1806 - 6 0 $\frac{0.23 + 1.63}{0.3} = 6.2$ **25. a.** 123.8 \times 80 9904.0 The area of the lawn is 9904 square feet. **b.** Multiply the number of square feet by the number of ounces per square foot. 9904 $\times 0.02$
 - 198.08

198.08 ounces of insecticide are needed.

Chapter 5

Exercise Set 5.1

- **1.** The ratio of 11 to 14 is $\frac{11}{14}$.
- 5. The ratio of 151 to 201 is $\frac{151}{201}$.
- 9. The ratio of 5 to $7\frac{1}{2}$ is $\frac{5}{1}$.

$$\frac{2}{7}$$
 7 $\frac{1}{2}$

13. The ratio of 16 to 24 is
$$\frac{16}{24} = \frac{8 \cdot 2}{8 \cdot 3} = \frac{2}{3}$$
.

17. The ratio of 4.63 to 8.21 is
$$\frac{4.63}{8.21} = \frac{4.63 \cdot 100}{8.21 \cdot 100} = \frac{463}{821}$$
.
21. The ratio of 10 hours to 24 hours is
 $\frac{10 \text{ hours}}{24 \text{ hours}} = \frac{10}{24} = \frac{2 \cdot 12}{2 \cdot 12} = \frac{5}{12}$.
25. The ratio of 24 days to 14 days is
 $\frac{24 \text{ days}}{14 \text{ days}} = \frac{24}{14} = \frac{2 \cdot 12}{2 \cdot 7} = \frac{17}{7}$.
29. The ratio of 8 inches to 20 inches is
 $\frac{8 \text{ inches}}{20 \text{ inches}} = \frac{8}{20} = \frac{4 \cdot 2}{4 \cdot 5} = \frac{2}{5}$.
33. The ratio of $7\frac{3}{5}$ hours to $1\frac{9}{10}$ hours is
 $\frac{7\frac{3}{5}}{1\frac{9}{10}}$ hours $= 7\frac{3}{5}$
 $\frac{9}{10}$
 $= 7\frac{3}{5} \div 1\frac{9}{10}$
 $= 3\frac{38}{5} \div \frac{19}{10}$
 $= \frac{38}{5} \div \frac{19}{10}$
 $= \frac{38}{5} \div \frac{19}{10}$
 $= \frac{19 \cdot 2 \cdot 5 \cdot 2}{5 \cdot 19}$
 $= \frac{4}{1}$
37. The perimeter of the mural is
 $2L + 2W = 2(32 \text{ feet}) + 2(19 \text{ feet})$
 $= 64 \text{ feet} + 38 \text{ feet}$
 $= 102 \text{ feet}$.
The ratio of the width to the perimeter is
 $\frac{322 \text{ feet}}{102} = \frac{32}{102} = \frac{2 \cdot 16}{2 \cdot 51} = \frac{16}{51}$.
41. The ratio of women to men is $\frac{125}{100} = \frac{25 \cdot 5}{25 \cdot 4} = \frac{5}{4}$.
45. The perimeter of the billboard is
 $8 \text{ feet} + 15 \text{ feet} + 17 \text{ feet} = 40 \text{ feet}$.
The ratio of the longest side to the perimeter of the
billboard is $\frac{17 \text{ feet}}{40 \text{ feet}} = \frac{17}{40}$.
49. The ratio of mountains over 14,000 \text{ feet tall
found in Alaska to those found in Colorado is
 $\frac{19 \text{ mountains}}{57 \text{ mountains}} = \frac{19}{19 \cdot 3} = \frac{1}{3}$.
53. There is 50 - 49 = 1 \text{ state without Target stores. The
of states without Target stores to states with Target stores. The

ratio ores is $\frac{1}{4}$

$$\frac{1 \text{ state}}{49 \text{ states}} = \frac{1}{49}.$$
0.15

57. 3.7)0.555 becomes 37)5.55

$$\frac{-37}{185} \\ \frac{-185}{0}$$

| | 61. 30 : 1 should be read as "the ratio of thirty to one." | 4.750.720 |
|--------------------|---|--|
| | 65. $\frac{\$3}{\$2}$ is not in simplest form: $\frac{\$3}{\$2} = \frac{3}{2}$. | 4,758,720 residents for 64 parishes is $\frac{74,555}{1}$ residents or 74,355 residents/parish. |
| | 69. $4\frac{1}{2}$ is not in simplest form: $4\frac{1}{2} = \frac{9}{2}$. | 8,200,350 |
| Selected Exercises | 73. a. The ratio of states with primary hand-held cell phone | 25. $20\overline{)164,007,000}$ |
| Ū. | laws to total U.S. states is | $\frac{-160}{40}$ |
| er | $\frac{14 \text{ states}}{50 \text{ states}} = \frac{14}{50} = \frac{2 \cdot 7}{2 \cdot 25} = \frac{7}{25}.$ | -40 |
| <u> </u> | | |
| D | b. There are 50 states -14 states $= 36$ states without primary hand-held cell phone laws. | -0 |
| ť | c. The ratio of states with primary hand-held cell phone | 07 |
| ē | laws to states without such laws is | $\frac{-0}{70}$ |
| | $\frac{14 \text{ states}}{36 \text{ states}} = \frac{14}{36} = \frac{2 \cdot 7}{2 \cdot 18} = \frac{2}{18}.$ | |
| 2 | | $\frac{-60}{100}$ |
| s | Exercise Set 5.2 | -100 |
| - O | 1. The rate of 5 shrubs every 15 feet is $\frac{5 \text{ shrubs}}{15 \text{ feet}} = \frac{1 \text{ shrub}}{3 \text{ feet}}$. | 0 |
| Solutions to | 5. The rate of 6 laser printers for 28 computers is | \$8,200,350 |
| 0 | $\frac{6 \text{ laser printers}}{28 \text{ computers}} = \frac{3 \text{ laser printers}}{14 \text{ computers}}.$ | \$164,007,000 for 20 players is $\frac{\$8,200,350}{1 \text{ player}}$ or
\$8,200,350/player. |
| U | | \$8,200,550/player. |
| | 9. The rate of 6 flight attendants for 200 passengers is
6 flight attendants 3 flight attendants | 65,000 |
| | $\frac{6 \text{ flight attendants}}{200 \text{ passengers}} = \frac{3 \text{ flight attendants}}{100 \text{ passengers}}.$ | 29. 400)26,000,000 |
| | 110 | $\frac{-24\ 00}{2\ 000}$ |
| | 13. 3)330 | -2000 |
| | | 0 |
| | $\frac{-3}{03}$ | \$65.000 |
| | $\frac{-3}{0}$ | \$26,000,000 for 400 species is $\frac{$65,000}{1 \text{ species}}$ or \$65,000/species |
| | - | 8.70 ≈ 8.7 |
| | 330 calories in a 3-ounce serving is $\frac{110 \text{ calories}}{1 \text{ ounce}}$ or | 33. 24)209.00 |
| | 110 calones/ounce. | <u>- 192</u> |
| | 17. 1 minute = 60 seconds 90 | 170 |
| | 60)5400 | $\frac{-168}{20}$ |
| | <u>- 540</u> | - 0 |
| | 00 | 20 |
| | $\frac{-0}{0}$ | 8.7 tornadoes |
| | 5400 wingbeats 5400 wingbeats | 209 tornadoes in 24 hours is about $\frac{6.7 \text{ tornadoes}}{1 \text{ hour}}$ or 8.7 tornadoes/hour. |
| | $\frac{1}{1 \text{ minute}} = \frac{1}{60 \text{ seconds}}$ | |
| | = 90 wingbeats | 27.58 ≈ 27.6 |
| | 1 second | 37. a. 14.5)400 becomes 145)4000.00 |
| | = 90 wingbeats/second | $\frac{-290}{1100}$ |
| | 74,355 | - 1015 |
| | 21. 64)4,758,720
-4 48 | 85 0 |
| | 278 | <u>- 72 5</u> |
| | -256 | 12 50 |
| | 22.7 | $\frac{-11\ 60}{90}$ |
| | $\frac{-192}{252}$ | |
| | 3 52
-3 20 | The unit rate for the car is approximately 27.6 miles/gallon. |
| | $\frac{-320}{320}$ | |
| | <u>-320</u> | |
| | 0 | |
| | | |

 $29.18 \approx 29.2$ **53.** 3.7 **b.** 9.25)270 becomes 925)27000.00 imes 1.2- 1850 74 8500 4.44 - 8325 175 0 - 92 5 82 50 -74008 50 The unit rate for the truck is approximately 29.2 miles/gallon. c. Since the unit rate of the truck is larger, the truck gets better gas mileage. 0.17 **41.** 7)1.19 - 7 49 - 49 0 The unit price is \$0.17 per banana. $0.1056 \approx 0.106$ **45.** 16)1.6900 -16 09 -090 -80100 __96 4 The 16-ounce size costs about \$0.106 per ounce. 0.115 9. 6)0.690 _ 6 09 13. - 6 30 - 30 false 0 The 6-ounce size costs \$0.115 per ounce. 21. The 16-ounce size is the better buy. $0.0059 \approx 0.006$ **49.** 100)0.5900 false - 500 900 <u>- 900</u> 25. 0 The 100-count napkins cost about \$0.006 per napkin. $0.0051~\approx~0.005$ 180)0.9300 $\frac{12}{5} \cdot \frac{1}{4} \stackrel{?}{=} \frac{10}{9} \cdot \frac{2}{3}$ -900300 $\frac{3}{5} \neq \frac{20}{27}$ -180120 false

The 180-count napkins cost about \$0.005 per napkin. The 180-count package is the better buy.

370 **57.** 29,543 - 29,286 = 257 $19.17 \approx 19.2$ 13.4)257 becomes 134)2570.00 -134 1230 -1206240-13410 60 -938 1 22 There were 257 miles driven and the miles per gallon were 19.2. $1.50 \approx 1.5$ **61.** 7759)11,674.00 -77593 915 0 -3 879 5 35 50 The unit rate is 1.5 steps/foot. 65. no; answers may vary **Exercise Set 5.3** 1. $\frac{10 \text{ diamonds}}{5 \text{ diamonds}} = \frac{5 \text{ diamonds}}{5 \text{ diamonds}}$ 6 opals 3 opals 5. $\frac{6 \text{ eagles}}{58 \text{ sparrows}} = \frac{3 \text{ eagles}}{29 \text{ sparrows}}$ $\frac{22 \text{ vanilla wafers}}{1 \text{ cup cookie crumbs}} = \frac{55 \text{ vanilla wafers}}{2.5 \text{ cups cookie crumbs}}$ $\frac{8}{6} \stackrel{?}{=} \frac{9}{7}$ $\frac{5}{8} \stackrel{?}{=} \frac{625}{1000}$ 17. $8 \cdot 7 \stackrel{?}{=} 9 \cdot 6$ $5 \cdot 1000 \stackrel{?}{=} 8 \cdot 625$ 56 ≠ 54 5000 = 5000true $\frac{8}{10} \stackrel{?}{=} \frac{5.6}{0.7}$ $8(0.7) \stackrel{?}{=} 10(5.6)$ 5.6 ≠ 56 $\frac{2\frac{2}{5}}{\frac{2}{3}} \stackrel{?}{=} \frac{1\frac{1}{9}}{\frac{1}{4}}$ $2\frac{2}{5} \cdot \frac{1}{4} \stackrel{?}{=} 1\frac{1}{9} \cdot \frac{2}{3}$

45. $\frac{24}{n} = \frac{60}{96}$ $24 \cdot 96 = 60 \cdot n$ $2304 = 60 \cdot n$ 38.4 = n

61. 8.01 8.1

| | 29. | $\frac{8}{12} \stackrel{?}{=} \frac{4}{6}$ $8 \cdot 6 \stackrel{?}{=} 12 \cdot 4$ $48 = 48$ |
|--|-----|---|
| Exercises | 33. | true
$\frac{1.8}{2} \stackrel{?}{=} \frac{4.5}{5}$ $1.8(5) \stackrel{?}{=} 4.5(2)$ $9 = 9$ true |
| Selected | 37. | $\frac{n}{5} = \frac{6}{10}$ $10 \cdot n = 6 \cdot 5$ $10 \cdot n = 30$ $n = 3$ |
| Solutions to Selected Exercises | 41. | $\frac{n}{8} = \frac{50}{100}$ $100 \cdot n = 8 \cdot 50$ $100 \cdot n = 400$ $n = 4$ |
| 20 | 49. | $\frac{0.05}{12} = \frac{n}{0.6}$ |
| | 53. | $0.05(0.6) = 12 \cdot n$
$0.03 = 12 \cdot n$
0.0025 = n
$\frac{\frac{1}{3}}{\frac{3}{3}} = \frac{\frac{2}{5}}{\frac{5}{n}}$
$\frac{\frac{1}{3}}{\frac{1}{3}} \cdot n = \frac{3}{\frac{2}{5}} \cdot \frac{2}{5}$
$\frac{1}{3} \cdot n = \frac{3}{\frac{2}{20}} \cdot \frac{1}{3}$
$n = \frac{3}{20} \cdot \frac{3}{1}$
$n = \frac{9}{20}$ |
| | 57. | $\frac{n}{1\frac{1}{5}} = \frac{4\frac{1}{6}}{6\frac{2}{3}}$ $\left(6\frac{2}{3}\right)n = \left(1\frac{1}{5}\right)\left(4\frac{1}{6}\right)$ $\frac{20}{3} \cdot n = \frac{6}{5} \cdot \frac{25}{6}$ $\frac{20}{3} \cdot n = \frac{5}{1}$ $n = \frac{5}{1} \div \frac{20}{3}$ $n = \frac{5}{1} \cdot \frac{3}{20}$ $n = \frac{3}{4}$ |
| | | т |

| \uparrow \uparrow |
|---|
| 0 < 1 so |
| 8.01 < 8.1 |
| 65. $5\frac{1}{3} = \frac{16}{3}$ |
| 5 5 |
| $6\frac{2}{3} = \frac{20}{3}$ |
| 5 5 |
| $16 < 20$, so $5\frac{1}{3} < 6\frac{2}{3}$ |
| 69. $\frac{6}{18} = \frac{1}{3}$ |
| 10 5 |
| $\frac{6}{1} = \frac{18}{3}$ |
| 1 5 |
| $\frac{3}{18} = \frac{1}{6}$ |
| $\frac{18}{6} = \frac{3}{1}$ |
| $\overline{6} = \overline{1}$ |
| 73. answers may vary |
| 77. $\frac{n}{5.2} = \frac{0.08}{6}$ |
| $5.2 	 6 \\ 6 \cdot n = 5.2 \cdot 0.08$ |
| $6 \cdot n = 0.416$ |
| $n = \frac{0.416}{6}$ |
| $n = \frac{1}{6}$ |
| $n \approx 0.07$ |
| 81. $\frac{n}{7} = \frac{0}{8}$ 85. $\frac{222}{1515} = \frac{37}{n}$ |
| 7 0 1515 <i>n</i> |
| $8 \cdot n = 0 \cdot 7 \qquad 222 \cdot n = 37 \cdot 1515 \\ 8 \cdot n = 0 \qquad 222 \cdot n = 56,055$ |
| |
| $n = \frac{0}{8}$ $n = \frac{56,055}{222}$ |
| $n = 0 \qquad \qquad n = 252.5$ |
| |
| |
| Exercise Set 5.4 |
| 1. Let <i>n</i> be the number of field goals (baskets) made. |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow 45 = n \leftarrow \text{baskets}$ |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow 5 \cdot 800 = 100 \cdot n$ |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow \frac{45}{800} = 100 \cdot n$
$36,000 = 100 \cdot n$ |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow 5 \cdot 800 = 100 \cdot n$ |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow \frac{100 \cdot n}{36,000} = 100 \cdot n$
$\frac{36,000}{100} = n$
360 = n |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow \frac{100 \cdot n}{36,000} = 100 \cdot n$
$\frac{36,000}{100} = n$
360 = n
He made 360 baskets. |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow \frac{45}{100} = 100 \cdot n$
$\frac{45 \cdot 800 = 100 \cdot n}{36,000} = 100 \cdot n$
$\frac{36,000}{100} = n$
He made 360 baskets.
5. Let <i>n</i> be the number of applications received. |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow \frac{45}{100} = 100 \cdot n$
$\frac{45 \cdot 800 = 100 \cdot n}{36,000} = 100 \cdot n$
$\frac{36,000}{100} = n$
He made 360 baskets.
5. Let <i>n</i> be the number of applications received. |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{attempts}$
$45 \cdot 800 = 100 \cdot n$
$36,000 = 100 \cdot n$
$\frac{36,000}{100} = n$
360 = n
He made 360 baskets.
5. Let <i>n</i> be the number of applications received.
accepted $\rightarrow \frac{2}{7} = \frac{180}{n} \leftarrow \text{accepted}$
applied $\rightarrow 7 \cdot 180$ |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{attempts}$
$45 \cdot 800 = 100 \cdot n$
$36,000 = 100 \cdot n$
$\frac{36,000}{100} = n$
360 = n
He made 360 baskets.
5. Let <i>n</i> be the number of applications received.
accepted $\rightarrow \frac{2}{7} = \frac{180}{n} \leftarrow \text{accepted}$
applied $\rightarrow 77 = \frac{180}{n} \leftarrow \text{applied}$
$2 \cdot n = 7 \cdot 180$
$2 \cdot n = 1260$ |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{attempts}$
$45 \cdot 800 = 100 \cdot n$
$36,000 = 100 \cdot n$
$\frac{36,000}{100} = n$
360 = n
He made 360 baskets.
5. Let <i>n</i> be the number of applications received.
accepted $\rightarrow \frac{2}{7} = \frac{180}{n} \leftarrow \text{accepted}$
applied $\rightarrow 77 = \frac{180}{n} \leftarrow \text{applied}$
$2 \cdot n = 7 \cdot 180$
$2 \cdot n = 1260$ |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow \frac{100 \cdot n}{3600} \leftarrow 100 \cdot n$
$\frac{36,000}{100} = 100 \cdot n$
$\frac{360}{100} = n$
He made 360 baskets.
5. Let <i>n</i> be the number of applications received.
accepted $\rightarrow \frac{2}{7} = \frac{180}{n} \leftarrow \text{accepted}$
applied $2 \cdot n = 7 \cdot 180$
$2 \cdot n = 1260$
$n = \frac{1260}{2}$ |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow 45 \over 100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow 100 = 100 \cdot n$
$36,000 = 100 \cdot n$
36,000 = n
360 = n
He made 360 baskets.
5. Let <i>n</i> be the number of applications received.
accepted $\rightarrow \frac{2}{7} = \frac{180}{n} \leftarrow \text{accepted}$
applied $2 \cdot n = 7 \cdot 180$
$2 \cdot n = 1260$
$n = \frac{1260}{2}$
n = 630 |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow \frac{100 \cdot n}{3600} \leftarrow 100 \cdot n$
$\frac{36,000}{100} = 100 \cdot n$
$\frac{360}{100} = n$
He made 360 baskets.
5. Let <i>n</i> be the number of applications received.
accepted $\rightarrow \frac{2}{7} = \frac{180}{n} \leftarrow \text{accepted}$
applied $2 \cdot n = 7 \cdot 180$
$2 \cdot n = 1260$
$n = \frac{1260}{2}$ |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{attempts}$
$45 \cdot 800 = 100 \cdot n$
$36,000 = 100 \cdot n$
$\frac{36,000}{100} = n$
360 = n
He made 360 baskets.
5. Let <i>n</i> be the number of applications received.
accepted $\rightarrow \frac{2}{7} = \frac{180}{n} \leftarrow \text{accepted}$
applied $\rightarrow 77 \cdot 180$
$2 \cdot n = 7 \cdot 180$
$2 \cdot n = 1260$
$n = \frac{1260}{2}$
n = 630
The school received 630 applications.
9. Let <i>n</i> be the number of square feet required.
floor space $\rightarrow 9 = n \leftarrow \text{floor space}$ |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{attempts}$
$45 \cdot 800 = 100 \cdot n$
$36,000 = 100 \cdot n$
$\frac{36,000}{100} = n$
360 = n
He made 360 baskets.
5. Let <i>n</i> be the number of applications received.
accepted $\rightarrow \frac{2}{7} = \frac{180}{n} \leftarrow \text{accepted}$
applied $\rightarrow \frac{7}{7} = \frac{180}{n} \leftarrow \text{applied}$
$2 \cdot n = 7 \cdot 180$
$2 \cdot n = 1260$
$n = \frac{1260}{2}$
n = 630
The school received 630 applications.
9. Let <i>n</i> be the number of square feet required.
floor space $\rightarrow \frac{9}{1} = \frac{n}{30} \leftarrow \text{floor space}$
students $\rightarrow 1 = \frac{n}{30} \leftarrow \text{students}$ |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{attempts}$
$45 \cdot 800 = 100 \cdot n$
$36,000 = 100 \cdot n$
$\frac{36,000}{100} = n$
360 = n
He made 360 baskets.
5. Let <i>n</i> be the number of applications received.
accepted $\rightarrow \frac{2}{7} = \frac{180}{n} \leftarrow \text{accepted}$
applied $\rightarrow \frac{7}{7} = \frac{180}{n} \leftarrow \text{applied}$
$2 \cdot n = 7 \cdot 180$
$2 \cdot n = 1260$
$n = \frac{1260}{2}$
n = 630
The school received 630 applications.
9. Let <i>n</i> be the number of square feet required.
floor space $\rightarrow \frac{9}{1} = \frac{n}{30} \leftarrow \text{floor space}$
students $\rightarrow 1 = \frac{1}{30} \leftarrow \text{students}$
$9 \cdot 30 = 1 \cdot n$ |
| 1. Let <i>n</i> be the number of field goals (baskets) made.
baskets $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{baskets}$
attempts $\rightarrow \frac{45}{100} = \frac{n}{800} \leftarrow \text{attempts}$
$45 \cdot 800 = 100 \cdot n$
$36,000 = 100 \cdot n$
$\frac{36,000}{100} = n$
360 = n
He made 360 baskets.
5. Let <i>n</i> be the number of applications received.
accepted $\rightarrow \frac{2}{7} = \frac{180}{n} \leftarrow \text{accepted}$
applied $\rightarrow \frac{2}{7} = \frac{180}{n} \leftarrow \text{applied}$
$2 \cdot n = 7 \cdot 180$
$2 \cdot n = 1260$
$n = \frac{1260}{2}$
n = 630
The school received 630 applications.
9. Let <i>n</i> be the number of square feet required.
floor space $\rightarrow \frac{9}{1} = \frac{n}{30} \leftarrow \text{floor space}$
students $\rightarrow 1 = \frac{n}{30} \leftarrow \text{students}$ |

13. Let *n* be the distance between Milan and Rome. kilometers $\rightarrow 30 = n \leftarrow \text{kilometers}$ cm on map $\rightarrow 1^{-1} = 15 \leftarrow$ cm on map

$$30 \cdot 15 = 1 \cdot n$$
$$450 = n$$

Milan and Rome are 450 kilometers apart.

17. Let *n* be the number of hits the player is expected to get.

hits $\rightarrow \frac{3}{8} = \frac{n}{40} \leftarrow$ hits at bats $\rightarrow \frac{3}{8} = \frac{n}{40} \leftarrow$ at hits $3 \cdot 40 = 8 \cdot n$ $120 = 8 \cdot n$ $\frac{120}{8} = n$ 15 = n

The player would be expected to get 15 hits.

21. Let *n* be the number of applications she should expect. applications $\rightarrow 4$ $n \leftarrow$ applications

ounces
$$\rightarrow \overline{3} = \overline{14} \leftarrow \text{ounces}$$

 $4 \cdot 14 = 3 \cdot n$
 $56 = 3 \cdot n$
 $\frac{56}{3} = n$
 $18\frac{2}{3} = n$

She should expect 18 applications from the 14-ounce bottle.

25. Let *n* be the number of servings he can make.

$$\begin{array}{l} \text{milk} \rightarrow \frac{1\frac{1}{2}}{4} = \frac{4}{n} \leftarrow \text{milk} \\ \text{servings} \rightarrow \frac{1}{4} = \frac{4}{n} \leftarrow \text{servings} \\ 1\frac{1}{2} \cdot n = 4 \cdot 4 \\ \frac{3}{2} \cdot n = 16 \\ n = 16 \div \frac{3}{2} \\ n = \frac{32}{3} = 10\frac{2}{3} \\ \text{He can make } 10\frac{2}{3} \text{ servings.} \end{array}$$

29. a. Let *n* be the number of teaspoons of granules needed.

water
$$\rightarrow \frac{25}{1} = \frac{450}{n} \leftarrow \text{water}$$

granules $\rightarrow \frac{25}{1} = \frac{450}{n} \leftarrow \text{granules}$
 $25 \cdot n = 1 \cdot 450$
 $25 \cdot n = 450$
 $n = \frac{450}{25}$
 $n = 18$

18 teaspoons of granules are needed.

b. Let *n* be the number of tablespoons of granules needed.

$$tsp \rightarrow \frac{3}{1} = \frac{18}{n} \leftarrow tsp$$
$$tbsp \rightarrow 1 = \frac{18}{n} \leftarrow tbsp$$
$$3 \cdot n = 1 \cdot 18$$
$$3 \cdot n = 18$$
$$n = \frac{18}{3}$$
$$n = 6$$

6 tablespoons of granules are needed.

33. Let *n* be the estimated head-to-toe height of the Statue of Liberty.

height
$$\rightarrow \frac{n}{42} = \frac{5\frac{1}{3}}{2} \leftarrow$$
 height
arm length $\rightarrow \frac{1}{42} = \frac{5\frac{1}{3}}{2} \leftarrow$ arm length
 $n \cdot 2 = 42 \cdot 5\frac{1}{3}$
 $2 \cdot n = 42 \cdot \frac{16}{3}$
 $2 \cdot n = 224$
 $n = \frac{224}{2}$
 $n = 112$
The estimated height is 112 feet

The estimated height is 112 feet.

$$112 - 111\frac{1}{12} = \frac{11}{12}$$

The difference is $\frac{11}{12}$ foot or 11 inches.

37. Let *n* be the estimated height of the Empire State Building.

height
$$\rightarrow \frac{n}{102} = \frac{850}{69} \leftarrow$$
 height
stories $\rightarrow \frac{102}{69} = \frac{850}{69} \leftarrow$ stories
 $n \cdot 69 = 102 \cdot 850$
 $69 \cdot n = 86,700$
 $n = \frac{86,700}{69}$
 $n \approx 1257$
The height of the Empire State Bu

The height of the Empire State Building is approximately 1257 feet. (The actual height is 1248 feet.)

41. Let *n* be the number of vehicles expected to be SUV crossovers. SUV crossovers $\rightarrow \frac{n}{7,000,000} = \frac{6}{20} \leftarrow \frac{5}{20}$ SUV crossovers vehicles $n \cdot 20 = 7,000,000 \cdot 6$ $20 \cdot n = 42,000,000$ $n = \frac{42,000,000}{20}$ n = 2,100,000 $n \approx 2,000,000$

2,000,000 of the vehicles sold are expected to be SUV crossovers.

45. a. Let *n* be the number of gallons of oil needed.

oil
$$\rightarrow n$$

 $gas \rightarrow 5 = \frac{1}{50} \leftarrow gas$
 $n \cdot 50 = 5 \cdot 1$
 $50 \cdot n = 5$
 $n = \frac{5}{50}$
 $n = \frac{1}{10} = 0.1$
0.1 gallon of oil is needed.
b. 0.1 gallon = 0.1(1 gallon)
 $= 0.1(128 \text{ fluid ounces})$
 $= 12.8 \text{ fluid ounces}$
0.1 gallon is approximately 13 fluid ounces.
49. $3\overline{)15}$
 $15 = 3 \cdot 5$

53.
$$5\overline{)25}$$

 $2\overline{)50}$
 $2\overline{)100}$
 $2\overline{)200}$
 $200 = 2 \cdot 2 \cdot 2 \cdot 5 \cdot 5 = 2^3 \cdot 5^2$
57. Let *n* be the number of ml.
 $mg \rightarrow 15$
 $n = 12$
 $n = 12$
 $n = 12$
 $n = \frac{12}{15}$
 $n = \frac{4}{5} = 0.8$
 0.8 ml of the medicine should be administered.
61. 11 muffins are approximately 1 dozen (12) muffins.
 $1.5 \cdot 8 = 12$
Approximately 12 cups of milk will be needed.
65. answers may vary
Chapter 5 Test
1. $\frac{\$75}{\$10} = \frac{75}{10} = \frac{5 \cdot 15}{5 \cdot 2} = \frac{15}{2}$
5. $\frac{8.6}{10} = \frac{8.6 \cdot 10}{10 \cdot 10} = \frac{80}{100} = \frac{2 \cdot 43}{2 \cdot 50} = \frac{43}{50}$
9. $\frac{8 \text{ inches}}{12 \text{ hours}} = \frac{8}{12} \text{ inch/hour} = \frac{2}{3} \text{ inch/hour}$
 $0.0931 \approx 0.093$
13. $16\overline{)1.4900}$
 $\frac{-144}{50}$
 $\frac{-48}{20}$
 $-\frac{-16}{4}$
The 16-ounce size costs approximately \$0.093/ounce.
 $0.0995 \approx 0.100$
 $24\overline{)2.3900}$
 $\frac{-216}{230}$
 $-\frac{216}{140}$
 $\frac{-120}{20}$

The 24-ounce size costs approximately \$0.100/ounce. The 16-ounce size is the better buy.

 $\frac{n}{3} = \frac{15}{9}$ 17. $9 \cdot n = 3 \cdot 15$ $9 \cdot n = 45$ 45 n =9 n = 5

21.
$$\frac{n}{2\frac{5}{8}} = \frac{1\frac{1}{6}}{3\frac{1}{2}}$$
$$\left(3\frac{1}{2}\right) \cdot n = \left(1\frac{1}{6}\right)\left(2\frac{5}{8}\right)$$
$$\frac{7}{2} \cdot n = \frac{7}{6} \cdot \frac{21}{8}$$
$$\frac{7}{2} \cdot n = \frac{49}{16}$$
$$n = \frac{49}{16} \div \frac{7}{2}$$
$$n = \frac{49}{16} \cdot \frac{2}{7}$$
$$n = \frac{7}{8}$$

1

- **25.** Let n = the number of cartons.
 - $\frac{\text{cartons} \rightarrow n}{\text{hours} \rightarrow 8} = \frac{86}{6} \xleftarrow{} \text{cartons}$ $6 \cdot n = 8 \cdot 86$ $6 \cdot n = 688$ $n = \frac{688}{6}$ $n = 114\frac{2}{3}$ He can pack $114\frac{2}{3}$ cartons in 8 hours.

Chapter 6

Exercise Set 6.1

- **1.** $\frac{96}{100} = 96\%$
- 5. The largest sector corresponds to football, so football was preferred by most adults.
 - 37 = 37%

100 37% of adults prefer football.

- 9. 41% = 41(0.01) = 0.41
- **13.** 100% = 100(0.01) = 1.00 or 1
- **17.** 2.8% = 2.8(0.01) = 0.028
- **21.** 300% = 300(0.01) = 3.00 or 3
- **25.** 38% = 38(0.01) = 0.38 **29.** 45% = 45(0.01) = 0.45
- **33.** 3.1 = 3.1(100%) = 310%
- **37.** 0.003 = 0.003(100%) = 0.3%
- **41.** 5.3 = 5.3(100%) = 530%**45.** 0.3328 = 0.3328(100%) = 33.28%
- **49.** 0.7 = 0.7(100%) = 70%
- **53.** 0.109 = 0.109(100%) = 10.9% **57.** $\frac{1}{4} = \frac{1}{4} \cdot \frac{25}{25} = \frac{25}{100} = 0.25$ **61.** $\frac{9}{10} = \frac{9}{10} \cdot \frac{10}{10} = \frac{90}{100} = 0.9$
- 65. If the percentages of the four blood types are added, the total will be 100%, since the blood types cover the whole population 45% + 40% + 11% = (45 + 40 + 11)% = 96%

100% - 96% = (100 - 96)% = 4%

4% of the U.S. population has the blood type AB.

69. The percent change for physician assistants is 30%. 30% = 30(0.01) = 0.30

Solutions to Selected Exercises

Exercise Set 6.2 1. 12% = $12 \cdot \frac{1}{100} = \frac{12}{100} = \frac{3 \cdot 4}{25 \cdot 4} = \frac{3}{25}$ **5.** $4.5\% = 4.5 \cdot \frac{1}{100}$ $=\frac{4.5}{100}$ $=\frac{4.5}{100}\cdot\frac{10}{10}$ $=\frac{45}{1000}$ $=\frac{9\cdot 5}{200\cdot 5}$ $=\frac{9}{200}$ 9. 73% = $73 \cdot \frac{1}{100} = \frac{73}{100}$ **13.** $6.25\% = 6.25 \cdot \frac{1}{100}$ $=\frac{6.25}{100}$ $= \frac{6.25}{100} \cdot \frac{100}{100}$ $=\frac{625}{10,000}$ $=\frac{1\cdot 625}{16\cdot 625}$ $=\frac{1}{16}$ **17.** $10\frac{1}{3}\% = \frac{31}{3}\% = \frac{31}{3} \cdot \frac{1}{100} = \frac{31}{300}$ **21.** $\frac{3}{4} = \frac{3}{4}(100\%) = \frac{300}{4}\% = 75\%$ **25.** $\frac{2}{5} = \frac{2}{5}(100\%) = \frac{200}{5}\% = 40\%$ **29.** $\frac{17}{50} = \frac{17}{50}(100\%) = \frac{1700}{50}\% = 34\%$ **33.** $\frac{5}{16} = \frac{5}{16}(100\%) = \frac{500}{16}\% = \frac{125}{4}\% = 31\frac{1}{4}\%$ **37.** $\frac{7}{9} = \frac{7}{9}(100\%) = \frac{700}{9}\% = 77\frac{7}{9}\%$ **41.** $2\frac{1}{2} = \frac{5}{2} = \frac{5}{2}(100\%) = \frac{500}{2}\% = 250\%$ **45.** $\frac{7}{11} = \frac{7}{11}(100\%) = \frac{700}{11}\% \approx 63.64\%$ 63.636... ≈ 63.64 11)700.000 -66 40 -33 70-6640 <u>-3</u>3 70 -66 4

| | $\frac{1}{7} = \frac{1}{7}(100\%) = \frac{1}{7}$ $\frac{14.285}{7} \approx 14.29$ $\frac{-7}{30}$ $\frac{-28}{20}$ $-\frac{14}{60}$ $\frac{-56}{40}$ $\frac{-35}{5}$ | $\frac{100}{7}\% \approx 14.29\%$ | |
|-------------------|--|---|---|
| 53. | Percent | Decimal | Fraction |
| | 35% | 35% = 0.35 | $35\% = \frac{35}{100} = \frac{7}{20}$ |
| | $\frac{1}{5} = \frac{20}{100} = 20\%$ | $\frac{1}{5} = \frac{2}{10} = 0.2$ | $\frac{1}{5}$ |
| | 0.5 = 0.50 = 50% | 0.5 | $0.5 = \frac{5}{10} = \frac{1}{2}$ |
| | 70% | 70% = 0.7 | $70\% = \frac{70}{100} = \frac{7}{10}$ |
| | $\frac{\frac{3}{8} = \frac{375}{1000} = \frac{37.5}{100}}{= 37.5\%}$ | $\frac{3}{8} = \frac{375}{1000} = 0.375$ | $\frac{3}{8}$ |
| 57. | | I | |
| 5% | Percent | Decimal | Fraction |
| 57. | Percent 200% | Decimal
200% = 2.00 = 2 | Fraction
$200\% = \frac{200}{100} = 2$ |
| 57. | | | |
| | 200% $2.8 = \frac{28}{10} = \frac{280}{100}$ $= 280\%$ 705% | 200% = 2.00 = 2
2.8
705% = 7.05 | $200\% = \frac{200}{100} = 2$ |
| | 200% $2.8 = \frac{28}{10} = \frac{280}{100}$ $= 280\%$ 705% | 200% = 2.00 = 2
2.8 | $200\% = \frac{200}{100} = 2$ $2.8 = 2\frac{8}{10} = 2\frac{4}{5}$ $705\% = \frac{705}{100}$ |
| 61.
65.
69. | 200% $2.8 = \frac{28}{10} = \frac{280}{100}$ $= 280\%$ 705% | $200\% = 2.00 = 2$ 2.8 $705\% = 7.05$ $4\frac{27}{50} = 4\frac{54}{100} = 4.54$ $\frac{592}{1000} = \frac{74}{125}$ | $200\% = \frac{200}{100} = 2$ $2.8 = 2\frac{8}{10} = 2\frac{4}{5}$ $705\% = \frac{705}{100}$ $= 7\frac{5}{100} = 7\frac{1}{20}$ |

- 81. a. To round 52.8647 to the nearest tenth observe that the digit in the hundredths place is 6. Since this digit is 5 or greater, we add 1 to the digit in the tenths place. The number 52.8647 rounded to the nearest tenth is 52.9. Thus 52.8647% ≈ 52.9%.
- b. To round 52.8647 to the nearest hundredth observe that the digit in the thousandths place is 4. Since this digit is less than 5, we do not add 1 to the digit in the hundredths place. The number 52.8647 rounded to the nearest hundredth is 52.86. Thus 52.8647% ≈ 52.86%.
 85. 0.65794 = 65.794%

To round 65.794 to the nearest hundredth observe that the digit in the thousandths place is 4. Since this digit is less than 5, we do not add 1 to the digit in the hundredths place. The number 65.794 rounded to the nearest hundredth is 65.79. Thus, $0.65794 = 65.794\% \approx 65.79\%$.

89. 3 of the 4 equal parts are shaded.

 $\frac{3}{4} = \frac{3}{4} \cdot \frac{25}{25} = \frac{75}{100} = 75\%$

75% of the figure is shaded.

93. A fraction written as a percent is greater than 100% when the numerator is <u>greater</u> than the denominator.

97. $\begin{array}{r} 0.2658 \approx 0.266\\ \hline 79)21.0000\\ \underline{-158}\\ 520\\ \underline{-474}\\ 460\\ \underline{-395}\\ 650\\ \underline{-632}\end{array}$

 $\frac{21}{79} \approx 0.266 \text{ or } 26.6\%$

Exercise Set 6.3

| 1. 18% of 81 is | what number? |
|--|--|
| $\downarrow \downarrow \downarrow \downarrow$ | Ļ |
| 18% · 81 = | п |
| 5. 0.6 is 40% of | what number? |
| $\downarrow \hspace{0.1cm} \downarrow \hspace{0.1cm} \downarrow \hspace{0.1cm} \downarrow \hspace{0.1cm} \downarrow$ | Ý |
| 0.6 = 40% . | п |
| 9. What number is | 9% of 43? |
| ↓ ↓ | $\downarrow \qquad \downarrow \qquad \downarrow$ |
| <i>n</i> = | 9% · 43 |
| 13. $10\% \cdot 35 = n$ | 17. $1.2 = 12\% \cdot n$ |
| $0.10 \cdot 35 = n$ | $1.2 = 0.12 \cdot n$ |
| 3.5 = n | 1.2 |
| 10% of 35 is 3.5. | $\frac{1}{0.12} = n$ |
| | 10 = n |
| | 1.2 is 12% of 10. |
| 21. $n \cdot 80 = 88$ | 25. $0.1 = 10\% \cdot n$ |
| | $0.1 = 0.10 \cdot n$ |
| $n = \frac{1}{80}$ | 0.1 |
| n = 1.1 | $\overline{0.1} = n$ |
| n = 110% | 1 = n |
| 88 is 110% of 80. | 0.1 is 10% of 1. |
| | |

| 29. $82.5 = 16\frac{1}{2}\% \cdot n$ | 33. $n = 42\% \cdot 60$ |
|---|---|
| $82.5 = 0.165 \cdot n$ $\frac{82.5}{0.165} = n$ $500 = n$ | $n = 0.42 \cdot 60$
n = 25.2
25.2 is 42% of 60. |
| 82.5 is $16\frac{1}{2}$ % of 500. | |
| 37. $120\% \cdot n = 42$
$1.20 \cdot n = 42$
$n = \frac{42}{1.2}$
n = 35
120% of 35 is 42. | 41. $n \cdot 600 = 3$
$n = \frac{3}{600}$
n = 0.005
n = 0.5%
0.5% of 600 is 3. |
| 45. $1575 = n \cdot 2500$
$\frac{1575}{2500} = n$
0.63 = n
63% = n
1575 is 63% of 2500.
53. $\frac{17}{12} = \frac{n}{20}$ | $49. \qquad \frac{27}{n} = \frac{9}{10}$ $27 \cdot 10 = 9 \cdot n$ $270 = 9 \cdot n$ $\frac{270}{9} = n$ $30 = n$ |

1

- **57.** In the equation $5 \cdot n = 32$, the step that should be taken to find the value of *n* is to divide by 5, obtaining $n = \frac{32}{5}$, which is choice **c**.
- **61.** 20% $\cdot n = 18.6$ in words is "twenty percent of some number is eighteen and six tenths."
- **65.** Since 85 is less than 120, the percent is less than 100%; **c**.
- **69.** Since 100% is 1, 100% of 45 is equal to 45; **a**.
- **73.** answers may vary
- 77. $22,113 = 180\% \cdot n$ $22,113 = 1.80 \cdot n$ $\frac{22,113}{1.8} = n$ 12,285 = n22,113 is 180% of 12,285.

Exercise Set 6.4

| 1. | 98% | of | 45 | is | what number? |
|----|------------------|-------------|--------------|--------------|--------------|
| | \downarrow | | \downarrow | | \downarrow |
| | perce | nt | base | | amount $= a$ |
| | a _ | | | | |
| | $\frac{1}{45} =$ | 100 | | | |
| 5. | 14.3 | is | 26% | of | what number? |
| | \downarrow | | \downarrow | | Ť |
| | amou | nt | percen | ıt | base $= b$ |
| | 14.3 | _ 26 | | | |
| | b | 100 | | | |
| 9. | What | percen | t of | 400 | is 70? |
| | | \uparrow | - | \downarrow | \downarrow |
| | perce | ent = μ |) | base | amount |
| | _70 _ | <i>p</i> | | | |
| | 400 | 100 | | | |

Solutions to Selected Exercises

13.
$$\frac{a}{65} = \frac{40}{100}$$
 or $\frac{a}{65} = \frac{2}{5}$
 $a \cdot 5 = 65 \cdot 2$
 $5 \cdot a = 130$
 $a = \frac{130}{5}$
 $a = 26$
 40% of 65 is 26.
17. $\frac{90}{b} = \frac{150}{100}$ or $\frac{90}{b} = \frac{3}{20}$
 $90 \cdot 20 = b \cdot 3$
 $1800 = b \cdot 3$
 $\frac{1800}{3} = b$
 $600 = b$
 15% of 600 is 90.
21. $\frac{42}{35} = \frac{p}{100}$ or $\frac{6}{5} = \frac{p}{100}$
 $6 \cdot 100 = 5 \cdot p$
 $\frac{600}{5} = p$
 $120 = p$
 $42 \text{ is } 120\%$ of 35.
25. $\frac{3.7}{b} = \frac{10}{100}$ or $\frac{3.7}{b} = \frac{1}{10}$
 $3.7 \cdot 10 = b \cdot 1$
 $37 = b$
 $3.7 \text{ is } 10\%$ of 37.
29. $\frac{160}{b} = \frac{16}{100}$ or $\frac{160}{b} = \frac{4}{25}$
 $160 \cdot 25 = b \cdot 4$
 $4000 = b$
 $160 \text{ is } 16\%$ of 1000.
33. $\frac{a}{62} = \frac{89}{100}$
 $a \cdot 100 = 62 \cdot 89$
 $a \cdot 100 = 5518$
 $a = \frac{5518}{100}$
 $a = 55.18$
 $55.18 \text{ is } 89\%$ of 62.
37. $\frac{105}{b} = \frac{140}{100}$ or $\frac{105}{b} = \frac{7}{5}$
 $105 \cdot 5 = b \cdot 7$
 $525 = b \cdot 7$

45. $\frac{a}{48} = \frac{20}{100}$ or $\frac{a}{48} = \frac{1}{5}$ $a \cdot 5 = 48 \cdot 1$ $a \cdot 5 = 48$ $a = \frac{48}{5}$ a = 9.620% of 48 is 9.6. **49.** $\frac{11}{16} + \frac{3}{16} = \frac{11+3}{16} = \frac{14}{16} = \frac{7 \cdot 2}{8 \cdot 2} = \frac{7}{8}$ 0.41 **53.** <u>+</u>0.29 0.70 57. answers may vary **61.** $\frac{p}{100} = \frac{13}{52}$ $\frac{25}{100} \stackrel{?}{=} \frac{13}{52}$ $\frac{1}{4} = \frac{1}{4}$ True Yes, the percent is 25. **65.** $\frac{a}{53,862} = \frac{22.3}{100}$ $a \cdot 100 = 22.3 \cdot 53,862$ $a \cdot 100 = 1,201,122.6$ $a = \frac{1,201,122.6}{100}$ $a \approx 12,011.2$ Exercise Set 6.5 **1.** 24 is 1.5% of what number? Method 1: $24 = 1.5\% \cdot n$ $24 = 0.015 \cdot n$ $\frac{24}{0.015} = n$ 1600 = n1600 bolts were inspected. Method 2: $\frac{24}{b} = \frac{1.5}{100}$ $24 \cdot 100 = 1.5 \cdot b$ $2400 = 1.5 \cdot b$ $\frac{2400}{1.5} = b$ 1600 = b1600 bolts were inspected. 5. 378 is what percent of 2700? Method 1: $378 = n \cdot 2700$ 378 $\frac{10}{2700} = n$ 0.14 = n14% = nThe student spent 14% of last semester's college costs on books.

Solutions to Selected Exercises

Method 2: $\frac{378}{100} = \frac{p}{100}$ $\overline{2700} - \overline{100}$ $378 \cdot 100 = 2700 \cdot p$ $37,800 = 2700 \cdot p$ 37,800 = p2700 14 = pThe student spent 14% of last semester's college costs on books. 9. 14,250 is what percent of 36,900? *Method 1*: $14,250 = n \cdot 36,900$ 14,250 = n36,900 $0.386 \approx n$ $38.6\% \approx n$ 38.6% of McDonald's restaurants were in the United States in 2016. Method 2: 14,250 = <u>p</u> 36,900 100 $14,250 \cdot 100 = 36,900 \cdot p$ $1,425,000 = 36,900 \cdot p$ 1,425,000 = p36,900 $38.6 \approx p$ 38.6% of McDonald's restaurants were in the United States in 2016. **13.** What number is 43% of 41,900? *Method 1*: $n = 43\% \cdot 41,900$ $n = 0.43 \cdot 41,900$ n = 18.017The number of people employed as occupational therapy assistants is expected to be 41,900 + 18,017 = 59,917. Method 2: а 43 $\frac{u}{41,900} = \frac{10}{100}$ $a \cdot 100 = 41,900 \cdot 43$ $100 \cdot a = 1,801,700$ 1,801,700 $a = \cdot$ 100 a = 18,017The number of people employed as occupational therapy assistants is expected to be 41,900 + 18,017 = 59,917. **17.** 38 is what percent of 131? Method 1: $38 = n \cdot 131$ 38 = *n* 131 $0.29 \approx n$ $29\% \approx n$ 29% of the ski runs at Keystone ski area are rated intermediate.

Method 2: $\frac{38}{100} = \frac{p}{100}$ $\frac{1}{131} - \frac{1}{100}$ $38 \cdot 100 = 131 \cdot p$ $3800 = 131 \cdot p$ $\frac{3800}{2} = p$ 131 $29 \approx p$ 29% of the ski runs at Keystone ski area are rated intermediate. **21.** 10 is what percent of 80? Method 1: $10 = n \cdot 80$ 10 = n80 0.125 = n12.5% = n12.5% of the total calories come from fat. *Method 2*: $\frac{10}{2} = -\frac{p}{2}$ $\frac{1}{80} - \frac{1}{100}$ $10 \cdot 100 = 80 \cdot p$ $1000 = 80 \cdot p$ 1000 = p80 12.5 = p12.5% of the total calories come from fat. **25.** 26,250 is 15% of what number? *Method 1*: $26,250 = 15\% \cdot n$ $26,250 = 0.15 \cdot n$ 26,250 = n0.15 175,000 = nThe price of the home was \$175,000. *Method 2*: 26,250 15 $\frac{b}{b} = \frac{b}{b}$ 100 $26,250 \cdot 100 = b \cdot 15$ $2,625,000 = b \cdot 15$ 2,625,000 = b15 175,000 = bThe price of the home was \$175,000. **29.** What number is 4.5% of 19,286? Method 1: $n = 4.5\% \cdot 19,286$ $n = 0.045 \cdot 19,286$ n = 867.87The price of the car will increase by \$867.87. The new price of that model will be \$19,286 + \$867.87 = \$20,153.87. Method 2: a = 4.519.286 100 $a \cdot 100 = 4.5 \cdot 19.286$ $a \cdot 100 = 86,787$ $a = \frac{86,787}{2}$ 100 a = 867.87

The price of the car will increase by 867.87. The new price of that model will be 19,286 + 867.87 = 20,153.87.

11.6%(8994) = n0.116(8994) = n1043.304 = n $1043 \approx n$

The increase in tuition was \$1043. The tuition for the 2016-2017 school year was \$8994 + \$1043 = \$10,037.Method 2

$$Method 2:$$

$$\frac{a}{8994} = \frac{11.6}{100}$$
 $a \cdot 100 = 11.6 \cdot 8994$
 $a \cdot 100 = 104,330.4$

$$a = \frac{104,330.4}{100}$$
 $a = 1043.304$
 $a \approx 1043$

The increase in tuition was \$1043. The tuition for the 2016-2017 school year was \$8994 + \$1043 = \$10,037.

| 37. | Original | New | Amount of | Percent of | | |
|-----|----------|--------|--------------|------------------------------|--|--|
| | Amount | Amount | Increase | Increase | | |
| | 50 | 80 | 80 - 50 = 30 | $\frac{30}{50} = 0.6 = 60\%$ | | |

| 41. | Original | New | Amount of | Percent of | | |
|-----|----------|--------|-----------|-----------------------------|--|--|
| | Amount | Amount | Decrease | Decrease | | |
| | 8 | 6 | 8 - 6 = 2 | $\frac{2}{8} = 0.25 = 25\%$ | | |

45. percent of decrease =
$$\frac{\text{amount of decrease}}{\text{original amount}}$$

= $\frac{150 - 84}{150}$
= $\frac{66}{150}$
= 0.44
The decrease in calories per cup is 44%.
49. percent of increase = $\frac{\text{amount of increase}}{\text{original amount}}$
= $\frac{421 - 174}{174}$
= $\frac{247}{174}$

$$1/4 \approx 1.420$$

The increase in the size of privately owned farms in the United States was about 142.0%.

53. percent of increase =
$$\frac{\text{amount of increase}}{\text{original amount}}$$

= $\frac{4151 \text{ thousand} - 3782 \text{ thousand}}{3782 \text{ thousand}}$
= $\frac{369 \text{ thousand}}{3782 \text{ thousand}}$
= $\frac{369}{3782}$
 ≈ 0.098

The increase in the number of elementary and secondary teachers in the United State is expected to be 9.8%

57. percent of increase =
$$\frac{\text{amount of increase}}{\text{original amount}}$$

= $\frac{8.87 - 6.88}{6.88}$
= $\frac{1.99}{6.88}$
 ≈ 0.289
The increase in the U.S. movie theater ticket price was 28.9%.
61. 0.12 65. 78.00
 $\frac{\times 38}{96}$ $\frac{-19.46}{58.54}$
 $\frac{360}{4.56}$

69. percent of increase =
$$\frac{\text{amount of increase}}{1}$$

original amount

$$= \frac{180 - 150}{150}$$

$$= \frac{30}{150}$$

$$= 0.20$$

The percent of increase is 20%.

Exercise Set 6.6

1. sales tax = $5\% \cdot \$150 = 0.05 \cdot \$150 = \$7.50$ The sales tax is \$7.50.

5.
$$\$335.30 = r \cdot \$4790$$

$$\frac{333.30}{1700} = r$$

0.07 = r

The sales tax rate is 7%. 9. sales tax = $6.5\% \cdot \$1800 = 0.065 \cdot \$1800 = \$117$

total price = \$1800 + \$117 = \$1917The sales tax is \$117 and the total price of the bracelet is \$1917.

13. $\$98.70 = r \cdot \1645

$$\frac{98.70}{1600} = r$$

1645

0.06 = r

The sales tax rate is 6%. **17.** commission = $4\% \cdot \$1,329,401 = 0.04 \cdot \$1,329,401$ \$53,176.04

21. commission =
$$1.5\% \cdot $325,900 = 0.015 \cdot $325,900$$

= \$4888.50 His commission will be \$4888.50.

| | Original
Price | Discount
Rate | Amount of
Discount | Sale Price |
|-----|-------------------|------------------|----------------------------------|-----------------------------|
| 25. | \$89 | 10% | $10\% \cdot \$89 = \8.90 | \$89 - \$8.90 = \$80.10 |
| 29. | \$410 | 35% | $35\% \cdot \$410$
= \$143.50 | \$410 - \$143.50 = \$266.50 |

33. discount = $15\% \cdot \$300 = 0.15 \cdot \$300 = \$45$ sale price = 300 - 45 = 255The discount is \$45 and the sale price is \$255.

| | 37. | Purchase
Price | Tax R | ate | Sales | Гах | Total Price | | |
|--|-----|--------------------------------|---|---------------|-----------------------------------|--------------------------------|-------------------------|--|--|
| | | \$56 | 5.5% | ,
D | 5.5% • \$56 | = \$3.08 | \$56 + \$3.08 = \$59.08 | | |
| ses | 41. | Sale | Com | missio | n Rate | Commiss | ion | | |
| Ū, | | Baic | \$1432 | | II Rute | Commiss | | | |
| Solutions to Selected Exercises | | \$17,900 | \$17,90 | - = 00 | 08 = 8% | \$1432 | | | |
| Б | 45. | $400 \cdot \frac{3}{100}$ | = 132 | | | | | | |
| cte | | 100 | \$68 to \$70 and 9.5% to 10%.
$70 = 0.10 \cdot $70 = 7 | | | | | | |
| <u>e</u> | | $10\% \cdot 70
\$70 + \$7 | | | | | | | |
| Š | | The best e | | of the | e total pri | ce is \$77; d | I. | | |
| t
t | 53. | Bill Am | ount | 10% | 1 | 5% | 20% | | |
| ns | | \$72.17 ≈ | \$72.00 | \$7.20 | \$7.20 + | $\frac{1}{2}$ (\$7.20) | 2(\$7.20) | | |
| E. | | | | | | $2^{(\psi,120)}$
0 + \$3.60 | = \$14.40 | | |
| E | | | | | = \$10. | | | | |
| So | 57. | 7.5% • \$24 | ,966 = | 0.075 | •\$24,966 | = \$1872. | 45 | | |
| | | \$24,966 + | | | | | - | | |
| | - | The total p | | the n | ecklace is | \$20,838.43 |). | | |
| | | ercise Set 6
simple inter | | princ | cipal • rate | • time | | | |
| | | | = | (\$20 | (0)(8%)(| 2) | | | |
| | 5 | simple int | | | | (2) = \$32 | | | |
| | 5. | simple int | | - | - | / \ | | | |
| | | | | | 00)(10% | (2) | | | |
| | 9. | simple int | | | | (1.5) = 3
• time | \$750 | | |
| | | simple int | | | 00)(16% | | | | |
| | | | | | | (12)
(1.75) = \$ | 700 | | |
| | 13. | simple int | erest = | princ | cipal · rate | • time | /00 | | |
| | | | = | \$500 | $0(9\%)\left(\frac{1}{-1}\right)$ | 15 | | | |
| | | | | | ` | (12)
(.25) = \$5 | 562 5 | | |
| | | Total = \$ | 5000 + | \$562 | | | 02.5 | | |
| | 17. | $A = P\left(1\right)$ | $\left(+ \frac{r}{r} \right)^n$ | ·t | | | | | |
| | | | $\binom{n}{1}$ | $.14)^{2}$ | 15 | | | | |
| | | = 6150 | | $\frac{1}{2}$ | | | | | |
| | | $= 6150$ $\approx 46,81$ | · / | | | | | | |
| | | The total a | amount | is \$46 | 5,815.37. | | | | |
| | 21. | A = P(1 | $\left(+ \frac{r}{r} \right)^n$ | •t | | | | | |
| | | (| n)
(| 0.09 | 2.20 | | | | |
| | | = 10,00 | | |) | | | | |
| | | = 10,00 | | $(5)^{40}$ | | | | | |
| | | $\approx 58,16$
The total a | | is \$58 | 3,163.65. | | | | |
| | 25. | A = P(1 | | | | | | | |
| | | | $\binom{n}{n}$ | 08/1 | •5 | | | | |
| | | = 2000 | (1 + - | $\frac{1}{1}$ | | | | | |
| | | = 2000 | $(1.08)^5$ | / | | | | | |
| | | ≈ 2938 | .66 | | | | | | |

The total amount is \$2938.66.

principal + interest **29.** monthly payment = number of payments 1500 + 61.886 \$1561.88 = 6 ≈ \$260.31 The monthly payment is \$260.31.

33. perimeter = 10 + 6 + 10 + 6 = 32

The perimeter is 32 yards. 37. answers may vary

Chapter 6 Test

1.
$$85\% = 85(0.01) = 0.85$$

5. 6.1 = 6.1(100%) = 610%

9.
$$0.2\% = \frac{0.2}{100} = \frac{2}{1000} = \frac{1}{500}$$

13. What number is 42% of 80? Method 1: $n = 42\% \cdot 80$

 $n = 0.42 \cdot 80$

n = 33.6

33.6 is 42% of 80. Method 2:

 $\frac{1}{80} = \frac{1}{100}$

 $a \cdot 100 = 80 \cdot 42$ $a \cdot 100 = 3360$

 $a = \frac{3360}{100}$

a = 33.60

33.6 is 42% of 80.

17. 20% of what number is 11,350? Method 1: $20\% \cdot n = 11,350$

$$0.20 \cdot n = 11,350$$

 $n = \frac{11}{0.20}$

n = 56,750

The total value of his potential crop was \$56,750. Method 2:

```
\frac{11,350}{b} = \frac{20}{100}
               100
11,350 1
```

$$\frac{b}{b} = \frac{1}{5}$$

 $11,350 \cdot 5 = b \cdot 1$

$$56,750 = b$$

The total value of his potential crop was \$56,750.

21. commission = $4\% \cdot \$9875 = 0.04 \cdot \$9875 = \$395$ His commission is \$395.

25. simple interest = principal \cdot rate \cdot time

$$= (\$400)(13.5\%)\left(\frac{6}{12}\right)$$

= (\$400)(0.135)(0.5)
= \$27.00

Total amount due the bank = 400 + 27 = 427.

Chapter 7

Exercise Set 7.1 **1.** 60 in. $= \frac{60 \text{ in.}}{1} \cdot \frac{1 \text{ ft}}{12 \text{ in.}} = \frac{60}{12} \text{ ft} = 5 \text{ ft}$

Solutions to Selected Exercises

5. 42,240 ft = $\frac{42,240 \text{ ft}}{1} \cdot \frac{1 \text{ mi}}{5280 \text{ ft}}$ $=\frac{42,240}{5280}$ mi = 8 mi **9.** 10 ft = $\frac{10 \text{ ft}}{1} \cdot \frac{1 \text{ yd}}{3 \text{ ft}} = \frac{10}{3} \text{ yd} = 3\frac{1}{3} \text{ yd}$ **13.** 162 in. $=\frac{162 \text{ in.}}{1} \cdot \frac{1 \text{ yd}}{36 \text{ in.}}$ $=\frac{162}{36}$ yd $\mathbf{17.} \ 40 \ \text{ft} = \frac{40 \ \text{ft}}{1} \cdot \frac{1 \ \text{yd}}{3 \ \text{ft}} = \frac{40}{3} \ \text{yd}$ 13 yd 1 ft 3)40 $\frac{-3}{10}$ $\frac{-9}{1}$ 40 ft = 13 yd 1 ft**21.** 10,000 ft = $\frac{10,000 \text{ ft}}{1} \cdot \frac{1 \text{ mi}}{5280 \text{ ft}} = \frac{10,000}{5280} \text{ mi}$ 1 mi 4720 ft 5280)10,000 -52804720 10,000 ft = 1 mi 4720 ft**25.** 8 yd 2 ft = $\frac{8 \text{ yd}}{1} \cdot \frac{3 \text{ ft}}{1 \text{ yd}} + 2 \text{ ft}$ = 24 ft + 2 ft $= 26 \, \text{ft}$ **29.** 3 ft 10 in. + 7 ft 4 in. = 10 ft 14 in.= 10 ft + 1 ft 2 in.= 11 ft 2 in.**33.** 22 ft 8 in. -16 ft 3 in. 6 ft 5 in. **37.** 28 ft 8 in. \div 2 = 14 ft 4 in. **41.** 60 m = $\frac{60 \text{ m}}{1} \cdot \frac{100 \text{ cm}}{1 \text{ m}} = 6000 \text{ cm}$ **45.** $500 \text{ m} = \frac{500 \text{ m}}{1} \cdot \frac{1 \text{ km}}{1000 \text{ m}} = \frac{500}{1000} \text{ km} = 0.5 \text{ km}$ **49.** $1500 \text{ cm} = \frac{1500 \text{ cm}}{1} \cdot \frac{1 \text{ m}}{100 \text{ cm}} = \frac{1500}{100} \text{ m} = 15 \text{ m}$ **53.** $7 \text{ km} = \frac{7 \text{ km}}{1} \cdot \frac{1000 \text{ m}}{1 \text{ km}} = 7000 \text{ m}$ **57.** 20.1 mm = $\frac{20.1 \text{ mm}}{1} \cdot \frac{1 \text{ dm}}{100 \text{ mm}}$ 100 mm $=\frac{20.1}{100}\,\mathrm{dm}$ $= 0.201 \, \mathrm{dm}$ **61.** 8.60 m +0.34 m 8.94 m **65.** 24.8 mm 24.8 mm 2.48 cm -1.19 cm -11.9 mm or -1.19 cm 12.9 mm 1.29 cm **69.** $18.3 \text{ m} \times 3 = 54.9 \text{ m}$

| 73. | | | Yards | Fee | 4 | Inches | $\overline{}$ | | | |
|------|--|-------------------------------|-------------------------------|----------------------|-----------------|------------------|---------------|------------|--|--|
| | Chrysler | | Tarus | гее | ι | Inches | 5 | | | |
| | Building i | | $348\frac{2}{3}$ | 104 | 6 | 12,552 | 2 | | | |
| | New York C | City | 3 | | | | | | | |
| | | Meters | s Millin | neters | Kil | ometers | C | entimeters | | |
| 77. | Length of elephant | 5 | 50 | 000 | (| 0.005 | | 500 | | |
| 81. | Distance
from London
to Paris | 342,00 | 0 342,0 | 00,000 | | 342 | 34 | 4,200,000 | | |
| | 85. 6 ft 10 in. + 3 ft 8 in. = 9 ft 18 in.
= 9 ft + 1 ft 6 in.
= 10 ft 6 in.
The bamboo is 10 ft 6 in. tall now.
89. 8 ft 11 in. = 96 in. + 11 in. = 107 in. | | | | | | | | | |
| 0,7 | 01011111 | , o 111 | | 4.97 | | | | | | |
| | 21.5)107 bee | comes | 215)10 | 70.00 | | | | | | |
| | | | $\frac{-8}{2}$ | | | | | | | |
| | | | | 10 0
93 5 | | | | | | |
| | | | | <u>75 5</u>
16 50 | | | | | | |
| | | | _ | 15 05 | | | | | | |
| | | | | 1 45 | | | | | | |
| 93 | Robert was 80 mm | about :
80.0 1 | | s the he | eigh | t of Cha | ind | ra. | | |
| 15 | -5.33 cm | -53.3 1 | | | | | | | | |
| | | 26.7 1 | | | | | | | | |
| | The ice mus | | | | | | | | | |
| 97. | The distance
one-half the | | | | | | | | | |
| | ings and the | | | | une | | | ne ound | | |
| | 192 ft 8 in.
192 ft ÷ 2 = | | = 192 f | t | | | | | | |
| | If $\frac{192}{10}$ ft $\frac{1}{2}$ It is 96 feet | | e wall to | o eithe | r of | the buil | din | <u>gs.</u> | | |
| | 3.35 | | | | | | | 8 | | |
| 101. | 20)67.00 | | | | | | | | | |
| | $\frac{-60}{7}$ | | | | | | | | | |
| | 70 | | | | | | | | | |
| | $\frac{-6\ 0}{1\ 00}$ | | | | | | | | | |
| | -1.00 | | | | | | | | | |
| | 0 | | | | | | | | | |
| 105 | Each piece | | | | ıg. | | | | | |
| 105 | $P = 2 \cdot 44 \text{ f}$ | | | | | 2 | | | | |
| | $218 \text{ ft} = \frac{21}{218}$ | $\frac{3}{1}\cdot\frac{1}{3}$ | $\frac{f}{ft} = \frac{21}{3}$ | $\frac{d}{d}$ yd = | = 72 | $\frac{2}{3}$ yd | | | | |
| | The perime | | ne billbo | ard is ' | $72\frac{2}{3}$ | yards. | | | | |
| 109 | $0.21 = \frac{21}{100}$ | | | | | | | | | |
| 113 | $\frac{1}{4} = \frac{1}{4} \cdot \frac{25}{25}$ | $=\frac{25}{100}$ | = 0.25 | | | | | | | |
| 117. | Yes, glass fo | or a drir | iking gla | iss beir | ng 2 | millime | ter | s thick is | | |
| 121. | reasonable.
5 yd 2 in. is | | | | | | | | | |
| 125. | 7 yd 36 in. =
answers ma | | Estimat | e: 5 yd | + 8 | 8 yd = 2 | 13 y | vd. | | |

Exercise Set 7.2

1. $2 \text{ lb} = \frac{2 \text{ lb}}{1} \cdot \frac{16 \text{ oz}}{1 \text{ lb}} = 2 \cdot 16 \text{ oz} = 32 \text{ oz}$ **5.** 18,000 lb = $\frac{18,000 \text{ lb}}{1} \cdot \frac{1 \text{ ton}}{2000 \text{ lb}}$ **Solutions to Selected Exercises** $=\frac{18,000}{2000}$ tons = 9 tons**9.** 3500 lb = $\frac{3500 \text{ lb}}{1} \cdot \frac{1 \text{ ton}}{2000 \text{ lb}}$ $=\frac{3500}{2000}$ tons $=\frac{7}{4}$ tons $=1\frac{3}{4}$ tons **13.** 4.9 tons = $\frac{4.9 \text{ tons}}{1} \cdot \frac{2000 \text{ lb}}{1 \text{ ton}}$ $= 4.9 \cdot 2000 \, \text{lb}$ $= 9800 \, lb$ **17.** 2950 lb = $\frac{2950 \text{ lb}}{1} \cdot \frac{1 \text{ ton}}{2000 \text{ lb}}$ $=\frac{2950}{2000}\,\mathrm{tons}$ $=\frac{59}{40}$ tons ≈ 1.5 tons **21.** $5\frac{3}{4}$ lb = $\frac{23}{4}$ lb $=\frac{\frac{23}{4}\,\mathrm{lb}}{1}\cdot\frac{16\,\mathrm{oz}}{1\,\mathrm{lb}}$ $=\frac{23}{4}\cdot 16 \text{ oz}$ $= 23 \cdot 4 \text{ oz}$ = 92 oz **25.** 89 oz = $\frac{89 \text{ oz}}{1} \cdot \frac{1 \text{ lb}}{16 \text{ oz}} = \frac{89}{16} \text{ lb}$ 5 lb 9 oz 16)89 -809 89 oz = 5 lb 9 oz**29.** 3 tons 1820 lb + 4 tons 930 lb = 7 tons 2750 lb= 7 tons + 1 ton 750 lb= 8 tons 750 lb **33.** 12 lb 4 oz 11 lb 20 oz - 3 lb 9 oz - 3 lb 9 oz 8 lb 11 oz **37.** 6 tons 1500 lb ÷ 5 = $\frac{6}{5}$ tons 300 lb $=1\frac{1}{5}$ tons 300 lb $= 1 \tan + \frac{2000 \text{ lb}}{5} + 300 \text{ lb}$ = 1 ton + 400 lb + 300 lb= 1 ton 700 lb**41.** 4 g = $\frac{4 \text{ g}}{1} \cdot \frac{1000 \text{ mg}}{1 \text{ g}} = 4 \cdot 1000 \text{ mg} = 4000 \text{ mg}$

45. 48 mg = $\frac{48 \text{ mg}}{1} \cdot \frac{1 \text{ g}}{1000 \text{ mg}} = \frac{48}{1000} \text{ g} = 0.048 \text{ g}$ **49.** 15.14 g = $\frac{15.14 \text{ g}}{1} \cdot \frac{1000 \text{ mg}}{1 \text{ g}}$ $= 15.14 \cdot 1000 \text{ mg}$ = 15,140 mg**53.** 35 hg = $\frac{35 \text{ hg}}{1} \cdot \frac{10,000 \text{ cg}}{1 \text{ hg}}$ $= 35 \cdot 10,000 \text{ cg}$ = 350,000 cg**57.** 205 mg + 5.61 g = 0.205 g + 5.61 g = 5.815 gor 205 mg + 5.61 g = 205 mg + 5610 mg= 5815 mg**61.** 1.61 kg - 250 g = 1.61 kg - 0.250 kg = 1.36 kg1.61 kg - 250 g = 1610 g - 250 g = 1360 g**65.** 17 kg ÷ 8 = $\frac{17}{8}$ kg 2.125 8)17.000 -1610-820 -1640 -400 $17 \text{ kg} \div 8 = 2.125 \text{ kg}$ 69. Object Tons Pounds Ounces 269 A 12-inch cube of osmium 1345 21,520 or 0.6725 400 73. Object Grams Kilograms Milligrams Centigrams A six-year-21,000 21 21,000,000 2,100,000 old boy 77. 64 lb 8 oz 63 lb 24 oz -28 lb 10 oz -28 lb 10 oz 35 lb 14 oz Elizabeth's zucchini was 35 lb 14 oz lighter than the record weight. 81. 1 lb 10 oz + 3 lb 14 oz 4 lb 24 oz = 4 lb + 1 lb 8 oz = 5 lb 8 ozThe chef has a total of 5 pounds 8 ounces of rice. **85.** $3 \times 16 = 48$ 3 cartons contain 48 boxes of fruit. $3 \text{ mg} \times 48 = 144 \text{ mg}$ 3 cartons contain 144 mg of preservatives. **89.** $3 \text{ lb } 4 \text{ oz} \times 10 = 30 \text{ lb } 40 \text{ oz}$ $= 30 \, lb + 2 \, lb \, 8 \, oz$ = 32 lb 8 ozEach box weighs 32 lb 8 oz. $32 \text{ lb } 8 \text{ oz} \times 4 = 128 \text{ lb } 32 \text{ oz}$ $= 128 \, lb + 2 \, lb$ $= 130 \, lb$ 4 boxes of meat weigh 130 lb. **93.** $\frac{4}{25} = \frac{4}{25} \cdot \frac{4}{4} = \frac{16}{100} = 0.16$

| 97. | No, a pill containing 2 kg of medication is not |
|-----|---|
| | reasonable. |

- 101. No, a professor weighing less than 150 g is not reasonable.
- 105. True, a kilogram is 1000 grams.

Exercise Set 7.3

1.
$$32 \text{ fl oz} = \frac{32 \text{ fl oz}}{1} \cdot \frac{1 \text{ gal}}{4 \text{ qt}} = \frac{14}{4} \text{ gal} = 3\frac{1}{2} \text{ gal}$$

9. $2 \text{ qt} = \frac{2 \text{ qt}}{1} \cdot \frac{2 \text{ pt}}{1 \text{ qt}} \cdot \frac{2 \text{ c}}{1 \text{ qt}} = 2 \cdot 2 \cdot 2 \text{ c} = 8 \text{ c}$
13. $42 \text{ c} = \frac{42 \text{ c}}{1} \cdot \frac{1 \text{ qt}}{4 \text{ c}} = \frac{42}{4} \text{ qt} = 10\frac{1}{2} \text{ qt}$
17. $5 \text{ gal } 3 \text{ qt} = \frac{5 \text{ gal}}{1} \cdot \frac{4 \text{ qt}}{1 \text{ gal}} + 3 \text{ qt}$
 $= 23 \text{ qt}$
21. $58 \text{ qt} = 56 \text{ qt} + 2 \text{ qt}$
 $= \frac{56 \text{ qt}}{1} \cdot \frac{1 \text{ gal}}{4 \text{ qt}} + 2 \text{ qt}$
 $= \frac{56 \text{ qt}}{1} \cdot \frac{1 \text{ gal}}{4 \text{ qt}} + 2 \text{ qt}$
 $= \frac{56 \text{ qt}}{1} \cdot \frac{4 \text{ qt}}{4 \text{ qt}} + 2 \text{ qt}$
 $= \frac{56 \text{ qt}}{1} \cdot \frac{2 \text{ pt}}{4 \text{ qt}} + 2 \text{ qt}$
 $= \frac{56 \text{ qt}}{1} \cdot \frac{2 \text{ pt}}{4 \text{ qt}} + 2 \text{ qt}$
 $= 23 \text{ qt}$
25. $2\frac{3}{4} \text{ gal} = \frac{11}{4} \text{ gal}$
 $= \frac{11}{4} \text{ gal} 2 \text{ qt}$
29. $1 \text{ cs fl oz} + 2 \text{ c 7 fl oz} = 3 \text{ c } 12 \text{ fl oz}$
 $= 3 \text{ c} + 1 \text{ c } 4 \text{ fl oz}$
 $= 3 \text{ c} + 1 \text{ c } 4 \text{ fl oz}$
 $= 3 \text{ c} + 1 \text{ c } 4 \text{ fl oz}$
 $= 3 \text{ c} + 1 \text{ c } 4 \text{ fl oz}$
 $33. 3 \text{ gal 1 qt}$
 2 gal 5 qt
 2 gal 4 qt 2 pt
 $= 8 \text{ gal 6 qt} \div 2$
 $= 4 \text{ gal 3 qt}$
41. $0.16 \text{ L} = \frac{0.16 \text{ L}}{1} \cdot \frac{1 \text{ kl}}{1000 \text{ l}} = 3.2 \cdot 100 \text{ cl} = 320 \text{ cl}$
49. $64 \text{ ml} = \frac{64 \text{ ml}}{1} \cdot \frac{100 \text{ cl}}{11 \text{ c}} = 3.6 \cdot 1000 \text{ ml} = 3600 \text{ ml}$
57. $2700 \text{ ml} + 1.8 \text{ L} = 270 \text{ ml} + 180 \text{ ml} = 4500 \text{ ml}$
57. $2700 \text{ ml} + 1.8 \text{ L} = 270 \text{ ml} + 180 \text{ ml} = 4500 \text{ ml}$
61. $17,500 \text{ ml} - 0.9 \text{ L} = 17.50 \text{ ml} - 90 \text{ ml} = 16.60 \text{ ml}$
65. $81.2 \text{ L} \div 0.5 = 81.2 \text{ L} \div \frac{1}{2}$
 $= 81.2 \text{ L} \cdot 2$
 $= 162.4 \text{ L}$

| 69. Capacity | Cups | Gallons | Quarts | Pints |
|---|------|---------------|--------|-------|
| Your kidneys filter about
this amount of blood every
minute | 4 | $\frac{1}{4}$ | 1 | 2 |

73. 354 ml + 18.6 L = 0.354 L + 18.6 L = 18.954 LThere were 18.954 liters of gasoline in the tank.

77. 5 pt 1 c + 2 pt 1 c

$$c = 7 \text{ pt } 2 c$$

$$= 7 \text{ pt } + 1 \text{ pt}$$

$$= 8 \text{ pt}$$

$$= \frac{8 \text{ pt}}{1} \cdot \frac{1 \text{ qt}}{2 \text{ pt}}$$

$$= \frac{8}{2} \text{ qt}$$

$$= 4 \text{ qt}$$

$$= \frac{4 \text{ qt}}{1} \cdot \frac{1 \text{ gal}}{4 \text{ qt}}$$

$$= \frac{4}{4} \text{ gal}$$

$$= 1 \text{ gal}$$

Yes, the liquid can be poured into the container without causing it to overflow.

- **81.** $\frac{20}{25} = \frac{4 \cdot 5}{5 \cdot 5} = \frac{4}{5}$ **85.** $\frac{72}{80} = \frac{8 \cdot 9}{8 \cdot 10} = \frac{9}{10}$
- 89. No, a tub filled with 3000 ml of hot water is not reasonable.
- **93.** answers may vary
- 97. B indicates 1.5 cc.
- **101.** B indicates 54 u or 0.54 cc.

Exercise Set 7.4

1. 756 ml
$$\approx \frac{756 \text{ ml}}{1} \cdot \frac{1 \text{ fl oz}}{29.57 \text{ ml}} \approx 25.57 \text{ fl oz}$$

5. 1000 g $\approx \frac{1000 \text{ g}}{1} \cdot \frac{0.04 \text{ oz}}{1 \text{ g}} \approx 40 \text{ oz}$

9.
$$14.5 \text{ L} \approx \frac{14.5 \text{ L}}{1} \cdot \frac{0.26 \text{ gal}}{1 \text{ L}} \approx 3.77 \text{ gal}$$

| 13. | | Meters | Yards | Centimeters | Feet | Inches |
|-----|-----------------------|--------|----------------|-------------|------|--------|
| | The height of a woman | 1.5 | $1\frac{2}{3}$ | 150 | 5 | 60 |

17. 10 cm = $\frac{10 \text{ cm}}{1} \cdot \frac{1 \text{ in.}}{2.54 \text{ cm}} \approx 3.94 \text{ in.}$

The balance beam is approximately 3.94 inches wide.

21. 200 mg = 0.2 g
$$\approx \frac{0.2 \text{ g}}{1} \cdot \frac{0.04 \text{ oz}}{1 \text{ g}} \approx 0.008 \text{ oz}$$

- **25.** 16 billion km $\approx \frac{16 \text{ billion km}}{1} \cdot \frac{0.62 \text{ mi}}{1 \text{ km}} \approx 9.92 \text{ billion mi}$ 16 billion kilometers is approximately 9.92 billion miles.
- **29.** 4500 km $\approx \frac{4500 \text{ km}}{1} \cdot \frac{0.62 \text{ mi}}{1 \text{ km}} \approx 2790 \text{ mi}$
- The trip is about 2790 miles. **33.** 1.5 lb - 1.25 lb = 0.25 lb $0.25 \text{ lb} \approx \frac{0.25 \text{ lb}}{1} \cdot \frac{0.45 \text{ kg}}{1 \text{ lb}} \cdot \frac{1000 \text{ g}}{1 \text{ kg}} \approx 112.5 \text{ g}$ The difference is approximately 112.5 grams.

37.
$$8 \text{ m} \approx \frac{8 \text{ m}}{1} \cdot \frac{3.28 \text{ ft}}{1 \text{ m}} \approx 26.24 \text{ ft}$$

The base diameter is approximately 26.24 feet.

Solutions to Selected Exercises

41. One dose every 4 hours results in $\frac{24}{4} = 6$ doses per day and $6 \times 7 = 42$ doses per week. $5 \text{ ml} \times 42 = 210 \text{ ml}$ $210 \text{ ml} \approx \frac{210 \text{ ml}}{1} \cdot \frac{1 \text{ fl oz}}{29.57 \text{ ml}} \approx 7.1 \text{ fl oz}$ 8 fluid ounces of medicine should be purchased. 45. A liter has greater capacity than a quart; b. **49.** An $8\frac{1}{2}$ -ounce glass of water has a capacity of about $250 \text{ ml}\left(\frac{1}{4}\text{ L}\right); \mathbf{d}.$ **53.** $6 \cdot 4 + 5 \div 1 = 24 + 5 = 29$ **57.** 3 + 5(19 - 17) - 8 = 3 + 5(2) - 8= 3 + 10 - 8= 13 - 8 **61.** BSA = $\sqrt{\frac{90 \times 182}{3600}} \approx 2.13$ The BSA is approximately 2.13 sq m. **65.** 60 in. = $\frac{60 \text{ in.}}{1} \cdot \frac{2.54 \text{ cm}}{1 \text{ in.}} = 152.4 \text{ cm}$ $150 \text{ lb} \approx \frac{150 \text{ lb}}{1} \cdot \frac{0.45 \text{ kg}}{1 \text{ lb}} \approx 67.5 \text{ kg}$ $BSA \approx \sqrt{\frac{67.5 \times 152.4}{3600}} \approx 1.690$ The BSA is approximately 1.69 sq m. **69.** $20 \text{ m} \times 40 \text{ m} = 800 \text{ sq m}$ $20 \text{ m} \approx \frac{20 \text{ m}}{1} \cdot \frac{3.28 \text{ ft}}{1 \text{ m}} \approx 65.6 \text{ ft}$ $40 \text{ m} \approx \frac{40 \text{ m}}{1} \cdot \frac{3.28 \text{ ft}}{1 \text{ m}} \approx 131.2 \text{ ft}$ $20 \text{ m} \times 40 \text{ m} \approx 65.6 \text{ ft} \times 131.2 \text{ ft} \approx 8606.72 \text{ sq ft}$ The area is 800 sq m or approximately 8606.72 sq ft. **Exercise Set 7.5**

1.
$$C = \frac{5}{9}(F - 32)$$

 $= \frac{5}{9}(41 - 32)$
 $= \frac{5}{9}(9)$
 $= 5$
 $41^{\circ}F \text{ is } 5^{\circ}C.$
5. $F = \frac{9}{5}C + 32$
 $= \frac{9}{5}(60) + 32$
 $= 108 + 32$
 $= 140$
 $60^{\circ}C \text{ is } 140^{\circ}F.$
9. $C = \frac{5}{9}(F - 32)$
 $= \frac{5}{9}(62 - 32)$
 $= \frac{5}{9}(30)$
 ≈ 16.7
 $62^{\circ}F \text{ is } 16.7^{\circ}C.$

13. F = 1.8C + 32= 1.8(92) + 32= 165.6 + 32= 197.6 92°C is 197.6°F. **17.** C = $\frac{5}{9}(F - 32)$ $=\frac{5}{9}(122-32)$ $=\frac{5}{9}(90)$ = 50122°F is 50°C. **21.** C = $\frac{5}{9}(F - 32)$ $=\frac{5}{9}(212-32)$ $=\frac{5}{9}(180)$ = 100212°F is 100°C. **25.** F = 1.8C + 32= 1.8(118) + 32= 212.4 + 32= 244.4118°C is 244.4°F. **29.** C = $\frac{5}{9}$ (F - 32) $=\frac{5}{9}(70-32)$ $=\frac{5}{9}(38)$ ≈ 21.1 70°F is 21.1°C. **33.** 4 cm + 3 cm + 5 cm = (4 + 3 + 5) cm = 12 cm37. False; the freezing point of water is 32°F. **41.** C = $\frac{5}{9}(F - 32)$ $=\frac{5}{9}(9,000,000,000,000-32)$ $=\frac{5}{9}(8,999,999,999,968)$ $\approx 4.999.999.999.982$

 $\approx 5,000,000,000,000$

9,000,000,000,000°F is approximately 5,000,000,000,000°C.

45. No, a fever of 40°F is not reasonable.

49. Yes, a fever of 40°C is reasonable.

Exercise Set 7.6

1. energy = 3 pounds \cdot 380 feet = 1140 foot-pounds 5. energy = $\frac{2.5 \text{ tons}}{1} \cdot \frac{2000 \text{ pounds}}{1 \text{ ton}} \cdot 85$ feet

$$= 425,000 \text{ foot-pounds}$$

9. 1000 BTU = 1000 BTU $\cdot \frac{778 \text{ foot-pounds}}{1 \text{ BTU}}$
= 778,000 foot-pounds

13. 34,130 BTU = 34,130 BTU
$$\cdot \frac{778 \text{ foot-pounds}}{1 \text{ BTU}}$$

$$= 26,553,140$$
 foot-pounds

17. total hours = $1 \cdot 7 = 7$ hours calories = $7 \cdot 115 = 805$ calories Copyright 2019 Pearson Education, Inc.

21. total hours $=\frac{1}{3} \cdot 6 = 2$ hours calories = $2 \cdot 720 = 1440$ calories **25.** miles $=\frac{3500}{200}=17.5$ miles 710 29. 18Ø - 17 163 **33.** energy = 123.9 pounds $\cdot \frac{9 \text{ inches}}{1} \cdot \frac{1 \text{ foot}}{12 \text{ inches}}$ 12 inches = 92.925 foot-pounds **37.** answers may vary Chapter 7 Test 23 1. 12)280 - 24 40 - 36 4 280 inches = 23 feet 4 inches **5.** 38 pt = $\frac{38 \text{ pt}}{1} \cdot \frac{1 \text{ qt}}{2 \text{ pt}} \cdot \frac{1 \text{ gal}}{4 \text{ qt}}$ $=\frac{38}{8}$ gal $=\frac{19}{4}$ gal $=4\frac{3}{4}$ gal **9.** 4.3 dg = $\frac{4.3 \text{ dg}}{1} \cdot \frac{1 \text{ g}}{10 \text{ dg}} = \frac{4.3}{10} \text{ g} = 0.43 \text{ g}$ **13.** 2 ft 9 in. \times 3 = 6 ft 27 in. = 6 ft + 2 ft 3 in.= 8 ft 3 in.**17.** C = $\frac{5}{9}$ (F - 32) $=\frac{5}{9}(84-32)$ $=\frac{5}{9}(52)$ ≈ 28.9 84°F is 28.9°C. **21.** 88 m + 340 cm = 88 m + 3.40 m = 91.4 mThe span is 91.4 meters. **25.** C = $\frac{5}{9}$ (F - 32) $=\frac{5}{9}(134-32)$ $=\frac{5}{9}(102)$ ≈ 56.7 134°F is 56.7°C. **29.** $5 \text{ km} \approx \frac{5 \text{ km}}{1} \cdot \frac{0.62 \text{ mi}}{1 \text{ km}} \approx 3.1 \text{ mi}$ 5 km is about 3.1 mi. 33. 1 hour 1 day She burns 900 calories.

Chapter 8

Exercise Set 8.1

- **1.** The figure extends indefinitely in two directions. It is line CD, line l, or \overrightarrow{CD} .
- **5.** The figure has two rays with a common endpoint. It is an angle, which can be named $\angle GHI$, $\angle IHG$, or $\angle H$.
- **9.** Two other ways to name $\angle x$ are $\angle CPR$ and $\angle RPC$.
- **13.** $\angle S$ is a straight angle.
- **17.** $\angle Q$ measures between 90° and 180°. It is an obtuse angle.
- **21.** The complement of an angle that measures 23° is an angle that measures $90^{\circ} 23^{\circ} = 67^{\circ}$.
- **25.** The complement of an angle that measures 58° is an angle that measures $90^{\circ} 58^{\circ} = 32^{\circ}$.
- **29.** $52^{\circ} + 38^{\circ} = 90^{\circ}$, so $\angle PNQ$ and $\angle QNR$ are complementary. $60^{\circ} + 30^{\circ} = 90^{\circ}$, so $\angle MNP$ and $\angle RNO$ are complementary.
- **33.** $m \angle x = 74^\circ 47^\circ = 27^\circ$
- **37.** $\angle x$ and the angle marked 150° are supplementary, so $m \angle x = 180^\circ 150^\circ = 30^\circ$. $\angle y$ and the angle marked 150° are vertical angles, so $m \angle y = 150^\circ$. $\angle z$ and $\angle x$ are vertical angles so $m \angle z = m \angle x = 30^\circ$.
- 41. $\angle x$ and the angle marked 80° are supplementary, so $m \angle x = 180^{\circ} 80^{\circ} = 100^{\circ}$. $\angle y$ and the angle marked 80° are alternate interior angles, so $m \angle y = 80^{\circ}$. $\angle x$ and $\angle z$ are corresponding angles, so $m \angle z = m \angle x = 100^{\circ}$.
- **45.** $\angle x$ can also be named $\angle ABC$ or $\angle CBA$.

49.
$$m \angle ABC = 15$$

53. *m∠DBA* = *m∠DBC* + *m∠CBA*
= 50° + 15°
= 65°
57.
$$\frac{7}{8} + \frac{1}{4} = \frac{7}{8} + \frac{2}{8} = \frac{9}{8}$$
 or $1\frac{1}{8}$
61. $3\frac{1}{3} - 2\frac{1}{2} = \frac{10}{3} - \frac{5}{2}$
= $\frac{20}{6} - \frac{15}{6}$
= $\frac{5}{6}$
65. Since there are 360° in a full revolut

- **65.** Since there are 360° in a full revolution, there are 360° around the earth at the equator.
- **69.** The complement of an angle that measures 45° is an angle with measure $90^{\circ} 45^{\circ} = 45^{\circ}$.
- **73.** True; because 120° is less than 180°, it is possible to find the supplement of a 120° angle.
- 77. no; answers may vary

Exercise Set 8.2

- 1. The figure has five sides, so it is a pentagon.
- **5.** The figure has four sides, so it is a quadrilateral.
- **9.** All three sides of the triangle have the same length, therefore the triangle is equilateral.
- **13.** Two sides of the triangle have the same length, therefore the triangle is isosceles.
- **17.** $m \angle x = 180^\circ 95^\circ 72^\circ = 13^\circ$
- **21.** Twice the radius of a circle is its diameter.
- 25. A quadrilateral with opposite sides parallel is a parallelogram.

29. $d = 2 \cdot r = 2 \cdot 7$ m = 14 m

33. $d = 2 \cdot r = 2 \cdot 20.3 \text{ cm} = 40.6 \text{ cm}$

- **37.** The solid is a cylinder.
- **41.** The solid is a cone.
- **45.** The object has the shape of a rectangular solid.
- **49.** The object has the shape of a pyramid.

53. $r = \frac{1}{2}d = \frac{1}{2} \cdot 26$ miles = 13 miles

57. 2(18) + 2(36) = 36 + 72 = 108

- **61.** True; since all four sides of a square are equal in length and a square is a parallelogram, a square is also a rhombus.
- **65.** False; a pentagon has five sides, so it cannot be a quadrilateral, which has four sides.

69. answers may vary

Exercise Set 8.3

Solutions to Selected Exercises

1. $P = 2 \cdot l + 2 \cdot w$

 $= 2 \cdot 17 \text{ ft} + 2 \cdot 15 \text{ ft}$

= 34 ft + 30 ft

 $= 64 \, \mathrm{ft}$

The perimeter is 64 feet.

- 5. P = a + b + c= 5 in. + 7 in. + 9 in.
 - = 21 in.

The perimeter is 21 inches.

- 9. All sides of a regular triangle have the same length. P = a + b + c = 14 in. + 14 in. + 14 in. = 42 in. The perimeter is 42 inches.
- **13.** Sum the lengths of the sides.
 - P = 5 ft + 3 ft + 2 ft + 7 ft + 4 ft= 21 ft
 - The perimeter is 21 feet.
- **17.** $P = 2 \cdot l + 2 \cdot w$
 - $= 2 \cdot 120 \text{ yd} + 2 \cdot 53 \text{ yd}$
 - = 240 yd + 106 yd

= 346 yd

The perimeter of the football field is 346 yards.

21. The amount of stripping needed is 22 feet. 22 feet \cdot \$2.50 per foot = \$55

The total cost of the stripping is \$55.

25. $P = 4 \cdot s = 4 \cdot 7$ in. = 28 in. The perimeter is 28 inches.

29. The unmarked vertical side must have length 28 m - 20 m = 8 m.

The unmarked horizontal side must have length 20 m - 17 m = 3 m.Sum the lengths of the sides. P = 17 m + 8 m + 3 m + 20 m + 20 m + 28 m= 96 m

The perimeter is 96 meters.

33. The unmarked vertical side must have length 5 cm + 14 cm = 19 cm. The unmarked horizontal side must have length 18 cm - 9 cm = 9 cm. Sum the lengths of the sides.
P = 18 cm + 19 cm + 9 cm + 14 cm + 9 cm + 5 cm = 74 cm The perimeter is 74 centimeters. **37.** $C = 2 \cdot \pi \cdot r$

$$= 2 \cdot \pi \cdot 8 \text{ mi}$$

- $= 16\pi$ mi
- ≈ 50.24 mi

The circumference is exactly 16π miles, which is approximately 50.24 miles.

- **41.** $C = \pi \cdot d = \pi \cdot 150 \text{ ft} = 150\pi \text{ ft} \approx 471 \text{ ft}$ The circumference of the barn is 150π feet, which is approximately 471 feet.
- **45.** Sum the lengths of the sides.
 - P = 9 mi + 6 mi + 11 mi + 4.7 mi= 30.7 mi
 - The perimeter is 30.7 miles.
- **49.** The sides of a regular pentagon all have the same length. Sum the lengths of the sides.
 - P = 8 mm + 8 mm + 8 mm + 8 mm + 8 mm= 40 mm
 - The perimeter is 40 millimeters.
- **53.** $5 + 6 \cdot 3 = 5 + 18 = 23$
- **57.** $72 \div (2 \cdot 6) = 72 \div 12 = 6$
- **61. a.** The first age category that 8-year-old children fit into is "Under 9." Thus the minimum width is 30 yards, and the minimum length is 40 yards.
 - **b.** $P = 2 \cdot l + 2 \cdot w$

$$= 2 \cdot 40 \text{ yd} + 2 \cdot 30 \text{ yd}$$

- = 80 yd + 60 yd
- = 140 yd
- The perimeter of the field is 140 yards.
- **65. a.** Smaller circle:
 - $C = 2 \cdot \pi \cdot r$
 - $= 2 \cdot \pi \cdot 10 \text{ m}$
 - $= 20\pi \,\mathrm{m}$
 - $\approx 62.8 \text{ m}$ Larger circle:
 - $C = 2 \cdot \pi \cdot r$

$$= 2 \cdot \pi \cdot 20 \text{ m}$$

$$= 40\pi \,\mathrm{m}$$

- $\approx 125.6 \text{ m}$
- **b.** Yes, when the radius of a circle is doubled, the circumference is also doubled.
- 69. Each of the three linear sides has length 6 meters. The length of the curved side is half of the circumference of a circle with diameter 6 meters, or $\frac{1}{2}\pi \cdot d = \frac{1}{2}\pi \cdot 6$ meters $= 3\pi$ meters ≈ 9.4 meters 6 m + 6 m + 9.4 m = 27.4 m

73.
$$P = 2 \cdot l + 2 \cdot w$$

$$31 \text{ ft} = 2 \cdot 9 \text{ ft} + 2 \cdot w$$

$$31 \text{ ft} = 18 \text{ ft} + 2 \cdot w$$

$$13 \text{ ft} = 2 \cdot w$$

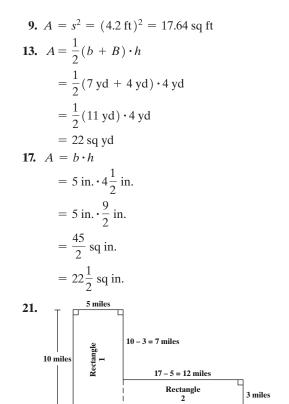
$$6.5 \text{ ft} = w$$

The width is 6.5 feet.

Exercise Set 8.4

1.
$$A = l \cdot w = 3.5 \text{ m} \cdot 2 \text{ m} = 7 \text{ sq m}$$

5. $A = \frac{1}{2} \cdot b \cdot h = \frac{1}{2} \cdot 6 \text{ yd} \cdot 5 \text{ yd} = 15 \text{ sq yd}$



Rectangle 1: $A = l \cdot w = 10 \text{ mi} \cdot 5 \text{ mi} = 50 \text{ sq mi}$ Rectangle 2: $A = l \cdot w = 12 \text{ mi} \cdot 3 \text{ mi} = 36 \text{ sq mi}$ The area of the figure is 50 sq mi + 36 sq mi = 86 sq mi.

25.
$$A = \pi r^2 = \pi (6 \text{ in.})^2 = 36\pi \text{ sq in.} \approx 113\frac{1}{7} \text{ sq in.}$$

29. $A = l \cdot w = 505$ ft $\cdot 255$ ft = 128,775 sq ft

The area of the flag is 128,775 square feet.

17 miles

33. $A = l \cdot w = 16$ in. $\cdot 8$ in. = 128 sq in.

128 sq in.
$$\cdot \frac{1 \text{ sq ft}}{144 \text{ sq in.}} = \frac{128}{144} \text{ sq ft} = \frac{8}{9} \text{ sq ft}$$

The side has area 128 square inches, which is $\frac{\delta}{\Omega}$ square foot.

- **37.** $A = l \cdot w = 7$ ft $\cdot 6$ ft = 42 sq ft
 - $4 \cdot 42$ sq ft = 168 sq ft

Four panels have an area of 168 square feet.

41. a.
$$A = \frac{1}{2}(b + B) \cdot h$$

 $= \frac{1}{2}(25 \text{ ft} + 36 \text{ ft}) \cdot 12\frac{1}{2} \text{ ft}$
 $= \frac{1}{2} \cdot 61 \text{ ft} \cdot 12\frac{1}{2} \text{ ft}$
 $= 381\frac{1}{4} \text{ sq ft}$

To the nearest square foot, the area is 381 square feet.

- **b.** Since each square covers 100 square feet, 4 squares of shingles need to be purchased.
- **45.** Sum the lengths of the sides.

$$3 \text{ ft} + 3\frac{1}{2} \text{ ft} + 6 \text{ ft} + 8\frac{1}{2} \text{ ft} + 4 \text{ ft} = 25 \text{ ft}$$

The perimeter is 25 feet.

- **49.** A fence goes around the edge of a yard, thus the situation involves perimeter.
- **53.** Paint covers the surface of a wall, thus the situation involves area.
- **57.** Note that the dimensions given are the diameters of the pizzas.

12-inch pizza: $r = \frac{1}{2} \cdot d = \frac{1}{2} \cdot 12$ in. = 6 in. $A = \pi \cdot r^2 = \pi (6 \text{ in.})^2 = 36\pi \text{ sq in.}$

Price per square inch = $\frac{\$10}{36\pi \text{ sq in.}} \approx \0.0884

8-inch pizzas:

$$r = \frac{1}{2} \cdot d = \frac{1}{2} \cdot 8 \text{ in.} = 4 \text{ in.}$$

$$A = \pi \cdot r^2 = \pi (4 \text{ in.})^2 = 16\pi \text{ sq in.}$$

$$2 \cdot A = 2 \cdot 16\pi \text{ sq in.} = 32\pi \text{ sq in.}$$

Price per square inch: $\frac{\$9}{32\pi \text{ sq in.}} \approx \0.0895
Since the price per square inch for the 12 inc

Since the price per square inch for the 12-inch pizza is less, the 12-inch pizza is the better deal.

61. The area of the shaded region is the area of the square minus the area of the circle.

Square:
$$A = s^2 = (6 \text{ in.})^2 = 36 \text{ sq in.}$$

Circle: $r = \frac{1}{2} \cdot d = \frac{1}{2}(6 \text{ in.}) = 3 \text{ in.}$
 $A = \pi \cdot r^2 = \pi (3 \text{ in.})^2 = 9\pi \text{ sq in.} \approx 28.26 \text{ sq in.}$
36 sq in. $- 28.26 \text{ sq in.} = 7.74 \text{ sq in.}$

The shaded region has area of approximately 7.74 square inches.

65. The skating area is a rectangle with a half circle on each end. Rectangle: $A = l \cdot w = 22 \text{ m} \cdot 10 \text{ m} = 220 \text{ sq m}$

Half circles:
$$A = 2 \cdot \frac{1}{2} \cdot \pi \cdot r^2$$

= $\pi (5 \text{ m})^2$
= $25\pi \text{ sg m} \approx 78.5 \text{ sg m}$

220 sq m + 78.5 sq m = 298.5 sq m

The skating surface has area of 298.5 square meters. **69.** no; answers may vary

Exercise Set 8.5

1.
$$V = l \cdot w \cdot h = 6$$
 in. $\cdot 4$ in. $\cdot 3$ in. $= 72$ cu in.
5. $V = \frac{1}{3}\pi \cdot r^2 \cdot h = \frac{1}{3}\pi \cdot (2 \text{ yd})^2 \cdot 3 \text{ yd} = 4\pi \text{ cu yd} \approx 12\frac{4}{7} \text{ cu yd}$
9. $V = \pi \cdot r^2 \cdot h$
 $= \pi (1 \text{ in.})^2 \cdot 9 \text{ in.}$
 $= 9\pi \text{ cu in.}$
 $\approx 28\frac{2}{7} \text{ cu in.}$
13. $V = s^3 = \left(1\frac{1}{3}\text{ in.}\right)^3$
 $= \left(\frac{4}{3}\text{ in.}\right)^3$
 $= \frac{64}{27} \text{ cu in.}$
 $= 2\frac{10}{27} \text{ cu in.}$

Solutions to Selected Exercises

17. Note: $1\frac{3}{10}$ in. $=\frac{13}{10}$ in. $V = \frac{1}{3}s^2h$ $V = \frac{1}{3}s^{2}h$ $= \frac{1}{3}(5 \text{ in})$ $= \frac{1}{3}\cdot 25 \cdot \frac{1}{3} \cdot 25 \cdot \frac{1}{3} \cdot 25 \cdot \frac{1}{6}$ $= 10\frac{5}{6}\text{ cm}$ 21. $V = \frac{4}{3}\pi r^{3}$ $= \frac{4}{3}\pi (7)$ $= \frac{1372}{3}r^{2}$ 25. $V = \frac{4}{3}\pi r^{3}$ $= \frac{4}{3}\pi (6)$ $= \frac{4}{3}\pi (6)$ $=\frac{1}{3}(5 \text{ in.})^2 \cdot \frac{13}{10} \text{ in.}$ $=\frac{1}{3}\cdot 25\cdot \frac{13}{10}\,\mathrm{cu\,in.}$ $= 10\frac{5}{6}$ cu in. $=\frac{4}{3}\pi(7 \text{ in.})^3$ $=\frac{1372}{3}\pi$ cu in. or 457 $\frac{1}{3}\pi$ cu in. $=\frac{4}{3}\pi(6\,\mathrm{ft})^3$ $=\frac{4}{3}\pi(216\,\mathrm{cu\,ft})$ $=\frac{4}{3}\cdot 216\cdot\pi$ cu ft $= 288\pi$ cu ft **29.** $r = \frac{1}{2} \cdot d = \frac{1}{2} \cdot 3$ m = 1.5 m $V = \frac{4}{3}\pi r^3$ $=\frac{4}{3}\pi(1.5\,\mathrm{m})^3$ $=\frac{4}{3}\pi \cdot 3.375 \,\mathrm{cu}\,\mathrm{m}$ $= \pi \cdot 4.5 \,\mathrm{cu} \,\mathrm{m}$ ≈ 14.13 cu m The exact volume is 4.5π cubic meters, which is about 14.13 cubic meters. **33.** V = lwh = (2 in.)(2 in.)(2.2 in.) = 8.8 cu in.The volume of the Space Cube is 8.8 cubic inches. **37.** $5^2 = 5 \cdot 5 = 25$ **41.** $1^2 + 2^2 = 1 \cdot 1 + 2 \cdot 2 = 1 + 4 = 5$ **45.** $r = \frac{1}{2} \cdot d = \frac{1}{2} \cdot 20 \text{ m} = 10 \text{ m}$ $V = \frac{1}{2} \cdot \frac{4}{3} \pi r^3$ $=\frac{2}{-\pi}(10 \text{ m})^3$

$$= \frac{2}{3}\pi \cdot 1000 \text{ cu m}$$
$$= \frac{2000}{3}\pi \text{ cu m}$$
$$\approx \frac{2000}{3} \cdot 3.14 \text{ cu m}$$

The volume of the dome is about 2093.33 cubic meters.

49. Kennel (a):

$$2\frac{1}{12} \text{ ft} \cdot 1\frac{8}{12} \text{ ft} \cdot 1\frac{7}{12} \text{ ft} = \left(\frac{25}{12} \cdot \frac{20}{12} \cdot \frac{19}{12}\right) \text{ cu ft}$$

$$= \frac{9500}{1728} \text{ cu ft}$$

$$= \frac{2375}{432} \text{ cu ft}$$

$$\approx 5.5 \text{ cu ft}$$
Kennel (b):

$$1\frac{1}{12} \text{ ft} \cdot 2 \text{ ft} \cdot 2\frac{8}{12} \text{ ft} = \left(\frac{13}{12} \cdot \frac{24}{12} \cdot \frac{32}{12}\right) \text{ cu ft}$$

$$= \frac{9984}{1728} \text{ cu ft}$$

$$=\frac{52}{9} \operatorname{cu}$$

ft

 $\approx 5.8 \text{ cu ft}$

Kennel (b) is larger.

Exercise Set 8.6

1. $\sqrt{4} = 2$ because $2^2 = 4$.

5.
$$\sqrt{\frac{1}{81}} = \frac{1}{9}$$
 because $\frac{1}{9} \cdot \frac{1}{9} = \frac{1}{81}$.

- **9.** $\sqrt{3} \approx 1.732$
- **13.** $\sqrt{47} \approx 6.856$
- **17.** Since 38 is between $36 = 6 \cdot 6$ and $49 = 7 \cdot 7$, $\sqrt{38}$ is between 6 and 7; $\sqrt{38} \approx 6.164$.

21.
$$\sqrt{256} = 16$$
 because $16^2 = 256$

25.
$$\sqrt{\frac{49}{144}} = \frac{7}{12}$$
 because $\left(\frac{7}{12}\right)^2 = \frac{7}{12} \cdot \frac{7}{12} = \frac{49}{144}$.
29. hypotenuse $= \sqrt{(\log)^2 + (other \log)^2}$
 $= \sqrt{(5)^2 + (12)^2}$
 $= \sqrt{25 + 144}$
 $= \sqrt{169}$
 $= 13$

The missing length is 13 inches.

33. hypotenuse =
$$\sqrt{(\log)^2 + (\text{other leg})^2}$$

= $\sqrt{(22)^2 + (48)^2}$
= $\sqrt{484 + 2304}$
= $\sqrt{2788}$
 ≈ 52.802

The missing length is approximately 52.802 meters.

37.
ypotenuse =
$$\sqrt{(leg)^2 + (other leg)^2}$$

= $\sqrt{(3)^2 + (4)^2}$
= $\sqrt{9 + 16}$

 $= \sqrt{9 + 16}$ $= \sqrt{25}$ = 5

The hypotenuse has length 5 units.

41.
[?]
hypotenuse =
$$\sqrt{(\log)^2 + (\text{other leg})^2}$$

= $\sqrt{(10)^2 + (14)^2}$
= $\sqrt{100 + 196}$
= $\sqrt{296}$
 ≈ 17.205

The hypotenuse is about 17.205 units.

45.
30
hypotenuse =
$$\sqrt{(\log)^2 + (\text{other leg})^2}$$

= $\sqrt{(30)^2 + (30)^2}$
= $\sqrt{900 + 900}$
= $\sqrt{1800}$
 ≈ 42.426

The hypotenuse is about 42.426 units.

49.
7.5
49.
hypotenuse =
$$\sqrt{(\log)^2 + (\text{other leg})^2}$$

= $\sqrt{(7.5)^2 + (4)^2}$
= $\sqrt{56.25 + 16}$
= $\sqrt{72.25}$
= 8.5
The hypotenuse has length 8.5 units.

53.
$$\log = \sqrt{(\text{hypotenuse})^2 - (\text{other leg})^2}$$

= $\sqrt{(32)^2 - (20)^2}$
= $\sqrt{1024 - 400}$
= $\sqrt{624}$
 ≈ 25.0

The tree is about 25 feet tall.

57.
$$\frac{n}{6} = \frac{2}{3}$$

 $3 \cdot n = 2 \cdot 6$
 $3 \cdot n = 12$
 $n = \frac{12}{3}$
 $n = 4$
61. $\frac{3}{n} = \frac{7}{14}$
 $3 \cdot 14 = 7 \cdot n$
 $42 = 7 \cdot n$
 $\frac{42}{7} = n$
 $6 = n$

65. From Exercise 19, $\sqrt{101}$ is between 10 and 11. Since 101 is closer to 100 than it is to 121, $\sqrt{101}$ is approximately $10.\sqrt{101} \approx 10.050$

69.
$$\sqrt{(25)^2 + (60)^2} = \sqrt{625 + 3600}$$

= $\sqrt{4225}$
= 65
Since $\sqrt{(25)^2 + (60)^2} = 65$, the set forms the

Since $\sqrt{(25)^2 + (60)^2} = 65$, the set forms the sides of a right triangle.

Exercise Set 8.7

- **1.** The triangles are congruent by Side-Side-Side.
- **5.** The triangles are congruent by Angle-Side-Angle.

9.
$$\frac{22}{11} = \frac{14}{7} = \frac{12}{6} = \frac{2}{1}$$

The ratio of corresponding sides is $\frac{2}{1}$.

| The facto of corresponding sides is $\frac{-}{1}$. | | | | |
|--|---|--|--|--|
| 13. $\frac{n}{2} = \frac{9}{6}$ | 17. $\frac{n}{3.75} = \frac{12}{9}$ | | | |
| 13. $\frac{n}{3} = \frac{9}{6}$ | 17. $\frac{1}{3.75} = \frac{1}{9}$ | | | |
| $6 \cdot n = 3 \cdot 9$ | $9 \cdot n = 12 \cdot 3.75$ | | | |
| $6 \cdot n = 27$ | $9 \cdot n = 45$ | | | |
| | | | | |
| $n = \frac{27}{6}$ | $n = \frac{45}{9}$ | | | |
| 0 | · · · · · · · · · · · · · · · · · · · | | | |
| n = 4.5 | n = 5 | | | |
| | | | | |
| 21. $\frac{n}{3.25} = \frac{17.5}{3.25}$ | 25. $\frac{n}{60} = \frac{15}{32}$ | | | |
| 3.25 3.25 | 00 52 | | | |
| $3.25 \cdot n = 17.5 \cdot 3.25$ | $32 \cdot n = 60 \cdot 15$ | | | |
| $3.25 \cdot n = 56.875$ | $32 \cdot n = 900$ | | | |
| 56.875 | $n = \frac{900}{32}$ | | | |
| $n = \frac{56.875}{3.25}$ | $n = \frac{1}{32}$ | | | |
| n = 17.5 | n = 28.125 | | | |
| | 49 | | | |
| 29. $\frac{n}{13} = \frac{80}{2}$ | 33. $\frac{n}{5} = \frac{48}{4}$ | | | |
| | 5 7 | | | |
| $2 \cdot n = 80 \cdot 13$ | $\frac{n}{5} = \frac{12}{1}$ | | | |
| $2 \cdot n = 1040$ | 5 1 | | | |
| $n = \frac{1040}{2}$ | $1 \cdot n = 12 \cdot 5$ | | | |
| n = -2 | n = 60 | | | |
| n = 520 | The tree is 60 feet tall. | | | |
| The observation deck is | | | | |
| 520 feet high. | | | | |
| 10 | 1 | | | |
| 37. $\frac{n}{55} = \frac{19}{20}$ | 41. ¹ / _{3.60} | | | |
| 20 20 | + 0.41 | | | |
| $20 \cdot n = 55 \cdot 19$ | $+ 0.41 \\ - 4.01$ | | | |
| $20 \cdot n = 1045$ | 1.01 | | | |
| $n = \frac{1045}{20}$ | | | | |
| $n = \frac{1}{20}$ | | | | |
| n = 52.25 | | | | |
| Pete would place 52 neon | | | | |
| tetras in a 55-gallon tank. | | | | |
| tetras in a 55 ganon tank. | | | | |
| n 5 in. | | | | |
| 45. $\frac{n}{7 \text{ in.}} = \frac{5 \text{ in.}}{9 \text{ in.}}$ | | | | |
| | | | | |
| $\frac{n}{7} = \frac{5}{9}$ | | | | |
| $7 \cdot 5 = 9 \cdot n$ | | | | |
| | | | | |
| $35 = 9 \cdot n$ | | | | |
| $\frac{35}{9} = n$ | | | | |
| | | | | |
| $n = \frac{35}{9} \text{ or } 3\frac{8}{9} \text{ in.}$ | | | | |
| $n = 9^{-013} 9^{-013}$ | | | | |
| | | | | |

The new width is $3\frac{8}{9}$ in. Since the print area is now $3\frac{8}{9}$ in.

by 5 in., it will not fit on a 3-by-5 inch index card. (Lengths are same but $3\frac{8}{0} > 3$.)

49. answers may vary

Chapter 8 Test

Solutions to Selected Exercises

- 1. The complement of an angle that measures 78° is an angle that measures $90^{\circ} 78^{\circ} = 12^{\circ}$.
- 5. $\angle x$ and the angle marked 73° are vertical angles, so $m \angle x = 73^\circ$. $\angle x$ and $\angle y$ are alternate interior angles, so $m \angle y = m \angle x = 73^\circ$. $\angle x$ and $\angle z$ are corresponding angles, so $m \angle z = m \angle x = 73^\circ$.

9. Circumference:

- $C = 2 \cdot \pi \cdot r$
 - $= 2 \cdot \pi \cdot 9$ in.
 - $= 18\pi$ in.
 - ≈ 56.52 in.

Area:

- $A = \pi r^2$
 - $= \pi (9 \text{ in.})^2$
 - $= 81\pi$ sq in.
 - ≈ 254.34 sq in.

13. $V = l \cdot w \cdot h = 5 \text{ ft} \cdot 3 \text{ ft} \cdot 2 \text{ ft} = 30 \text{ cu ft}$

17. $P = 4 \cdot s = 4 \cdot 4$ in. = 16 in.

The perimeter of the photo is 16 inches.

21. First find the area of the lawn. $A = l \cdot w = 123.8 \text{ ft} \cdot 80 \text{ ft} = 9904 \text{ sq ft}$

0.02 ounce per square foot is $\frac{0.02 \text{ oz}}{1 \text{ sq ft}}$.

 $\frac{0.02 \text{ oz}}{1 \text{ sq ft}} \cdot 9904 \text{ sq ft} = 198.08 \text{ oz}$

Vivian needs to purchase 198.08 ounces of insecticide.

Chapter 9

Exercise Set 9.1

- 1. Kansas has the greatest number of wheat icons, so the greatest acreage of wheat was planted in the state of Kansas.
- **5.** The states with fewer than 3 wheat icons are South Dakota, Colorado, and Washington, so the states of South Dakota, Colorado, and Washington plant less than 3 million acres in wheat.
- 9. The year 2013 has 4 flames and each flames represents 12,000 wildfires, so there were approximately 4(12,000) = 48,000 wildfires in 2013.
- 13. 2012 has 5.5 flames and 2013 has 4 flames, which is 1.5 less. Thus, the decrease in the number of wildfires from 2012 to 2013 was about 1.5(12,000) = 18,000.
- **17.** The longest bar corresponds to September, so the month in which most hurricanes made landfall is September.
- **21.** Two of the 78 hurricanes that made landfall in August did

so in 2008. The fraction is
$$\frac{2}{78} = \frac{1}{39}$$

- **25.** The only bar corresponding to a city in the United States is the bar for New York City. The population is approximately 20.6 million or 20,600,000.
- 29. Fiber Content of Selected Foods

| | 1 | 2 | 3 | 4 | 5 |
|-----------------|---|------------------|---|---|---|
| Kidnev heans | | F | H | H | |
| 1000 | | | | | |
| 1711) | | | | | |
| Oatmeal (3/4 c) | | | | | |
| Peanut hutter | | _ | | | |
| 5 | | | | | |
| Dongoun (1 a) | | | | | |
| | ŀ | | | | |
| Potato, Daked | | | | | |
| Whole wheat | | - | - | | |
| bread (1 slice) | | $\left \right $ | | | |

- **33.** The height of the bar for 100–149 miles per week is 15, so 15 of the adults drive 100–149 miles per week.
- **37.** 15 of the adults drive 100–149 miles per week and 9 of the adults drive 150–199 miles per week, so 15 + 9 = 24 of the adults drive 100–199 miles per week.
- **41.** 9 of the 100 adults surveyed drive 150–199 miles per week, so the ratio is $\frac{9}{2}$

so the ratio is
$$\frac{100}{100}$$
.

- **45.** According to the bar graph, the population of 20- to 44-year-olds is projected to be 109 million in 2020.
- **49.** answers may vary

| - | Class Interval
(Scores) | | Class Frequency
(Number of Games) |
|----------------------------|------------------------------------|-------|---------------------------------------|
| 90- | 99 | 1 | 8 |
| Class In
(Acco
Balan | ount | Tally | Class Frequency
(Number of People) |
| \$200- | \$299 | 11111 | 6 |
| Number of Games | | | |
| | 70-79
80-89
90-99
100-109 | | |
| G | olf Scores | | |

- **65.** The highest point on the graph corresponds to 2003, so the average number of goals per game was the highest in 2003.
- **69.** The dots for 2001, 2007, and 2013 are below the 8-level, so the average number of goals per game was less than 8 in 2001, 2007, and 2013.
- **73.** 10% of 62 is $0.10 \cdot 62 = 6.2$

77.
$$\frac{17}{50} = \frac{17}{50} \cdot 100\% = \frac{17 \cdot 2 \cdot 50}{50}\% = 34\%$$

- **81.** The lowest point on the graph of low temperatures corresponds to Sunday. The low temperature on Sunday was 68°F.
- 85. answers may vary

Exercise Set 9.2

- **1.** The largest sector corresponds to the category "parent or guardian's home," so most of the students live in a parent or guardian's home.
- **5.** 180 of the students live in campus housing while 320 live in a parent or guardian's home.

A76

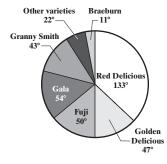
$$\frac{180}{320} = \frac{9}{16}$$

The ratio is $\frac{9}{16}$

- 9. 30% + 7% = 37%37% of the land on Earth is accounted for by Europe and Asia.
- 13. Australia accounts for 5% of the land on Earth. 5% of 57,000,000 = $0.05 \cdot 57,000,000$ = 2.850.000Australia is 2,850,000 square miles.
- 17. The second-largest sector corresponds to nonfiction, so the second-largest category of books is nonfiction.
- 21. Children's fiction accounts for 22% of the books. 22% of $125,600 = 0.22 \cdot 125,600$ = 27,632

The library has 27,632 children's fiction books.

| ~ - | | | |
|-----|------------------|---------|--|
| 25. | Type of Apple | Percent | Degrees in Sector |
| | Red Delicious | 37% | $37\% \text{ of } 360^\circ = 0.37(360^\circ) \approx 133^\circ$ |
| | Golden Delicious | 13% | $13\% \text{ of } 360^\circ = 0.13(360^\circ) \approx 47^\circ$ |
| | Fuji | 14% | $14\% \text{ of } 360^\circ = 0.14(360^\circ) \approx 50^\circ$ |
| | Gala | 15% | $15\% \text{ of } 360^\circ = 0.15(360^\circ) = 54^\circ$ |
| | Granny Smith | 12% | $12\% \text{ of } 360^\circ = 0.12(360^\circ) \approx 43^\circ$ |
| | Other varieties | 6% | $6\% \text{ of } 360^\circ = 0.06(360^\circ) \approx 22^\circ$ |
| | Braeburn | 3% | $3\% \text{ of } 360^\circ = 0.03(360^\circ) \approx 11^\circ$ |
| | | | |



- **29.** $20 = 2 \times 10 = 2 \times 2 \times 5 = 2^2 \times 5$
- **33.** $85 = 5 \times 17$

37. Pacific Ocean: $49\% \cdot 264,489,800 = 0.49 \cdot 264,489,800$ = 129,600,002 square kilometers

- **41.** $24\% \cdot 2800 = 0.24 \cdot 2800 = 672$ 672 respondents said that they spend \$0 online each month. number of respondents who spend \$0 672
- 45. number of respondents who spend 1-100 - 1736 $=\frac{12\cdot 56}{31\cdot 56}$ $\frac{12}{31}$
- 49. answers may vary

Exercise Set 9.3

1. Mean: $\frac{15 + 23 + 24 + 18 + 25}{5} = \frac{105}{5} = 21$

Median: Write the numbers in order: 15, 18, 23, 24, 25 The middle number is 23.

Mode: There is no mode, since each number occurs once.

5. Mean:

$$\underbrace{ 0.5 + 0.2 + 0.2 + 0.6 + 0.3 + 1.3 + 0.8 + 0.1 + 0.5}_{9}$$

$$=\frac{4.5}{2}$$

9 = 0.5

Median: Write the numbers in order:

0.1, 0.2, 0.2, 0.3, 0.5, 0.5, 0.6, 0.8, 1.3

The middle number is 0.5.

Mode: Since 0.2 and 0.5 occur twice, there are two modes, 0.2 and 0.5.

9. Mean: 27

$$\frac{17 + 2073 + 1972 + 1965 + 1819}{5} = \frac{10,546}{5} = 2109.2$$

The mean height of the five tallest buildings is 2109.2 feet. **13.** answers may vary

17. GPA =
$$\frac{4 \cdot 3 + 4 \cdot 3 + 4 \cdot 4 + 3 \cdot 3 + 2 \cdot 1}{3 + 3 + 4 + 3 + 1}$$

= $\frac{51}{14}$
 ≈ 3.64

- 21. Mode: 6.9 since this number appears twice.
- $\frac{\text{sum of 15 pulse rates}}{15} = \frac{1095}{15} = 73$ 25. Mean: -
- **29.** There are 9 rates lower than the mean. They are 66, 68, 71, 64, 71, 70, 65, 70, and 72

33. range =
$$20 - 8 = 12$$

37. range =
$$11 - 9 = 2$$

41. a. mean =
$$\frac{1 \cdot 5 + 1 \cdot 6 + 2 \cdot 7 + 5 \cdot 8 + 6 \cdot 9 + 2 \cdot 10}{1 + 1 + 2 + 5 + 6 + 2}$$

$$= \frac{139}{17} \approx 8.2$$

b. median: $\frac{n+1}{2} = \frac{17+1}{2} = 9$. Thus the median is the data item in the 9th position.

median = 8

c. mode: 9 occurs most often.
45. a. mean:
$$=\frac{2 \cdot 5 + 3 \cdot 10 + 6 \cdot 15 + 5 \cdot 20 + 1 \cdot 25}{2 + 3 + 6 + 5 + 1}$$

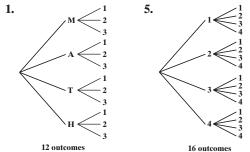
 $=\frac{255}{17} = 15$
b. median: $\frac{n+1}{2} = \frac{17 + 1}{2} = 9$. Thus the median is

the 2 2 data item in the 9th position. median = 15

c. mode: 15 occurs most often. **49.** $\frac{12}{12} = \frac{3 \cdot 4}{3} = \frac{3}{2}$ **53.** $\frac{35}{5 \cdot 7} = \frac{5 \cdot 7}{5 \cdot 7}$

57.
$$20 \quad 4.5 \quad 5 \quad 100 \quad 5.20 \quad$$

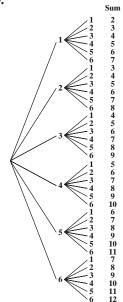
Exercise Set 9.4



A77



- **13.** A 1 or a 6 are two of the six possible outcomes. The probability is $\frac{2}{6} = \frac{1}{3}$.
- 17. Four of the six possible outcomes are numbers greater than 2. The probability is $\frac{4}{6} = \frac{2}{3}$.
- **21.** A 1, a 2, or a 3 are three of three possible outcomes. The probability is $\frac{3}{3} = 1$.
- **25.** One of the seven marbles is red. The probability is $\frac{1}{7}$.
- **29.** Four of the seven marbles are either green or red. The probability is $\frac{4}{7}$.
- **33.** The blood pressure did not change for 10 of the 200 people. The probability is $\frac{10}{200} = \frac{1}{20}$.
- **37.** $\frac{1}{2} \cdot \frac{1}{3} = \frac{1 \cdot 1}{2 \cdot 3} = \frac{1}{6}$
- **41.** One of the 52 cards is the king of hearts. The probability is $\frac{1}{52}$.
- **45.** Thirteen of the 52 cards are hearts. The probability is $\frac{13}{52} = \frac{1}{4}$.



Five of the 36 sums are 6. The probability is $\frac{5}{36}$.

53. answers may vary

Chapter 9 Test

1. There are $4\frac{1}{2}$ dollar symbols for the second week. Each dollar symbol corresponds to \$50.

$$4\frac{1}{2} \cdot \$50 = \frac{9}{2} \cdot \$50 = \frac{\$450}{2} = \$225$$

\$225 was collected during the second week.

- 5. The shortest bar corresponds to February. The normal monthly precipitation in February in Chicago is 3 centimeters.
- **9.** The line is above the 3 level for 2008 and 2011. Thus, the inflation rate was greater than 3% in 2008 and 2011
- **13.** People under 18 are expected to account for 22% of the U.S. population in 2020.

22% of 335 million = 0.22×335 million = 73.7 million

74 million people are projected to be under 18 in 2020.

17.

| Class Intervals
(Scores) | Tally | Class Frequency
(Number of Students) |
|-----------------------------|---------|---|
| 40–49 | | 1 |
| 50–59 | | 3 |
| 60–69 | | 4 |
| 70–79 | HH | 5 |
| 80–89 | HHT III | 8 |
| 90–99 | | 4 |

| 21 | |
|----------|--|
| <i>4</i> | |

| Grade | Point
Value | Credit
Hours | $\left(\frac{\text{Point}}{\text{Value}}\right) \cdot \left(\frac{\text{Credit}}{\text{Hours}}\right)$ | |
|-------|----------------|-----------------|--|--|
| А | 4 | 3 | 12 | |
| В | 3 | 3 | 9 | |
| С | 2 | 3 | 6 | |
| В | 3 | 4 | 12 | |
| А | 4 | 1 | 4 | |
| | Totals | 14 | 43 | |

$$\frac{43}{14} \approx 3.07$$

The grade point average is about 3.07.

25. a. mean =
$$\frac{3 \cdot 15 + 6 \cdot 20 + 7 \cdot 25 + 3 \cdot 30 + 8 \cdot 35}{3 + 6 + 7 + 3 + 8}$$

$$=\frac{710}{27}\approx 26.3$$

- **b.** median: $\frac{n+1}{2} = \frac{27+1}{2} = 14$. Thus, the median is the data item in the 14th position. median = 25 **c.** mode: 35 occurs most often
- **d.** range = 35 15 = 20
- **29.** A 3 or a 4 are two of the ten possible outcomes. The probability is $\frac{2}{10} = \frac{1}{5}$.

Solutions to Selected Exercises

Chapter 10

Exercise Set 10.1

- **1.** If 0 represents ground level, then 1235 feet underground can be represented by -1235.
- **5.** 125 degrees above zero Fahrenheit can be represented by +125.
- **9.** A loss of \$1270 million can be represented by -1270 million.
- **13.** A decrease of 8 percent can be represented by -8.

- $-5 4 3 2 1 \ 0 \ 1 \ 2 \ 3 \ 4 \ 5$
- **21.** The graph of 4 is to the right of 0 on a number line so 4 is greater than 0, or 4 > 0.
- **25.** The graph of 0 is to the right of -3 on a number line, so 0 is greater than -3, or 0 > -3.
- **29.** The graph of $-1\frac{3}{4}$ is to the left of 0 on a number line, so

$$1\frac{3}{4}$$
 is less than 0, or $-1\frac{3}{4} < 0$.

33. The graph of
$$-2\frac{1}{2}$$
 is to the left of $-\frac{9}{10}$ on a number line,

so
$$-2\frac{1}{2}$$
 is less than $-\frac{9}{10}$, or $-2\frac{1}{2} < -\frac{9}{10}$.
37. $|-8| = 8$ since -8 is 8 units from 0.
41. $|-5| = 5$ since -5 is 5 units from 0.

- **45.** $\left| -\frac{1}{2} \right| = \frac{1}{2}$ since $-\frac{1}{2}$ is $\frac{1}{2}$ unit from 0.
- **49.** |7.6| = 7.6 since 7.6 is 7.6 units from 0.
- 53. The opposite of -4 is -(-4) or 4.

57. The opposite of
$$-\frac{9}{16}$$
 is $-\left(-\frac{9}{16}\right)$ or $\frac{9}{16}$.

61. The opposite of
$$\frac{1}{18}$$
 is $-\frac{1}{18}$.

65.
$$-|20| = -20$$

73.
$$-(-29) = 29$$

| 77. | Number | Absolute Value of
Number | Opposite of
Number |
|-----|--------|-----------------------------|-----------------------|
| | -8.4 | -8.4 = 8.4 | -(-8.4) = 8.4 |

- **81.** The tallest bar on the graph corresponds to Lake Superior, so Lake Superior has the highest elevation.
- **85.** The number on the graph closest to -200 °F is -186 °C, which corresponds to the element oxygen.

89. 15

$$\frac{+20}{35}$$
93. $2^2 = 2 \cdot 2 = 4$
 $-|3| = -3$
 $-(-5) = 5$
 $-|-8| = -8$
In order from least to greatest:
 $-|-8|, -|3|, 2^2, -(-5)$
97. $-(-2) = 2$
 $5^2 = 5 \cdot 5 = 25$
 $-10 = -10$
 $-|-9| = -9$
 $|-12| = 12$
In order from least to greatest:
 $-10, -|-9|, -(-2), |-12|, 5^2$

101.
$$-(-|-5|) = -(-5) = 5$$

- **105.** True; since every positive number is to the right of 0 on a number line and every negative number is to the left of 0, a positive number is always greater than a negative number.
- 109. answers may vary

Exercise Set 10.2

- Summerhays: 0 + 0 + 0 + (+1) + 0 + 0 + 0 + 0 + (-1) = 0After 9 holes, Day's score was 0 and Summerhays' score was 0
- **73.** The height of the bar for 2012 is marked as -39, so the net income for Amazon.com, Inc. in 2012 was -\$39,000,000.
- **77.** -10 + 12 = 2The temperature at 11 p.m. was 2°C.
- **81.** -55 + 8 = -47West Virginia's record low temperature is -47 °F.
- **85.** 44 0 = 44
- **89.** $\begin{array}{c} 1 & \cancel{9} & 10 \\ \cancel{2} & \cancel{9} & \cancel{9} \\ & 5 & 9 \\ \hline 1 & 4 & 1 \end{array}$
- 93. Since the signs are different, the absolute values should be subtracted, rather than added. 7 + (-10) = -3
- **97.** True; since two negative numbers have the same sign, the sum will have the common sign. That is, the sum will be negative.
- **101.** answers may vary

-1) = 0

A80

| S | 13. | 2 - |
|---------------------------------|-------------------|------------------------|
| is. | 17. | 3.6 |
| erc | 21. | $\frac{2}{5}$ |
| ш | 25 | ~ |
| σ | 29. | 2 - |
| te | 25.
29.
33. | 9 - |
| ns to Selected Exercises | 37. | $\frac{4}{7}$ |
| 0 | 41. | |
| itions t | 45. | -1 |
| Solu | 49. | 19 |
| | 53. | $-1 \\ -6$ |
| | 57. | Th
Re
wit
12: |
| | 61. | His -2 |
| | 65. | |
| | 05. | - 1 (1 |

Exercise Set 10.3 **1.** -5 - (-5) = -5 + 5 = 05. 3 - 8 = 3 + (-8) = -59. -5 - (-8) = -5 + 8 = 3-16 = 2 + (-16) = -1452 - (-0.4) = 3.62 + 0.4 = 4.02 $-\frac{7}{10} = \frac{2}{5} + \left(-\frac{7}{10}\right) = \frac{4}{10} + \left(-\frac{7}{10}\right) = -\frac{3}{10}$ 20 - 18 = -20 + (-18) = -38-(-11) = 2 + 11 = 13-20 = 9 + (-20) = -11 $+\left(-\frac{1}{7}\right)=\frac{3}{7}$ -5 - 7 = 12 + (-5) + (-7)= 7 + (-7)10 + (-5) - 12 = -10 + (-5) + (-12)= -15 + (-12)= -27-14 + (-6) + (-50) = 19 + (-14) + (-6) + (-50)= 5 + (-6) + (-50)= -1 + (-50)= -51e two months with the lowest temperatures are January, 10° F, and December, -6° F. 6 - (-10) = -6 + 10 = 4e difference is 4°F. present checks with negative numbers and deposits th positive numbers. 5 - 117 + 45 - 69 = 125 + (-117) + 45 + (-69)= 8 + 45 + (-69)= 53 + (-69)= -16s balance is -\$16. 282 - (-436) = -282 + 436 = 154e difference in elevations is 154 feet. 65. The elevation of Lake Superior is 600 feet. The elevation of Lake Eyre is -52 feet. 600 - (-52) = 600 + 52 = 652The difference in elevation is 652 feet. **69.** 867 - (-330) = 867 + 330 = 1197The difference in temperatures is 1197° Fahrenheit. **73.** $8 \cdot 0 = 0$ 77. 23 $\times 46$ 138 920 1058 **81.** 9 - (-7) = 9 + 7 = 16**85.** |-3| - |-7| = 3 - 7 = 3 + (-7) = -4**89.** |-15| - |-29| = 15 - 29 = 15 + (-29) = -1493. answers may vary **Exercise Set 10.4** 1. -2(-3) = 65. (2.6)(-1.2) = -3.12

9. $-\frac{3}{5}\left(-\frac{2}{7}\right) = \frac{6}{35}$ **13.** (-1)(-2)(-4) = 2(-4) = -8**17.** 10(-5)(-1)(-3) = -50(-1)(-3)= 50(-3)= -150**21.** $-5^2 = -(5 \cdot 5) = -25$ **25.** $-2^3 = -(2 \cdot 2 \cdot 2) = -8$ **29.** $\left(-\frac{5}{11}\right)^2 = \left(-\frac{5}{11}\right)\left(-\frac{5}{11}\right) = \frac{25}{121}$ **33.** $\frac{-30}{6} = -5$ because $-5 \cdot 6 = -30$ **37.** $\frac{0}{14} = 0$ because $0 \cdot 14 = 0$ **41.** $\frac{7.8}{0.2} = -26$ because $-26 \cdot -0.3 = 7.8$ **45.** $\frac{100}{-20} = -5$ because $-5 \cdot -20 = 100$ **49.** $\frac{-12}{-4} = 3$ because $3 \cdot -4 = -12$. **53.** $-\frac{8}{15} \div \frac{2}{3} = -\frac{8}{15} \cdot \frac{3}{2}$ $= -\frac{8\cdot 3}{15\cdot 2}$ $= -\frac{2 \cdot 4 \cdot 3}{3 \cdot 5 \cdot 2}$ **57.** $(-5)^3 = (-5)(-5)(-5) = 25(-5) = -125$ **61.** -1(2)(7)(-3.1) = -2(7)(-3.1)= -14(-3.1)= 434 $\mathbf{65.} \ \frac{4}{3} \div \left(-\frac{8}{9}\right) = \frac{4}{3} \cdot \left(-\frac{9}{8}\right)$ $=-\frac{4\cdot 9}{3\cdot 8}$ $=-\frac{4\cdot 3\cdot 3}{3\cdot 4\cdot 2}$ $= -\frac{3}{2}$ or $-1\frac{1}{2}$ 69. 42 $\times 6$ 252

$$-42(-6) = 252$$

73. Moving down 20 feet can be represented by -20. $5 \cdot (-20) = -100$ The diver reached a depth of 100 feet below the surface.

```
77. -3 \cdot 63 = -189
```

- The melting point of argon is -189 °C.
- **81. a.** 869 6533 = -5664The number of analog (non-digital) U.S. movie screens changed by -5664 screens from 2012 to 2016. b

a. 2012 to 2016 is 4 years
$$-5664$$

$$\frac{1}{4} = -1416$$

The average change was -1416 screens per year.

sum of numbers

93. -9 - 10 = -9 + (-10) = -19

- **97.** False; since the product of two numbers having the same sign is positive, the product of two negative numbers is always a positive number.
- **101.** The product of an odd number of negative numbers is negative, so the product of seven negative numbers is negative.
- **105.** The product of an odd number of negative numbers will be negative and the product of an even number of negative numbers will be positive. Also, |-2| = 2 < 5 = |-5| and -5 < -2. In order from least to greatest, the numbers are $(-5)^{17}$, $(-2)^{17}$, $(-2)^{12}$, $(-5)^{12}$.

Exercise Set 10.5

1.
$$-1(-2) + 1 = 2 + 1 = 3$$

5. $9 - 12 - 4 = -3 - 4 = -7$
9. $\frac{4}{9} \left(\frac{2}{10} - \frac{7}{10}\right) = \frac{4}{9} \left(-\frac{5}{10}\right)$
 $= -\frac{2}{9}$
13. $25 \div (-5) + \sqrt{81} = 25 \div (-5) + 9$
 $= -5 + 9$
 $= 4$
17. $\frac{24}{10 + (-4)} = \frac{24}{6} = 4$
21. $-19 - 12(3) = -19 - 36 = -55$
25. $[8 + (-4)]^2 = [4]^2 = 16$
29. $(3 - 12) \div 3 = (-9) \div 3 = -3$
33. $(5 - 9)^2 \div (4 - 2)^2 = (-4)^2 \div (2)^2$
 $= 16 \div 4$
 $= 4$
37. $(-12 - 20) \div 16 - 25 = (-32) \div 16 - 25$
 $= -27$
41. $(0.2 - 0.7)(0.6 - 1.9) = (-0.5)(-1.3)$
 $= 0.65$
45. $(-36 \div 6) - (4 \div 4) = (-6) - (1) = -7$
49. $(-5)^2 - 6^2 = 25 - 36 = -11$
53. $2(8 - 10)^2 - 5(1 - 6)^2 = 2(-2)^2 - 5(-5)^2$
 $= 2(4) - 5(25)$
 $= 8 - 125$
 $= -117$
57. $\frac{(-7)(-3) - 4(3)}{3[7 \div (3 - 10)]} = \frac{21 - 12}{3[7 \div (-7)]}$
 $= \frac{9}{-3}$
 $= -3$
61. $-3^2 + (-2)^3 - 4^2 = -9 + (-8) - 16$
 $= -17 - 16$
 $= -33$

65.
$$\frac{\sinh 01 \ \sinh 021}{number \ of \ numbers}$$

$$= \frac{-10 + 8 + (-4) + 2 + 7 + (-5) + (-12)}{7}$$

$$= \frac{-2 + (-4) + 2 + 7 + (-5) + (-12)}{7}$$

$$= \frac{-2 + (-4) + 2 + 7 + (-5) + (-12)}{7}$$

$$= \frac{-4 + 7 + (-5) + (-12)}{7}$$

$$= \frac{-4 + 7 + (-5) + (-12)}{7}$$

$$= \frac{-2 + (-12)}{7}$$

$$= \frac{-2 + (-12)}{7}$$

$$= \frac{-14}{7}$$

$$= -2$$
The average of the numbers is -2.
69.
$$\frac{\text{sum of temperatures}}{number \text{ of temperatures}}$$

$$= \frac{-11 + (-14) + (-16) + (-14)}{4}$$

$$= \frac{-25 + (-16) + (-14)}{4}$$

$$= \frac{-25 + (-16) + (-14)}{4}$$

$$= \frac{-55}{4}$$

$$= -13.75$$
The average temperature for December through March is -13.75°F
73. $45 \cdot 90 = 4050$
77. $P = 4 \cdot s = 4 \cdot 8 \text{ in.} = 32 \text{ in.}$
The perimeter is 32 inches.
81. $2 \cdot (7 - 5) \cdot 3 = 2 \cdot 2 \cdot 3 = 4 \cdot 3 = 12$
85. answers may vary

89. $(-12)^4 = (-12)(-12)(-12)(-12) = 20,736$

Chapter 10 Test

1.
$$\begin{array}{c} -6.5 \\ -7.6 \\ -7.6 \\ -7.6 \\ -5.4 \\ -7.6 \\ -5.4 \\ -7.6 \\ -5.4 \\ -7.6 \\ -5.4 \\ -7.6 \\ -5.4 \\ -7.6 \\ -5.4 \\ -7.6 \\ -5.4 \\ -7.6 \\ -5.4 \\ -7.6 \\$$

29. Checks and withdrawals are represented by negative numbers, while deposits are represented by positive numbers. 129 - 79 - 40 + 35 = 50 - 40 + 35 = 10 + 35= 45

His balance is \$45, which can be represented by the integer 45.

Solutions to Selected Exercises

Chapter 11

Exercise Set 11.1 1. 3 + 2z = 3 + 2(-3)= 3 + (-6)**Solutions to Selected Exercises** = -35. z - x + y = -3 - (-2) + 5= -3 + 2 + 5= -1 + 5= 4**9.** $8 - (5y - 7) = 8 - (5 \cdot 5 - 7)$ = 8 - (25 - 7)= 8 - 18= -10**13.** $\frac{6xy}{4} = \frac{6(-2)(5)}{4} = \frac{-12(5)}{4} = \frac{-60}{4} = -15$ **17.** $\frac{x+2y}{2z} = \frac{-2+2\cdot 5}{2(-3)} = \frac{-2+10}{-6}$ $=\frac{8}{-6}$ $= -\frac{4}{3}$ or $-1\frac{1}{3}$ **21.** $\frac{xz}{y} + \frac{3}{10} = \frac{-2(-3)}{5} + \frac{3}{10}$ $=\frac{6}{5}+\frac{3}{10}$ $=\frac{12}{10}+\frac{3}{10}$ $=\frac{15}{10}$ $=\frac{3}{2} \text{ or } 1\frac{1}{2}$ **25.** 3x + 5x = (3 + 5)x = 8x**29.** 4c + c - 7c = (4 + 1 - 7)c= (5 - 7)c= -2c**33.** 4a + 3a + 6a - 8 = (4 + 3 + 6)a - 8= (7 + 6)a - 8= 13a - 8**37.** 3x + 7 - x - 14 = 3x - x + 7 - 14= (3-1)x + (7-14)= 2x + (-7)= 2x - 7 **41.** $\frac{5}{6} - \frac{7}{12}x - \frac{1}{3} - \frac{3}{10}x = \frac{5}{6} - \frac{1}{3} - \frac{7}{12}x - \frac{3}{10}x$ $= \left(\frac{5}{6} - \frac{1}{3}\right) + \left(-\frac{7}{12} - \frac{3}{10}\right)x$ $=\left(\frac{5}{6}-\frac{2}{6}\right)+\left(-\frac{35}{60}-\frac{18}{60}\right)x$ $=\frac{3}{6}+\left(-\frac{53}{60}\right)x$ $=\frac{1}{2}-\frac{53}{60}x$ **45.** $6(5x) = (6 \cdot 5)x = 30x$ **49.** $-0.6(7a) = (-0.6 \cdot 7)a = -4.2a$ **53.** $2(y+2) = 2 \cdot y + 2 \cdot 2 = 2y + 4$ **57.** $-4(3x + 7) = -4 \cdot 3x + (-4) \cdot 7$ $= (-4 \cdot 3)x + (-28)$ = -12x - 28

61. $\frac{1}{2}(-8x-3) = \frac{1}{2}(-8x) - \frac{1}{2}(3)$ $=\left(\frac{1}{2}\cdot-8\right)x-\frac{3}{2}$ $= -4x - \frac{3}{2}$ **65.** $4(6n-5) + 3n = 4 \cdot 6n - 4 \cdot 5 + 3n$ = 24n - 20 + 3n= 24n + 3n - 20= (24 + 3)n - 20= 27n - 20**69.** -2(3x + 1) - 5(x - 2) $= -2 \cdot 3x + (-2) \cdot 1 - 5 \cdot x - (-5) \cdot 2$ $= (-2 \cdot 3)x + (-2) - 5x - (-10)$ = -6x - 2 - 5x + 10= (-6 - 5)x + (-2 + 10)= -11x + 8**73.** 2a + 2a + 6 + 5a + 6 + 2a= 2a + 2a + 5a + 2a + 6 + 6= (2+2+5+2)a+6+6= 11a + 12The perimeter is (11a + 12) feet. 77. Area = $(length) \cdot (width)$ $= (4y) \cdot (9)$ $= (4 \cdot 9)y$ = 36yThe area is 36y square inches. 81. Area = (length) \cdot (width) $= (3y + 1) \cdot (20)$ $= 3y \cdot 20 + 1 \cdot 20$ $= (3 \cdot 20)y + 20$ = 60y + 20The area is (60y + 20) square miles. **85.** Perimeter = $2 \cdot (\text{length}) + 2 \cdot (\text{width})$ $= 2 \cdot (18) + 2 \cdot (14)$ = 36 + 28= 64 The perimeter is 64 feet. **89.** I = PRT $= (3000) \cdot (0.06) \cdot (2)$ = 360The account will earn \$360 in interest. **93.** $F = \frac{9}{5}C + 32$ $=\frac{9}{5}(-5)+32$ = -9 + 32= 23The low temperature is 23°F. **97.** Let l = 7.6, w = 3, and h = 4x. $V = lwh = 7.6 \cdot 3 \cdot 4x = 91.2x.$ The volume is 91.2x cubic inches. **101.** -4 - (-12) = -4 + 12 = 8105. The given result is incorrect. $5(3x-2) = 5 \cdot 3x - 5 \cdot 2$ = 15x - 10109. The parentheses have been removed by the distributive property.

113. answers may vary

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117. Let d = 173. $A = 0.7854d^2$ $= 0.7854(173)^2$ $= 0.7854 \cdot 29,929$ $\approx 23,506.2$ The trunk area is approximately 23,506.2 square inches.

Exercise Set 11.2

1. x - 8 = 2 $10 - 8 \stackrel{?}{=} 2$ $2 \stackrel{?}{=} 2$ True Yes, 10 is a solution of the equation. 5. -9f = 64 - f $-9(-8) \stackrel{?}{=} 64 - (-8)$ $72 \stackrel{?}{=} 64 + 8$ $72 \stackrel{?}{=} 72$ True Yes, -8 is a solution of the equation. 9. a + 5 = 23a + 5 - 5 = 23 - 5a = 18Check: a + 5 = 23 $18 + 5 \stackrel{?}{=} 23$ $23 \stackrel{?}{=} 23$ True The solution of the equation is 18. **13.** 7 = y - 27 + 2 = y - 2 + 29 = yCheck: 7 = y - 2 $7 \stackrel{?}{=} 9 - 2$ $7 \stackrel{?}{=} 7$ True The solution of the equation is 9. $x + \frac{1}{2} = \frac{7}{2}$ 17. $x + \frac{1}{2} - \frac{1}{2} = \frac{7}{2} - \frac{1}{2}$ $x = \frac{6}{2}$ x = 3Check: $x + \frac{1}{2} =$ $3 + \frac{1}{2} \stackrel{?}{=}$ $\frac{7}{2}$ $\frac{6}{2} + \frac{1}{2} \stackrel{?}{=} \frac{7}{2}$ $\frac{7}{2} \stackrel{?}{=} \frac{7}{2}$ True The solution of the equation is 3. x - 3 = -1 + 421. x - 3 = 3x - 3 + 3 = 3 + 3x = 6Check: x - 3 = -1 + 4 $6 - 3 \stackrel{?}{=} -1 + 4$ $3 \stackrel{?}{=} 3$ True The solution of the equation is 6. 25. x - 0.6 = 4.7x - 0.6 + 0.6 = 4.7 + 0.6x = 5.3

Check: x - 0.6 = 4.7 $5.3 - 0.6 \stackrel{?}{=} 4.7$ 4.7 ² 4.7 True The solution of the equation is 5.3. 29. y + 2.3 = -9.2 - 8.6y + 2.3 = -17.8y + 2.3 - 2.3 = -17.8 - 2.3y = -20.1Check: y + 2.3 = -9.2 - 8.6 $-20.1 + 2.3 \stackrel{?}{=} -9.2 - 8.6$ $-17.8 \stackrel{?}{=} -17.8$ True The solution of the equation is -20.1. **33.** 5 + (-12) = 5x - 7 - 4x5 + (-12) = 5x - 4x - 7-7 = x - 7-7 + 7 = x - 7 + 70 = xCheck: 5 + (-12) = 5x - 7 - 4x $5 + (-12) \stackrel{?}{=} 5(0) - 7 - 4(0)$ $5 + (-12) \stackrel{?}{=} 0 - 7 - 0$ $-7 \stackrel{?}{=} -7$ True The solution of the equation is 0. 37. 2(5x - 3) = 11x $2 \cdot 5x - 2 \cdot 3 = 11x$ 10x - 6 = 11x10x - 10x - 6 = 11x - 10x-6 = x21y = 5(4y - 6)41. $21y = 5 \cdot 4y - 5 \cdot 6$ 21y = 20y - 3021y - 20y = 20y - 20y - 30y = -30**45.** $\frac{-7}{-7} = 1$ because $1 \cdot -7 = -7$. **49.** $-\frac{2}{3} \cdot -\frac{3}{2} = \frac{2 \cdot 3}{3 \cdot 2} = \frac{6}{6} = 1$ **53.** To solve $-\frac{1}{7} = -\frac{4}{5} + x$, $\frac{4}{5}$ should be added to both sides of the equation. x - 76,862 = 86,10257. x - 76,862 + 76,862 = 86,102 + 76,862x = 162,964**61.** Use I = R - E, where I = 556,000,000 and E = 18,130,000,000.I = R - E556,000,000 = R - 18,130,000,000556,000,000 + 18,130,000,000 = R - 18,130,000,000+ 18,130,000,00018,686,000,000 = RKohl's total revenues for the year were \$18,686,000,000. **Exercise Set 11.3** 1. 5x = 20 $\frac{5x}{5} = \frac{20}{5}$

x = 4

5. 0.4y = -12

 $\frac{0.4y}{0.4} = \frac{-12}{0.4}$

y = -30

Solutions to Selected Exercises

Solutions to Selected Exercises

| | 9. | $\frac{-0.3x = -15}{-0.3x} = \frac{-15}{-0.3}$ |
|---------------------|-----|---|
| EXercises | 13. | $x = 50$ $\frac{1}{6}y = -5$ $\frac{6}{1} \cdot \frac{1}{6}y = \frac{6}{1} \cdot -5$ |
| Ited | 17. | y = -30
$-\frac{2}{9}z = \frac{4}{27}$
$-\frac{9}{2} \cdot -\frac{2}{9}z = -\frac{9}{2} \cdot \frac{4}{27}$ |
| solutions to select | 21. | $z = -\frac{2}{3}$ $16 = 10t - 8t$ $16 = 2t$ $\frac{16}{2} = \frac{2t}{2}$ |
| 2010 | 25. | $8 = t 4 - 10 = -3z -6 = -3z \frac{-6}{-3} = \frac{-3z}{-3}$ |
| | 29. | 2 = z
0.4 = -8z
$\frac{0.4}{-8} = \frac{-8z}{-8}$
-0.05 = z |
| | 33. | $-\frac{3}{5}x = -\frac{6}{15}$ $-\frac{5}{3} \cdot -\frac{3}{5}x = -\frac{5}{3} \cdot -\frac{6}{15}$ |
| | 37. | $x = \frac{2}{3}$
5 - 5 = 2x + 7x
0 = 9x
$\frac{0}{9} = \frac{9x}{9}$ |
| | 41. | $0 = x -3x - 3x = 50 - 2 -6x = 48 \frac{-6x}{-6} = \frac{48}{-6}$ |
| | 45. | x = -8
$\frac{1}{4}x - \frac{5}{8}x = 20 - 47$
$\frac{2}{8}x - \frac{5}{8}x = -27$ |
| | | $-\frac{3}{8}x = -27$ $-\frac{8}{3} \cdot -\frac{3}{8}x = -\frac{8}{3} \cdot -27$ $x = 72$ |

49.
$$\frac{x}{-4} = 1 - (-6)$$
$$\frac{x}{-4} = 1 + 6$$
$$\frac{x}{-4} = 7$$
$$-4 \cdot \frac{x}{-4} = 7$$
$$-4 \cdot \frac{x}{-4} = -4 \cdot 7$$
$$x = -28$$
53.
$$\frac{x - 3}{-3} = \frac{5 - 3}{-3} = \frac{2}{2} = 1$$
57. The longest bar corresponds to 2015, so the number of acres burned by wildfires was greatest in 2015.
61. Addition should be used to solve the equation 12 = x - 5. Specifically, 5 should be added to both sides of the equation.
65. answers may vary
69. Use $d = r \cdot t$, where $d = 294$ and $t = 5$.
 $\frac{d = r \cdot t}{294} = 5 \cdot r$
 $\frac{294}{5} = \frac{5r}{5}$
 $\frac{294}{5} = r$
The driver should trip at $\frac{294}{5} = 58.8$ miles per hour to make the trip in 5 hours.
73. $\frac{y}{72} = -86 - (-1029)$
$$\frac{y}{72} = -86 + 1029$$
$$\frac{y}{72} = 943$$

 $72 \cdot \frac{y}{72} = 72 \cdot 943$
$$y = 67,896$$

Exercise Set 11.4
1. $2x - 6 = 0$
 $2x - 6 + 6 = 0 + 6$
 $2x = 6$
 $\frac{2x}{2} = \frac{6}{2}$
 $x = 3$
5. $6 - n = 10$
 $6 - 6 - n = 10 - 6$
 $-n = 4$
 $-\frac{n}{-1} = \frac{4}{-1}$
 $n = -4$
9. $1.7 = 2y + 9.5$
 $1.7 - 9.5 = 2y + 9.5 - 9.5$
 $-7.8 = 2y$
 $-7.8 = \frac{2y}{2}$
 $-3.9 = y$
13. $3x - 7 = 4x + 5$
 $3x - 7 - 5 = 4x + 5 - 5$
 $3x - 7 - 5 = 4x + 5 - 5$
 $3x - 7 - 5 = 4x - 3x$
 $-12 = 4x$

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17. 9 - 3x = 14 + 2x9 - 14 - 3x = 14 - 14 + 2x-5 - 3x = 2x-5 - 3x + 3x = 2x + 3x-5 = 5x $\frac{-5}{5} = \frac{5x}{5}$ -1 = x**21.** x + 20 + 2x = -10 - 2x - 15x + 2x + 20 = -10 - 15 - 2x3x + 20 = -25 - 2x3x + 2x + 20 = -25 - 2x + 2x5x + 20 = -255x + 20 - 20 = -25 - 205x = -45 $\frac{5x}{5} = \frac{-45}{5}$ x = -9**25.** -2(y+4) = 2-2y - 8 = 2-2y - 8 + 8 = 2 + 8-2y = 10 $\frac{-2y}{-2} = \frac{10}{-2}$ y = -5**29.** 35 - 17 = 3(x - 2)18 = 3x - 618 + 6 = 3x - 6 + 624 = 3x $\frac{24}{3x} = \frac{3x}{3x}$ 3 3 8 = x33. 2t - 1 = 3(t + 7)2t - 1 = 3t + 212t - 1 - 21 = 3t + 21 - 212t - 22 = 3t2t - 2t - 22 = 3t - 2t-22 = t**37.** -4x = 44 $\frac{-4x}{-4} = \frac{44}{-4}$ x = -118 - b = 1341. 8 - 8 - b = 13 - 8-b = 5 $\frac{-b}{-1} = \frac{5}{-1}$ b = -52x - 1 = -745. 2x - 1 + 1 = -7 + 12x = -6 $\frac{2x}{2} = \frac{-6}{2}$ x = -39a + 29 = -749. 9a + 29 - 29 = -7 - 299a = -36 $\frac{9a}{9} = \frac{-36}{9}$ a = -4

53.
$$11(x-2) = 22$$
$$11x - 22 = 22$$
$$11x - 22 + 22 = 22 + 22$$
$$11x = 44$$
$$\frac{11x}{11} = \frac{44}{11}$$
$$x = 4$$

57.
$$3(x-5) = -7 - 11$$
$$3x - 15 = -18$$
$$3x - 15 + 15 = -18 + 15$$
$$3x = -3$$
$$\frac{3x}{3} = \frac{-3}{3}$$
$$\frac{3x}{3} = \frac{-3}{3}$$
$$\frac{3x}{3} = \frac{-3}{3}$$
$$\frac{3x}{3} = \frac{2x}{3}$$
$$\frac{14x + 3 = 2x + 11}{4x + 3 - 3 = 2x + 11 - 3}$$
$$4x = 2x + 8$$
$$4x - 2x = 2x - 2x + 8$$
$$2x = 8$$
$$\frac{2x}{2} = \frac{8}{2}$$
$$x = 4$$

65.
$$\frac{3}{8}x + 14 = \frac{5}{8}x - 2$$
$$\frac{3}{8}x + 14 = \frac{5}{8}x - 2$$
$$\frac{3}{8}x + 14 = \frac{5}{8}x - 2 + 2$$
$$\frac{3}{8}x + 16 = \frac{5}{8}x$$
$$\frac{3}{8}x - \frac{3}{8}x + 16 = \frac{5}{8}x - 2 + 2$$
$$\frac{3}{8}x + 16 = \frac{5}{8}x - 2 + 2$$
$$\frac{3}{8}x + 16 = \frac{5}{8}x - 2 + 2$$
$$\frac{3}{8}x + 16 = \frac{5}{8}x - 2 + 2$$
$$\frac{3}{8}x + 16 = \frac{5}{8}x - 2 + 2$$
$$\frac{3}{8}x + 16 = \frac{5}{8}x - 2 + 2$$
$$\frac{3}{8}x + 16 = \frac{5}{8}x - \frac{3}{8}x$$
$$16 = \frac{1}{4}x$$
$$4 \cdot 16 = 4 \cdot \frac{1}{4}x$$
$$4 \cdot 16 = 4 \cdot \frac{1}{4}x$$
$$64 = x$$
$$69. \qquad \frac{5}{8}a = \frac{1}{8}a - \frac{1}{8}a + \frac{3}{4}$$
$$\frac{4}{8}a = \frac{3}{4}$$
$$\frac{1}{2}a = \frac{3}{4}$$
$$2 \cdot \frac{1}{2}a = 2 \cdot \frac{3}{4}$$
$$a = \frac{3}{2}$$
$$73. 3 + 2(2n - 5) = 1$$
$$3 + 4n - 10 = 1$$
$$4n - 7 = 1$$
$$4n - 7 = 1$$
$$4n - 7 = 1$$
$$4n = 8$$
$$\frac{4n}{4} = \frac{8}{4}$$
$$n = 2$$

77. $-20 - (-50) = \frac{x}{0}$ $-20 + 50 = \frac{x}{9}$ $30 = \frac{x}{9}$ $9 \cdot 30 = 9 \cdot \frac{x}{0}$ 270 = x**81.** 3(5c - 1) - 2 = 13c + 315c - 3 - 2 = 13c + 315c - 5 = 13c + 315c - 5 + 5 = 13c + 3 + 515c = 13c + 815c - 13c = 13c - 13c + 82c = 8 $\frac{2c}{2c} = \frac{8}{2}$ 2 2 c = 485. "The sum of -42 and 16 is -26" translates to -42 + 16 = -26.**89.** "Three times the difference of -14 and 2 amounts to -48" translates to 3(-14 - 2) = -48. 93. From the label of the 2014 bar, 126 million or 126,000,000 returns were filed electronically in 2014. 97. The first step in solving 2x - 5 = -7 is to add 5 to both sides, which is choice **b**. 101. The error is in the second line. 2(3x-5) = 5x - 76x - 10 = 5x - 76x - 10 + 10 = 5x - 7 + 106x = 5x + 36x - 5x = 5x + 3 - 5xx = 3 $2^{3}(x+4) = 3^{2}(x+4)$ 105. 8(x + 4) = 9(x + 4)8x + 32 = 9x + 368x + 32 - 36 = 9x + 36 - 368x - 4 = 9x8x - 4 - 8x = 9x - 8x-4 = x**109.** Use $C = \frac{5}{9} (F - 32)$ with C = 50.7. $C = \frac{5}{9} \left(F - 32 \right)$ $50.7 = \frac{5}{9}(F - 32)$ $\frac{9}{5}(50.7) = \frac{9}{5} \cdot \frac{5}{9}(F - 32)$ 91.26 = F - 3291.26 + 32 = F - 32 + 32123.26 = FThe temperature was 123.26°F. Exercise Set 11.5 **1.** "The sum of a number and five" is x + 5. 5. "Twenty decreased by a number" is 20 - x. 9. "A number divided by 2" is $\frac{x}{2}$. **13.** "A number added to -5 is -7" is -5 + x = -7.

- **17.** "A number subtracted from -20 amounts to 104" is -20 x = 104.
- **21.** "A number subtracted from 11" is 11 x.

- **25.** "Fifty decreased by eight times a number" is 50 8x.
- **29.** "Three times a number, added to 9, is 33" is 9 + 3x = 33.
 - 9 + 3x = 33 9 + 3x - 9 = 33 - 9 3x = 24 $\frac{3x}{3} = \frac{24}{3}$ x = 8The number is 8. "The difference of a
- **33.** "The difference of a number and 3 is equal to the quotient 10^{10}

of 10 and 5" is
$$x - 3 = \frac{10}{5}$$

 $x - 3 = \frac{10}{5}$
 $x - 3 = 2$
 $x - 3 + 3 = 2 + 3$
 $x = 5$

- The number is 5.
- **37.** "40 subtracted from five times a number is 8 more than the number" is 5x 40 = x + 8.
 - 5x 40 = x + 8 5x - 40 + 40 = x + 8 + 40 5x = x + 48 5x - x = x - x + 48 4x = 48 $\frac{4x}{4} = \frac{48}{4}$ x = 12
 - The number is 12.
- **41.** "The product of 4 and a number is the same as 30 less twice that same number" is 4x = 30 2x.
 - 4x = 30 2x
 - 4x + 2x = 30 2x + 2x
 - 6x = 30

$$\frac{6x}{6} = \frac{30}{6}$$

- 6 6
- x = 5The number is 5.
- **45.** Let *x* be the fastest speed for the pheasant. Since the top speed of the falcon is five times the top speed of the pheasant, the top speed of the falcon is 5x. Since the total of the speeds is 222 miles per hour, the sum of *x* and 5x is 222.
 - $\begin{array}{r} x + 5x = 222\\ 6x = 222 \end{array}$
 - $\frac{6x}{222}$
 - $\overline{\begin{array}{c} 6 \end{array}} = \overline{\begin{array}{c} 6 \end{array}}$ x = 37

The top speed of the pheasant is 37 miles per hour and the top speed of the falcon is $5 \cdot 37 = 185$ miles per hour.

49. Let x be the cost of *Kinect Adventures*. Since the cost of *Grand Theft Auto V* is \$24 more than the cost of *Kinect Adventures*, the cost of *Grand Theft Auto V* is x + 24. Since the total cost is \$36, the sum of x and x + 24 is 36.

24

- x + x + 24 = 36
- 2x + 24 = 362x + 24 24 = 36

$$2 + 24 - 24 - 30 - 24$$

$$2x = 12$$

 $2x = 12$

$$\frac{2\pi}{2} = \frac{11}{2}$$

$$x = 6$$

The cost of *Kinect Adventures* is \$6 and the cost of *Grand Theft Auto V* is \$6 + \$24 = \$30.

Solutions to Selected Exercises

53. Let *x* be the capacity of Beaver Stadium. Since the capacity of Michigan Stadium is 3329 more than the capacity of Beaver Stadium, the capacity of Michigan Stadium is x + 3329. Since the total capacity of the two stadiums is 216,473, the sum of *x* and x + 3329 is 216,473.

$$x + x + 3329 = 216,473$$

$$2x + 3329 = 216,473$$

$$2x + 3329 - 3329 = 216,473 - 3329$$

$$2x = 213,144$$

$$\frac{2x}{2} = \frac{213,144}{2}$$

$$x = 106,572$$

The capacity of Beaver Stadium is 106,572 and the capacity of Michigan Stadium is 106,572 + 3329 = 109,901.

57. Let x be the number of points scored by the Gonzaga Bulldogs. Since the North Carolina Tar Heels scored 6 points more than the Gonzaga Bulldogs, the North Carolina Tar Heels scored x + 6 points. Since the total number of points scored by the two teams was 136 points, the sum of x and x + 6 is 136.

$$x + x + 6 = 136$$

$$2x + 6 = 136$$

$$2x + 6 - 6 = 136 - 6$$

$$2x = 130$$

$$\frac{2x}{2} = \frac{130}{2}$$

$$x = 65$$

$$x + 6 = 65 + 6 = 71$$

The 2017 Champion North Carolina Tar Heels scored 71 points.

61. Let x be the number of Super Bowl wins by the Pittsburgh Steelers. Since the Miami Dolphins have 4 fewer Super Bowl wins than the Pittsburgh Steelers, the Miami Dolphins have x - 4 Super Bowl wins. Since the total number of Super Bowl wins for the two teams is 8, the sum of x and x - 4 is 8.

$$x + x - 4 = 8$$

$$2x - 4 = 8$$

$$2x - 4 + 4 = 8 + 4$$

$$2x = 12$$

$$\frac{2x}{2} = \frac{12}{2}$$

$$x = 6$$

The Pittsburgh Steelers have 6 Super Bowl wins and the Miami Dolphins have 6 - 4 = 2 Super Bowl wins.

65. Let *x* be the number of Internet users, in millions, in Europe. Since Asia had 1250 million more Internet users than Europe, the number of Internet users in Asia is x + 1250. Since the total number of Internet users for both continents was 2550 million, the sum of *x* and x + 1250 is 2550.

$$x + x + 1250 = 2550$$

$$2x + 1250 = 2550$$

$$2x + 1250 - 1250 = 2550 - 1250$$

$$2x = 1300$$

$$\frac{2x}{2} = \frac{1300}{2}$$

$$x = 650$$

Europe had 650 million Internet users and Asia had

650 million + 1250 million = 1900 million Internet users.

73. yes; answers may vary

77. Use
$$P = C + M$$
, where $P = 999$ and $M = 450$.
 $P = C + M$
 $999 = C + 450$
 $999 - 450 = C + 450 - 450$
 $549 = C$
The wholesale cost is \$549.

Chapter 11 Test

1.
$$\frac{3x-5}{2y} = \frac{3 \cdot 7 - 5}{2(-8)}$$

$$= \frac{21-5}{-16}$$

$$= \frac{16}{-16}$$

$$= -1$$

5. Area = length · width
 $A = 4 \cdot (3x - 1)$

$$= 4 \cdot 3x - 4 \cdot 1$$

$$= 12x - 4$$

The area is $(12x - 4)$ square meters.
9. $-\frac{5}{8}x = -25$
 $-\frac{8}{5} \cdot -\frac{5}{8}x = -\frac{8}{5} \cdot -25$
 $x = 40$
13. $-4x + 7 = 15$
 $-4x + 7 - 7 = 15 - 7$
 $-4x = 8$
 $\frac{-4x}{-4} = \frac{8}{-4}$
 $x = -2$
17. $10y - 1 = 7y + 21$
 $10y - 1 + 1 = 7y + 21 + 1$
 $10y - 7y = 7y - 7y + 22$
 $10y - 7y = 7y - 7y + 22$
 $3y = 22$
 $\frac{3y}{3} = \frac{22}{3}$
 $y = \frac{22}{3}$
21. Use $A = \frac{1}{2}bh$, where $b = 5$ and $h = 12$.
 $A = \frac{1}{2}bh = \frac{1}{2} \cdot 5 \cdot 12 = 30$
The area is 30 square feet.

25. Let x be the number of women runners entered. Then the number of men runners entered is x + 112, and the sum of these two quantities is 600.

$$x + x + 112 = 600$$

$$2x + 112 = 600$$

$$2x + 112 - 112 = 600 - 112$$

$$2x = 488$$

$$\frac{2x}{2} = \frac{488}{2}$$

$$x = 244$$

There were 244 women runners entered.

Appendices

| ercises | 5 |
|---------|---|
| ted Ex | 9 |
| Select | 1 |
| ons to | 1 |
| Soluti | A |

| | e Hundred Addition Facts | | | |
|--|--|---|--|--|
| 1. 1 | 21. 6 | 41. 2 | 61. 6 | 81. 2 |
| +4 | +4 | +4 | +7 | +8 |
| 5 | 10 | 6 | 13 | 10 |
| 5. 3 | 25. 9 | 45. 3 | 65. 0 | 85. 5 |
| +9 | +8 | +6 | +7 | $\frac{+0}{5}$ |
| 12 | 17 | 9 | 7 | |
| 9. 9 | 29. 7 | 49. 2 | 69. 4 | 89. 9 |
| +5 | ± 5 | $\frac{+5}{7}$ | $\frac{\pm 1}{5}$ | ± 2 |
| 14 | 12 | | | 11 |
| 13. 5 | 33. 4 | 53. 8 | 73. 7 | 93. 2 |
| ± 5 | $\frac{+3}{7}$ | +3 | +9 | +7 |
| 10 | | 11 | 16 | 9 |
| 17. 2 | 37. 7 | 57. 0 | 77. 1 | 97. 6 |
| $\frac{+9}{-1}$ | $\frac{\pm 1}{2}$ | $\frac{+5}{5}$ | $\frac{+0}{1}$ | $\frac{+8}{1}$ |
| 11 | 8 | 5 | 1 | 14 |
| A.2: One | e Hundred Multiplication F | acts | | |
| 1. 1 | 21. 5 | 41. 8 | 61. 9 | 81. 1 |
| $\underline{\times 1}$ | $\times 8$ | $\underline{\times 6}$ | $\underline{\times 2}$ | $\times 5$ |
| 1 | 40 | 48 | 18 | 5 |
| 5. 8 | 25. 9 | 45. 9 | 65. 6 | 85. 3 |
| $\underline{\times 4}$ | $\underline{\times 6}$ | $\underline{\times 0}$ | $\underline{\times 6}$ | $\times 7$ |
| 32 | 54 | 0 | 36 | 21 |
| 9. 2 | 29. 6 | 49. 3 | 69. 7 | 89. 8 |
| | | | | $^{\vee 2}$ |
| $\underline{\times 2}$ | $\underline{\times 9}$ | $\times 5$ | $\times 5$ | <u>~2</u> |
| $\frac{\times 2}{4}$ | $\frac{\times 9}{54}$ | 15 | $\frac{\times 5}{35}$ | $\frac{\times 2}{16}$ |
| $\frac{\times 2}{4}$ 13. 3 | 33. 4 | | 73. 8 | 93. 4 |
| $\frac{\times 2}{4}$ 13. 3
$\times 2$ | 33. 4 × 9 | 53. 1×0 | 73. 8 × 5 | 93. 4 <u>×1</u> |
| $ \frac{\times 2}{4} $ 13. 3 $ \frac{\times 2}{6} $ | $33. 4 \\ \frac{\times 9}{36}$ | $ \begin{array}{r} \overline{15} \\ \overline{53.} 1 \\ \underline{\times 0} \\ \overline{0} \end{array} $ | 73. $8 \\ \frac{\times 5}{40}$ | 93. 4
×1
4 |
| $ \frac{\times 2}{4} $ 13. 3 $ \frac{\times 2}{6} $ 17. 4 | 33. 4
$\times 9$
36
37. 9 | 53. 1
$\times 0$
57. 0 | 73. 8
$\frac{\times 5}{40}$
77. 9 | 93. 4
×1
4
97. 3 |
| $\frac{\times 2}{4}$ 13. 3
$\frac{\times 2}{6}$ 17. 4
$\frac{\times 6}{5}$ | 33. $4 \\ \frac{\times 9}{36} \\ 37. 9 \\ \times 4$ | 53. 1
$\times 0$
57. 0
$\times 6$ | 73. 8
$\times 5$
40
77. 9
$\times 1$ | 93. 4
$\times \frac{1}{4}$
97. 3
$\times \frac{6}{3}$ |
| $ \frac{\times 2}{4} $ 13. 3 $ \frac{\times 2}{6} $ 17. 4 | 33. 4
$\times 9$
36
37. 9 | 53. 1
$\times 0$
57. 0 | 73. 8
$\frac{\times 5}{40}$
77. 9 | 93. 4
×1
4
97. 3 |

Exercise Set B

1. a. $\frac{\$16}{1 \text{ hr}} \cdot \frac{40 \text{ hr}}{1} = \frac{\$16 \cdot 40}{1 \cdot 1} = \640 Before deductions, your earnings for 40 hours are \$640. **b.** $\frac{\$240}{1} \cdot \frac{1}{\$16} = \frac{240 \cdot 1}{1 \cdot 16} = 15$ hr It takes you 15 hours to earn \$240 before deductions. $\frac{1 \text{ bed}}{155 \text{ people}} \cdot \frac{31,000 \text{ people}}{1} = \frac{1 \text{ bed} \cdot 31,000}{155 \cdot 1}$ 5. a. = 200 beds There would be 200 hospital beds in the city. $\frac{155 \text{ people}}{1 \text{ bed}} \cdot \frac{73 \text{ beds}}{1} = \frac{155 \text{ people} \cdot 73}{1 \cdot 1}$ b. = 11,315 people The population is about 11,315 people. \$0.75 . 26 components . 33 hr 9. $\frac{1}{1 \text{ component}}$ 1 hr 1 $=\frac{\$0.75\cdot26\cdot33}{1\cdot1\cdot1}$ = \$643.50 Her pay before deductions was \$643.50.

13. a.
$$\frac{16 \text{ tortillas}}{1 \text{ min}} \cdot \frac{60 \text{ min}}{1 \text{ hr}} \cdot \frac{7.5 \text{ hr}}{1}$$

 $= \frac{16 \text{ tortillas} \cdot 60 \cdot 7.5}{1 \cdot 1 \cdot 1}$
 $= 7200 \text{ tortillas}$
The machine could make 7200 tortillas in 75 hours.
b. $\frac{200 \text{ tortillas}}{1} \cdot \frac{1 \text{ min}}{16 \text{ tortillas}} = \frac{200 \cdot 1 \text{ min}}{1 \cdot 16}$
 $= 12\frac{1}{2} \text{ min or } 12.5 \text{ min}$
It takes the machine 12.5 minutes to make 200 tortillas.
17. a. $\frac{45 \text{ miles}}{1 \text{ hr}} \cdot \frac{\frac{1}{4} \text{ hr}}{1} = \frac{45 \text{ miles} \cdot \frac{1}{4}}{1 \cdot 1} = 11\frac{1}{4} \text{ miles}$
The cheetah has traveled $11\frac{1}{4}$ miles in $\frac{1}{4}$ hour.
b. $\frac{5 \text{ miles}}{1} \cdot \frac{1 \text{ hr}}{45 \text{ miles}} = \frac{5 \cdot 1 \text{ hr}}{1 \cdot 45} = \frac{1}{9} \text{ hr}$
 $\frac{\frac{1}{9} \text{ hr}}{1} \cdot \frac{60 \text{ min}}{1 \text{ hr}} = \frac{\frac{1}{9} \cdot 60 \text{ min}}{1 \cdot 1} = \frac{60}{9} \text{ min} = 6\frac{2}{3} \text{ min}$

It takes the cheetah $\frac{1}{9}$ hour or $6\frac{2}{3}$ minutes to travel 5 miles.

Practice Final Exam

1.
$$600$$

 $-\frac{487}{113}$
5. $\frac{64 \div 8 \cdot 2}{(\sqrt{9} - \sqrt{4})^2 + 1} = \frac{8 \cdot 2}{(3 - 2)^2 + 1} = \frac{16}{1^2 + 1}$
 $= \frac{16}{1 + 1}$
 $= \frac{16}{2}$
9. $3\frac{1}{3} \cdot 6\frac{3}{4} = \frac{10}{3} \cdot \frac{27}{4} = \frac{10 \cdot 27}{3 \cdot 4} = \frac{2 \cdot 5 \cdot 3 \cdot 9}{3 \cdot 2 \cdot 2}$
 $= \frac{5 \cdot 9}{2}$
 $= \frac{45}{2}$
 $= 22\frac{1}{2}$

13. To round 34.8923 to the nearest tenth, observe that the digit in the hundredths place is 9. Since the digit is at least 5, we add 1 to the digit in the tenths place and drop all digits to the right of the tenths place. The number 34.8923 rounded to the nearest tenth is 34.9.

17.
$$\frac{3}{8} = \frac{3}{8} (100\%) = \frac{300}{8}\% = 37.5\%$$

 $\frac{37.5}{8)\overline{300.0}}$
 $\frac{-24}{60}$
 $\frac{-56}{40}$
 $\frac{-40}{0}$

21. The rate of 9 inches in 30 days is $\frac{9 \text{ inches}}{30 \text{ days}} = \frac{3 \text{ inches}}{10 \text{ days}}$.

- 20.0 **25.** <u>-</u> 8.6
- 11.4

29. 0.6% of what number is 7.5?

Method 1: $0.6\% \cdot n = 7.5$ $0.006 \cdot n = 7.5$ $n = \frac{7.5}{0.006}$ n = 12500.6% of 1250 is 7.5.

Method 2:

$$\frac{7.5}{b} = \frac{0.6}{100}$$
7.5 \cdot 100 = 0.6 \cdot b
750 = 0.6 \cdot b
 $\frac{750}{0.6} = b$
1250 = b
0.6% of 1250 is 7.5.
33. 2.4 kg = $\frac{2.4 \text{ kg}}{1000 \text{ g}} \cdot \frac{1000 \text{ g}}{1000 \text{ g}} = 2400 \text{ g}$

37. $\angle x$ and the angle marked 62° are supplementary, so $m \angle x = 180^\circ - 62^\circ = 118^\circ$.

 $\angle y$ and the angle marked 62° are vertical angles, so $m \angle y = 62^\circ$.

 $\angle x$ and $\angle z$ are vertical angles, so $m \angle z = m \angle x = 118^{\circ}$.

41. 5 of the students are 5'0'' - 5'3'' and 6 of the students are 5'3'' - 5'7'', so 5 + 6 = 11 of the students are 5'7'' or shorter.

$$45. \left(\frac{5}{9} - \frac{7}{9}\right)^2 + \left(-\frac{2}{9}\right) = \left(\frac{5-7}{9}\right)^2 + \left(-\frac{2}{9}\right)$$
$$= \left(-\frac{2}{9}\right)^2 + \left(-\frac{2}{9}\right)$$
$$= \left(-\frac{2}{9}\right) \cdot \left(-\frac{2}{9}\right) + \left(-\frac{2}{9}\right)$$
$$= \frac{4}{81} + \left(-\frac{2}{9}, \frac{9}{9}\right)$$
$$= \frac{4}{81} + \left(-\frac{18}{81}\right)$$
$$= \frac{4-18}{81}$$
$$= -\frac{14}{81}$$
$$49. 5x + 12 - 4x - 14 = 22$$
$$5x - 4x + 12 - 14 = 22$$
$$x - 2 = 22$$
$$x - 2 + 2 = 22 + 2$$
$$x - 2 + 2 = 24$$

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