a separate section will focus on the issues of specific importance to halogen lamps.

The first commercially successful electric incandescent lamp, made by Thomas Edison in 1879, generated light by passing an electric current through a thin strand of carbon. The initial carbon filament lamp marketed by Edison operated at around 110 V, consumed about 80 W, lasted about 600 h, and provided light at an efficiency approximately 11 times below that for lamps of similar wattage and life today. Lamp efficiencies are referred to as efficacy, and the units (discussed later in more detail) are given in lumens per watt of input power, where the lumen is a measure of the visible light output. To improve on efficacy and life, a higher melting point material capable of being formed easily into a compact filament had to be found.

In 1908, William Coolidge working at the GE Research Laboratory developed the method for converting tungsten, a brittle metal with a melting point of 3650 K, into a ductile material capable of being formed into a practical filament for a lamp. By 1911, the first lamps made with ductile tungsten filaments were introduced into the market, and today tungsten is used almost exclusively as the material of choice for commercial use. The next major advancement was made in 1913. It actually paved the way for the eventual development of the halogen lamp in the late 1950s. This was the discovery by Irving Langmuir (also at the GE labs) that the addition of a nonreactive gas such as nitrogen or argon can retard tungsten evaporation, thus extending life and enabling higher temperature operation. At the same time, coiling the tungsten filament would result in reducing the power that went to heat the gas as well as enabling the easy fit of a long thin wire filament into a small bulb envelope. The net result was a lamp with extended life and/or higher efficacy (i.e., more light per input power). Figure 1 shows the historical trend toward increased efficacy for filament lamps expending 60 W at 120 V with a life of 1000 h (one of the most common lamp types of the A-line series). As we will see, each new development (use of tungsten, gas, and the related requirement for coiling) which enabled higher temperature operation and resulted in higher luminous efficacy, needed to be accomplished without sacrificing the life of the filament as a result of market considerations. For further discussion on the history of the incandescent lamp including the development of ductile tungsten,

as the Edison base. In the industry, these are also called A- Mathematically, the radiant emission properties of incanline in North America, or the older term GLS, for General descent solid materials can be quite well represented by ideal-Lamp Service. This paper discusses the science and general izing the material as a blackbody, where deviations from the design considerations of incandescent and halogen lamp ideal are dealt with by employing the concept of emissivity. A types. Even though the bulk of the discussion is valid for both, *blackbody* is defined as an ideal body blackbody is defined as an ideal body of uniform temperature

FILAMENT LAMPS see Refs. 1–4.

Electric filament lamps are light sources containing a solid **SCIENCE OF INCANDESCENCE** body that is brought to a high enough temperature that some fraction (typically \sim 10%) of the emitted radiation is in the **Blackbody Characteristics** visible portion of the spectrum. The emitting body is generally in the form of a coil or coiled-coil and is referred to as a fila- When radiation encounters an object three things can occur. ment. Light sources incorporating such filaments are often re- The radiation can be transmitted through the body, be referred to as incandescent lamps, although halogen lamps em- flected from the body, or be absorbed by the body. A material ploy the same type of filaments. Many different designs of that perfectly transmits all radiation impinging on it is called incandescent lamps exist in the market today, each satisfying *colorless,* that which reflects all radiation is called *white,* and a particular market niche. Wattages range from 1 to several that which absorbs all radiation is called *black.* No physical thousand, though the most common are the 60 W, 75 W, and materials are perfect representatives, but air is nearly color-100 W lamps with the screw base, which is often referred to less, chalk is nearly white, and carbon black is nearly black.

Figure 1. Historical efficacy of incandescent lamps.

that perfectly absorbs all radiation incident upon it. By Kirch- visible range. As will shortly be shown mathematically, the impinging radiation. Thus, since a blackbody absorbs per- blackbody radiator. fectly it also, for equal areas, radiates more total power and Integrating Eq. (1) over all wavelengths, we find that the operating at the same temperature. The unique feature of the power of the temperature (Stefan–Boltzmann Law): blackbody is that its radiation characteristics may be specified solely by the absolute temperature.

Radiative Emission where

Max Planck, in about 1900, derived an equation for the spectral distribution of radiation from a blackbody, by using the second law of thermodynamics and assuming that the energy
levels available for the radiation are quantized. This equation
fit the known spectral measurements extremely well and was
a great improvement over earlier theoret per unit wavelength), is

$$
M_{\mathrm{e},\lambda}(T) = \frac{c_1}{\lambda^5 (\exp[c_2/\lambda T]-1)} \mathrm{W}\cdot\mathrm{m}^{-3} \tag{1}
$$

where the latest values for the constants are

$$
c_1 = 2\pi h c^2 = 3.7415 \times 10^{-16} \,\text{W} \cdot \text{m}^2 \tag{2a}
$$

$$
c_2 = hc/k = 1.4388 \times 10^{-2} \,\text{m-K} = 14,388 \,\mu\text{m} \cdot \text{K} \qquad (2b)
$$

In these expressions, *h* is Planck's constant (6.6256 \times 10⁻³⁴ $\rm J\cdot s$), k is Boltzmann's constant (1.38 \times 10^{-23} $\rm J\cdot K^{-1}$), and c is the speed of light $(3.0 \times 10^8 \text{ m} \cdot \text{s}^{-1})$. Figure 2 shows the spectral emittance distribution for temperatures between 2000 K perature range encloses all known tungsten-based incandescent lamps. It is clear from Fig. 2 that higher temperatures **Figure 2.** Spectral radiant emittance of a blackbody with temperawould be desirable to put more of the emitted power in the ture as a parameter.

hoff's Law, the temperature radiation of a body is at any tem- fraction of radiated power in the middle of the visible region perature and any frequency the same percentage of blackbody reaches a maximum at around 6500 K. This, of course, is radiation as the absorbed radiation of the body is of the total about the temperature of the sun, which is also nearly a

more power at any given wavelength than any other source total emittance of a blackbody is proportional to the fourth

$$
M_e^b = \sigma T^4 W \cdot m^{-2}
$$
 (3)

$$
\sigma = 2\pi^5 k^4/(15 h^3 c^2) = 5.6697 \times 10^{-8}\,\text{W}\cdot\text{m}^{-2}\cdot\text{K}^{-4}
$$

angle) is equal to the emittance divided by π , or

$$
L_{\rm e}^{\rm b} = M_{\rm e}^{\rm b}/\pi\tag{4}
$$

$$
\lambda_{\rm m} = 2897.8/T \,\mu\text{m} \tag{5}
$$

to be the real surface to that of a blackbody. In other words,

$$
M_{e}(\lambda_{m}) = 1.2867 \times 10^{-5} T^{5} W/m^{3}
$$
 (6) $\epsilon = M/M^{b}$ (8)

In Fig. 2, this implies that the line, not shown, joining the where, as earlier, the b superscript denotes blackbody. peaks of the emittance for each temperature in the log-log The emissivity of a given surface can vary with the wavescale is a straight line, and furthermore that the peak values length, the angle of observation, and the temperature. Thus increase proportionally to the temperature to the fifth power. the *spectral emissivity* ϵ _s is defined by

It is also clear from Fig. 2 that the emitted power at any given wavelength below the maximum emitted power increases more and more rapidly with temperature as the wavelength decreases. Thus for temperatures between 2500 K and 3000 K, typical of ordinary general lighting lamps, the emitted power in the middle of the visible increases at about the ninth power of the temperature.

By integrating Eq. (1) from 400 nm to 750 nm, the approximate radiant emittance of a blackbody in the visible region of the spectrum can be obtained. Dividing this integral by the total emittance [i.e., Eq. (3)], we obtain the fraction of the emittance (emitted power) in the visible region. Figure 3 shows this fraction as a function of temperature between 1000 K and 10,000 K. Note that between 2500 K and 3500 K the visible emittance fraction increases from about 5% to 20% of the total radiated power. The peak emittance value is slightly over 40% and occurs around 6900 K.

Luminous Efficacy of a Blackbody

The luminous efficacy of a blackbody is equal to the ratio of **Figure 4.** Lumen efficacy of a blackbody as a function of temperits total luminous emittance (flux) to its total radiant emit- ature.

tance (flux). This value is obtained in a similar manner to that for the fraction in the visible shown in Fig. 3. The difference is that the luminous flux is obtained by integrating the product of the spectral emittance by the eye sensitivity curve $V₁$. The eye sensitivity curve, not shown, is a near bell-shaped curve peaking at a value of one at 555 nm and going to approximately zero at 380 nm and 760 nm, respectively. Further, a scaling factor of 683 is used to define the lumen output per watt at 555 nm. The total radiant flux is given by Eq. (3). Thus the equation for the luminous efficacy is

$$
\eta_{\rm b} = \frac{683 \int_{380}^{760} V_{\lambda} M_{\rm e,\lambda} d\lambda}{\sigma T^4} \tag{7}
$$

The luminous efficacy is plotted as a function of temperature **Figure 3.** Fraction of blackbody irradiance in visible as a function in Fig. 4. Here we show only values above 1 lm/W of input of temperature. power. Note that the lumen efficacy of a blackbody is around 20 lm/W at 3000 K and peaks at a value of about 98 lm/W at Blackbodies are, by definition, perfectly diffuse. Thus the a temperature of around 6500 K. As we will see, the luminous radiance (i.e., the emitted power per unit area per unit solid blackbody.

Radiation from Actual Surfaces *^L*^b

Emissivity. As was mentioned earlier, perfect blackbody By differentiating Eq. (1) with respect to λ and equating the materials do not exist in nature, even though some such as derivative to zero, we find that the maximum spectral emit- carbon come close to exhibiting blackbody characteristics. In tance occurs at general, however, the radiation properties of most material surfaces can be described by using the blackbody radiation laws in conjunction with the material surface's *emissivity*. Emissivity is a measure of how closely the flux radiated from Equation (5) is called Wien's Law. Substituting this expres- a given material approaches that of a blackbody. The total sion for λ_m into Eq. (1), we find the peak spectral emittance emissivity is defined as the ratio o emissivity is defined as the ratio of the radiant emittance of

$$
\epsilon = M/M^{\rm b} \tag{8}
$$

$$
K_{\lambda}(T) = M_{\lambda}(T)/M_{\lambda}^{b}(T) \tag{9}
$$

Directional spectral emissivity $\epsilon_{\lambda}(\varphi, \phi)$ is defined by

$$
\epsilon_{\lambda}(\varphi,\phi) = L_{\lambda}(\varphi,\phi)/L_{\lambda}^{b}(\varphi,\phi)
$$
 (10)

where $L_{\lambda}(\varphi, \phi)$ is the spectral radiance of the surface element in the direction (φ, ϕ) , and $L^b(\varphi, \phi)$ is the spectral radiance of a blackbody at the same temperature. In this context, ϵ may be referred to as hemispherical total emissivity, ϵ_{λ} as hemispherical spectral emissivity, and $\epsilon(\varphi, \varphi)$ as directional total emissivity. They are all related to the directional spectral emissivity above by appropriate integrations over wavelength and/or angles.

If the material is uniformly diffuse, the directional emissivity follows that of a blackbody (i.e., $\epsilon \propto \cos \varphi$ at all angles and wavelengths). If the material surface is gray, the spectral

The normal spectral emissivity of tungsten, based on data from Ref. 5, is shown in Fig. 5. Note that the emissivity changes quite dramatically with wavelength and also with
temperature. Note, interestingly, that the emissivity is inde-
femochator of the persium pendent of temperature at around 1300 nm. The directional emissivity, excep

vided by the total radiant emittance, σT^4 . Because spectral
emissivity values are not well known in the infrared nor are
directional emissivities known in general, the total emissivity
as a function of temperature is way to do this is to measure the total power used to re-
sistively heat a long tungsten wire of known surface area up that matches the shape of the emissive body's emittance sistively heat a long tungsten wire of known surface area up
to a known (measured) temperature. Such a measurement
would be done in yacuum to ensure no cooling and nower loss at a cool K, the color temperature of tungsten would be done in vacuum to ensure no cooling and power loss ature of 2800 K, the color temperature of tungsten wire will
to the gas, and with long enough wire so that the end losses be about 60 K higher, even though the ab

emissivity is independent of wavelength. **Figure 6.** Total and average visible emissivity of tungsten versus
The normal spectral emissivity of tungsten based on data temperature.

to the gas, and with long enough wire so that the end losses be about 60 K higher, even though the absolute emission is
are minimal. The result is shown in Fig. 6. Also shown is higher overall for the blackbody. Coiling th of internal reflections on the coil, so the difference between the color and material temperature decreases. For doublecoiled filaments, which are typical in common household (Aline) lamps, the average color temperature exceeds the true temperature by about 40 K at 2800 K.

> Another related concept is that of *brightness* temperature at a particular wavelength (generally 665 nm, the value used by most optical pyrometers). This is the temperature of a blackbody that gives the same absolute emittance at 665 nm as the material in question, in our case tungsten. The brightness or luminance temperature of tungsten is significantly lower (about 275 K at 2800 K at 665 nm) than the true temperature. This, of course, is a direct consequence of tungsten's spectral emissivity being below unity (ϵ = 0.419 at 2800 K at 10 $\frac{\text{spectral}}{665 \text{ nm}}$.

Figure 5. Normal spectral emissivity of tungsten for several temper- **Tungsten Efficacy.** The spectral selectivity of tungsten (i.e., ature values. the fact that the emissivity in the visible is higher than that in the infrared) is an important contributor to the efficacy sten atom will escape the wire. In argon at about 1 atm, the that can be obtained at a given temperature. Adding the spec- number of tungsten atoms that escape is about 1 in every tral emissivity term to the numerator of Eq. (7) and the total 500 that evaporate from the surface. Obviously, the less likely emissivity to the denominator, the luminous efficacy is given escape is, the longer it will take to erode the wire, signifi-

$$
\eta_{\epsilon} = \frac{683 \int_{380}^{760} \epsilon_{\lambda} V_{\lambda} M_{\mathrm{e},\lambda}^{\mathrm{b}} d\lambda}{\epsilon \sigma T^{4}} \,\mathrm{lm/W} \tag{11}
$$

a blackbody is shown in Fig. 7. Note that at a temperature of on the properties of the inert gas (i.e., gas density, atomic 3000 K the radiant efficacy of tungsten wire is about 27 Im/mass , and the cross sections for 3000 K the radiant efficacy of tungsten wire is about 27 lm W, whereas that of a blackbody is about 21 lm/W, an increase gas and tungsten atoms). Because a gas atmosphere near a of about 30% resulting from the spectral selectivity of tung- hot wire sets up a convective flow, a major difficulty is ensten. Coiling the tungsten, as is the practice in all lamps, re- countered in determining whether, and to what extent, a staduces the selectivity somewhat because the coil tends to be- ble density gradient, which assumes a quiescent gas, can be have more like a blackbody. The same of the set of the se

$$
m = 3.8 \times 10^8 \exp^{-\Delta H^{\circ}/RT} \text{ g} \cdot \text{cm}^{-2} \cdot \text{s}^{-1} \tag{12}
$$

perature. The could calculate the heat loss by conduction over a sheath of

by cantly increasing life expectancy. Thus adding a gas to surround the filament increases life at a given temperature. Fur- $\eta_{\epsilon} = \frac{683 \int_{380}^{760} \epsilon_{\lambda} V_{\lambda} M_{e,\lambda}^{b} d\lambda}{\epsilon \sigma T^{4}}$ lm/W (11) thermore, the mass loss process with an inert gas of atoms from the cylindrical wire filament in a tungsten A plot of the radiant efficacy of tungsten compared to that of mass density gradient. The diffusion coefficient is dependent

In addition to reducing the mass loss of tungsten, the Mass and Heat Loss in a Gas
Mass and Heat Loss in a Gas and Gas
Thus a sizable fraction of the power input is expended on non-Operating a tungsten wire at high temperature in a vacuum
leads to evaporation of tungsten atoms from the surface. The
evaporation rate is a very strong function of temperature, be-
ing proportional to about the 36th power ter. Moreover, a coil dissipates heat as if it were a wire with *A* diameter equal to that of the cylindrical coil. Thus he reawhere $\Delta H/R = 102,300$ K.

The evaporation rate changes by about a factor of 3 every

100°C when the temperature is between 2700 K and 2900 K.

At a temperature of 2800 K, the evaporation rate, using Eq.

(12) is about 13 (12) is about 13×10^{-9} g·cm⁻²·s⁻¹.
When gas is added to surround the filament in the lamp,
the tungsten evaporating from the surface encounters these
the tungsten evaporating from the surface encounters these
diam tile wire. The development of a ductile wire process by Coolidge in 1909 made possible the coiled tungsten filament used in current incandescent lamps.

Langmuir explained the reason for the slow increase in convective heat loss with wire diameter as follows: the velocity distribution around the hot wire of diameter *d* is such that the velocity at the surface of the wire is zero. Furthermore, at the surface, the temperature of the gas is equal to the wire surface temperature and decreases with distance from the wire surface. Also, because the viscosity of the gas increases with temperature, it could be expected that there exists a gas layer around the wire where the gas is quiescent. Thus the heat loss to the gas near the filament surface could be assumed to be the result of conduction, not convection. On the other hand, at some distance from the filament, the gas is in convective motion. In the convective region, Langmuir made ³⁰⁰⁰ ³⁵⁰⁰ the simplifying assumption that the gas temperature was Figure 7. Total and average visible efficacy of tungsten versus tem- equal to the wall or lamp envelope temperature. Thus he

called the Langmuir sheath. The difficulty comes in calculat- is beneficial to reducing gas losses, there is a small penalty ing the thickness of the sheath. See Chapter 2 and Annex A paid in efficacy. This is because light exiting a filament from of Ref. 8 for how this can be done. the inside of a coil has the opportunity to first undergo one or

lamps for about 80 years. What specifically are the advan- double-coil the tungsten wire. That is, the wire is first coiled tages of tungsten over other incandescent materials? Three into what is called a primary coil. This coil is itself then coiled major advantages of tungsten over other materials are of pri- into what is referred to as the secondary coil. Some coils are mary importance. Tungsten has: even triple coiled, although in most cases the benefits are

-
-
-

The primary reason tungsten is the preferred material for in-
candescence is that it can be operated at a *higher temperature*
than any other metal. The melting temperature is about 3650
K. Furthermore, the evaporation ra tungsten as a function of temperature is lower than any conductive solid; about a factor of ten lower than tantalum, the next best material in terms of vapor pressure. Everything else being equal, the higher the operating temperature the higher the lumen efficacy as demonstrated in Fig. 4 for a blackbody.

As discussed previously, the *spectral selectivity* of tungsten Here, *h* is the turn separation of the coil (measured from the is also an important contributor to the efficacy that can be center of the wire on one turn to That is, at a given temperature, they give off more radiant The pitch ratio given in Eq. (12a) is actually slightly differencient energy in the visible region and less in the infrared compared ent than that used by most en to tungsten. These have so far proved unsuitable for incandes- The latter, "engineer's" pitch ratio is given by cent lamps because of their extreme brittleness, which causes an inability to form into suitable filaments and the tendency to disproportionate at high temperatures. Furthermore, despite higher melting point temperatures, these materials generally display higher vaporization rates for typical lamp gas fills than does tungsten (see Ref. 9).

Finally, the fact that tungsten wire is ductile enough that it can be drawn from solid tungsten ingots at low temperatures and then transformed into a stiff, rigid body through doping and recrystallization at high temperatures is a unique and important feature of doped tungsten. Without this property coiled filaments would not be practical. The capability of extended operation without sag or distortion at temperatures greater than 90% of melting is noteworthy; it is a characteristic not found in most metals.

Coiling

As mentioned earlier, the primary reason for coiling a tungsten filament is to reduce the amount of heat lost to the gas. Instead of having a long thin wire with a large surface area in conductive contact with the gas, the wire is coiled into what **Figure 8.** Schematic of single coil with definitions of *h*, *h*, *D*, is effectively a much shorter cylinder with a dramatically re- and *m*.

gas surrounding the filament. This quiescent gas layer is duced effective surface area. Even though the effect of coiling more internal reflections. This has the effect of making that **PRACTICAL FILAMENT LAMPS** portion of the light more blackbody-like with a lower selectiv-
ity, albeit higher overall emissivity, than that of a straight **tungsten wire.** The effect of coiling on lamp efficacy will be **Why Tungsten?** Seen later when the basics of filament coils are introduced.

Tungsten has been the material of choice in incandescent Often, to minimize the thermal gas-loss, it is beneficial to small to nonexistent.

1. The lowest evaporation rate (vapor pressure) of any Coiling is accomplished in practice using wire mandrels metal (discussed previously), about which the wire or primary coil is wound. The primary 2. The spectral selectivity which enhances visible light coil is usually made by winding the tungsten wire around a output (also discussed previously), and molybdenum wire mandrel. This primary mandrel stays in-
3. Thermo-

$$
\text{pitch ratio:} \qquad K_{\text{p}} = \frac{h}{D} \tag{12a}
$$

mandrel ratio:
$$
K_m = \frac{m}{D}
$$
 (12b)

is also an important contributor to the efficacy that can be center of the wire on one turn to the center of the wire on an obtained at a given temperature. Some ceramic compounds adjacent turn). D is the wire diameter, a adjacent turn), D is the wire diameter, and m is the inside such as hafnium nitride or tantalum carbide display an emis-
diameter of the coil. This is equivalent to the outer diameter sivity curve that is even more selective than that of tungsten. of the mandrel wire about which the tungsten wire is wound.

ent than that used by most engineers and coil manufacturers.

$$
K'_{\rm p} = \frac{h'}{D} \tag{13}
$$

turns per unit length (usually written as TPI, for turns per

$$
K_{\rm p} = \frac{2K'_{\rm p}(K_{\rm m}+1)}{\sqrt{K_{\rm p}^{'2} + 4(K_{\rm m}+1)^2}}
$$
(14)

(Note that the expression for this found on page 146 of Ref. 2 is incorrect.) These coiling parameters are used to relate the Similarly, we can obtain an expression for the wire length *l* wire length and diameter to the coil length and diameter, from the equation for power. The power which show up in the gas loss equation and a multiplying filament is dissipated by radiative losses P_r , which dominate, factor δ for the efficacy, as will be shown later.

Rudiments of Lamp Design $P = P_r + P_g + P_l = P_r + \Delta$
An incandescent lamp is rated by how much power it consumes, how much light it generates, and how long it is ex- where the two nonradiative loss terms have been collected pected to burn before failure. In addition, the voltage or cur- together in ΔP .
rent of the power source needs to be specified. These lamp The radiated ratings or operating characteristics are met by choosing a by multiplying the blackbody emittance in Eq. (3) by the total tungsten wire of a given length and diameter such that, when tungsten emissivity and the wire surfac placed across a given power source, it reaches a temperature reabsorption of radiated power by a coiled wire, called the that gives the specified power, lumens, and life values. Thus coiling factor δ , will be described that gives the specified power, lumens, and life values. Thus coiling factor δ , will be described later. The coiling is weakly incandescent lamp design is principally concerned with simul-
dependent on both the wavelen taneously matching the conditions of *voltage* (or current or power, which represents integration over all wavelengths, the resistance), *power* consumption, *lumen* output, and *life* by ma- ϵ expression δ_t will be used. Thus nipulating the wire *length,* wire *diameter,* and filament *temperature*. Note that because there are only three intrinsic parameters that relate to the filament (i.e., wire length and diameter and filament temperature), only three of the four Solving Eq. (17) for the wire length *l* gives lamp characteristics listed here can be specified indepen-
dently. $l = \frac{P - \Delta}{I + \Delta Q}$

Even though only three filament-related parameters are considered to be intrinsic (i.e., affect all parameters), other
lamp-related parameters such as coiling, gas type and pres-
sure, and wall temperature have a significant impact on some
of the lamp characteristics. These o are considered to be supplemental rather than intrinsic parameters as are the wire dimensions and temperature. A brief review of the underlying principle physical relationships be-

desired power P as being fixed. From Ohm's Law, this fixes values for d, l, and T become better defined in the calcula-
the filament resistance $R = V^2/P$. As will be shown momen-
torily the filament wire length and wire di tarily, the filament wire length and wire diameter may then
be derived from simultaneous solutions of the resistance and
net derived using Eqs. (15) and (19), an initial value for the
neuron countion where an initial value power equation, where an initial value of the temperature has total luminous flux from the filament may be derived by mul-
been specified. Given these initial values for wire length, di-
tiplying the wire surface area, S now calculated. With this new temperature, the wire length and wire diameter are recalculated. This process is iterated until the solution no longer changes within a specified error. This process is shown in detail later.

This latter definition is the one generally known because h['] Consider the two equations for resistance and power. First, is easy to measure. It is simply the inverse of the number of the resistance of a wire is a given by the ratio of the wire length *l* to the cross sectional area, $A = \pi d^2/4$, times a temperinch). The relation between K'_p and K_p is ature-dependent material property, the resistivity $\rho(T)$. Here, *d* is the wire diameter. Thus an initial value for the wire length is given by

$$
l = \frac{RA}{\rho(T)} = \frac{V^2 \pi d^2}{4P \rho(T)}\tag{15}
$$

from the equation for power. The power input P to a lamp as well as heat loss to the gas P_g and conduction to the leads *P*l. Thus

$$
P = P_{\rm r} + P_{\rm g} + P_{\rm l} = P_{\rm r} + \Delta P \tag{16}
$$

The radiated power from a tungsten wire can be obtained tungsten emissivity and the wire surface area. The effect of dependent on both the wavelength and temperature. For the

$$
P = \pi \cdot d \cdot l \cdot \delta_t(T) \cdot \epsilon(T) \cdot \sigma \cdot T^4 + \Delta P \tag{17}
$$

$$
l = \frac{P - \Delta P}{\pi \cdot d \cdot \delta_t(T) \cdot \epsilon(T) \cdot \sigma \cdot T^4}
$$
(18)

$$
d = \left[\frac{4P\rho(T)(P - \Delta P)}{V^2\pi^2\delta_t(T)\epsilon(T)\sigma T^4}\right]^{1/3} \tag{19}
$$

tween the lamp characteristics and filament parameters fol-
lows. These relationships constitute the fundamentals of de-
sign. Because of the interrelating relationships of the various
parameters, the approach is by neces age lamps, the lead conduction losses and gas convection **Design Procedure** losses are about equal, usually around 5% each. A value for One approach is to start with the lamp voltage *V* and the ΔP of about $0.1 \times P$ is a good place to start the iteration. As desired nower *P* as heing fixed From Ohm's Law this fixes values for *d*, *l*, and *T* become

been specified. Given these initial values for wire length, di-
ameter, and temperature, the luminous flux and life may also blackbody distribution function weighted by the eye sensitiv-
be derived. From the ratio of calc $\phi(T)$ is given by

$$
\Phi(T) = S \int_{380}^{760} V_{\lambda} \epsilon_{\lambda}(T) \delta_{\lambda}(T) M_{e,\lambda}^{b}(T) d\lambda \tag{20}
$$

the initial estimate of temperature T_0 and given the values source. A second-order fit to the data from 2400 K to 3600 K for *l* and *d* calculated earlier. However, since the lumen value gives the following functional form: is assumed specified, the ratio of Φ_{given} to $\Phi(T_0)$ can be used to calculate a new value for the temperature, T_1 , from the exponential part of the $M_{e,\lambda}^{\text{b}}$ term, which is then inserted into Eqs. (15) and (19).

emissivity of the coil. For straight wire, $\delta = 1$. For a coil, the Ref. 5. A second-order fit gives the following functional form: light generated on the inside of the coil has a chance of being reabsorbed, thereby increasing the filament temperature. For a tungsten coiled coil, a typical value at 2700 K is $\delta \sim 0.79$. The coiling factor δ is a function of temperature and coiling
parameters, and is given, for a single coil, by the following
expression (see Ref. 2):
 $P_e(T)$, the gas-loss term, may be taken from the following ex-
expres

$$
\delta_1(T_1) = \frac{1}{2}\Bigg[1 + \frac{1}{\pi(K_{\rm m}+1)} + \left(1 - \frac{1}{\pi(K_{\rm m}+1)}\right)\frac{K_{\rm p}-1}{K_{\rm p}-r(T_1)}\Bigg] \eqno(21)
$$

The coiling parameters K_m and K_p are given by Eqs. (12)–(14). The temperature dependence of δ is carried through the reflectivity $r(T)$, which is given by

$$
r(T) = 1 - \epsilon(T) \tag{22}
$$

$$
\delta = \delta_1 \delta_2 \tag{23}
$$

$$
\delta_2 = \frac{1}{2} \left[\left(1 + \frac{1}{\pi(K_{\mathrm{m2}}+1)}\right)\delta_1 + \left(1 - \frac{1}{\pi(K_{\mathrm{m2}}+1)}\right)\frac{K_{\mathrm{p2}} - f_1}{K_{\mathrm{p2}} - r_1}\right] \eqno(24)
$$

$$
f_1 = 1 - \left(\frac{K_{p1} - 1}{K_{p1}}\right)^2 \tag{25}
$$

that are needed in this iterative procedure are the tungsten reduction in filament temperature, which greatly reduces the resistivity, total emissivity, and spectral emissivity along evaporation rate. In the long run, the evaporation rate would with the gas-loss term needed for Eqs. (16)–(19). A second- become so small as to be inconsequential. Thus when we asorder polynomial fit to the resistivity data from 2000 K to sume that evaporation is uniform from the whole filament, we 3600 K taken from Ref. 10 provides the following functional find the predicted behavior is one of infinite life. form for $\rho(T)$, with *T* measured in Kelvin: This obviously is not what happens. Instead it is known

$$
\rho(T) = -3.19353 \times 10^{-6} + (2.63402 \times 10^{-8})T
$$

+
$$
(1.8011 \times 10^{-12})T^2 \Omega \text{ cm}
$$
 (26)

This equation is solved for the flux value $\Phi(T_0)$, in terms of The total tungsten emissivity is also taken from the same

$$
\epsilon(T) = -2.03926 \times 10^{-2} + (1.88601 \times 10^{-4})T
$$

– (2.35764 × 10⁻⁸)T² (27)

The coiling factor δ can be thought of as modifying the The spectral emissivity for tungsten at 2600 K is taken from

$$
\epsilon(\lambda, T = 2600) = 0.55788 - (233904)\lambda + (4.91792 \times 10^{10})\lambda^2
$$
\n(28)

pressions, which were derived for a typical 40 W, 120 V filament lamp with 80 kPa (~600 torr) cold pressure fill:

(21)
$$
\text{for } N_2: P_g(T) = -1.2522 + (1.6968 \times 10^{-3})T + (6.4245 \times 10^{-7})T^2 \text{ W}
$$
 (29)

for Ar:
$$
P_{\rm g}(T) = -0.8535 + (1.3868 \times 10^{-3})T
$$

 $+ (3.1375 \times 10^{-7})T^2$ W (30)

$$
r(T) = 1 - \epsilon(T) \qquad (22) \qquad \text{for Kr: } P_g(T) = -0.6236 + (9.9857 \times 10^{-4})T + (1.5576 \times 10^{-7})T^2 W \qquad (31)
$$

where $\epsilon(T)$ is the total emissivity of tungsten.
Figure 9 shows these gas-loss terms as a function of temper-
Figure 9 shows these gas-loss terms as a function of temperature.

Filament Life. Predicting the life expectancy of a lamp filament is by far the most difficult and least understood of the where δ_2 is the coiling factor for the secondary coil and is lamp design problems. Several mechanisms are involved in given by causing filament burn-out, which is the normal predictable end-of-life mechanism. The most important phenomenon, and the easiest to understand theoretically, is tungsten evaporation from the surface of the wire. This was discussed earlier. Obviously, as tungsten evaporates, the wire diameter decreases. When the wire is reduced to some critical size, the and where $r_1 = 1 - \delta_1 \epsilon$ is the reflectivity of the primary coil,
and ϵ is the temperature-dependent total emissivity. The
opacity f₁ is given by
opacity f₁ is given by ture, the thicker the wire, the longer it would take to reduce it, leading to a linear increase with life with wire diameter.

Even though it has been found empirically that filament life does vary inversely with the evaporation rate, the problem is not as simple as it appears. Consider what is expected to happen to an evaporating filament on a constant voltage Here, all subscripts 1 and 2 refer to the primary and second-
source. As the wire diameter decreases as a result of evaporaary coils, respectively. tion, the resistance increases causing the current, and hence The temperatures and wavelength-dependent parameters the power, to decrease. But a power decrease must imply a

> that the filament develops hot spots (i.e., regions that are slightly higher in temperature than those nearby). The hotter regions evaporate more rapidly, causing more rapid thinning of the wire than on average. These thin areas will run even

different gas fills for 40 W, 120 V lamp.

hotter because the resistance is higher there, and because the The temperature dependencies of the radiated power, lu-

$$
\Lambda = \frac{C_{\Lambda}d^{x}}{\Gamma(T, \text{gas}, p, \text{coil}, T_{\text{w}})}
$$
(32)

Here C_A is a normalizing constant empirically determined. It **TUNGSTEN-HALOGEN LAMPS** is also found empirically that the dependence of life on wire diameter *d* is about linear for very large wire diameter [i.e., What should emerge from the preceding discussion on incanover 10 mils $(2.54 \times 10^{-4} \text{ m})$, but this dependence increases descent lamps is an expectation that if some gas (when comin magnitude as the wire diameter gets smaller, becoming bined with a coiled filament) is good for increasing life and larger than d^3 for wire diameters less than 2 mils (5.08 \times efficacy, more gas should be better. Furthermore, the denser 10⁵ m). Because this dependence is difficult to determine, *x* the gas, the better. Both would reduce tungsten loss through is used for the diameter dependence. The tungsten atom diffu- evaporation and would enable higher- temperature filament sion term Γ depends strongly on the temperature T but also operation, which results in a more efficacious lamp. Typical depends on the gas type and pressure, the coiling parameters, incandescent lamps are filled with a mix of argon and nitroand the wall temperature. Predictive models for the diffusion gen to a pressure of ~ 0.8 bar. When lit, these lamps are term are most easily done by extensions of the Langmuir roughly at atmospheric pressure. To hold higher pressures sheath simplification, but for greater accuracy convective- would require a stronger and smaller lamp body. However,

current must be continuous throughout the wire, the thin mens, radiant efficacy, and life for tungsten wire are shown areas dissipate more power. Thus a positive feedback cycle in Fig. 10. Here the data for each parameter is normalized to develops, causing the hot spot to increase in temperature one at a temperature of 2800 K to show more clearly the more and more rapidly until it reaches the melting point of strength of the temperature dependence. Note that because tungsten and the filament fails (see Ref. 11). It is known that lumens increase about the square of the radiated power, the hot-spot development is the cause of filament failure, but all efficacy increases at about the same rate as the radiated the causes of hot-spot development are not known nor is their power. Note further that life, based on the temperature derelationship to each other understood well at all. It is proba- pendence of the evaporation rate, decreases most rapidly with bly because the life-ending mechanism involves hot spots in increasing temperature. Hence, for a given design situation, which the distribution of life is found to follow a normal curve luminous efficacy increases can be traded against shorter life. extremely well. Furthermore, the standard distribution of the However, the efficacy increase is only on the order of 10% of normal life curve is usually quite large being about 20% to the decrease in life. This situation always holds for incandes-25% of the expected life. The expected life. Cent and halogen lamps. The life at a given temperature can From the diffusional flow of tungsten atoms through the be increased by increasing the fill gas pressure, going to a Langmuir sheath, as already discussed, a relationship be- denser rare gas, increasing the wall temperature (all of which tween expected filament life Λ and the filament parameters are done in halogen lamps), and decreasing the voltage that can be put into the following form: results in larger diameter wire, but the temperature dependence remains as shown in Fig. 10. For further discussion on the filament lamp design approach used here, see Ref. 12.

based FEM models have been developed. with a smaller lamp body, the surface area is greatly reduced,

Figure 10. Temperature dependence of various parameters for tungsten wire.

and the flux of evaporating tungsten atoms, although reduced **Mechanism of the Halogen Cycle**

incandescent coil from depositing on and darkening the lamp wall. The tungsten evaporating from the coil reacts with the halogen in the cooler regions of the lamp and is converted into gaseous halogen-containing compounds. These compounds decompose en route to the hotter regions of the lamp, depositing tungsten metal on the leads or cooler parts of the coil and releasing the active halogen to continue the cycle. For halogen cycles used today, the tungsten is not deposited in exactly the same places on the coil from which it evaporated (13), so the coil in a halogen lamp does not last forever and eventually

can be made with a much smaller, and consequently much sion reaction between the tungsten filament and the iodine,
stronger, bulb. This permits the use of higher pressure fill which slightly increases the mass loss rate of gases and the economical use of rarer denser inert gases such This is represented by Reaction 4. as krypton and xenon. With higher pressures and denser gases, the rate of tungsten mass loss from the coil is decreased, and so life is increased. Denser inert gases also have lower thermal conductivity, which results in less energy lost by gas conduction. With these changes, the coil may be redesigned for increased light output, increased life, or some com- It is likely that an analogous mechanism operates for the brobination thereof. A typical halogen lamp may be 10% brighter mine cycle where the transport species is WO_2Br_2 . There is and last twice as long as an ordinary incandescent lamp. On also the possibility of an oxygen-free the negative side, halogen lamps can operate with the lamp mine where the transport species are WBr₄ and WBr₅. These walls as hot as 900 K and with internal pressures of 1.5 MPa species are less stable than WO₂Br₂ (15 atm) or more. For safe operation, such lamps must be pre- rates. Wall cleaning and lead corrosion rates are so sensitive vented from contacting combustible materials and a means of to trace amounts of oxygen that it is difficult to say that, in containing any fragments from potential wall rupturing must practical bromine cycle lamps, oxygen is not involved. Oxygen be provided. usually enters the lamp in the form of water or metal oxides.

because of the higher pressure, would nonetheless cause
eventual wall blackening. What is needed is a way to keep
the vall clean despite the close proximity of the wall to the
filament.
Halogen lamps are incandescent lamp

At filament:

$$
W(solid) \to W(gas) \tag{R1}
$$

At/near filament:

$$
W(solid, gas) + 2O(gas) \rightarrow WO_2(gas) \tag{R2}
$$

At/near wall:

$$
WO_2(gas, solid) + 2I(gas) \rightarrow WO_2I_2(gas) \qquad \quad (R3)
$$

fails, generally in the same manner as an ordinary incandes-

ent coil.

the chemical sense. Not enough is known for that level of de-

With such a wall-cleaning agent, the incandescent lamp

can be made with a much smalle which slightly increases the mass loss rate of the filament.

At filament:

$$
W(solid) + n I(gas) \to WI_n(gas), n = 1, 2
$$
 (R4)

also the possibility of an oxygen-free transport cycle for brospecies are less stable than WO_2Br_2 and are formed at lower

Control of reaction rates limits use of the elemental forms to I_2 , while Br_2 , Cl_2 , and F_2 are too reactive. The addition of **Materials Requirements.** To prevent reaction and loss of Cl-, to I-based halogen doses with the lamp walls, the glass hydrogen inhibits the rate of lead corrosion and wall cleaning Br-, or I-based halogen doses with the lamp walls, the glass
and permits the use of lamps dosed with HBr CH-Br, and used must not contain alkali or alkaline ea and permits the use of lamps dosed with HBr, CH_2Br_2 , and used must not contain alkali or alkaline earth elements. This CH_2Br_2 and used must not contain alkali or alkaline earth elements. This CH_2Br_2 and CH_2Br_2 lim CH_3Br . The addition of oxygen accelerates the rate of lead limits the choice of wall materials to alumino-silicate glasses corrosion and wall cleaning, permits the use of lamps dosed of negligible alkali content, 96% corrosion and wall cleaning, permits the use of lamps dosed of negligible alkali content, 96% silica glass (such as Vycor, with $CH₃I$, and mandates very precise control of the oxygen level in all types of bromine lamps. With the improved manu- temperatures of halogen lamps, Vycor and quartz are both facturing processes of today, most halogen lamps use bro- permeable to H_2 whereas the alumino-silicate glasses are not.

Doses used in special cases include CH_3I , $PNBr_2$, and mix-
tures of halogen compounds HRr , CH_3Br_3 , CH_3Br_4 and CH_3I commercially available fluorine cycle lamps. The internal tures of halogen compounds. HBr, CH_2Br_2 , CH_3Br_3 and CH_3I commercially available fluorine cycle lamps. The internal are gases and are added to the lamp along with the inert fill metal parts of halogen lamps are tungs are gases and are added to the lamp along with the inert fill metal parts of halogen lamps are tungsten or gas. PNBr_a is a solid and is added to the lamp as a solution lead wires and supports and the tungsten coil. gas. PNBr₂ is a solid and is added to the lamp as a solution in petroleum ether, with the petroleum ether solvent allowed to evaporate prior to evacuation and inert gas fill. CH₃Br and **Temperature Requirements.** Vycor and quartz require the CH₃Br, doses are less corrosive than HBr and have a much use of molybdenum foil hermetic seals for CH_2Br_2 doses are less corrosive than HBr and have a much use of molybdenum foil hermetic seals for the current-car-
lower tendency to adsorb on the inner surface of the lamp rying leads. This restricts the temperature o lower tendency to adsorb on the inner surface of the lamp rying leads. This restricts the temperature of the seal area to exhaust and fill equipment, which increases dose reproduc-
less than 620 K if the seal life is to ex exhaust and fill equipment, which increases dose reproduc-
ideas than 620 K if the seal life is to exceed 1000 h, unless
these seals are not exposed to air. The lamp walls must be

Within seconds of first lighting the coil, CH_3Br and hot enough to prevent the volatile tungsten-halogen-con-
CH₃Br₃ are converted to HBr as shown in Reactions 5 and 6 taining compounds from condensing and removing t CH_2Br_2 are converted to HBr as shown in Reactions 5 and 6 taining compounds from condensing and removing the halo-
(17).

$$
CH3Br(gas) \rightarrow HBr(gas) + H2(gas) + C(solid)
$$
 (R5)

$$
CH2Br2(gas) \rightarrow 2 HBr(gas) + C(solid)
$$
 (R6)

ment. The additional hydrogen released from Reaction 5 has of unacceptable water released from Reaction 5 has to the lamp interior. an inhibiting effect both on the kinetics of wall cleaning and on the kinetics of lead corrosion.

The amount of the halogen added typically ranges from **Lamp Orientation Requirements.** Ordinarily, halogen lamps 0.03% to about 5% (mole or volume percent). The amount of can be operated in any orientation. A special case arises for halogen added increases with increasing tungsten evapora- the linear halogen lamps [i.e., those with lengths over 5 cm tion rate, increasing hydrogen to bromine ratio, and decreas- \sim 2 inches) having outer lamp wall diameters of about 1.2 cm ing amounts of oxygen. The hydrogen to bromine ratio is a (0.5 inch)]. To ensure uniform distribution of halogen, these function of the type of halogen dose, because little additional lamps must be burnt within about 4° of horizontal. When

ficient amounts remain in the lamp as contaminants during where the halogen is depleted (p. 71 in Ref. 15, p. 143 in Ref. normal manufacture. The most common sources of this oxy- 34) Occasionally, corrosion problems will result for lamps opgen include water adsorbed on lamp parts and in the exhaust/ erated in certain orientations when the hot gas flow from the fill system, water and other oxygen-containing species dis- coil is directed onto metal parts (35,36), but these problems solved in the lamp walls, oxygen dissolved in the metal parts, are usually resolved in the design phase before production.

Halogen Lamp Engineering and metal surface oxides. In some cases, there is too much halogen and metal surface oxides. In some cases, there is too much **Halogen Types Used**. In an operating lamp, the halogen wygen contamination, and oxygen getters are required. Many dose must react quickly enough to convert all evaporating getters. have been proposed for use with halogen

mine doses.

Common bromine doses are HBr CH.Br, and CH.Br sists attack by fluorine-based halogen doses. Nor has any eco-Common bromine doses are HBr, CH_2Br_2 , and CH_3Br , sists attack by fluorine-based halogen doses. Nor has any eco-
ses used in special cases include CH₂I PNBr, and mix- nomical coating been developed. Consequently, ther

lity.
Within seconds of first lighting the coil. CH₂Br and bot enough to prevent the volatile tungstep-balogen-congen from the cycle. For iodine cycle lamps, the coldest permissible wall temperature is about 520 K (33). For bromine cycle lamps, the coldest permissible wall temperature is about 440 K (33) . In general, the upper limit to the lamp wall temperature is determined by either its rupture strength or the stabil-If used in excess, the carbon released from Reactions 5 or 6 ity of the tungsten transport species. The latter consideration
can deposit on the bulb wall causing darkening or can be
transported to localized areas of the c

hydrogen arises from the manufacturing process. burnt off-horizontal, the linear lamps act like thermal separa-Oxygen is not usually added to bromine lamps because suf- tor columns, and wall blackening will occur in the regions

A complete understanding of the halogen relae would require maximum mount of tongeto that can exist in the gas phase. See all the single points of the gas phase of the complexity of the problem, and nobody yel has determi

derstanding of tungsten–halogen lamps. balance in the rest of the lamp. Calculations were per-

Scientific Understanding the scientific Understanding discussion is merited. The tungsten elemental solubility is the

oxybromides, which lose stability as the temperature exceeds about 1300 K. In the intermediate temperature region, only the simpler bromides and oxides contribute to the tungsten elemental solubility. Eventually, as the temperature reaches the normal operating range, the tungsten elemental solubility becomes dominated by tungsten gas from the physical evaporation of the coil. The tungsten elemental solubility for an incandescent lamp in a pure atmosphere is shown as curve W, gas in Fig. 12.

Focusing on the curve for 0.1 ppm oxygen contamination in Fig. 12, at a temperature typical for a 1000 h life lamp, 2850 K, denoted by arrow A, the gas in the region of the filament will contain 4×10^{-9} moles tungsten per mole of inert gas, arrow B. If this gas is suddenly moved to the wall, no solid tungsten compounds will form as long as the wall temperature is lower than about 1500 K, arrow C. Which tungsten compounds are formed is answered by looking at the details of the thermodynamic calculation to see which, if any, condensed phases are formed.

Maps can be made to show which condensed phases are formed for various lamp operating conditions using thermodynamic calculations. One such map is shown in Fig. 13 where the condensed phases are shown for various lamp wall temperatures and oxygen contamination levels for a 2850 K tungsten coil operating in 2 MPa (20 atm) Ar containing 0.05% HBr. In this map, the tungsten elemental **Figure 11.** Many phenomena must be considered for a complete un- solubility at the coil was used to set the tungsten atom

Figure 12. Tungsten elemental solubility calculated for a tungsten–halogen lamp filled with 2 MPa (20 atm) inert gas containing 0.05% HBr is very sensitive to trace levels of oxygen contamination. Transport of tungsten can occur from high elemental solubility regions to low elemental solubility regions.

formed every 100 K and 0.5 log units in oxygen level, which duced, the minimum wall temperature is increased, and causes the jagged boundaries between phases. Figure 13 maximum wall temperature is decreased. depicts the purity and wall temperature required to prevent **The Future** wall deposits in this halogen lamp. Figure 13 shows that as the oxygen contamination is reduced below 0.1 ppm, the The performance of halogen lamps will continue to improve as wall temperature range for deposit-free operation is re-
designs become more optimized. This will be an wall temperature range for deposit-free operation is re-

Figure 13. Thermodynamic calculations can be used to map operating conditions leading to clean deposit-free walls. This figure indicates such a region for a tungsten-halogen lamp filled with 0.05% HBr operating at 2 MPa (20 atm) with a coil temperature of 2850 K. Rough boundaries are the result of the discrete nature of the calculations. These maps are useful for showing trends but may not be accurate.

Type	Power W)	% Visible	$\%$ Non-Vis.	% Non-Rad.	Efficacy (lm/W)	Life (h)
Incandescent	100	10	75	15	17.1	750
Halogen	90		74	15	17.5	2000

Table 1. Power Balance and Performance of 100 W Incandescent and 90 W Halogen Lamps

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provement, Final report for New York St tive, area where halogen or other chemical transport cycles Development Authority contract No. 3034-IABR-BR-94, 1996. may find use is to stabilize the phases of other materials that 10. R. C. Weast and M. J. Astle (eds.), *Handbook of Chemistry and* could be used as incandescent bodies at temperatures ex- *Physics,* 62nd ed., Boca Raton, FL: CRC Press, 1981–82. ceeding the melting point of tungsten. 11. H. Hörster, E. Kauer, and W. Lechner, The burnout mechanism

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Table 1 shows the power balance and performance compari-
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son for a typical 100 W incandescent lamp and a 90 W halo-
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ways, though, there is a price to be paid for the performance

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standard incandescen

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