PHYSICAL ACOUSTICS

Physical acoustics deals with the principles of high-frequency sound and related phenomena, as well as their applications to basic research in physics, chemical physics, and biophys- remarkably stable oscillation. The electric pulse technique ics. Physical acoustics has a wide scope, including problems originally developed for radar systems during World War II of wave propagation (i.e., reflection, refraction, transmis- was soon introduced to ultrasonics and magnified the potension, scattering, diffraction, interference, and resonance or tial of ultrasound on a large scale. Physical acoustics today mode conversion, of which the essential part is in common owes much to these modern developments of ultrasonics, elecwith optics); mechanisms of generating and receiving sound tronics, and optics. waves; and linear and nonlinear interactions with light, electric, magnetic, or stress fields in the medium. Coupling **ULTRASOUND** with microscopic structures of matter in a static or a dynamic manner is also an important subject and provides
fundamental knowledge for studies of materials science by
sound involves sound or mechanical vibration with fre-
sound waves. In contrast to general acoustics, which

While the history of acoustics can be traced back to the age the molecular mean free path or the interatomic distance,
of Pythagoras, physical acoustics in a modern sense started
in the seventeenth century when Galileo int Concerning Two New Sciences'' (1). Physicists in the eigh- **Ultrasonic Velocity** teenth century, including Newton, Euler, and Laplace, developed theories of sound propagation (Newton's equation of Sound waves propagate with a kind of dynamic balance be-

demand for underwater detection stimulated by the *Titanic* hydrogen (1707 m/s) and helium (997 m/s). The moduli for disaster and the submarine menace in World War I, in 1917 longitudinal and transverse modes are $K + 4/3G$ and G , re-Langevin invented a piezoelectric quartz oscillator that pro- spectively, where *K* is the bulk modulus for hydrostatic volduced ultrasonic waves of controlled frequency and ampli- ume change and *G* the shear modulus. In liquid, $G = 0$ with tude. The quartz transducer was immediately applied to the very rare exceptions and only longitudinal waves propagate ultrasonic interferometer by Pierce, who studied the velocity whose velocity is roughly between 1000 m/s and 2000 m/s dispersion and absorption in $CO₂$ gas and launched molecular (the transverse waves travel but a very short distance in a acoustics, an important branch of physical acoustics. Wood highly viscous liquid). On the other hand, solids exhibit much and Loomis demonstrated the physical, chemical, and biologi- more complicated features (2). In an isotropic medium with cal effects of high-intensity ultrasound generated with a large infinite extension, longitudinal and doubly degenerated transquartz plate. As for the optical effects of sound, which had verse waves propagate, the former having a velocity roughly been known since the 1800s, Brillouin proposed a basic theory twice as high as the latter. Anisotropic media such as crystal of light diffraction in 1922, and experiments were conducted or composites have three independent modes that differ in in water and transparent solids soon after. The invention of velocity. In many cases, they are quasi-longitudinal and the laser in the 1960s was an encounter of two coherent quasi-transverse modes whose wave vector is pointed off the waves; the ideal light source led to the breakthrough of direction of propagation. Waves in a medium with boundaries acousto-optics, with brilliant applications both in the labora- are also of interest (3). The Rayleigh mode appears on the tory and industry. The progress of ultrasonics kept pace with surface of a semi-infinite solid, is usually referred to as a surthe progress of electronics. Cady incorporated a quartz oscilla- face acoustic wave (SAW), and has important applications in

used in low-temperature physics. The upper limit of ultrasonic frequency is not explicitly defined. At such a high **HISTORY** frequency range, where the wavelength is comparable to

sound velocity in air was somewhat strange), and the outline tween the inertia of mass and the elastic restoring force, and of physical acoustics was established by Rayleigh in his cele- the velocity is generally given as $v = \sqrt{E/\rho}$, where ρ is the brated ''Theory of Sound'' at the end of nineteenth century. density and *E* is the adiabatic modulus of elasticity appro-Sound with frequency beyond the audible limit also was stud- priate for the sound mode. In ideal gas, this equation is simied in those days. Savart generated frequencies up to 24 kHz ply reduced to $v = \sqrt{\gamma RT/M}$ with the aid of thermodynamics, with a toothed wheel and an elastic plate, and Galton in-
where γ is the specific-heat ratio, *R* the gas constant, and *M* vented a whistle that achieved 80 kHz. Savart and Galton the molecular weight. The velocity depends only on *T* (not on conducted auditory tests on humans and animals. pressure) and can be used for temperature measurement. Of In the early twentieth century, there was a breakthrough the three states of matter, gas has the lowest longitudinal in the modern age of physical acoustics. Spurred by urgent velocity, ranging from 200 to 400 m/s with the exceptions of tor in the vacuum tube circuit in 1920; the oscillator showed electronics devices. Lamb waves propagating in the plane of

on the ratio of the thickness to the wavelength. Generally Thermal energy drives a collective motion of atoms interconspeaking, ultrasonic waves have a linear relation between ω , nected with elastic force and excites the lattice vibration the angular frequency, and *k*, the wave number: The phase around their equilibrium positions, which propagates as a velocity defined as ω/k is a constant. There are cases, how- phonon with a certain frequency and wavelength. When the ever, in which the velocity depends on frequency. Such veloc- wavelength is much longer than the lattice constant (inity dispersion appears in a medium with boundaries, as is the teratomic distance), the phonon is regarded as ultrasound in case in Lamb waves, or in a medium involved in relaxation a continuum with a linear dispersion relation between ω and phenomena (described in the section entitled Molecular *k*. In the frequency range above terahertz, where one wave-Acoustics). The length includes only a few atoms, the lattice dynamics are

quency carrier waves and the other associated with a high-
energy concentration of elastic vibration. Regarding the for-
with *k* and perfectly vanishes at $k = \pi/d$, as shown in Fig. 1, quency carrier waves and the other associated with a mgn-
energy concentration of elastic vibration. Regarding the for-
mer, ultrasound has a great advantage under water, where d is the lattice constant. This is the limit phy. Nondestructive evaluation of opaque substances, such as
in defect detection or imaging, is also an important applications. The curve generally has three branches representing
tion of ultrasound as carrier waves. Ultr man body in comparison with X rays. In the field of modern
electronics, ultrasound has found a variety of new applications, each phonon has energy $\hbar\omega$ and behaves as a
electronics, ultrasound has found a variety of ne ing irreversible changes of materials and has widespread ap-
plications. Cleaning, welding, drilling, cutting, material pro-
crease in the vibration amplitude in a classical sense is an plications. Cleaning, welding, drilling, cutting, material pro-
crease in the vibration amplitude in a classical sense is an
cessing, emulsification, and atomization of liquids with increase in n the quantum number. This q cessing, emulsification, and atomization of liquids with increase in *n*, the quantum number. This quantum descrip-
ultrasonic vibration are standard techniques in industry; and tion is very important in dealing with prob ultrasonic vibration are standard techniques in industry; and tion is very important in dealing with problems such as heat vibrating surgical tools are commonly used in hospitals. Most conduction in dielectric solids, elec vibrating surgical tools are commonly used in hospitals. Most conduction in dielectric solids, electric conductivity in pure
of the applications in sonochemistry, such as polymerization, metals and Brillouin scattering in of the applications in sonochemistry, such as polymerization, metals, and Brillouin scattering in transparent media. These cutting of polymer chains, and promotion of reactions with phenomena are interpreted in terms of in cutting of polymer chains, and promotion of reactions with phenomena are interpreted in terms of interparticle colli-
ultrasound, take advantage of ultrasound's energy concen-
sions—phonon-phonon. phonon-electron, and phon ultrasound, take advantage of ultrasound's energy concen-

sions—phonon–phonon, phonon–electron, and phonon–

tration.

electrodes on both faces converts electric oscillation into elas- **Thermal and Electric Conduction** tic vibration and emits ultrasonic waves into a medium in Any substance at a finite temperature is considered a con-
direct contact with it. Piezoelectric transducers of different Any substance at a finite temperature is considered a con-
materials and trans are available: the mo materials and types are available; the most suitable one is chosen depending on the frequency range and the kind of medium. Piezoelectric ceramics such as PZT are currently used for all purposes over the range of 10 kHz to 10 MHz. Quartz is preferred in laboratories for its high Q factor and stability over the range from 1 MHz to 1 GHz. Thin films of zinc oxide or cadmium sulfide sputtered on a substrate of sapphire or fused quartz are effective in the hypersonic range (5). The piezoelectric polymer polyvinylidene fluoride (PVDF) is a flexible film that fits curved surfaces. These ultrasonic transducers are used for receiving signals as well.

PHONON

While ultrasound is a macroscopic vibration in an elastic continuum, the phonon is a quantum concept of microscopic vi- **Figure 1.** Dispersion of longitudinal and two transversal modes of bration in an atomic lattice that was originally introduced in phonon in lattice.

elastic plates have many modes of different orders depending describing the heat capacity of solids at low temperatures (6). better understood with the concept of the phonon. The disper-**Characteristic Features of Ultrasound and Its Applications** sion curve shows a strong nonlinearity reflecting the discrete
nature of the lattice. In the simplest lattice of identical atoms, There are two aspects of ultrasonic waves: one as high-fre-
for example, the group velocity defined as $d\omega/dk$ decreases photon, respectively.

Originally developed for crystals, the concept of the phonon **Ultrasonic Transduction** is expanded to other substances, amorphous, liquid, or gas: A common technique to generate ultrasonic waves is based
on piezoelectricity (4). A plate of piezoelectric material with
with excited by thermal energy.

perature means a local increase in *n*, and the natural preference for equilibrium drives some of the phonons out of the heated region. Free flight of the phonon at its own group velocity is immediately intercepted by other phonons, however, and the successive collisions give rise to multiple scattering. (The phonon-phonon interaction occurs through the anharmonic term in the interatomic potential.) Here is the image of phonon diffusion, leading to a good analogy with gas kinetics, in which molecules collide with each other and diffuse. The thermal conductivity is then given by the familiar equation common to various transport phenomena: $\kappa = (1/3)Cvl$, where *l* is the phonon mean free path (mean distance between successive collisions) and *C* is the heat capacity of the lattice per unit volume. At room temperature, *l* is on the order of nanometers, while $d = 0.1$ nm.

In metals, free electrons have a major role in thermal conduction as well as in electric conduction, in which phonons have significant influence (7). Phonon-electron collisions are
the dominant cause of resistance in metals that have few
the dominant cause of resistance in metals that have few
con crystal. After Tamura, Shields, and Wolfe structural imperfections (impurities, dislocations, and point defects), and the resistivity decreases rapidly as the phonon population decreases at low temperatures. In metals in a su-
nerconducting state on the other hand, phonons have a position of the light passing through the area is modulated spatially and perconducting state, on the other hand, phonons have a posi-
the light passing through the area is modulated spatially and
time effect on electron conduction. Superconductivity is theo-
temporally. On the other hand, photo tive effect on electron conduction. Superconductivity is theo-
retically explained by the electron pairs, and such pairing tion of sound by light: The optical energy is dissipated into retically explained by the electron pairs, and such pairing tion of sound by light: The optical energy is dissipated into
occurs because the phonon-electron interactions induce an at. heat, and the local expansion in the m occurs because the phonon-electron interactions induce an attractive force between two electrons, and the force exceeds the elastic waves. There is also a case in which the electric field
normal coulomb repulsive force below the critical temper. of light directly introduces strain normal coulomb repulsive force below the critical tempereffect (the second-order effect of strain proportional to the ature.

Phonon Imaging The Trials).

At very low temperatures, where *l* has a macroscopic length **Acousto-optics** of 1 mm or longer, phonon propagation becomes rather ballis-
tic than diffusive, as is observed by the experiment with a
heat pulse. A very short laser pulse strikes a single crystal
immersed in liquid helium and instanta which fly through the crystal toward the opposite surface and are detected with the bolometer of a superconducting device. The signal typically has three peaks arriving at different times, which are assigned to the three phonon modes, and the delay time determines the group velocity of each mode. More interesting is phonon imaging (8). The anisotropic group velocity inherent in the crystal deflects the phonon orbit, which otherwise would be straight, and the deflection depends on the direction of flight. Consequently, the phonons arriving at the detection surface are far from uniform; they are focused and dense at some positions while sparse at others. The phonon distribution thus exhibits a pattern characteristic to crystal symmetry. In the experiment, the role of the exciter and the detector are exchanged without any significant difference: The bolometer is fixed and, instead, the laser spot scans over the exciting surface in a raster manner (TV scan). The twodimensional display of the detected signal gives the phonon image as shown in Fig. 2.

INTERACTION BETWEEN SOUND AND LIGHT

There are generally two effects, sound on light and light on **Figure 3.** Three phenomena of acousto-optics: (a) Beam deflection at sound, which are referred to as acousto-optics (9) and photo- $f \le 1$ MHz, (b) Raman-Nath diffraction at a few megahertz, and (c) acoustics (10), respectively. In the former, sound waves give Bragg reflection at $f \ge 50$ MHz.

square of the electric field and common to all dielectric mate-

gradient that deflects a narrow beam (usually laser) crossing the sound, as understood in geometrical optics. Since the gradient changes from negative through zero to positive with the phase advance, the light beam moves to and fro at the sound frequency. The sound oscillation is expressed as an alternating change in the refractive index from its average value n_0 as $n(t) = n_0 + \delta n$ sin ωt , where δn is the amplitude of the refractive index. Under a low-amplitude assumption that the light trajectory is approximated with an arc, the deflection angle θ after the sound beam with width *L* is given by sin $\theta(t) = (kL/2)$ δn sin ωt . This assumption holds at $kL\sqrt{\delta n/n_0} \leq$ 1. The deflection phenomenon provides absolute measurement of sound pressure amplitude P_0 . The maximum angle of deflection θ_{M} gives P_0 as sin $\theta_{\text{M}} = (kL/2)(dn/dP)P_0$, where (dn/dP) is a material constant and 1.47×10^{-10} Pa⁻¹ in water.

In the intermediate region from 1 MHz to \sim 10 MHz, Raman-Nath diffraction is observed, as shown in Fig. 3(b). The **Figure 4.** Generation and reception of photoacoustic signal in solid. periodical dense and sparse regions in the medium work as a phase grating, which modulates the plane waves into sinusoi- **Photoacoustics** dal wave fronts, and diffraction of several orders appears in the far field. The intensity of the *m*th-order diffraction is Light irradiation raises some degree of freedom in the megiven by dium to an excited state, which recovers the initial equilib-

$$
I_m = I_{\rm i} J_m^2(r) \tag{1}
$$

parameter and is written as $r = qL \, \delta n$, with q being the light dium. The grating running at the speed of sound imparts a sion lengths μ , determined by the chopping frequency as μ frequency shift of mf to the *m*th diffracted because of light, where $f = \omega/2\pi$ is the sound frequency. Since J_1^2

$$
2q\sin\theta_{\rm B} = k\tag{2}
$$

up by f if the sound direction is against the light, as shown face structure within the depth of μ , which affects any of the in the figure, and shifted down in the opposite configuration. four aforementioned properties. Microcracks, voids, or fabri-

$$
I = Ii \sin2(r/2)
$$
 (3)

that total reflection occurs at $r = \pi$. The harmonic nature of sound gives rise only to first-order diffraction in contrast to laser. X-ray diffraction, which causes many higher orders. The pre- Light wavelength is swept from visible to infrared in PAS, ceding description of acousto-optics is based on the simplest and the photoacoustic signal is used for detection of absorpcase of longitudinal waves in isotropic media. The transverse tion in spectroscopy. In addition to its high sensitivity, PAS waves introduce an anisotropic index and rotate the polariza- has the advantage of observing the spectrum of opaque subtion plane of light (i.e., a kind of photoelasticity occurs). In stances. Care should be taken, however, that PAS involves single crystals, the sound velocity and refractive index have the preceding four properties, while standard spectroscopy oban anisotropy that should be expressed in tensors, and the serves only light absorption. Photoacoustics in the spectroacousto-optic phenomena exhibit a complicated feature in- scopic sense is very effective in detecting infinitesimal compovolving both longitudinal and transverse waves. nents in liquid and gas and is commonly used for checking air

rium through a radiative or nonradiative relaxation process; the latter is observed as photoacoustics (the former is photoluminescence). The light source chopped at *f* Hz (typically lower where I_i is the incident intensity and $J_m(r)$ is the *m*th-order than 1 MHz) generates an acoustic signal, which reflects local Bessel function. The argument r is termed the Raman-Nath properties for (1) light absorption, (2) heat generation, (3) *n*, thermal conduction, and (4) expansion. The principle of photowave number in the medium. The angle of the *m*th-order light acoustics is shown in Fig. 4 for the case of solid samples. Heat is given by $\sin \theta_m = mk/q$, where θ_m is the value in the me- generated by the light diffuses over a range of thermal diffu- $\sqrt{\kappa/(n f \rho C)}$, where κ and *C* are the thermal conductivity and specific heat of the medium, respectively. The periodic expantional to r^2 at $r < 1$, this phenomenon is used for optical detec- sion within the range of μ excites elastic waves at f, which tion of ultrasonic waves. propagate out of the range and are detected by a microphone At frequencies higher than \sim 50 MHz, Bragg reflection oc- in air, which picks up small pressure changes in a tight cell curs, as shown in Fig. 3(c), which is analogous to X-ray dif- containing the specimen or a piezoelectric transducer bonded fraction in crystals. Light is reflected by sound wave fronts if to the specimen. Information on microscopic structure or comthe angle of incidence satisfies the following equation of position in the range of μ is obtained from the amplitude and Bragg's condition: phase of the acoustic signal. Two different types of experiment are usually conducted: photoacoustic microscopy (PAM) and photoacoustic spectroscopy (PAS). A focused laser spot scans the surface of the specimen in PAM, and the photowhere θ_B is the Bragg angle. The optical frequency is shifted acoustic signal is used to form a magnified image of subsur-Reflected intensity is given by cated structures hidden underneath appear in the image. At typical frequencies of 10 kHz to 1 MHz, μ is in the range from 150 to 5 μ m, and information at different depths is available by varying *f*. Spatial resolution of PAM is determined by the The acousto-optic light modulators have the advantage larger of either the laser spot size or μ . In some cases, an electron beam is useful as an exciting source instead of the

pollution or the quality of super-pure water for semiconductor processes.

Since the origin of photoacoustics is the photothermal effect, direct observation of the heat produced is also useful. There are various techniques that detect, for example, infrared radiation, surface expansion with a laser Michelson interferometer, and beam deflection of a prove laser passing through air in close vicinity of the heated region. These techniques are usually included in photoacoustics in a wider sense, though they do not pertain to the acoustic signal.

VISUALIZATION OF THE SOUND FIELD

Visual observation of the ultrasonic field is sometimes very helpful in studying the various wave phenomena, and different techniques have been developed for this purpose. In the **Figure 6.** Ultrasonic pulse visualized by (a) stroboscopic Schlieren
photographic method, a printing paper is put in a tank of di- and (b) dynamic photoelasticit paper. The ultrasonic field promotes development and soon plicated diffraction pattern. Both longitudinal (L) and transversal (T) reveals its sectional distribution as a dark and bright pattern. This experiment can be cond teric liquid crystal can be used as the detector, which displays the intensity distribution in color. High-intensity ultrasound that align vertically on the focal plane. The 0th-order light is
in water is directly seen for the accompanying sonolumines-
shut out and all the others observ cence (11): The ultrasonic cavitations emit very weak visible reproduce the CW sound field.

light when they collapse at each cycle. A small amount of lum-

Illtrasonic pulse is also view

Fig. 5. The second lens forms bright spots of different orders **Dynamic Photoelasticity**

picture of an ultrasonic pulse propagating in water. 6(b) shows short pulses of longitudinal and transversal waves

photographic method, a printing paper is put in a tank of di- and (b) dynamic photoelasticity. In (a), a long pulse at 10 MHz has luted developer and ultrasonic waves normally illuminate the just passed through a slit with luted developer and ultrasonic waves normally illuminate the just passed through a slit with 3 mm width in water, showing a com-
naper. The ultrasonic field promotes development and soon plicated diffraction pattern. Both

shut out and all the others observed by an eye or a camera

light when they collapse at each cycle. A small amount of lum-

in alkane solution strengthens the emission and the

three-dimensional distribution can be seen with the naked

eye. Propagation of CW (continuous wave) or p

Schlieren Technique

The inhomogeneous refractive index in a transparent medium

The inhomogeneous refractive index in a transparent medium

was visualized by Schlieren, whose principle is very simple.

Was visualized by S

The Schlieren technique lacks sufficient sensitivity in solids due to their low compressibility, and birefringence induced by the sound waves is used for visualization instead (12). The experimental arrangement with a point light source and two lenses is similar to that of the Schlieren technique, except for a polarizer and $\lambda/4$ plate put before the medium and another λ /4 plate and analyzer behind it. The light passes through the medium as circularly polarized waves, and any change in polarization due to the waves is detected by the analyzer, whose axis is adjusted for highest contrast. This configuration is sensitive in all directions of propagation in the plane perpendicular to the optical axis, and both longitudinal and transversal waves are visualized. Note that the longitudinal mode has a component of shear strain that is four-thirds of Figure 5. The stroboscopic Schlieren method provides a slow-motion the bulk strain and contributes to the photoelasticity. Figure

in a glass block. A slow-motion picture is also available with the stroboscope and variable delay.

MEASUREMENT OF ULTRASONIC VELOCITY AND ABSORPTION

Many different techniques have been developed for measuring velocity and absorption, which are the fundamental quanti-
Figure 8. Resonance method for velocity and absorption measureties characterizing materials. The pulse method is most com- ment in solid. monly used in laboratories and industry over a wide frequency range (13); the CW method includes the various types of resonance techniques and the ultrasonic interferometer The reflection type of pulse method has one transducer (14); and the optical method is used at high frequencies for that works as a transmitter and a receiver. The pulse method transparent liquids and solids. Accuracy higher than 0.1% is has the advantages that the injected acoustic energy is low, readily obtained for velocity measurements, while absorption on average, which otherwise would heat the specimen; and

Pulse Method

CW Method The through-transmission type of pulse method has two piezoelectric transducers bonded to parallel surfaces of the solid Sound waves confined between two interfaces interfere and block under study or attached to a cell for the liquid sample, resonate when the distance equals half the wavelength as shown in Fig. 7. An ultrasonic pulse of $\sim 1\mu$ s duration is multiplied by an integer. Figure 8 shows the principle of the injected into the specimen and multiply reflected between the resonance method used for a solid specimen. The driving fretwo faces. The interval between the adjacent echoes in the quency is swept and the resonance spectrum is observed. The received pulse-echo train gives 2t, the round-trip time of the peak interval Δf determines the velocity as $v = 2\Delta f d$, and the pulse, from which the velocity is obtained with the distance between the two transducers. There are a few techniques for the piezoelectric transducers affect the resonance, they are the precise determination of *t*. In the pulse-echo-overlap used below their own fundamental resonance where an even method, the first and the second pulses are displayed on an frequency response is expected. The resonance method is also oscilloscope. The trigger frequency is adjusted so that there is used in liquid for absorption measurement in the megahertz an overlap from cycle to cycle, and the period gives 2*t*. In the range. sing-around method, the first pulse is gated out and triggers An ultrasonic interferometer is used for liquid or gas. The the next excitation of ultrasonic pulse. Thus the pulse runs distance is swept instead of the frequency and the velocity is around the loop of the acoustic and electric circuit, and t is determined as $v = 2\Delta df$ from Δd , the interval in the resoobtained from the period. The period includes a delay in the nance peak obtained as a function of *d*. The ratio of the peak electric circuit, however, and absolute measurement is diffi- to the bottom decreases as *d* increases, from which the abcult. This method is useful for automatic measurement of sorption is obtained. In the correlation method, the received

the distance *x* between the transducers, and attenuation in sonic waveform in the sweep of *d*. the pulse height, written as $\exp(-\alpha x)$, gives α , the absorption coefficient. At frequencies lower than 10 MHz, the sound dif- **Optical Method** fraction causes an apparent loss that should be corrected the-
ortically. Above 100 MHz, on the other hand, parallelism be-
tween the two transducers is most important for accuracy.

ment in liquid. The interest of the centered at θ_0 and with a width $\Delta \theta$, and one gets $v =$

measurement usually has a 5 to 20% error. the crosstalk between the received signal and stray of the driving signal is avoided.

f gives the absorption as $\alpha = \pi \delta f/v$. For fear that

small changes in velocity. Signal electrically interferes with the driving signal by a Absorption measurement in liquid is made by increasing mixer, whose output reproduces the spatial decay of the ultra-

tional to the square of the ultrasonic amplitude (i.e., $I \propto \delta n^2$ tween the two transducers is most important for accuracy.

Absorption in a solid sample is obtained from decay in the

echo train. Absolute measurement is difficult, however, since

the reflection at the transducer/sample resolution Bragg reflection (HRB) method useful in the UHF (ultrahigh frequency) range is based on the following principle (15): The spatial decay of ultrasonic amplitude is expressed as $\exp(-\alpha x)$ sin k_0x . The Fourier transform of this equation gives the wave number spectrum of Lorentzian form written by

$$
S(k) = 1/((1 + [(k - k_0)/\alpha]^2)
$$
 (4)

The spectrum has a peak at $k_0 = \omega/v$ and a width of α . Hence, Figure 7. Sample cell of pulse method used for velocity measure- the Bragg angle for spatially decaying waves has a distribu-

Figure 9. High-resolution Bragg reflection (HRB) method for velocity and absorption measurement in the UHF range.

photon with $\hbar \mathbf{q}_s$, conserving the momentum as $\hbar \mathbf{q}_i + \hbar \mathbf{k} = \delta \omega$ gives the lifetime of the phonon and hence the absorption:
 $\hbar \mathbf{q}_s$; and a photon creates one phonon to make a scattered $\alpha = \delta \omega/2v$. T photon as $\hbar q_i = \hbar q_s + \hbar k$. The energy conservation law in-
creases or decreases the photon energy by $\hbar \omega$ in the former or
latter process, which is referred to as anti-Stokes or Stokes
latter process, which is refer $\bm{q}_{\text{i}}\!\!\mid\, \cong \, \left|\bm{q}_{\text{s}}\right|$ scattering, respectively. Since $|\mathbf{q}_i| \cong |\mathbf{q}_s| = q$ is a very good
approximation, the preceding two equations of momentum
conservation are rewritten with the scattering angle Θ in scalar form as

$$
2q\sin(\Theta/2) = k \tag{5}
$$

Figure 10. Typical curve of the HRB method, which is associated with the spectrum of *k*. The peak and width give the velocity and absorption, respectively. The sample is liquid CS₂. **Figure 11.** Basic system of Brillouin scattering experiment.

 $\omega/(2q \sin \theta_0)$ and $\alpha = 2q\Delta\theta \cos \theta_0$ from Eqs. (2) and (4). Figure In a classical description, Brillouin scattering is interpre-9 shows a block diagram of the HRB method for liquid speci- ted in terms of Bragg reflection by sound generated in thermens. A ZnO piezoelectric film excites continuous waves in mal fluctuation. With $\Theta = 2\theta_B$, Eq. (5) agrees perfectly with the liquid where the laser is incident, and the reflected light the Bragg's condition of Eq. (2). the Bragg's condition of Eq. (2) . The change in the phonon is observed as sweeping the angle of incidence around θ_0 . Fig- energy is understood as the Doppler shift. Figure 11 schemature 10 shows an example of the *k* spectrum obtained at 1.5 ically shows the standard system of experiment. The incident GHz as a function of θ , from which velocity and absorption laser is scattered by phonons in the specimen into all the solid are determined. The optical heterodyne detection gives high angles, and a component with scattering angle Θ passes sensitivity and sufficient angular resolution. through the Fabry-Perot interferometer and is detected by a photomultiplier, which yields the power spectrum of the scat-**Brillouin Scattering**
the Brillouin triplet. The central one is the Rayleigh compo-
the Brillouin triplet. The central one is the Rayleigh compo-Measurement of velocity and absorption generally requires
artificial excitation of ultrasound; one exception is Brillouin in the tothe slow diffusive decay of the spontaneous in-
scattering (16). Every substance has spont

MOLECULAR ACOUSTICS

Sound propagation in fluids is strongly influenced by various phenomena of molecular origin, and measurement of the velocity and absorption provides an experimental approach to the microscopic structures and their dynamics. Velocity in liq-

uid generally decreases with temperature since the elasticity decreases to a degree that exceeds the positive effect of decreasing density. The exception is water, which has a positive temperature gradient with a broad maximum at $\sim 75^{\circ}$ C. This anomaly is explained by the icelike clusters of associated molecules coexisting with monomers. An increase in temperature breaks these clusters, which have a lower elasticity than a collection of monomers, and increases the velocity. This effect is canceled at 75°C by the normal decrease.

A common mechanism of absorption in liquid is the viscous loss, referred to as classical absorption, which has f^2 dependence on frequency as

$$
\alpha = (8\pi^2/3)(\eta f^2/v^3 \rho) \tag{6}
$$

where η is the viscosity. This equation includes the factor 4/ 3 for the shear strain component in the longitudinal vibra- **Figure 12.** Strong velocity dispersion and anomalous absorption in tion. Since α/f^2 is independent of f, this quantity is often used liquid CS₂ are caused by the vibrational relaxation phenomenon. for characterizing the material. Most kinds of liquid have abosrption larger than the classical value, however, and the excess absorption is attributed to relaxation loss (17). Heat flow and ϵ , dispersion and absorption are given by linear combinawithin one wavelength could be a loss mechanism at higher tions of the relevant equations. frequencies. However, sound propagation in the range of For relaxation studies in liquid, ultrasonic spectroscopy, usual experiment is regarded as an adiabatic process: This which observes v and α over a wide frequen usual experiment is regarded as an adiabatic process: This which observes *v* and α over a wide frequency range, is usu-
absorption is safely ignored.

A sudden increase in temperature, for example, disturbs the equilibrium of a system with some inner degrees of freedom, **Various Mechanisms of Relaxation** and the excess thermal energy is properly distributed among them with a finite time constant: The system gradually recov- The most typical example of ultrasonic relaxation is observed ers balance through the relaxation process. Sound waves im- in some kinds of polyatomic molecules, which have molecular
part a periodic disturbance of temperature or pressure to the vibration as the inner degrees of freedo part a periodic disturbance of temperature or pressure to the medium. If the period *T* is much greater than the relaxation translation motions of the molecules exchange energy time τ (time required for the recovery), the system always through collisions. Analysis of vibrational relaxation is outkeeps its equilibrium. As T becomes shorter than τ , on the lined in the following by considering the case of liquid carbonother hand, the system cannot follow the rapid alteration of disulfide (CS_2) (18). Figure 12 shows the dispersion and absound and is brought into a nonequilibrium state with a con- sorption at 20C observed by three techniques: the pulse stant strain. Some of the degrees of freedom freeze, losing method, HRB, and Brillouin scattering. The solid lines are their function as energy capacity. The medium apparently the theoretical curves of Eqs. (7) and (8), which give $\epsilon = 0.15$, stiffens: The velocity increases and the absorption in α/f^2 de- $f_r = 105$ MHz, and other parameters. This molecule has three creases as the frequency increases through $f_r = 1/\tau$, the relax-
ation modes of vibration—doubly degenerated defor-
ation frequency. This is the general description of ultrasonic mation, symmetric stretching, and antisymm ation frequency. This is the general description of ultrasonic relaxation, and the velocity dispersion and absorption are ex-

$$
v^2 = v_0^2 + (v_\infty^2 - v_0^2) / [1 + (f_r/f)^2]
$$
 (7)

$$
\alpha/f^2 = A/[1 + (f/f_r)^2] + B \tag{8}
$$

 $v^2_{\infty} - v^2_0/v^2_{\infty}$; $A = \pi \epsilon / (v_0 f_r)$ is a magnitude of the sorption. Besides v^2 and α/f^2 , absorption per wavelength $\alpha'\lambda$ are more than two relaxation mechanisms with different f_r ber of collisions per second and the probability of vibrational

ally conducted. Since f_r is proportional to pressure in most cases of gas, the spectrum is obtained as varying *P* instead of **Ultrasonic Relaxation** *f* and is shown as a function of *f*/*P*. Temperature is often pre-
ferred as the variable in the study of solids.

ing—whose fundamental frequencies are at $\nu_1 = 397$ cm $^{-1}$, ν_2 pressed by the following equations: $= 658 \text{ cm}^{-1}$, and $\nu_3 = 1540 \text{ cm}^{-1}$, respectively. Each mode contributes to the specific heat in a static sense (at $f \leq f_r$), and the value is theoretically predicted by the equation of specific heat for a harmonic oscillator: $C_i = R \zeta_i^2 \exp \zeta_i/(\exp \zeta_i - 1)^2$, $\alpha/f^2 = A/[1 + (f/f_r)^2] + B$ (8) where $\zeta_i = h \nu_i/kT$. The contribution of all three modes is thus calculated to be $\Delta C = \sum C_i = 16.2$ J/mol K (the effect of the where v_0 and v_x are, respectively, the limiting velocities at degeneracy is taken into account). At $f \geq f_r$, however, the lower and higher frequencies in the definition of relaxation modes are assumed to lose the contribution and C_P decreases by this amount. Since the sound propagation is an adiabatic absorption change; and *B* is a constant representing the con- process, the decrease causes a dispersion whose magnitude is tribution of other relaxation mechanisms and the classical ab- given by $\epsilon = (\gamma - 1) \Delta C/(C_P - \Delta C)$. This equation gives the theoretical value $\epsilon = 0.153$, which is in good agreement with is also used for the discussion of relaxation, where $\alpha' =$ the experimental value. This liquid has strong absorption in $\alpha - Bf^2$ is the contribution of relaxation to absorption. The the megahertz range, which is $\sim 10^3$ times the value in water. spectrum of $\alpha' \lambda$ has a bell shape with a maximum at f_r . Equa- The reason is that A is inversely proportional to f_r and that tions (7) and (8) are for a single relaxation process. If there f_r is very low. Further, f_r is given by the product of the num-

excitation in a collision. The latter rapidly decreases as *h* exceeds *kT*, since such a high level can only be excited by a few rare molecules with speed much greater than the average. Even the lowest level is almost twice kT (\sim 200 cm⁻¹ at 20° C) in CS₂, and this is the intrinsic reason for the very slow relaxation at \sim 100 MHz. Vibrational relaxation is observed in a few other liquids, including halogen derivatives of methane or cyclic compounds such as benzene or pyridine. These liquids have strong absorption in the megahertz range without exception.

Rotational isomers can also be a relaxation mechanism, in which the entropy difference between the isomers determines ϵ , and the energy barrier in between determines f_r . Other relaxation mechanisms include the hybrid association of molecules in alcohol-water mixtures, most chemical reactions in solutions, and the deformation of polymer chains (19). In many cases, the relaxation is not a single process, but is distributed in f_r . Dispersion extends over decades of frequency, as in polymer solutions.

ADVANCED TOPICS

Hyperresolution Phonon Spectroscopy

While Brillouin scattering is a very good means of phonon study, the experiment should be conducted with a sufficient resolution if qualitative discussion is to follow. A stable laser at its single-frequency oscillation is used as the light source. As for the spectrometer, the sophisticated system of tandem multipath Fabry-Perot gives the highest resolution of optical devices (20). It has two sets of scanning Fabry-Perot with different interorders, and the light is filtered three or five times

can break through the limit of Fabry-Perot and yields a hy-
perresolution that is $\sim 10^3$ times as high depending on the tively. Resonance of spontaneous phonons in a small cavity is obphonon frequency (21). Figure 13 shows the optical hetero- served in (b). dyne system for this purpose, in which the incident and the local oscillator light cross at Θ in the specimen. The local oscillator and the light scattered in the same direction take ex-
actly the same path to a high-speed photodiode, which mixes Rayleigh peak and the anti-Stokes Brillouin component,
them and generates heat current between th them and generates beat current between them. A spectrum which is $\sim 10^2$ times broader and only $\sim 10^{-2}$ as high. Parts A spectrum and B show the expansion of $\sim 10^2$ along the abscissa and oranalyzer gives the phonon power spectrum. The frequency
resolution is determined by the receiving bandwidth and can
be increased up to 1 kHz, if necessary. Figure 14 shows two
examples of a fine structure of the spectrum

heterodyne technique. the technique of the technique

through each of them. Computer control of the whole system
is required for stable operation.
Electronic spectroscopy instead of the optical spectrometer
for from triplet, as shown in (a), where A and B are horizontal and
d tively. Resonance of spontaneous phonons in a small cavity is ob-

tained by the hyperresolution. Figure 14(a) is half the Bril-
louin spectrum in liquid CS₂ with the very narrow and tall and filled with liquid toluene. Since a finite beam width
apart and filled with liquid toluene. Si of the laser introduces some ambiguity to Θ and hence to k , phonons with a certain range of ω are simultaneously observed. The spontaneous phonons in the cavity multiply reflect and resonate at an interval given by $v/(2d)$.

The optical spectrometer analyzes the phonon signal at \sim 10^9 Hz that is carried on a light wave with frequency \sim 10^{15} Hz. Accuracy of 1% in phonon measurement requires a very severe resolution of $\sim 10^{-8}$. In electronic spectroscopy, on the other hand, the optical mixing demodulates the carrier light to give the bare phonon signal whose frequency is in the **Figure 13.** Hyperresolution Brillouin spectroscopy with the optical range easily treated by a spectrum analyzer. This is the in-

Figure 15. Time-reversal property of phase conjugate waves (a), and the function to correct the wavefront distortion automatically (b).

Given a wave expressed by a complex function $\phi(r, t)$ exp have 3.5 mm height. $(-j\omega t)$, the phase conjugate wave of the wave is defined as $\phi^*(r, t) \exp(-j\omega t)$, where **r** is a position vector and the aster-
isk means the complex conjugate. Their amplitudes are writ-
integral is a thin metal plate with letter-shaped holes and put
ten in a scalar form as $U(r, t)$ conjugation, nonlinear piezoelectricity provides sufficient ef-
ficiency, fidelity, and high-speed response (22). The phase con-
jugator is made of a PZT ceramic block with two electrodes.
The ultrasonic pulse at ω (~1 The nonlinear interaction then occurs between the ultrasonic **Laser-induced Ultrasound** and electric field, and the crossterm yields a component of $-\omega t$ (= ωt - 2 ωt), which returns as the phase conjugate pulse. The photoacoustic effect is applied for the purpose of noncon-In addition to piezoelectricity, nonlinearity in the elastic or tact ultrasonic generation in gas, liquid, and solids, and many dielectric constant is part of the effect, though the contribu- varieties of techniques are being studied, as shown in Fig. 18. tion is smaller. Slow-motion video taken by the Schlieren A giant Q-switched laser pulse strikes a metal surface in Fig. technique visually confirms the time reversal property of the 18(a) and the sudden heating of a small area excites elastic phase conjugate propagation in water. Figure 16 shows the vibration, which propagates into all the possible directions as three shots of the video: (a) A focused incident pulse has just SAW and bulk waves of both longitudinal and transverse arrived at the PZT surface and (b) is specularly reflected, and modes (23). The frequency has a distribution depending on (c) the phase conjugate appears after a few microseconds. the sharpness of the laser pulse. The conversion efficiency is

aging system operating at 10 MHz, which is essentially the level for fear of surface ablation and damage. The lack in the

Figure 17. Comparison of images reconstructed by a scanning acoustic system (a) without and (b) with the phase conjugator. The target is put in agarose gel with an irregular shape, which disturbs the **Acoustic Phase Conjugate Waves** wavefront. The ultrasonic frequency is at 10 MHz and the letters

The phase conjugator was installed as a reflector in an im- rather low, but the laser power should be kept below a certain

Figure 16. The time-reversal property is visually shown by the storoboscopic Shlieren technique: (a) focused incidence at $t = 0$, (b) specular reflection at $t = 7$ μ s, and (c) phase conjugate reflection at $t = 15 \text{ }\mu\text{s}$.

 (b)

 (c)

Figure 18. Various mechanisms of laser-induced ultrasound: (a) A giant pulse laser strikes the surface to generate both surface acoustic waves (SAW) and bulk waves; (b) two beams crossing at the surface project a fringe that generates SAW; (c) running standing waves of electric field made by two beams with different frequencies effectively generate ultrasound in liquid; and (d) sinusoidally modulated output of infrared laser generates ultrasound on the metal film.

efficiency, mode selectivity, directivity, and wave coherence is be swept by means of thermal control. In the absence of optiimproved in Fig. 18(b). Two laser pulses irradiate the same cal absorption, the electrostrictive effect is the origin of photoarea from different directions and instantaneously project a acoustic coupling. A simple yet effective method is shown in fringe pattern whose interval Λ is determined by the crossing Fig. 18(d) that utilizes a CW semiconductor laser. The infraangle Θ as $\Lambda = \pi/(q \sin \Theta/2)$. The plane SAW with wavelength Λ is selectively excited and propagates in the direction metal film evaporated on a fused quartz rod, which works as normal to the fringe. The efficiency is further increased by an the ultrasonic transducer with an even frequency response. acousto-optic modulator, which gives a frequency difference The signal can be detected by Brillouin scattering, as shown of f between the two pulses. The fringe runs on the surface at in Fig. 19. The phonon density is $\sim 10^4$ times as high as the a speed of $f\Lambda$ and efficiently excites SAW when the speed spontaneous phonons excited by kT . agrees with the phase velocity. Since most of the SAW genera- The most remarkable example of sound-and-light interacinterferometer. The coustics and acoustics and acousto-optics occur simultaneously.

Figure 18(c) shows bulk wave generation at \sim 3 GHz in a transparent liquid based on the same principle as the crossbeam method, but with two CW lasers whose frequency can **BIBLIOGRAPHY**

Figure 19. Coherent phonons generated by the method (d) in Fig. 18 ^{3011, 1991.} have $\sim 10^4$ as large population as the spontaneous phonons. 9. J. Sapriel, *Acousto-Optics*, New York: Wiley, 1979.

red output is electrically modulated at *f* and irradiates a thin

tions aims at noncontact ultrasonic evaluation (for example, tion can be seen in the phenomenon of stimulated Brillouin of very hot plates for which piezoelectric transducers are of scattering. A giant-pulse laser induces a coherent beam of no use), noncontact detection is also essential. A laser probe phonons in a transparent medium, and the phonon beam, in provides remote sensing of the waves in the optical lever or turn, reflects the laser in a backward direction. Thus photo-

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PHYSICAL MECHANISMS AND CHEMICAL EFFECTS OF ULTRASOUND. See ULTRASONIC PHYSICAL MECHA-

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