

Chapter 16

16–1. $H_0: \tilde{\mu} = 7.0$ $n = 10$
 $H_1: \tilde{\mu} < 7.0$

$$\alpha = 0.05$$

$CR: R \leq R_\alpha^*$ (Table X)

$$R^+ = 8, R^- = 2 \Rightarrow R = 2$$

Since $R > R_\alpha^*$, do not reject H_0

16–2. $H_0: \tilde{\mu} = 8.5$
 $H_1: \tilde{\mu} \neq 8.5$

$$\alpha = 0.05$$

$$R^+ = 8, R^- = 11, R = \min(8, 11) = 8, R_{0.05}^* = 5$$

Since $R > R_{0.05}^*$, do not reject H_0

- 16–3. (a) $H_0: \tilde{\mu} = 3.5$ Critical Region: $R^- < R_d^*$
 $H_1: \tilde{\mu} > 3.5$
- (b) $n = 10$ $\alpha = 0.05$ $R_{0.05}^* = 1$
 $R = 3$ Since $R^- > R_{0.05}^*$, do not reject H_0
- (c) Probability of not rejecting H_0 ($\tilde{\mu} = 3.5$) when $\tilde{\mu} = 4.5$

$$p = P(X > 1) = \int_1^\infty \frac{1}{\beta} e^{-(1/\beta)x} dx = e^{-1/\beta}$$

16–4. $n = 10$ $\sigma = 1$
 $H_0: \mu = 0$
 $H_1: \mu > 0$

- (a) $\alpha = 0.025$
- (b) $p = P(X > 0) = P(Z > -1) = 1 - \Phi(-1) = 0.8413$
 $R_{0.05}^* = 1$
 $\beta = 1 - \sum_{x=0}^1 \binom{10}{x} (0.1587)^x (0.8413)^{10-x} = 0.487$

$$\begin{aligned} 16-5. \quad H_0: \tilde{\mu}_d = 0 \\ H_1: \tilde{\mu}_d \neq 0 \end{aligned}$$

$$\alpha = 0.05$$

$$\begin{aligned} CR: R < R_{0.05}^* = 1 \\ R^- = 2, R^+ = 6 \Rightarrow R = 2 \\ \text{Since } R \text{ is not less than } R^*, \text{ do not reject } H_0 \end{aligned}$$

$$\begin{aligned} 16-8. \quad H_0: \mu = 7 \quad R^+ = 50.5 \\ H_1: \mu \neq 7 \quad R^- = 4.5 \\ R = \min(50.5, 4.5) = 4.5 \\ R_{0.05} = 8 \quad \text{reject } H_0 \end{aligned}$$

$$\begin{aligned} 16-9. \quad H_0: \mu = 8.5 \quad n = 20 \\ H_1: \mu \neq 8.5 \end{aligned}$$

$$\alpha = .05$$

$$CR: R \leq R_{0.05}^* = 52$$

$$\begin{aligned} R^+ &= 19 + 10.5 + \dots + 1 = 88.5 \\ R^- &= 12 + 20 + \dots + 3.5 = 121.5 \\ R &= 88.5 > R_{0.05}^* \\ \therefore &\text{ do not reject } H_0 \\ &\text{conclude titanium content is 8.5\%} \end{aligned}$$

$$\begin{aligned} 16-10. \quad H_0: \mu = 8.5 \quad \mu_R = \frac{20(21)}{4} = 10.5 \\ H_1: \mu \neq 8.5 \quad \sigma_R^2 = \frac{10(21)(41)}{24} = 717.5 \\ Z_0 = \frac{85 - 105}{\sqrt{717.5}} = -0.747 \end{aligned}$$

$$\begin{aligned} 16-12. \quad R^+ &= 24.5 \quad R = \min(24.5, 11.5) = 11.5 \\ R^- &= 11.5 \quad R_{0.05}^* = 3 \end{aligned}$$

Do not reject H_0 , $\mu_d = 0$.

$$\begin{aligned} 16-13. \quad H_0: \mu_1 = \mu_2 & \quad n_1 = 8 \quad n_2 = 9 \\ H_1: \mu_1 > \mu_2 & \end{aligned}$$

$CR: R_1 < R_{\alpha}^* = 51$ Table IX

$$\alpha = 0.05$$

$$R_2 = 75, R_1 = 78$$

Since R_2 is not less than or equal to 51, do not reject H_0 . Conclude the two circuits are equivalent.

$$\begin{aligned} 16-14. \quad n_1 = n_2 & \\ R_1 = 40 & \\ R_2 = 6(13) - 40 = 38 & \\ R_{0.05}^* = 26 & \end{aligned}$$

Do not reject H_0

Airline	Minutes	Rank
D	0	1
D	1	2.5
A	1	2.5
A	2	4
A	3	5
A	4	6.5
D	4	6.5
A	8	8
D	9	9
D	10	10
D	13	11
A	15	12

16–15. $n_1 = n_2 = 10$, $n > 8$ large-sample approximation

$$H_0: \mu_1 = \mu_2$$

$$H_1: \mu_1 \neq \mu_2$$

$$\alpha = 0.05$$

$$CR: |Z_0| > Z_{0.025} = 1.96$$

$$\mu_{R_1} = \frac{(20)(21)}{4} = 105, \quad \sigma_{R_1}^2 = \frac{10(10)(21)}{12} = 175$$

$$R_1 = 1 + 2 + 3 + \cdots + 19.5 = 77$$

$$Z_0 = \frac{77 - 105}{\sqrt{175}} = -2.117; |Z_0| = 2.117 > 1.96$$

Reject H_0 ; conclude unit 2 is superior.

16–16. H_0 : techniques do not differ

H_1 : techniques differ

	Ranks					R_i
1	14	11.5	6	7		38.5
2	16	11.5	9	15		51.5
3	5	8	10	13		36
4	15	3	1.5	4		10

$$S^2 = \frac{1}{15} \left[1495 - \frac{16(17)^2}{4} \right] = 22.6$$

$$K = \frac{1}{22.6} \left[\frac{38.5^2}{4} + \frac{51.5^2}{4} + \frac{36^2}{4} + \frac{10^2}{4} - \frac{16(17)^2}{4} \right] = 10.03$$

$\chi^2_{0.05,3} = 7.81$, reject H_0 ; conclude the techniques differ

16–17. H_0 : methods do not differ

H_1 : methods differ

$$\alpha = 0.10$$

$$CR: K > \chi^2_{0.10,2} = 4.61$$

	Method					Ranks	r_i
1	10.5	9	12	7	5		43.5
2	10.5	15	14	8	6		53.5
3	1	4	3	2	13		83

$$K = \frac{12}{15(16)} \left(\frac{43.5^2}{5} + \frac{53.5^2}{5} + \frac{53.5^2}{5} + \frac{23^2}{5} \right) - 3(16) = 4.835$$

at 0.1 significance, reject H_0 .

16–18. H_0 : manufacturers do not differ

H_1 : they differ

	Ranks						R_i
A	12	1	3	9	13		38
B	4	17	14	7	20		62
C	19	15	16	11	18		79
D	5	10	2	8	6		31

$$K = \frac{12}{20(21)} \left[\frac{38^2 + 62^2 + 79^2 + 31^2}{5} \right] - 3(21) = 8.37$$

$\chi^2_{0.05,3} = 7.81$. Reject H_0 ; conclude the manufacturers differ.